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Non Fermi Liquid Ground States in Strongly Correlated f-Electron Materials

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Experimental efforts to characterize and develop an understanding of non Fermi liquid (NFL) behavior at low temperature in f-electron materials are reviewed for three f-electron systems: $M_{1-x}U_xPd_3$ ($M = Sc, Y$), $U_{1-x}Th_xPd_2Al_3$, and $UCu_{5-x}Pd_x$. The emerging systematics of NFL behavior in f-electron systems, based on the present sample of nearly ten f-electron systems, is updated. Many of the f-electron systems exhibit the following temperature dependences of the electrical resistivity ρ , specific heat C , and magnetic susceptibility χ for $T \ll T_0$, where T_0 is a characteristic temperature: $\rho(T) \sim 1 - aT/T_0$, where $a < 0$ or > 0 , $C(T)/T \sim (-1/T_0) \ln(T/bT_0)$, and $\chi(T) \sim 1 - c(T/T_0)^{1/2}$. In several of the f-electron systems, the characteristic temperature T_0 can be identified with the Kondo temperature T_K .

1. INTRODUCTION

During the past several years, there has been a great deal of interest in a new class of f-electron heavy fermion materials which exhibit non Fermi liquid (NFL) behavior at low temperatures. These materials are Ce and U intermetallics which, with a few possible exceptions, have been doped with a nonmagnetic element. The Ce and U ions have partially-filled f-electron shells and contribute magnetic dipole or electric quadrupole moments which can interact with the spins and charges of the conduction electrons and participate in magnetic and quadrupole ordering at low temperatures. What is striking about these materials is the non Fermi liquid behavior of their physical properties which exhibit weak power law or logarithmic divergences in temperature and suggest the existence of a critical point at $T =$

0 K. One possible origin of the 0 K critical point is an unconventional moment compensation process such as a multichannel Kondo effect. Such a single ion effect would seem to be appropriate for systems such as $Y_{1-x}U_xPd_3$, $U_{1-x}Th_xPd_2Al_3$, and $La_{1-x}Ce_xCu_2Si_2$, where the NFL characteristics persist to low concentrations of Ce or U. Another candidate for the source of the 0 K critical point is fluctuations of the order parameter in the vicinity of a 0 K second order phase transition. Such a transition could be associated with long-range or glassy magnetic or quadrupolar order. Systems in which this seems to be a viable mechanism include $UCu_{3.5}Pd_{1.5}$ and $CeCu_{5.9}Au_{0.1}$, in which the Ce and U sublattices are atomically ordered.

Some of the interest in non Fermi liquid behavior in strongly correlated electron systems, particularly copper oxides and f-electron materials, is associated with the unconventional superconductivity found in these two classes of materials. In spite of the disparity in the values of the superconducting critical temperatures T_c , which are as high as ~ 133 K for the copper oxide superconductors but only $\lesssim 2$ K for the f-electron heavy fermion materials, the superconducting states of both of these classes of materials share some striking similarities — the superconducting state appears to be anisotropic, with an energy gap that may vanish at points or lines on the Fermi surface, and the superconducting electron pairing may be mediated by antiferromagnetic spin fluctuations. An understanding of the source of the NFL behavior in these systems may provide important information about the electronic structure and excitations in these systems, as well as the origin of the unconventional superconductivity.

In this paper, we describe recent experimental efforts to characterize and develop an understanding of NFL behavior at low temperature in f-electron materials. Experiments are reviewed for three f-electron systems: $M_{1-x}U_xPd_3$ ($M = Sc, Y$), $U_{1-x}Th_xPd_2Al_3$, and $UCu_{5-x}Pd_x$. We also give an update of the emerging systematics of NFL behavior in f-electron systems, based on the present sample of nearly ten f-electron systems.

2. THE $M_{1-x}U_xPd_3$ ($M = Sc, Y$) SYSTEM

The $M_{1-x}U_xPd_3$ ($M = Sc, Y$, lanthanide) system exhibits many interesting phenomena including a structural phase transition, spin-glass freezing, crystalline electric field (CEF) effects, Fermi level tuning, and unusual Kondo behavior.^{1,2} Of particular interest is the Kondo behavior, which occurs at low U concentrations for $M = Sc$ and Y and has low temperature properties with NFL characteristics.

Shown in Fig. 1 is the temperature - U concentration ($T-x$) phase diagram of $Y_{1-x}U_xPd_3$ which summarizes the general behavior as a function of x . There is a mixed phase region for $0.6 \leq x \leq 0.8$. The samples which form in the hexagonal Ni_3Ti crystal structure ($0.9 \leq x \leq 1$) appear to have nonmagnetic ground states, although UPd_3 has recently been studied by inelastic neutron scattering and reported to undergo a quadrupolar transition at 6.5 K, followed by a magnetic transition at 4.5 K.³ The samples which form in the cubic Cu_3Au structure ($0 \leq x \leq 0.5$) with higher U concentrations ($0.3 \leq x \leq 0.5$) exhibit spin-glass freezing below a temperature T_{SG} which increases monotonically with x , as shown in Fig. 1. Such an increase is expected for RKKY interactions whose strength increases as $\sim J^2 \mathcal{N}(E_F)x$ where J is the exchange interaction parameter and $\mathcal{N}(E_F)$ is the density of states at the

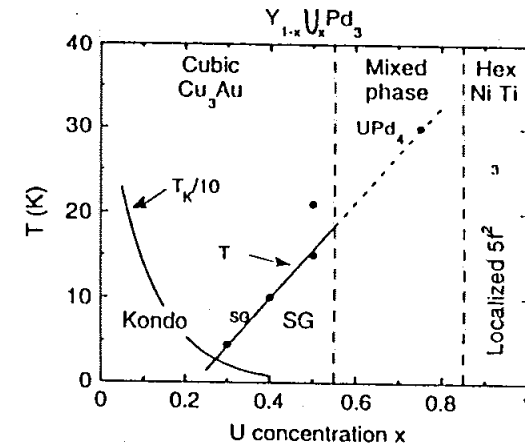


Fig. 1. Low temperature - U concentration phase diagram of $Y_{1-x}U_xPd_3$. From Ref. 2.

Fermi level. Recent muon spin relaxation measurements on $Y_{1-x}U_xPd_3$ demonstrate that the spin-glass order in this system can be understood in the context of induced moments.⁴

For $0 < x \leq 0.2$, $Y_{1-x}U_xPd_3$ exhibits unusual Kondo behavior with a Kondo temperature T_K that increases with decreasing x , as indicated in Fig. 1. This is consistent with the "Fermi level tuning" revealed by previous photoemission studies of $Y_{1-x}U_xPd_3$, where it was found that the separation between E_F and the 5f peak below it, $|E_F - E_{5f}|$, decreases with decreasing x as UPd_3 is diluted with Y.⁵ This was interpreted as "Fermi level tuning" because substitution of trivalent Y for tetravalent U causes a decrease in the conduction electron density and, in turn, E_F . Because $\mathcal{N}(E_F)$ is low throughout the series (≈ 1 state/eV cell⁶), the drop in E_F is rather large (~ 1 eV as x decreases from 1 to 0). The nearly linear decrease in the binding energy with decreasing x should cause a large increase in T_K since

$$k_B T_K \sim E_F \exp(-1/|J\mathcal{N}(E_F)|) \sim E_F \exp(-|E_F - E_{5f}|/(V_{kf}^2 \mathcal{N}(E_F))), \quad (1)$$

where V_{kf} is the hybridization matrix element.

From Eq. (1) it is evident that an increase in either V_{kf} or $\mathcal{N}(E_F)$ will also cause T_K to increase. To investigate this, we substituted other trivalent elements for Y to form $M_{1-x}U_xPd_3$, including (in order of increasing ionic radius R) $M = Sc, Y, Pr,$ and La . For given U concentration x , a larger R results in a larger lattice parameter, as shown in Fig. 2. For a Kondo system, a larger lattice constant is expected to yield a smaller hybridization strength and a corresponding smaller T_K value. Furthermore, specific heat measurements of the host MPd_3 compounds demonstrate that $\mathcal{N}(E_F)$ decreases with R , with linear coefficients $\gamma = 8.20, 3.48,$ and 0.28 mJ/mol K² for $M = Sc, Y,$ and La , respectively.⁷ Note the extremely small value of γ for $LaPd_3$. Thermal, transport, and magnetic measurements of

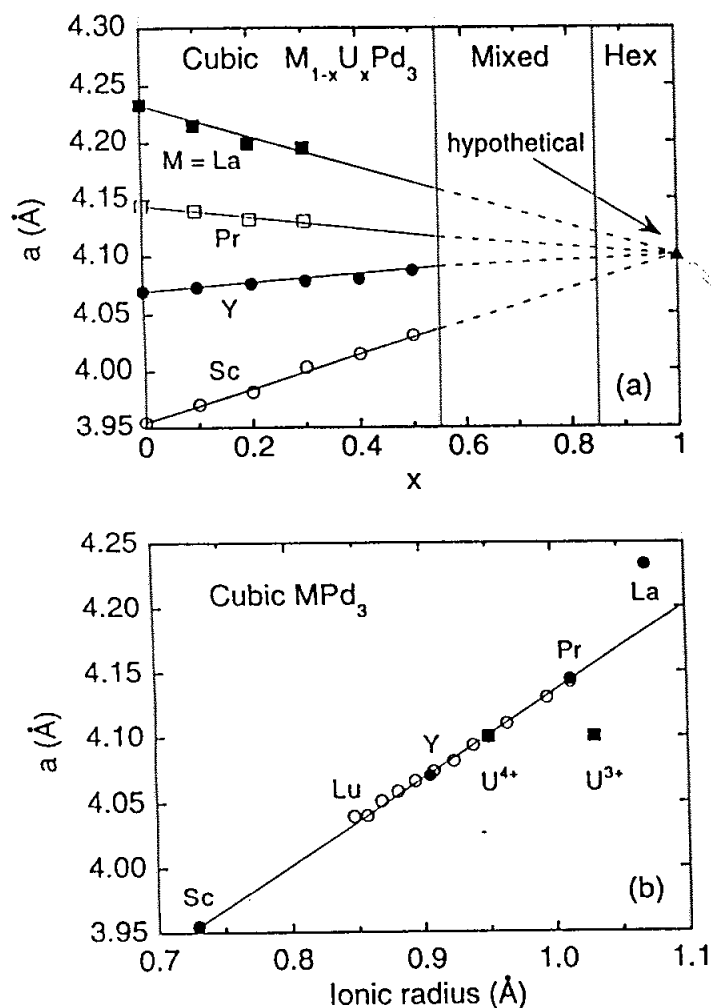


Fig. 2. (a) Cubic lattice parameters of $M_{1-x}U_xPd_3$ compounds as a function of x . Solid lines represent linear fits to the data, which extrapolate (dashed lines) to a common value of $4.100 \pm 0.005 \text{ \AA}$ for hypothetical cubic UPd_3 . (b) Lattice parameters of cubic MPd_3 compounds versus ionic radius of the trivalent ion. With the exception of $LaPd_3$, the data fall on a straight line. The hypothetical value for cubic UPd_3 obtained from (a) (filled triangle) is consistent with U being tetravalent in the $M_{1-x}U_xPd_3$ compounds. From Ref. 8.

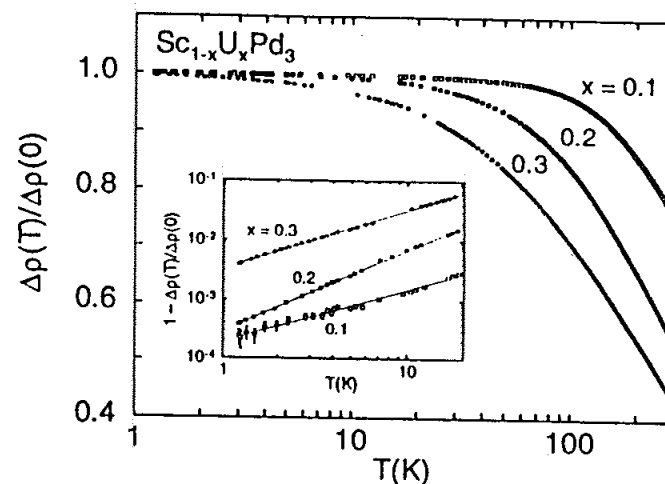


Fig. 3. Uranium contribution to the electrical resistivity $\Delta\rho(T)$ of $Sc_{1-x}U_xPd_3$ ($x = 0.1, 0.2, 0.3$), normalized to the extrapolated zero temperature value $\Delta\rho(0)$, versus $\log T$. Inset: Log-log plot of $1 - \Delta\rho(T)/\Delta\rho(0) = a(T/T_K)^n$ with $n = 0.9 \pm 0.2, 1.4 \pm 0.2, \text{ and } 1.0 \pm 0.2$ for $x = 0.1, 0.2, \text{ and } 0.3$, respectively. From Ref. 10.

the $M_{1-x}U_xPd_3$ systems are indeed consistent with Fermi level tuning in which T_K decreases with increasing R . Sc behaves like Y, but with a larger T_K for given x . Pr has a smaller T_K , which is barely evident as an increase in ρ with decreasing T for $x = 1$. The La system does not display a Kondo effect at all down to at least 1 K, for x as low as 0.1. The non Fermi liquid properties of the Kondo systems $M = Y$ and Sc are summarized below.

The observation of Fermi level tuning in cubic $M_{1-x}U_xPd_3$ and the absence of Fermi level tuning in hexagonal $M_{1-x}U_xPd_3$ ($M^{4+} = Zr$ and Th),⁹ imply that U is tetravalent in all of these $M_{1-x}U_xPd_3$ compounds. Further evidence for tetravalent U comes from considering the evolution of the cubic lattice parameters of $M_{1-x}U_xPd_3$ ($M = Sc, Y, La, Pr; x \leq 0.5$), derived from X-ray diffraction measurements, and shown in Fig. 2. The cubic lattice parameters, plotted as a function of x for each of the $M_{1-x}U_xPd_3$ series, extrapolate to a common value of $4.100 \pm 0.005 \text{ \AA}$ for $x = 1$, which represents the lattice parameter of hypothetical cubic UPd_3 . Comparison of this value to the lattice parameters of cubic MPd_3 compounds, which when plotted as a function of M^{3+} ionic radius are seen to fall on a straight line,⁸ yield a value for the ionic radius of U that is consistent with U being tetravalent in $M_{1-x}U_xPd_3$.

2.1. Non Fermi Liquid Properties

The existence of a Kondo effect in the $M_{1-x}U_xPd_3$ ($M = Sc, Y$) system for $x \leq 0.3$ is evident from the electrical resistivity $\rho(T)$, which increases logarithmically

Table 1. Approximate T_K values (in K) for $M_{1-x}U_xPd_3$ ($M = Sc, Y$), estimated as the temperature at which $\Delta\rho(T)/\Delta\rho(0) = 0.8$.

x	0.02	0.05	0.1	0.2	0.3
M = Sc	- ^a	- ^a	260	120	60
Y	200	160	140	50	spin glass

^aNot measured.

with decreasing temperature at high temperatures $T > T_K$.¹ Data for $Sc_{1-x}U_xPd_3$ are shown in Fig. 3.¹⁰ The U contribution to the resistivity $\Delta\rho(T)$ was estimated by subtracting $\rho(T)$ of the host MPd₃ compound. Estimates of the Kondo temperature T_K as the temperature at which the normalized resistivity $\Delta\rho(T)/\Delta\rho(0)$ equals 0.8 yield T_K values which increase with decreasing x , in accordance with Fermi level tuning. Approximate values are listed in Table 1. At low temperatures $T \ll T_K$, $\rho(T)$ does not saturate quadratically as

$$\frac{\Delta\rho(T)}{\Delta\rho(0)} = 1 - a(T/T_K)^n \quad (2)$$

with $n = 2$ which is expected for a conventional Kondo effect and reflects the behavior of a Fermi liquid. Rather, we find $n \approx 1.0 \pm 0.2$ for all $M = Y$ samples in the temperature range $T \leq 20$ K. Power law fits for $M = Sc$ are shown as solid lines in the inset of Fig. 3 with slopes which correspond to $n = 0.9, 1.4$, and 1.0 ± 0.2 for $x = 0.1, 0.2$, and 0.3 , respectively. Taking a value for a of 0.23, values of T_K from these power law fits vary from ~ 40 K for $x = 0.2$ to ~ 500 K for $x = 0.05$ for $M = Y$, and from ~ 70 K for $x = 0.3$ to ~ 2900 K for $M = Sc$. It is difficult to determine the power law temperature dependence of $\rho(T)$ for smaller values of x because of the large values of T_K which yield small $d\rho(T)/dT$ slopes at low temperatures.

In an attempt to approach the single impurity limit while holding T_K approximately constant, we have made similar $\rho(T)$ measurements on the series of alloys $Y_{0.8}Th_{0.2-x}U_xPd_3$ ($0.01 \leq x \leq 0.2$), shown in Fig. 4.⁸ Because nonmagnetic Th is tetravalent, the total concentration of tetravalent ions remains fixed at 0.2, which should yield a constant value $T_K \approx 40$ K according to the Fermi level tuning scenario, everything else remaining constant. From a similar analysis of $\rho(T)$, T_K appears to increase slightly with decreasing x , as listed in Fig. 4 (a). The low temperature power law fits to Eq. (2), shown in Fig. 4 (b), again yield exponents of $n = 1.0 \pm 0.1$ in the temperature range $T \leq 20$ K. The electrical resistivity thus has a NFL linear temperature dependence at the lowest measured temperatures even for samples with U concentrations as low as 1%. The U concentration independence of this feature suggests that it is not due to interimpurity interactions.

Recently, an $Y_{0.8}U_{0.2}Pd_3$ polycrystalline specimen was investigated optically over a broad frequency range from 15 to 10^5 cm^{-1} by Degiorgi *et al.*¹¹ Evaluation of the frequency dependence of the transport relaxation rate τ^{-1} at several temperatures reveals that τ^{-1} increases linearly with decreasing frequency and temperature. This was interpreted as another manifestation of NFL behavior in the $Y_{1-x}U_xPd_3$ system.

Shown in Fig. 5 is the uranium contribution to the specific heat ΔC , plotted as

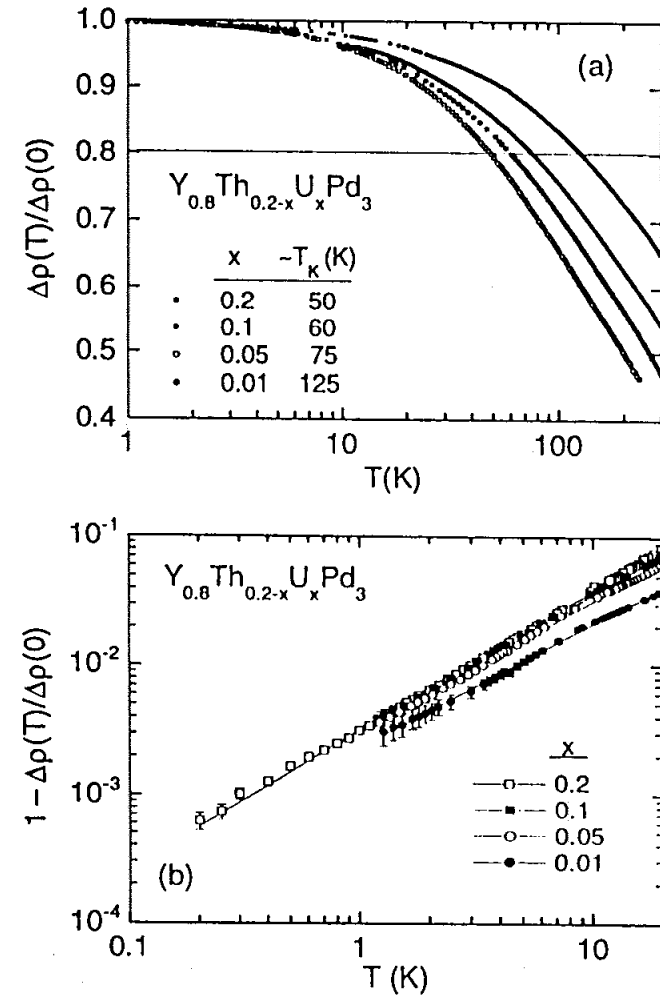


Fig. 4. (a) Normalized electrical resistivity $\Delta\rho(T)/\Delta\rho(0)$ versus $\log T$ for the $Y_{0.8}Th_{0.2-x}U_xPd_3$ ($0 \leq x \leq 0.2$) system revealing Kondo behavior with a Kondo temperature T_K which increases only slightly with decreasing x . (b) Low temperature resistivity data ($T \leq 20$ K) plotted as $\log(1 - \Delta\rho(T)/\Delta\rho(0))$ versus $\log T$. Solid lines represent fits to a power law $\Delta\rho(T)/\Delta\rho(0) = 1 - a(T/T_K)^n$, with $n = 1.0 \pm 0.1$ for all samples, exhibiting NFL behavior. This value is in between that expected for single channel ($n = 2$) and two channel ($n = 1/2$) $S = 1/2$ Kondo models. From Ref. 8.

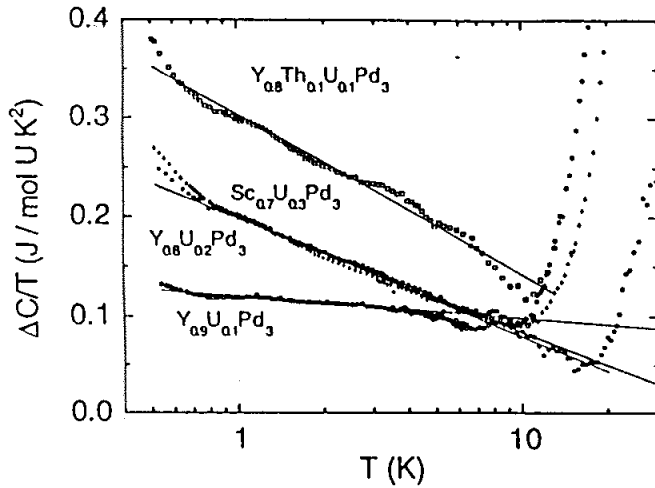


Fig. 5. Low temperature specific heat $\Delta C/T$ versus $\log T$ for various Kondo alloys which exhibit a $T = 0$ logarithmic divergence, a non Fermi liquid behavior. Solid lines are fits of the data to the two channel, $S = 1/2$ Kondo model plus a constant B' : $\Delta C/T = -(0.251/T_K)R \ln(T/0.41T_K) + B'$. The associated entropy suggests a finite zero temperature entropy of $S(0) \approx (R/2) \ln(2)$. From Ref. 8.

$\Delta C/T$ versus $\log T$, for several samples which display a characteristic logarithmic divergence over the temperature range $0.7 \text{ K} \lesssim T \lesssim 10 \text{ K}$, including $Y_{0.8}U_{0.2}Pd_3$, $Y_{0.9}U_{0.1}Pd_3$, $Y_{0.8}Th_{0.1}U_{0.1}Pd_3$, and $Sc_{0.7}U_{0.3}Pd_3$.⁸ Such NFL behavior is in striking contrast to a conventional Kondo effect where $\Delta C/T$ approaches a constant value which varies as $1/T_K$ at low temperatures $T \ll T_K$. At higher temperatures, the data increase sharply due to difficulties in subtracting the phonon contribution and/or a Schottky anomaly arising from an excited state CEF level above the ground state. The solid lines represent least squares linear fits of the data to the equation $\Delta C/T = A \ln T + B$. (Here, \ln represents the natural logarithm). Irrespective of the microscopic mechanism responsible for such NFL behavior, it is useful to investigate how the data scale with the characteristic energy of the system, the Kondo temperature T_K , according to

$$\Delta C/T = (-A'R/T_K) \ln(T/bT_K) + B', \quad (3)$$

where A' , b , and B' are constants and R is the gas constant. If we assume this form of scaling with T_K , larger logarithmic slopes (coefficient A) correspond to smaller values of T_K . Using values $b = 0.41$ and $A' = 0.251$ (the value for a two channel Kondo effect), one can extract a value for T_K from the slope A of these lines, and B' from the offset B . Values for B' are comparable to measured values of the linear coefficient of the specific heat γ for the host metals: $\gamma \approx 3.5$, 6.9 , and 8.2 mJ/mol K^2 for YPd_3 ,⁷ $Y_{0.8}Th_{0.2}Pd_3$, and $ScPd_3$,⁷ respectively, which have not been subtracted from the data. A hybridization broadened Schottky anomaly

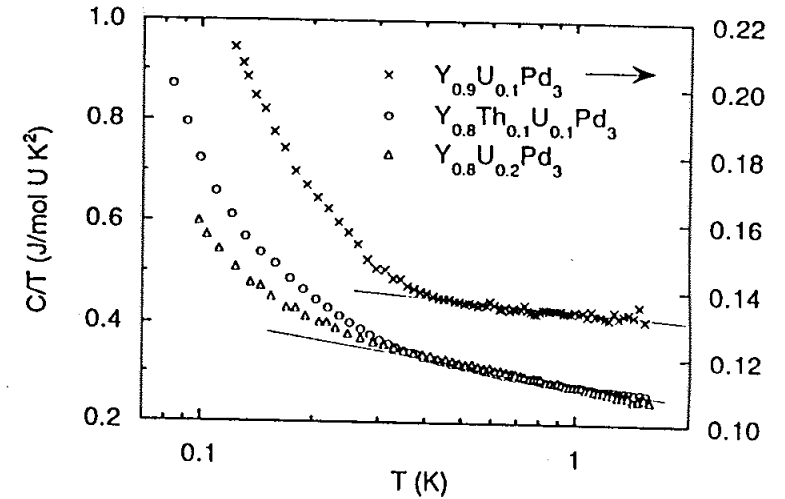


Fig. 6. Specific heat C/T versus $\log T$ to temperatures as low as 80 mK for three of the Kondo alloys from Fig. 5, measured in a $^3\text{He}-^4\text{He}$ dilution refrigerator. Solid lines are fits of the data to the two channel, $S = 1/2$ Kondo model plus a constant B' .

at higher temperatures can also contribute to B' . Especially noteworthy is the behavior of the more dilute compound $Y_{0.8}Th_{0.1}U_{0.1}Pd_3$ which is nearly identical to that of $Y_{0.8}U_{0.2}Pd_3$, which suggests that the observed NFL behavior is not due to interimpurity interactions which decrease with decreasing U concentration, but is dominated by single impurity effects. Parameter values for $Sc_{0.7}U_{0.3}Pd_3$ are also comparable to those for $Y_{0.8}U_{0.2}Pd_3$. Fits of the $\Delta C/T$ data for $Y_{0.9}U_{0.1}Pd_3$ yield a larger T_K value than for $Y_{0.8}U_{0.2}Pd_3$, in agreement with the resistivity data and Fermi level tuning mechanism.

A remarkable aspect of the specific heat data is that the associated entropy $S(T)$ for all of these samples saturates to a value close to $(R/2) \ln(2)$ before continuing to increase due to the higher temperature upturns in $\Delta C/T$ seen in Fig. 5.¹ This suggests a finite zero temperature entropy of the same value, in order that the full degeneracy of the ground doublet be recovered at high temperatures. Such an unusual $T = 0$ entropy is predicted for the two channel, $S = 1/2$ Kondo model.¹² However, this entropy is expected to be removed at low but finite temperatures due to any weak interactions which might lift the ground state degeneracy.

The results of recent heat capacity measurements on several samples in the $Y_{1-x}(Th_yU_{1-y})_xPd_3$ series taken in a $^3\text{He}-^4\text{He}$ dilution refrigerator to temperatures as low as 80 mK are shown in Fig. 6. The logarithmic temperature dependence of C/T persists down to about 0.5 K. Straight lines through the C/T data above 0.5 K over the limited temperature range shown correspond to $T_K = 40 \text{ K}$,

$B' = 0.132$, for $Y_{0.8}U_{0.2}Pd_3$ and $Y_{0.8}Th_{0.1}U_{0.1}Pd_3$ and $T_K = 680$ K, $B' = 0.117$, for $Y_{0.9}U_{0.1}Pd_3$. The C/T data for $Y_{0.8}U_{0.2}Pd_3$ in Fig. 6 are somewhat higher than the corresponding data in Fig. 5; the origin of this discrepancy is presently under investigation. Below ~ 0.5 K, C/T rises dramatically without any sign of saturation down to the lowest temperature studied. This behavior is similar to that previously found by Olt *et al.* for $Y_{0.8}U_{0.2}Pd_3$ who reported that the upturn in C/T persisted to at least 0.05 K.¹³ The deviation away from logarithmic dependence is well described by $\Delta C/T = AT^{-2}$, which is the temperature dependence of a Schottky anomaly in the high temperature limit. The magnitude of A from the measurements of Olt *et al.*¹³ is too large for a nuclear Schottky anomaly, but for a two level electronic Schottky anomaly corresponds to a level splitting of 2.5 mK. It has been suggested previously⁸ that this rise may account for the missing entropy of $\sim (R/2)\ln(2)$. Our results are consistent with this proposition.

The magnetic susceptibility of $M_{1-x}U_xPd_3$ ($M = Sc, Y, La$), as well as that of $Y_{1-x}(Th_yU_{1-y})_xPd_3$, exhibits a Curie-Weiss temperature dependence $N\mu_{eff}^2/3k_B(T - \theta_p)$, where N is the number of U ions, μ_{eff} is the U effective moment, and θ_p is the Curie-Weiss temperature, at high temperatures $T > 150$ K, after subtraction of a temperature independent background term χ_0 .¹ The effective moment is close to the free ion value for either tetravalent or trivalent U. The Curie-Weiss temperature θ_p is large and negative, indicative of antiferromagnetic exchange interactions, with a magnitude that correlates with the Kondo temperature such that $|\theta_p| \approx 4T_K$, typical of Kondo systems. The T_K inferred from θ_p is associated with the antiferromagnetic exchange interaction between the conduction electrons and the excited magnetic states which are thermally populated at higher temperatures.

At low temperatures, $\chi(T)$ of $M_{1-x}U_xPd_3$ ($M = Y, Sc$) increases more rapidly with decreasing temperature than the Curie-Weiss temperature dependence, and continues to increase with positive curvature down to the lowest measured temperature for $x \leq 0.2$ and 0.3 for $M = Y$ and Sc , respectively. This is in contrast to the Fermi liquid behavior of the single channel, $S = 1/2$ Kondo effect in which $\chi(T)$ becomes temperature independent for $T \ll T_K$ due to screening of the impurity moments by the conduction electrons. The precise temperature dependence of $\chi(T)$ at the lowest temperatures is masked by the possible presence of magnetic impurities other than U. We have estimated and subtracted the impurity contribution of $Y_{0.8}U_{0.2}Pd_3$ through analysis of isothermal $M(H)$ curves as described elsewhere,² yielding the intrinsic susceptibility at various temperatures from 0.6 K to 40 K shown in Fig. 7. The $\chi(T)$ data are well described by the equation

$$\chi(T) = \chi(0) \left(1 - c(T/T_K)^{1/2} \right), \quad (4)$$

represented by the solid line in Fig. 7. The data appear to exhibit a $T^{1/2}$ temperature dependence over a wide temperature range, down to the lowest temperatures, extrapolating to a value of 5.9×10^{-3} emu/mol U at $T = 0$. If we assume $T_K = 42$ K, then from the fit we obtain $c = 0.36$.

A number of other measurements have been performed on the $Y_{1-x}U_xPd_3$ system in order to further characterize and explore the NFL behavior in this system. Thermoelectric power $S(T)$ measurements from 2-200 K have been made in

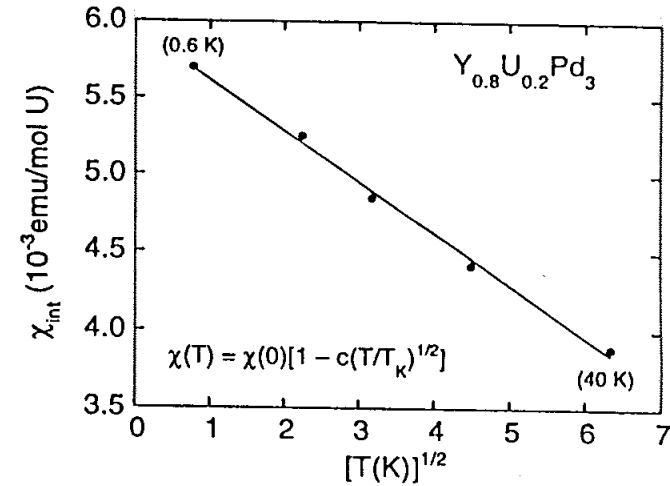


Fig. 7. Intrinsic magnetic susceptibility χ_{int} versus square root of the temperature for $Y_{0.8}U_{0.2}Pd_3$. The solid line represents a fit of the data to the equation $\chi(T) = \chi(0)[1 - c(T/T_K)^{1/2}]$, where $\chi(0) = 5.9 \times 10^{-3}$ emu/mol U and $c = 0.36$ for $T_K = 42$ K. From Ref. 2.

$Y_{1-x}U_xPd_3$ in the range $0 \leq x \leq 0.4$.¹⁴ The behavior of $S(T)$ for $x = 0.05, 0.1$ is reminiscent of typical Kondo materials in the sense that there is a "giant" positive contribution linear in T at low temperatures and independent of x . However, this result suggests that T_K is independent of x , in contrast to the $\rho(T)$, $C(T)$, and $\chi(T)$ measurements discussed herein. At high temperatures, $S(T)$ changes from positive to negative as x is varied from 0.1 to 0.3, suggestive of a cross-over or transition in electronic structure near $x = 0.2$. The spin-glass transition of the $x = 0.3, 0.4$ alloys is signaled by a zero-crossing of S , similar to that observed for conventional spin glasses.

2.2. Fermi Level Tuning in the $(Y_{1-y}Th_y)_{1-x}U_xPd_3$ System

Besides Fermi level tuning, the substitution of U^{4+} for Y^{3+} in the $Y_{1-x}U_xPd_3$ system has the additional effect of increasing the U intersite interaction strength as x is increased which leads to spin-glass freezing below a characteristic temperature T_{SG} that increases with x . In order to study the effect of the increase of $|E_F - E_{5f}|$ on T_K , with U intersite interactions held constant to first approximation, we have performed measurements of $\rho(T)$, $\chi(T)$, and $C(T)$ as functions of y for a fixed value $x = 0.1$ in the $(Y_{1-y}Th_y)_{1-x}U_xPd_3$ system.¹⁶ The data clearly reveal the scaling of the physical properties with T_K and the phenomenon of Fermi level tuning in this system.

Shown in Fig. 8(a) are plots of ρ versus T between 1.2 K and 300 K for $Y_{0.9-y}Th_yU_{0.1}Pd_3$ samples with $y = 0, 0.1, 0.2, 0.3$, and 0.4. The $\rho(T)$ data for $0 \leq y \leq 0.2$ reveal that ρ increases with decreasing T , indicative of a Kondo effect.

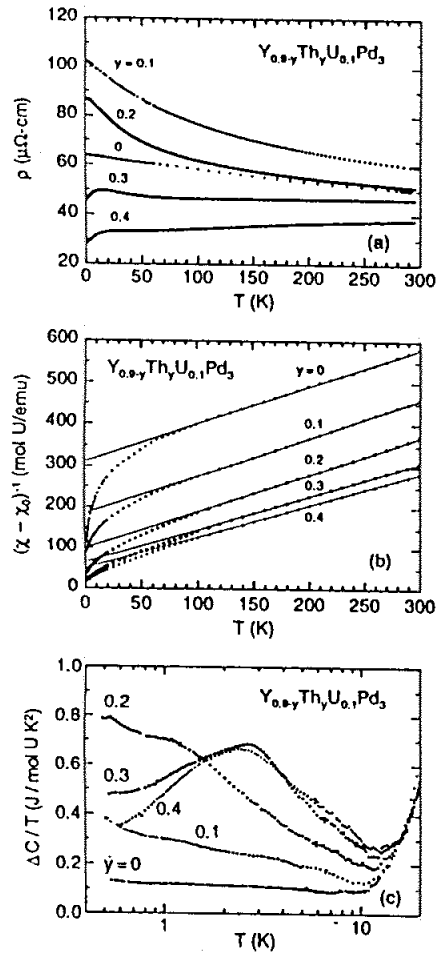


Fig. 8. Temperature T dependence of the electrical resistivity ρ , magnetic susceptibility χ , and electronic specific heat ΔC of the $Y_{0.9-y}Th_yU_{0.1}Pd_3$ ($y = 0, 0.1, 0.2, 0.3, 0.4$) system: (a) ρ versus T ; (b) $(\chi - \chi_0)^{-1}$ versus T , where χ_0 is defined in the text; (c) $\Delta C/T$ versus $\ln T$. From Ref. 15.

The increase of the temperature dependence of ρ with y for $0 \leq y \leq 0.2$ suggests that T_K decreases with y , consistent with Fermi level tuning.

Displayed in Fig. 8(b) are plots of $(\chi - \chi_0)^{-1}$ versus T between 1.8 K and 300 K, where χ_0 was determined by fitting the $\chi(T)$ data to the sum of a constant χ_0 and a Curie-Weiss law. Below ~ 100 K, the $(\chi - \chi_0)^{-1}$ versus T data fall below the linear fits to the higher T data and approach a finite value as $T \rightarrow 0$, indicative of a nonmagnetic ground state, which is presumably the $U \Gamma_3$ nonmagnetic doublet. The magnitude of the negative Curie-Weiss temperature $|\theta_p|$ decreases exponentially and saturates to a value of 57 K for large y . A comparable x -independent value of θ_p was observed for the related system $La_{1-x}U_xPd_3$ which does not show a Kondo effect. This decrease is consistent with the decrease of T_K with y inferred from the $\rho(T)$ data of Fig. 8(a) since for Kondo systems, $|\theta_p| \approx 3 - 4 T_K$.

Presented in Fig. 8(c) are plots of $\Delta C/T$ versus $\ln T$ for $Y_{0.9-y}Th_yU_{0.1}Pd_3$ between ~ 0.5 K and 20 K. The increase of the magnitude of the slope $|d(\Delta C/T)/d \ln T|$ with y is consistent with a decrease of T_K with y . The features in the $\Delta C/T$ versus $\ln T$ data at ~ 1 K (a shoulder) for the sample with $y = 0.2$ and at ~ 2.4 K (a maximum) for the samples with $x = 0.3$ and 0.4 may be due to the splitting of the Γ_3 nonmagnetic doublet ground state, which is analogous to Zeeman splitting of the magnetic doublet for a magnetic two-channel Kondo effect. It is interesting that the evolution of the shape of the $\Delta C(T)$ curves with y resembles that of the calculated $\Delta C(T)$ curves with y in the presence of an applied magnetic field.¹⁶ Such a splitting of the $U \Gamma_3$ doublet could arise from a local charge asymmetry or distortion of the lattice from cubic symmetry about a U site due to the substitution of Th. An analysis of the slope $|d(\Delta C/T)/d \ln T|$ within the context of the two channel Kondo model yields a decrease of T_K with y , similar to that deduced from the $\chi(T)$ data.

2.3. Crystalline Electric Field Energy Level Scheme for U^{4+}

In order to understand the microscopic origin of the observed NFL behavior in the thermal, transport, and magnetic properties, it is important to determine the CEF energy level scheme of the U 5f electrons. Tetravalent U ions have two localized 5f electrons ($5f^2$) which have a Hund's rules magnetic ground state multiplet configuration 3H_4 ($S = 1, L = 5, J = 4$). In a cubic CEF, the 9-fold degeneracy is lifted, leaving a Γ_1 singlet, Γ_4 and Γ_5 triplets, and a Γ_3 nonmagnetic (non Kramers) doublet.¹⁷ According to Lea, Leask, and Wolf, it is possible for either the Γ_1, Γ_3 , or Γ_5 state to lie lowest in energy. These states, in turn, can hybridize with conduction electron states leading to Kondo, heavy fermion, or intermediate valence behavior. For actinide compounds, the CEF splitting and hybridization energy scales are often comparable and can range from 1 K to 10^3 K.

Previous inelastic neutron scattering measurements on $Y_{0.8}U_{0.2}Pd_3$ at 10 K revealed two magnetic peaks centered at energies $E \approx 5$ meV and 16 meV, attributed to hybridization broadened CEF levels, with integrated intensities consistent with Γ_5 and Γ_4 first and second excited state triplets, respectively, lying above a Γ_3 doublet ground state.¹⁸ For a magnetic Kondo effect, one expects to observe quasielastic scattering with a half width of the order of $k_B T_K$, which for $Y_{0.8}U_{0.2}Pd_3$ is at least 4 meV. The absence of a pronounced low energy quasielastic response provided

further evidence that the nonmagnetic Γ_3 doublet lies lowest in energy.

The possibility of a low energy quasielastic response was investigated further by performing inelastic neutron scattering at low energies. Low temperature (~ 1.5 K) data with ~ 0.5 meV resolution showed no indication of substantial scattering below the first CEF peak at ~ 7 meV, while higher resolution (0.1 meV) measurements up to 0.6 meV showed no scattering above ~ 0.2 meV. In an attempt to identify the magnetic scattering even at zero energy transfer, polarized measurements of the spin flip scattering by subtracting the spectra taken using a vertical field from that using a horizontal field are in progress.

The Γ_3 state consists of two degenerate singlet states which can be expressed as linear combinations of the J_z eigenstates $|J_z\rangle$ as $0.5401(|4\rangle + |-4\rangle) - 0.6455|0\rangle$ and $(1/\sqrt{2})(|2\rangle + |-2\rangle)$. It is apparent that the magnetic moment, which is proportional to the expectation value of J_z , $\langle \Gamma_3 | J_z | \Gamma_3 \rangle$, vanishes. However, the expectation value of the z-component of the electric quadrupole moment, which is proportional to $\langle \Gamma_3 | 3J_z^2 - J(J+1) | \Gamma_3 \rangle$, is finite. Thus, an electric field gradient, which can be obtained through the application of uniaxial stress or some other interaction which drives the system away from CEF cubic symmetry, will induce a net electric quadrupole moment on the impurity in which the charge distribution of the 5f electrons in the Γ_3 state no longer has spherical symmetry. It is this charge asymmetry that the conduction electrons overcompensate through the two channel quadrupolar Kondo effect (QKE). While it is not clear that a QKE is responsible for the NFL low temperature behavior in the $Y_{1-x}U_xPd_3$ system, the ground state does appear to be a Γ_3 nonmagnetic doublet with an electric quadrupole moment so that the conditions for a QKE seem to be satisfied. However, recent elastic constant measurements on a polycrystalline specimen of $Y_{0.8}U_{0.2}Pd_3$ by Amara *et al.*¹⁹ revealed no strong variation with T as expected for a quadrupolar interaction.

3. THE $U_{1-x}Th_xPd_2Al_3$ SYSTEM

In 1991, Geibel *et al.* discovered two new U-based heavy fermion superconductors, UNi_2Al_3 ²⁰ and UPd_2Al_3 ,²¹ which crystallize in the hexagonal $PrNi_2Al_3$ structure. These two compounds exhibit the coexistence of superconductivity and antiferromagnetism (AFM) with $T_c < T_N$; for UNi_2Al_3 , $T_c \approx 1$ K and $T_N = 4.6$ K, while for UPd_2Al_3 , $T_c \approx 2$ K and $T_N = 14.6$ K.

The compound UPd_2Al_3 has the highest T_c of the heavy fermion superconductors and a large ordered magnetic moment of $0.85 \mu_B$,²² in contrast to the small ordered moments ($\sim 0.02 \mu_B$) observed for URu_2Si_2 ²³ and UPt_3 ,²⁴ two other heavy fermion compounds in which superconductivity and AFM coexist with $T_c < T_N$. The antiferromagnetic structure of UPd_2Al_3 consists of alternating ferromagnetic sheets, with the moments lying in the hexagonal basal plane.²² The temperature dependence of the upper critical field is consistent with singlet superconductivity and the antiferromagnetic transition appears to involve the opening of a 30 meV gap over part of the Fermi surface,²⁵ similar to that observed in URu_2Si_2 .²⁶

In an effort to find new examples of NFL behavior, we embarked on an investigation of the $U_{1-x}Th_xPd_2Al_3$ system about a year ago. Our initial studies revealed NFL behavior in the low temperature physical properties of this system^{2,27} which we have characterized in more detail during the past year. Based upon measurements

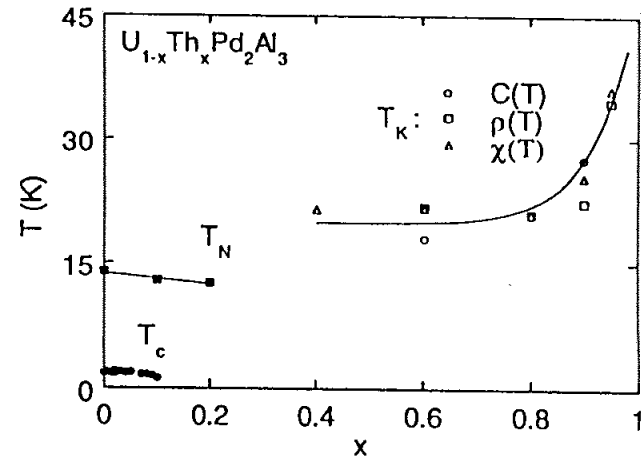


Fig. 9. Low temperature phase diagram of the $U_{1-x}Th_xPd_2Al_3$ system. As the Th concentration x is increased, the Neel temperature T_N and the superconducting critical temperature T_c decrease slightly, but the features associated with AFM and superconductivity are rapidly suppressed and eventually become undetectable. The line in the right hand side of the figure represents the estimated value of the Kondo temperature T_K .

of $\rho(T)$, $C(T)$, and $\chi(T)$, which will be briefly reviewed below, the low temperature phase diagram of the $U_{1-x}Th_xPd_2Al_3$ system shown in Fig. 9 has been established. However, this phase diagram is incomplete near $x = 1$ since we have discovered during the course of this investigation that the compound $ThPd_2Al_3$ is superconducting with a $T_c = 0.2$ K. This is an extraordinary result, since it is the first case where a Ce or U heavy fermion superconductor has an isostructural counterpart based on a rare earth or actinide element with an empty or filled f-electron shell (i. e., Sc, Y, La, Lu, Th) which is also superconducting. We are presently measuring the $T_c(x)$ curve for the $U_{1-x}Th_xPd_2Al_3$ system near $x = 1$.

Electrical resistivity $\rho(T)$ data for the $U_{1-x}Th_xPd_2Al_3$ system for various values of x between 0 and 1 are shown in Fig. 10. With increasing x , the Neel temperature T_N remains nearly constant up to $x = 0.4$, while the drop in ρ below T_N is rapidly suppressed. For values of $x \geq 0.6$, no magnetic ordering is evident and $\rho(T)$ exhibits single ion Kondo like behavior. However, $\rho(T)$ is nearly linear over an appreciable temperature range between about ~ 4 K and ~ 30 K, indicative of NFL behavior and similar to that observed for the $M_{1-x}U_xPd_3$ ($M = Sc, Y$) systems discussed in the preceding section. The resistivity $\rho(T)$ levels off below ~ 4 K, suggesting that the degeneracy of the conduction electron channels or the localized electron spin or charge degrees of freedom has been removed by some type of residual interaction, producing an evolution towards single channel FL behavior.

Plots of $\log(1 - \Delta\rho(T)/\Delta\rho(0))$ versus $\log T$ between 0.1 K and 20 K for $x = 0.6, 0.8, 0.9$, and 0.95 are shown in Fig. 11. The U contribution $\Delta\rho$ to the

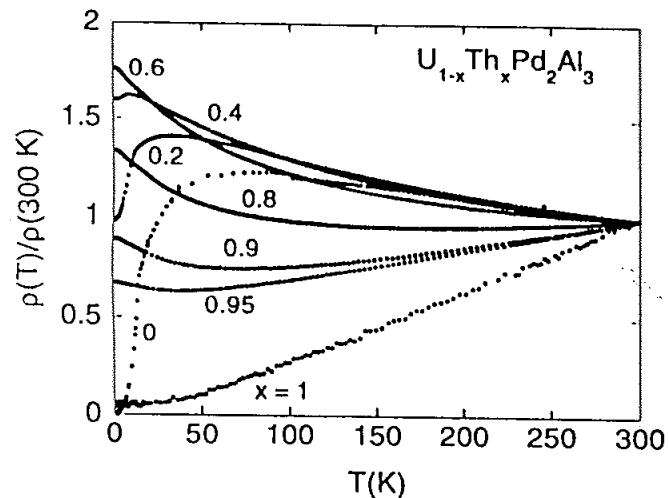


Fig. 10. Electrical resistivity $\rho(T)$, normalized to its room temperature value $\rho(300 \text{ K})$, versus temperature T for the $U_{1-x}Th_xPd_2Al_3$ system for various values of x between 0 and 1.

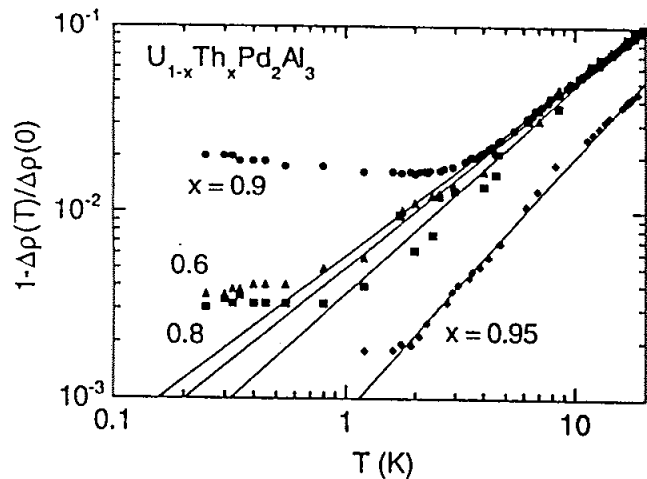


Fig. 11. Low temperature electrical resistivity data ($T \leq 20 \text{ K}$) plotted as $\log(1 - \Delta\rho(T)/\Delta\rho(0))$ versus $\log T$. Solid lines represent fits to a power law $\Delta\rho(T)/\Delta\rho(0) = 1 - a(T/T_K)^n$, with $n \approx 1$, indicative of NFL behavior.

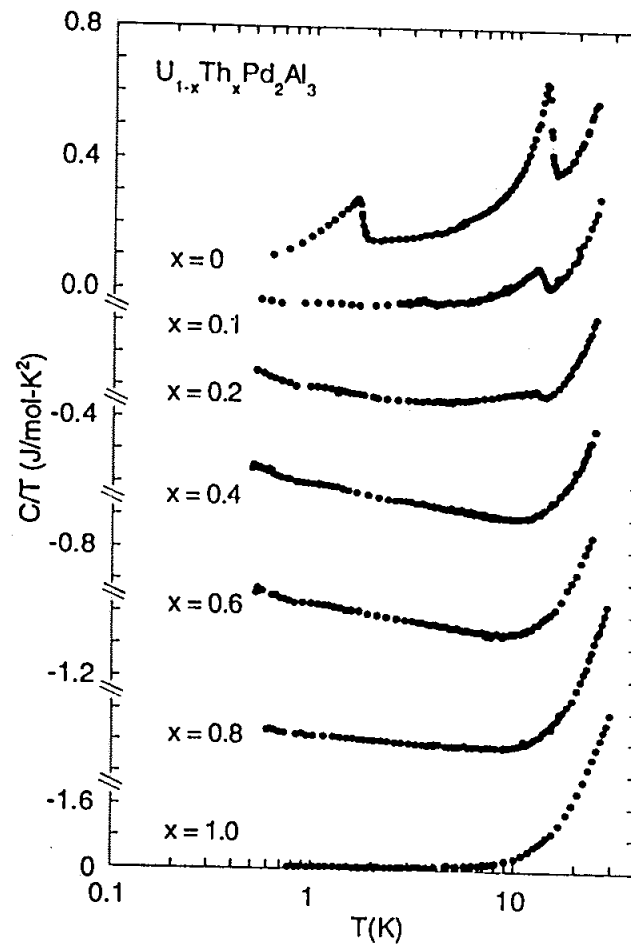


Fig. 12. Specific heat divided by temperature C/T versus T of $U_{1-x}Th_xPd_2Al_3$ for various values of x between 0 and 1.

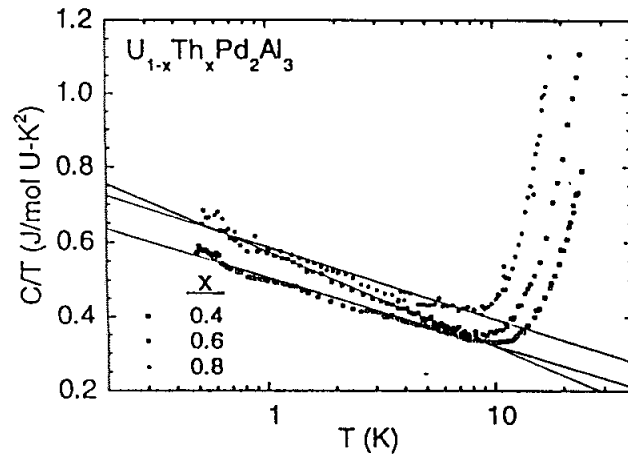


Fig. 13. Low temperature specific heat divided by temperature, C/T , versus $\log T$ for $U_{1-x}Th_xPd_2Al_3$ alloys with $x = 0.4, 0.6$, and 0.8 .

resistivity was estimated by subtracting the resistivity of $ThPd_2Al_3$ from that of each $U_{1-x}Th_xPd_2Al_3$ alloy to remove the phonon background contribution, at least to a first approximation. In the range $4\text{ K} \leq T \leq 20\text{ K}$, the data in Fig. 11 can be described by the relation $\Delta\rho(T) = \Delta\rho(0)(1 - a(T/T_K)^n)$, yielding values for the residual resistivity $\Delta\rho(0)$, the slope n , and the intercept a/T_K . Taking $a = 0.1$ to achieve agreement with the T_K values calculated from the measured heat capacity, the fits yield the following values of n and T_K : $n = 1.0, 1.1, 0.95, 1.4$; $T_K = 22\text{ K}, 21\text{ K}, 22\text{ K}, 35\text{ K}$; for $x = 0.6, 0.8, 0.9, 0.95$, respectively.

Displayed in Fig. 12 are plots of C/T versus $\log T$ for various values of x between 0 and 1 for $U_{1-x}Th_xPd_2Al_3$. The specific heat anomalies due to AFM at T_N and superconductivity at T_c , which are evident in the data for $x = 0$, are rapidly suppressed with increasing x , similar to that observed in the $U_{1-x}Th_xRu_2Si_2$ system.²⁸ A $\ln T$ divergence in the C/T data, emerging in the sample with $x = 0.2$, is fully developed for the samples with $x = 0.4, 0.6$, and 0.8 . Plots of $C(T)/T$, per mole $U\text{ K}^2$, versus $\log T$ are presented in Fig. 13 for the samples with $x = 0.4, 0.6$, and 0.8 . Analysis of the specific heat data in terms of the two-channel spin 1/2 Kondo formula yields values of T_K of 26 K, 18 K, and 21 K, for $x = 0.4, 0.6$, and 0.8 , respectively, in good agreement with the values inferred from the electrical resistivity. Experiments are in progress to determine whether the specific heat exhibits a sharp upturn below $\sim 0.4\text{ K}$, as it does in the $Y_{1-x}U_xPd_3$ system.

Figure 14 contains plots of the magnetic susceptibility χ versus temperature for the $U_{1-x}Th_xPd_2Al_3$ system for various values of x in the range $0 \leq x \leq 1$. The $\chi(T)$ data for UPd_2Al_3 exhibit a maximum near 40 K and an abrupt drop at $T_N = 14.5\text{ K}$. With increasing x , the maximum in $\chi(T)$ is suppressed until it disappears

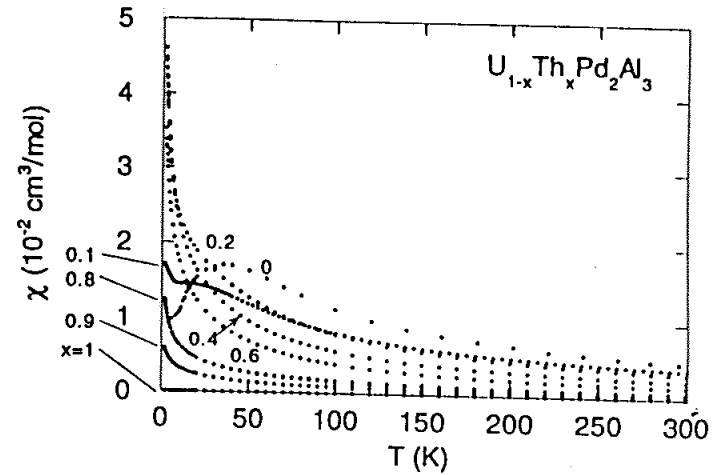


Fig. 14. Magnetic susceptibility χ versus temperature T for the $U_{1-x}Th_xPd_2Al_3$ system for various values of x between 0 and 1.

at $x = 0.1$ and, below 10 K, is accompanied by an increase in χ with decreasing temperature. For values of $x > 0.2$, $\chi(T)$ follows a Curie-Weiss law between $\sim 50\text{ K}$ and 300 K ; the effective magnetic moment μ_{eff} and Curie-Weiss temperature θ_p vary somewhat with x and have values $\mu_{eff} \approx 3.4\mu_B$ and $\theta_p \approx -40\text{ K}$ in the NFL regime $x \geq 0.8$. Since for Kondo systems, $|\theta_p| \approx 3 - 4 T_K$, this suggests a value $T_K \approx 10\text{ K}$, in reasonable agreement with values of T_K obtained from the scaling of the electrical resistivity and specific heat. At lower temperatures, the $\chi(T)$ data can be described by the relation $\chi(T) = \chi(0)(1 - c(T/T_K)^{1/2})$, with values of T_K in reasonable agreement with those obtained from $\rho(T)$ and $C(T)$ for $U_{1-x}Th_xPd_2Al_3$ (Fig. 9), along with the values determined from $\rho(T)$ and $C(T)$. We have also compared the $\chi(T)$ data to the two-channel spin 1/2 Kondo model result $\chi(T) \sim (-1/T_K)\ln(T/cT_K)$ where $c = 2.2$ ($T \ll T_K$). However, the fits are only qualitatively satisfactory and give values of T_K that have a different dependence on x than those obtained from $\rho(T)$ and $C(T)$.

4. THE $UCu_{5-x}Pd_x$ SYSTEM

The family of compounds $UCu_{5-x}Pd_x$ is unique among the uranium based intermetallics known to have NFL scaling properties as it is a concentrated moment system. All $x \leq 2.5$ share the common $AuIn_5$ structure, characterized by a periodic uranium lattice with two inequivalent copper sites.²⁹ The parent compound UCu_5 is a Kondo lattice antiferromagnet with Neel temperature $T_N = 15\text{ K}$ ³⁰ and a Kondo temperature of $\sim 10^2\text{ K}$, taken from the quasielastic linewidth in inelastic neutron scattering experiments.³¹ With Pd doping x , the AFM is quickly suppressed, van-

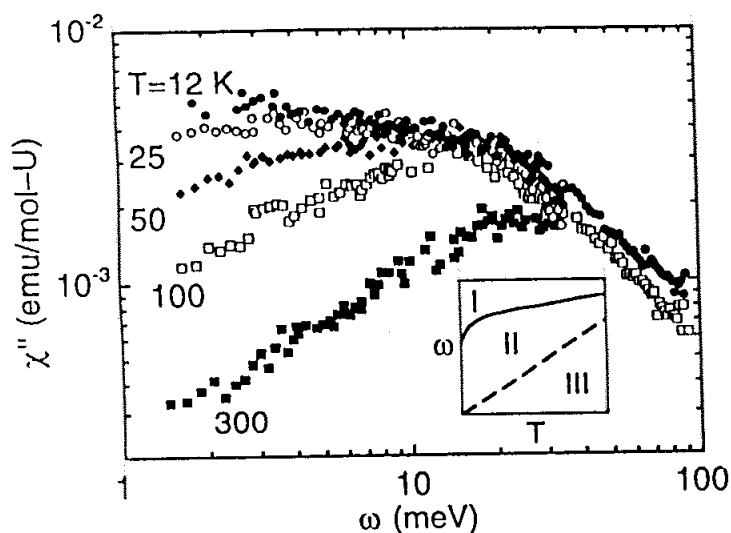


Fig. 15. $\chi''(\omega)$ for UCu_4Pd at constant temperatures ranging from 12 K to 300 K. Inset: three qualitatively different regimes are observed in the response: I. $\omega \geq \omega^*$: $\chi''(\omega, T) \sim (\omega/T_0) / [1 + (\omega/T_0)^2]$. II. $\omega \ll T$: $\chi''(\omega, T) \sim \omega/T^\eta$, $\eta = 1 \pm 1/3$. III. $\omega \gg T$: $\chi''(\omega, T) \sim \omega^{-1/3}$. Solid line: $\omega^*(T)$, dashed line: $\omega = T$. From Ref.³³

ishing for x between 0.5 and 1.^{29,32} A spin glass regime is observed for $x \geq 2$. The intermediate values $x = 1, 1.5$ display no long range order of any kind at the lowest temperatures, although thermal and transport measurements at temperatures below ~ 20 K reveal that both have remarkable temperature and magnetic field scaling.^{2,32} These NFL properties are similar to those found in the dilute moment systems like $\text{Y}_{0.8}\text{U}_{0.2}\text{Pd}_3$ described above, with the electrical resistivity $\rho(T) \sim 1 - a(T/T_0)$, the specific heat $C(T)/T \sim (-1/T_0) \ln(T/bT_0)$, and static magnetic susceptibility $\chi(T) \sim 1 - c(T/T_0)^{1/2}$ for both $\text{UCu}_{3.5}\text{Pd}_{1.5}$ and UCu_4Pd . These weak low temperature divergences suggest the existence of magnetic excitations with unusual scaling properties.

We have used neutron time of flight measurements³³ performed for energy transfers between 0.5 meV and 400 meV at temperatures from 10 K to 300 K to study the frequency/temperature scaling properties of these excitations. Although both systems display virtually identical temperature dependences in ρ , C , and χ , the nature of the magnetic excitations for $\text{UCu}_{3.5}\text{Pd}_{1.5}$ and UCu_4Pd are qualitatively different from those of $\text{Y}_{0.8}\text{U}_{0.2}\text{Pd}_3$.^{18,34} The uranium ions in the latter compound have a nonmagnetic ground state, and a magnetic response $S(\omega)$ consisting of two inelastic crystal field levels at ~ 5 meV and ~ 16 meV. In contrast, we have found a broad, quasielastic magnetic response $S(\omega)$ which is virtually identical for UCu_4Pd and $\text{UCu}_{3.5}\text{Pd}_{1.5}$, indicative of a magnetic ground state for the uranium ions, with

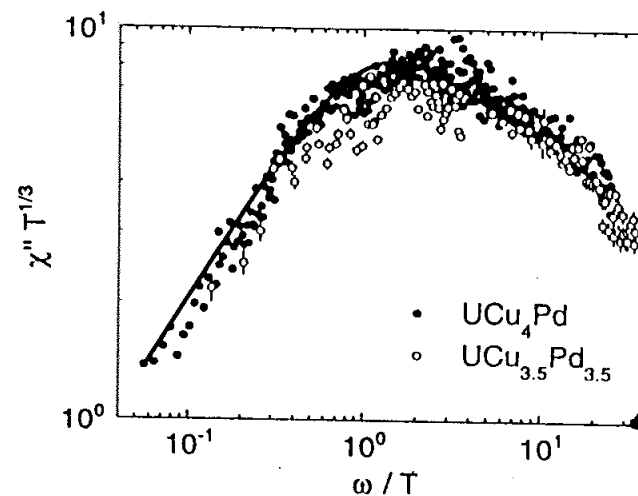


Fig. 16. $\chi''(\omega, T)T^{1/3}$ has almost identical universal scaling properties for UCu_4Pd (filled circles) and $\text{UCu}_{3.5}\text{Pd}_{1.5}$ (open circles). Data with energy transfers $\omega \geq 25$ meV are not included in this plot. Solid line: $\chi''(\omega, T)T^{1/3} \sim (T/\omega)^{1/3} \tanh(\omega/1.2T)$. From Ref.³³

no evidence for distinct crystal field excitations. Further, $S(\omega)$ displays no appreciable wavevector dependence beyond that of the $\text{U}^{3+}/\text{U}^{4+}$ magnetic form factor so in every case we have summed the magnetic response over experimental wavevectors.

The detailed frequency and temperature dependences of the dynamical susceptibilities $\chi(\omega, T)$ of $\text{UCu}_{5-x}\text{Pd}_x$ ($x = 1, 1.5$) are obtained from $S(\omega, T)$ by

$$S(\omega) = (n(\omega) + 1)\chi''(\omega, T) \quad (5)$$

where $n(\omega) + 1$ is the thermal occupation factor. The resulting $\chi''(\omega, T)$ is detailed for UCu_4Pd in Fig. 15. As schematically indicated in the inset, there are three qualitatively different regimes of behavior. At every temperature, a quasi-Lorentzian regime is found for energy transfers $\omega \geq \omega^* \approx 25$ meV. Here, $\chi''(\omega, T) = \chi_{Lor}(\omega/\Gamma) / (1 + (\omega/\Gamma)^2)$ has a weak temperature dependence stemming from that of χ_{Lor} and Γ . For $\omega < \omega^*$, $\chi''(\omega, T)$ is well described by a universal scaling relation

$$\chi''(\omega, T)T^{1/3} = (T/\omega)^{1/3} Z(\omega/T) \quad (6)$$

demonstrated in Fig. 16 for both UCu_4Pd and $\text{UCu}_{3.5}\text{Pd}_{1.5}$. While our choice may not be unique, it is clear from Fig. 16 that $Z \sim \tanh(\omega/1.2T)$ fits the data very well. $Z \sim 1/(n(\omega) + 1)$ is another intriguing possibility, although this scaling function fails for $T > \omega^*$.

The scaling behavior found for $\omega < \omega^*$ represents a qualitatively new type of magnetic response for an f-electron based system. It is interesting to investigate

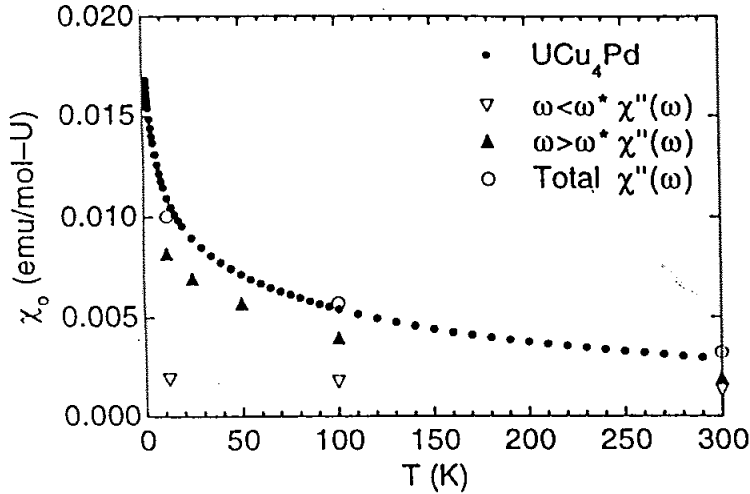


Fig. 17. A Comparison of the measured static susceptibility $\chi(T)$ to that calculated from the measured dynamical susceptibility (see text) for energy transfers larger (filled triangles) and smaller (open triangles) than $\omega^* = 25$ meV. Integrating over the total response for $1 \text{ meV} \leq \omega \leq 200 \text{ meV}$ (open circles) accounts for virtually the entire measured $\chi(T)$.

how these unusual excitations are reflected in the temperature dependences of static properties, in particular, the static susceptibility $\chi(T)$. A Kramers-Kronig relation links $\chi''(\omega, T)$ and $\chi(T)$:

$$\chi(T) = \frac{2}{\pi} \int_0^{\infty} d\omega \frac{\chi''(\omega, T)}{\omega} = \int_0^{\omega^*} d\omega \frac{\omega^{-1/3} Z(\omega/T)}{\omega} + \int_{\omega^*}^{\infty} d\omega \frac{\chi_{Lor} \omega / \Gamma}{\omega(1 + (\omega/\Gamma)^2)}. \quad (7)$$

That is, both the NFL like excitations for $\omega < \omega^*$ and the higher energy localized magnetic excitations contribute, in principle, to the temperature dependence of the measured $\chi(T)$. We have performed numerical integrations over both of the terms appearing in Eq. (7) to determine the relative magnitudes of the two contributions in UCu_4Pd , depicted in Fig. 17.

The high energy, localized moment excitations ($\omega > \omega^*$) make a Curie-Weiss like contribution to χ_0 , which is almost temperature independent for $T < 300$ K. The temperature dependence of $\chi(T)$ is consequently dominated for $85 \text{ K} \leq T \leq 300 \text{ K}$ by the low energy excitations ($\omega < \omega^*$), and reflects their unusual scaling properties. As demonstrated in Fig. 17, the sum of these two terms agrees very well with the measured static susceptibility $\chi(T)$, indicating that relatively little of the magnetic response falls outside our experimental energy window, $1 \text{ meV} \leq \omega \leq$

200 meV. However, extending this window to lower energy transfers is imperative to establish whether the non Fermi liquid scaling properties of the excitations we have observed correspond to true critical scattering related to a $T = 0$ K phase transition or, alternatively, represent an intermediate temperature/frequency crossover regime preceding the actual critical regime.

5. CONCLUDING REMARKS

It is apparent that NFL behavior in f-electron systems is a general phenomenon. Low temperature NFL characteristics have been identified in the physical properties of nearly ten f-electron systems. With a few possible exceptions (e.g., UBe_{13} ³⁵), all of the examples of NFL behavior in f-electron systems are found in alloy systems. The main result of the alloying process seems to be to "tune" the system into the NFL regime, although the alloying also introduces disorder into the system, which may also play an important role. The NFL behavior is found in two types of systems: (1) Systems containing small concentrations of rare earth and actinide ions with partially-filled f-electron shells, where the NFL behavior appears to be a single ion effect. Examples of this type of system include $\text{M}_{1-x}\text{U}_x\text{Pd}_3$ ($\text{M} = \text{Sc}, \text{Y}$), $\text{Th}_{1-x}\text{U}_x\text{Ru}_2\text{Si}_2$,³⁶ $\text{La}_{0.9}\text{Ce}_{0.1}\text{Cu}_2\text{Si}_2$,³⁷ and $\text{U}_{1-x}\text{Th}_x\text{Pd}_2\text{Al}_3$ for small U concentrations. (2) Systems containing large concentrations of rare earth or actinide ions with partially-filled f-electron shells, which sometimes form an ordered sublattice, where the NFL behavior appears to be due to interactions between the ions. Examples of this type of system include $\text{CeCu}_{5.9}\text{Au}_{0.1}$,³⁸ and $\text{UCu}_{3.5}\text{Pd}_{1.5}$.³² In the $\text{CeCu}_{5-x}\text{Au}_x$ system, the NFL regime exists in a narrow range of x-values between a nonmagnetic heavy fermion ground state at $x = 0$ and an antiferromagnetically ordered state at $x = 0.2$.

Many of the f-electron systems in which NFL behavior is found exhibit the Kondo effect as evidenced by an increase of the electrical resistivity with decreasing temperature and a magnetic susceptibility χ at high temperatures ($T \gg T_K$) that follows a Curie-Weiss law with a negative Curie-Weiss temperature $|\theta_p| \approx (3-4 T_K)$. In the cases where T_K can be estimated from the $\ln T$ behavior of the electrical resistivity or the Curie-Weiss temperature, the NFL behavior occurs at temperatures much less than T_K . The NFL behavior is manifested in the temperature dependences of the electrical resistivity, specific heat, and magnetic susceptibility for $T \ll T_K$: $\rho(T) \sim 1 - aT/T_K$ where a can be > 0 (usual Kondo effect) or < 0 , $C(T)/T \sim (-1/T_K) \ln(T/bT_K)$, and $\chi(T) \sim 1 - c(T/T_K)^{1/2}$, where $|a|$, b , and c are constants of the order of unity. These low temperature properties scale with T_K where T_K is comparable to the value determined from the high temperature Kondo behavior when $a > 0$. This is summarized in Table 2, which is an updated version of a table we first presented in reference 2. However, these temperature dependences of ρ , C , and χ have also been observed in f-electron systems in which a Kondo effect has not been clearly identified. Therefore, we refer to a characteristic temperature T_0 that is equal to T_K in the systems where the Kondo effect is operative. The two new entries are for $\text{M}_{0.1}\text{U}_{0.9}\text{Ni}_2\text{Al}_3$ ³⁹ ($\text{M} = \text{Pr}, \text{Th}$) and $\text{Ce}_{1-x}\text{Th}_x\text{RhSb}$.⁴⁰ Materials conforming to these temperature dependences are indicated by "yes" and the exceptions by an entry describing the behavior, or a "dash" where the behavior has not yet been established. As we stated in reference 2, taken of face value,

Table 2. Examples of f-electron systems which exhibit characteristic non Fermi liquid behavior in the low temperature electrical resistivity $\rho(T) \sim 1 - aT/T_0$, specific heat $C(T)/T \sim (-1/T_0) \ln(T/bT_0)$, and magnetic susceptibility $\chi(T) \sim 1 - c(T/T_0)^{1/2}$.

System	ρ	C/T	χ	T_0^* (K)
$\text{La}_{0.9}\text{Ce}_{0.1}\text{Cu}_2\text{Si}_2$	yes	yes	—	9
$\text{M}_{1-x}\text{U}_x\text{Pd}_3$ (M = Sc, Y)	yes	yes	yes	40-220
$\text{UCu}_{3.5}\text{Pd}_{1.5}$	yes	yes	yes	28
$\text{U}_{1-x}\text{Th}_x\text{Pd}_2\text{Al}_3$	yes	yes	yes	20
$\text{M}_{0.1}\text{U}_{0.9}\text{Ni}_2\text{Al}_3$ (M = Pr, Th)	—	yes	yes	200
$\text{Ce}_{1-x}\text{Th}_x\text{RhSb}$	—	yes	—	33
$\text{Th}_{1-x}\text{U}_x\text{Ru}_2\text{Si}_2$	($a < 0$)	yes	$-\ln(T/bT_K)$	11
$\text{U}_{0.9}\text{Th}_{0.1}\text{Be}_{13}$	($a < 0$)	yes	yes	8
$\text{CeCu}_{5.9}\text{Au}_{0.1}$	($a < 0$)	yes	yes	3.5

* Deduced from the slope $A = d(C/T)/dT$ of the logarithmic divergence in the specific heat: $T_0 = -0.251R/A$

the results presented in Table 2 suggest that the low temperature behavior of the electrical resistivity, specific heat, and magnetic susceptibility of f-electron systems that exhibit NFL behavior have some common characteristics, irrespective of the microscopic mechanisms responsible for the NFL behavior.

Since many examples of NFL behavior are found in f-electron systems that exhibit the Kondo effect, the multichannel Kondo model would be expected to provide an explanation since it predicts that the physical properties have NFL characteristics at low temperatures $T \ll T_K$. The two-channel spin 1/2 Kondo model does, in fact, give $C(T)/T \sim (-1/T_K) \ln(T/bT_K)$, which agrees with experiment, but predicts that $\rho(T) \sim 1 - a(T/T_K)^{1/2}$ and $\chi(T) \sim (-1/T_K) \ln(T/cT_K)$, in disagreement with experiment. The quadrupolar Kondo model, which maps onto the two channel spin 1/2 Kondo model, can account for the $1 - c(T/T_K)^{1/2}$ dependence of the magnetic susceptibility at low temperature. For a magnetic two channel spin 1/2 Kondo effect, the magnetic susceptibility is also found to diverge logarithmically at $T = 0$, while for a two channel quadrupolar Kondo effect, it is the electric quadrupolar susceptibility that diverges logarithmically. The quadrupolar susceptibility can be extracted from ultrasound measurements. For the quadrupolar Kondo effect, the magnetic susceptibility is van Vleck in character, resulting from coupling of the Γ_3 ground state to the Γ_5 and Γ_4 magnetic excited states.³⁵ Cox and Makivic have estimated that $\chi(T)$ should vary like $\chi(T) = \chi(0)(1 - c(T/T_K)^{1/2})$ at low temperatures, where $\chi(0)$ is of the order of the van Vleck susceptibility and the coefficient $c \approx 1$.⁴¹ As we have discussed in Section 2, this seems to be the case for $\text{Y}_{1-x}\text{U}_x\text{Pd}_3$ where the ground state of the U^{4+} ions in the cubic CEF appears to be a Γ_3 nonmagnetic doublet. However, a quadrupolar Kondo effect would not be expected to be appropriate for all of the other f-electron systems which exhibit NFL behavior. Furthermore, the quadrupolar Kondo model cannot account for the linear temperature dependence of the electrical resistivity. One system that does appear to satisfy the predictions of the quadrupolar Kondo model for $\rho(T)$, $C(T)$, and $\chi(T)$, is $\text{U}_{0.9}\text{Th}_{0.1}\text{Be}_{13}$, according to recent measurements by Aliev *et al.*,⁴²

although in this case the coefficient a that appears in the resistivity is negative. It will be interesting to see whether U is tetravalent in $\text{U}_{0.9}\text{Th}_{0.1}\text{Be}_{13}$ and has a nonmagnetic Γ_3 doublet ground state in the cubic CEF.

Andraka and Tsvetlik⁴³ have raised several objections to the multichannel Kondo interpretation of the NFL behavior in $\text{Y}_{1-x}\text{U}_x\text{Pd}_3$ and other f-electron systems. One of these objections is based on specific heat measurements on $\text{Y}_{0.8}\text{U}_{0.2}\text{Pd}_3$ where they find that the specific heat scales as $C(H, T)/T = C(0, T)/T = -f(H/T^\beta)$ with $\beta = 1.3 \pm 0.1$. They argue that a scaling dimension β greater than one precludes a single site interpretation of this phenomenon. Moreover, it has been noted⁴⁴ that scaling of the magnetic field for a two channel spin 1/2 Kondo effect has predicted scaling dimensions of 1/2 for the magnetic case¹² and 1/4 for the nonmagnetic (quadrupolar) case,⁴⁵ well outside the experimental uncertainty of β . A phenomenological theory for the NFL behavior of f-electron systems such as $\text{Y}_{0.8}\text{U}_{0.2}\text{Pd}_3$ and $\text{UCu}_{3.5}\text{Pd}_{1.5}$ has been proposed by Tsvetlik and Reizer.⁴⁶ According to this theory, the alloys have a critical point at $T = 0$ K so that their low temperature thermodynamics is determined by collective modes corresponding to fluctuations in the order parameter in the vicinity of a critical point, rather than single particle fermion excitations, as in a Fermi liquid. This scenario would seem to be applicable to the $\text{CeCu}_{5.9}\text{Au}_{0.1}$ system, mentioned above. However, we caution that the scaling exponents deduced from experiment so far lack internal consistency within the context of this particular theory. Nonetheless, the NFL behavior in systems such as $\text{Y}_{1-x}\text{U}_x\text{Pd}_3$ and $\text{U}_{1-x}\text{Th}_x\text{Pd}_2\text{Al}_3$, which definitely do exhibit Kondo like features in $\rho(T)$ and $\chi(T)$ at high temperatures $T \lesssim T_K$, persists into the dilute U concentration limit, suggesting that a single site mechanism such as a multichannel Kondo effect is operative.

ACKNOWLEDGMENTS

We thank our many collaborators for their contributions to this work. Research at UCSD was supported by the U.S. NSF under Grant No. DMR-9107698 and the U.S. DOE under Grant No. DE-FG03-86ER45230. Some equipment used in this research was provided by the Center for Interface and Materials Science and funded by the W. A. Keck Foundation. Work at Los Alamos and Argonne was carried out under the auspices of the U.S. DOE, Office of Basic Energy Sciences, the latter under Contract No. W-31-109-ENG-38. J. H. acknowledges financial support from the German Academic Exchange Service. M. C. de A. acknowledges financial support from CNPq, Brazil. M.C.A. is grateful to the Phoenix Memorial Project, University of Michigan, for travel support.

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