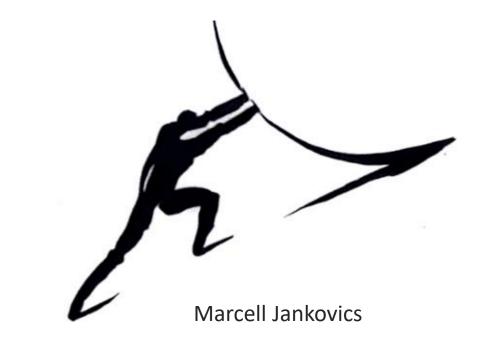
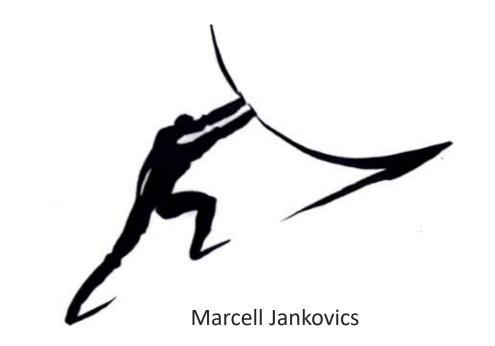
Cooling stuff Doppler molasses Sisyphus and related evaporation expansion Sideband cooling Cooling stuff Doppler molasses Sisyphus and related evaporation expansion Sideband cooling



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Sisyphus and related

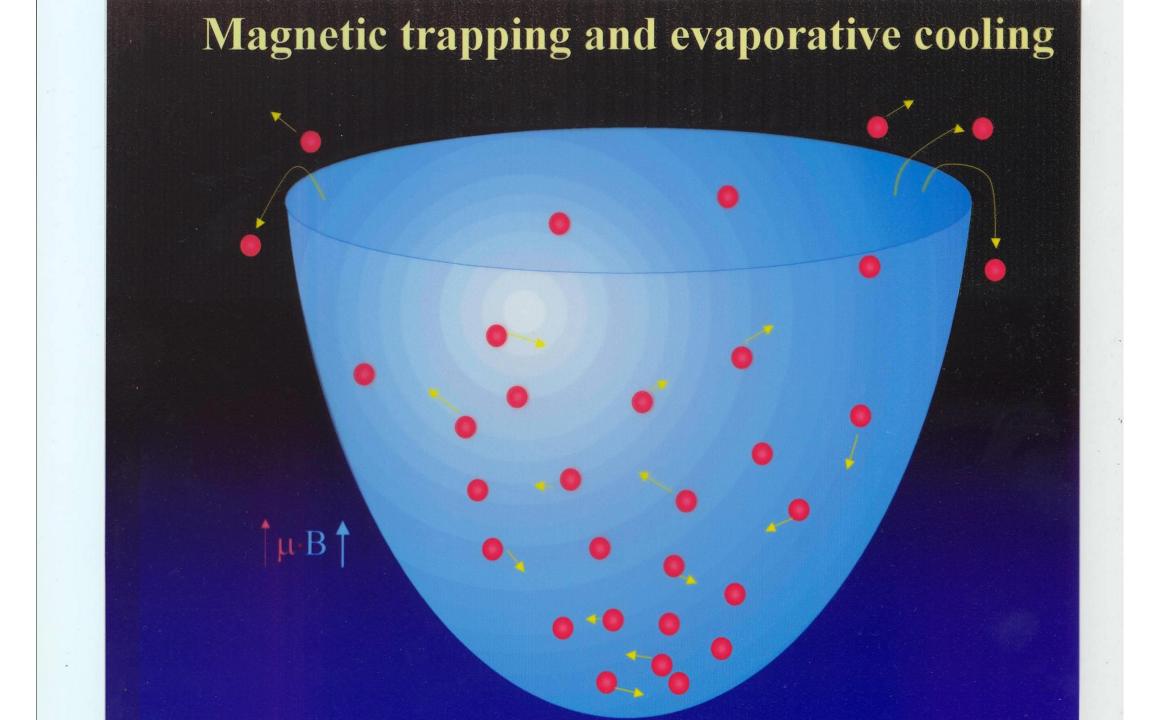
Sisyphus and related

Sisyphus and related velocity and B-field limits.

Cooling efficiency. The Carnot limit

Black-body radiation and molecules

Can we do optical cooling to degeneracy?



Evaporation.

Good, but large in volume, complicated, expensive, slow. Can we make BEC small, cheap, fast? Evaporation.

Good, but large in volume, complicated, expensive, slow. Can we make BEC small, cheap, fast?

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Good, but large in volume, complicated, expensive, slow. Can we make BEC small, cheap, fast?

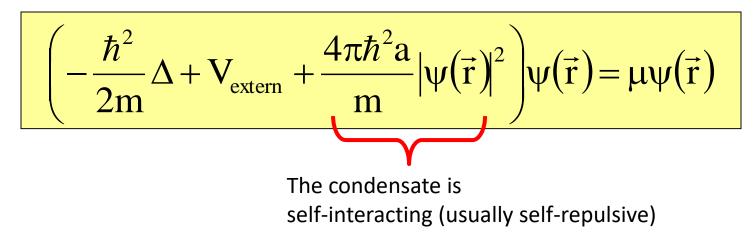
Tweezers!

many-body Schroedinger Equation. The GPE mean-field solution.

QM: Particle described by Schrödinger equation

$$\left(-\frac{\hbar^2}{2m}\Delta + V_{\text{extern}}\right)\psi(\vec{r}) = E\psi(\vec{r})$$

BEC: many weakly interacting particles → Gross-Pitaevskii equation

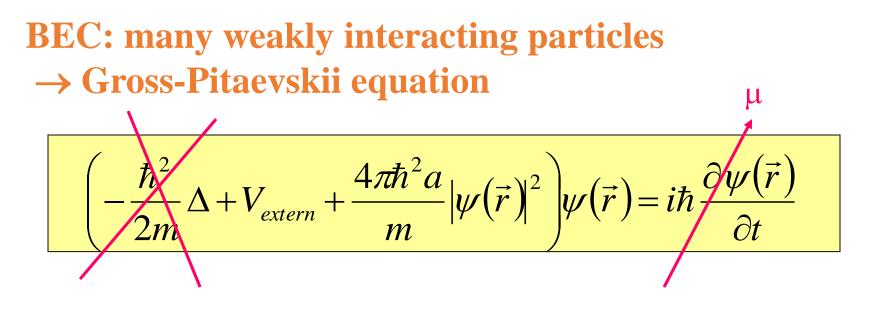


BEC: many weakly interacting particles → Gross-Pitaevskii equation

$$\left(-\frac{\hbar^2}{2m}\Delta + V_{extern} + \frac{4\pi\hbar^2 a}{m} |\psi(\vec{r})|^2\right) \psi(\vec{r}) = i\hbar \frac{\partial \psi(\vec{r})}{\partial t}$$

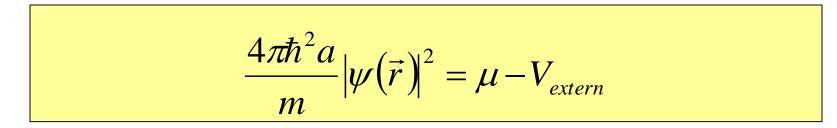
Can be solved in various approximations.

The Thomas-Fermi approximation: ignore KE term, look for stationary states



Can be solved in various approximations.

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The Thomas-Fermi approximation: ignore KE term, look for stationary states

$$\frac{4\pi\hbar^2 a}{m} |\psi(\vec{r})|^2 = \mu - V_{extern}$$
V(x)

Self-interacting condensate expands to fill confining potential to height $\boldsymbol{\mu}$

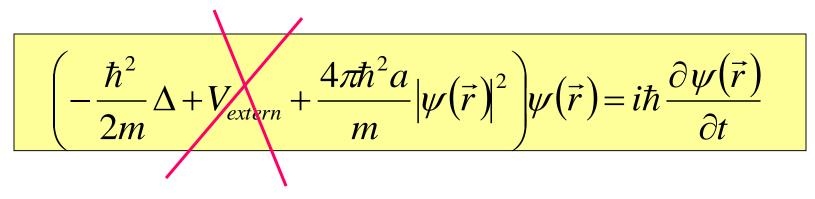
BEC: many weakly interacting particles → Gross-Pitaevskii equation

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Can be solved in various approximations.

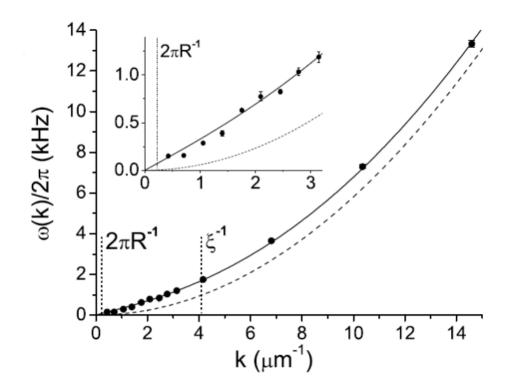
Ignore external potential, look for plane-wave excitations

BEC: many weakly interacting particles → Gross-Pitaevskii equation



Can be solved in various approximations.

Ignore external potential, look for plane-wave excitations



speed of sound:

 $c = (\mu/m)^{1/2}$

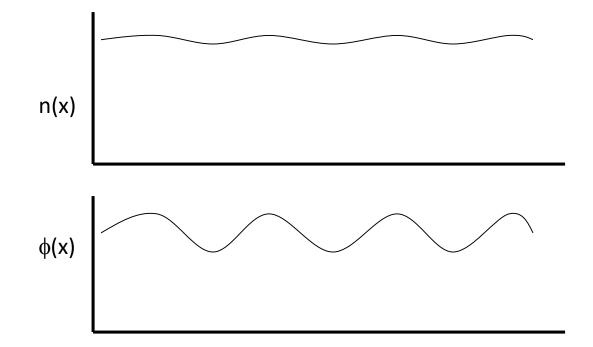
Healing length:

 $\xi = (hbar^2 / m \mu)^{1/2}$

Chemical potential:

 μ = 4 π hbar² a n /m

Data from Nir Davidson



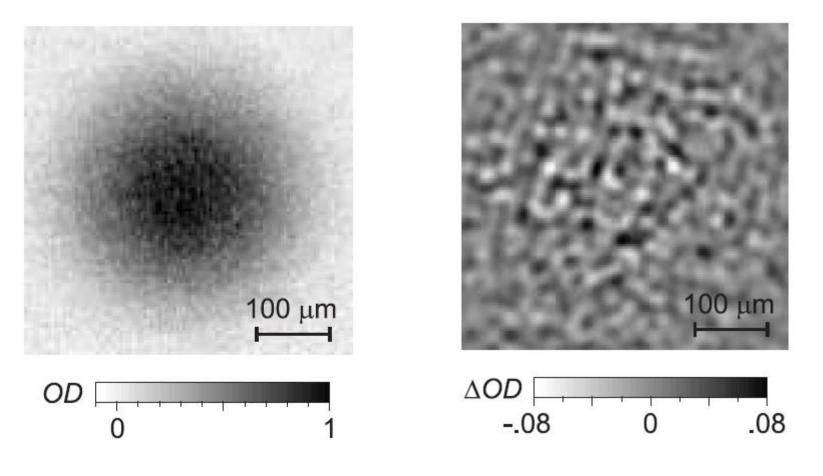
Long wavelength excitations (k << 1/ξ)

relatively little density fluctuation, large phase fluctuation (which we can't directly image). coherent breathing

limits to GPE

fluctuations at low d finite T damping T ~ Tc na³ > 1/4pi discrete-atom density fluctuations

Atom shot noise limited imaging



Data from lab of Debbie Jin.

limits to GPE

fluctuations at low d finite T damping T ~ Tc na³ > 1/4pi (for na³ < ¼ pi, perturbative corrections exist) discrete-atom density fluctuations

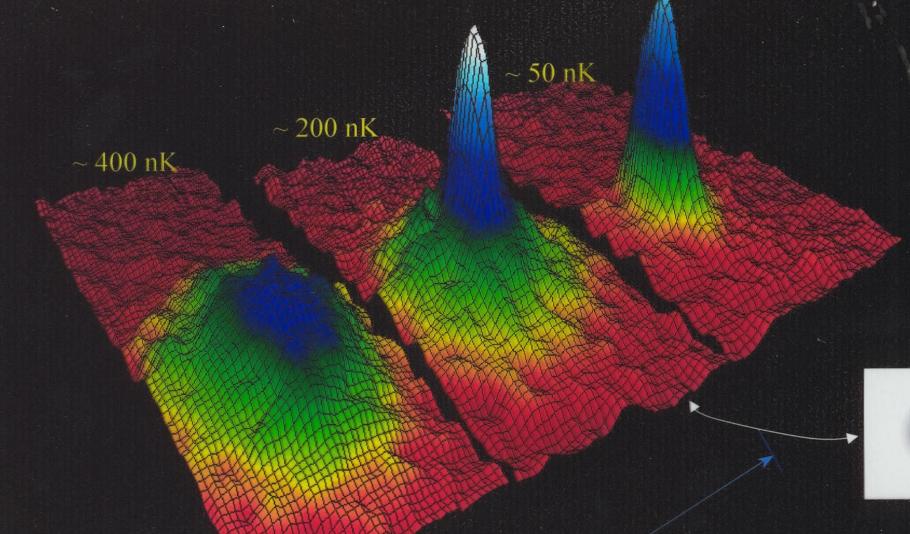
Hard to study strong interactions in atomic BEC, because of 3-body recombination. But for "s=1/2" fermions, yes, possible. limits to GPE

fluctuations at low d finite T damping T ~ Tc na³ > 1/4pi (for na³ < ¼ pi, perturbative corrections exist) discrete-atom density fluctuations

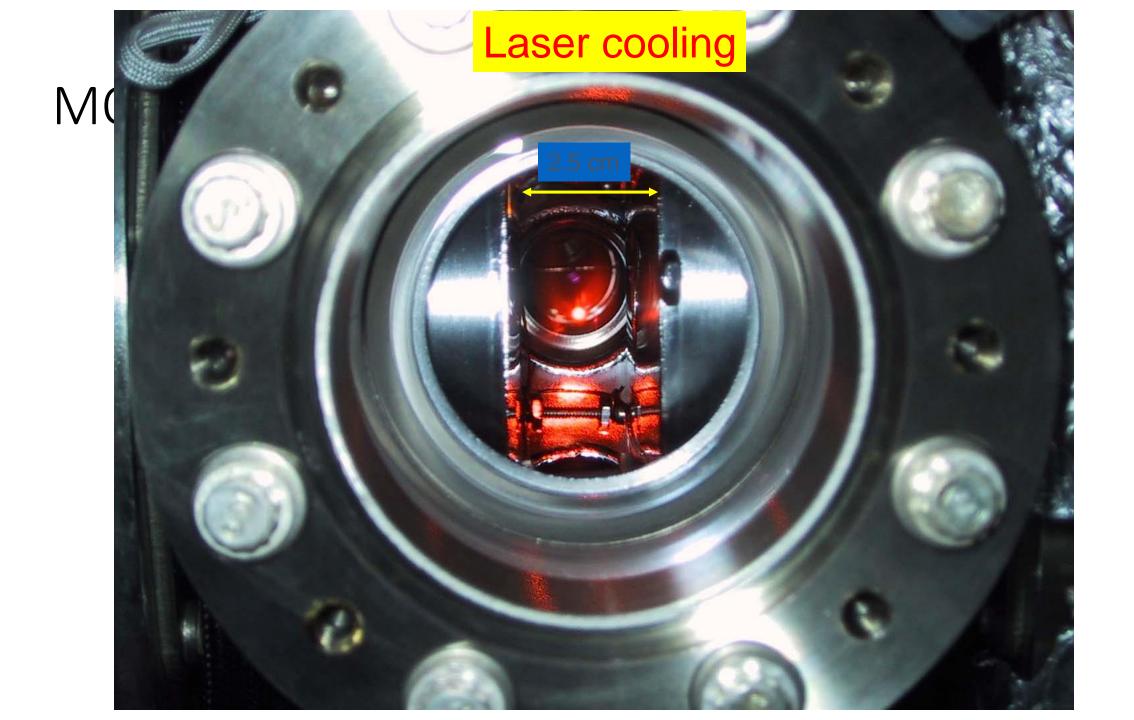
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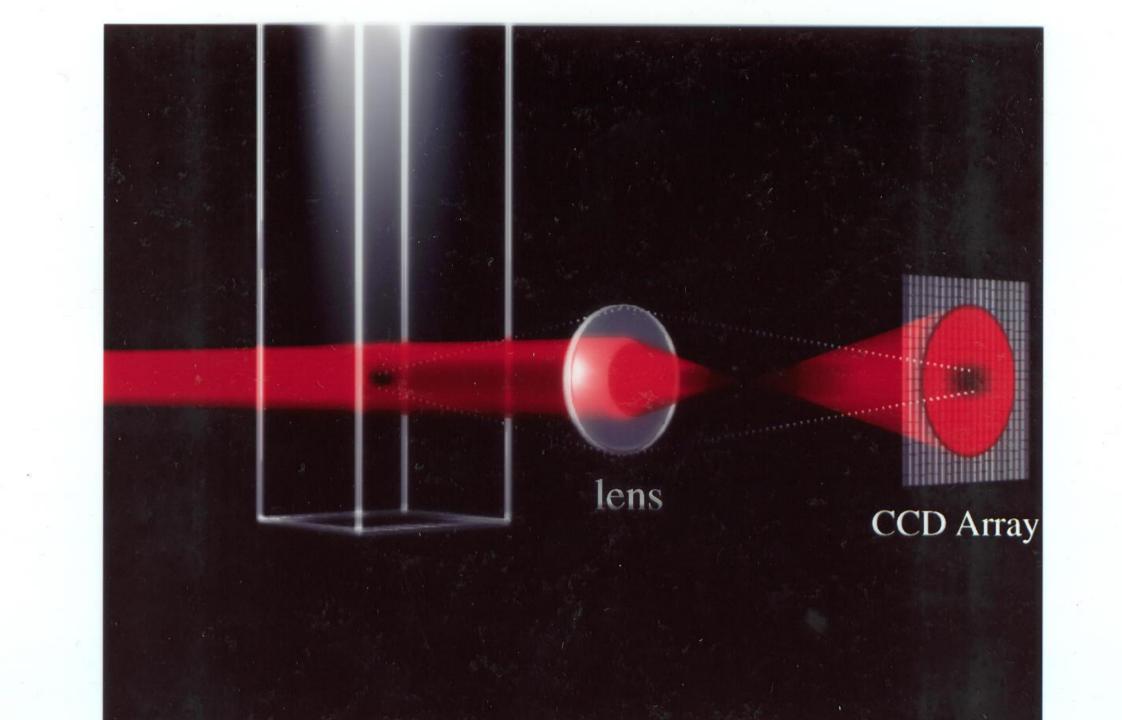
cf work of Deborah Jin 1967-2016.

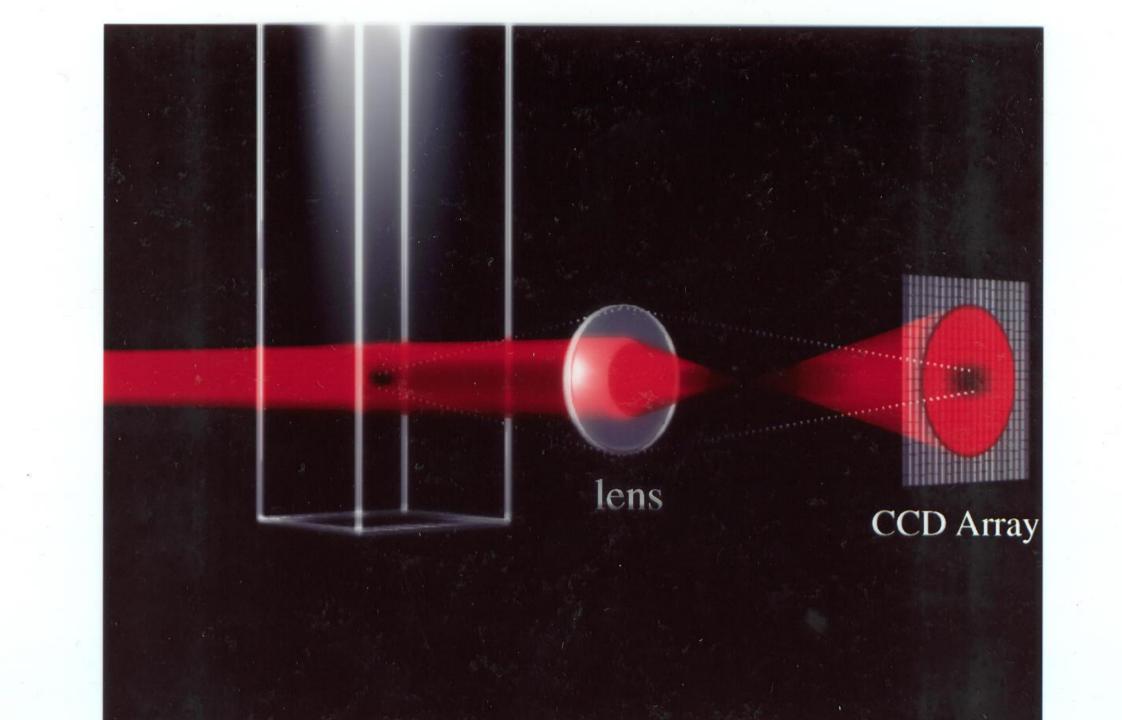
2 D velocity/density distributions

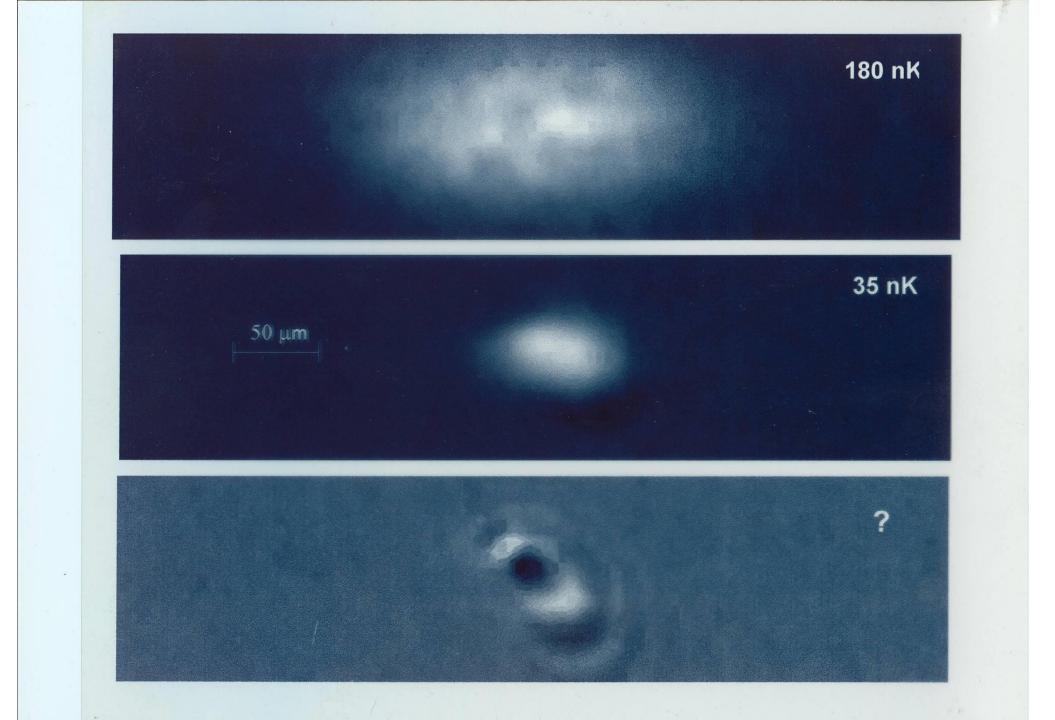


0.2 mm



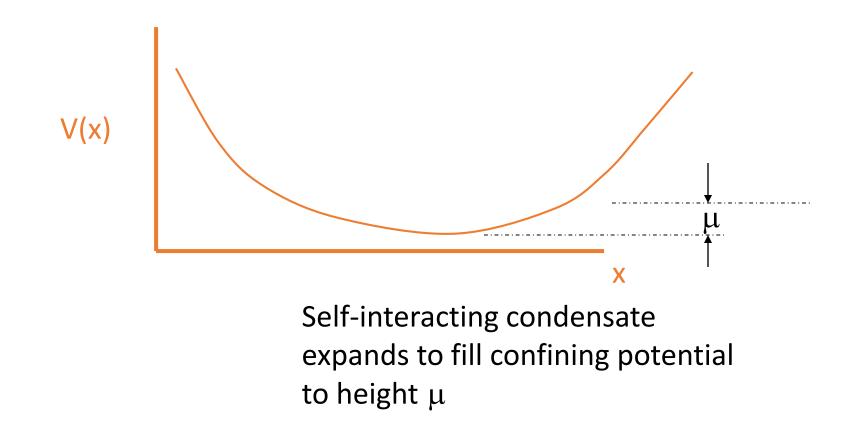


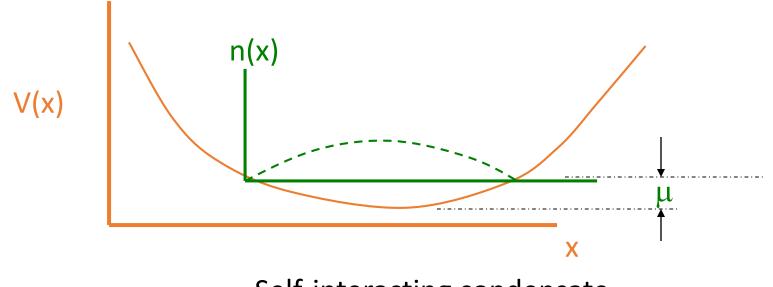




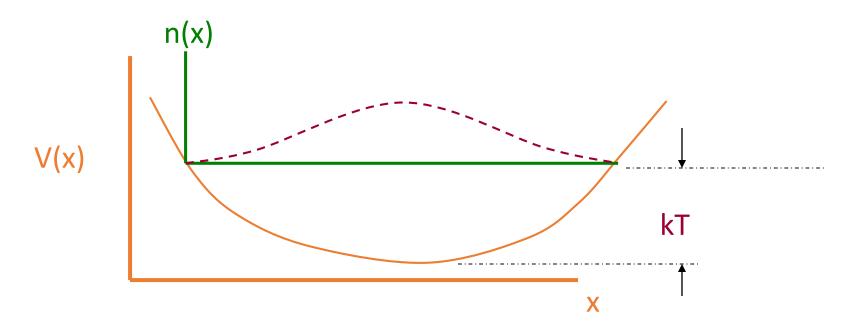
Turn magnetic trap off

atoms fly apart

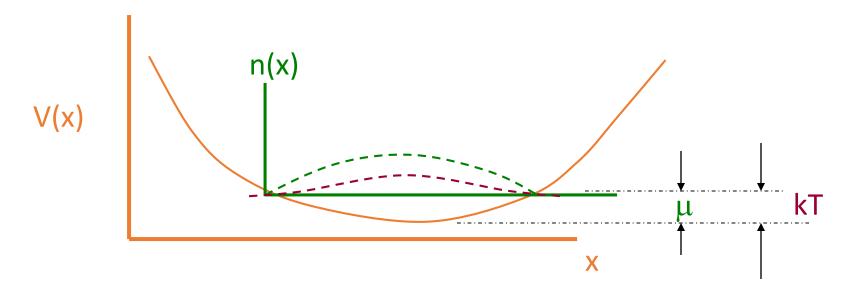




Self-interacting condensate expands to fill confining potential to height $\boldsymbol{\mu}$

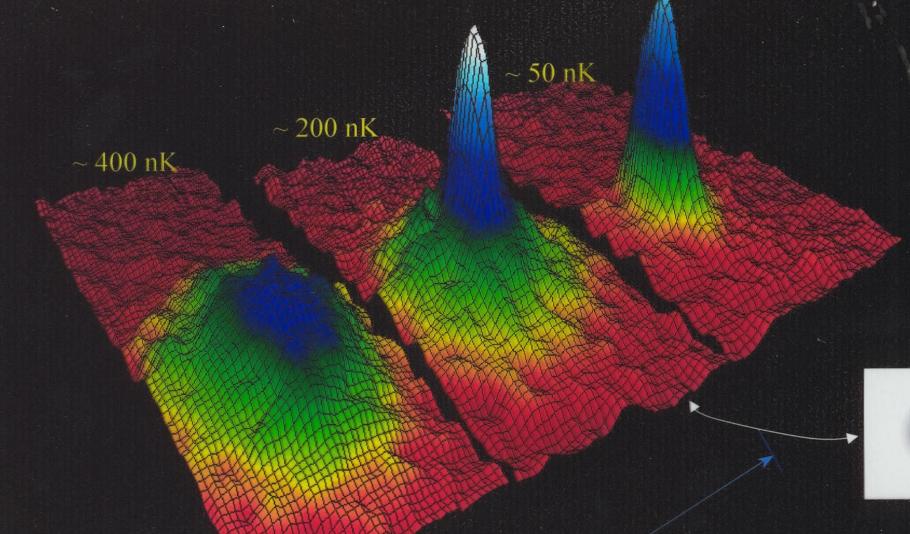


Cloud of thermal excitations made up of atoms on trajectories that go roughly to where the confining potential reaches kT



When $kT < \mu$ then there are very few thermal excitations extending outside of condensate. Thus evaporation cooling power is small.

2 D velocity/density distributions



0.2 mm

