

# Physics of iron-based high temperature superconductors (I)

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# Superconducting Elements

NIST

Technology Administration, U.S. Department of Commerce  
Standards and Technology

Group	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
IA	IIA	IIIB	IVB	VB	VIB	VII	VIII	VIII	VIII	IB	IIB	IIIA	IVA	VA	VIA	VIIA	VIIIA	
1	<b>H</b> Hydrogen 1.00794 1s																	<b>He</b> Helium 4.002602 1s <sup>2</sup>
2	<b>Li</b> Lithium 6.941 1s <sup>2</sup> 2s <sup>1</sup>	<b>Be</b> Beryllium 9.012182 1s <sup>2</sup> 2s <sup>2</sup>											<b>B</b> Boron 10.811 1s <sup>2</sup> 2s <sup>2</sup> 2p <sup>1</sup>	<b>C</b> Carbon 12.0107 1s <sup>2</sup> 2s <sup>2</sup> 2p <sup>2</sup>	<b>N</b> Nitrogen 14.0067 1s <sup>2</sup> 2s <sup>2</sup> 2p <sup>3</sup>	<b>O</b> Oxygen 15.9994 1s <sup>2</sup> 2s <sup>2</sup> 2p <sup>4</sup>	<b>F</b> Fluorine 18.9984032 1s <sup>2</sup> 2s <sup>2</sup> 2p <sup>5</sup>	<b>Ne</b> Neon 20.1797 1s <sup>2</sup> 2s <sup>2</sup> 2p <sup>6</sup>
3	<b>Na</b> Sodium 22.989770 [Ne]3s <sup>1</sup>	<b>Mg</b> Magnesium 24.3050 [Ne]3s <sup>2</sup>											<b>Al</b> Aluminum 26.9815386 [Ne]3s <sup>2</sup> 3p <sup>1</sup>	<b>Si</b> Silicon 28.0855 [Ne]3s <sup>2</sup> 3p <sup>2</sup>	<b>P</b> Phosphorus 30.973762 [Ne]3s <sup>2</sup> 3p <sup>3</sup>	<b>S</b> Sulfur 32.065 [Ne]3s <sup>2</sup> 3p <sup>4</sup>	<b>Cl</b> Chlorine 35.453 [Ne]3s <sup>2</sup> 3p <sup>5</sup>	<b>Ar</b> Argon 39.948 [Ne]3s <sup>2</sup> 3p <sup>6</sup>
4	<b>K</b> Potassium 39.0983 [Ar]4s <sup>1</sup>	<b>Ca</b> Calcium 40.078 [Ar]4s <sup>2</sup>	<b>Sc</b> Scandium 44.955910 [Ar]3d <sup>1</sup> 4s <sup>2</sup>	<b>Ti</b> Titanium 47.867 [Ar]3d <sup>2</sup> 4s <sup>2</sup>	<b>V</b> Vanadium 50.9415 [Ar]3d <sup>3</sup> 4s <sup>2</sup>	<b>Cr</b> Chromium 51.9961 [Ar]3d <sup>5</sup> 4s <sup>1</sup>	<b>Mn</b> Manganese 54.938044 [Ar]3d <sup>5</sup> 4s <sup>2</sup>	<b>Fe</b> Iron 55.845 [Ar]3d <sup>6</sup> 4s <sup>2</sup>	<b>Co</b> Cobalt 58.933200 [Ar]3d <sup>7</sup> 4s <sup>2</sup>	<b>Ni</b> Nickel 58.6934 [Ar]3d <sup>8</sup> 4s <sup>2</sup>	<b>Cu</b> Copper 63.546 [Ar]3d <sup>10</sup> 4s <sup>1</sup>	<b>Zn</b> Zinc 65.409 [Ar]3d <sup>10</sup> 4s <sup>2</sup>	<b>Ga</b> Gallium 69.723 [Ar]3d <sup>10</sup> 4s <sup>2</sup> 4p <sup>1</sup>	<b>Ge</b> Germanium 72.64 [Ar]3d <sup>10</sup> 4s <sup>2</sup> 4p <sup>2</sup>	<b>As</b> Arsenic 74.92160 [Ar]3d <sup>10</sup> 4s <sup>2</sup> 4p <sup>3</sup>	<b>Se</b> Selenium 78.956 [Ar]3d <sup>10</sup> 4s <sup>2</sup> 4p <sup>4</sup>	<b>Br</b> Bromine 79.904 [Ar]3d <sup>10</sup> 4s <sup>2</sup> 4p <sup>5</sup>	<b>Kr</b> Krypton 83.798 [Ar]3d <sup>10</sup> 4s <sup>2</sup> 4p <sup>6</sup>
5	<b>Rb</b> Rubidium 85.4678 [Kr]5s <sup>1</sup>	<b>Sr</b> Strontium 87.62 [Kr]5s <sup>2</sup>	<b>Y</b> Yttrium 88.90585 [Kr]4d <sup>1</sup> 5s <sup>2</sup>	<b>Zr</b> Zirconium 91.224 [Kr]4d <sup>2</sup> 5s <sup>2</sup>	<b>Nb</b> Niobium 92.90638 [Kr]4d <sup>4</sup> 5s <sup>1</sup>	<b>Mo</b> Molybdenum 95.94 [Kr]4d <sup>5</sup> 5s <sup>1</sup>	<b>Tc</b> Technetium (98) [Kr]4d <sup>5</sup> 5s <sup>2</sup>	<b>Ru</b> Ruthenium 101.07 [Kr]4d <sup>7</sup> 5s <sup>1</sup>	<b>Rh</b> Rhodium 102.90550 [Kr]4d <sup>8</sup> 5s <sup>1</sup>	<b>Pd</b> Palladium 106.42 [Kr]4d <sup>10</sup> 5s <sup>0</sup>	<b>Ag</b> Silver 107.8682 [Kr]4d <sup>10</sup> 5s <sup>1</sup>	<b>Cd</b> Cadmium 112.411 [Kr]4d <sup>10</sup> 5s <sup>2</sup>	<b>In</b> Indium 114.818 [Kr]4d <sup>10</sup> 5s <sup>2</sup> 5p <sup>1</sup>	<b>Sn</b> Tin 118.710 [Kr]4d <sup>10</sup> 5s <sup>2</sup> 5p <sup>2</sup>	<b>Sb</b> Antimony 121.760 [Kr]4d <sup>10</sup> 5s <sup>2</sup> 5p <sup>3</sup>	<b>Te</b> Tellurium 127.60 [Kr]4d <sup>10</sup> 5s <sup>2</sup> 5p <sup>4</sup>	<b>I</b> Iodine 126.90447 [Kr]4d <sup>10</sup> 5s <sup>2</sup> 5p <sup>5</sup>	<b>Xe</b> Xenon 131.29 [Kr]4d <sup>10</sup> 5s <sup>2</sup> 5p <sup>6</sup>
6	<b>Cs</b> Cesium 132.90545 [Xe]6s <sup>1</sup>	<b>Ba</b> Barium 137.327 [Xe]6s <sup>2</sup>		<b>Hf</b> Hafnium 178.49 [Xe]4f <sup>14</sup> 5d <sup>2</sup> 6s <sup>2</sup>	<b>Ta</b> Tantalum 180.9479 [Xe]4f <sup>14</sup> 5d <sup>3</sup> 6s <sup>2</sup>	<b>W</b> Tungsten 183.84 [Xe]4f <sup>14</sup> 5d <sup>4</sup> 6s <sup>2</sup>	<b>Re</b> Rhenium 186.207 [Xe]4f <sup>14</sup> 5d <sup>5</sup> 6s <sup>2</sup>	<b>Os</b> Osmium 190.23 [Xe]4f <sup>14</sup> 5d <sup>6</sup> 6s <sup>2</sup>	<b>Ir</b> Iridium 192.217 [Xe]4f <sup>14</sup> 5d <sup>7</sup> 6s <sup>2</sup>	<b>Pt</b> Platinum 195.078 [Xe]4f <sup>14</sup> 5d <sup>9</sup> 6s <sup>1</sup>	<b>Au</b> Gold 196.96655 [Xe]4f <sup>14</sup> 5d <sup>10</sup> 6s <sup>1</sup>	<b>Hg</b> Mercury 200.59 [Xe]4f <sup>14</sup> 5d <sup>10</sup> 6s <sup>2</sup>	<b>Tl</b> Thallium 204.3833 [Xe]4f <sup>14</sup> 5d <sup>10</sup> 6s <sup>2</sup> 6p <sup>1</sup>	<b>Pb</b> Lead 207.2 [Xe]4f <sup>14</sup> 5d <sup>10</sup> 6s <sup>2</sup> 6p <sup>2</sup>	<b>Bi</b> Bismuth 208.98038 [Xe]4f <sup>14</sup> 5d <sup>10</sup> 6s <sup>2</sup> 6p <sup>3</sup>	<b>Po</b> Polonium (209) [Xe]4f <sup>14</sup> 5d <sup>10</sup> 6s <sup>2</sup> 6p <sup>4</sup>	<b>At</b> Astatine (210) [Xe]4f <sup>14</sup> 5d <sup>10</sup> 6s <sup>2</sup> 6p <sup>5</sup>	<b>Rn</b> Radon (222) [Xe]4f <sup>14</sup> 5d <sup>10</sup> 6s <sup>2</sup> 6p <sup>6</sup>
7	<b>Fr</b> Francium (223) [Rn]7s <sup>1</sup>	<b>Ra</b> Radium (226) [Rn]7s <sup>2</sup>		<b>Rf</b> Rutherfordium (261) [Rn]5f <sup>14</sup> 6d <sup>2</sup> 7s <sup>2</sup>	<b>Db</b> Dubnium (262) [Rn]5f <sup>14</sup> 6d <sup>3</sup> 7s <sup>2</sup>	<b>Sg</b> Seaborgium (266) [Rn]5f <sup>14</sup> 6d <sup>4</sup> 7s <sup>2</sup>	<b>Bh</b> Bohrium (264) [Rn]5f <sup>14</sup> 6d <sup>5</sup> 7s <sup>2</sup>	<b>Hs</b> Hassium (277) [Rn]5f <sup>14</sup> 6d <sup>6</sup> 7s <sup>2</sup>	<b>Mt</b> Meitnerium (268) [Rn]5f <sup>14</sup> 6d <sup>7</sup> 7s <sup>2</sup>	<b>Uun</b> Ununnilium (281) [Rn]5f <sup>14</sup> 6d <sup>8</sup> 7s <sup>2</sup>	<b>Uuu</b> Unununium (272) [Rn]5f <sup>14</sup> 6d <sup>9</sup> 7s <sup>2</sup>	<b>Uub</b> Ununbium (285) [Rn]5f <sup>14</sup> 6d <sup>10</sup> 7s <sup>2</sup>	<b>Uuq</b> Ununquadium (289) [Rn]5f <sup>14</sup> 6d <sup>10</sup> 7s <sup>2</sup> 7p <sup>1</sup>	<b>Uuh</b> Ununhexium (292) [Rn]5f <sup>14</sup> 6d <sup>10</sup> 7s <sup>2</sup> 7p <sup>2</sup>				
			<b>La</b> Lanthanum 138.9055 [Xe]5d <sup>1</sup> 6s <sup>2</sup>	<b>Ce</b> Cerium 140.116 [Xe]4f <sup>1</sup> 5d <sup>1</sup> 6s <sup>2</sup>	<b>Pr</b> Praseodymium 140.90765 [Xe]4f <sup>3</sup> 6s <sup>2</sup>	<b>Nd</b> Neodymium 144.24 [Xe]4f <sup>4</sup> 6s <sup>2</sup>	<b>Pm</b> Promethium (145) [Xe]4f <sup>5</sup> 6s <sup>2</sup>	<b>Sm</b> Samarium 151.964 [Xe]4f <sup>6</sup> 6s <sup>2</sup>	<b>Eu</b> Europium 151.964 [Xe]4f <sup>7</sup> 6s <sup>2</sup>	<b>Gd</b> Gadolinium 157.25 [Xe]4f <sup>7</sup> 5d <sup>1</sup> 6s <sup>2</sup>	<b>Tb</b> Terbium 158.92534 [Xe]4f <sup>9</sup> 6s <sup>2</sup>	<b>Dy</b> Dysprosium 162.500 [Xe]4f <sup>10</sup> 6s <sup>2</sup>	<b>Ho</b> Holmium 164.93032 [Xe]4f <sup>11</sup> 6s <sup>2</sup>	<b>Er</b> Erbium 167.259 [Xe]4f <sup>12</sup> 6s <sup>2</sup>	<b>Tm</b> Thulium 168.93421 [Xe]4f <sup>13</sup> 6s <sup>2</sup>	<b>Yb</b> Ytterbium 173.04 [Xe]4f <sup>14</sup> 6s <sup>2</sup>	<b>Lu</b> Lutetium 174.967 [Xe]4f <sup>14</sup> 6s <sup>2</sup>	
			<b>Ac</b> Actinium (227) [Rn]6d <sup>1</sup> 7s <sup>2</sup>	<b>Th</b> Thorium 232.0381 [Rn]6d <sup>2</sup> 7s <sup>2</sup>	<b>Pa</b> Protactinium 231.03688 [Rn]5f <sup>2</sup> 6d <sup>1</sup> 7s <sup>2</sup>	<b>U</b> Uranium 238.02891 [Rn]5f <sup>3</sup> 6d <sup>1</sup> 7s <sup>2</sup>	<b>Np</b> Neptunium (237) [Rn]5f <sup>4</sup> 6d <sup>1</sup> 7s <sup>2</sup>	<b>Pu</b> Plutonium (244) [Rn]5f <sup>6</sup> 7s <sup>2</sup>	<b>Am</b> Americium (243) [Rn]5f <sup>7</sup> 7s <sup>2</sup>	<b>Cm</b> Curium (247) [Rn]5f <sup>8</sup> 7s <sup>2</sup>	<b>Bk</b> Berkelium (247) [Rn]5f <sup>9</sup> 7s <sup>2</sup>	<b>Cf</b> Californium (251) [Rn]5f <sup>10</sup> 7s <sup>2</sup>	<b>Es</b> Einsteinium (252) [Rn]5f <sup>11</sup> 7s <sup>2</sup>	<b>Fm</b> Fermium (257) [Rn]5f <sup>12</sup> 7s <sup>2</sup>	<b>Md</b> Mendelevium (258) [Rn]5f <sup>13</sup> 7s <sup>2</sup>	<b>No</b> Nobelium (259) [Rn]5f <sup>14</sup> 7s <sup>2</sup>	<b>Lr</b> Lawrencium (262) [Rn]5f <sup>14</sup> 7s <sup>2</sup> 7p <sup>1</sup>	

**In Bulk at Ambient Pressure**

**At High Pressure**

- Solids
- Liquids
- Gases
- Artificially Prepared

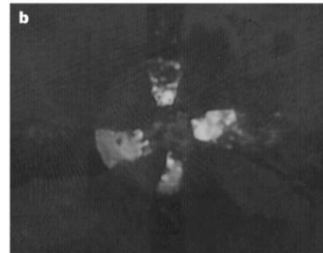
Atomic Number: 58  
Ground-state Level: 1G<sub>4</sub>  
Symbol: **Ce**  
Name: Cerium  
Atomic Weight: 140.116  
Ground-state Configuration: [Xe]4f<sup>1</sup>5d<sup>1</sup>6s<sup>2</sup>  
Ionization Energy (eV): 5.5387

# At pressures of around 100 GPa, solid oxygen becomes superconducting, with $T_c$ of 0.6 K.

40GPa



60GPa

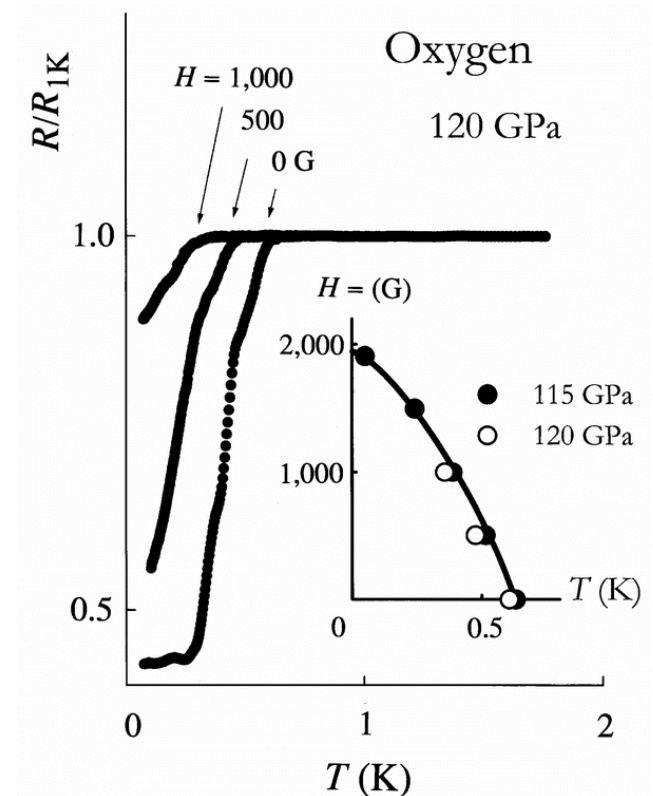
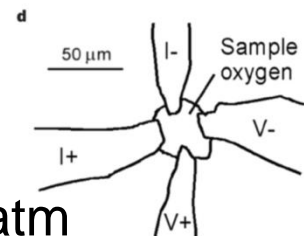


120GPa



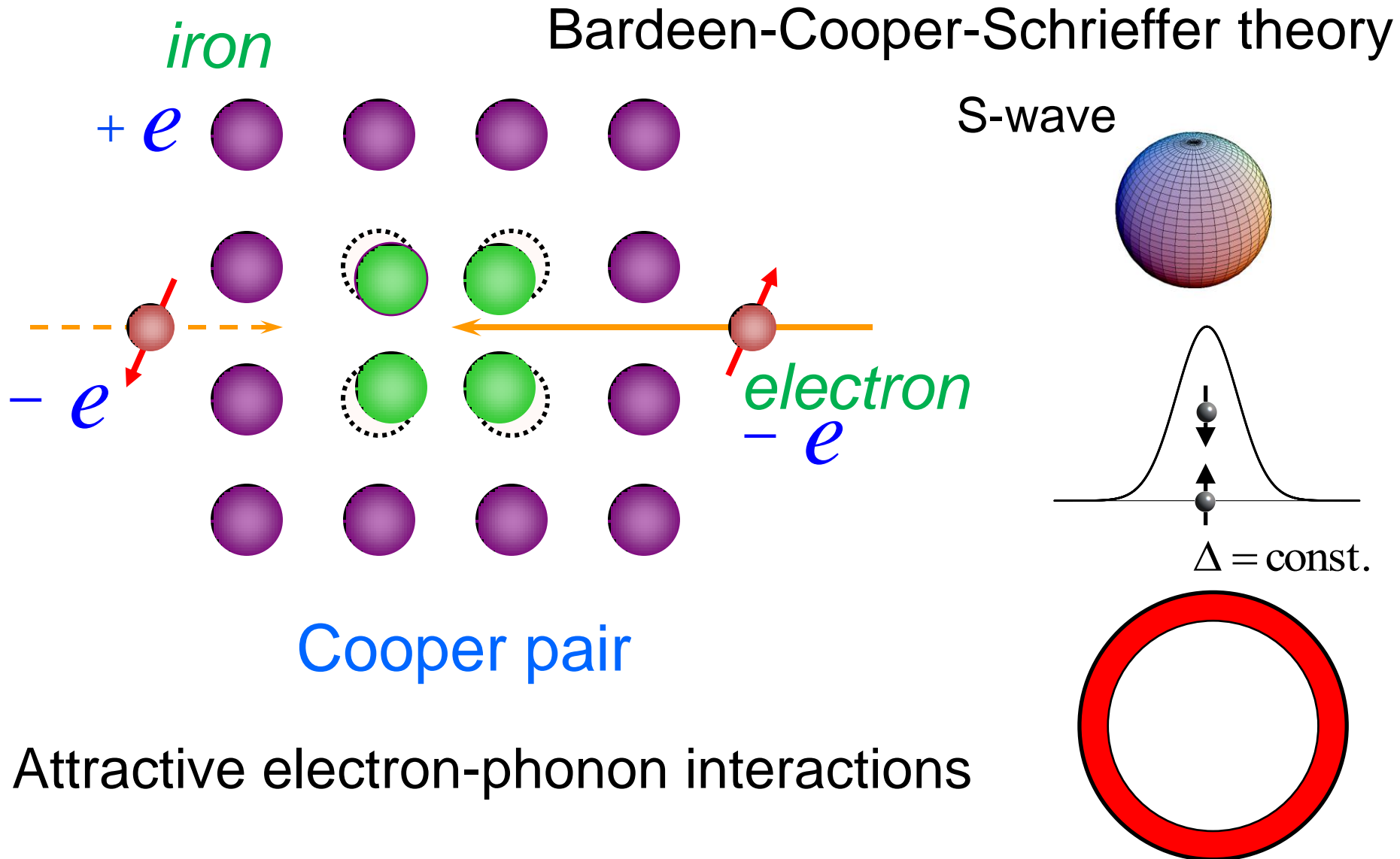
*Solid Oxygen becomes shiny at high pressure (metallic color)*

1GPa=10kbar=10,000 atm  
 cf. 1 atm~10m water depth  
 10,000 atm~100 km water depth



K. Shimizu et al. Nature (1998)

# Conventional Superconductor





# MgB<sub>2</sub> ( $T_c = 39$ K)

J. Nagamatsu *et al.*, Nature (2001)

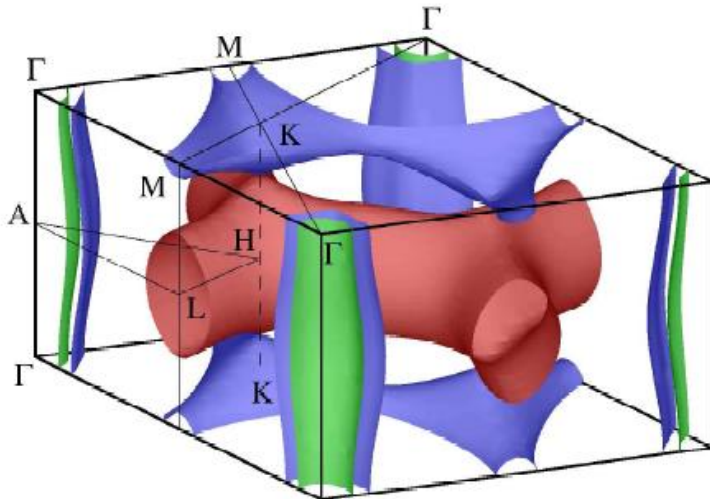
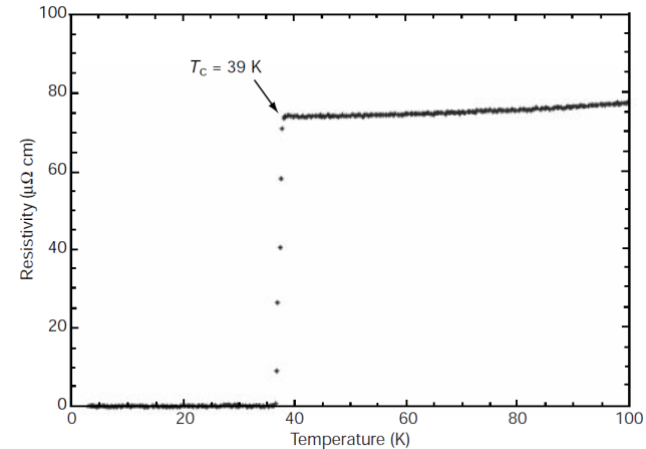
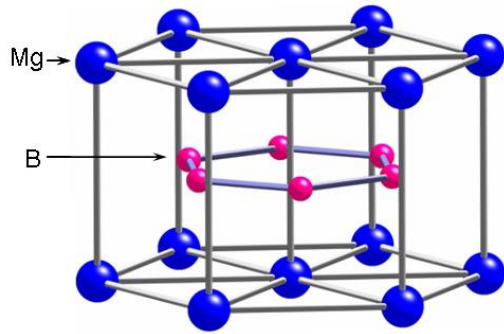
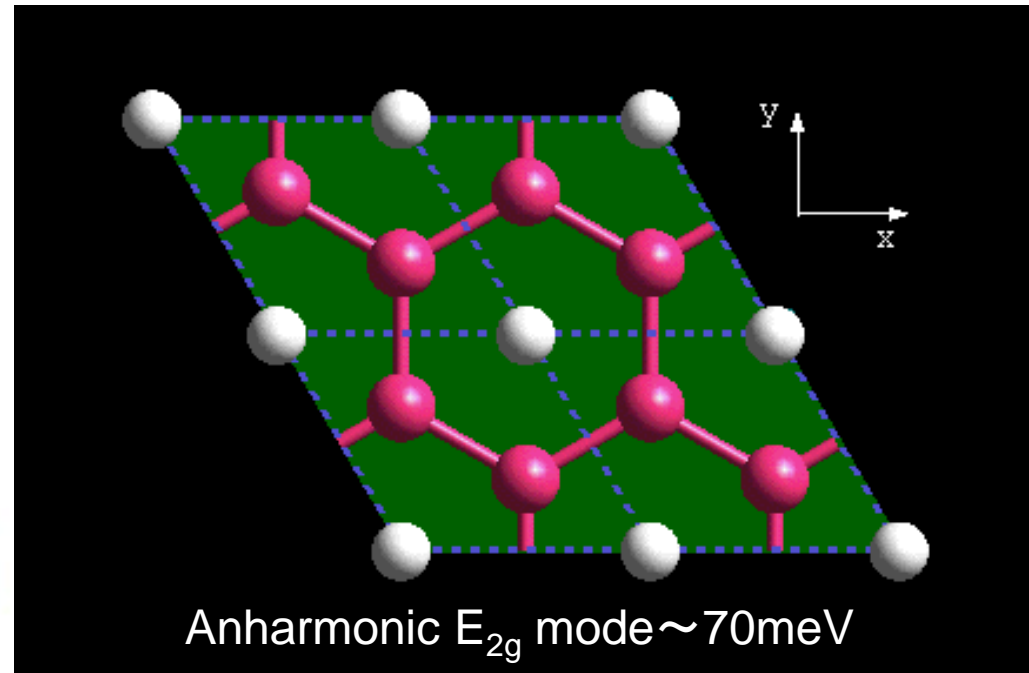


FIG. 1. Fermi surface of MgB<sub>2</sub>. The figure is taken from Ref. [5]. Holes in the  $\sigma$ -band form cylinders around the  $\Gamma$ A-line. The  $\pi$ -band has electron and hole pockets located near the  $H$ - and  $K$ -points, respectively.



# High- $T_c$ cuprates

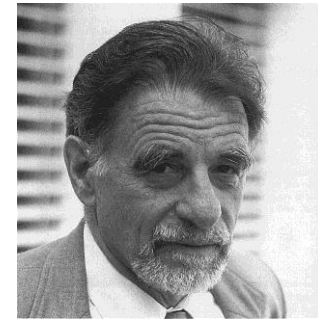
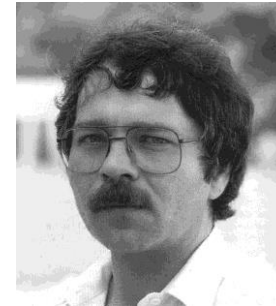
## Possible High $T_c$ Superconductivity in the Ba – La – Cu – O System

J.G. Bednorz and K.A. Müller

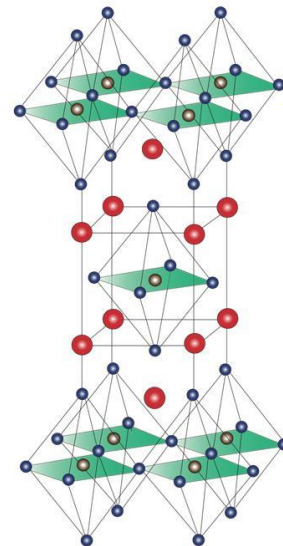
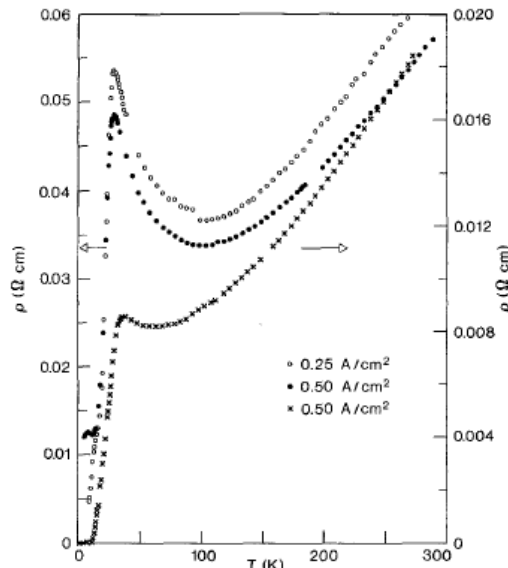
IBM Zürich Research Laboratory, Rüschlikon, Switzerland

Received April 17, 1986

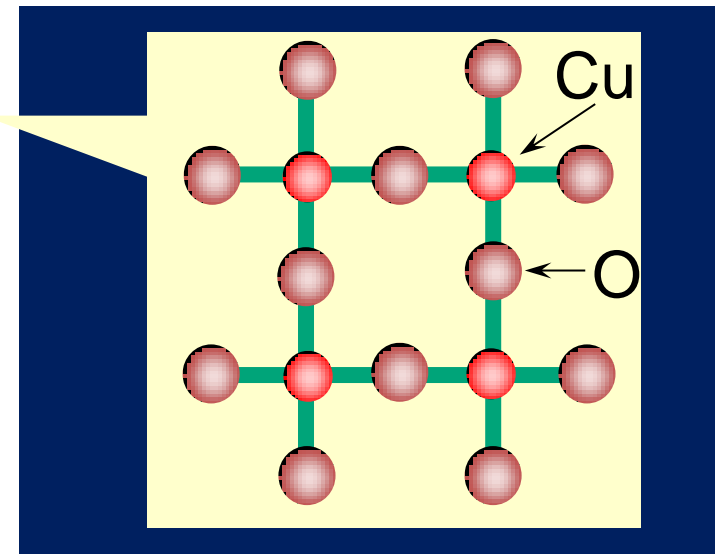
Metallic, oxygen-deficient compounds in the Ba – La – Cu – O system, with the composition  $\text{Ba}_x\text{La}_{5-x}\text{Cu}_5\text{O}_{5(3-y)}$  have been prepared in polycrystalline form. Samples with  $x=1$  and  $0.75$ ,  $y>0$ , annealed below  $900^\circ\text{C}$  under reducing conditions, consist of three phases, one of them a perovskite-like mixed-valent copper compound. Upon cooling, the samples show a linear decrease in resistivity, then an approximately logarithmic increase, interpreted as a beginning of localization. Finally an abrupt decrease by up to three orders of magnitude occurs, reminiscent of the onset of percolative superconductivity. The highest onset temperature is observed in the 30 K range. It is markedly reduced by high current densities. Thus, it results partially from the percolative nature, but possibly also from 2D superconducting fluctuations of double perovskite layers of one of the phases present.



## Superconductivity in $\text{CuO}_2$ planes

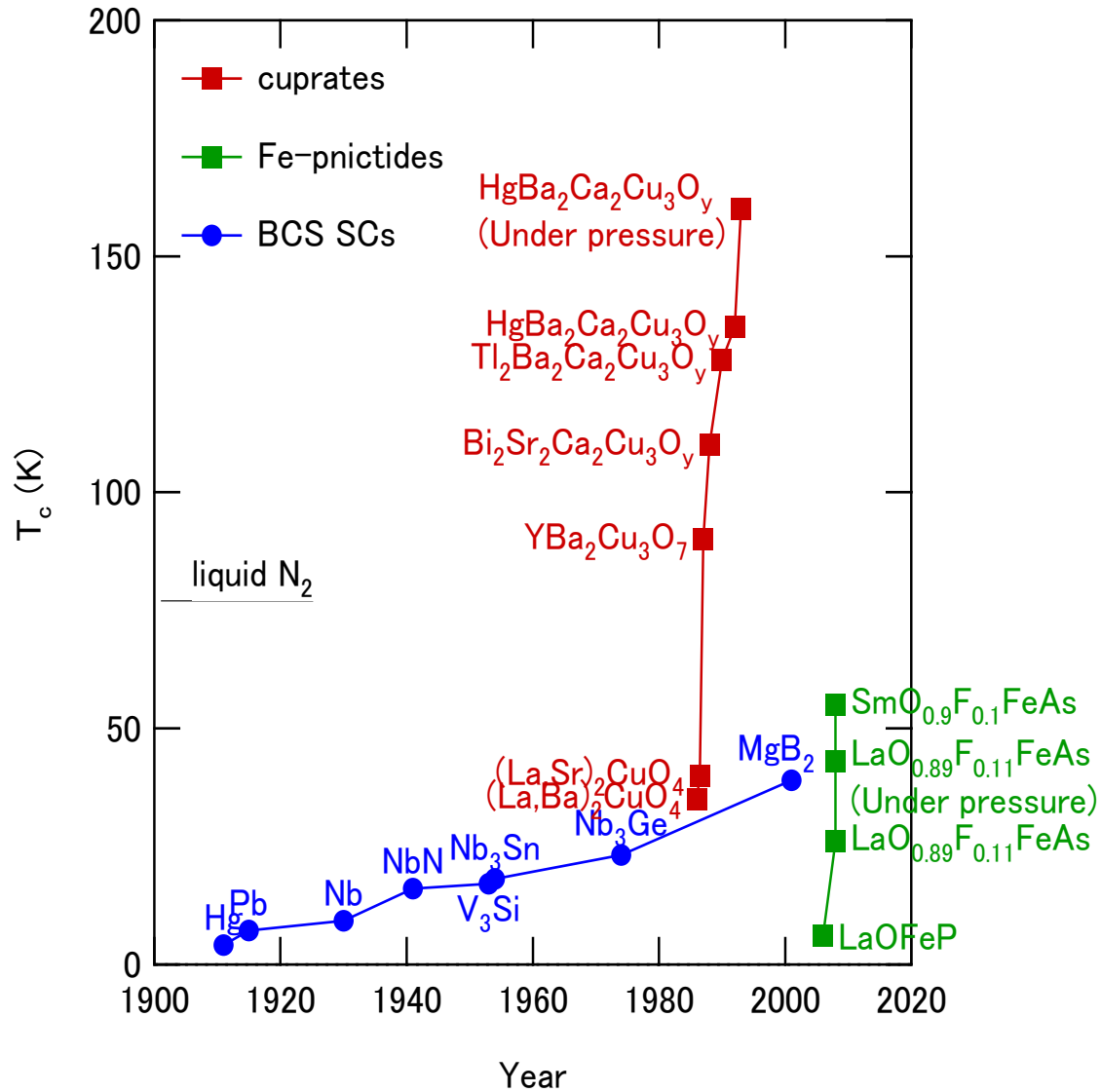


● La/Sr ● Cu ● O



J. G. Bednorz and K.A. Müller, *Zeitschrift für Physik B* **64**, 189 (1986).

# Fe-based high- $T_c$ superconductors



# Superconductivity in Fe-Pnictides — Discovery

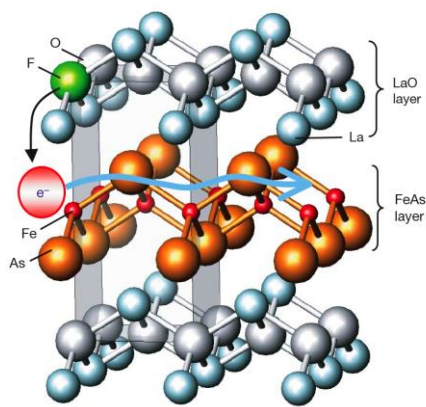
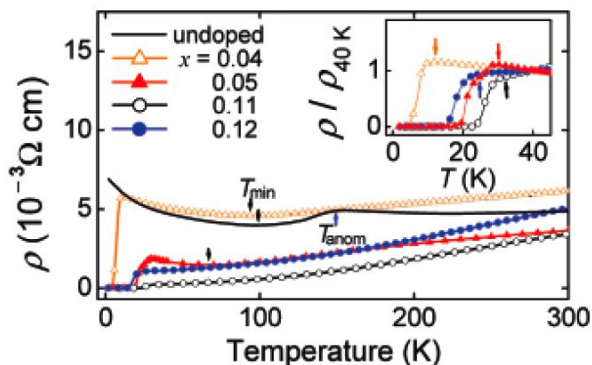
J|A|C|S  
COMMUNICATIONS

Published on Web 02/23/2008

## Iron-Based Layered Superconductor $\text{La}[\text{O}_{1-x}\text{F}_x]\text{FeAs}$ ( $x = 0.05\text{--}0.12$ ) with $T_c = 26\text{ K}$

Yoichi Kamihara,<sup>\*,†</sup> Takumi Watanabe,<sup>‡</sup> Masahiro Hirano,<sup>†,§</sup> and Hideo Hosono<sup>†,‡,§</sup>

*ERATO-SORST, JST, Frontier Research Center, Tokyo Institute of Technology, Mail Box S2-13, Materials and Structures Laboratory, Tokyo Institute of Technology, Mail Box R3-1, and Frontier Research Center, Tokyo Institute of Technology, Mail Box S2-13, 4259 Nagatsuta, Midori-ku, Yokohama 226-8503, Japan*



$\text{LaFeAs}(\text{O}_{1-x}\text{F}_x)$



Y. Kamihara *et al.*, JACS, **130**, 3296 (2008).

# Superconductivity in Fe-Pnictides — Discovery

Hosono's group was not looking for superconductor, but trying to create new kind of transparent semiconductors for flat-panel display.

LaFePO  $T_c=4$  K

LaFeP(O,F)  $T_c=7$  K

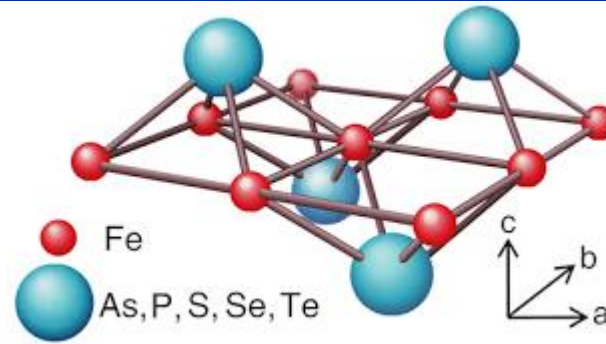
LaFeAs(O,F)  $T_c=26$  K

SmFeAs(O,F)  $T_c=56$  K

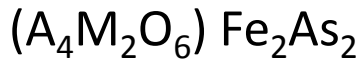
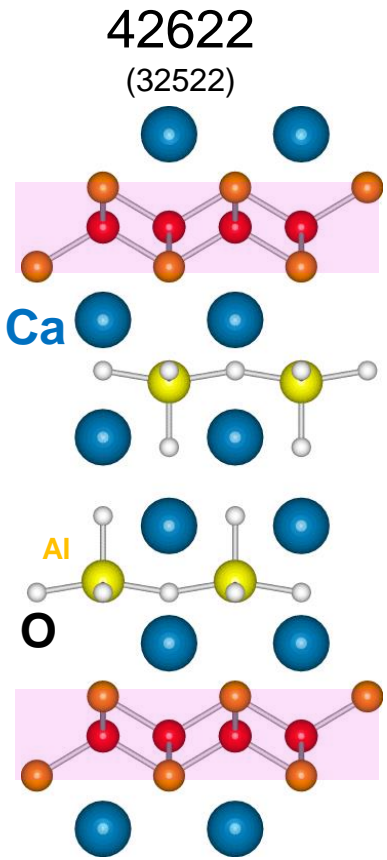


Only two months!

# Fe-based high- $T_c$ superconductors

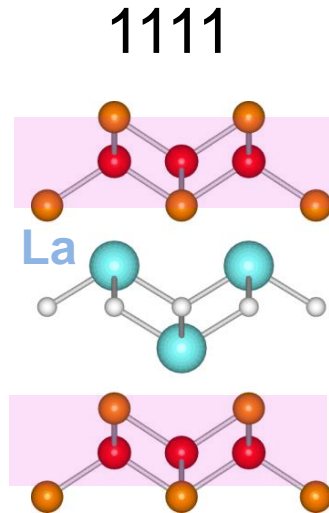


2D square lattice of Fe



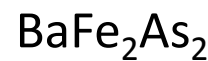
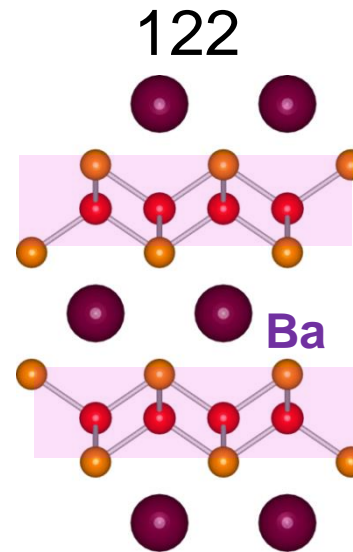
$T_c(\text{max})=47\text{K}$

Zhu et al.(2009)  
Ogino et al. (2009)



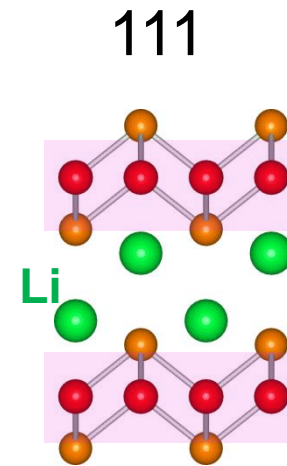
$T_c(\text{max})=55\text{K}$

Y. Kamihara et al.(2008)



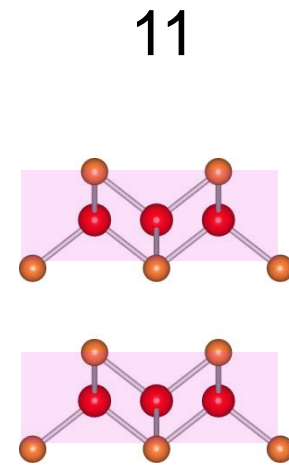
$T_c(\text{max})=38\text{K}$

M. Rotter et al.(2008)



$T_c=18\text{K}$

X.C.Wang et al.(2008)



$T_c=8\text{K}$

F.C.Hsu et al.(2008)



# Fe-based high- $T_c$ superconductors

Are iron-pnictides an Electron-Phonon Superconductor?

$$T_c \sim \omega_D e^{-\frac{1}{\lambda}} \quad \omega_D \sim 200 \text{ K}$$

$\omega_D$  Debye frequency

$$\lambda \sim 0.2$$

$\lambda$  Electron-phonon coupling      Comparable to the conventional metals

$$\Rightarrow T_c \sim 1 \text{ K}$$

Electron-phonon coupling is not sufficient to explain superconductivity in the whole family of Fe-As based superconductors

# Why are Fe-based HTSC important?

## 1. A new class of high temperature superconductors

They knocked the cuprates off their pedestal as a unique class of high temperature superconductors.

## 2. A new family of unconventional superconductors

A possible new mechanism of high- $T_c$  superconductivity

## 3. They would be easier to work into technological applications than the cuprates.

# Physics of iron-based high temperature superconductors

---

1) Introduction

2) Similarities and differences between cuprates and Fe-pnictides

3) Normal state properties

Electronic structure and magnetism

4) Superconducting properties

Superconducting gap structure

5) Some recent topics

QCP, BCS-BEC crossover,  
A novel high field SC state, Nematicity . . . .



# Superconductivity

Macroscopic wave function with a well defined amplitude and phase

$$\psi(r) = \sqrt{n_s} e^{i\theta(r)}$$

2<sup>nd</sup> order phase transition

Symmetry breaking

Gauge transformation

$$\psi \rightarrow e^{i\theta} \psi \quad \psi^\dagger \rightarrow e^{-i\theta} \psi^\dagger$$

Order parameter

$$\Delta \sim \langle \psi\psi \rangle \rightarrow \Delta e^{2i\theta}$$

**U(1)** Gauge symmetry breaking

# Unconventional superconductivity

## Conventional definition of unconventional superconductivity

Full symmetry group  $\mathbf{G}$

$$\mathbf{G} = U(1) \times \mathbf{G} \times SU(2) \times T$$

$U(1)$  gauge symmetry

$\mathbf{G}$  symmetry group of **crystal lattice**

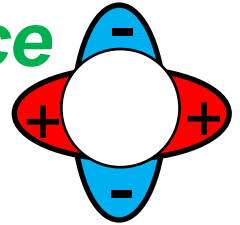
e.g. *d*-wave in tetragonal lattice

$SU(2)$  symmetry group of **spin** rotation

Spin triplet

$T$  **time** reversal symmetry operation

$$\Psi \rightarrow \Psi_1 + i\Psi_2$$



One or more symmetries in addition to  $U(1)$  are broken at  $T_c$

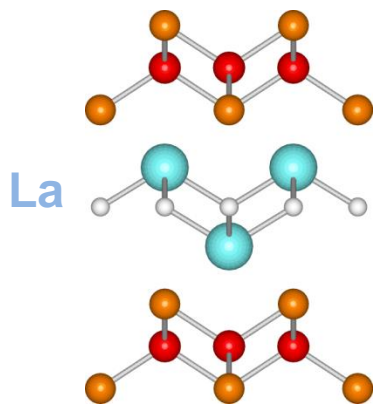
## A more general definition

Superconductivity not mediated by phonon

e.g. Nodal superconductors

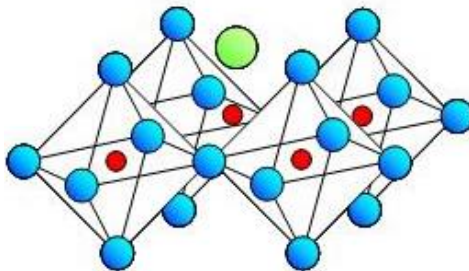
# Three families of unconventional superconductor

Iron pnictide (Fe)



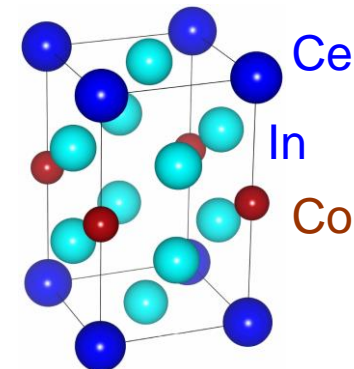
Weakly localized  
3*d*-electrons

Cuprate (Cu)



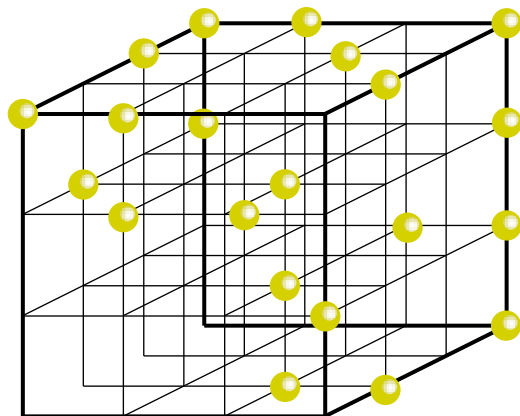
Strongly localized  
3*d*-electrons

Heavy fermion compound  
(Ce, U)

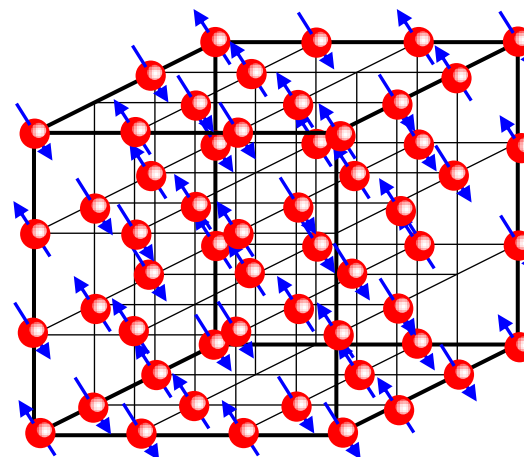


Very strongly localized  
4*f*, 5*f* electrons

Weak correlation



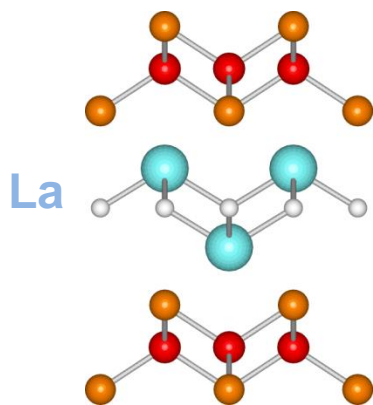
Strong correlation



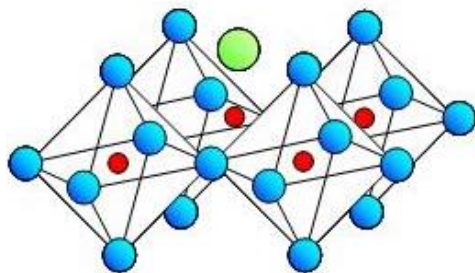


# Three classes of unconventional superconductor

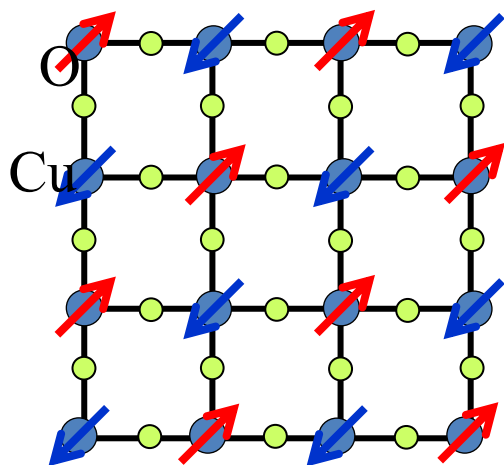
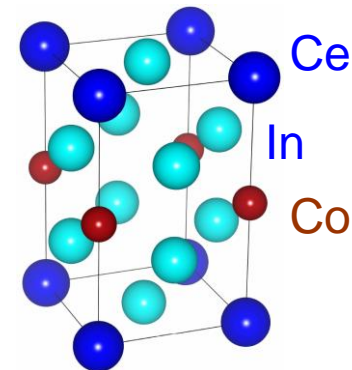
Iron pnictide (Fe)



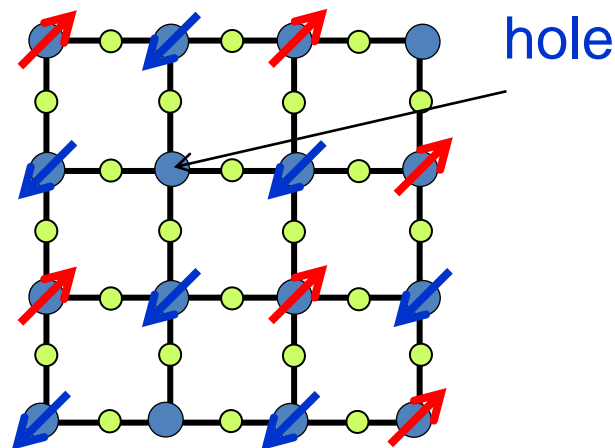
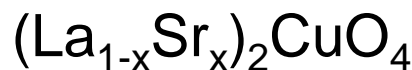
Cuprate (Cu)



Heavy fermion compound (Ce, U)



Mott insulator

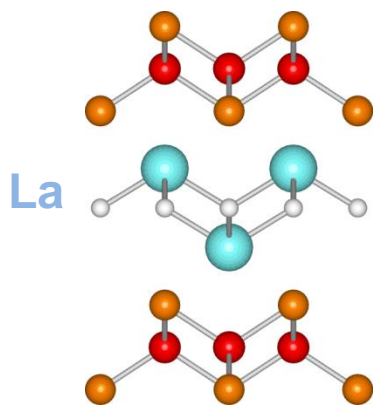


High- $T_c$  superconductor

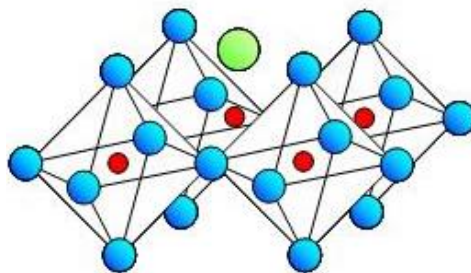
Carrier doping

# Three families of unconventional superconductor

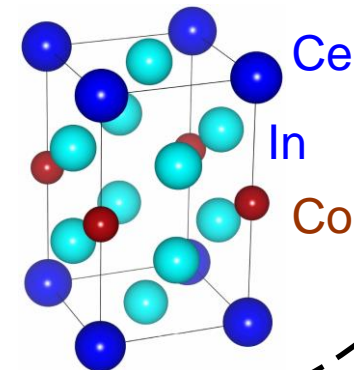
Iron pnictide (Fe)



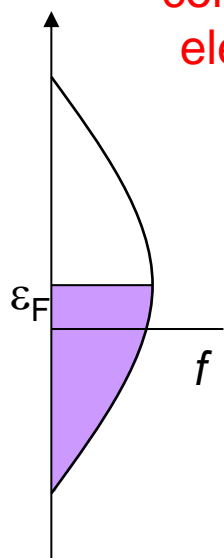
Cuprate (Cu)



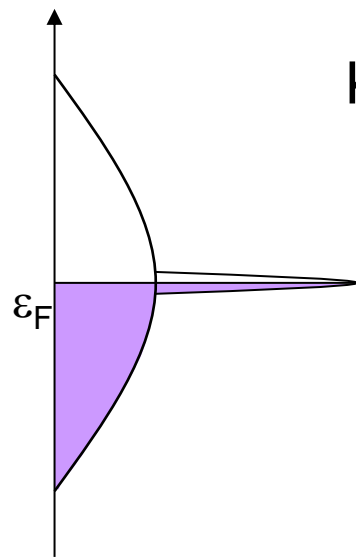
Heavy fermion compound (Ce, U)



Hybridization with conduction electrons

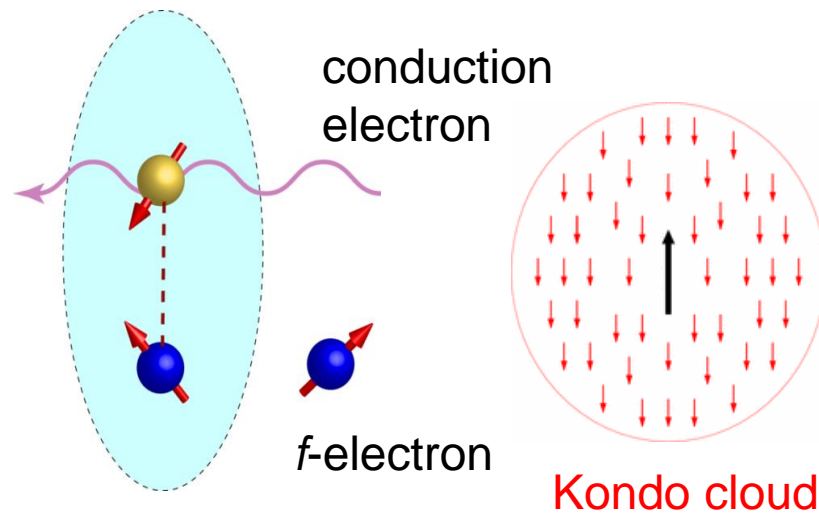


High temperature



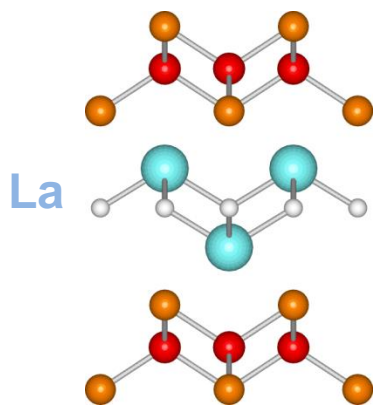
Low temperature

Kondo effect

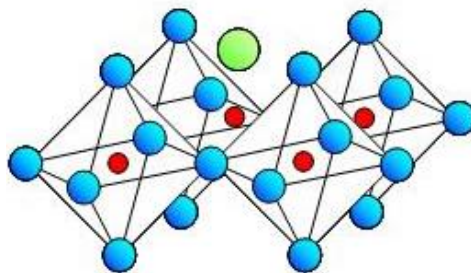


# Three families of unconventional superconductor

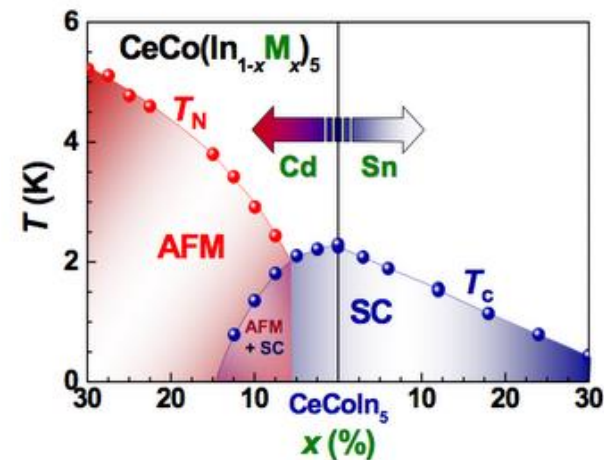
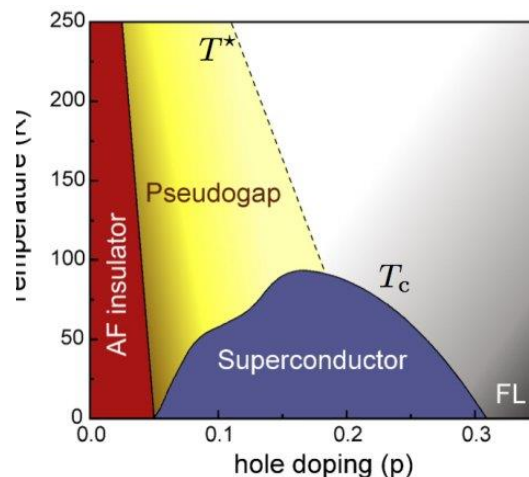
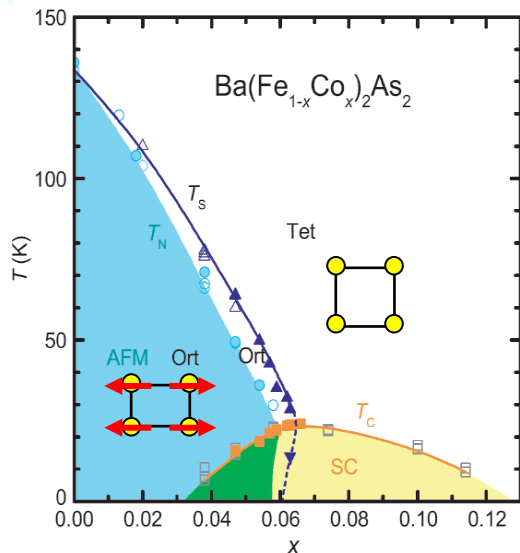
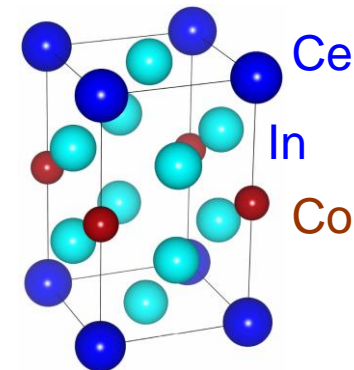
## Iron pnictide (Fe)



## Cuprate (Cu)



## Heavy fermion compound (Ce, U)

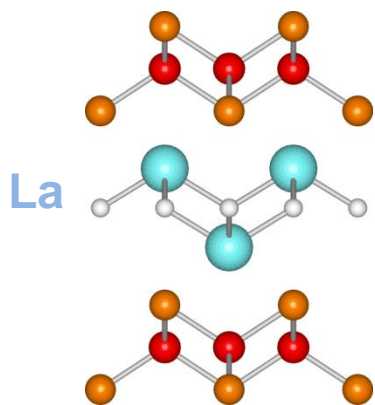


Superconductivity is induced by suppressing a magnetically ordered phase

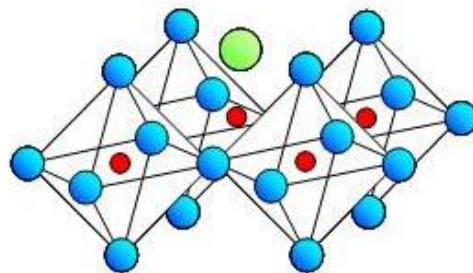
Magnetic fluctuations may bind the Cooper pairs

# Three families of unconventional superconductor

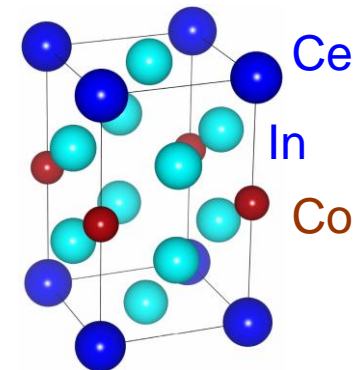
Iron pnictide (Fe)



Cuprate (Cu)



Heavy fermion compound (Ce, U)



	Pnictide		Cuprate		Heavy Fermion
Electron correlation	strong	<	strong	<	very strong
Fermi surface	simple 2D		Very simple 2D		Complicated 3D
Magnetic structure	simple		simple		complicated
Physics	Multi-orbital		Mott		Kondo

# Physics of iron-based high temperature superconductors

---

1) Introduction

2) Similarities and differences between cuprates and Fe-pnictides

3) Normal state properties

Electronic structure and magnetism

4) Superconducting properties

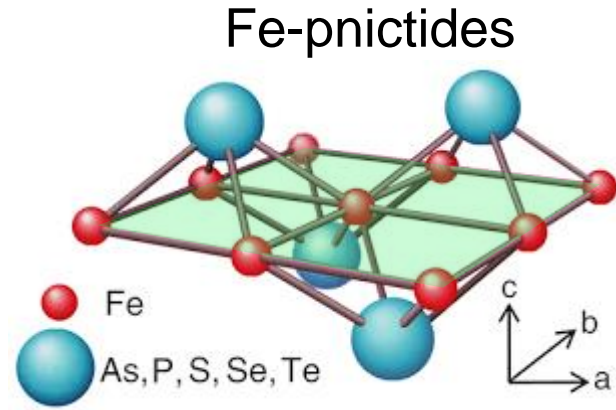
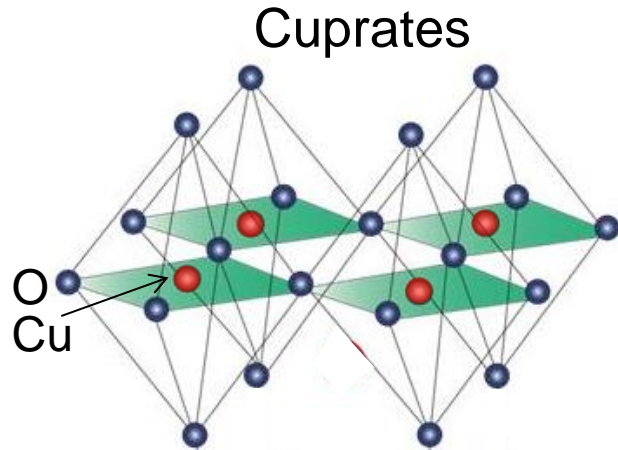
Superconducting gap structure

5) Some recent topics

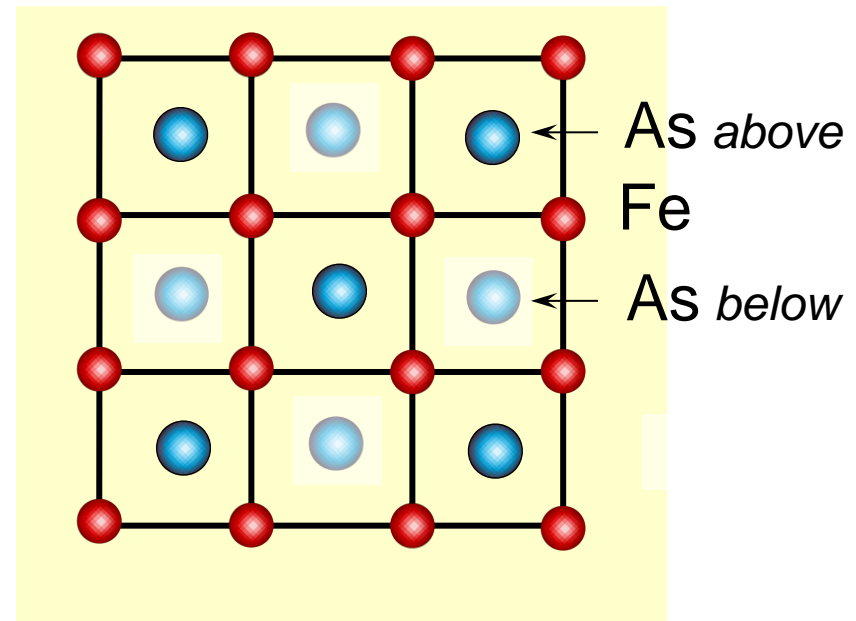
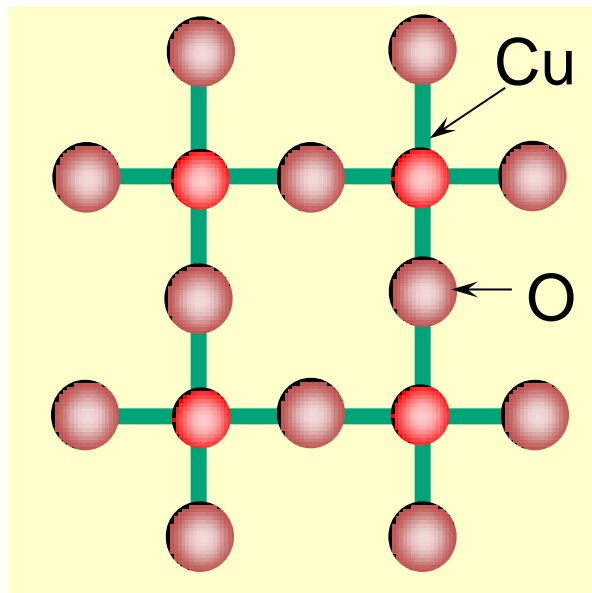
QCP, BCS-BEC crossover,  
A novel high field SC state, Nematicity . . . .



# Similarities and differences between cuprates and pnictides



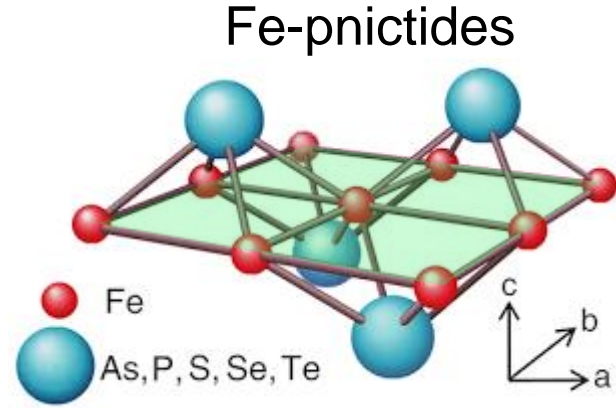
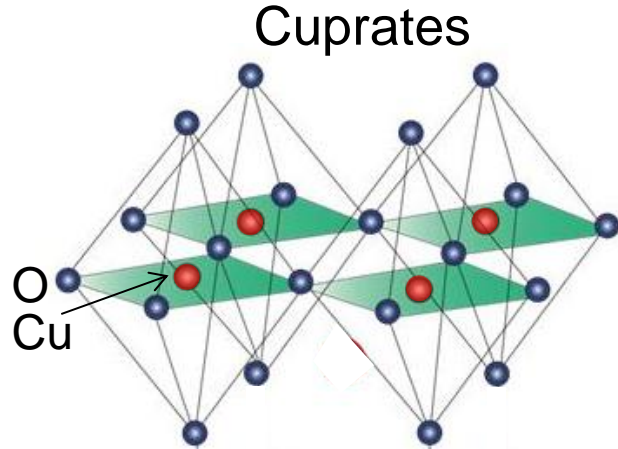
Superconductivity in 2D planes



Enhanced fluctuations  $\rightarrow$  suppression of magnetic order

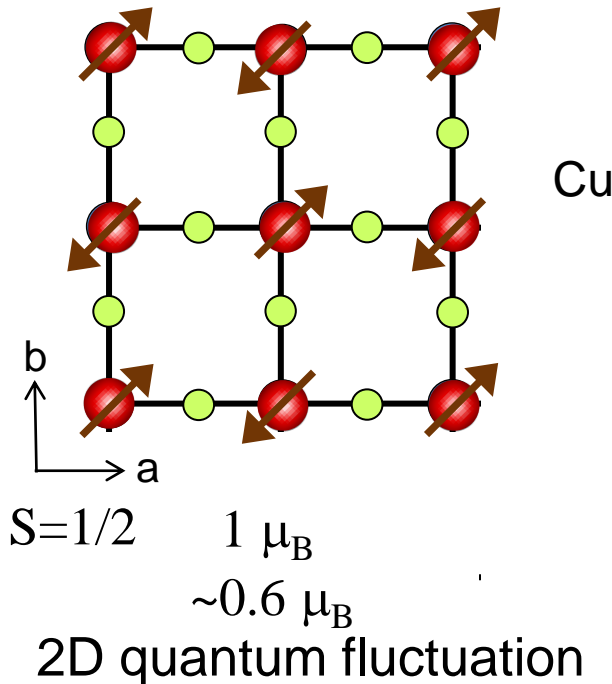


# Similarities and differences between cuprates and pnictides

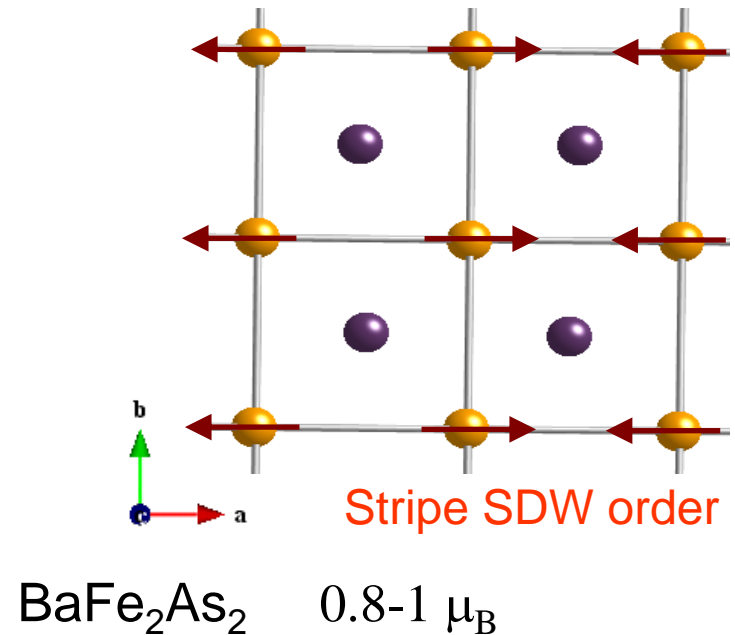


Parent compound

AFM insulator

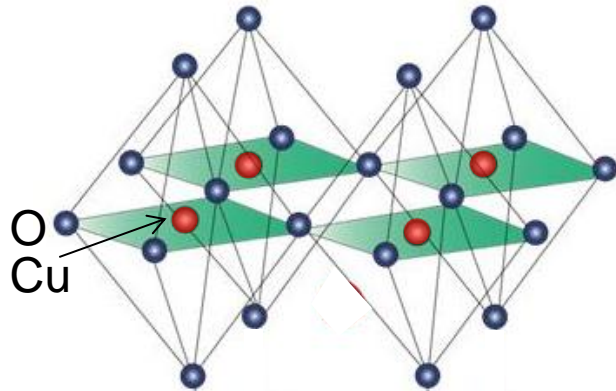


SDW metal

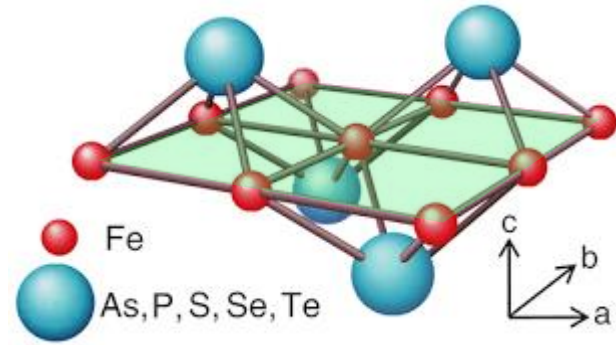


# Similarities and differences between cuprates and pnictides

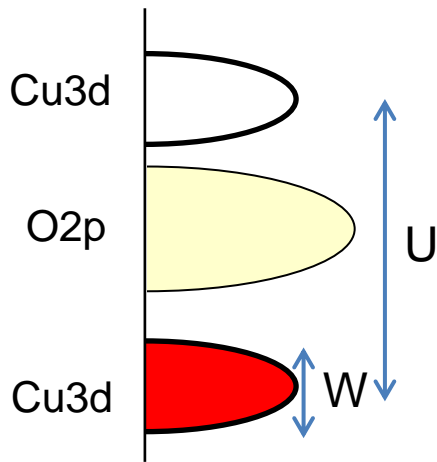
## Cuprates



## Fe-pnictides



Parent compound

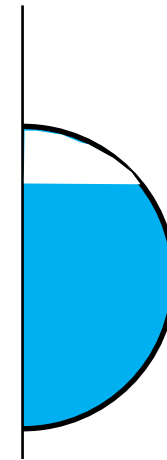


$U$  : Coulomb  $\sim 8\text{eV}$

$W$  : Band width  $\sim 3\text{eV}$

Strong electron-electron correlation

Mott insulator



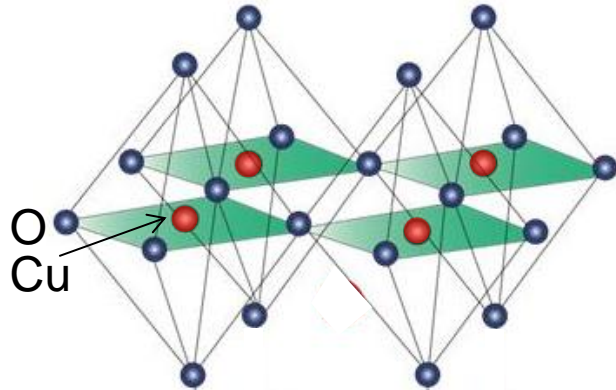
$U \sim W \sim 2\text{-}3\text{ eV}$

Intermediate correlation

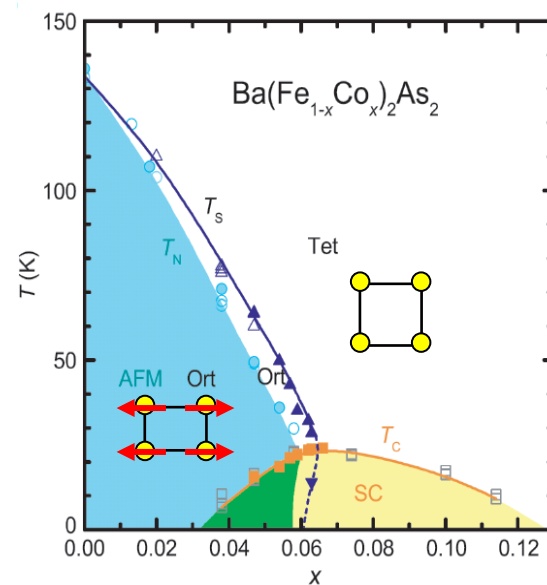
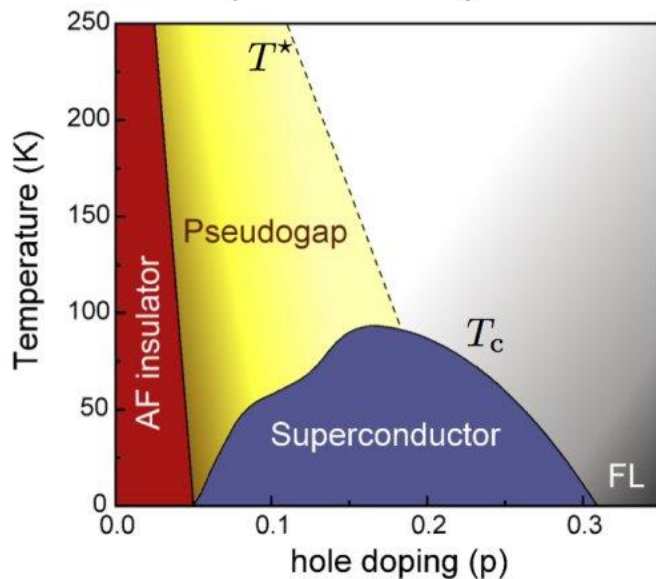
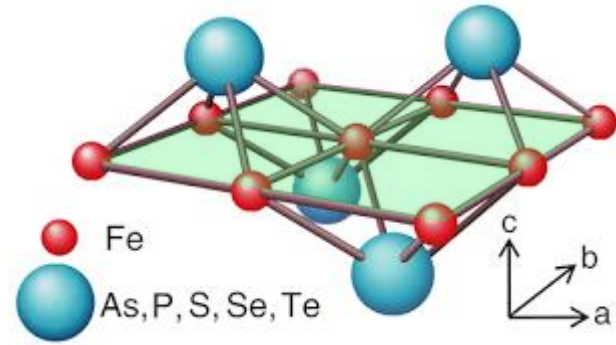
Spin density wave (SDW) metal

# Similarities and differences between cuprates and pnictides

## Cuprates



## Fe-pnictides

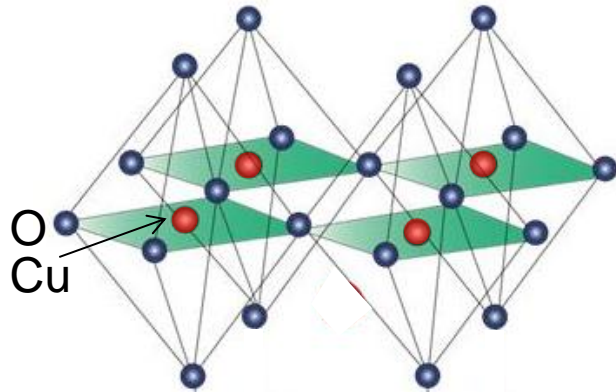


Superconductivity occurs in the vicinity of magnetic order

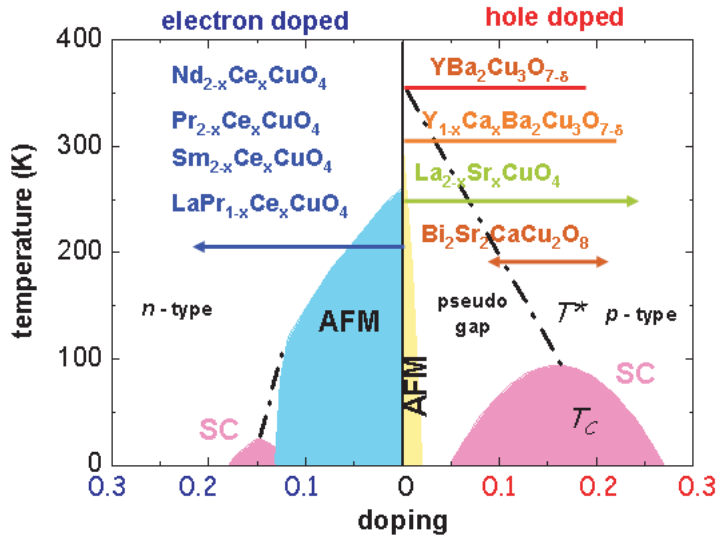
In Fe-pnictides, structural ( $T_s$ ) and AFM transition ( $T_N$ ) lines follow closely each other

# Similarities and differences between cuprates and pnictides

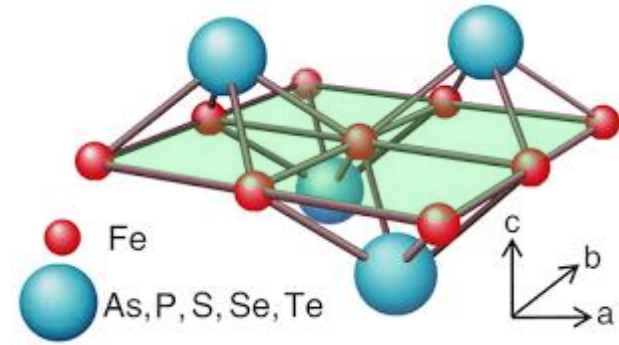
## Cuprates



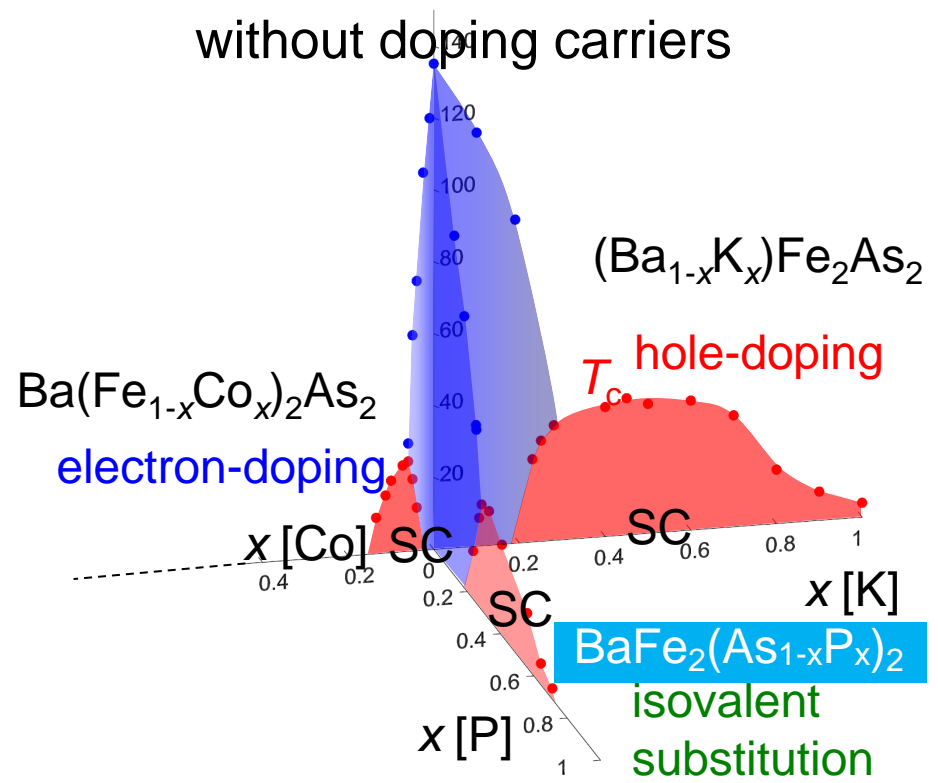
Superconductivity induced by doping holes or electrons



## Fe-pnictides

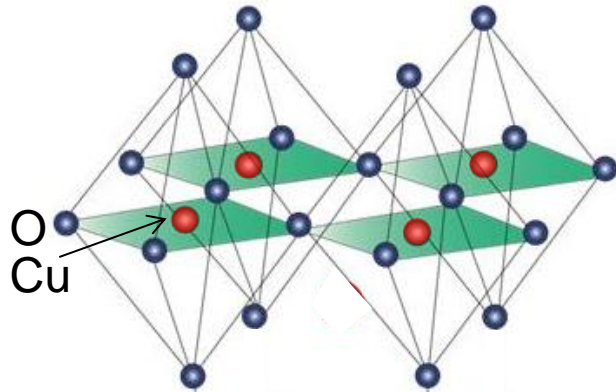


Ground state can be tuned without doping carriers

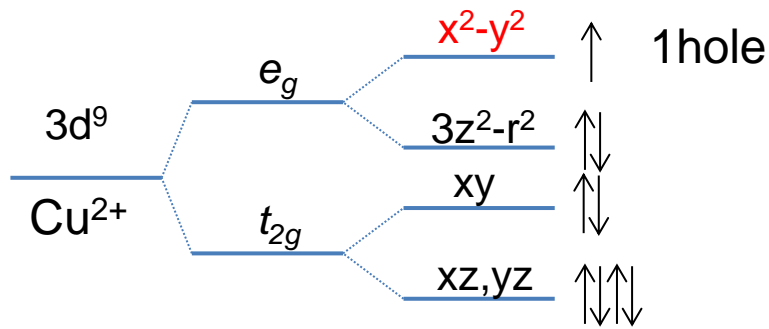
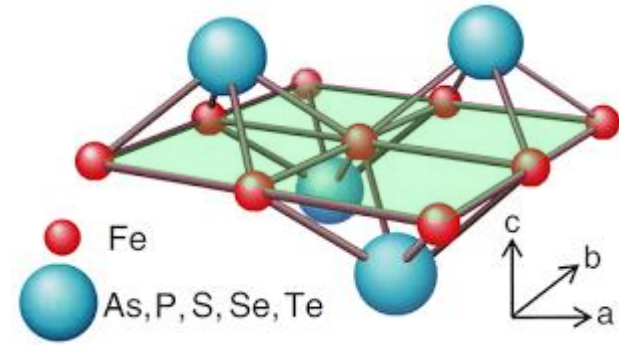


# Similarities and differences between cuprates and pnictides

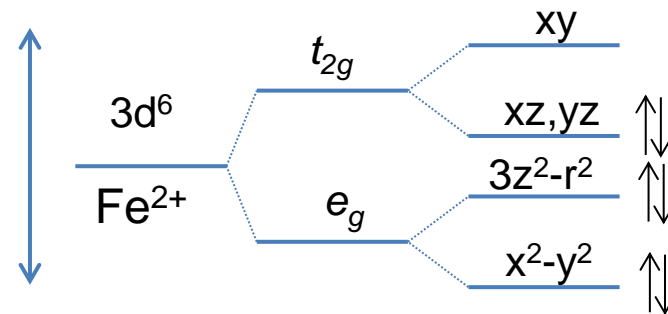
## Cuprates



## Fe-pnictides



Large crystal field  $\sim 2-3$  eV

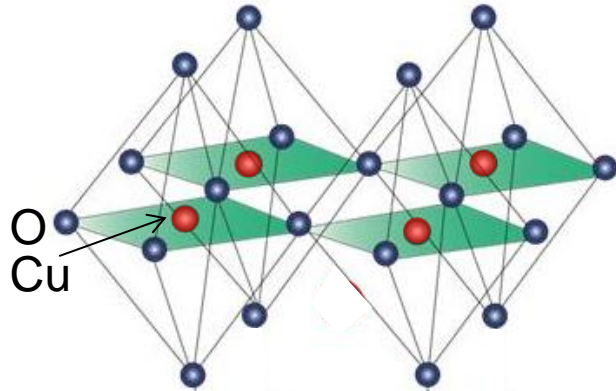


Small crystal field ( $\sim 500$  meV)

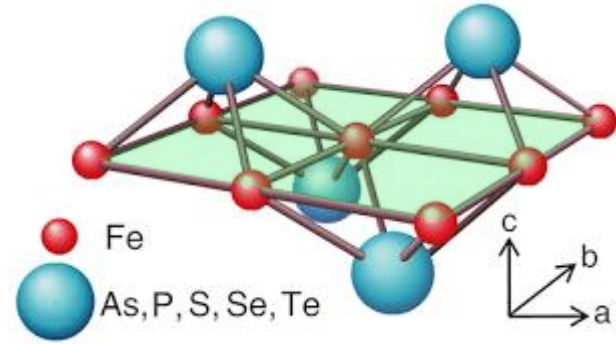


# Similarities and differences between cuprates and pnictides

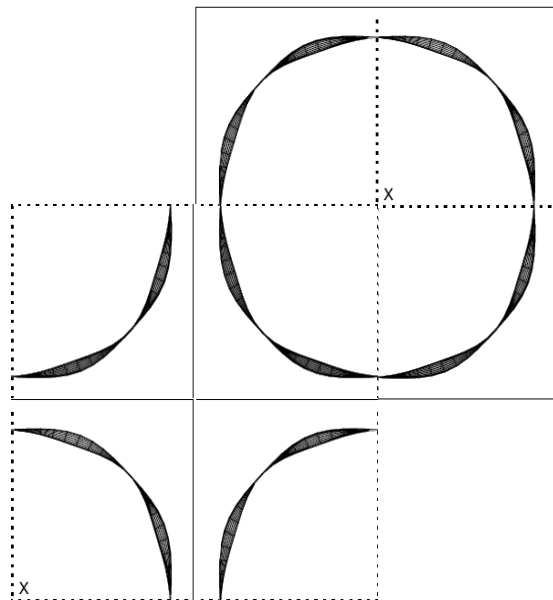
## Cuprates



## Fe-pnictides

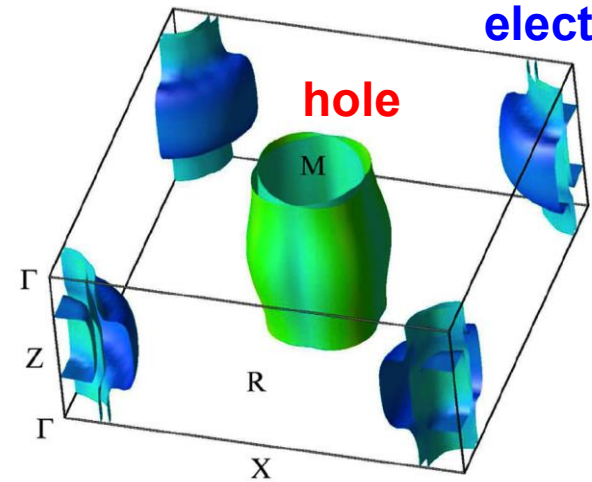


hole



Only hole band

electron

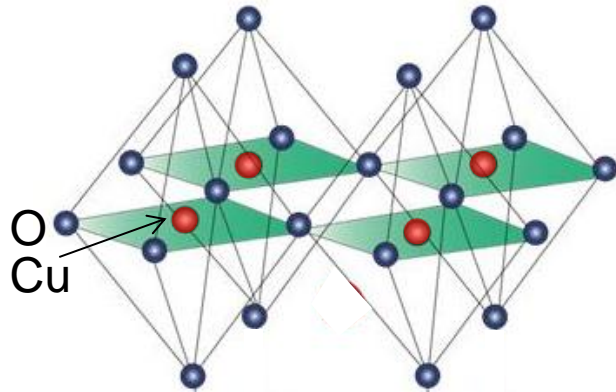


Well separated hole and electron bands



# Similarities and differences between cuprates and pnictides

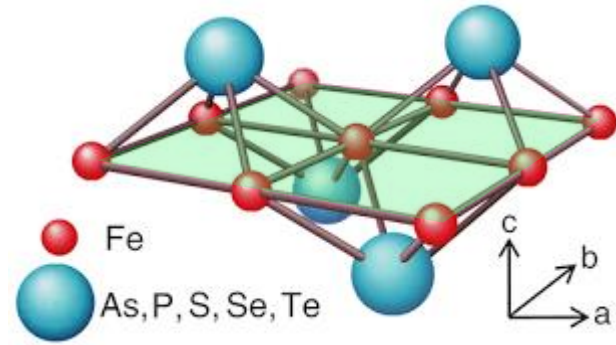
## Cuprates



One orbital

$$x^2-y^2$$

## Fe-pnictides

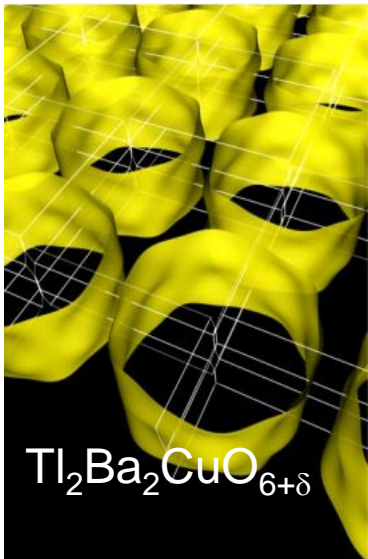


Mainly three orbitals

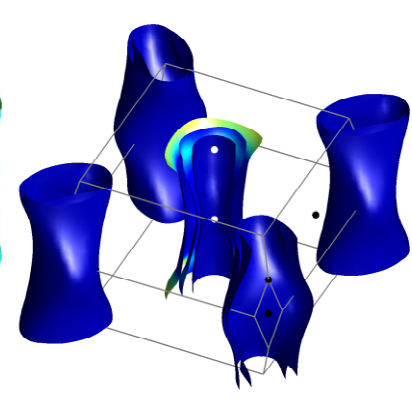
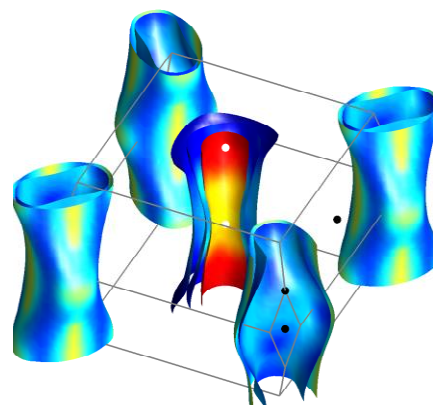
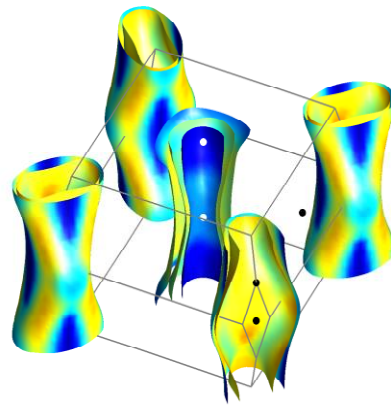
$$xz+yz$$

$$xy$$

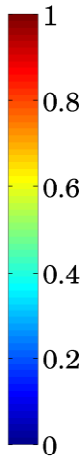
$$3z^2-r^2$$



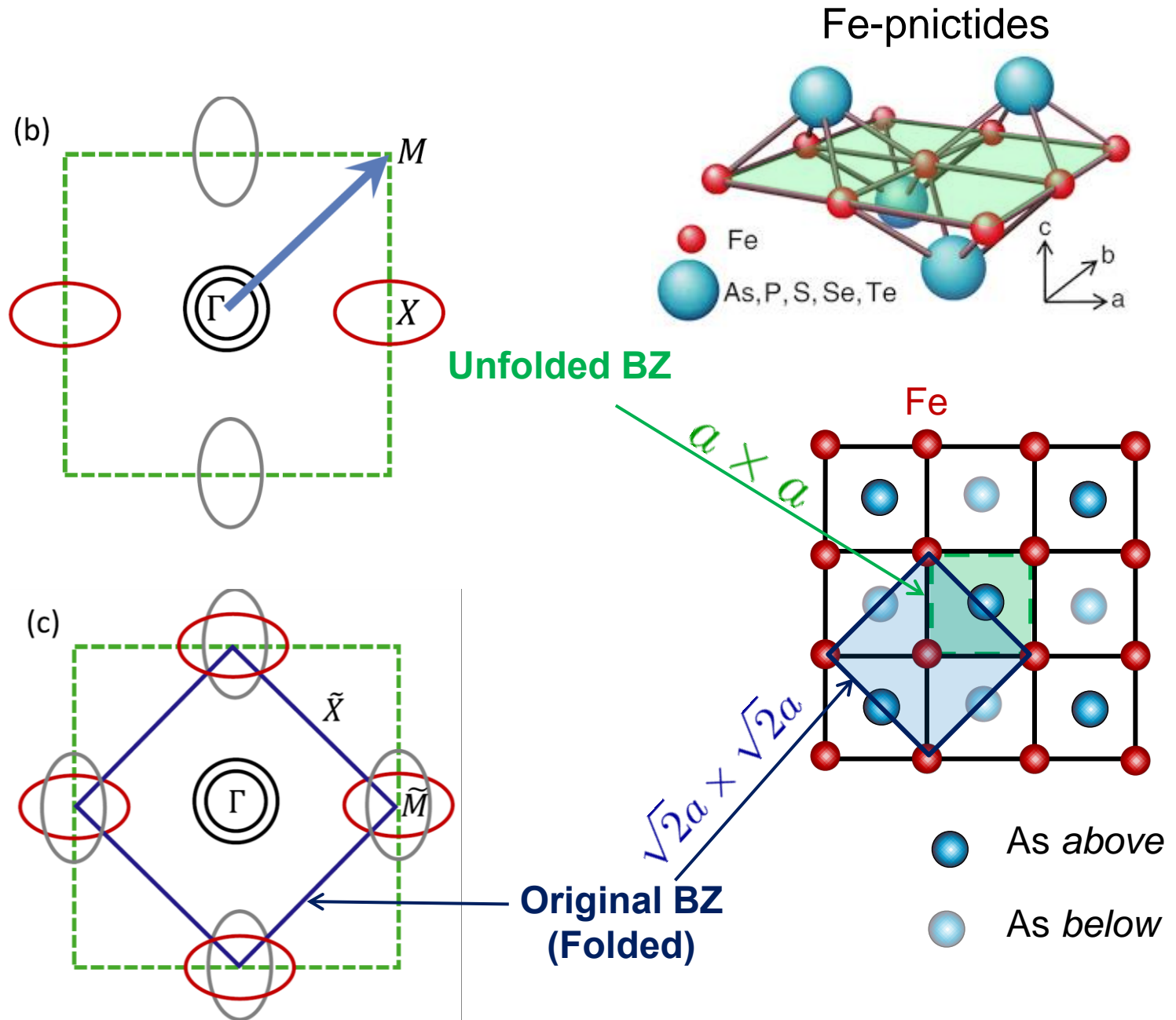
N. E. Hussey *et al.*,  
Nature (2003).



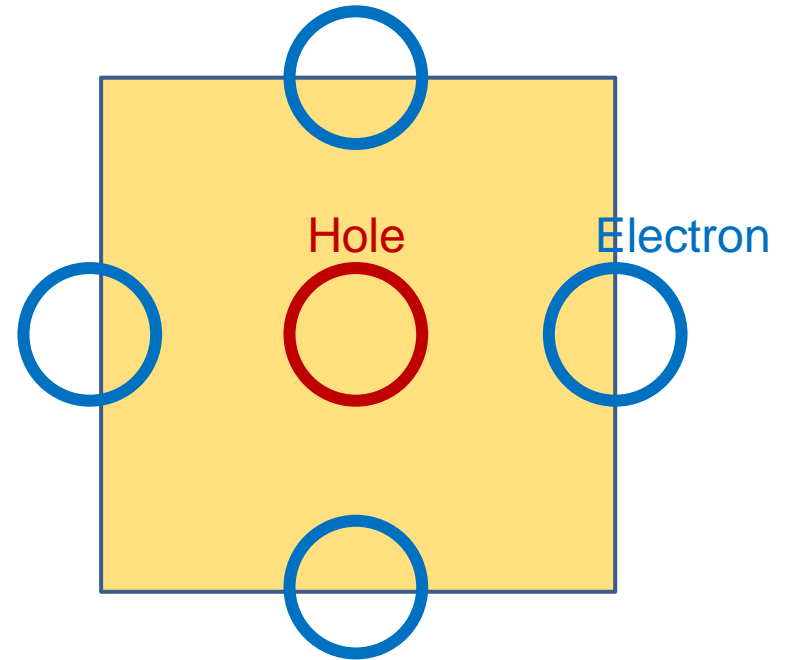
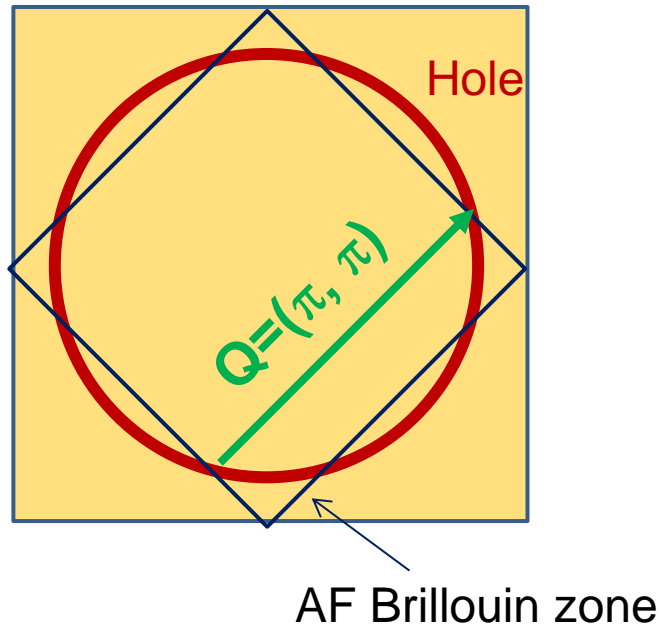
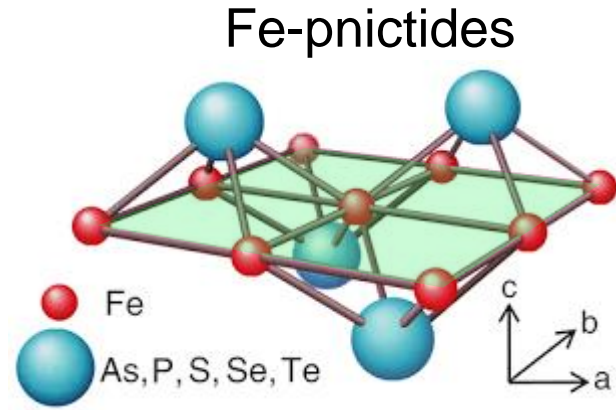
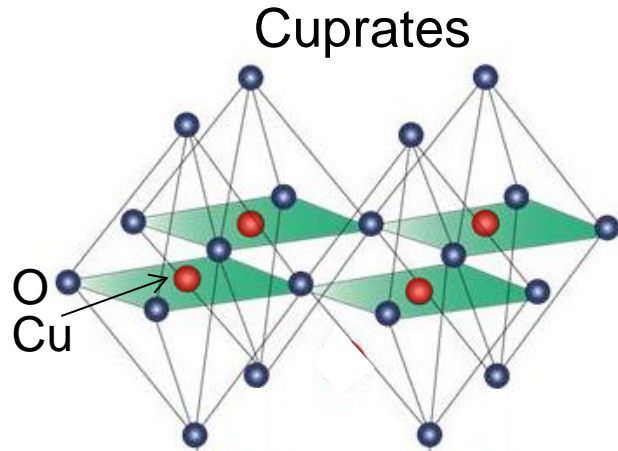
$BaFe_2As_2$



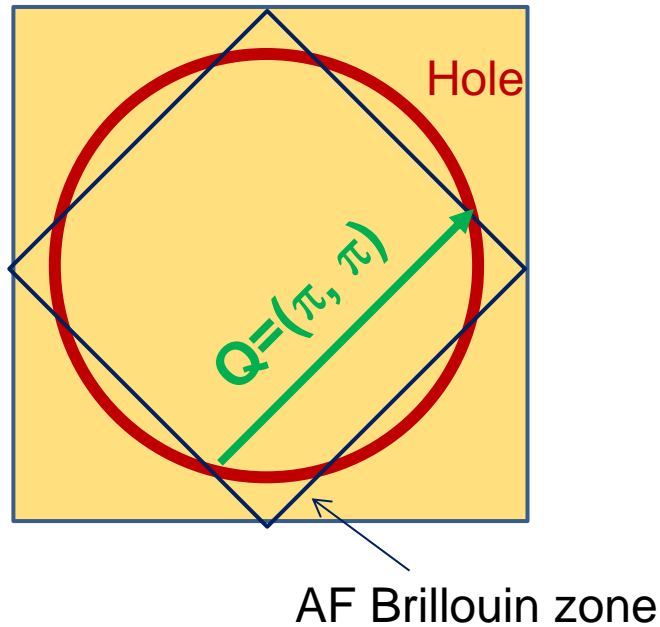
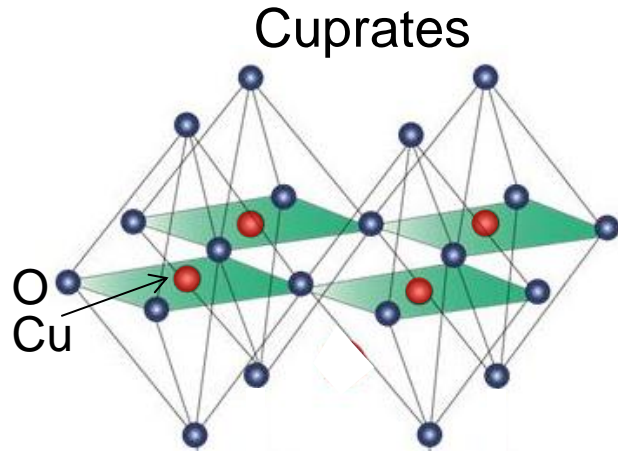
# Brillouin Zone of Fe pnictides



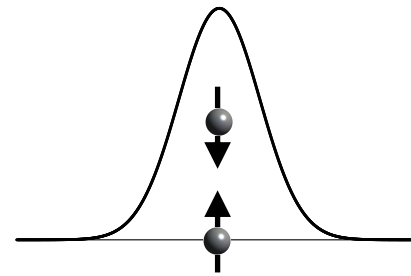
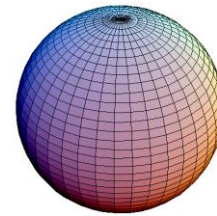
# Similarities and differences between cuprates and pnictides



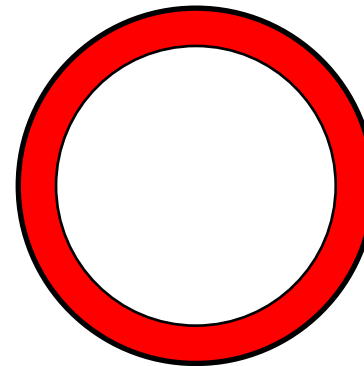
# Similarities and differences between cuprates and pnictides



***s-wave***

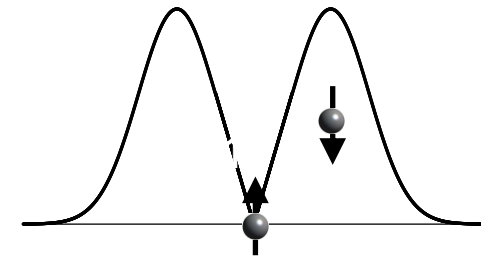
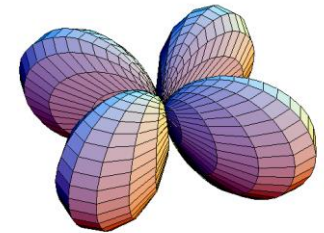


**Attractive**

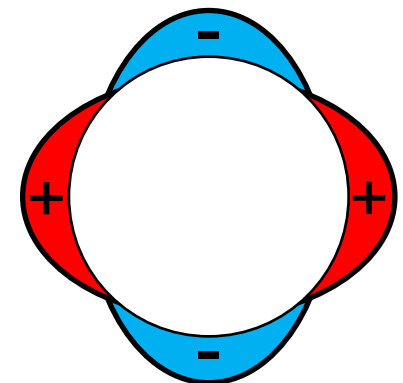


$\Delta = \text{const.}$

***d-wave***

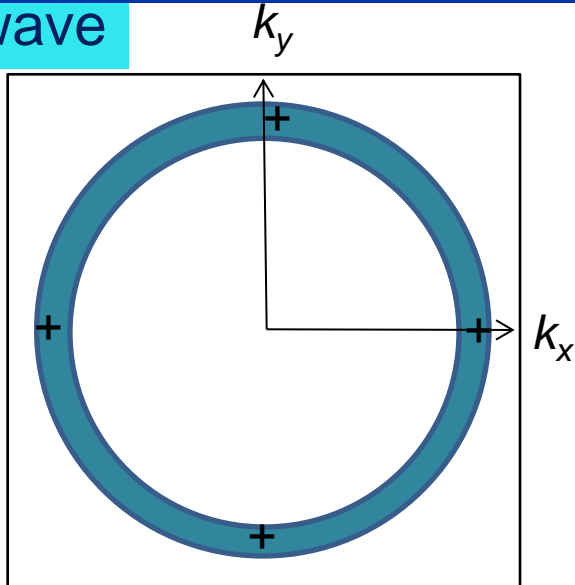


**Onsite repulsive**

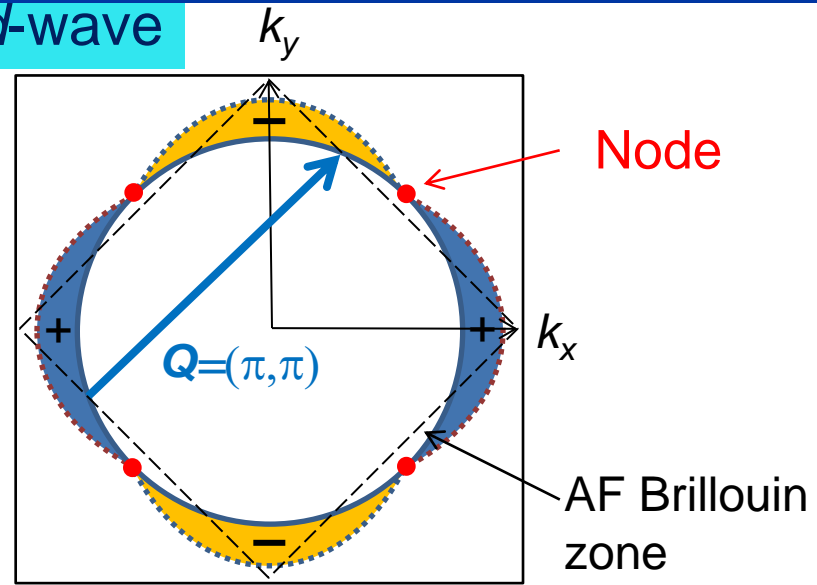


# $d$ -wave superconductivity in cuprates

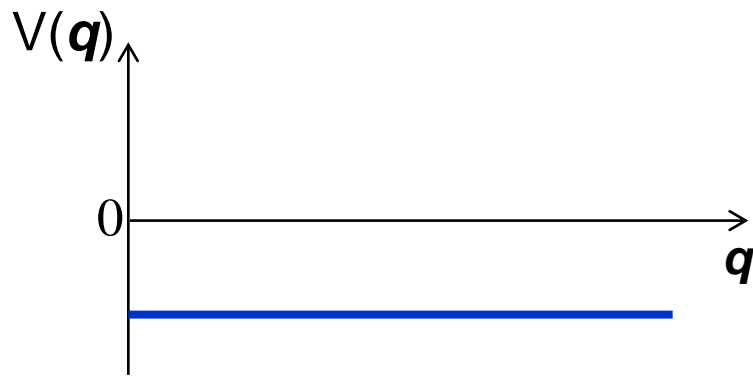
**s-wave**



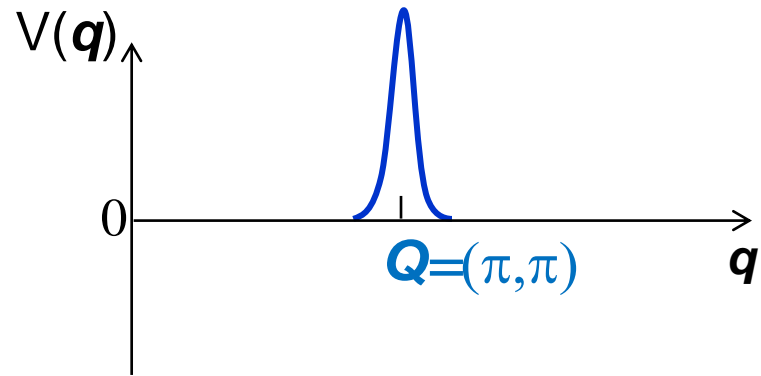
**d-wave**



$V(\mathbf{q})$ : pairing interaction



$V(\mathbf{q})$  is negative and constant

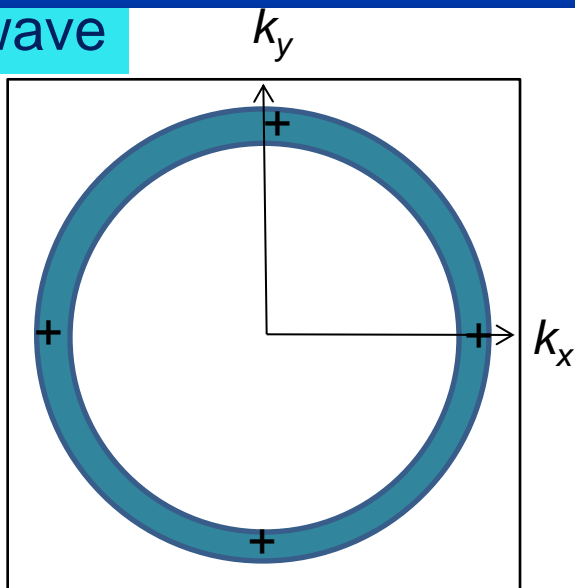


$V(\mathbf{q})$  is positive and peaks at  $\mathbf{q}=\mathbf{Q}$

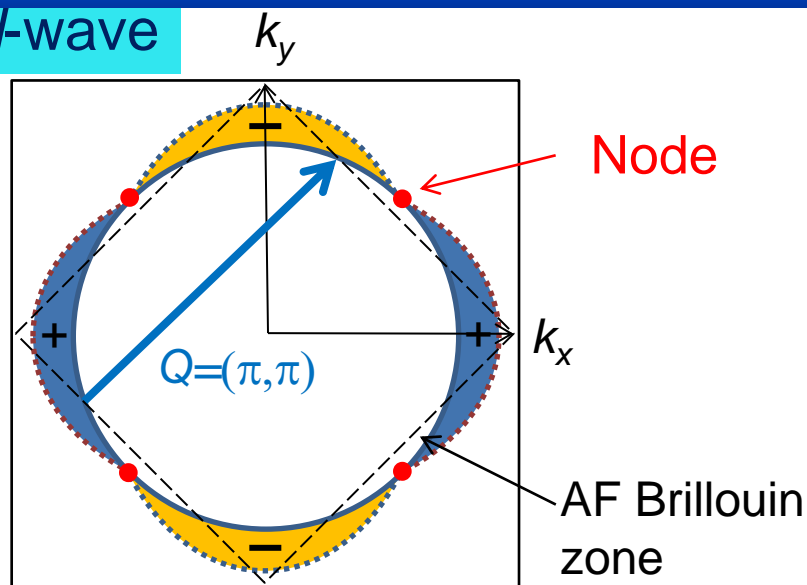
$$V_{kp} \simeq \frac{3}{2}U^2\chi(k-p) \quad \chi(q) \sim \delta(q-Q)$$

# d-wave superconductivity in cuprates

s-wave



d-wave



Gap equation

$$\Delta(k) = - \sum_p V_{kp} \frac{\tanh(\varepsilon_p/2T)}{2\varepsilon_p} \Delta(p) \quad \varepsilon_p = \sqrt{\Delta_p^2 + \xi_p^2}$$

$$\Delta(k) = \Delta$$

$$\Delta = - \sum_p V_{kp} \frac{\tanh(\varepsilon_p/2T)}{\varepsilon_p} \Delta$$

$$V_{kp} = V < 0$$

$$V(r) \sim -\delta(r)$$

$$V_{kp} \simeq \frac{3}{2} U^2 \chi(k-p) \quad \chi(q) \sim \delta(q-Q) \quad Q=(\pi, \pi)$$

Coulomb Magnetic fluctuation

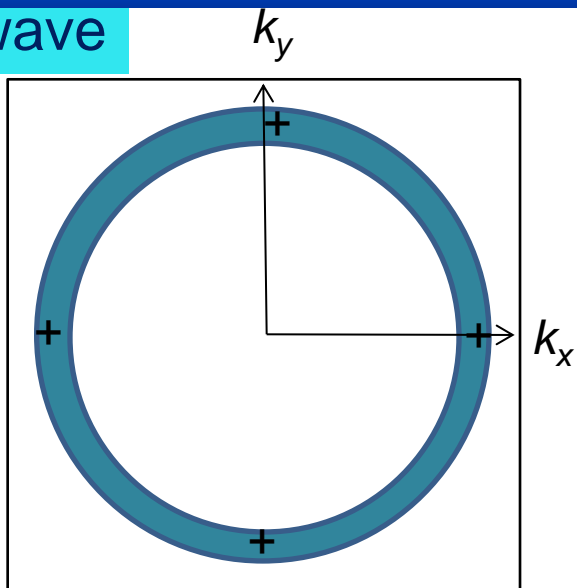
$$\begin{aligned} \Delta(k) &\sim - \sum_p U^2 \delta(k-p+Q) \frac{\tanh(\varepsilon_p/2T)}{2\varepsilon_p} \Delta(p) \\ &= -U^2 \frac{\tanh(\varepsilon_{k+Q}/2T)}{2\varepsilon_{k+Q}} \Delta(k+Q) \end{aligned}$$

$$\Delta(k+Q)\Delta(k) < 0 \quad \text{sign change}$$

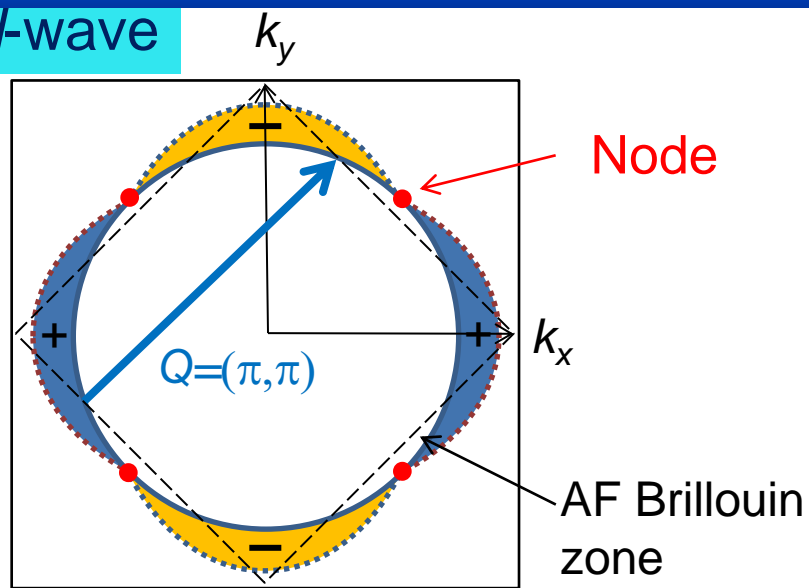
$$V(x, y) \sim \cos \pi(x+y) + \cos \pi(x-y)$$

# $d$ -wave superconductivity in cuprates

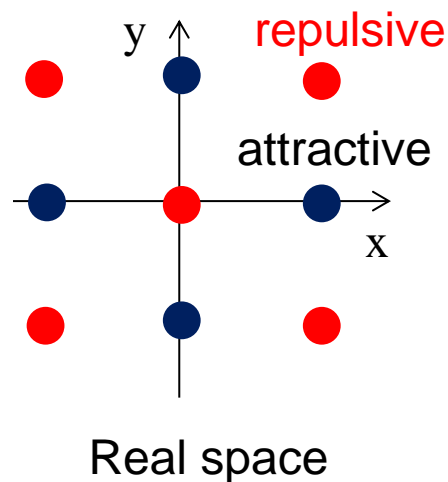
$s$ -wave



$d$ -wave

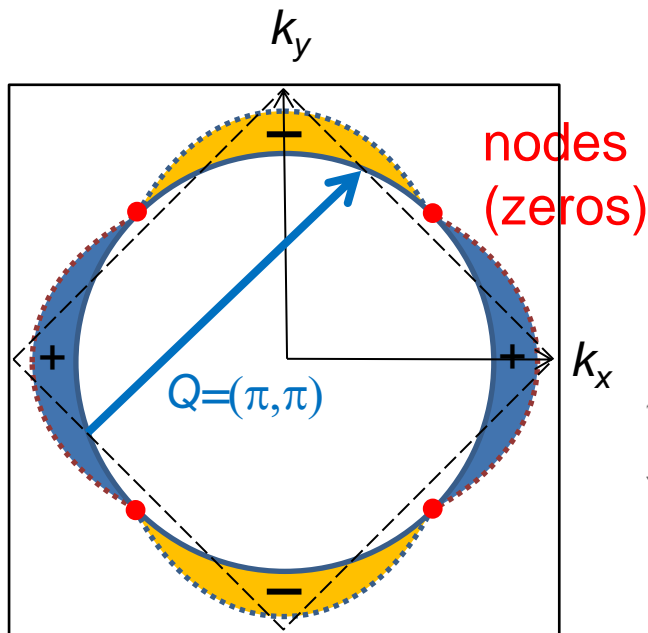


$$V(x, y) \sim \cos \pi(x + y) + \cos \pi(x - y)$$



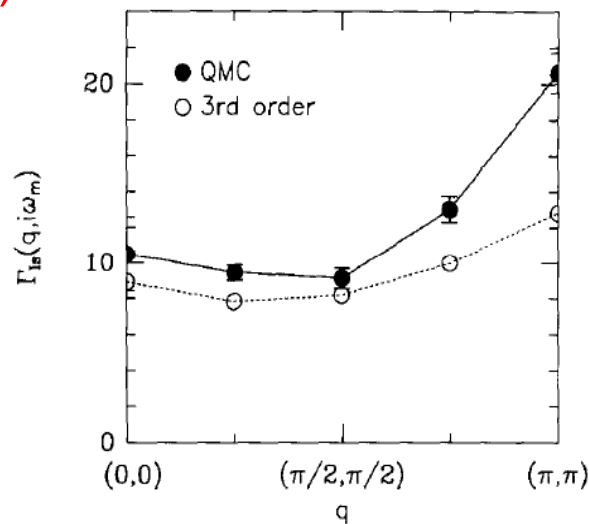


# d-wave superconductivity in cuprates



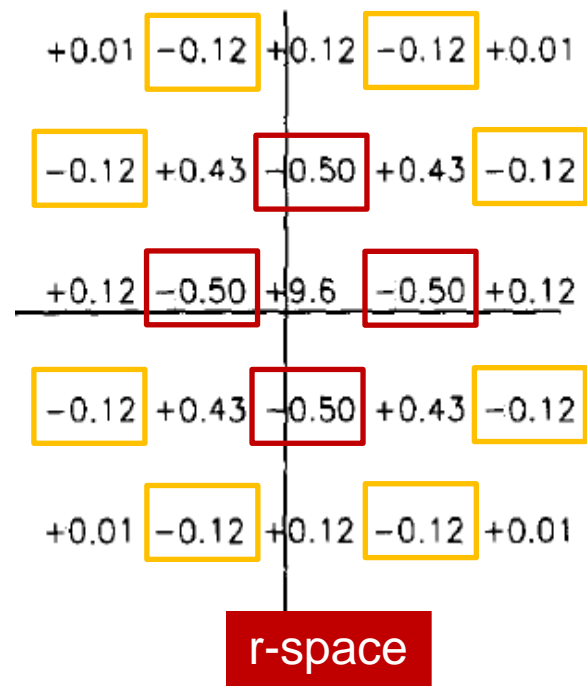
$d_{x^2-y^2} \quad (k_x^2 - k_y^2)$   
 zeros at  $k_x = +k_y, -k_y$

$V(q)$  broadly peaks at  $(\pi, \pi)$   
 Repulsive  $V(q) > 0$



q-space

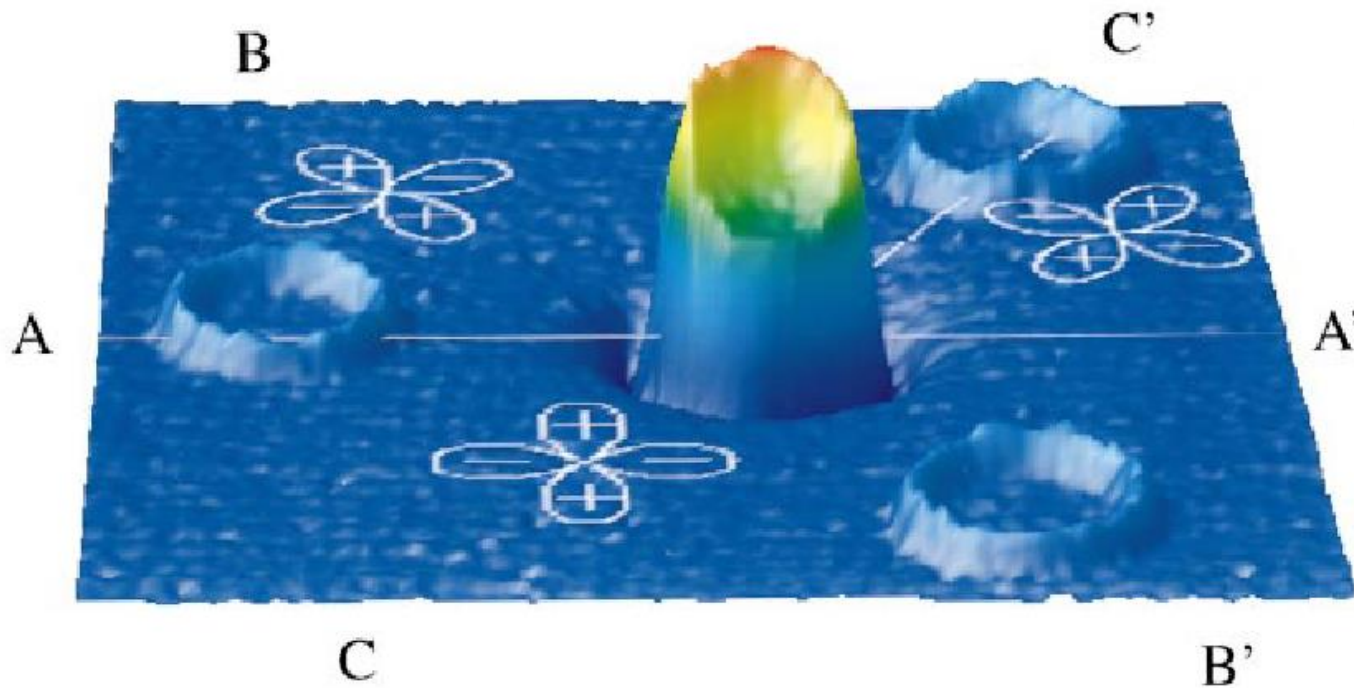
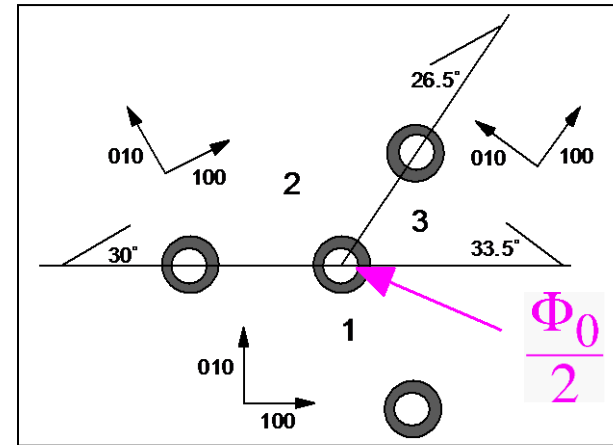
Repulsive on-site and  
 attractive off-site interaction



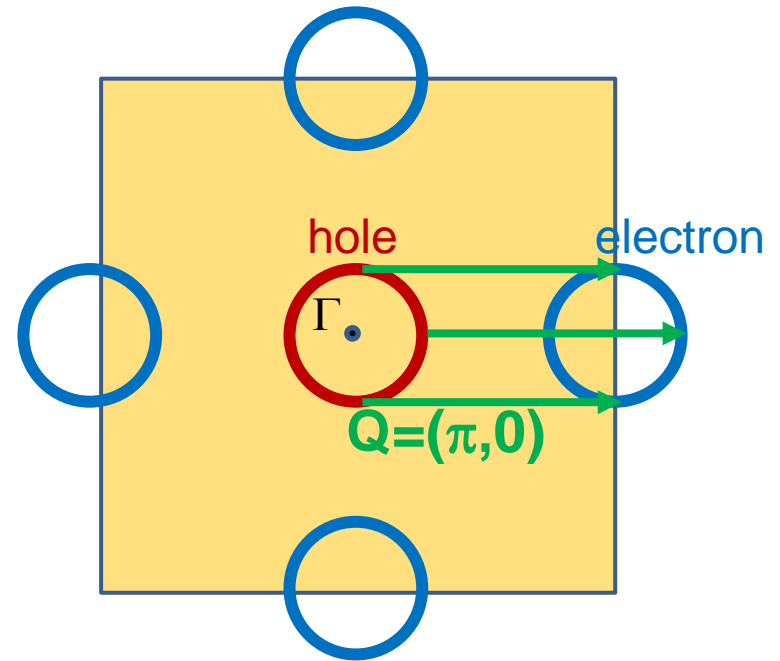
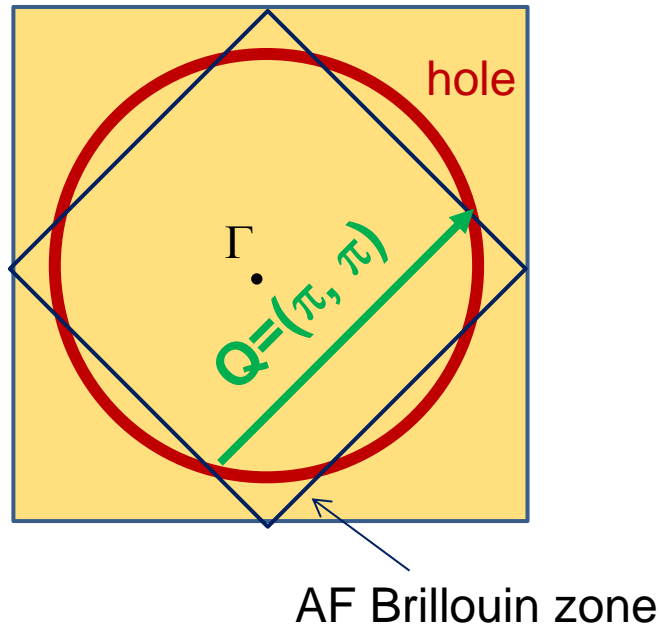
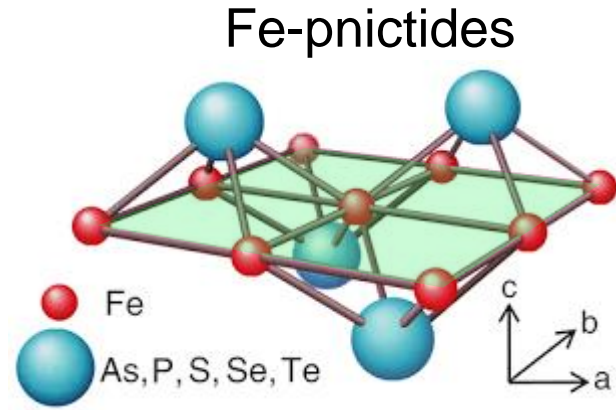
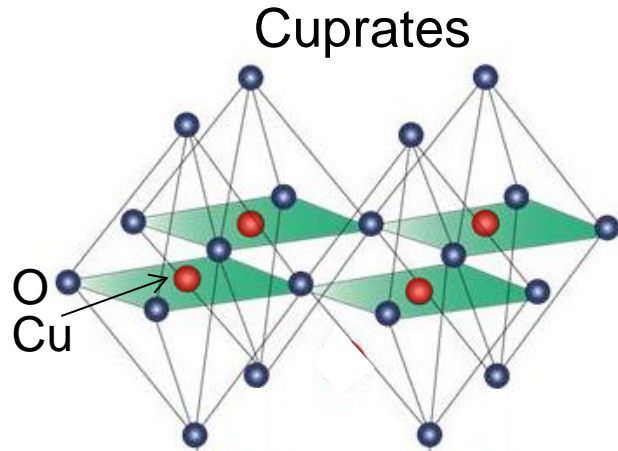
r-space

# *d*-wave superconductivity in cuprates

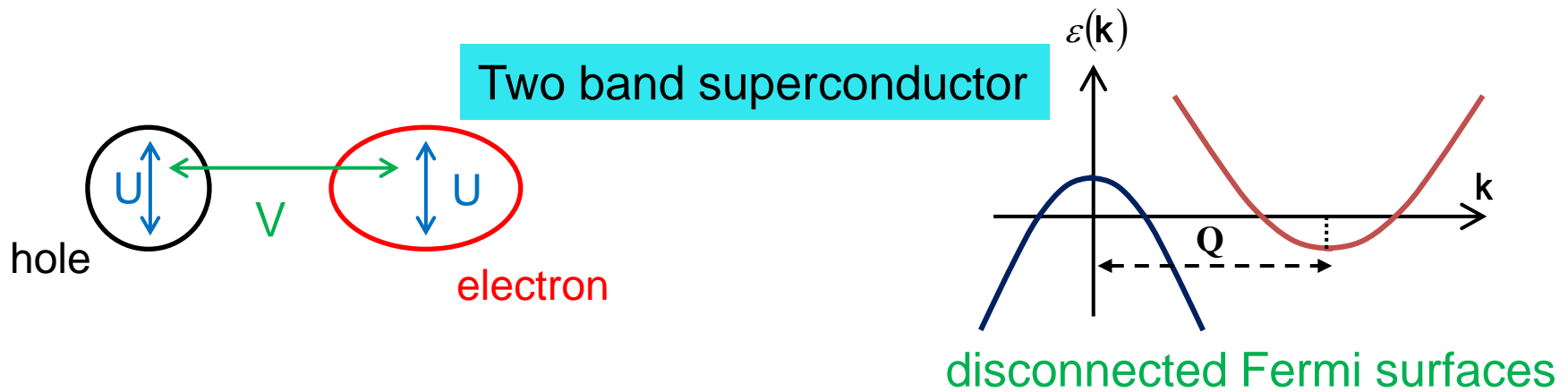
YBCO tricrystal  
superconducting ring  
(1994)



# Similarities and differences between cuprates and pnictides



# Iron pnictides: candidate for the SC state



Gap equation

$$\Delta_e = -V \Delta_h \sum_q \frac{\tanh \frac{\epsilon_q}{2T_c}}{\epsilon_q} - U \Delta_e \sum_q \frac{\tanh \frac{\epsilon_q}{2T_c}}{\epsilon_q}$$

$$\Delta_h = -V \Delta_e \sum_q \frac{\tanh \frac{\epsilon_q}{2T_c}}{\epsilon_q} - U \Delta_h \sum_q \frac{\tanh \frac{\epsilon_q}{2T_c}}{\epsilon_q}$$

$$U = 0$$

$$|V|N(0) \ln \frac{W}{T_c} = 1$$

$W$ : band width

At  $T_c$ :

$$\begin{pmatrix} \Delta_e \\ \Delta_h \end{pmatrix} = A \begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix} \begin{pmatrix} \Delta_e \\ \Delta_h \end{pmatrix} \quad A = \pm 1$$

$V > 0$   
repulsive

$$A = +1$$

$$\Delta_e = -\Delta_h$$

Sign change

$S_{\pm}$

$V < 0$   
attractive

$$A = -1$$

$$\Delta_e = \Delta_h$$

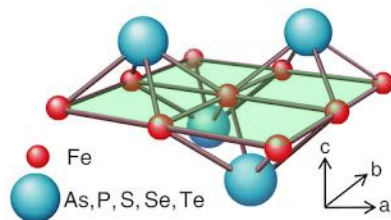
No sign change

$S_{++}$

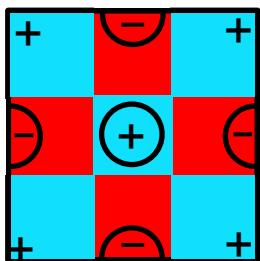
# Iron pnictides: candidate for the SC state

$S_{+-}$

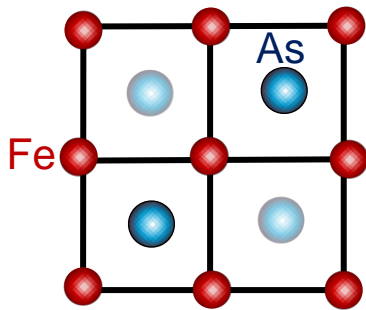
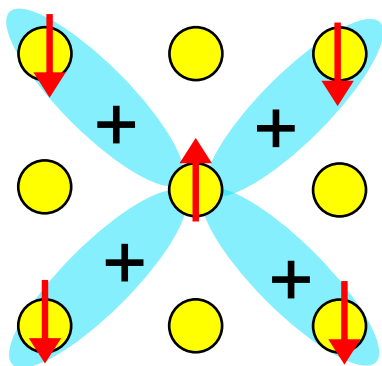
Fe-pnictides



$k$ -space (repulsive)



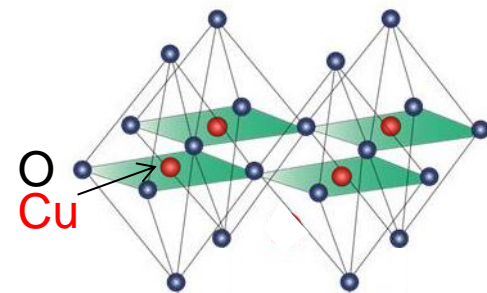
$r$ -space



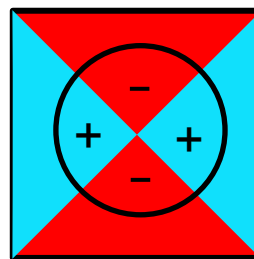
$$\Delta(\cos k_x \cos k_y)$$

$d_{x^2-y^2}$

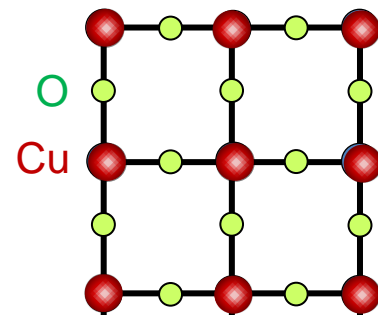
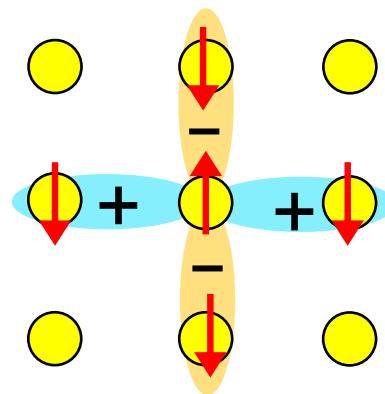
Cuprates



$k$ -space (repulsive)



$r$ -space

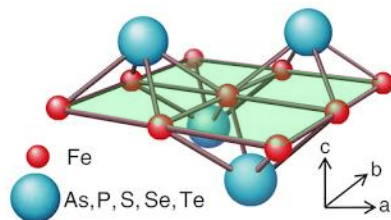


$$\Delta(\cos k_x - \cos k_y)$$

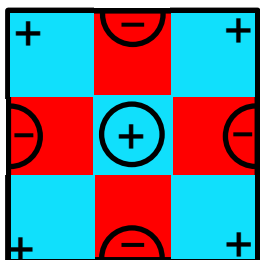
# Iron pnictides: candidate for the SC state

$S_{+-}$

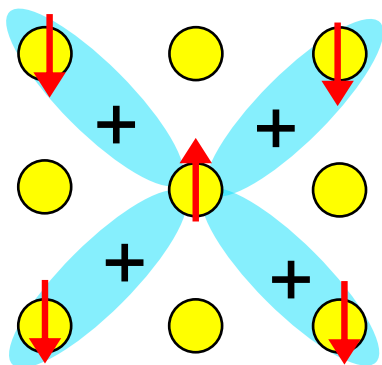
Fe-pnictides



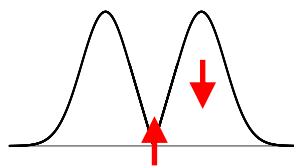
$k$ -space (repulsive)



$r$ -space

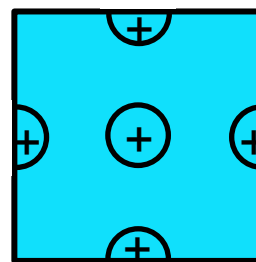


$$\Delta(\cos k_x \cos k_y)$$

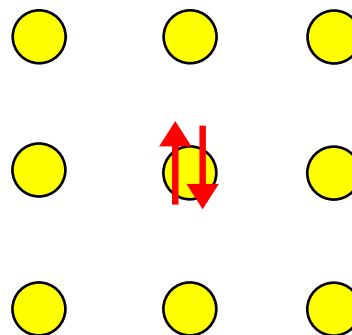


$S_{++}$

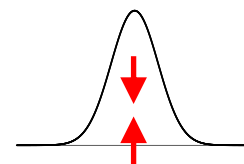
$k$ -space (attractive)



$r$ -space



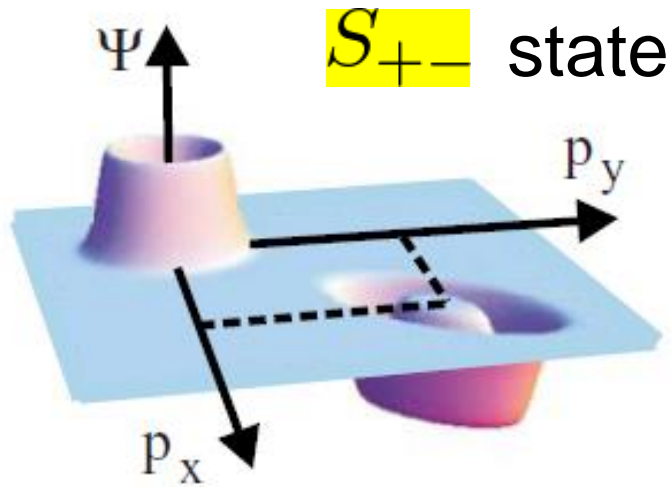
$$\Delta$$



# Iron pnictides: candidate for the SC state

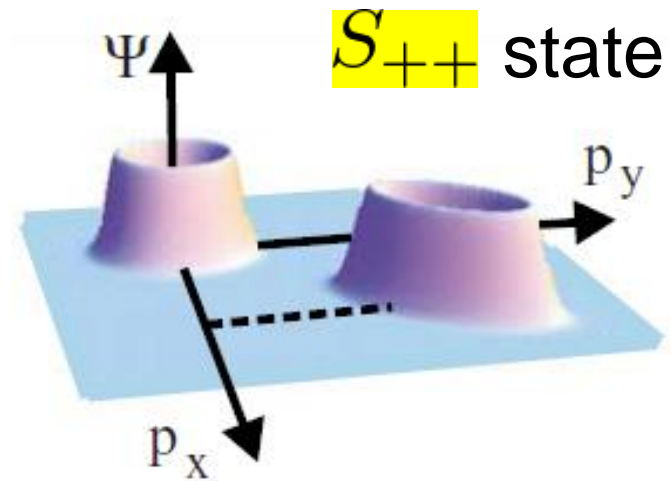
- Pairing due to purely **repulsive** interaction

$$V > 0$$



- Pairing due to **attractive** interaction

$$V < 0$$



I. I. Mazin *et al.*, PRL **101**, 057003 (2008).

K. Kuroki *et al.*, PRL **101**, 087004 (2008).

& PRB **79**, 224511 (2009).

A. V. Chubkov *et al.*, PRB **80**, 140515(R) (2009).

S. Graser *et al.*, NJP **11**, 025016 (2009).

H. Ikeda, PRB **81**, 054502 (2010).

K. Seo *et al.*, PRL **101**, 206404 (2008).

F. Wang *et al.*, PRL **102**, 047005 (2009).

⋮

H. Kontani & S. Onari, PRL **104**, 157001 (2010).

F. Kruger *et al.*, PRB **79**, 054504 (2009).

Y. Yanagi *et al.*, PRB **81**, 054518 (2010).

⋮



# Physics of iron-based high temperature superconductors

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1) Introduction

2) Similarities and differences between cuprates and Fe-pnictides

3) **Normal state properties**

**Electronic structure** and magnetism

4) Superconducting properties

Superconducting gap structure

5) Some recent topics

QCP, BCS-BEC crossover,

A novel high field SC state, Nematicity . . . .



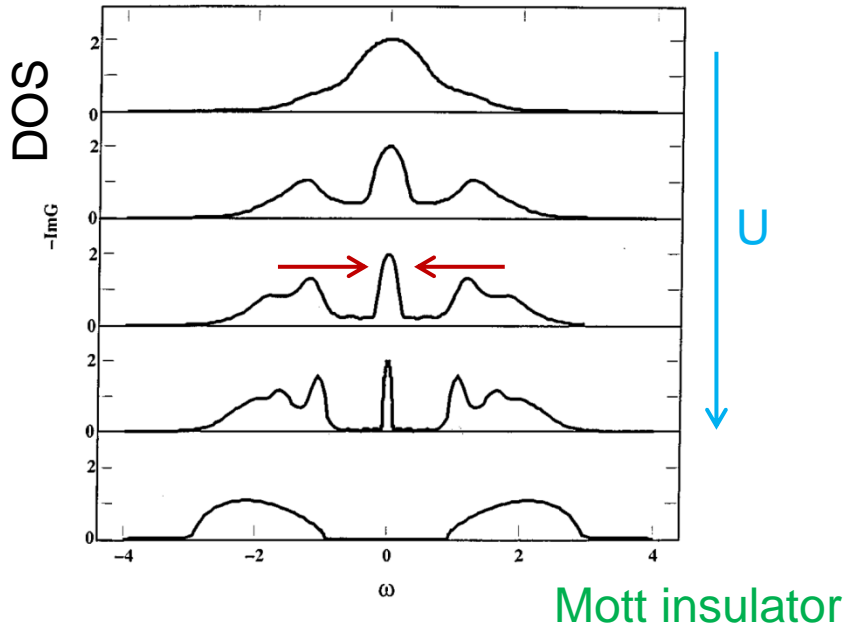
# Electron correlations

## Electron correlations change the band structure

Band narrowing

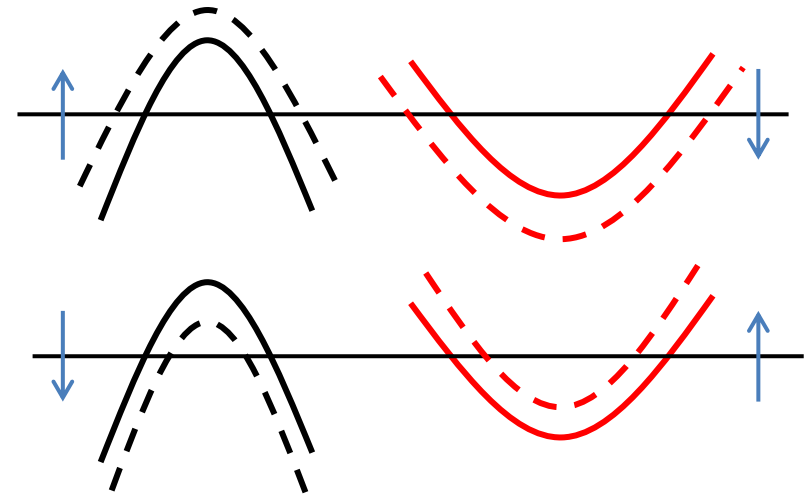
Mass enhancement

Metal



Band shift

Particularly important for multiband system



A. Georges, G. Kotliar, W. Krauth and M.J. Rozenberg, Rev. Mod. Phys. 68, 13 (1996)

LDA calculation (major part of electron correlation is dropped.)

LDA: local density approximation

Difference between LDA and measured Fermi surface is a measure of the influence of the electron correlation.

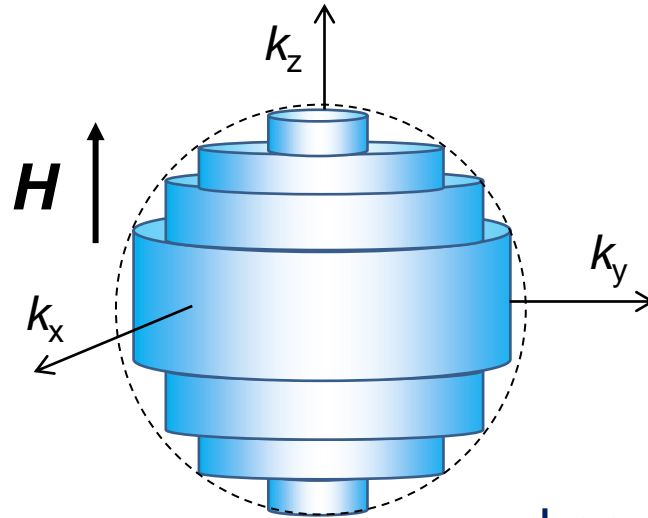
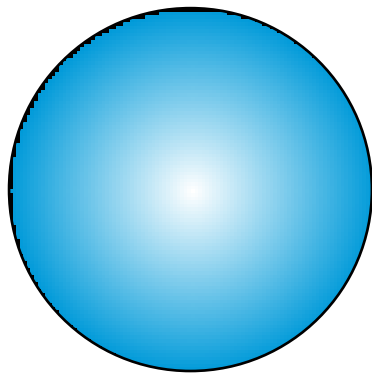
# Determination of Fermi surface

## Quantum oscillations

### Landau quantization

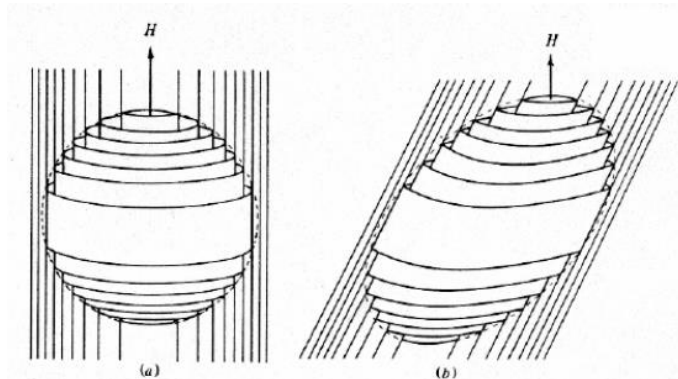
Quantization of the orbital motion of electrons in magnetic field

$$E = (n + 1/2)\hbar\omega_c \quad \omega_c = \frac{eB}{m^*c}$$



Allowed orbits are in the plane perpendicular to the magnetic field direction on a series space of constant energy surfaces in  $k$ -space.

### Landau tubes



De Haas–van Alphen effect  
Magnetization

Shubnikov–de Haas effect  
Resistivity

# Determination of Fermi surface

Lifshits-Kosevich formula (1954)

$$\Delta \left( \frac{1}{B} \right) = \frac{2\pi e}{\hbar c S}$$

$$M_{osc} = A \sin \left( \frac{2\pi F}{H} + \Phi \right)$$

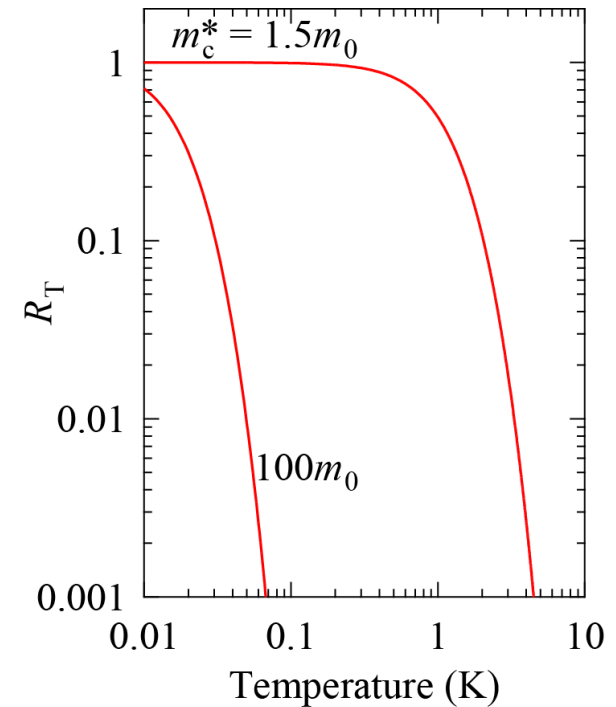
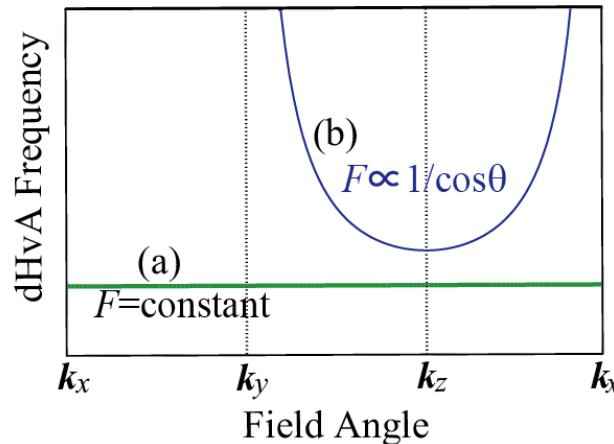
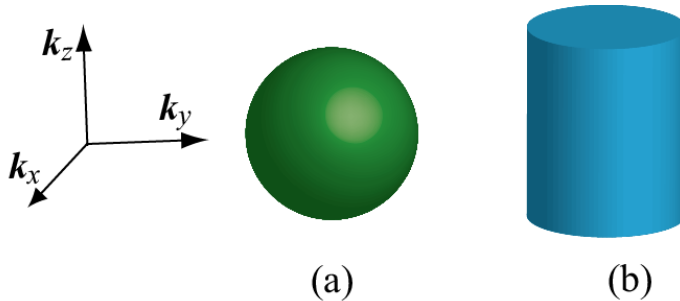
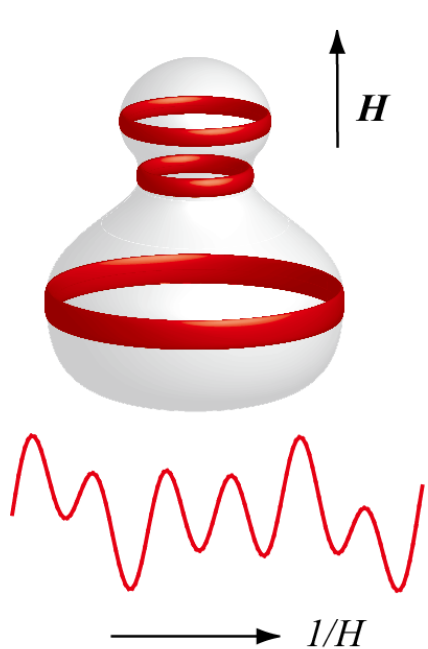
$$F = \frac{\hbar c}{2\pi e} S_F$$

$$A \propto J_2(x) T H^{-1/2} \left| \frac{\partial^2 S}{\partial k_H^2} \right|^{-1/2} R_T R_D R_S$$

Oscillatory (dHvA) frequency

$S_F$

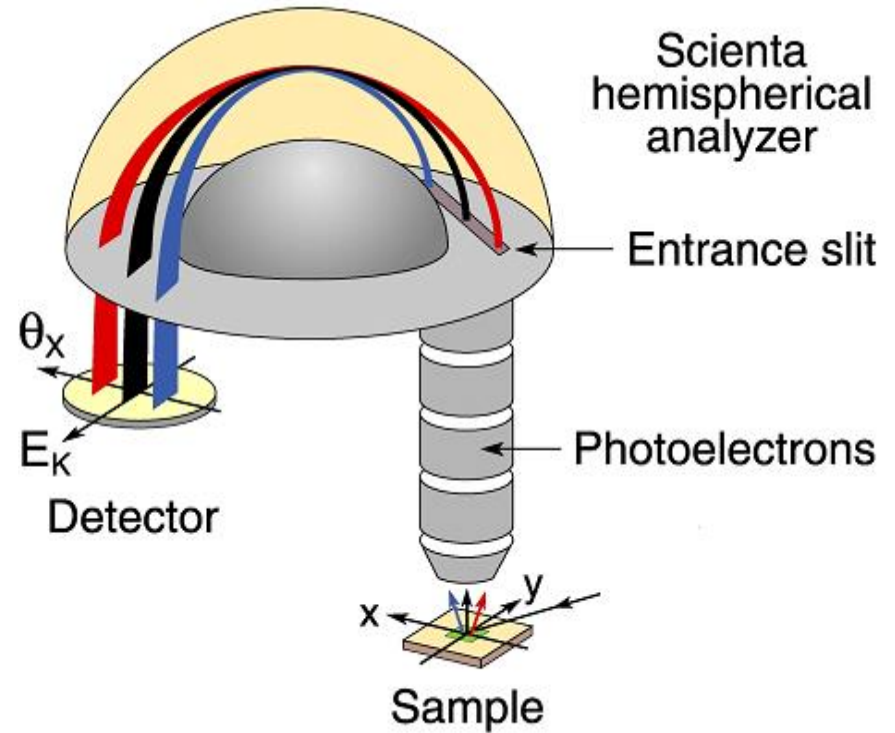
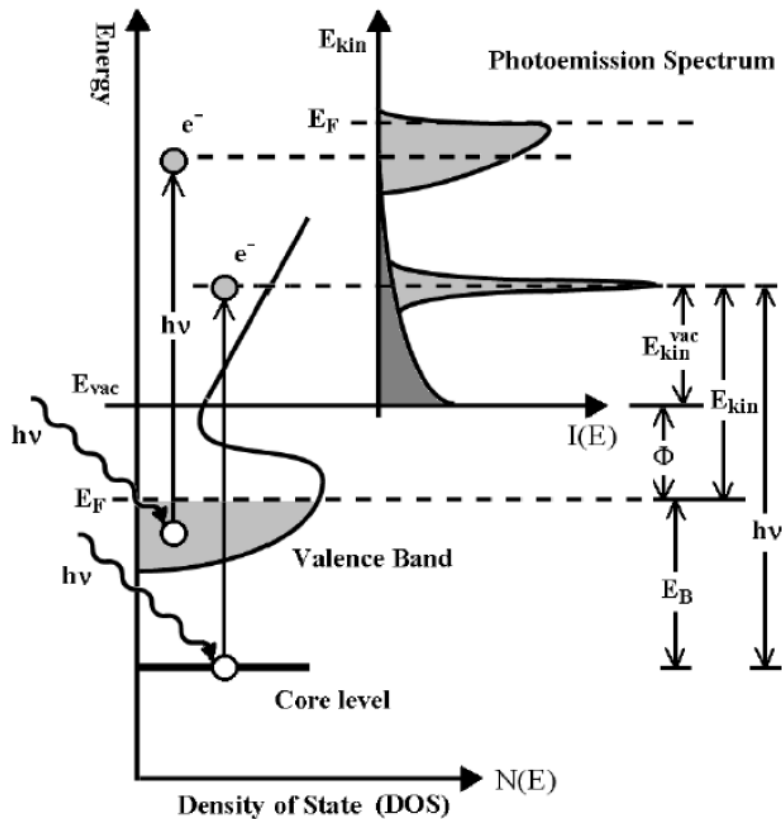
Fermi surface extremal cross section



$$R_T = \frac{\alpha m_c^* T}{H} \times \frac{1}{\sinh \left( \alpha m_c^* \frac{T}{H} \right)}$$

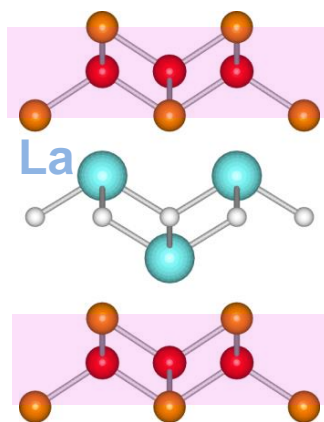
# Determination of Fermi surface

## Angle resolved photoemission spectroscopy



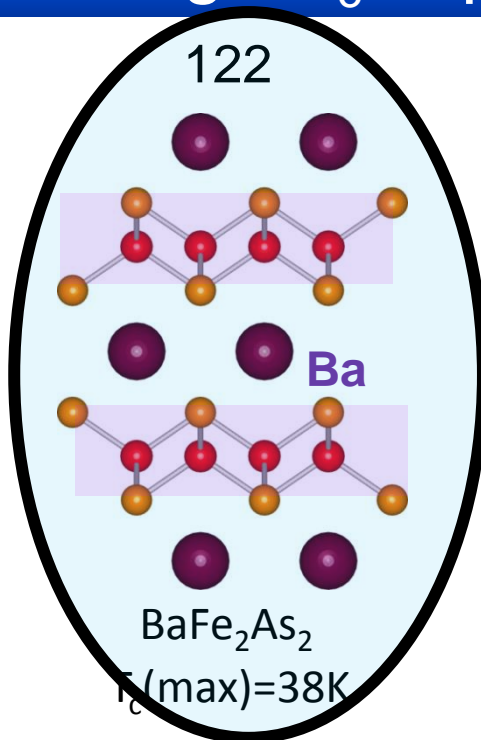
# Fe-based high- $T_c$ superconductors

1111



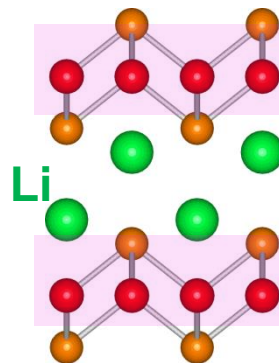
$Ln$  FeAsO  
 $T_c(\text{max})=55\text{K}$

122

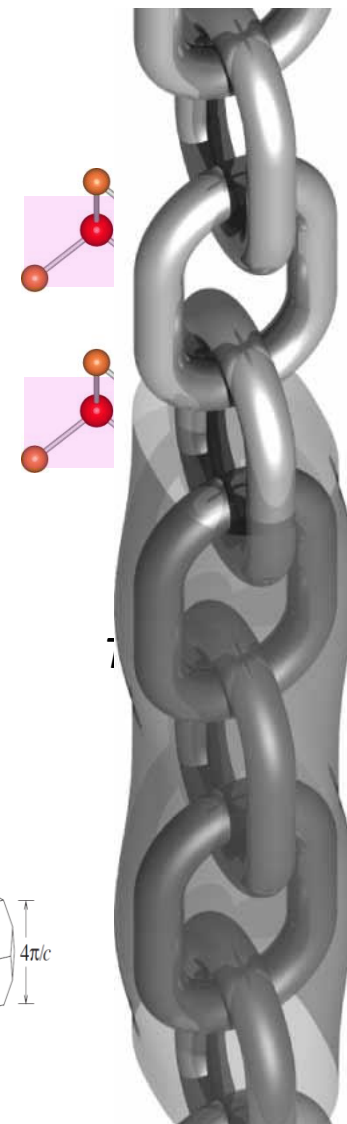


BaFe<sub>2</sub>As<sub>2</sub>  
 $T_c(\text{max})=38\text{K}$

111



LiFeAs  
 $T_c=18\text{K}$

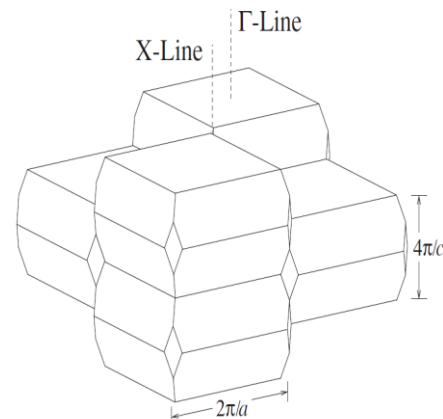
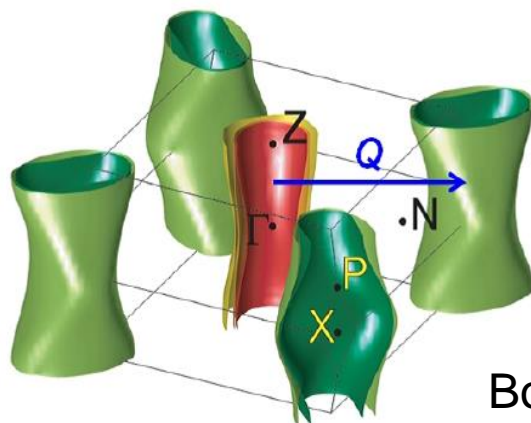


**Parent compound**  
**BaFe<sub>2</sub>As<sub>2</sub>**  
**(AF Metal)**

**Correlated metal**

Similar to overdoped  
cuprates

D.N.Basov *et al.*  
Nature Phys. (09)



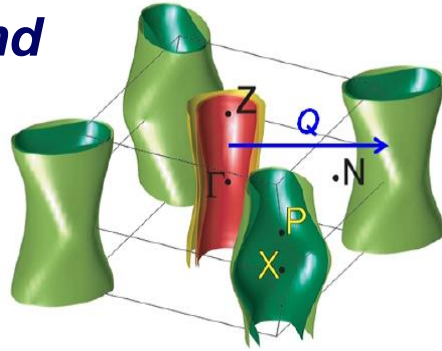
Body-centered  
tetragonal

The 'snake that  
swallowed a chain'

# Superconductivity in BaFe<sub>2</sub>As<sub>2</sub> systems

Parent compound

BaFe<sub>2</sub>As<sub>2</sub>  
(AF Metal)



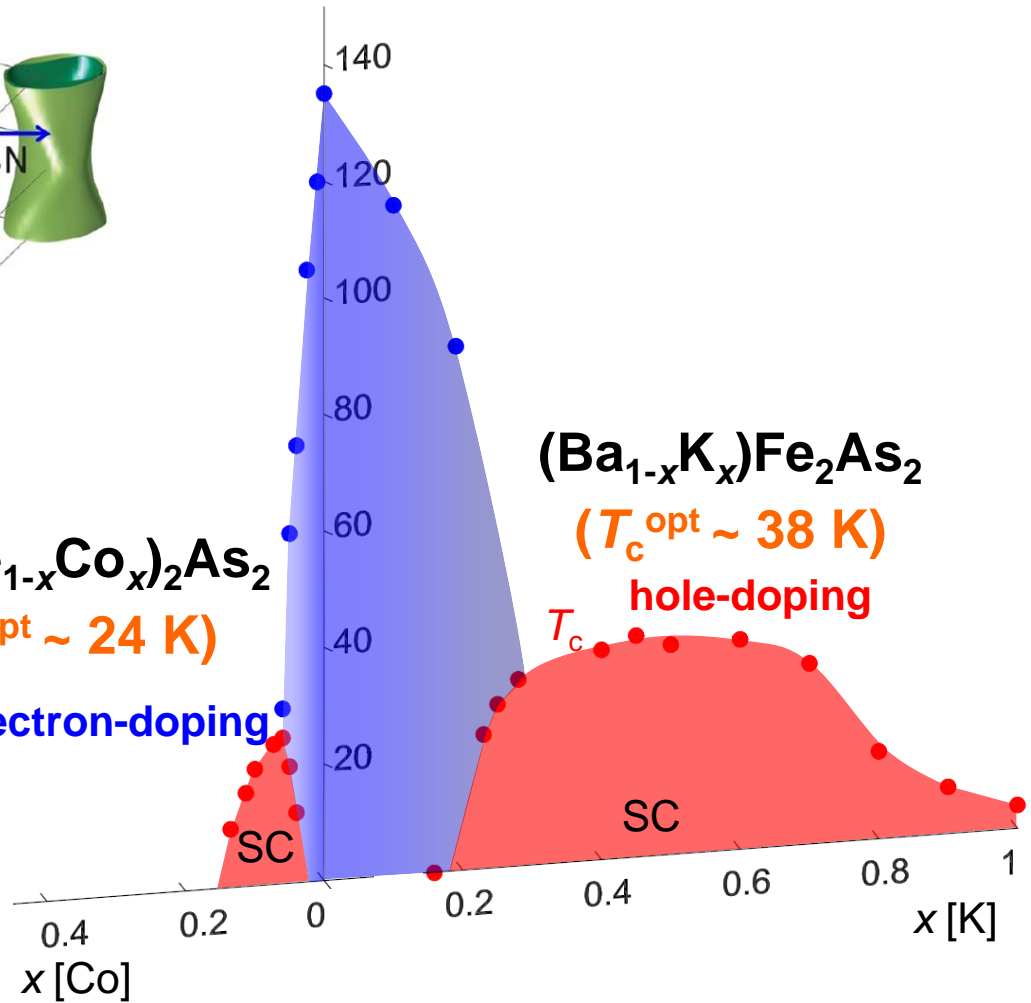
Ba(Fe<sub>1-x</sub>Co<sub>x</sub>)<sub>2</sub>As<sub>2</sub>  
( $T_c^{opt} \sim 24$  K)

electron-doping

(Ba<sub>1-x</sub>K<sub>x</sub>)Fe<sub>2</sub>As<sub>2</sub>

( $T_c^{opt} \sim 38$  K)

hole-doping

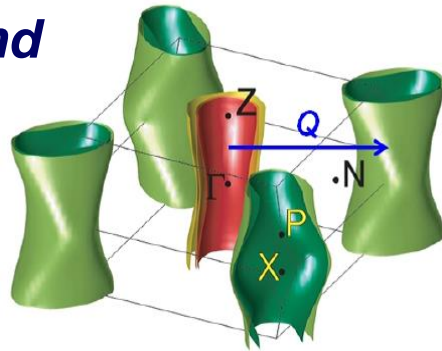




# Superconductivity in BaFe<sub>2</sub>As<sub>2</sub> systems

Parent compound

BaFe<sub>2</sub>As<sub>2</sub>  
(AF Metal)



Ba(Fe<sub>1-x</sub>Co<sub>x</sub>)<sub>2</sub>As<sub>2</sub>  
( $T_c^{opt} \sim 24$  K)

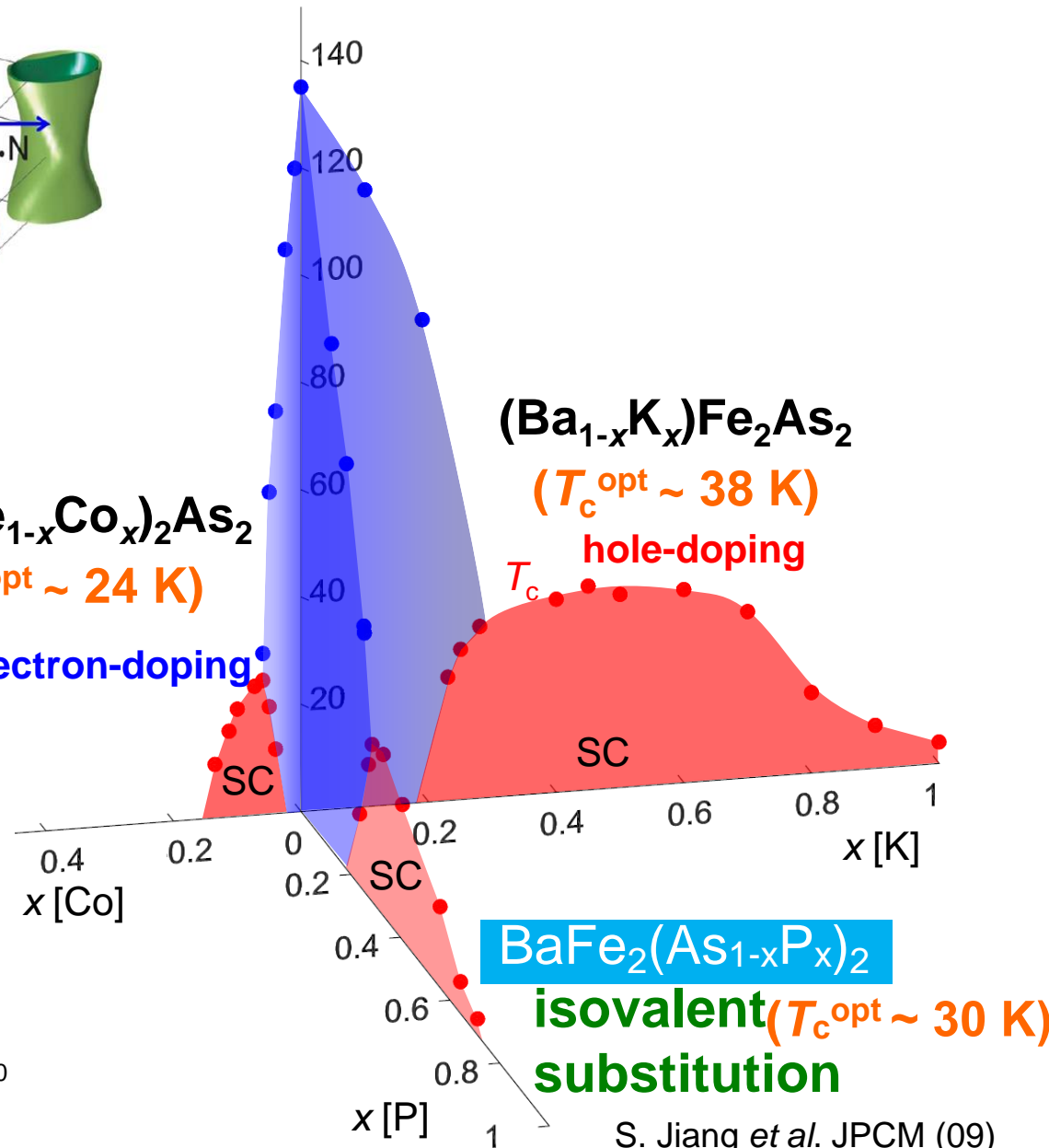
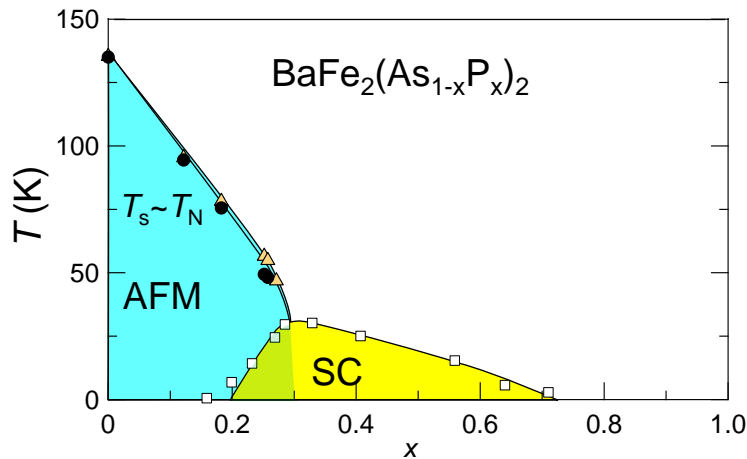
electron-doping

(Ba<sub>1-x</sub>K<sub>x</sub>)Fe<sub>2</sub>As<sub>2</sub>

( $T_c^{opt} \sim 38$  K)

hole-doping

$T_c$



S. Jiang *et al.* JPCM (09)

Ground state can be tuned without doping carriers

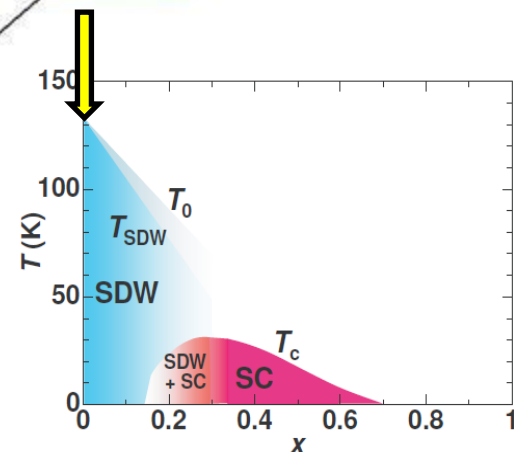
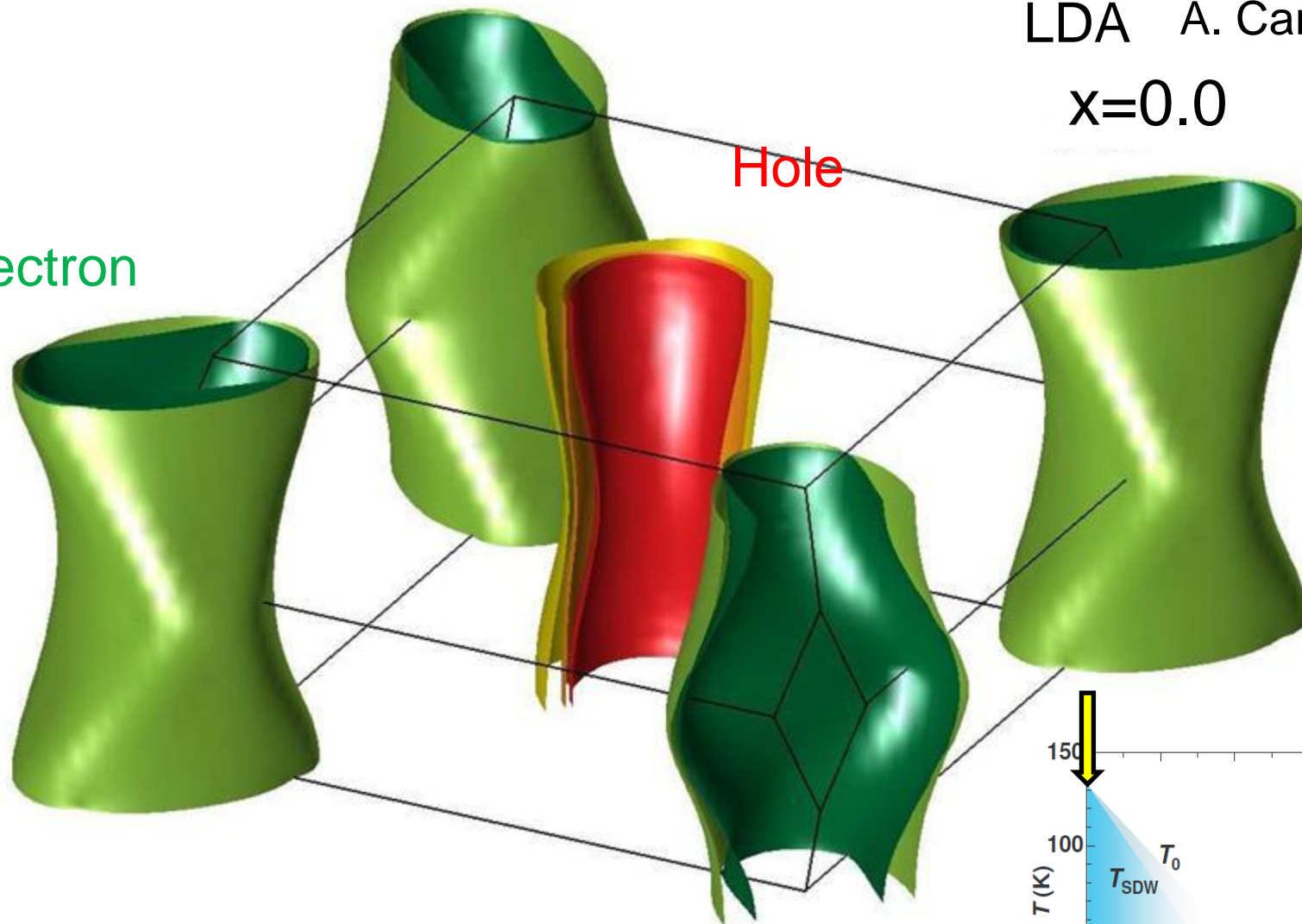
# BaFe<sub>2</sub> (As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>

LDA A. Carrington

x=0.0

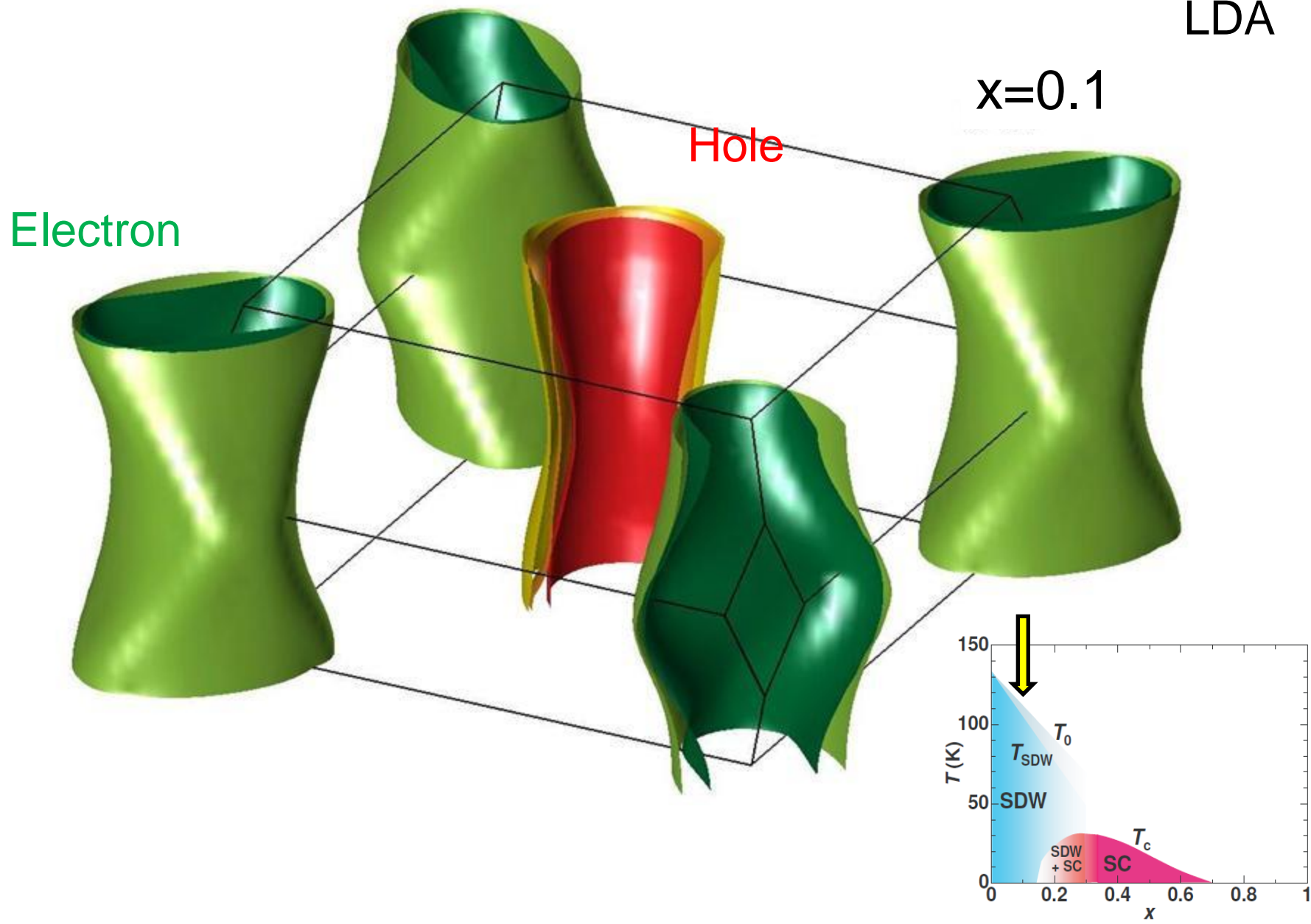
Electron

Hole



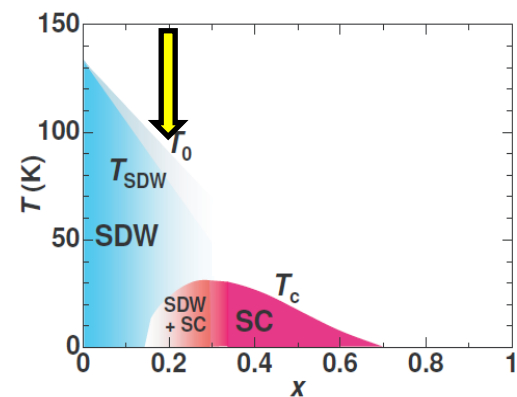
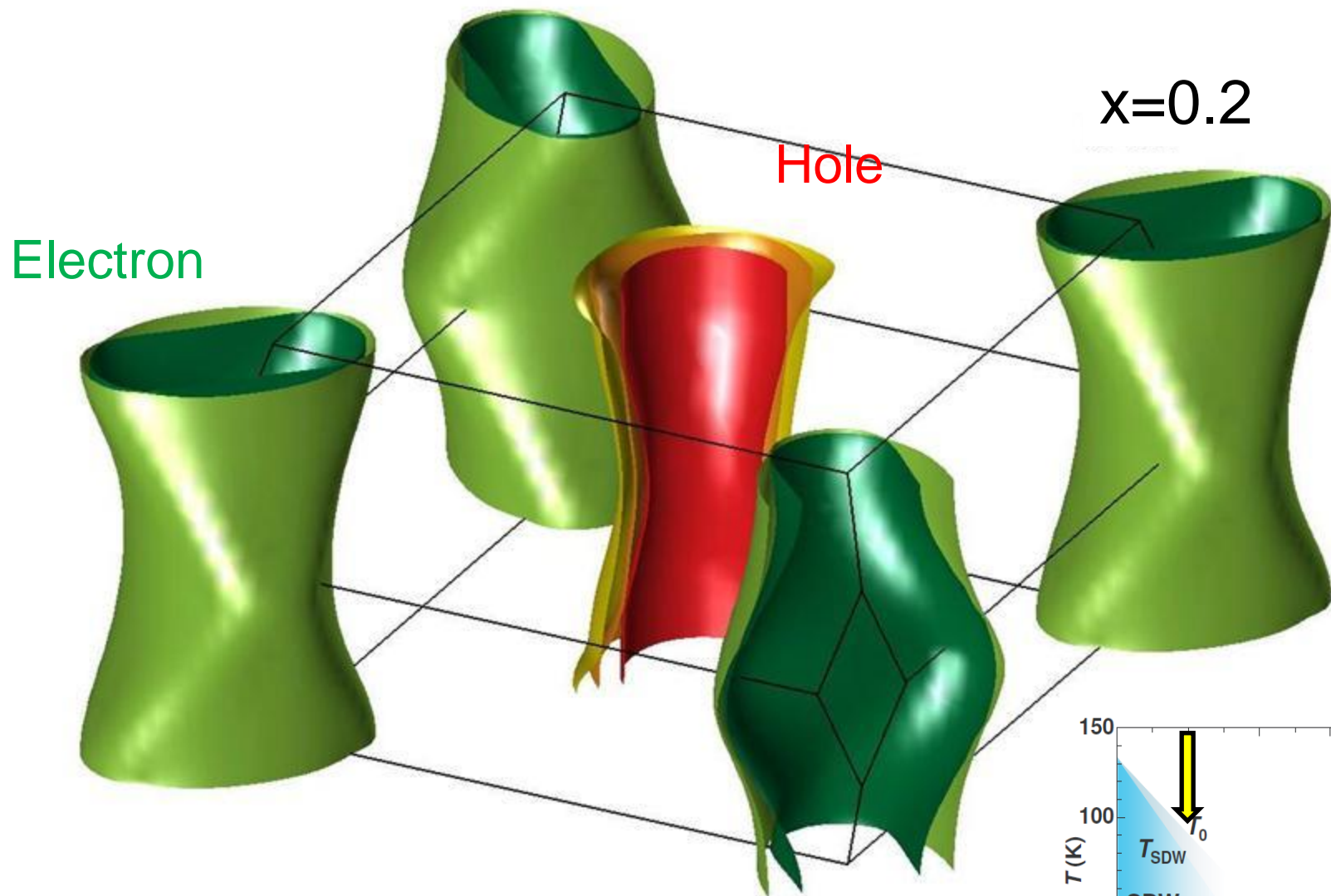
# BaFe<sub>2</sub> (As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>

LDA



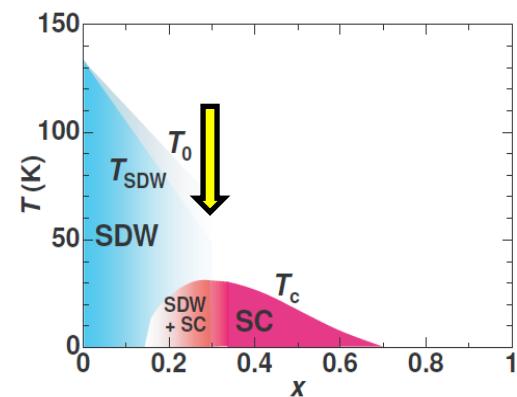
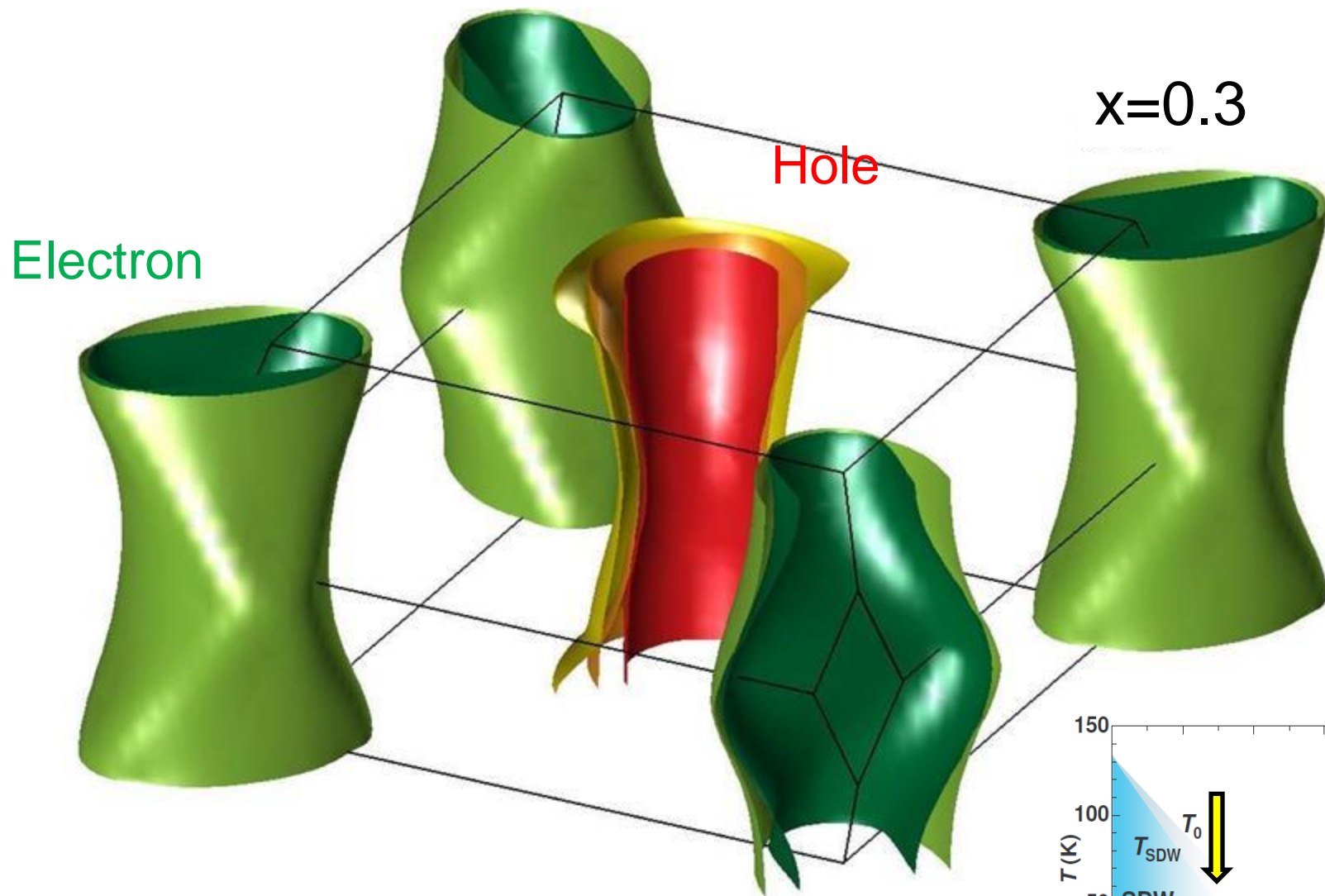
# BaFe<sub>2</sub> (As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>

LDA



# BaFe<sub>2</sub> (As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>

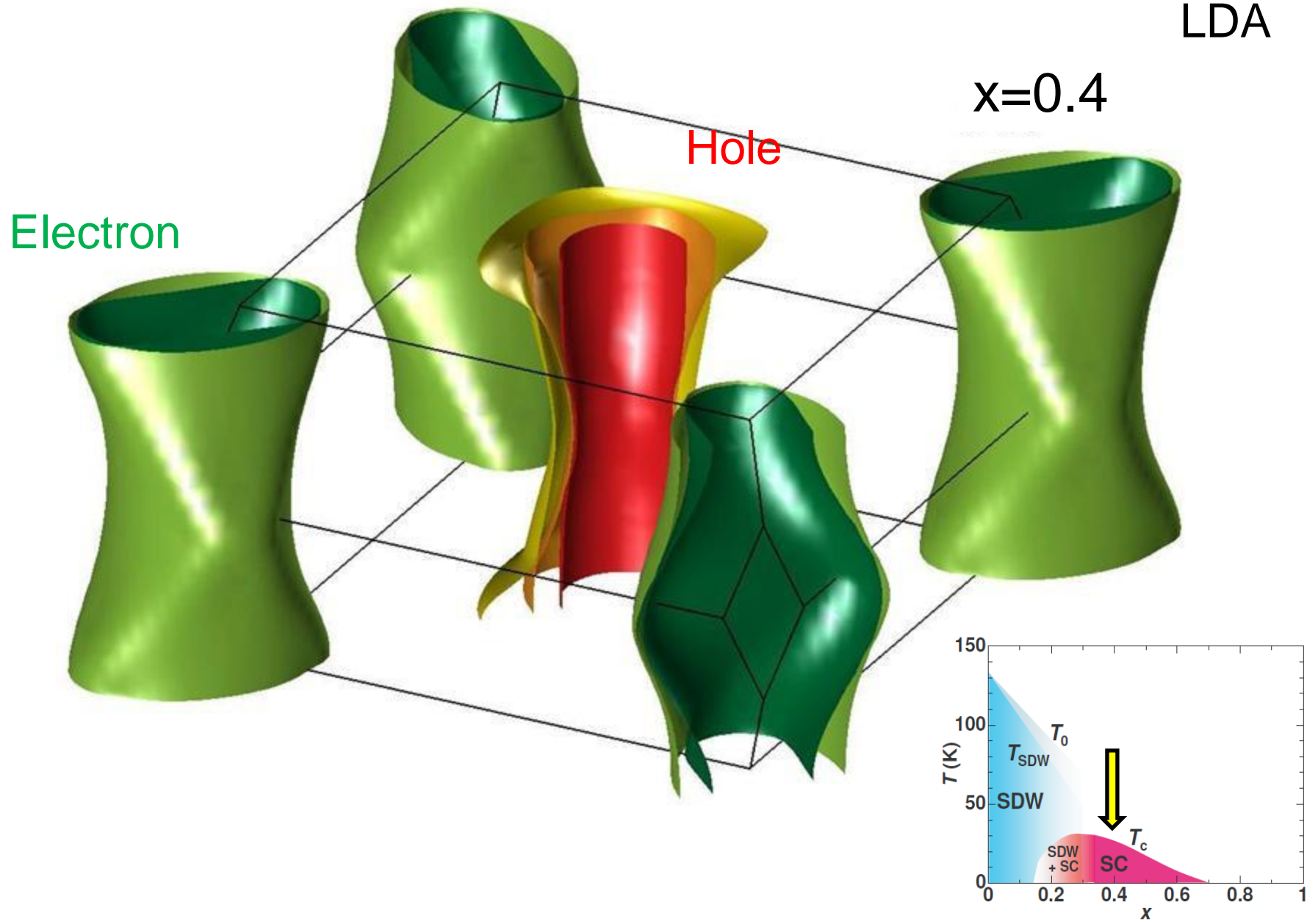
LDA





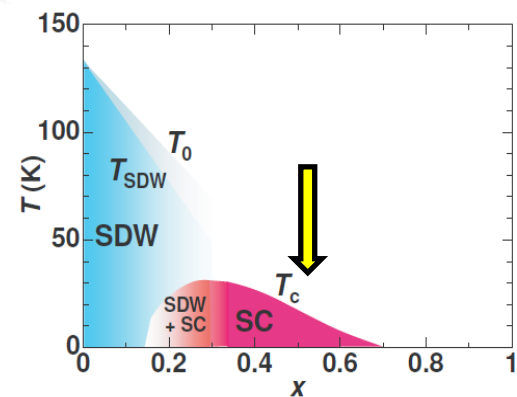
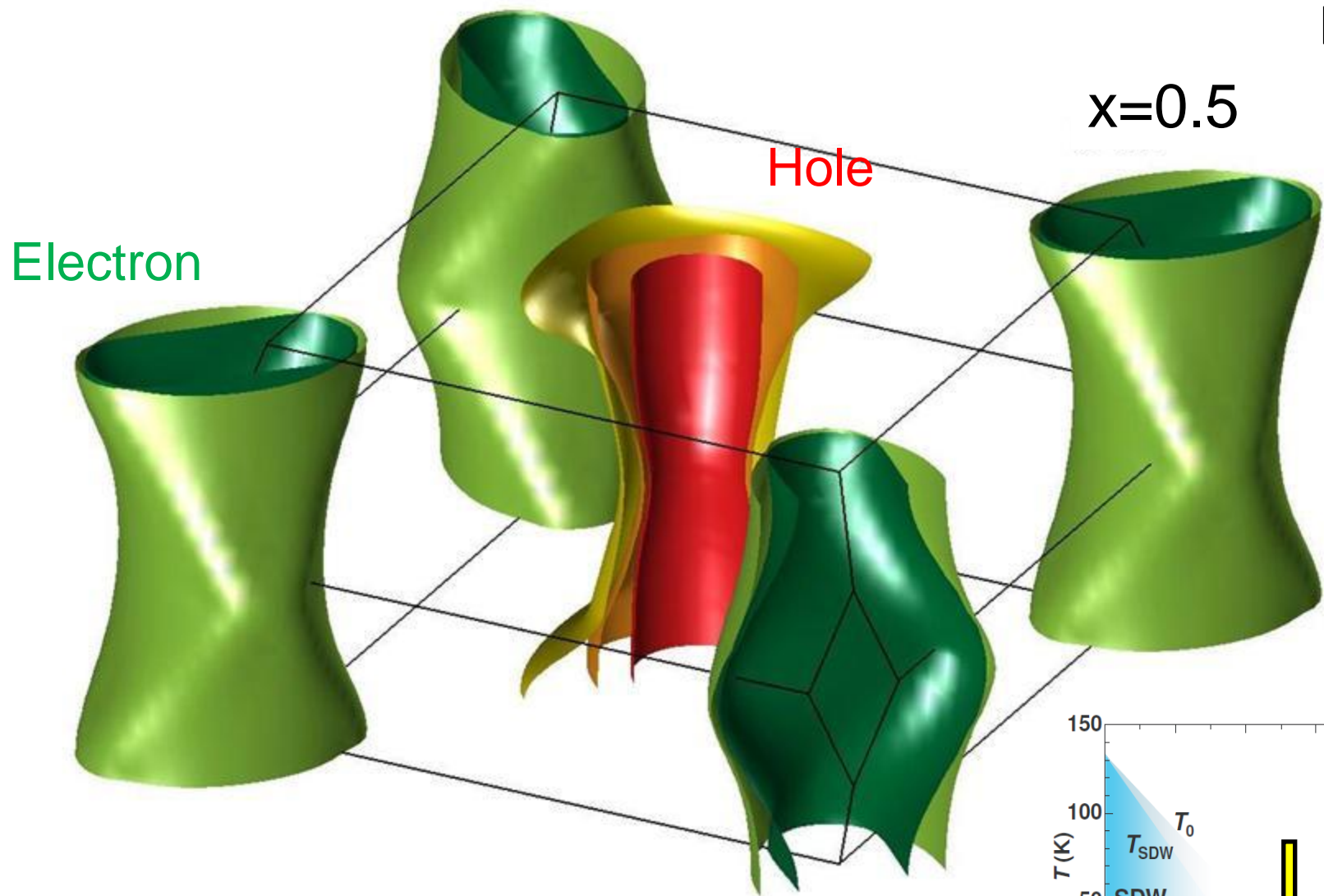
# BaFe<sub>2</sub> (As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>

LDA



# BaFe<sub>2</sub> (As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>

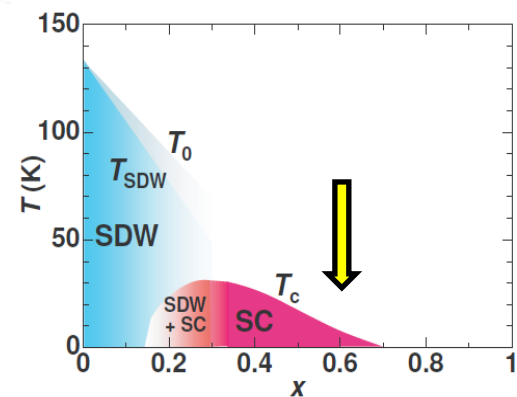
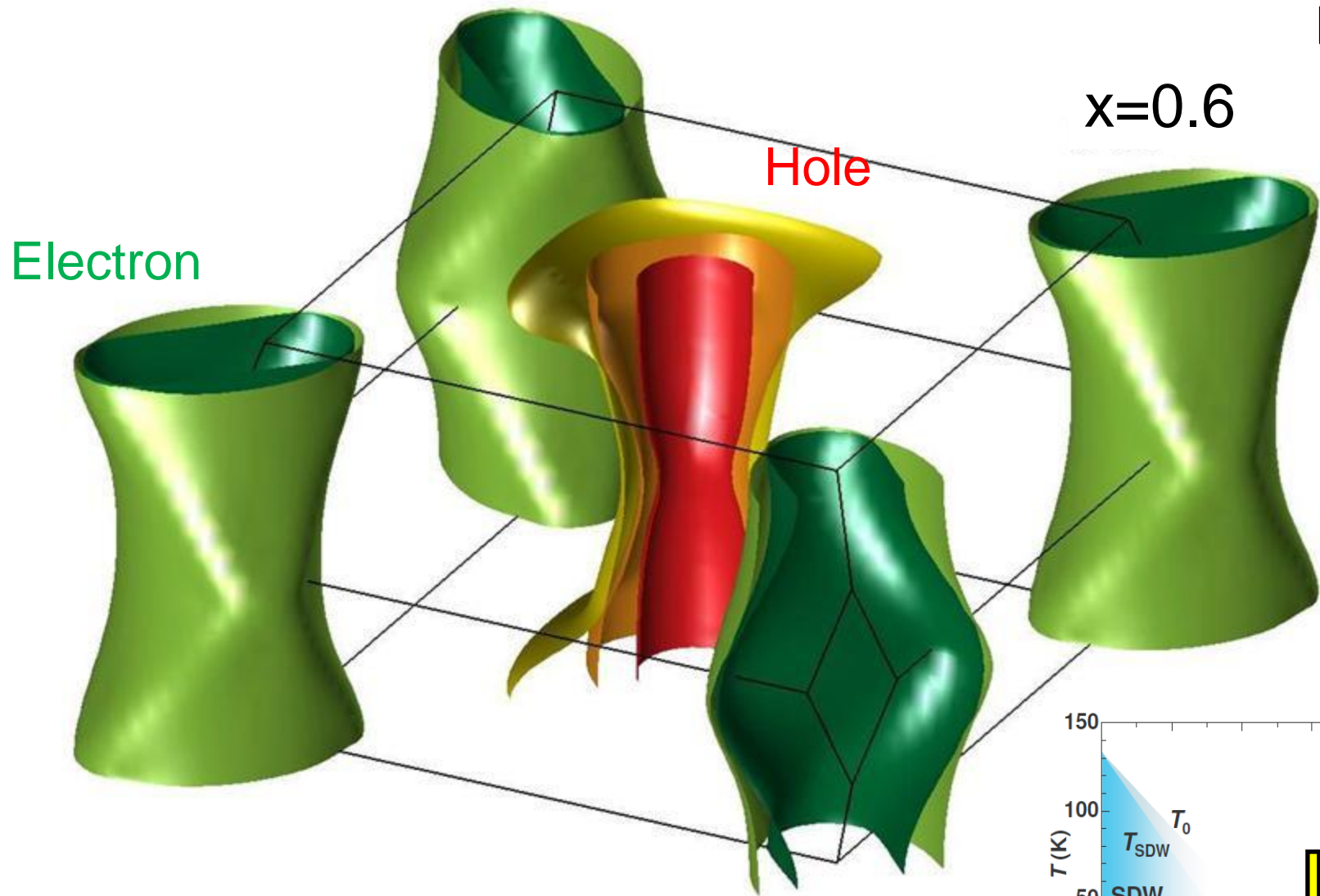
LDA





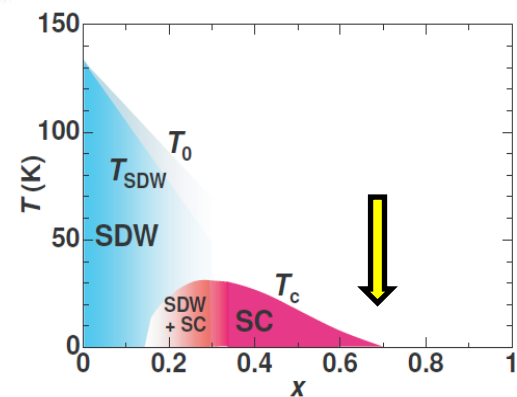
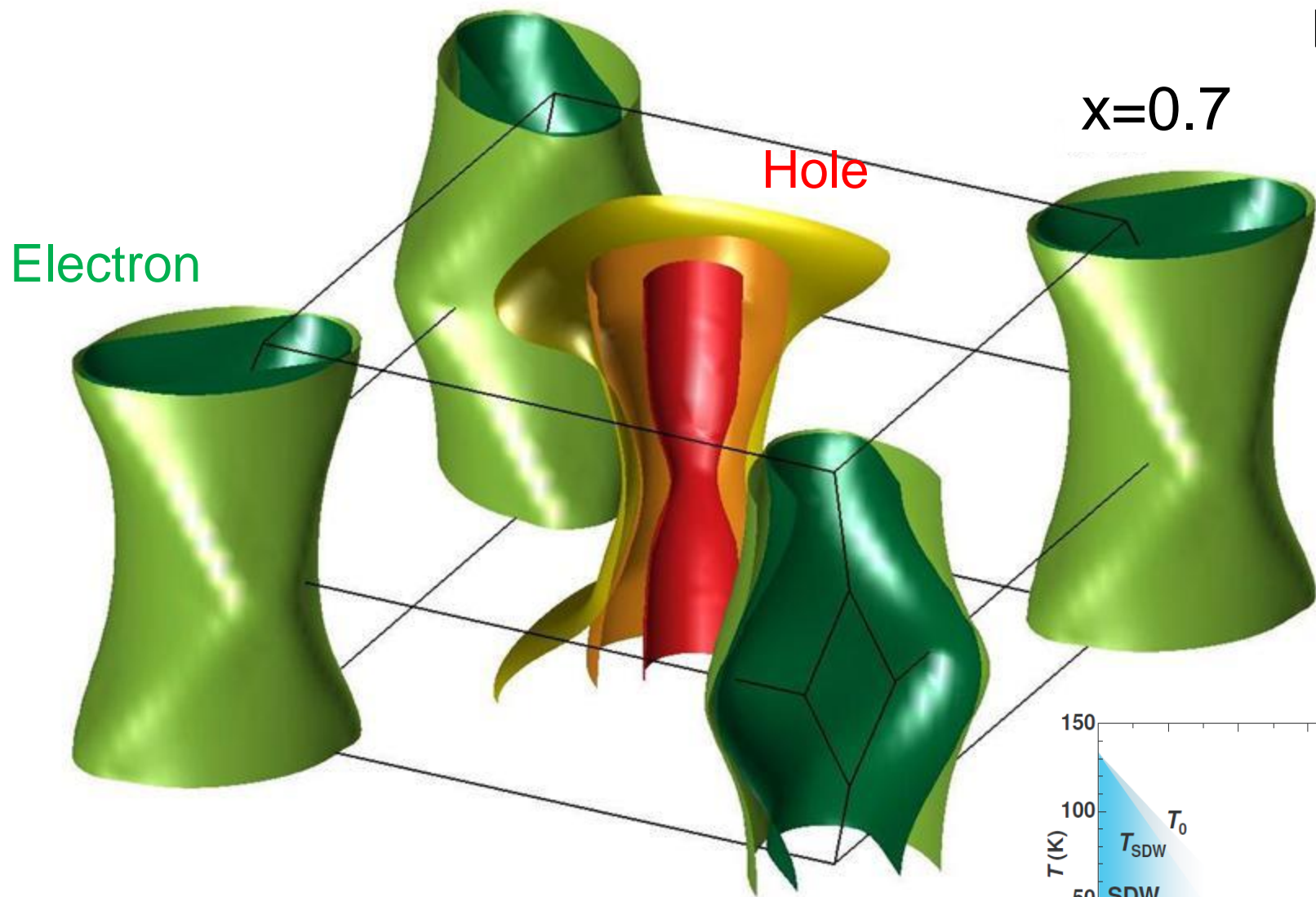
# BaFe<sub>2</sub> (As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>

LDA



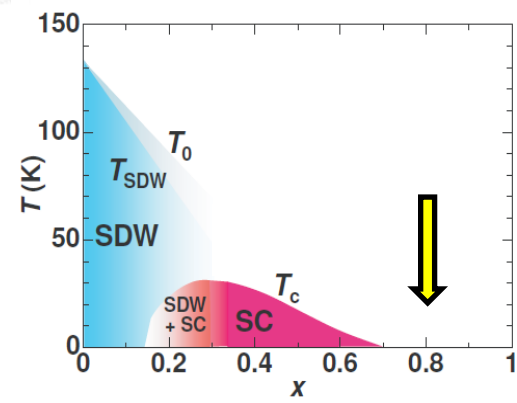
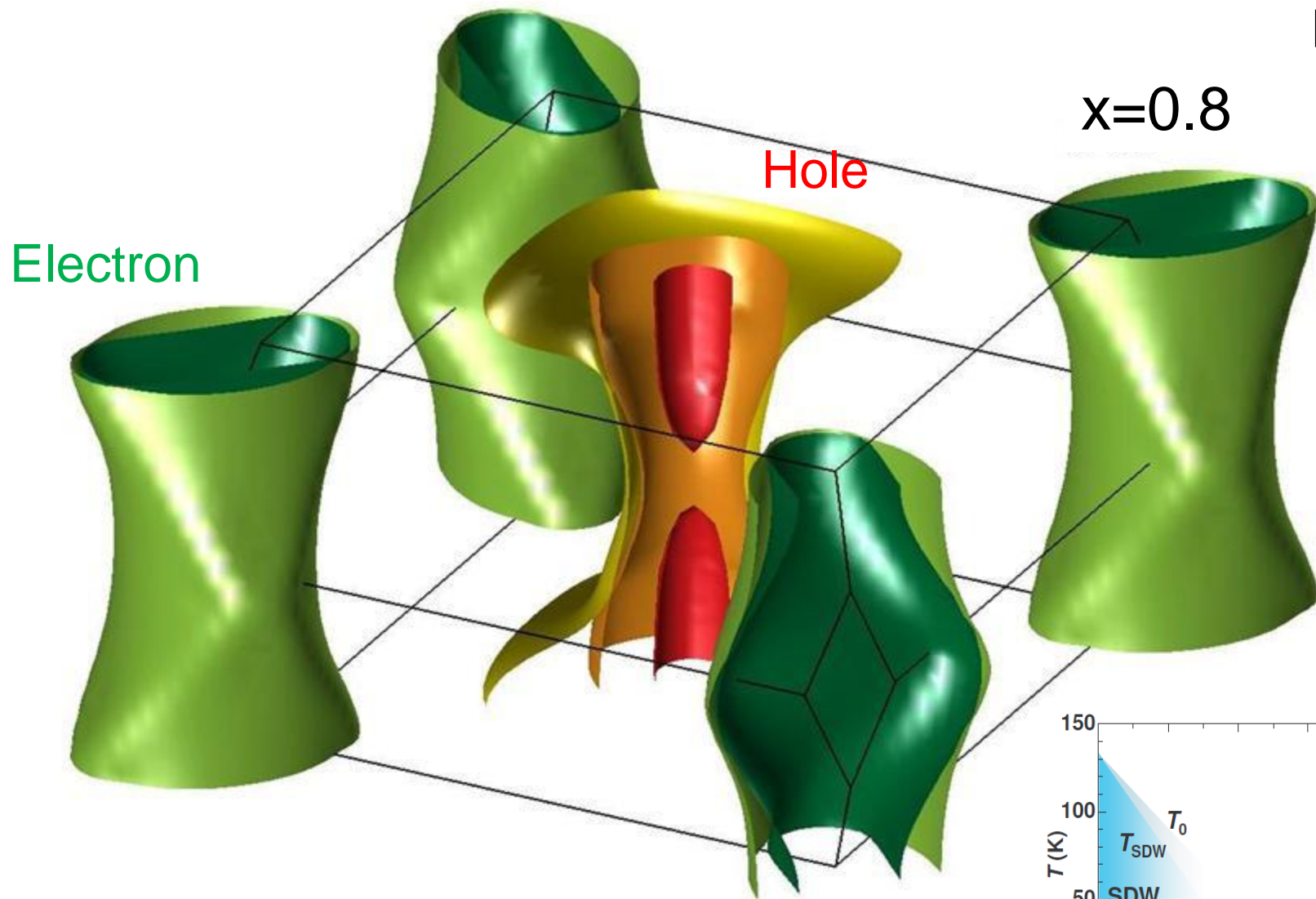
# BaFe<sub>2</sub> (As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>

LDA



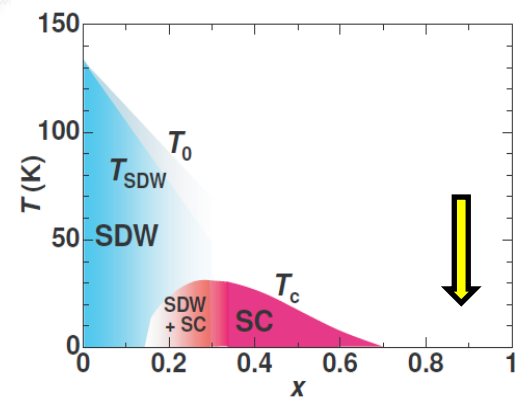
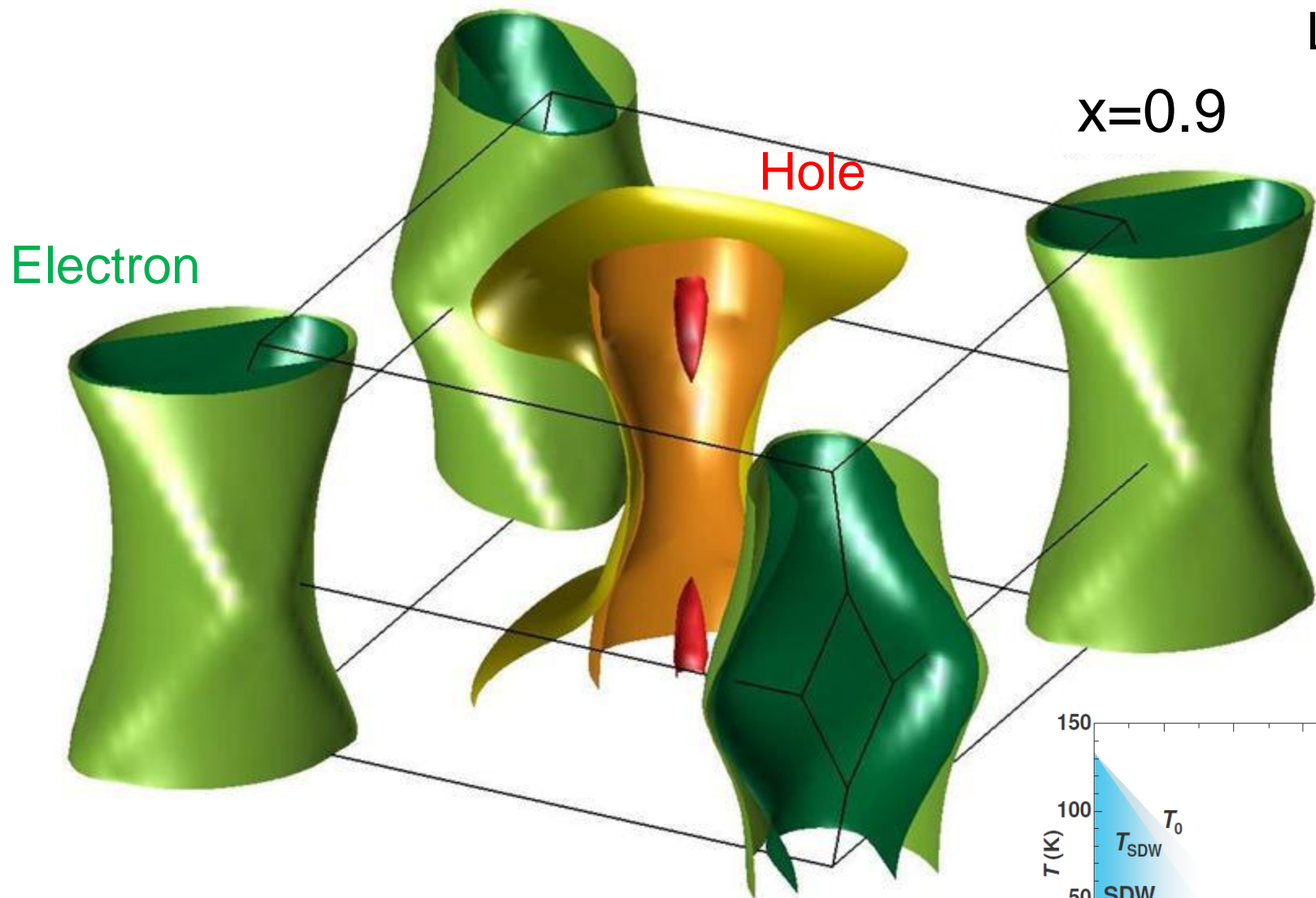
# BaFe<sub>2</sub> (As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>

LDA



# BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>

LDA





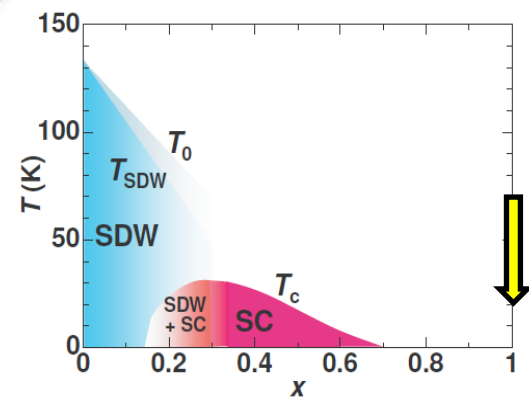
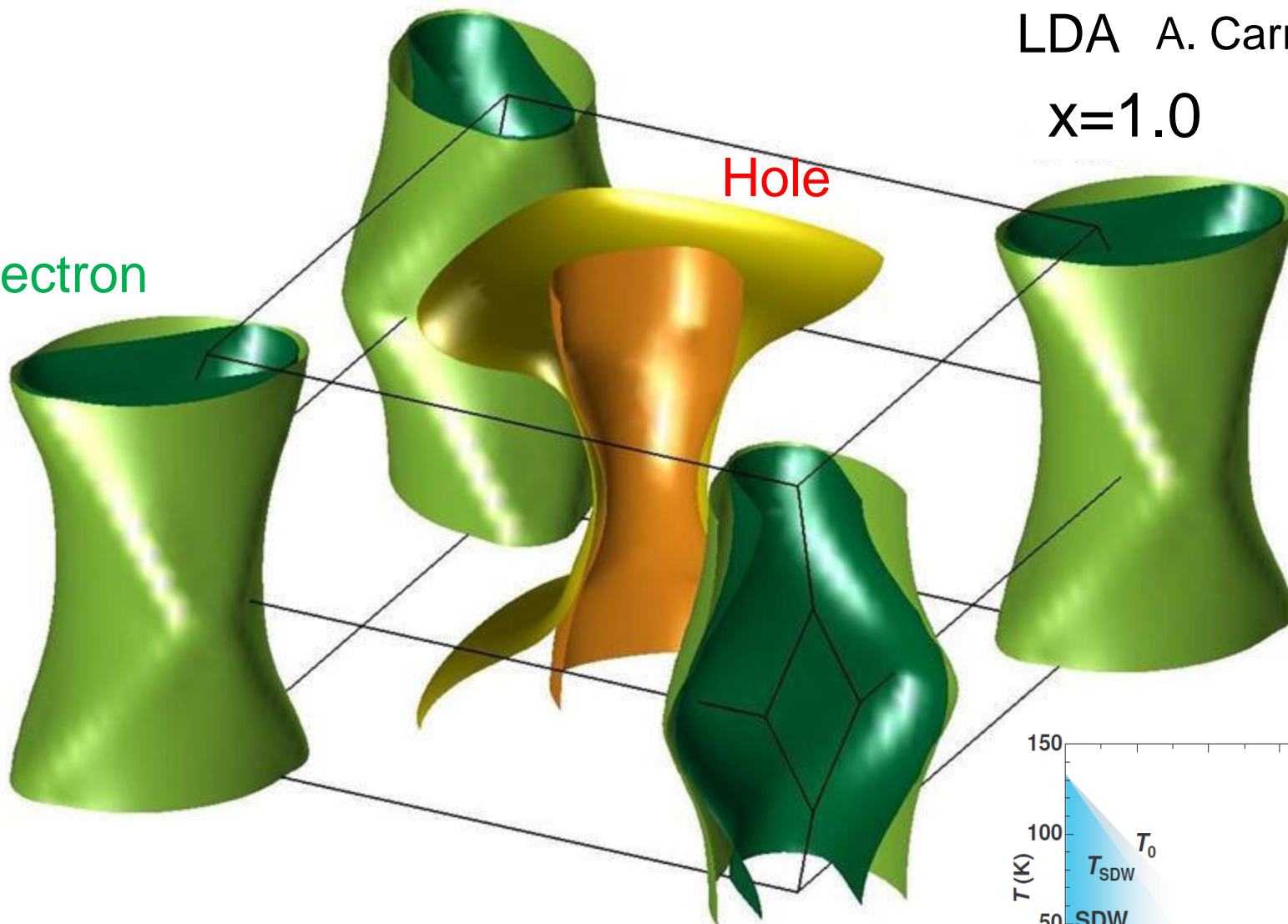
# BaFe<sub>2</sub> (As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>

LDA A. Carrington

x=1.0

Electron

Hole



# Electron correlations

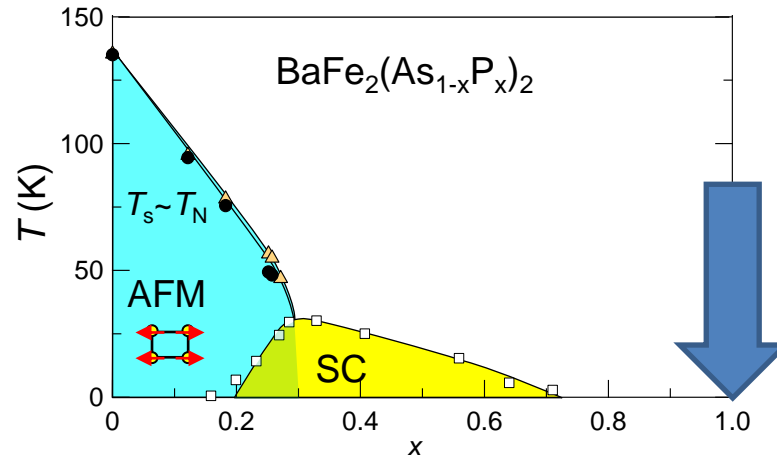
Electron correlations change the band structure

Band narrowing

Mass enhancement

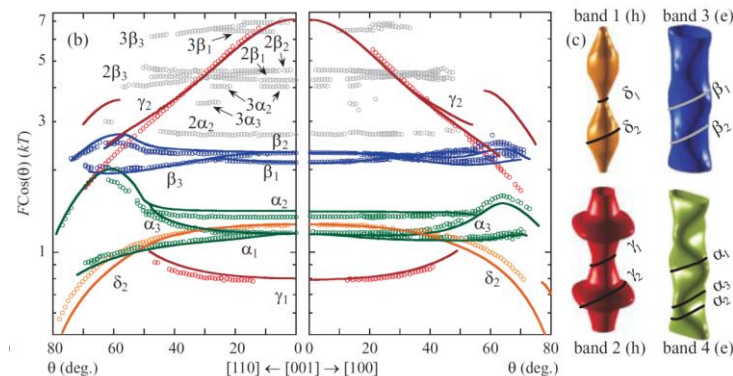
Band shift

Difference between LDA and measured Fermi surface

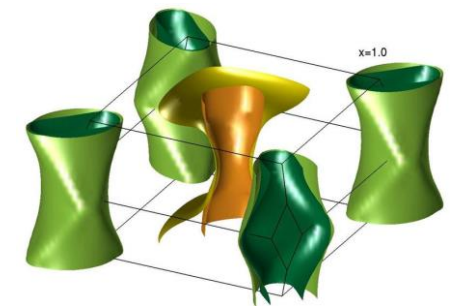


$\text{BaFe}_2\text{P}_2$

Weak electron correlation



FS is well reproduced by LDA



$m^*/m_b \sim 1.5-1.8$

# Electron correlations

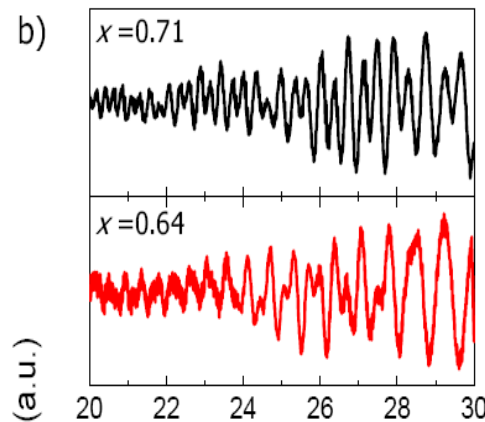
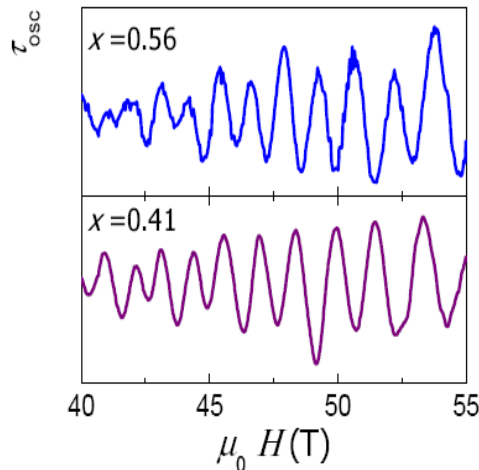
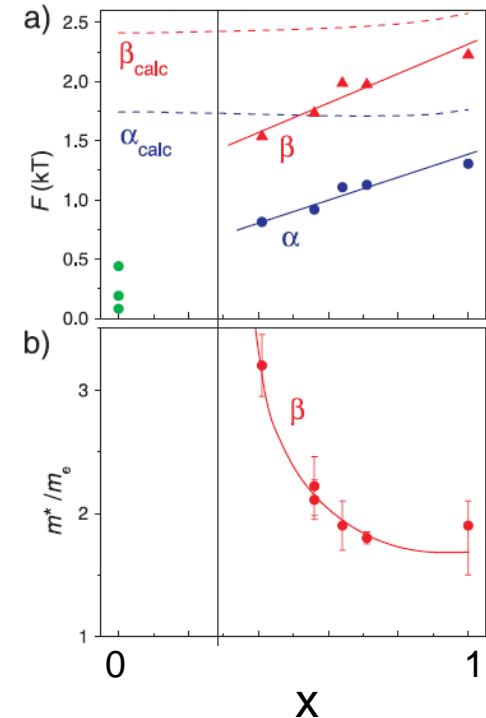
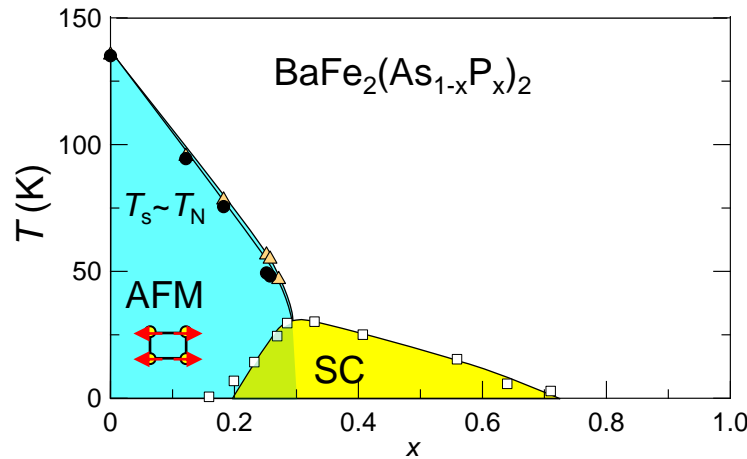
Electron correlations change the band structure

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Mass enhancement

Band shift

Difference between LDA and measured Fermi surface

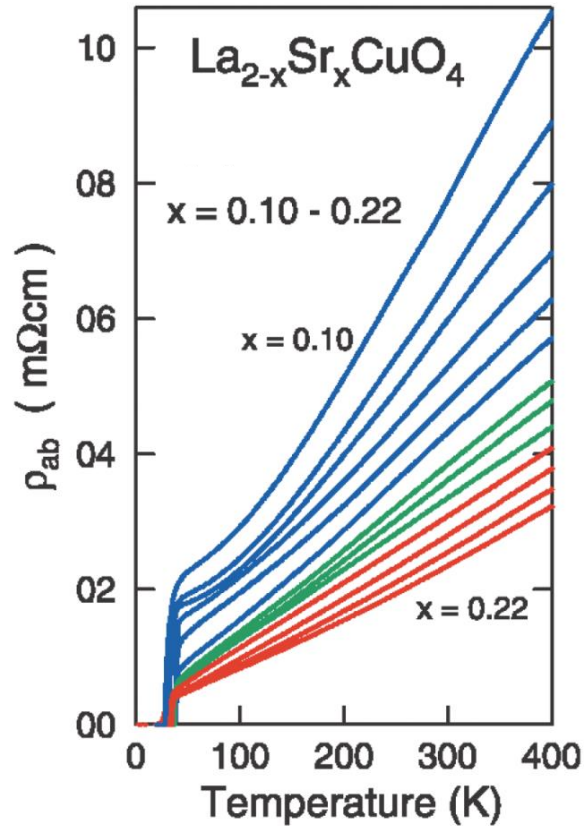


$F$  decreases:  
shrinkage of the FS  
Correlation induced  
band shift



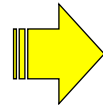
# Electron correlations

## Cuprates

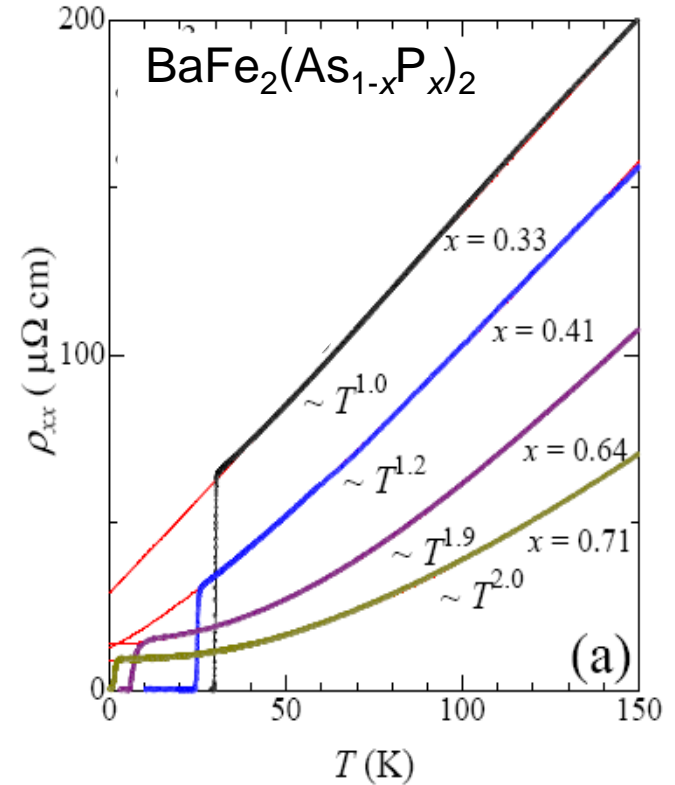


Y. Ando *et al.* PRL (04).

$T$ -linear resistivity



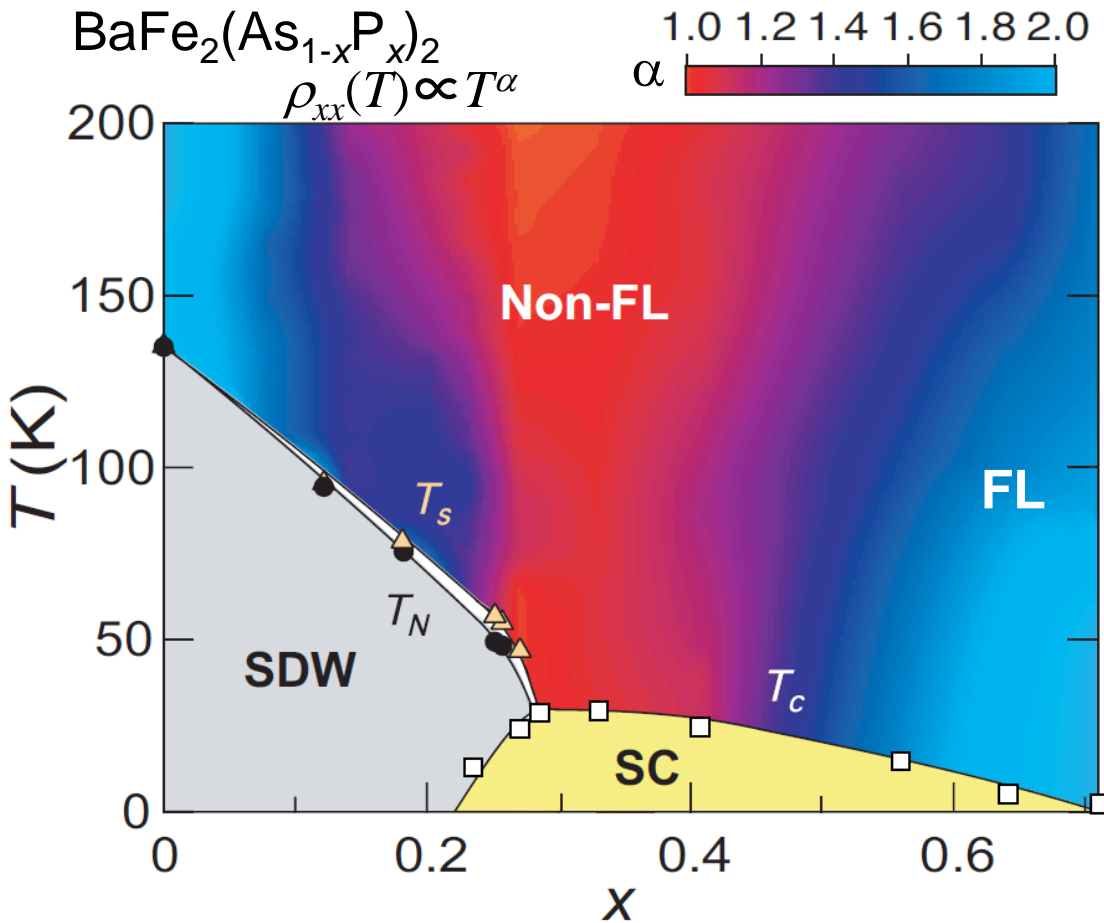
## Fe-pnictides



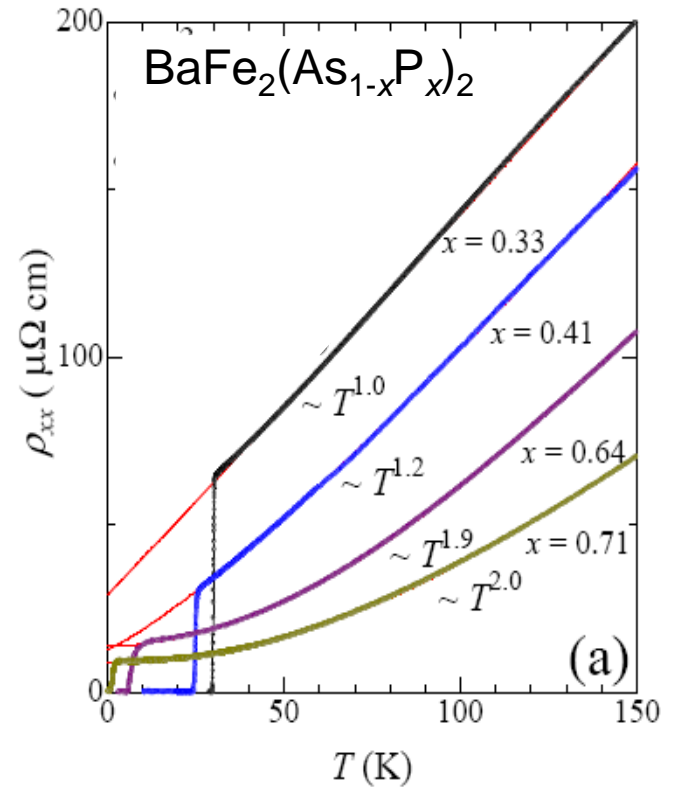
S. Kasahara *et al.*, PRB (10)

Importance of electron correlation

# Electron correlations



S. Kasahara *et al.*, PRB **81**, 184519 (10)



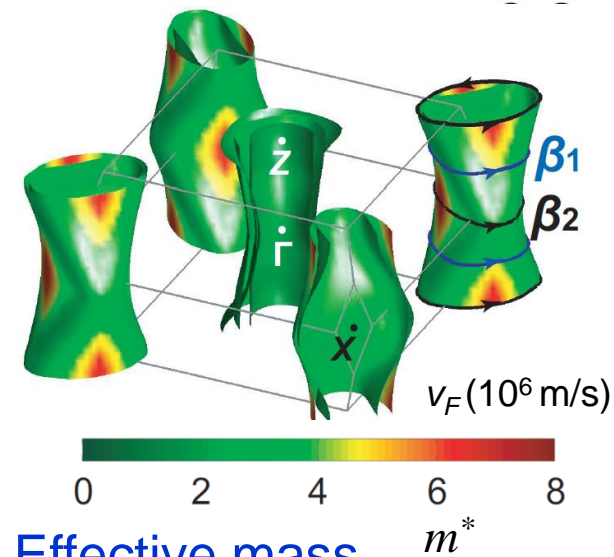
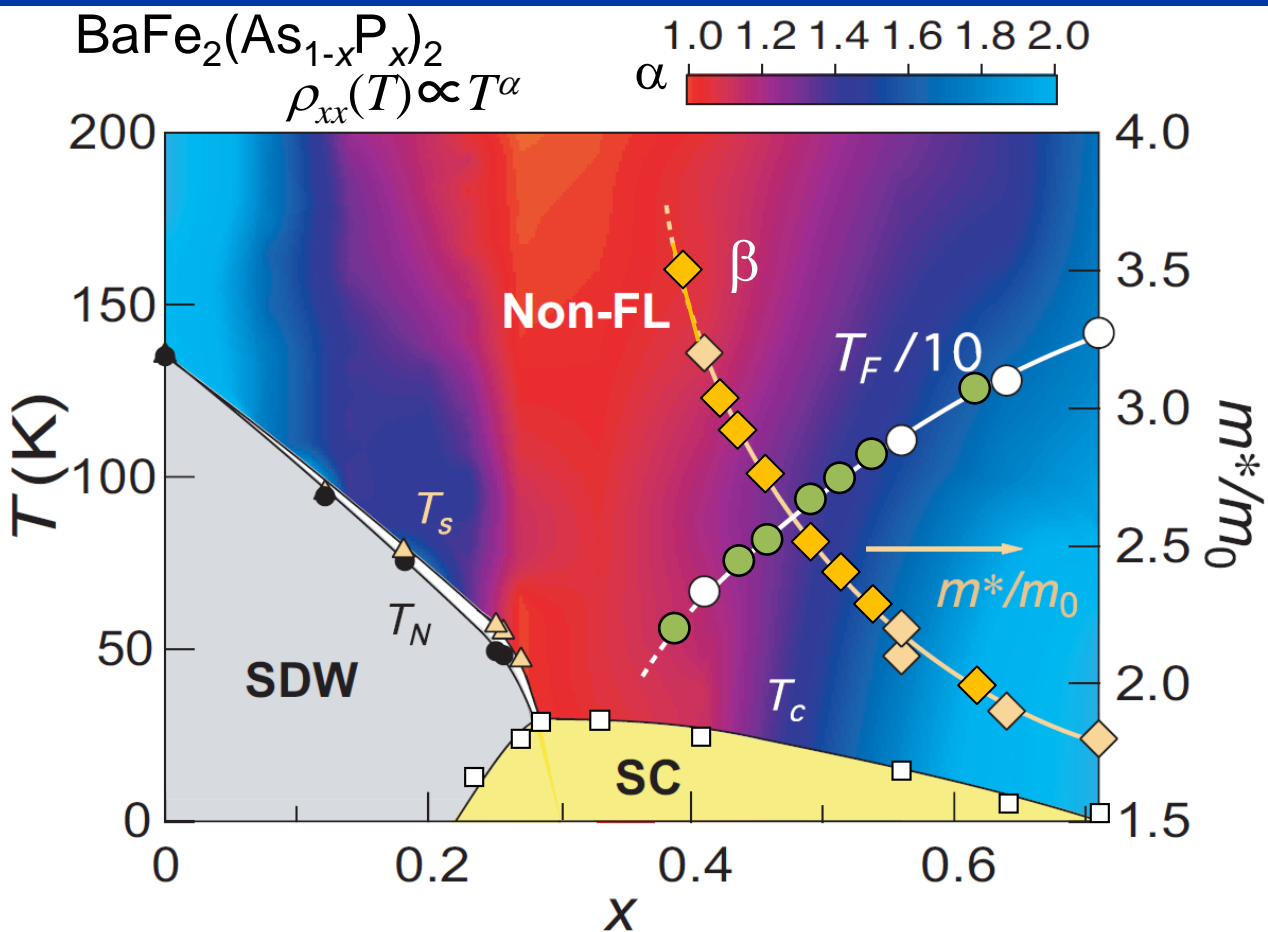
$T$ -linear resistivity at  $x=0.33$  just beyond SDW end point ( $x_c=0.3$ )

Hallmark of non-Fermi liquid

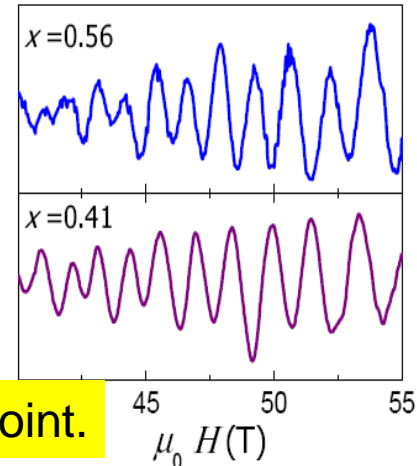
$T^2$ -dependence at  $x=0.71$

Fermi-liquid behavior

# Electron correlations



dHvA  
 $T_F = \hbar v_F / m^* k_B$



As  $x$  is tuned towards the maximum  $T_c$ ,

Effective mass  $m^*$  is strongly enhanced

Measured FS strikingly deviates from LDA calculation

Electron correlations are particularly important at the SDW end point.

# Electron correlations

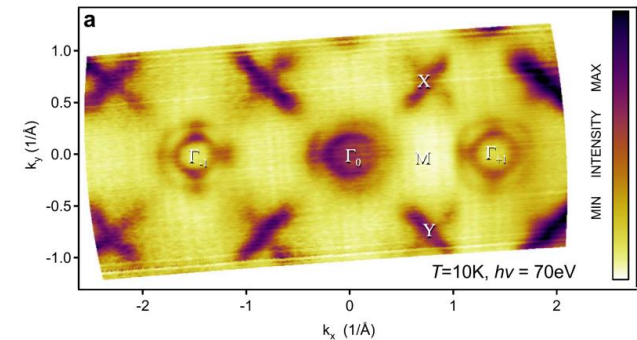
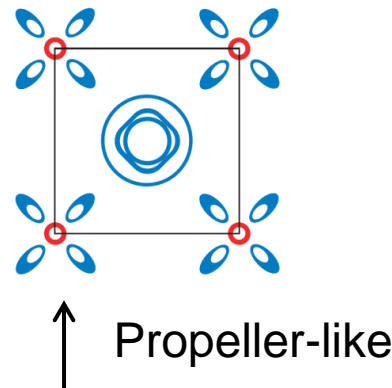
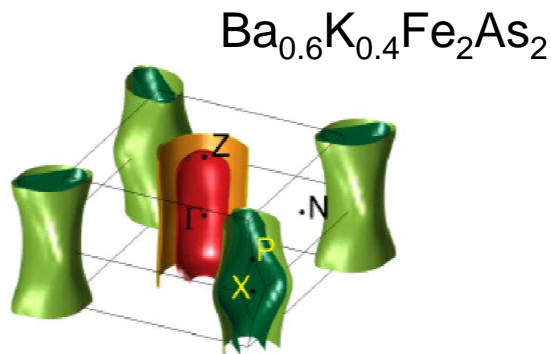
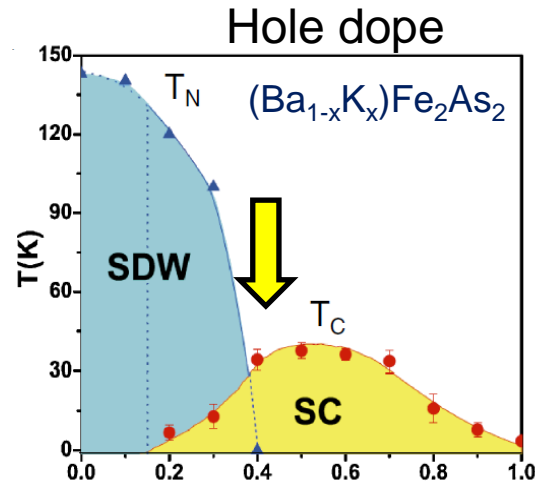
Electron correlations change the band structure

Band narrowing

Mass enhancement

Band shift

Difference between LDA and measured Fermi surface



Fermi surface topologically different from LDA.

Large band shift

# Electron correlations

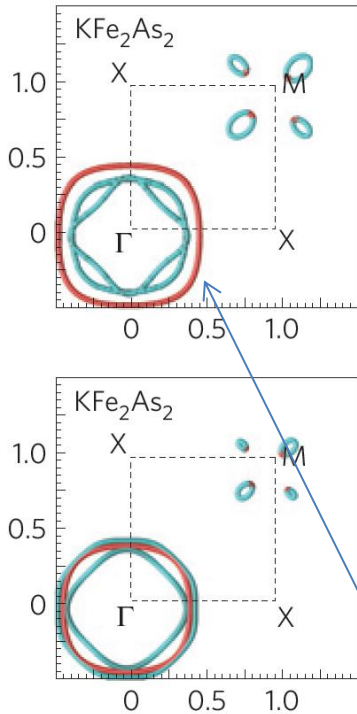
Electron correlations change the band structure

Band narrowing

Mass enhancement

Band shift

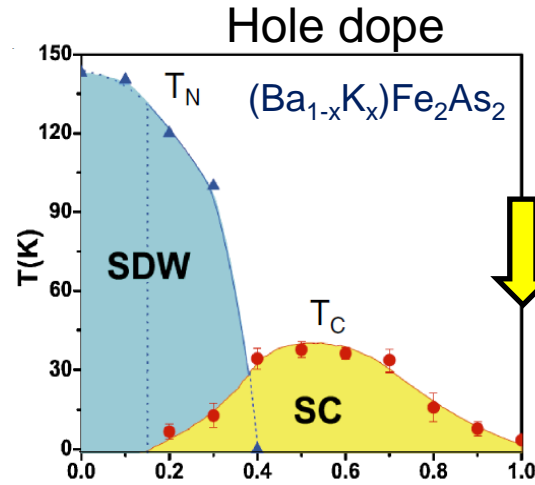
Difference between LDA and measured Fermi surface



LDA + DMFT

LDA

No correlation



ARPES xy-character

T. Yoshida *et al.* Frontiers in Phys.('14)

$\gamma \sim 100 \text{ mJ/K}^2\text{mol}$

**Heavy fermion!**

Z.P. Yin, K. Haule and G. Kotliar, Nature Mat. 10, 932 (2011)

Mass enhancement  $m^*/m_{\text{LDA}} \sim 10$

Strong electron correlation

# Physics of iron-based high temperature superconductors

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1) Introduction

2) Similarities and differences between cuprates and Fe-pnictides

3) Normal state properties

Electronic structure and magnetism

4) Superconducting properties

Superconducting gap structure

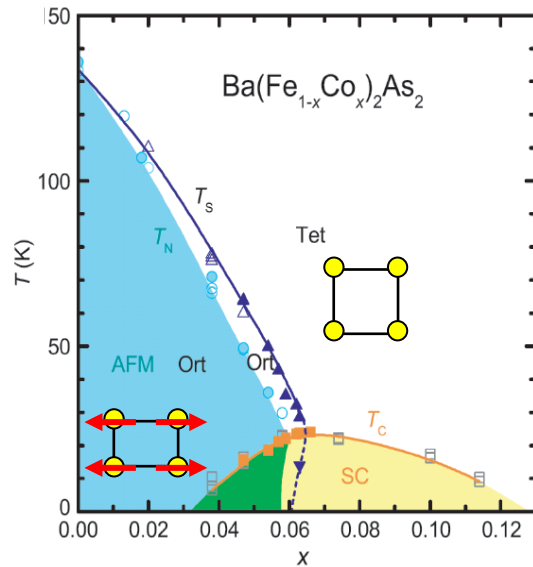
5) Some recent topics

QCP, BCS-BEC crossover,

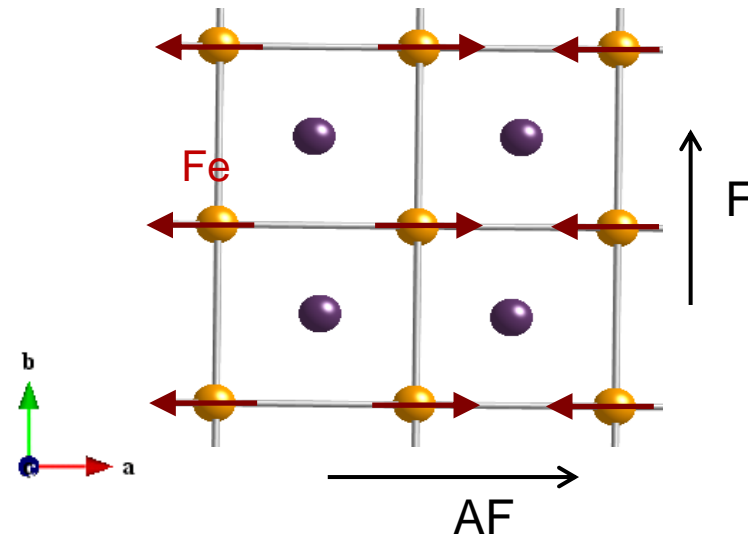
A novel high field SC state, Nematicity . . . .



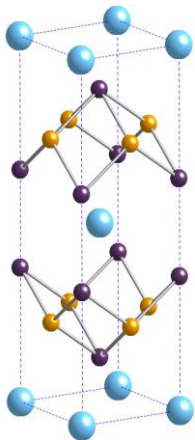
# Magnetic structure



## Stripe type AFM

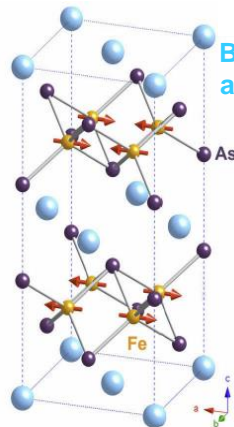


## High- $T$



Tetragonal  
Paramagnetic

## Low- $T$



Orthorhombic.  
Antiferromagnetic

What is the origin of stripe type AFM?

### 1) Orbital ordering

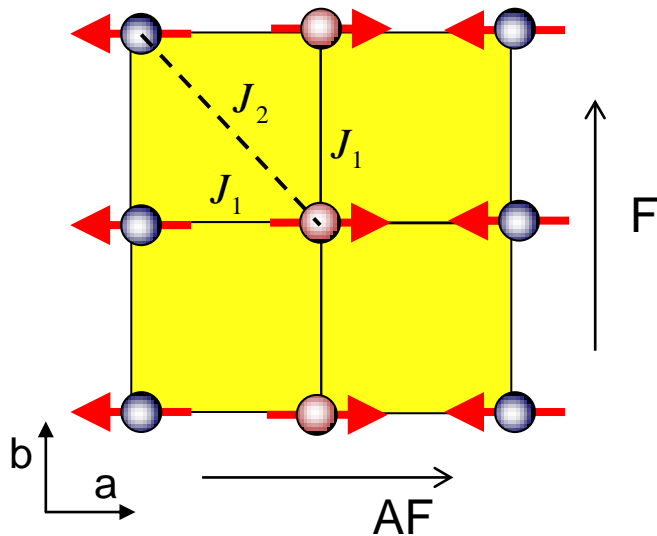
- i) Localized picture
- ii) Itinerant picture

### 2) Spin nematic ordering



# Magnetic structure (orbital ordering, localized spin)

Approach using localized spins:  $J_1$ - $J_2$  model

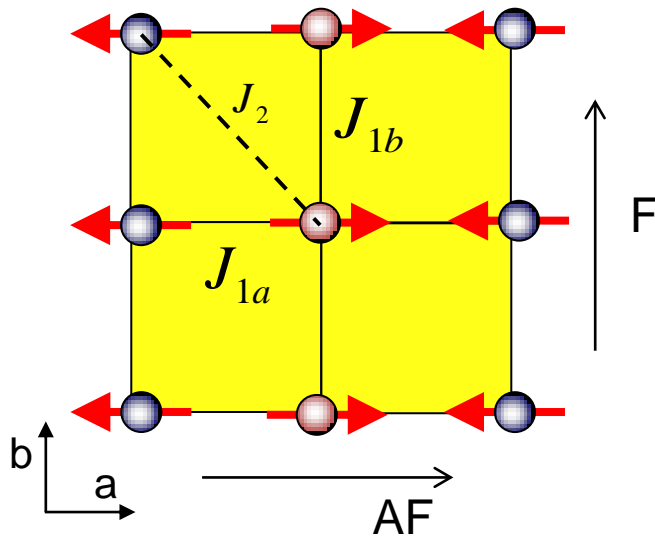


Strong frustration

$$J_2 > J_1/2$$

P. Chandra, P. Coleman and A.I. Larkin,  
PRL 64, 88 (1990)

# Magnetic structure (orbital ordering, localized spin)



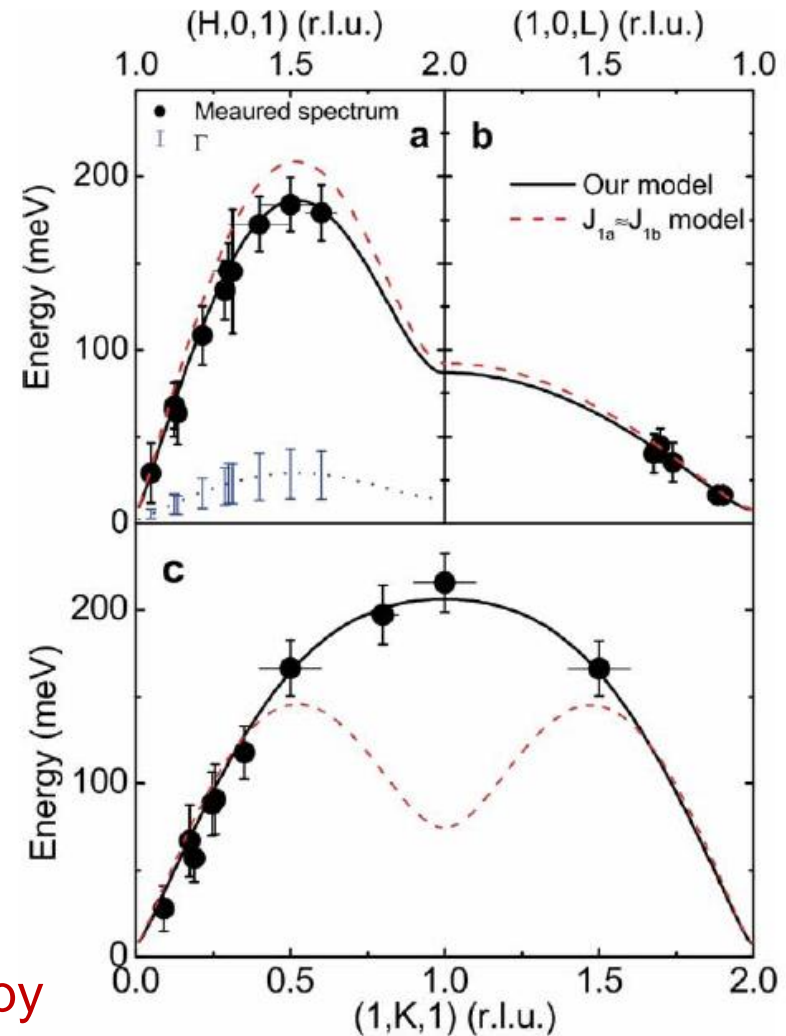
$$J_{1a} = 49 \quad J_{1b} = -5.7 \quad J_2 = 19 \text{ meV}$$

Large in-plane exchange coupling anisotropy

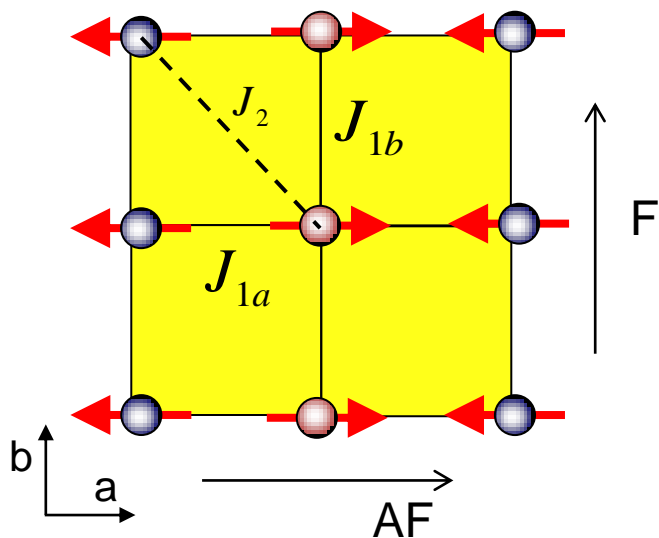
Localized model in tetragonal lattice ( $J_{1a} = J_{1b}$ ) cannot explain the magnetic excitations

Jun Zhao *et al.*, Nature Phys. (2009)

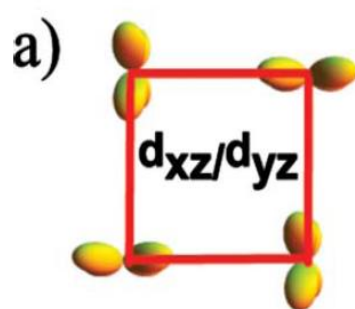
What is the origin of the in-plane anisotropy?



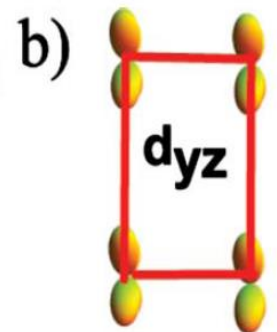
# Magnetic structure (orbital ordering, localized spin)



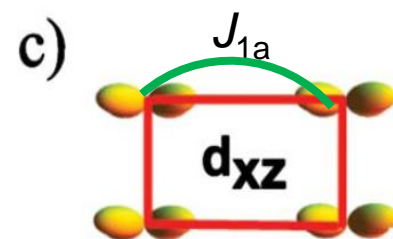
## Orbital ordering



$$J_{1a} = J_{1b}$$



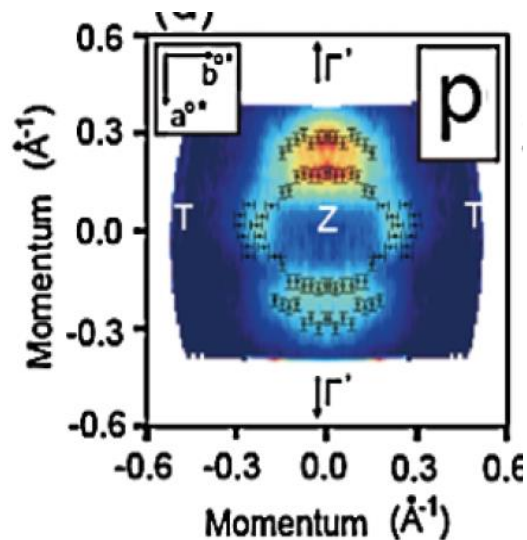
$$J_{1a} < J_{1b}$$



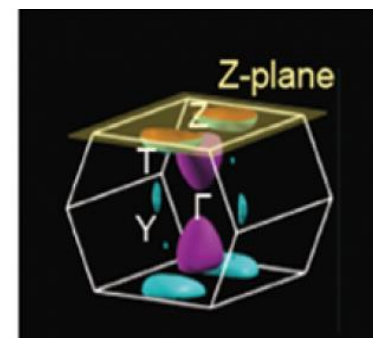
$$J_{1a} > J_{1b}$$

$$xz \downarrow \quad yz \uparrow$$

## ARPES in $\text{BaFe}_2\text{As}_2$



Kruger et al., PRB (09)  
Lv et al., PRB (09)



T. Shimojima *et al.*,  
PRL (2010).

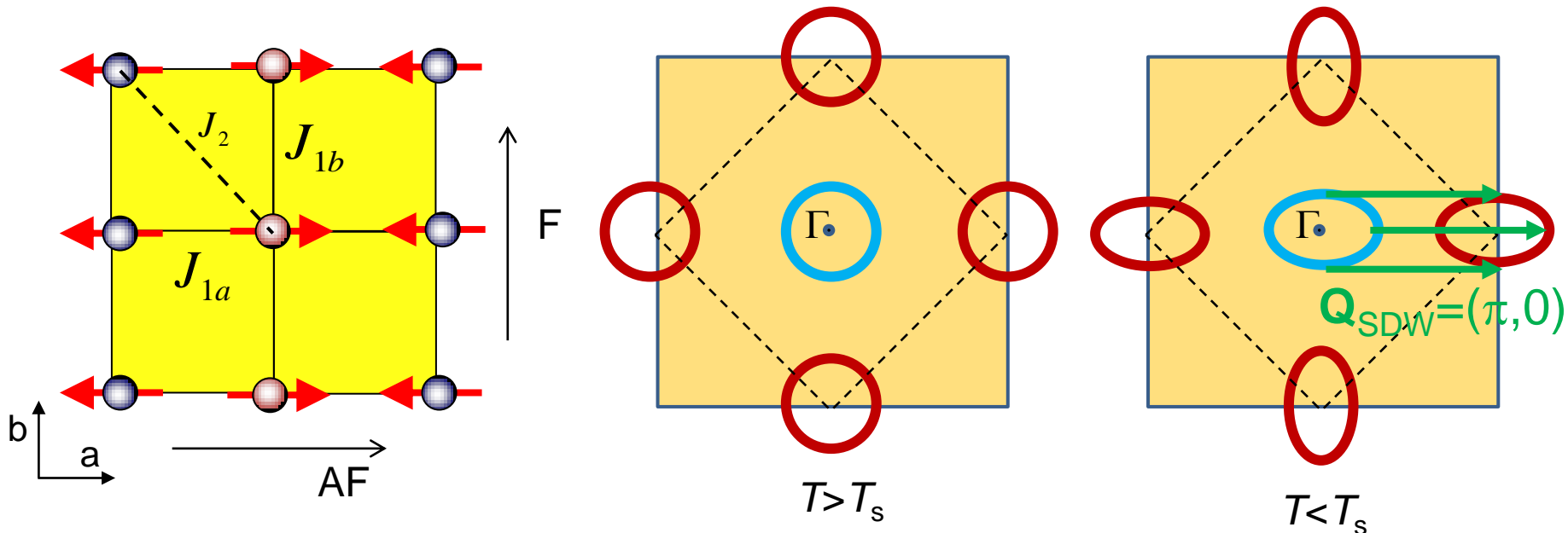
# Magnetic structure (orbital ordering, itinerant)

Fermi Surface

→ **Multiband** electronic structure with well-separated **hole** and **electron** sheets

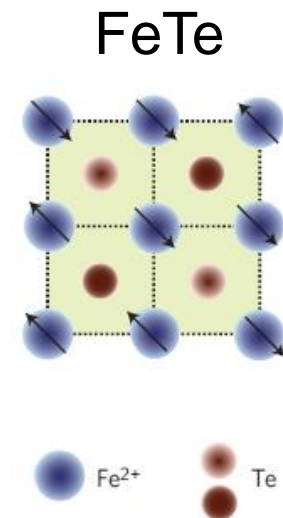
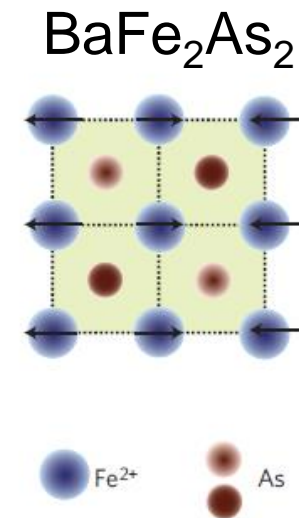
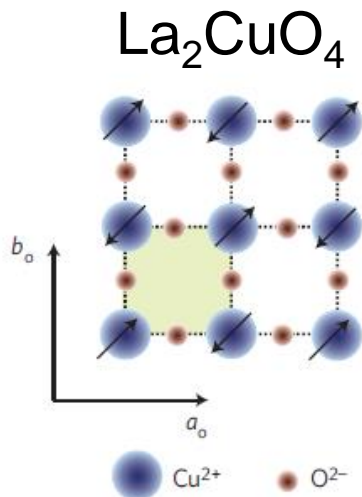
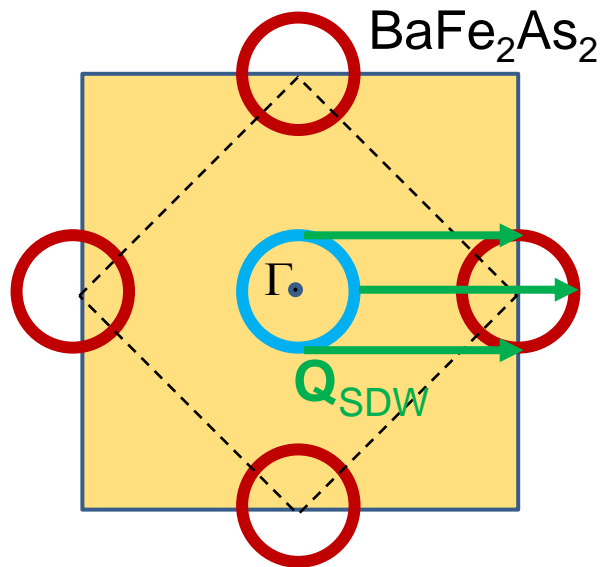
**Good nesting condition**

→ **Antiferromagnetic SDW ordering**

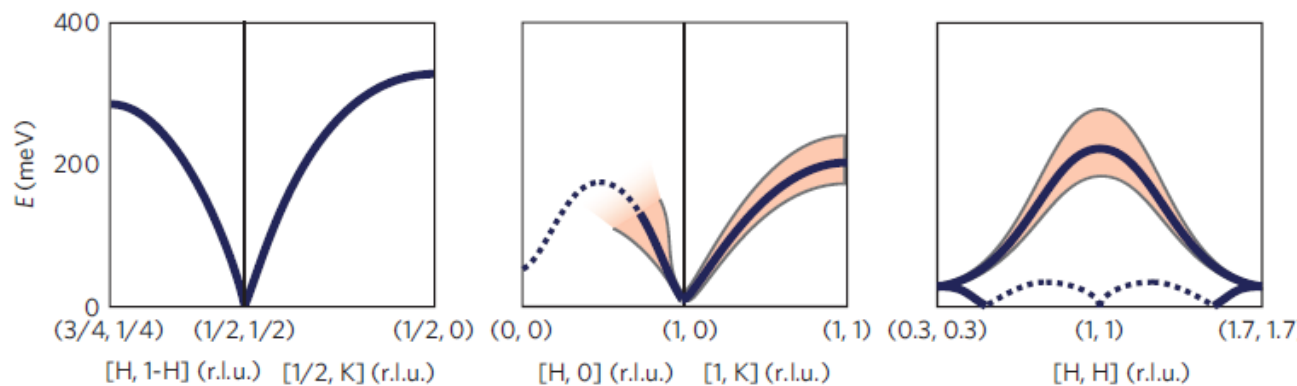


Because of orbital ordering,  $(\pi, 0)$  nesting becomes better than  $(0, \pi)$ .

# Magnetic structure (orbital ordering, itinerant)



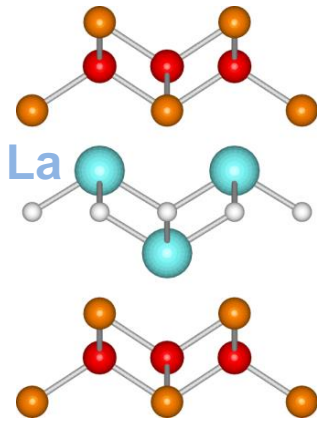
P. Dai, J. Hu, and E. Dagotto, Nat. Phys (12)



- Well defined spin wave at the BZ boundary
- No observation of Landau damping
- Cannot explain bi-collinear structure of FeTe with similar FS

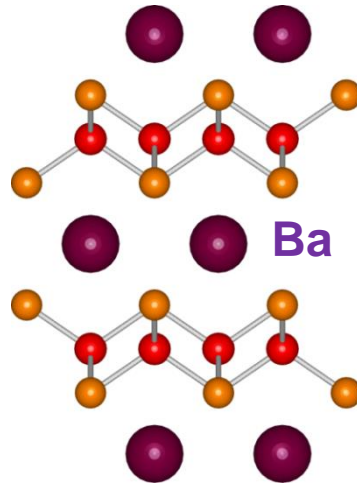
# Magnetic structure (orbital ordering)

1111



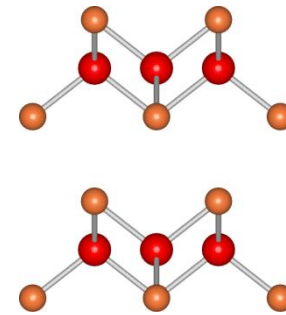
0.3-0.5  $\mu_B$

122



0.8-1  $\mu_B$

11



$\sim 2 \mu_B$

itinerant



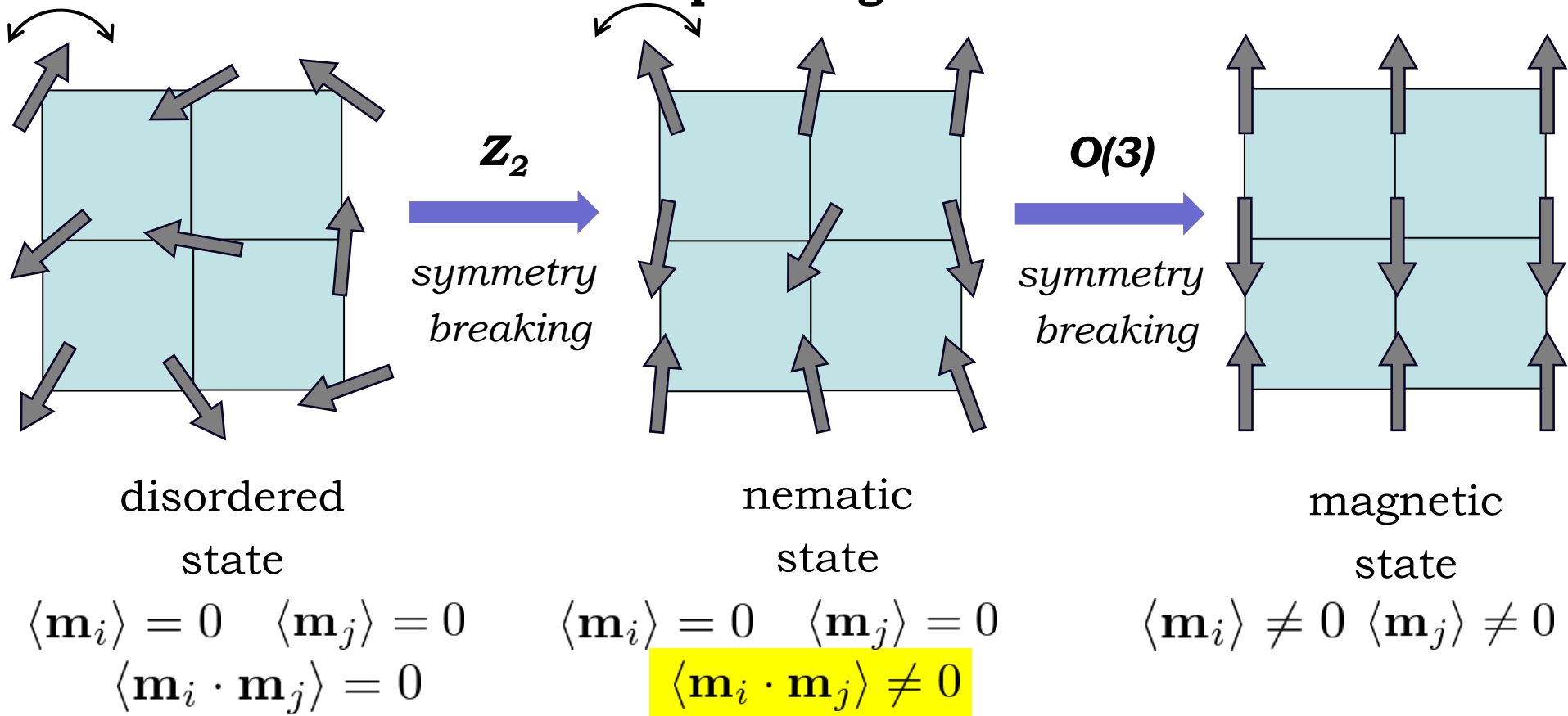
localized

# Magnetic structure (spin nematic)

## Spin nematic order

R.M. Fernandes, A.V. Chubkov and J. Schmalian, Nature Phys. (14)

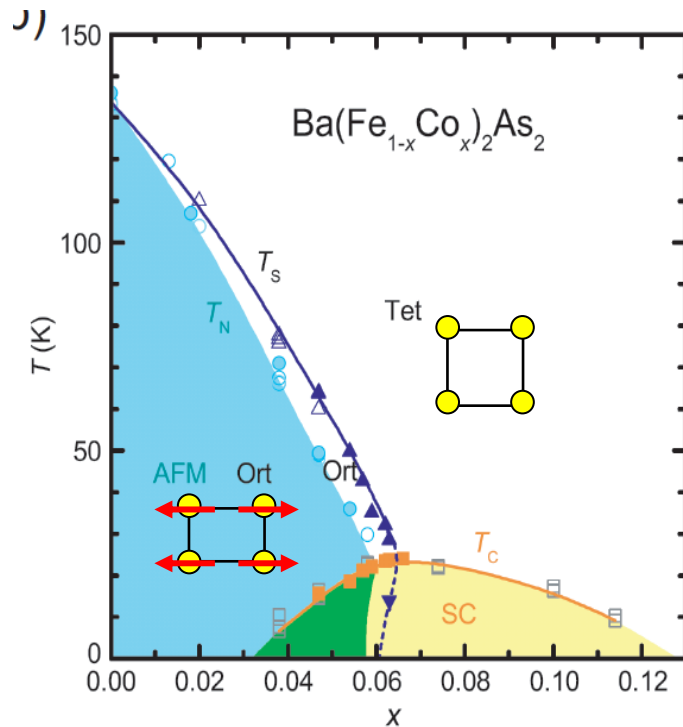
**a state that breaks  $Z_2$  (Ising) symmetry,  
but remains paramagnetic**



Spin nematic induces orbital order through the spin-lattice coupling



# Relationship between magnetic order and structural transition



## Two scenarios

- 1) Orbital ordering triggers stripe SDW order.
- 2) Magnetic interaction (spin nematic) induces orbital order through the spin-lattice coupling.

Structural ( $T_s$ ) and AFM transition ( $T_N$ ) lines follow closely each other

$T_s$ : orbital order

$T_N$ : SDW order



Who is the driver?

# Summary

## Iron pnictide

A new family of unconventional superconductors

## Normal state properties

Electron correlation effects are definitely important.

Importance of orbital degrees of freedom.

Relationship between orbital order and stripe SDW order is controversial.

# Physics of iron-based high temperature superconductors (II)

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Yuji Matsuda



*Department of Physics  
Kyoto University  
Kyoto, Japan*



# Physics of iron-based high temperature superconductors

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1) Introduction

2) Similarities and differences between cuprates and Fe-pnictides

3) Normal state properties

Electronic structure and magnetism

4) Superconducting properties

Superconducting gap structure

5) Some recent topics

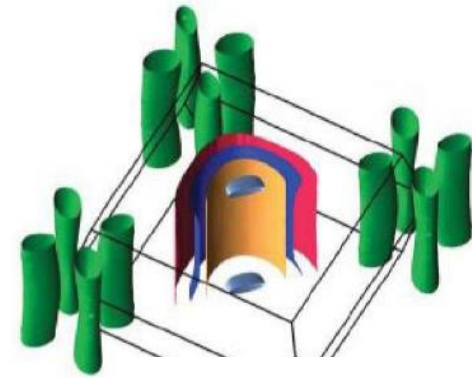
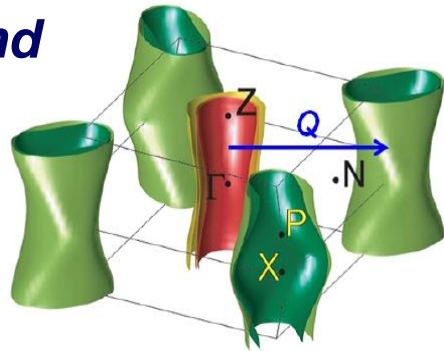
QCP, BCS-BEC crossover, Nematicity . . . .



# Superconductivity in BaFe<sub>2</sub>As<sub>2</sub> systems

Parent compound

BaFe<sub>2</sub>As<sub>2</sub>  
(AF Metal)



KFe<sub>2</sub>As<sub>2</sub> ( $T_c=3$  K)

(Ba<sub>1-x</sub>K<sub>x</sub>)  $\gamma \sim 100$  mJ/K<sup>2</sup>mol

( $T_c^{opt} \sim 38$  K) no electron pockets

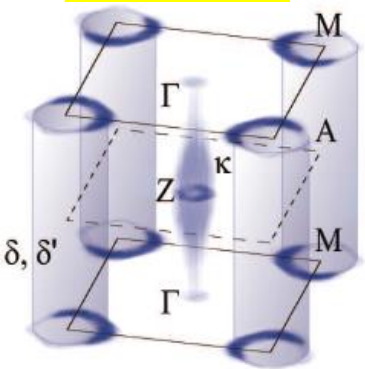
Ba(Fe<sub>1-x</sub>Co<sub>x</sub>)<sub>2</sub>As<sub>2</sub>

K<sub>x</sub>Fe<sub>2-y</sub>Se<sub>2</sub> ( $T_c^{opt} \sim 24$  K)

( $T_c^{opt} \sim 31$  K)

electron-doping

no hole pockets



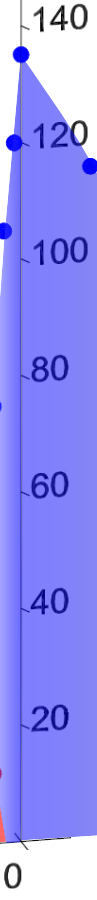
SC

SC

SC

x [Co]

x [K]



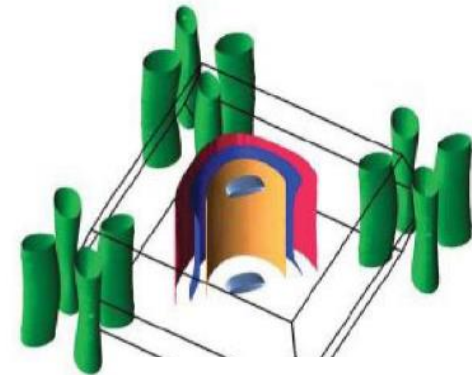
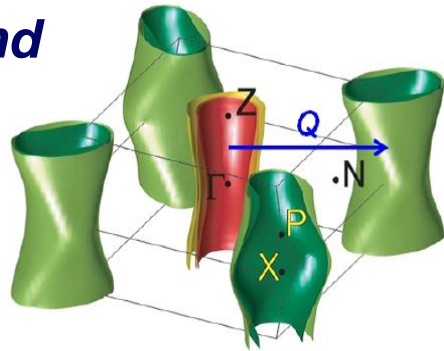
hole-doping

no electron pockets



# Superconductivity in BaFe<sub>2</sub>As<sub>2</sub> systems

Parent compound  
BaFe<sub>2</sub>As<sub>2</sub>  
(AF Metal)



KFe<sub>2</sub>As<sub>2</sub> ( $T_c=3$  K)

(Ba<sub>1-x</sub>K<sub>x</sub>)  $\gamma \sim 100$  mJ/K<sup>2</sup>mol

( $T_c^{opt} \sim 38$  K) no electron pockets

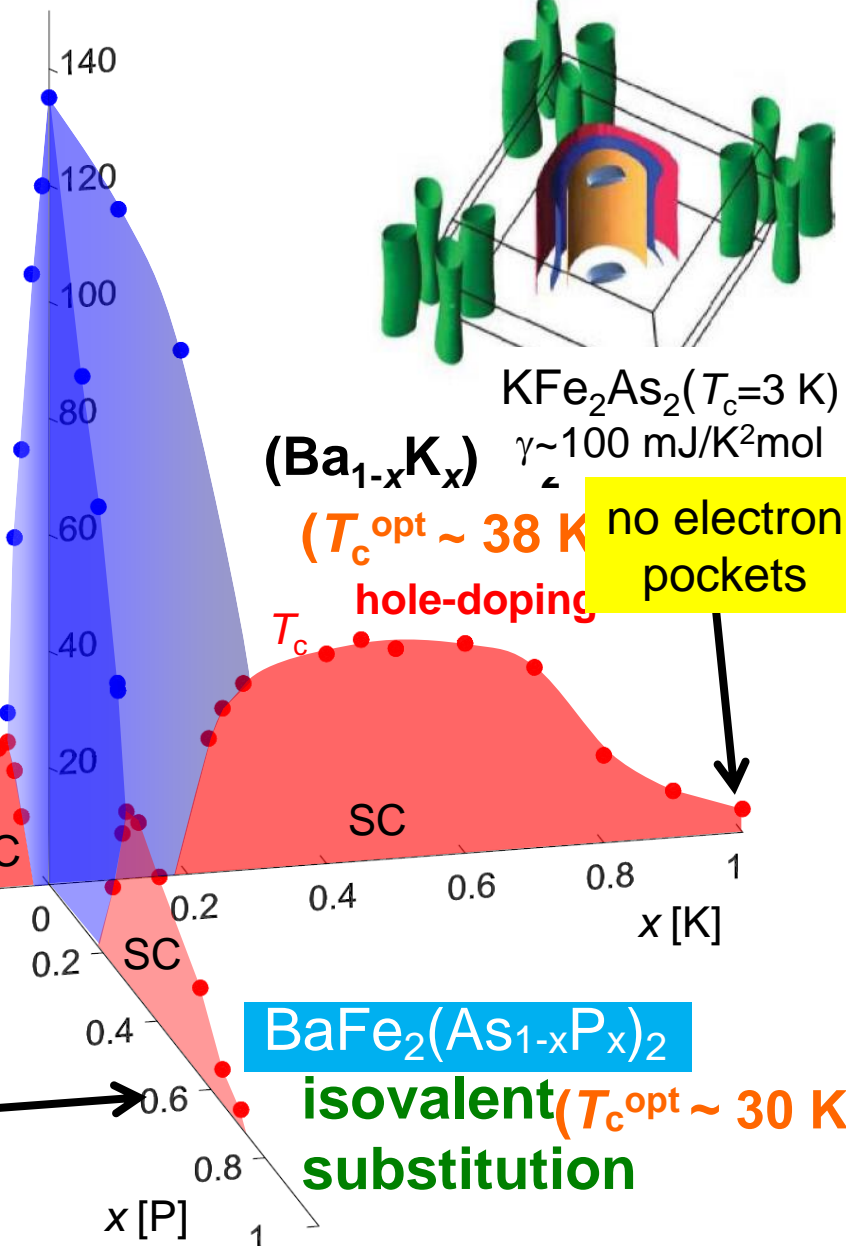
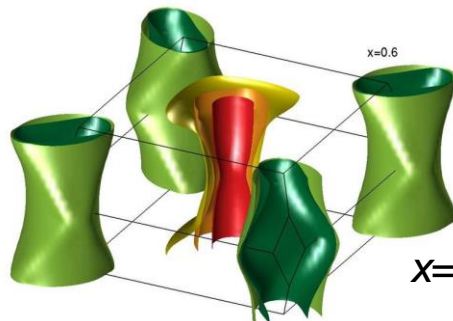
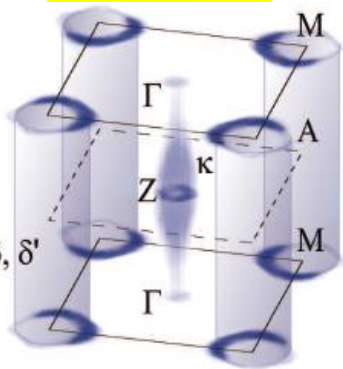
Ba(Fe<sub>1-x</sub>Co<sub>x</sub>)<sub>2</sub>As<sub>2</sub>

K<sub>x</sub>Fe<sub>2-y</sub>Se<sub>2</sub> ( $T_c^{opt} \sim 24$  K)

( $T_c^{opt} \sim 31$  K)

electron-doping

no hole pockets



BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>  
isovalent ( $T_c^{opt} \sim 30$  K)  
substitution

Ground state can be tuned without doping carriers



# Superconducting gap structure of iron pnictides

Gap structure is closely related to the pairing interaction

**Full gap or nodal?**

## Full gap

**Does the gap change sign between the hole and electron pockets?**

Is the major pairing interaction repulsive or attractive?

## Nodal

⇒ Presence of repulsive interaction.

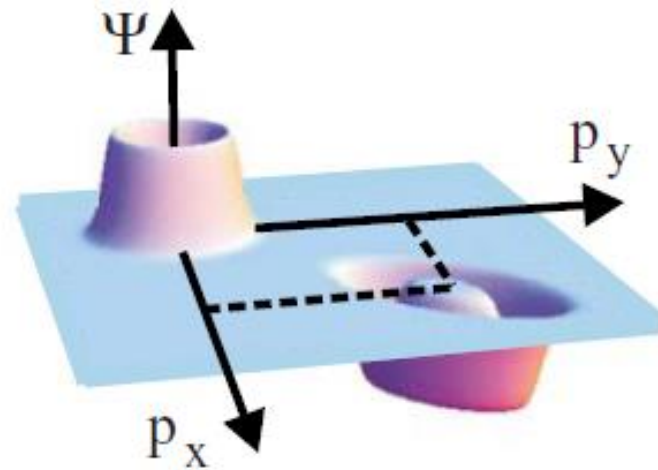
**Is the node accidental or symmetry protected?**

Accidental : presence of two (or more) competing pairing interactions

# Iron pnictides: candidate for the SC state

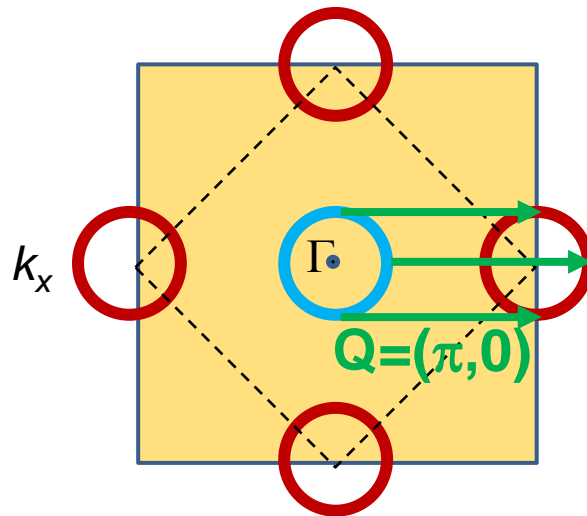
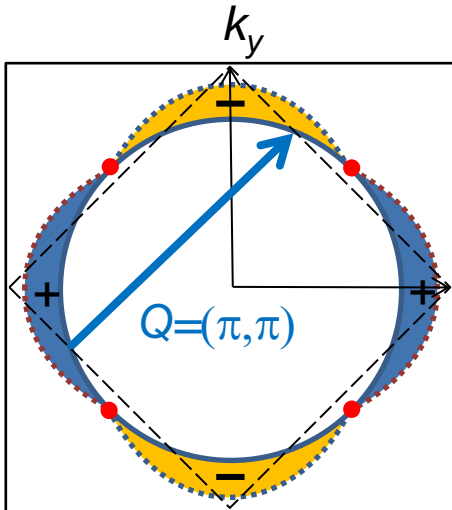
- Pairing due to purely **repulsive** electronic interaction (enhanced by spin fluctuations)

$$V > 0$$



$$S_{+-}$$

cf. *d*-wave cuprate



- I. I. Mazin *et al.*, PRL **101**, 057003 (2008).
- K. Kuroki *et al.*, PRL **101**, 087004 (2008).  
& PRB **79**, 224511 (2009).
- A. V. Chubkov *et al.*, PRB **80**, 140515(R) (2009).
- S. Graser *et al.*, NJP **11**, 025016 (2009).
- H. Ikeda, PRB **81**, 054502 (2010).
- K. Seo *et al.*, PRL **101**, 206404 (2008).
- F. Wang *et al.*, PRL **102**, 047005 (2009).

⋮

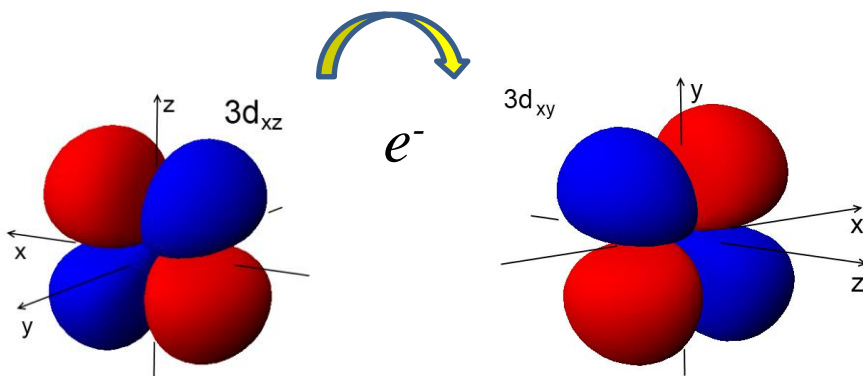
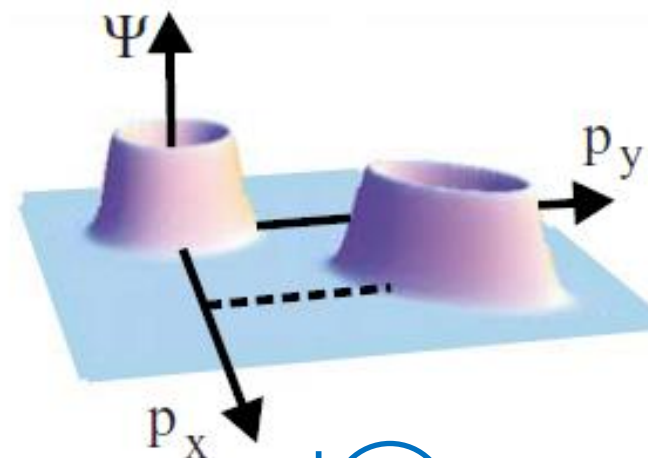
# Iron pnictides: candidate for the SC state

- Pairing due to **attractive** interaction caused by charge/orbital fluctuations.

$$S_{++}$$

$$V < 0$$

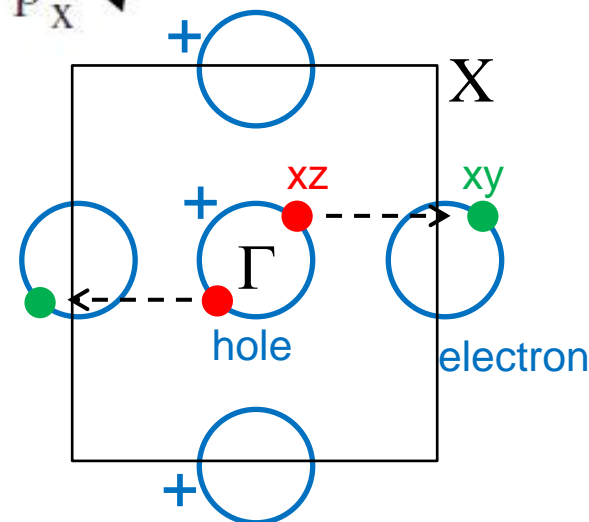
Orbital fluctuations  
(Quadrupole fluctuation)



Charge up

Charge down

Occupation number of each orbit  
at each Fe site fluctuates



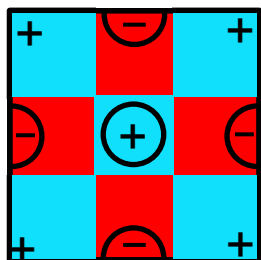
H. Kontani & S. Onari, PRL **104**, 157001 (2010).  
 F. Kruger *et al.*, PRB **79**, 054504 (2009).  
 Y. Yanagi *et al.*, PRB **81**, 054518 (2010).

# Iron pnictides: candidate for the SC state

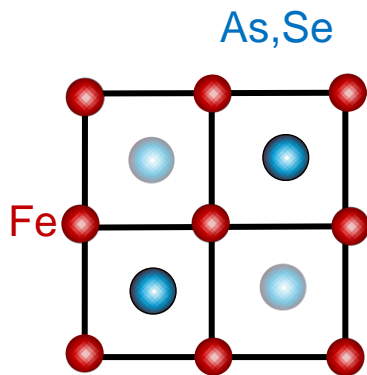
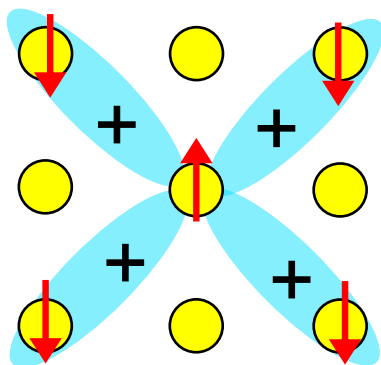
$S_{+-}$

Spin fluctuations

$k$ -space (repulsive)



$r$ -space

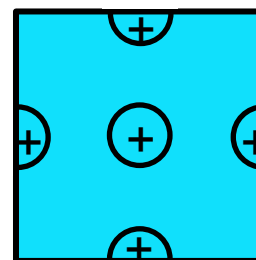


$$\Delta(\cos k_x \cos k_y)$$

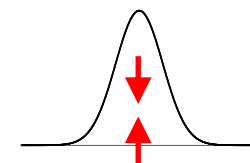
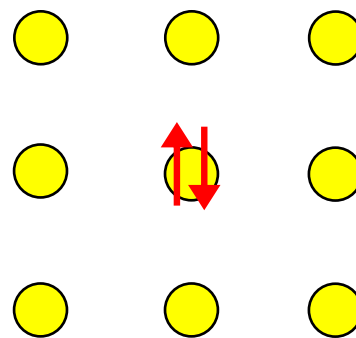
$S_{++}$

Orbital fluctuations

$k$ -space (attractive)



$r$ -space



$$\Delta$$

# Iron pnictides: candidate for the SC state



Chicken or the egg?

Spin fluctuations or orbital fluctuations?

AF I

ng

# Possible gap functions of iron-based superconductors

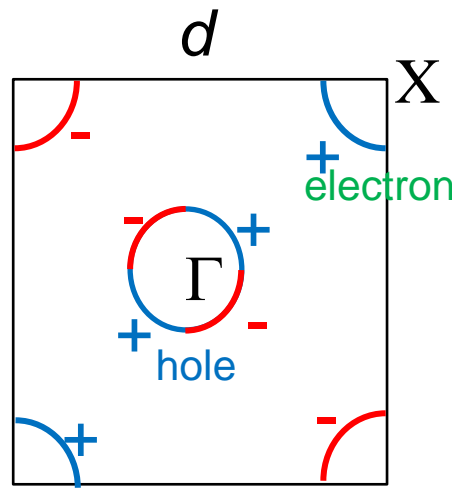
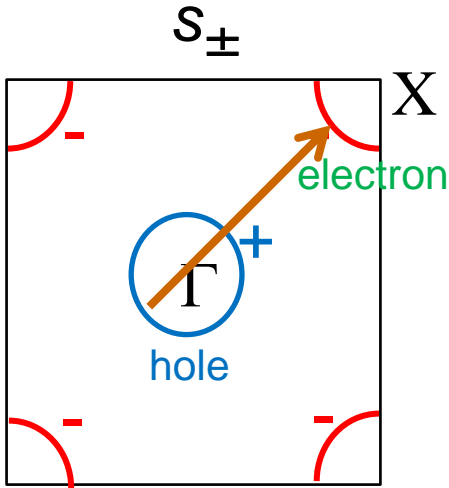
2D

Nodeless

Nodal

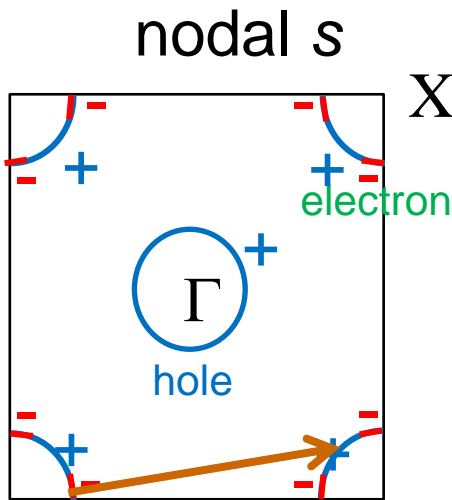
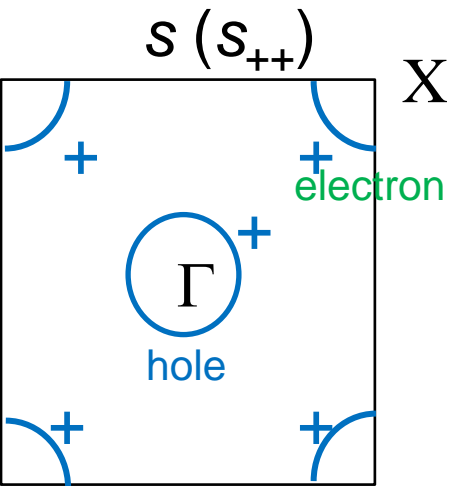
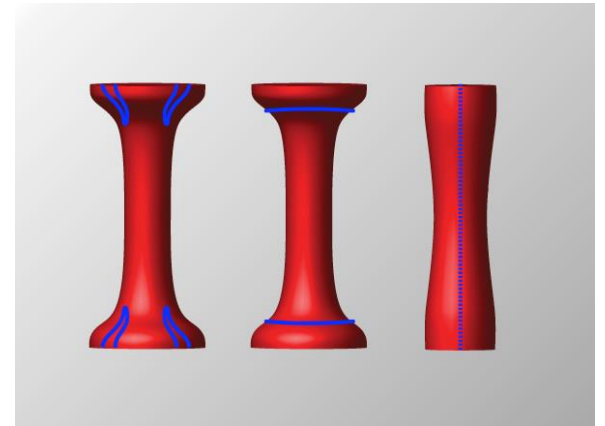
Large  $\chi(\mathbf{q})$

$\Delta(\mathbf{k}+\mathbf{q})\Delta(\mathbf{k}) < 0$   
Sign change



3D

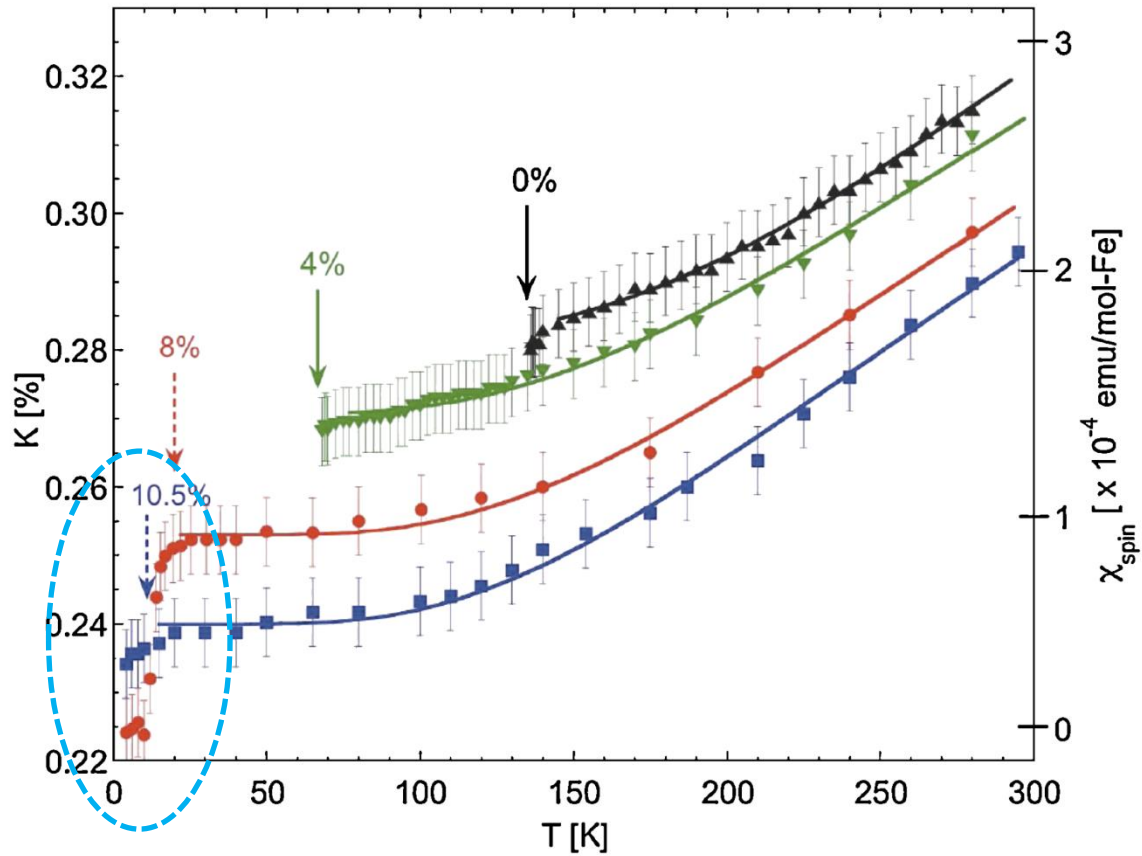
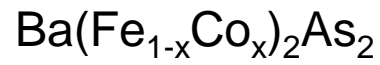
Node in hole band



Node in electron band



# Knight shift

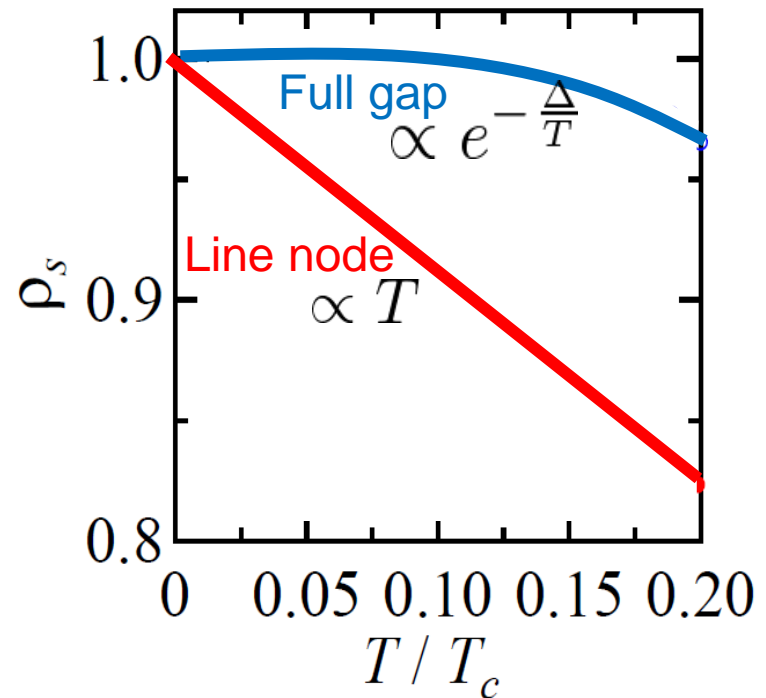
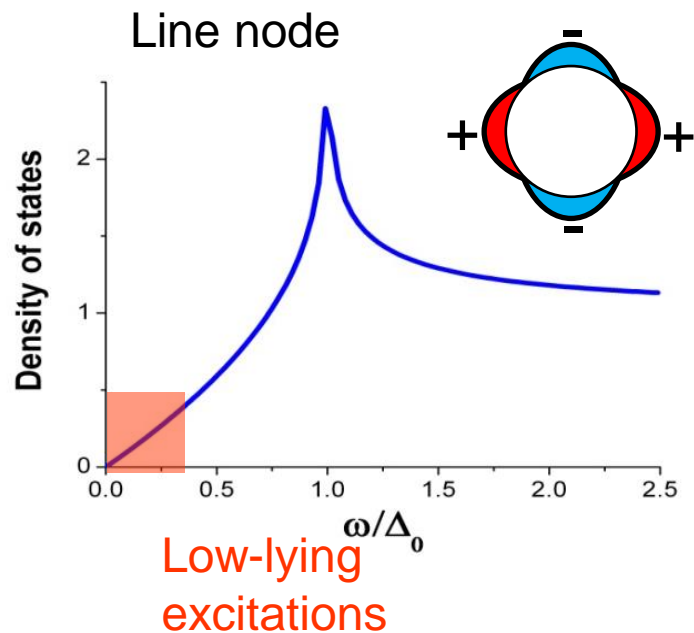
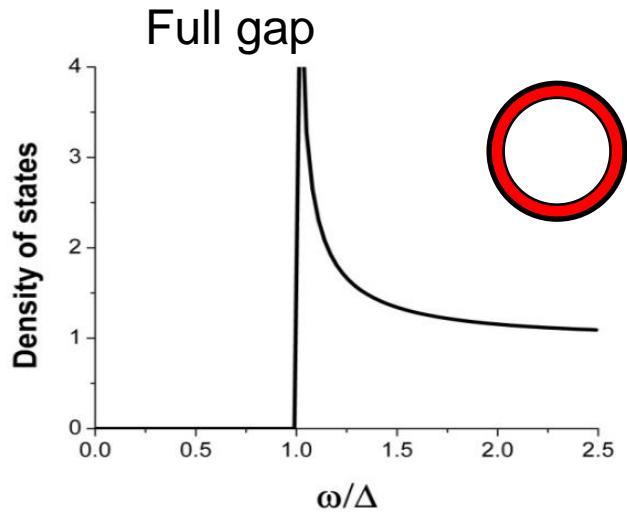


Spin-singlet



Full gap or nodal?

# Thermally excited QPs



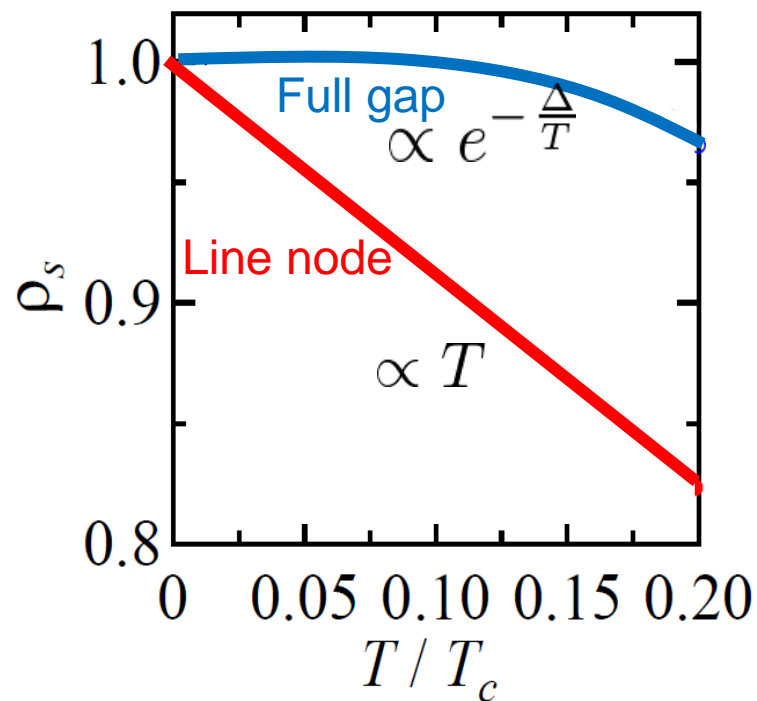
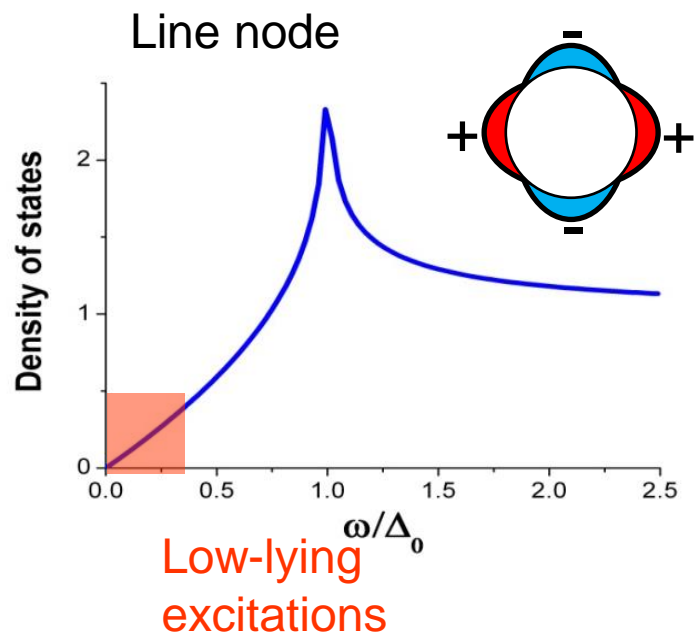
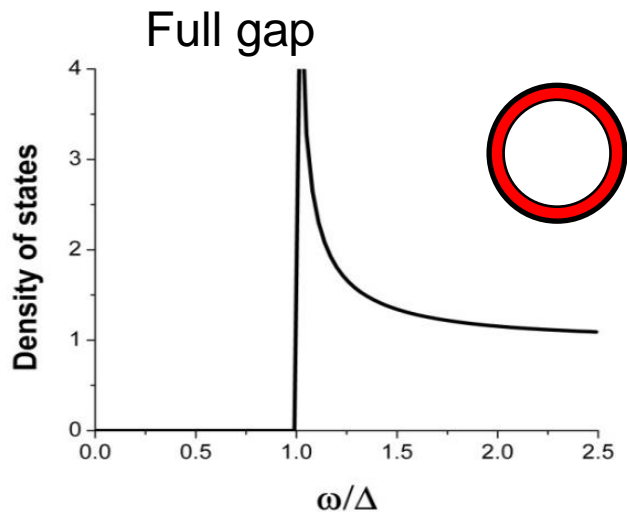
$$\rho_s = \frac{n_s(T)}{n_s(0)} n_s(T) \quad \text{Superfluid density}$$

$$\lambda_L = \left( \frac{m}{\mu_0 n e^2} \right)^{\frac{1}{2}}$$

London penetration depth

$$\rho_s = \frac{\lambda_L^2(0)}{\lambda_L^2(T)}$$

# Gap structure



Line node

Full gap

$$\lambda_L^{-2} \propto T$$

$$\lambda_L^{-2} \propto e^{-\frac{\Delta}{T}}$$

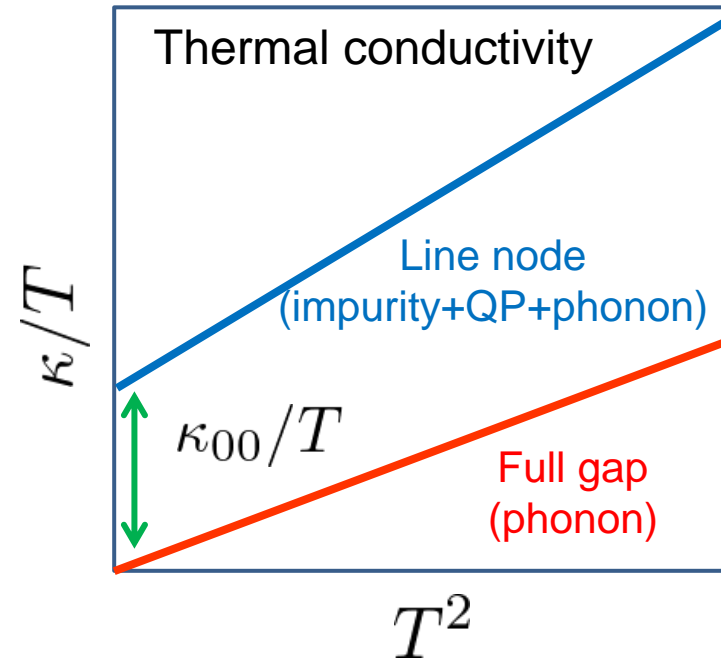
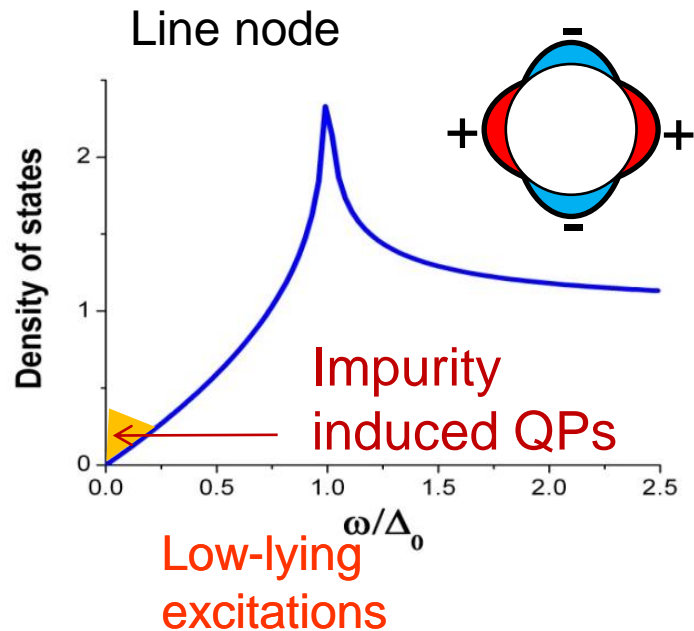
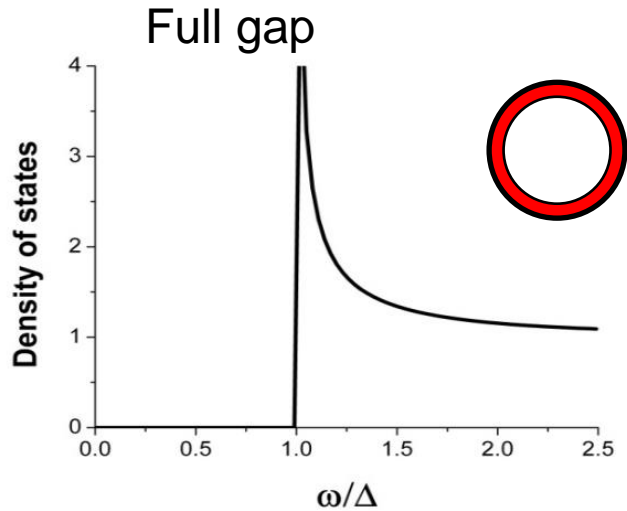
$$C \propto T^2$$

$$C \propto e^{-\frac{\Delta}{T}}$$

$$1/T_1 \propto T^3$$

$$1/T_1 \propto e^{-\frac{\Delta}{T}}$$

# Gap structure



Superfluid does not carry the heat

$$\kappa_e = C_e v_F^2 \tau \quad \kappa/T = \alpha + \beta T^2$$

$$\alpha = \kappa_{00}/T$$

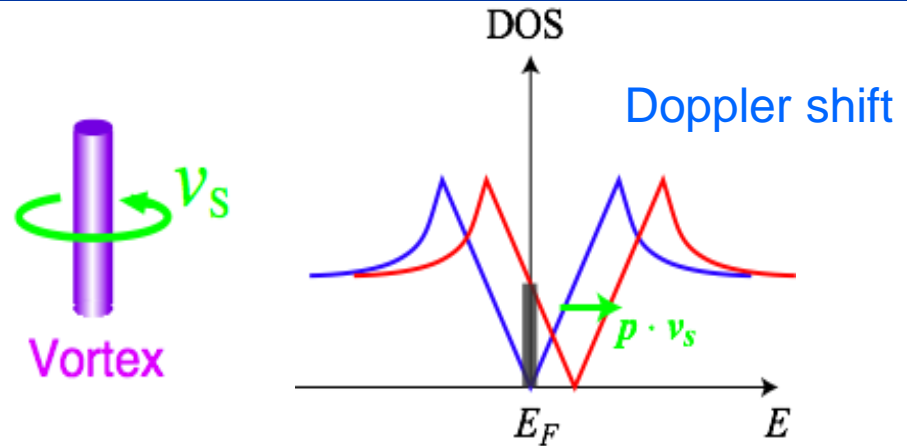
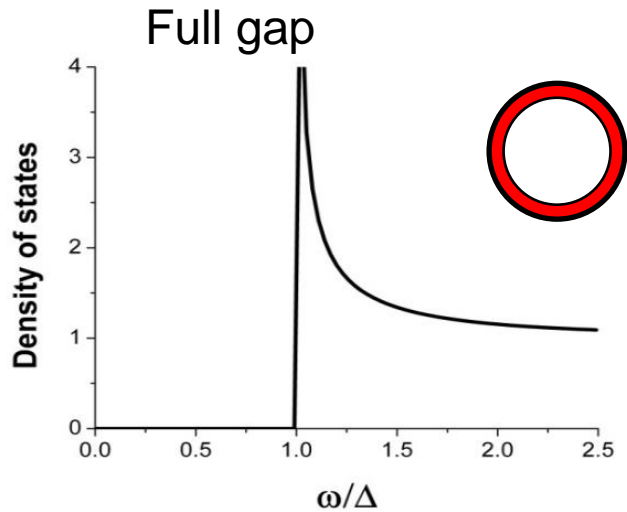
$$\kappa_{00}/T = N_{imp}(0) v_F^2 \tau_{imp}$$

$$\tau_{imp} \propto 1/N_{imp}(0)$$

Independent of impurity

Universal thermal conductivity

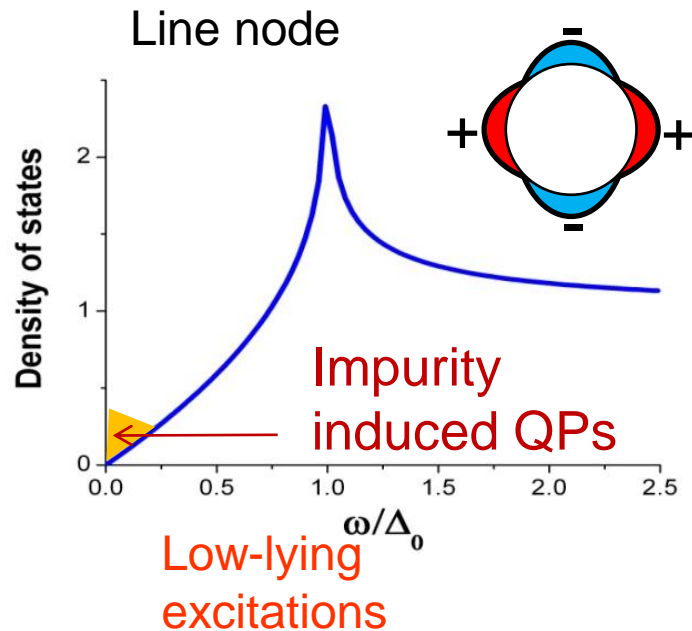
# Doppler shift of QP excitations



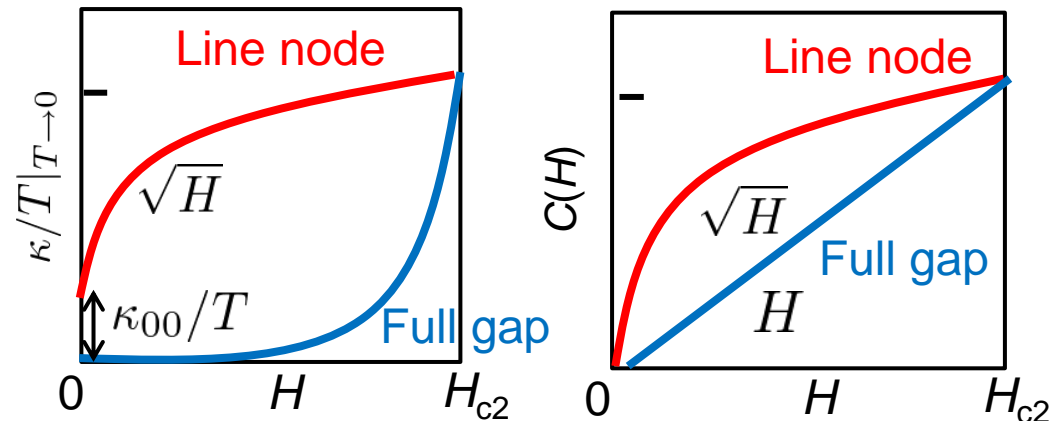
$$E'(\mathbf{p}) \rightarrow E(\mathbf{p}) + \mathbf{v}_s \cdot \mathbf{p}$$

$v_s$ : supercurrent

G.E. Volovik, JETP Lett. **58**, 469 (1993)



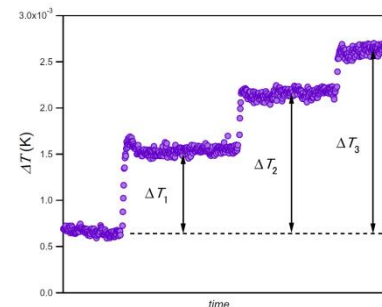
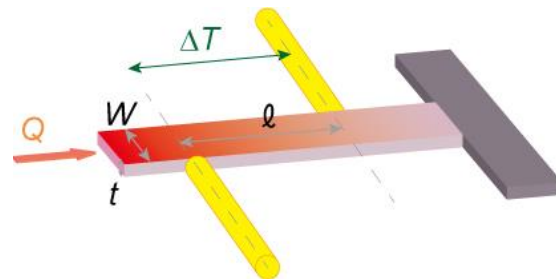
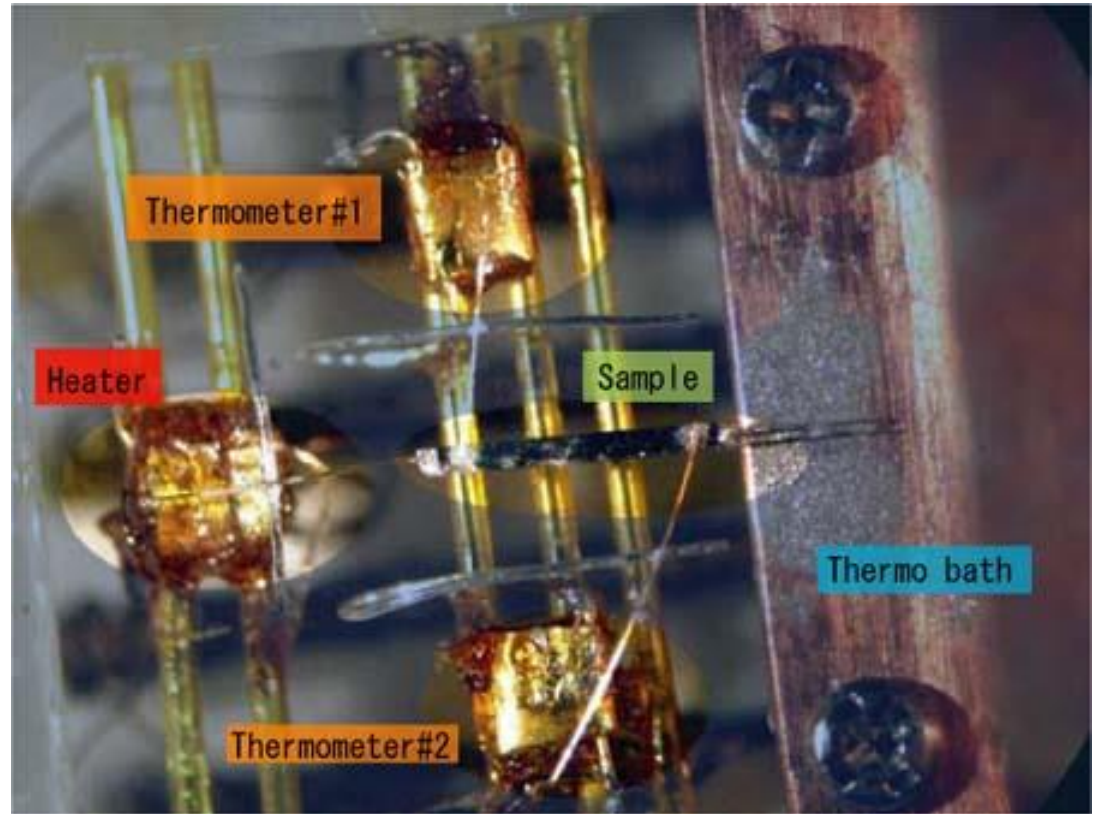
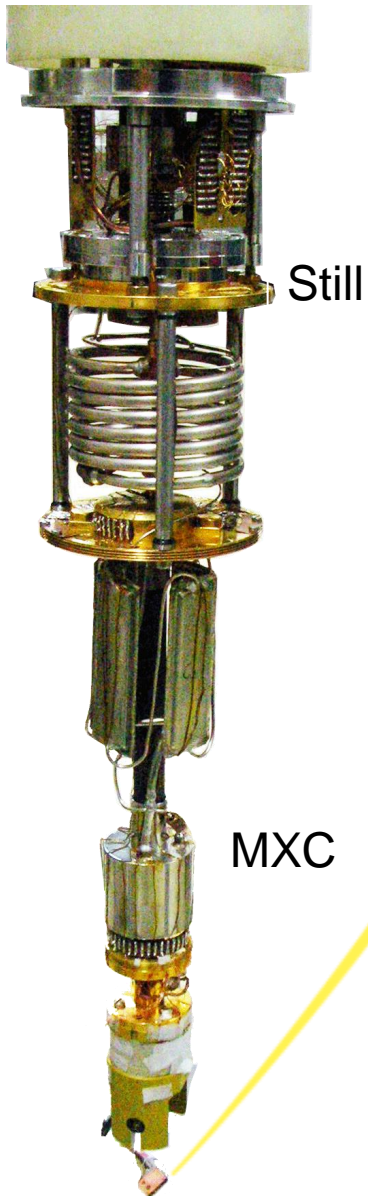
$$N(0) \sim \sqrt{H} \rightarrow C(H), \kappa(H) \sim \sqrt{H}$$



Thermal conductivity is governed by QPs **outside** of vortex core.

# Thermal conductivity Measurement below 1 K

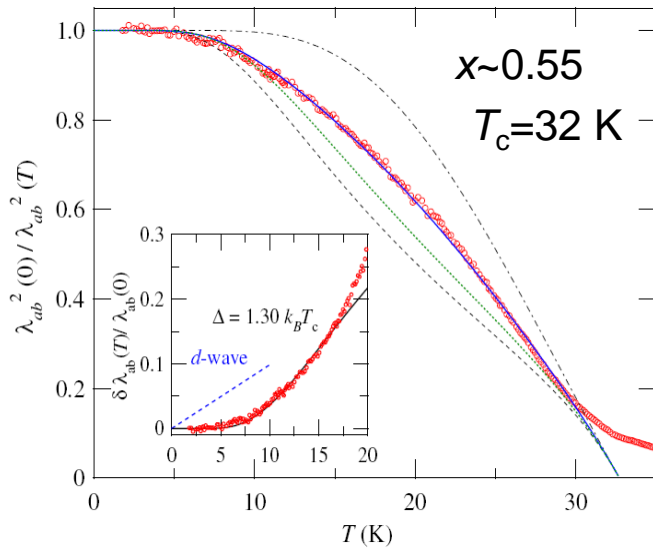
dilution refrigerator



# Full gap superconductivity

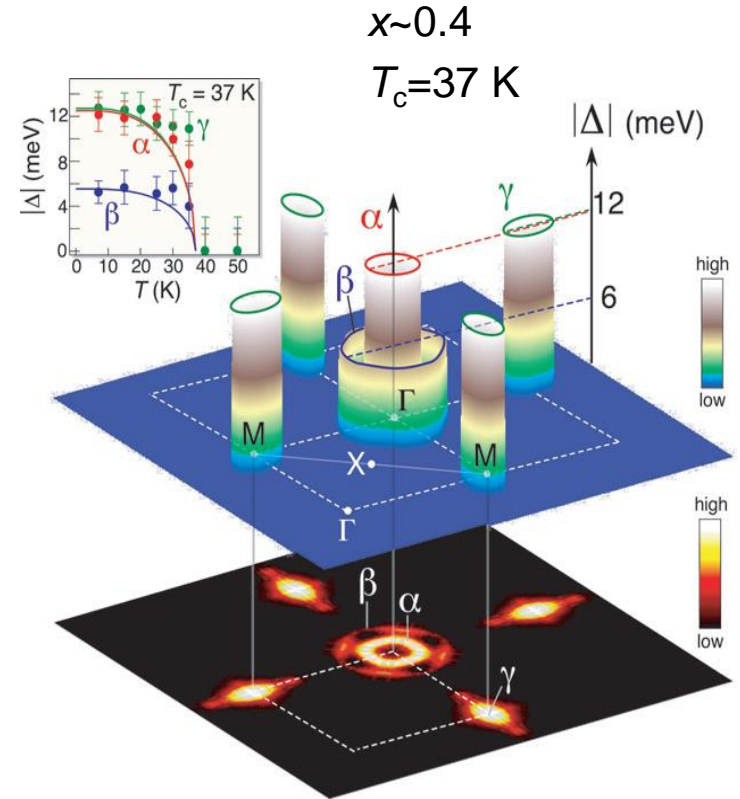
## Penetration depth

hole doped  $\text{Ba}_{1-x}\text{K}_x\text{Fe}_2\text{As}_2$



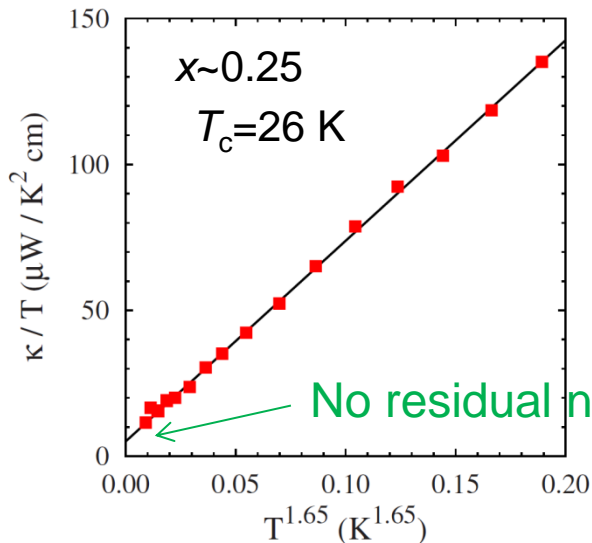
K. Hashimoto, *et al.*, PRL **102**, 027001 (2009).

## ARPES



H. Ding *et al.*, EPL **83**, 47001 (2008).

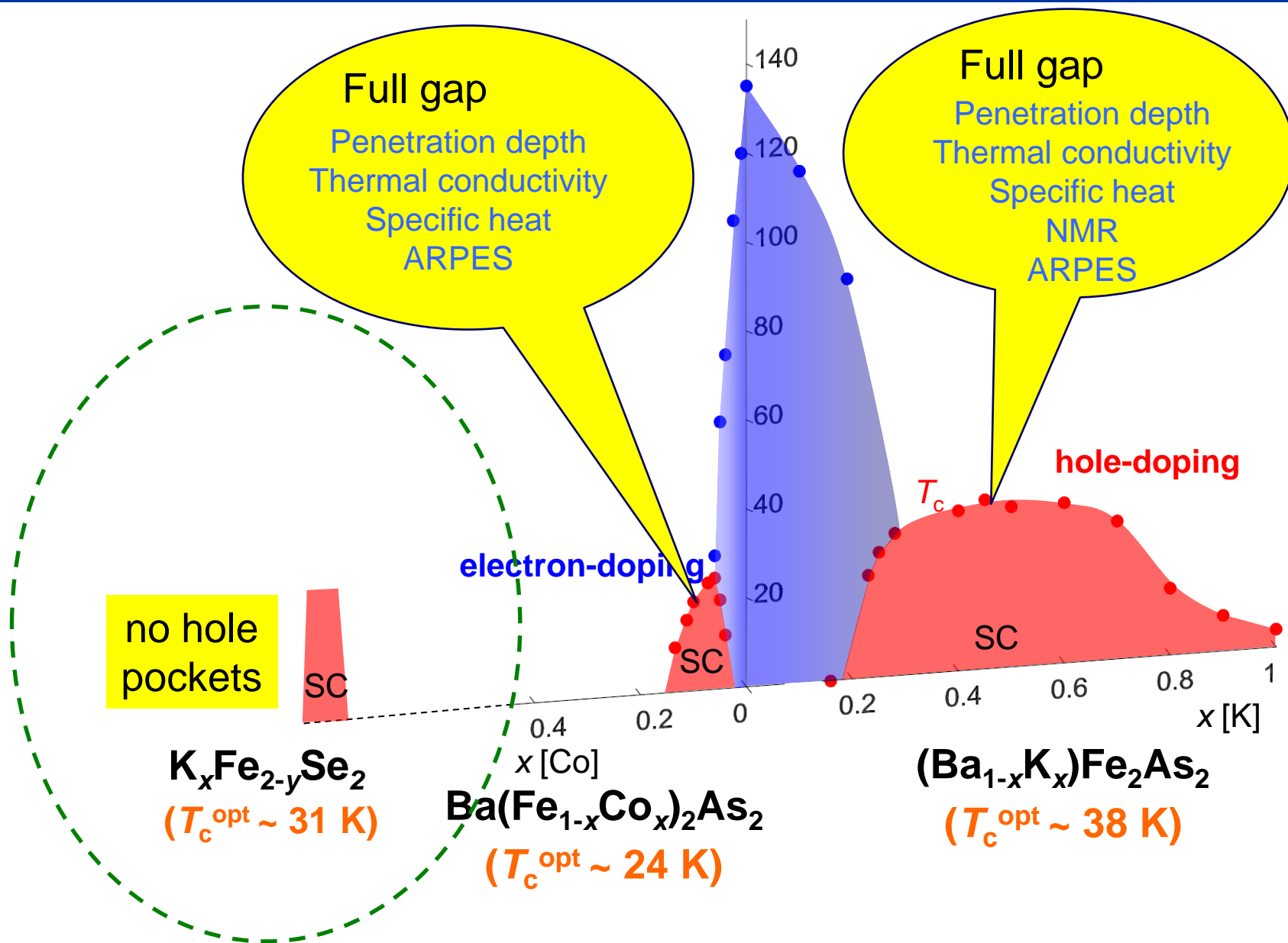
## Thermal conductivity



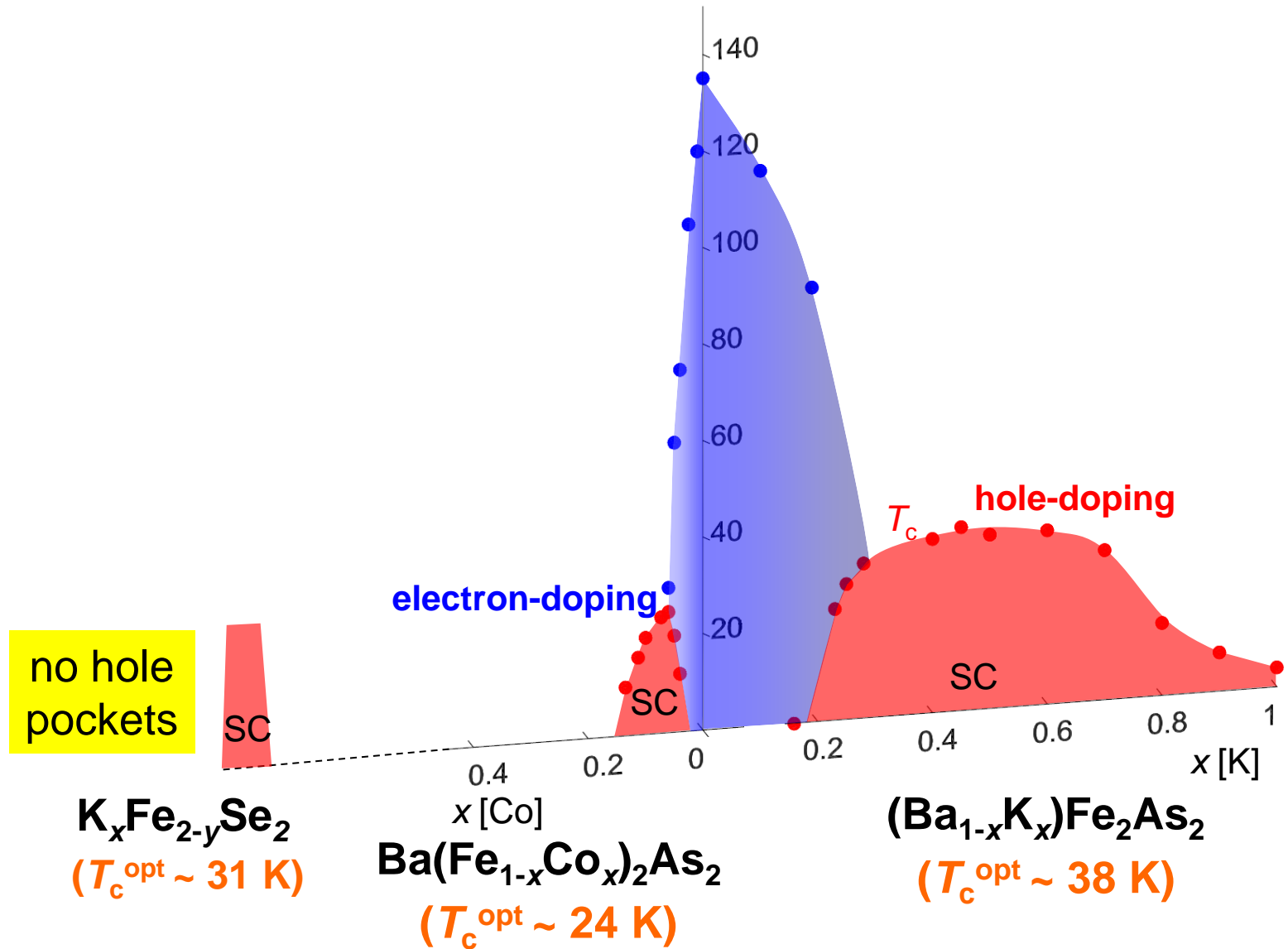
X.G. Luo *et al.* PRB **80**, 140503 (2009).



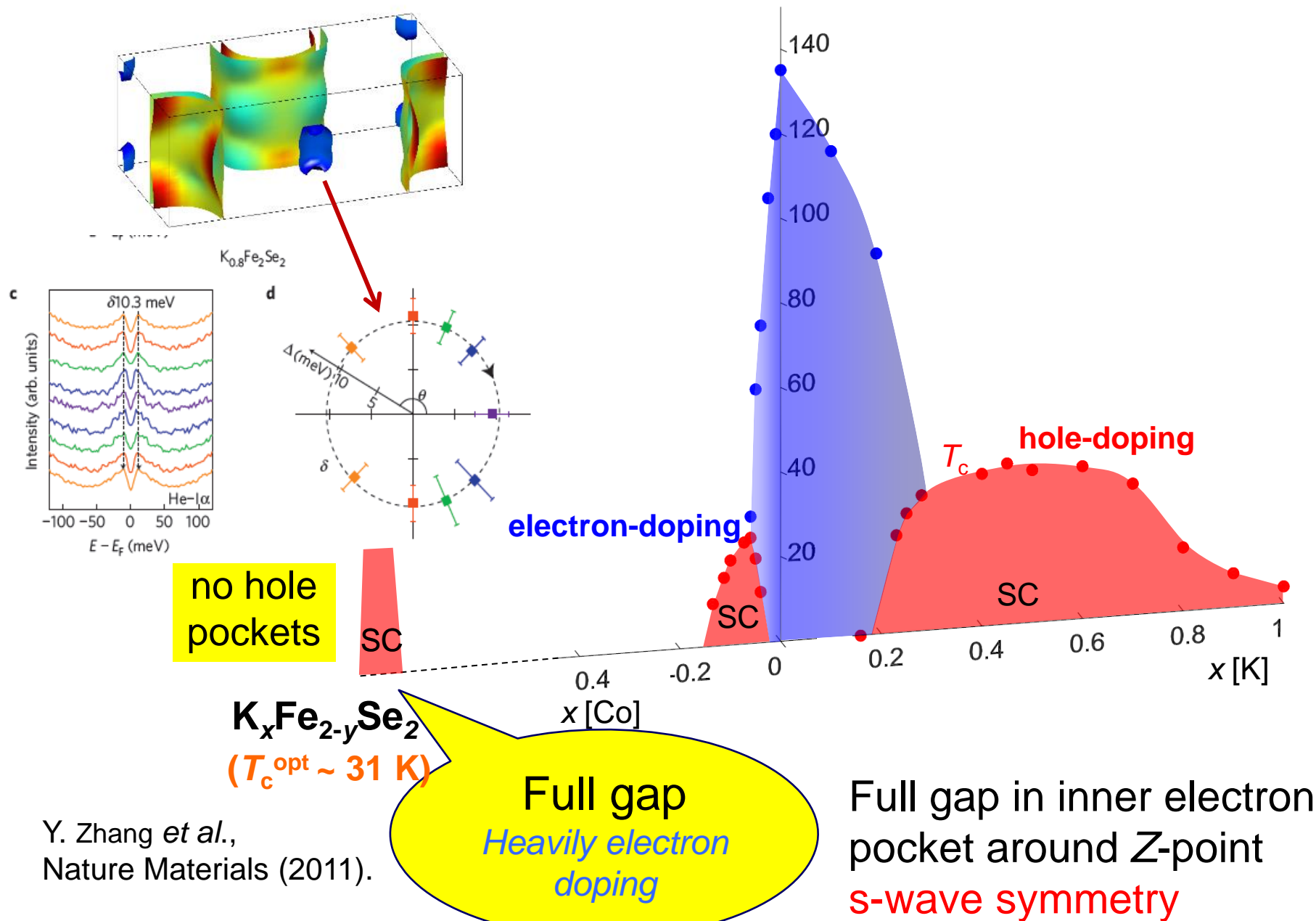
# Superconducting gap structure of BaFe<sub>2</sub>As<sub>2</sub> systems



# Superconducting gap structure of BaFe<sub>2</sub>As<sub>2</sub> systems

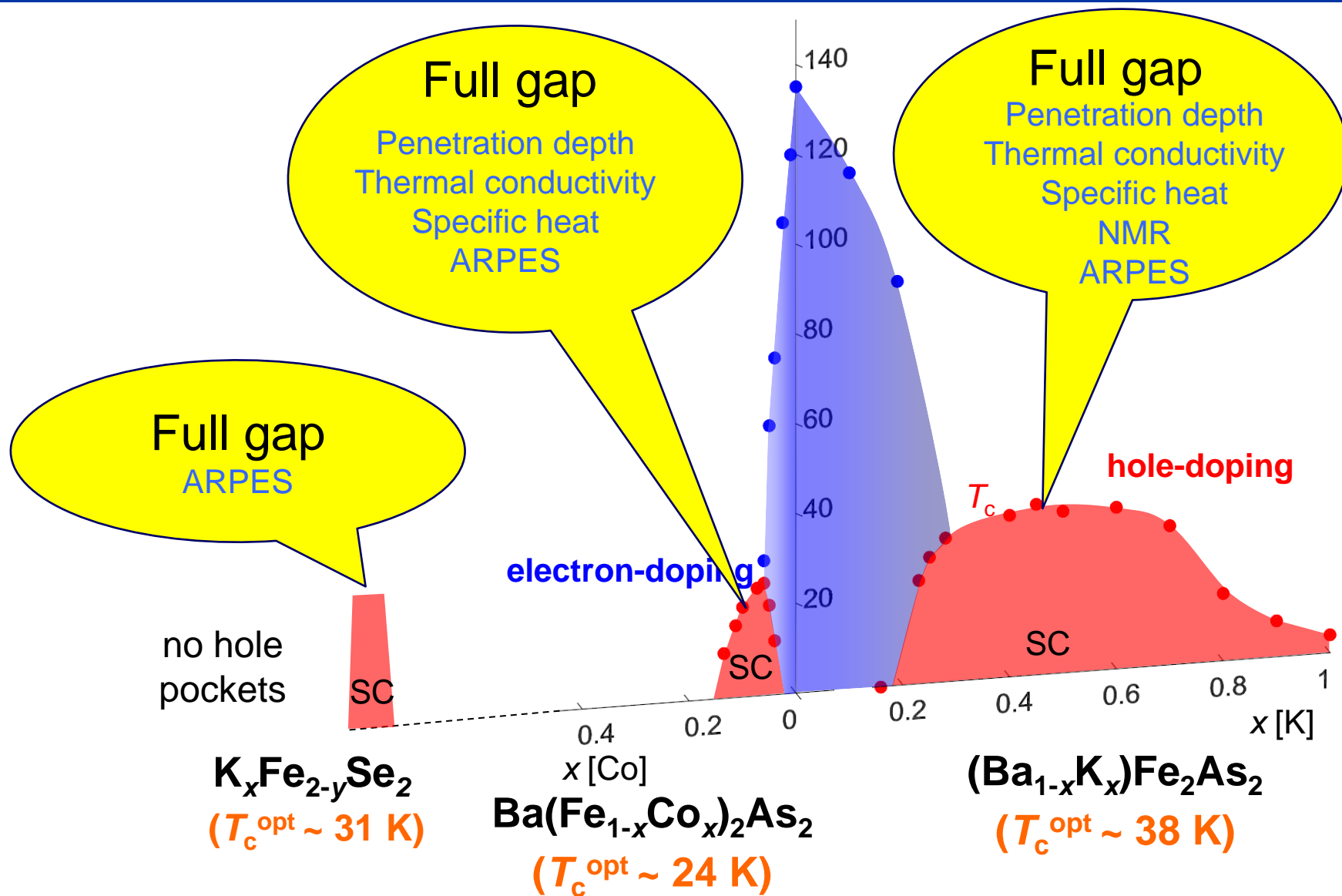


# SC gap structure in heavily electron doped systems



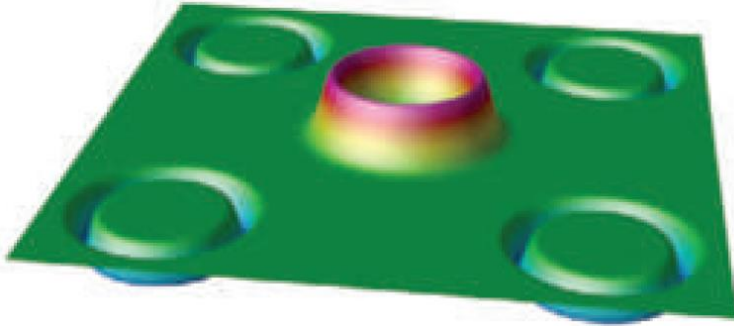
Y. Zhang *et al.*,  
Nature Materials (2011).

# Superconducting gap structure of BaFe<sub>2</sub>As<sub>2</sub> systems

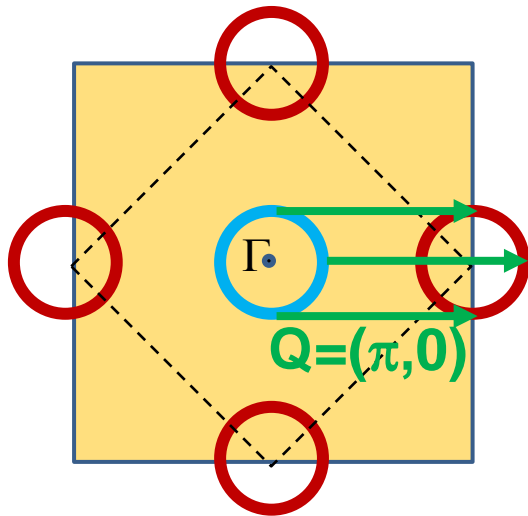


# Sign change or no sign change?

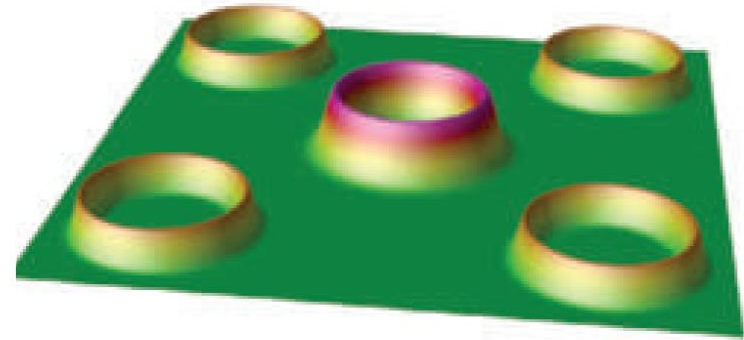
$S_{+-}$



Spin fluctuations

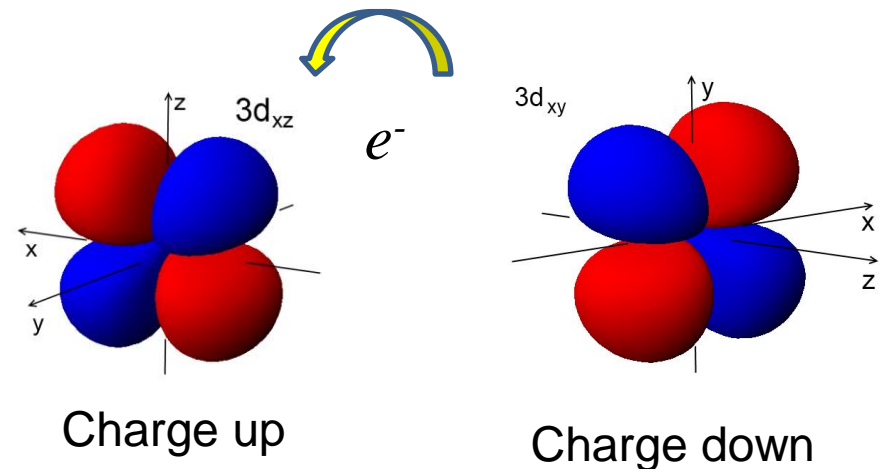


$S_{++}$



or

Orbital fluctuations  
(Quadrupole fluctuation)



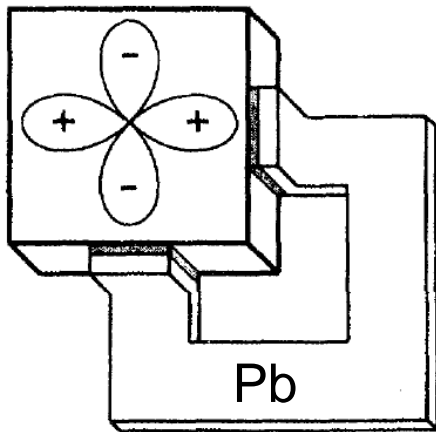
# S+- or S++?

1. Phase sensitive test
2. NMR
3. Neutron scattering
4. Quasi-particle interference
5. Impurity effect

# S+- or S++?: Phase sensitive tests



*d*-wave



PRL 102, 227007 (2009)

PHYSICAL REVIEW LETTERS

week ending  
5 JUNE 2009

## Possible Phase-Sensitive Tests of Pairing Symmetry in Pnictide Superconductors

D. Parker<sup>1</sup> and I.I. Mazin<sup>1</sup>

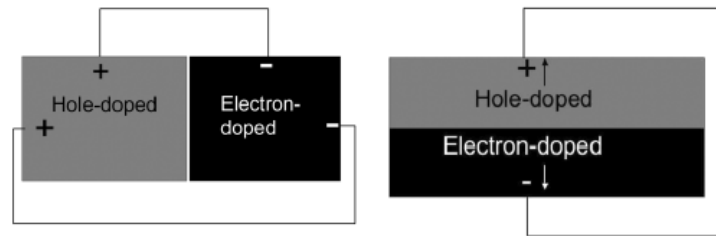
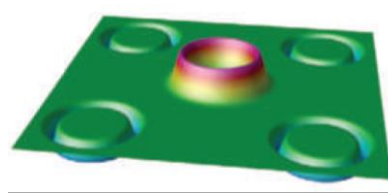


FIG. 3. A schematic view of the tunneling geometry for the proposed bicrystal experiments. Left: an *ab*-plane orientation with two possible lead orientations; right: a *c*-axis orientation.

Practically very difficult to fabricate such junctions

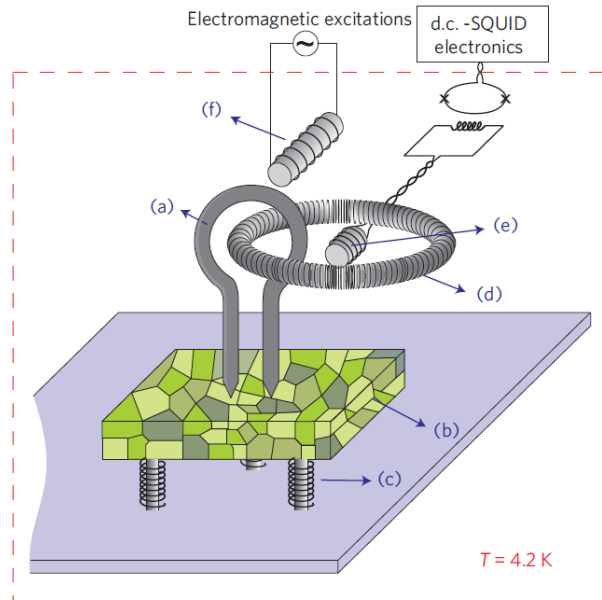
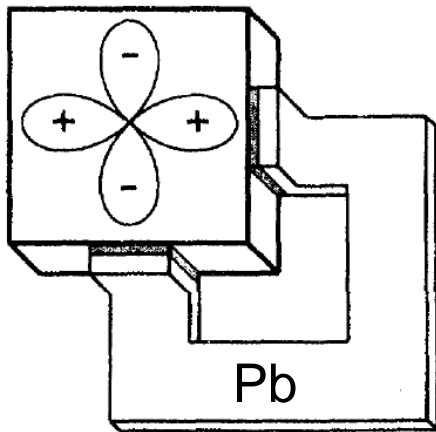


# S+- or S++?: Phase sensitive tests

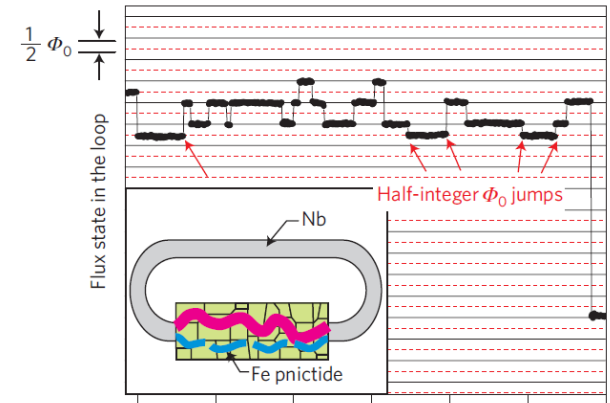


$S_{+-}$

d-wave



$\text{NdFeAsO}_{0.88}\text{F}_{0.12}$



C.T. Chen et al. Nature Phys. (10)

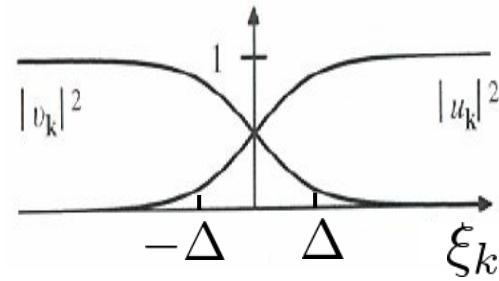
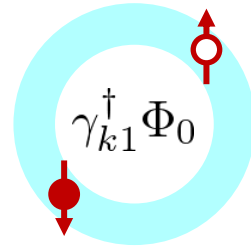
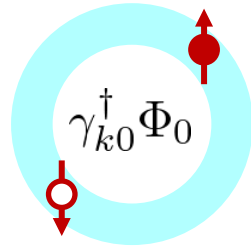
Experiments have been performed on polycrystals

# Sign change or no sign change?

Quasiparticle excitations from the SC ground state

$$\gamma_{k0}^\dagger = u_k c_{k\uparrow}^\dagger - v_k c_{-k\downarrow}$$

$$\gamma_{k1}^\dagger = u_k c_{-k\downarrow}^\dagger + v_k c_{k\uparrow}$$



$$|u_k|^2 = \frac{1}{2} \left( 1 + \frac{\xi_k}{\sqrt{\Delta_k^2 + \xi_k^2}} \right) \quad |v_k|^2 = \frac{1}{2} \left( 1 - \frac{\xi_k}{\sqrt{\Delta_k^2 + \xi_k^2}} \right) \quad \xi_k \equiv \frac{\hbar^2 k^2}{2m} - \varepsilon_F$$

**B-quasiparticle: a superposition of an electron and a hole**

$$\mathbf{k}\sigma \rightarrow \mathbf{k}'\sigma'$$

$$\mathcal{H}_1 = \sum_{k\sigma, k'\sigma'} B_{k\sigma, k'\sigma'} c_{k\sigma}^\dagger c_{k'\sigma'} \left\{ \begin{array}{l} B_{k\sigma, k'\sigma'} c_{k\sigma}^\dagger c_{k'\sigma'} \\ B_{-k'-\sigma', -k-\sigma} c_{-k'-\sigma'}^\dagger c_{-k-\sigma} \end{array} \right. \quad \text{connected by time-reversal symmetry}$$

## Coherence factor

Scattering of QPs  $(u_k u_{k'} \pm v_k v_{k'})^2 = \frac{1}{2} \left( 1 \pm \frac{\Delta^2}{E_k E_{k'}} \right)$

Creation and annihilation of two QPs  $(v_k u_{k'} \pm u_k v_{k'})^2 = \frac{1}{2} \left( 1 \pm \frac{\Delta^2}{E_k E_{k'}} \right)$

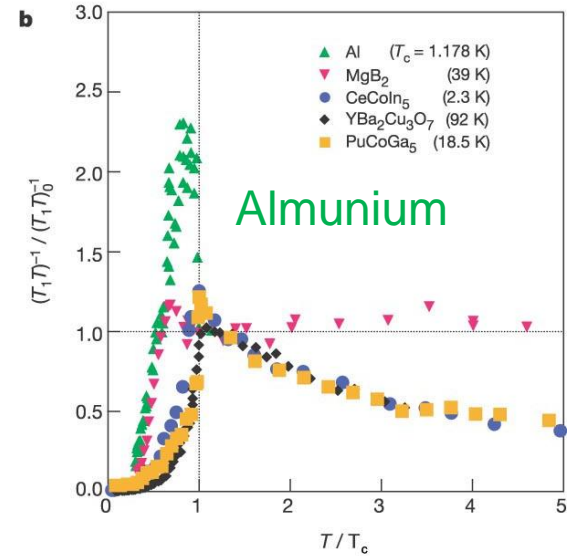
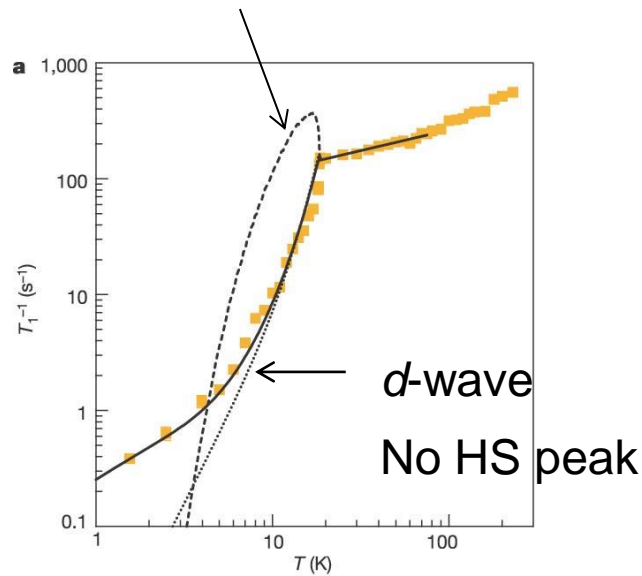
# S+- or S++?: NMR

$$\frac{1}{T_1 T} \propto \sum_{kk'} \left( 1 + \frac{\Delta_k \Delta_{k'}}{E_k E_{k'}} \right) \left[ -\frac{\partial f(E_k)}{\partial E_k} \right] \delta(E_k - E_{k'})$$

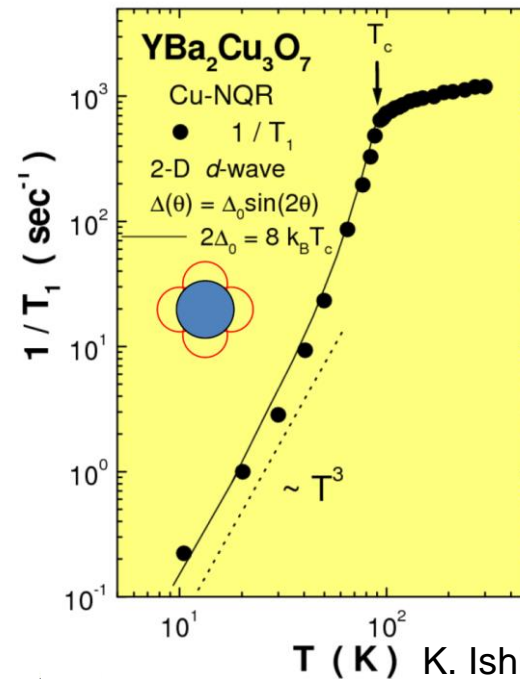
s-wave

$$\frac{1}{T_1} \propto \int_{\Delta(T)}^{\infty} dE \frac{E^2 + \Delta^2}{E^2 - \Delta^2} \operatorname{sech}^2 \left( \frac{E}{2T} \right)$$

Hebel-Slichter peak



N. Curro *et al.* Nature (12)



K. Ishida *et al.* JPSJ (93)

# S+- or S++?: NMR

$$\frac{1}{T_1 T} \propto \sum_{kk'} \left( 1 + \frac{\Delta_k \Delta_{k'}}{E_k E_{k'}} \right) \left[ -\frac{\partial f(E_k)}{\partial E_k} \right] \delta(E_k - E_{k'})$$

**S<sub>++</sub>**

$$\Delta_k = \Delta_{k'} = \Delta$$

$$\frac{1}{T_1} \propto \int_{\Delta(T)}^{\infty} dE \frac{E^2 + \Delta^2}{E^2 - \Delta^2} \operatorname{sech}^2 \left( \frac{E}{2T} \right)$$

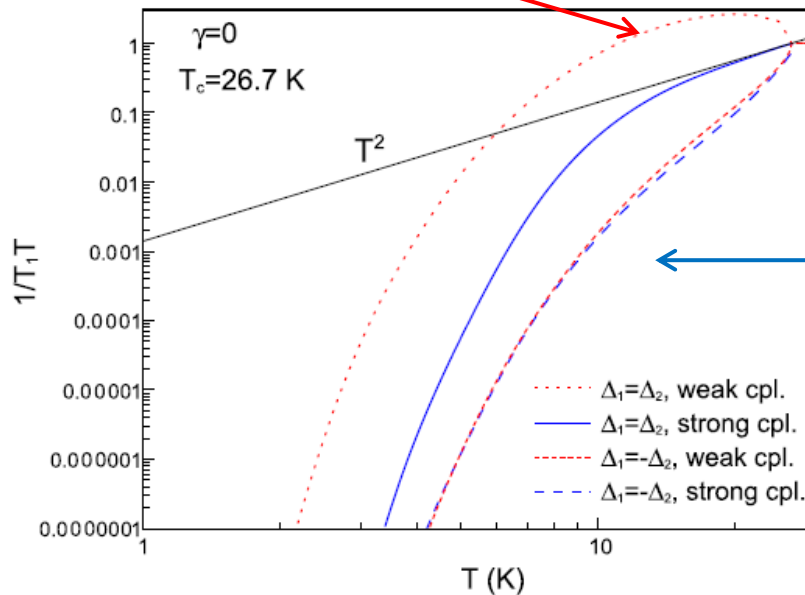
**S<sub>+-</sub>**

$$\Delta_k = -\Delta_{k'} = \Delta$$

$$\frac{1}{T_1} \propto \int_{\Delta(T)}^{\infty} dE \operatorname{sech}^2 \left( \frac{E}{2T} \right)$$

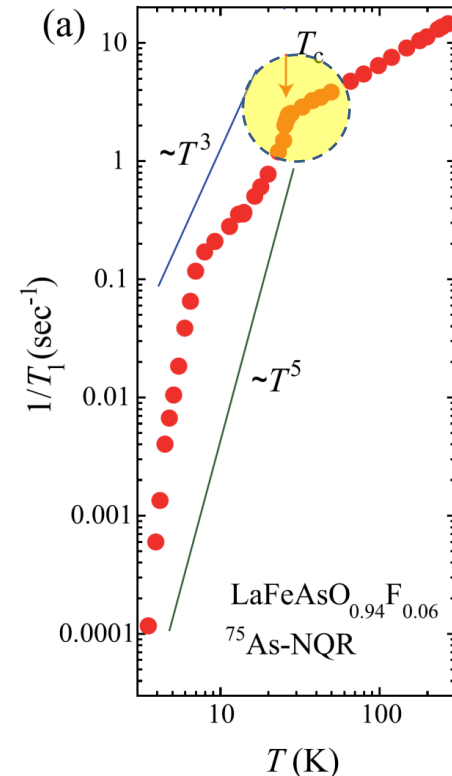
No HS peak

Hebel-Slichter peak



No HS peak

D. Parker *et al.*  
PRB (08)



T. Oka *et al.*  
PRL (12)

However, the HS peak readily disappears by inelastic scatterings, eg. Pb.

Absence of the coherence peak is not evidence of **S<sub>+-</sub>**

# S+- or S++?: Neutron resonance peak at Q

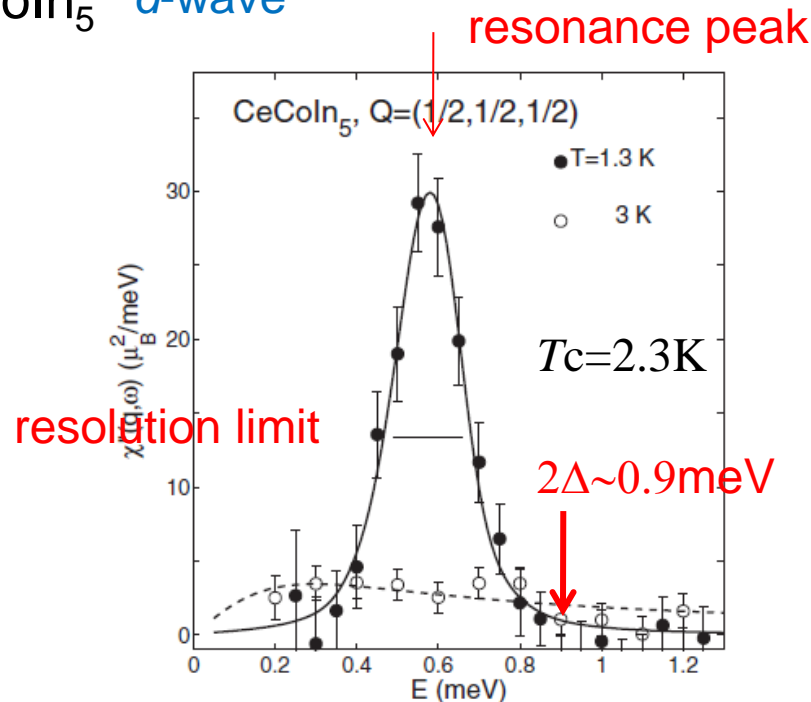
In the superconducting state

$$\text{Im}\chi_0(\mathbf{q}, \omega) = \frac{1}{4} \frac{1}{(2\pi)^3} \int d^3k \left( 1 - \frac{\Delta_k \Delta_{k+q}}{E_{k+q} E_k} \right) \delta(\omega - E_{k+q} - E_k) \quad E_k = \sqrt{\xi_k^2 + \Delta_k^2}$$

The coherence factor becomes 2 for  $\Delta_{k+Q} = -\Delta_k$

Sharp resonance peak at  $\omega_{\text{res}} < 2\Delta$

CeCoIn<sub>5</sub> *d-wave*



# S+- or S++?: Neutron resonance peak at Q

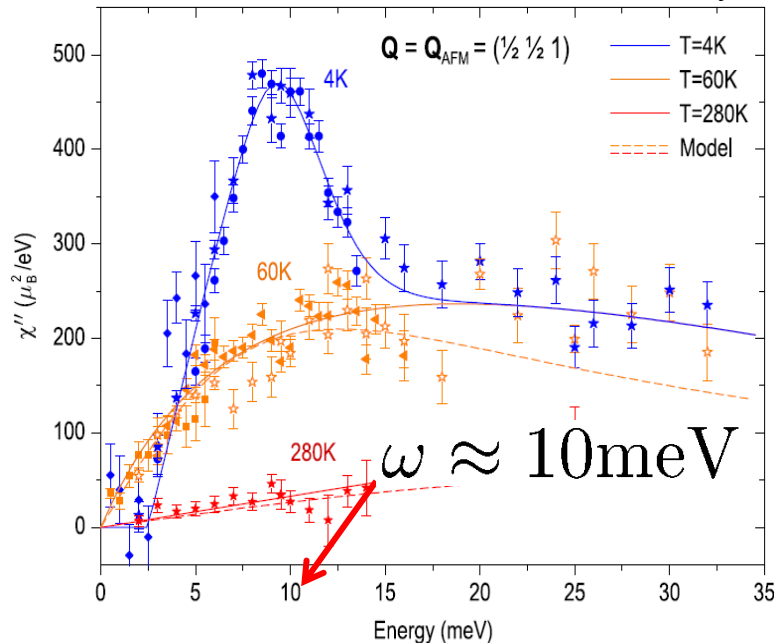
In the superconducting state

$$\text{Im}\chi_0(\mathbf{q}, \omega) = \frac{1}{4} \frac{1}{(2\pi)^3} \int d^3k \left( 1 - \frac{\Delta_k \Delta_{k+q}}{E_{k+q} E_k} \right) \delta(\omega - E_{k+q} - E_k) \quad E_k = \sqrt{\xi_k^2 + \Delta_k^2}$$

The coherence factor becomes 2 for  $\Delta_{\mathbf{k}+\mathbf{Q}} = -\Delta_{\mathbf{k}}$

- $S_{+-}$       Sharp resonance peak at  $\omega_{\text{res}} < 2\Delta$  ( $\Delta_{\text{el}} + \Delta_{\text{hole}}$ )
- $S_{++}$       Broad peak at  $\omega_{\text{res}} > 2\Delta$  ( $\Delta_{\text{el}} + \Delta_{\text{hole}}$ )

BaFe<sub>1.85</sub>Co<sub>0.15</sub>As<sub>2</sub> Inosov *et al.*, Nat. Phys. (10).



ARPES (bulk-sensitive):

$$\Delta_{\text{el}} + \Delta_{\text{hole}} \approx 11.6 \text{ meV}$$

Terashima *et al.*, PNAS 2009

penetration depth:

$$\Delta_{\text{el}} + \Delta_{\text{hole}} \approx 8.4 \text{ meV}$$

Luan *et al.*, PRL 2011

specific heat:

$$\Delta_{\text{el}} + \Delta_{\text{hole}} \approx 7 \text{ meV}$$

Hardy *et al.*, EPL 2010

# S+- or S++?: Neutron resonance peak at Q

In the superconducting state

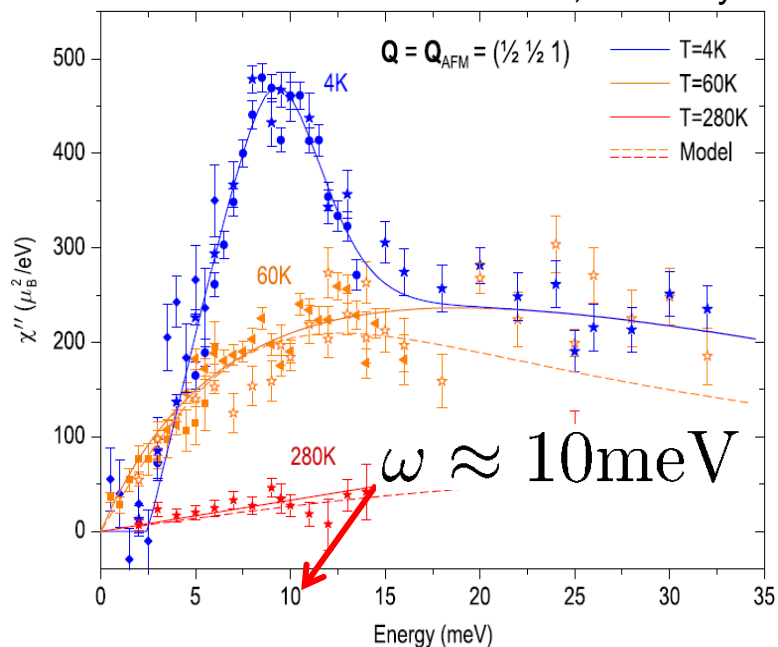
$$\text{Im}\chi_0(\mathbf{q}, \omega) = \frac{1}{4} \frac{1}{(2\pi)^3} \int d^3k \left( 1 - \frac{\Delta_k \Delta_{k+q}}{E_{k+q} E_k} \right) \delta(\omega - E_{k+q} - E_k) \quad E_k = \sqrt{\xi_k^2 + \Delta_k^2}$$

The coherence factor becomes 2 for  $\Delta_{k+Q} = -\Delta_k$

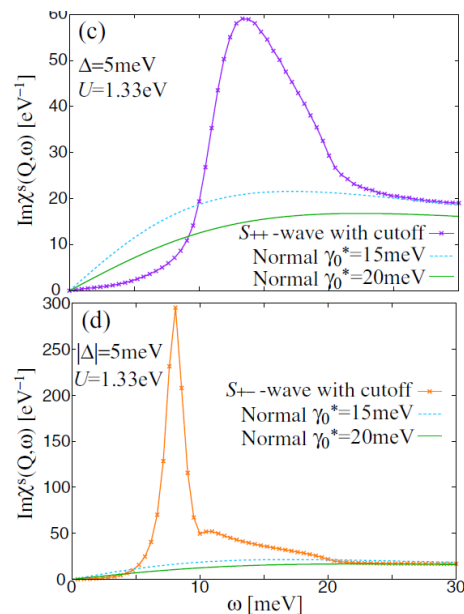
$S_{+-}$       Sharp resonance peak at  $\omega_{\text{res}} < 2\Delta$  ( $\Delta_{\text{el}} + \Delta_{\text{hole}}$ )

$S_{++}$       Broad peak at  $\omega_{\text{res}} > 2\Delta$  ( $\Delta_{\text{el}} + \Delta_{\text{hole}}$ )

BaFe<sub>1.85</sub>Co<sub>0.15</sub>As<sub>2</sub> Inosov *et al.*, Nat. Phys. (10).



S. Onari and H. Kontani, PRB (11)



Neutron scattering experiments can be explained by either models.

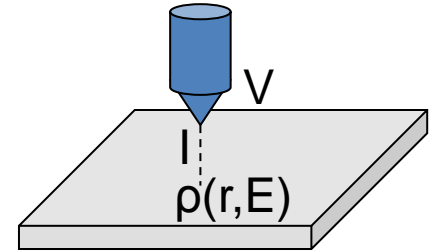


# S+- or S++?: Quasiparticle interference (QPI)

## Quasi-Particle Interference

$$Z(\mathbf{r}, E) \equiv \frac{dI/dV(\mathbf{r}, +E)}{dI/dV(\mathbf{r}, -E)} = \frac{\rho(\mathbf{r}, +E)}{\rho(\mathbf{r}, -E)} \xrightarrow{\text{FT}} Z(\mathbf{q}, E)$$

Tunnel conductance



No impurity (no scattering)  $Z(\mathbf{q}, E) = 0$  for  $\mathbf{q} \neq 0$   
 Nonmagnetic impurity

QP scattering probability (SC state)

$$w(\mathbf{k}\sigma \rightarrow \mathbf{k}'\sigma) \propto |V(\mathbf{k}, \mathbf{k}')|^2 \underbrace{(u_k u_{k'} - v_k v_{k'})^2}_{\text{coherence factor}}$$

Nonmagnetic  
(no spin flip)

matrix element

coherence factor

$$(u_k u_{k'} - v_k v_{k'})^2 = \frac{1}{2} \left( 1 - \frac{\Delta_k \Delta_{k'}}{E_k E_{k'}} \right)$$

sign-preserving scattering

$$\Delta_k \Delta_{k'} > 0 \quad (u_k u_{k'} - v_k v_{k'})^2 \quad \text{small}$$

sign-reversing scattering

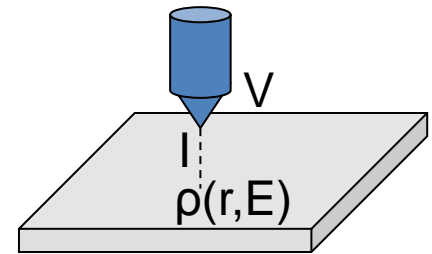
$$\Delta_k \Delta_{k'} < 0 \quad (u_k u_{k'} - v_k v_{k'})^2 \quad \text{large}$$

# S+- or S++?: Quasiparticle interference (QPI)

## Quasi-Particle Interference

$$Z(\mathbf{r}, E) \equiv \frac{dI/dV(\mathbf{r}, +E)}{dI/dV(\mathbf{r}, -E)} = \frac{\rho(\mathbf{r}, +E)}{\rho(\mathbf{r}, -E)} \xrightarrow{\text{FT}} Z(\mathbf{q}, E)$$

Tunnel conductance

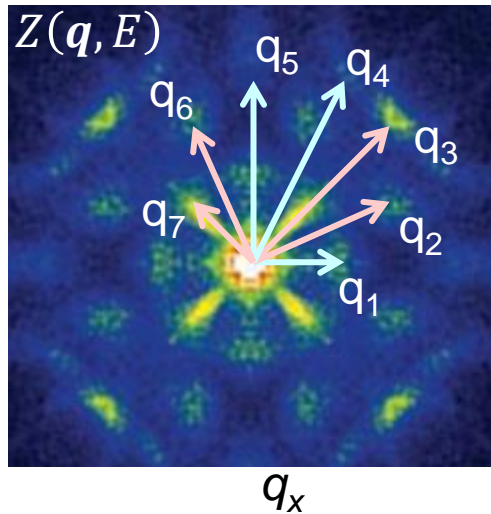
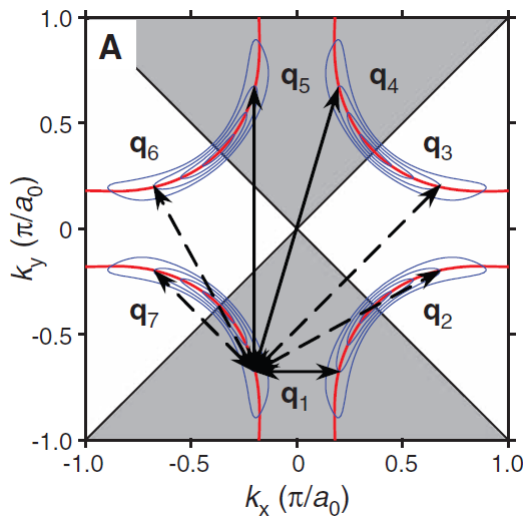


No impurity (no scattering)  $Z(\mathbf{q}, E) = 0$  for  $\mathbf{q} \neq 0$   
 Nonmagnetic impurity

## Cuprate : Octet Model

J. Hoffman *et al.*, Science (2002), K. McElroy, *et al.*, Nature (2003).

$\Delta_{\mathbf{k}}$  and  $\Delta_{\mathbf{k}+\mathbf{q}}$  {  
 sign-preserving scattering => suppression  
 sign-reversing scattering => enhancement



sign-preserving  
 $(\mathbf{q}_1, \mathbf{q}_4, \mathbf{q}_5)$

sign-reversing  
 $(\mathbf{q}_2, \mathbf{q}_3, \mathbf{q}_6, \mathbf{q}_7)$

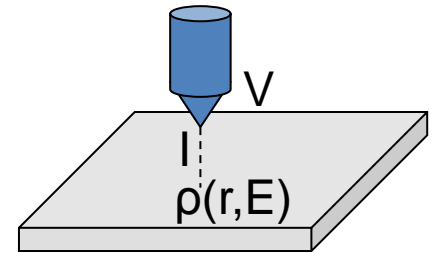
T. Hanaguri *et al.*

# S+- or S++?: Quasiparticle interference (QPI)

## Quasi-Particle Interference

Tunnel conductance

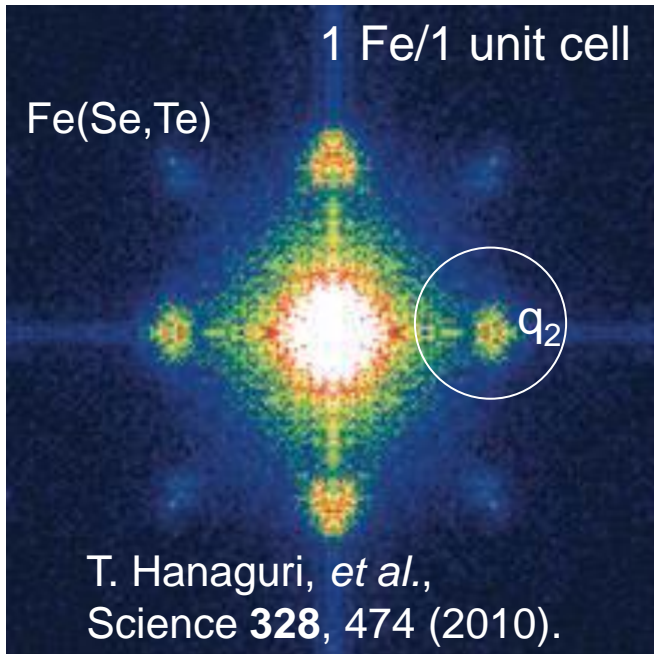
$$Z(\mathbf{r}, E) \equiv \frac{dI/dV(\mathbf{r}, +E)}{dI/dV(\mathbf{r}, -E)} = \frac{\rho(\mathbf{r}, +E)}{\rho(\mathbf{r}, -E)} \xrightarrow{\text{FT}} Z(\mathbf{q}, E)$$



No impurity (no scattering)  $Z(\mathbf{q}, E) = 0$  for  $\mathbf{q} \neq 0$   
 Nonmagnetic impurity

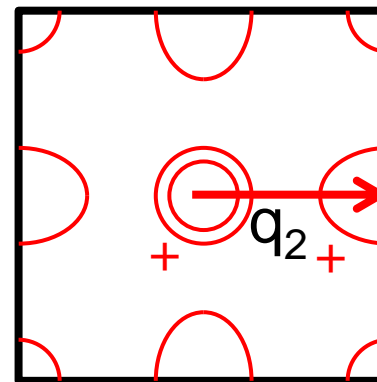
## Fe-based superconductor

$\Delta_{\mathbf{k}}$  and  $\Delta_{\mathbf{k}+\mathbf{q}}$   $\left\{ \begin{array}{l} \text{sign-preserving scattering} \Rightarrow \text{suppression} \\ \text{sign-reversing scattering} \Rightarrow \text{enhancement} \end{array} \right.$



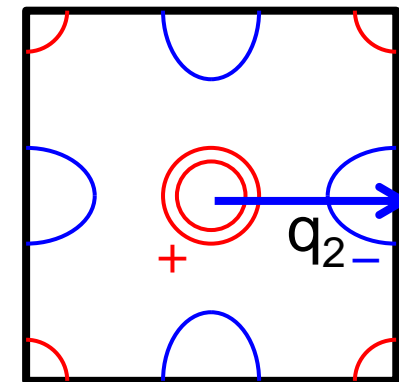
$q_y$

$S_{++}$ -wave SC



Zero at  $q_2$

$S_{\pm}$ -wave SC



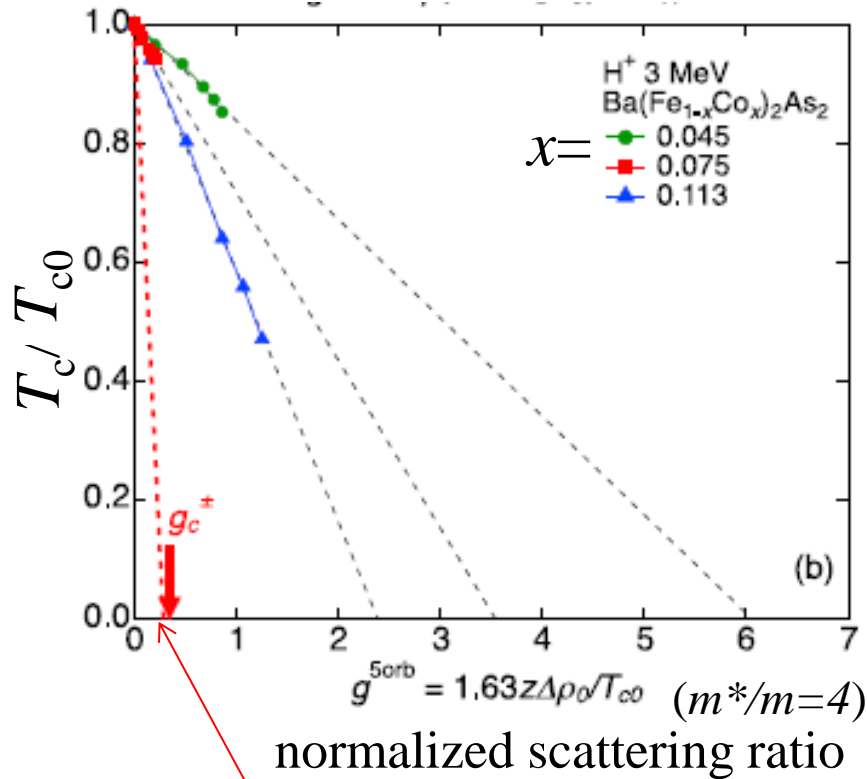
Peak at  $q_2$

However,  $q_2$  spot can appear even in  $S_{++}$  case when  $\Delta_e \neq \Delta_h$

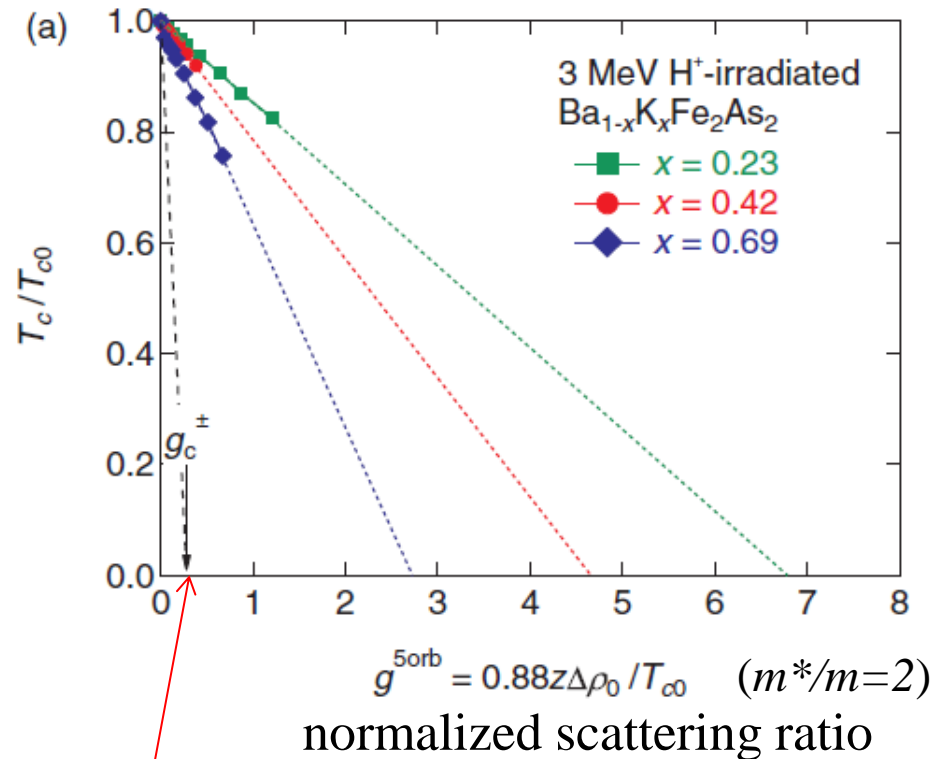
# S+- or S++?: Impurity effect



Nakajima *et al.*, Phys. Rev. B 82, 220504(R)



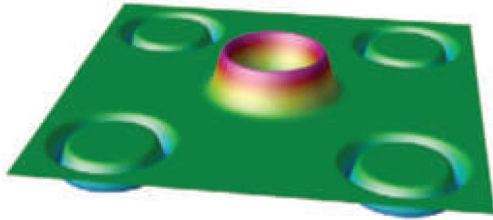
Taen *et al.*, Phys. Rev. B 88, 224514



theoretical prediction for  $S_{+-}$  wave (Onari and Kontani, PRL 2009)

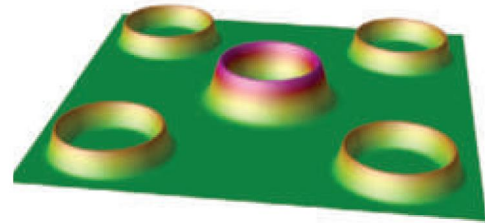
The robustness of the SC state against impurity contradicts with the  $S_{+-}$  wave state.

$S_{+-}$



?

$S_{++}$



?

No conclusive experimental evidence so far

# Are all iron-based high- $T_c$ superconductors fully gapped?

If some are nodal

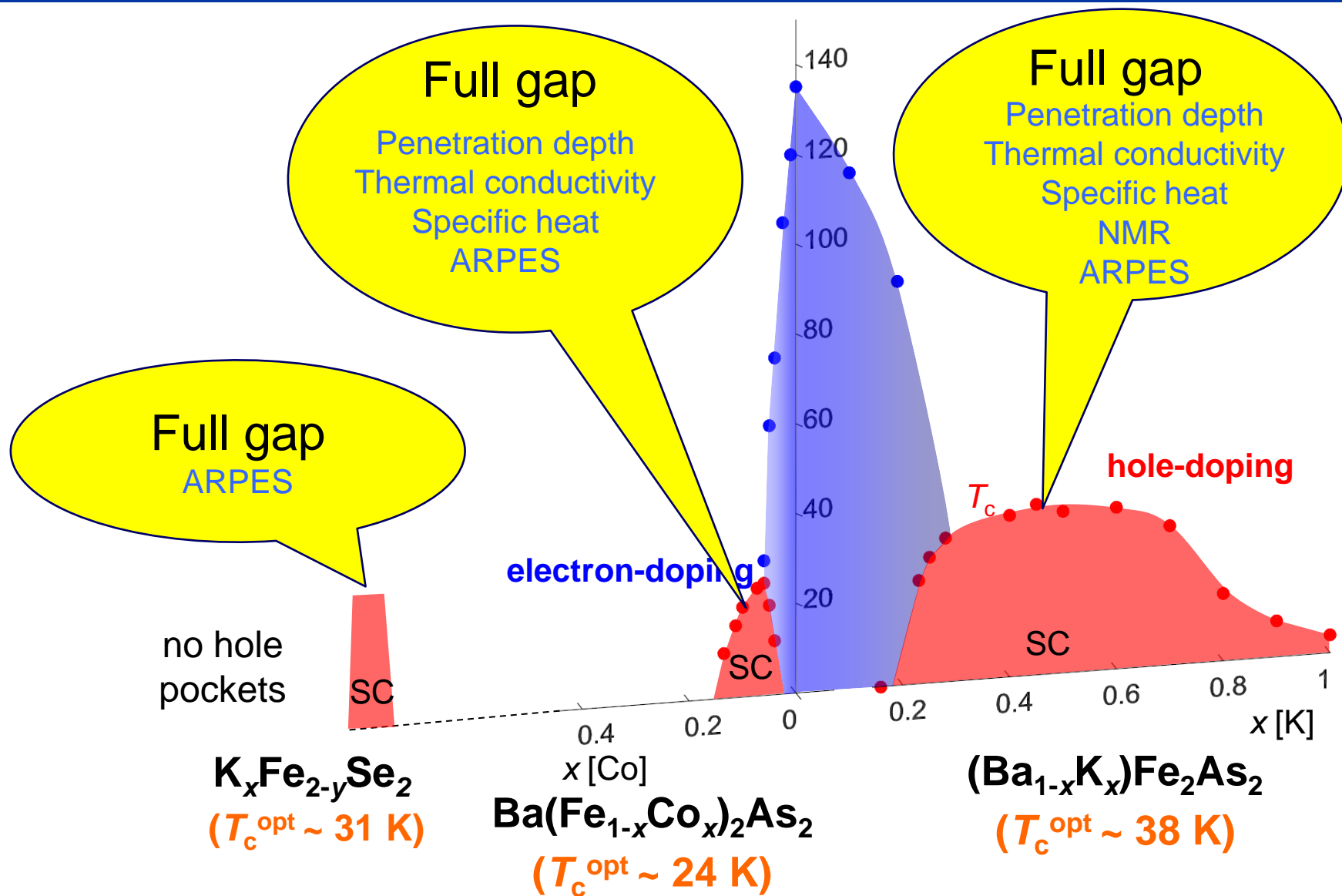
→ Presence of repulsive interaction

Accidental or symmetry protected?

If accidental

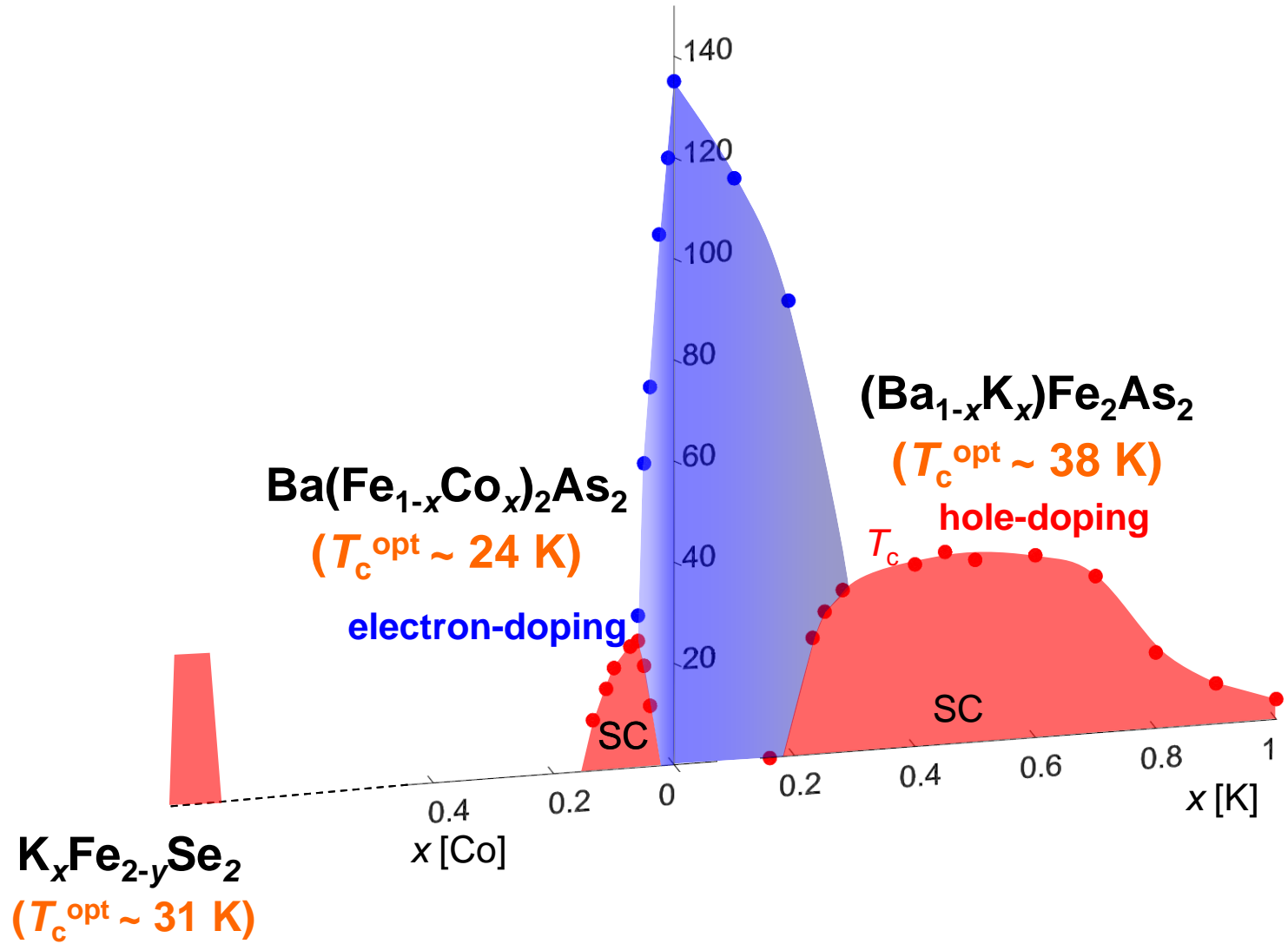
→ Presence of two (or more) competing pairing interactions

# Superconducting gap structure of BaFe<sub>2</sub>As<sub>2</sub> systems

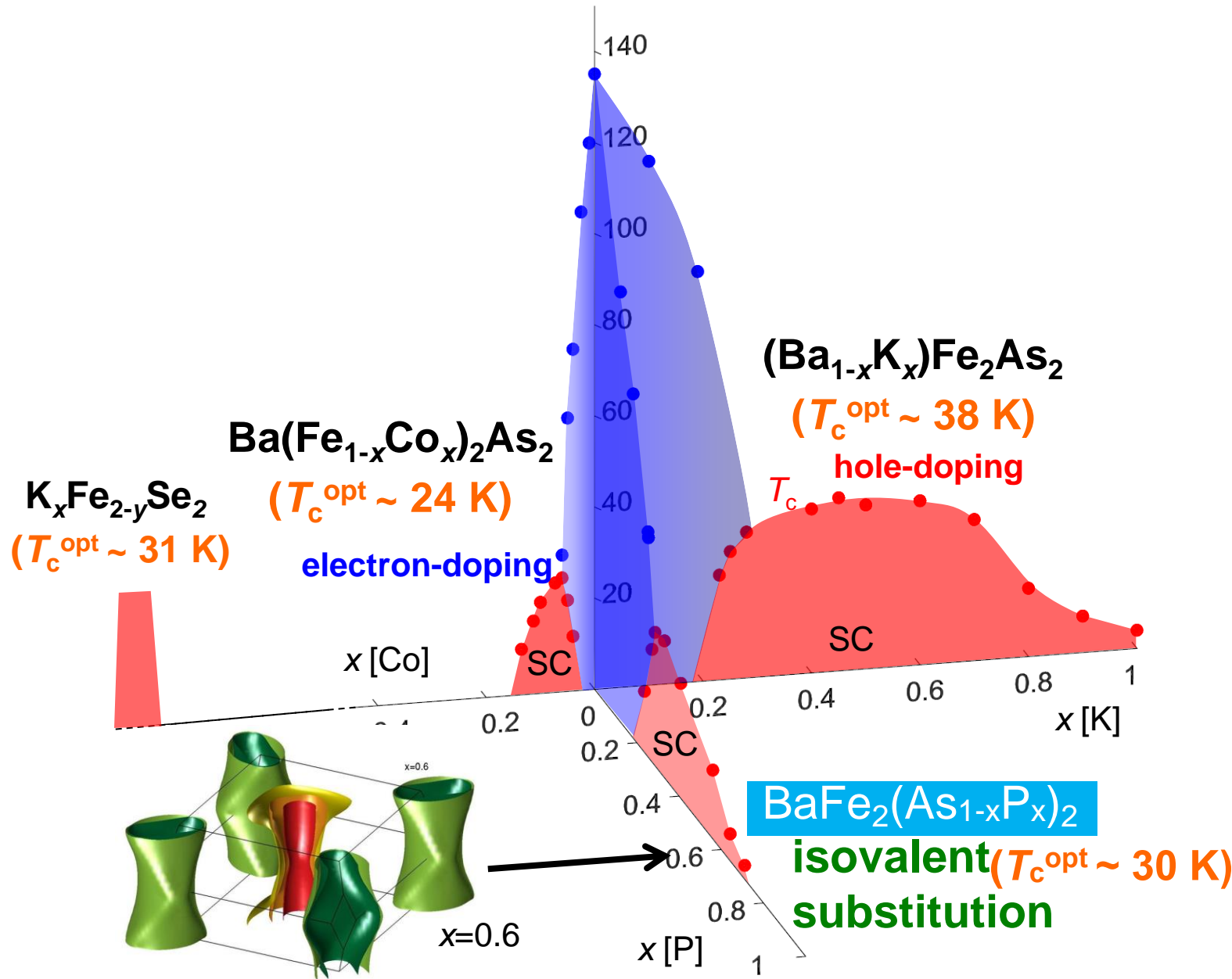




# SC gap structure in isovalent doped systems

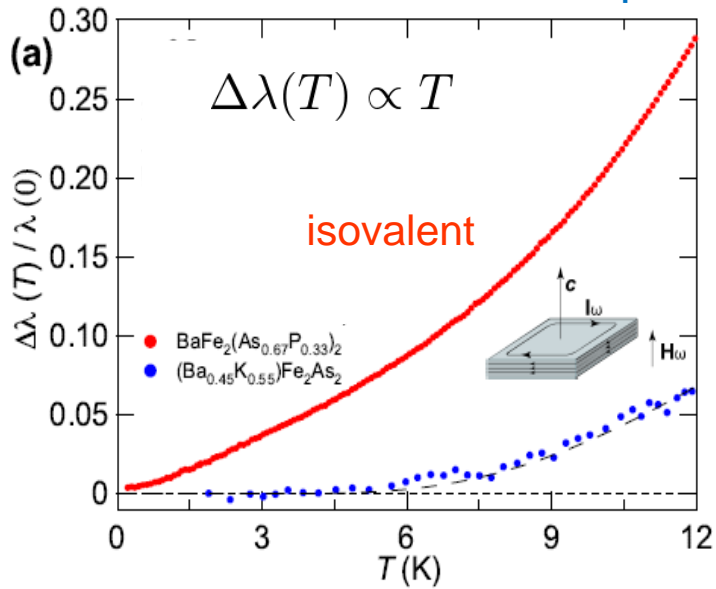


# SC gap structure in isovalent doped systems

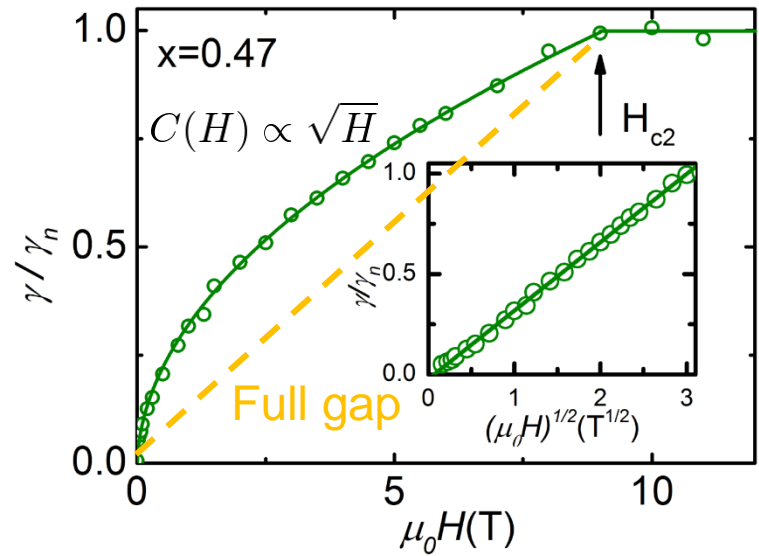


# SC gap structure in isovalent doped systems

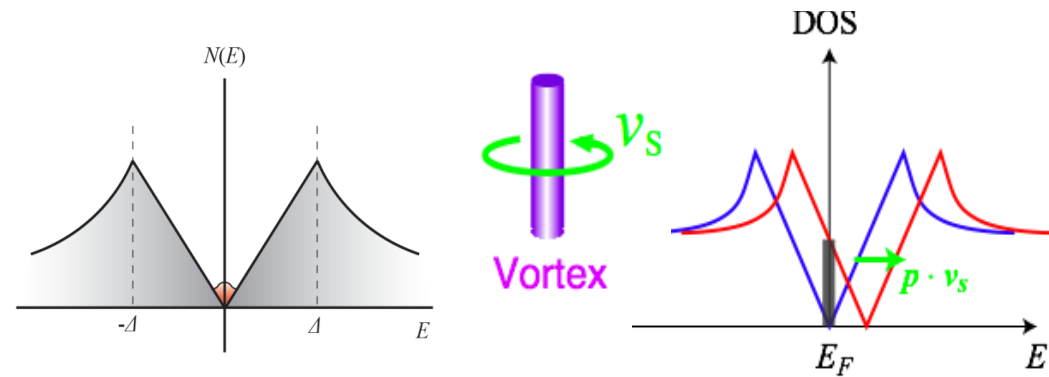
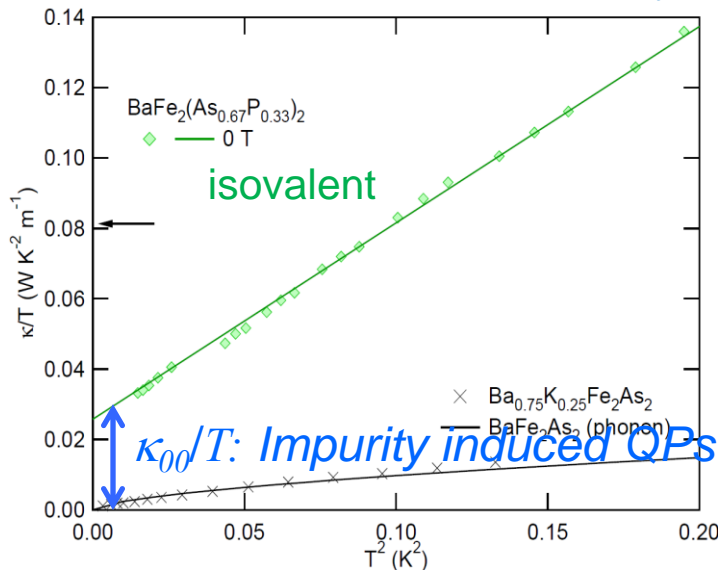
## Penetration depth



## Specific heat $\text{BaFe}_2(\text{As}_{0.53}\text{P}_{0.47})_2$



## Thermal conductivity

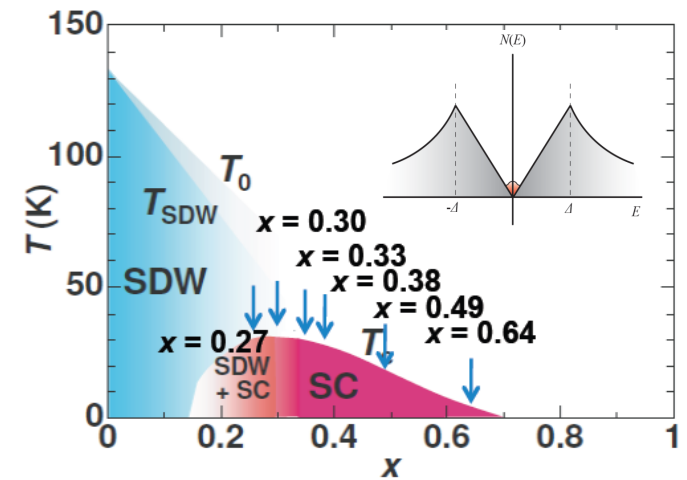
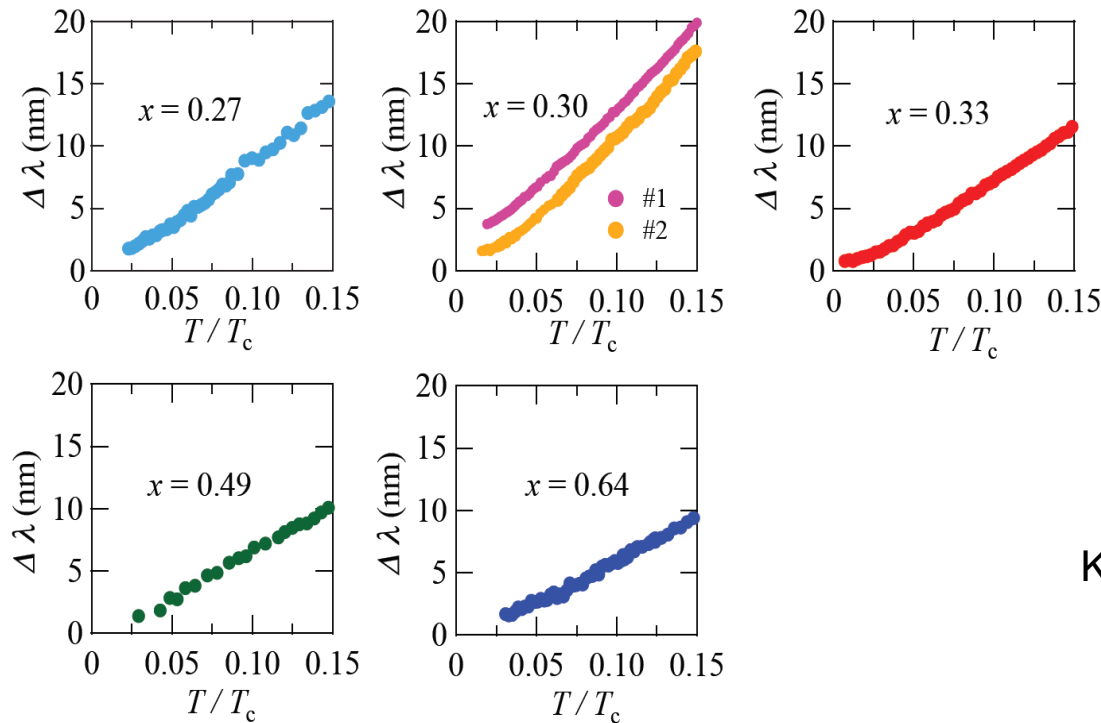


Luo *et al.*  
Kurita *et al.*

Doppler shift

K. Hashimoto *et al.*, PRB (2010)  
K. Hashimoto *et al.*, PRL (2009)  
K. Hashimoto *et al.*, Science (2012)  
A. Carrington *et al.* (2014)

# SC gap structure in isovalent doped systems



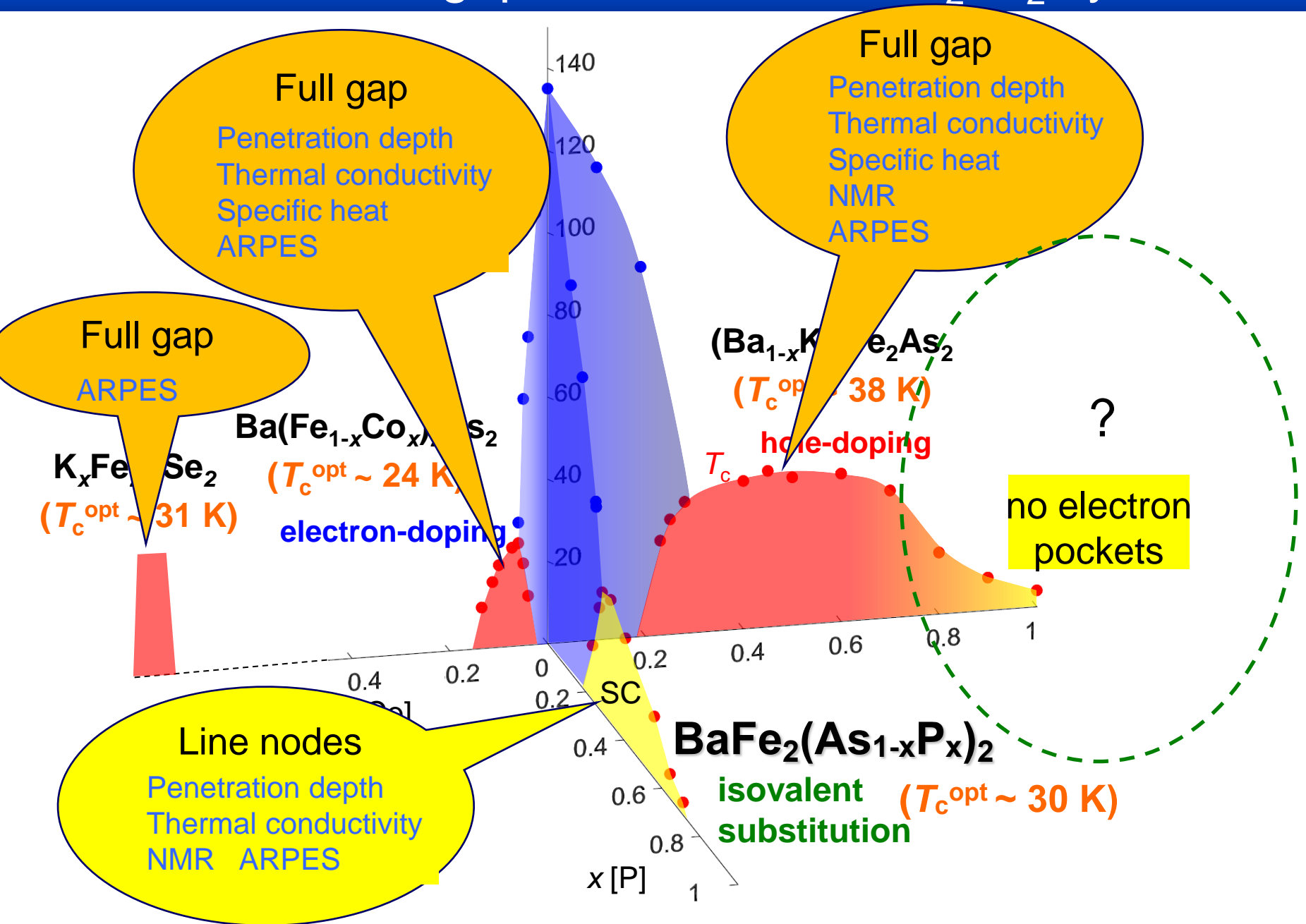
K. Hashimoto *et al.*, Science (2012)

- The presence of line nodes is a robust feature for all  $x$ .

Presence of repulsive interaction

non-phononic (magnetic) pairing interaction

# Non-universal gap structure in BaFe<sub>2</sub>As<sub>2</sub> systems



# Gap structure of hole doped $\text{Ba}_{1-x}\text{K}_x\text{Fe}_2\text{As}_2$

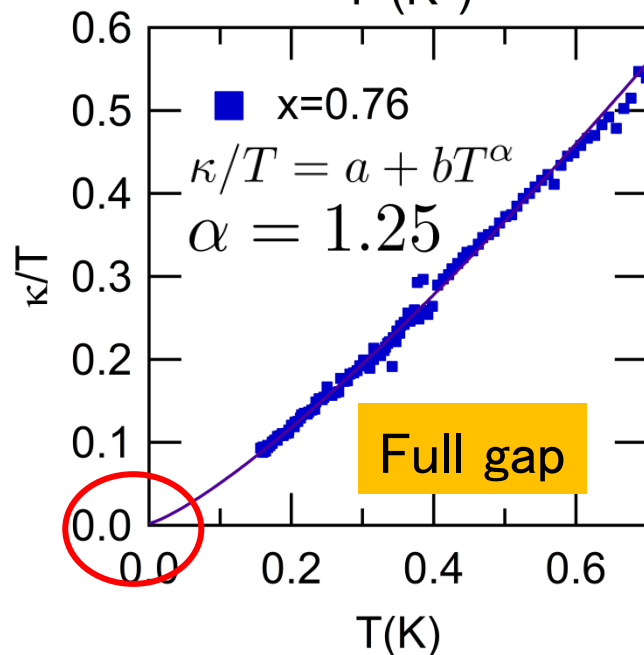
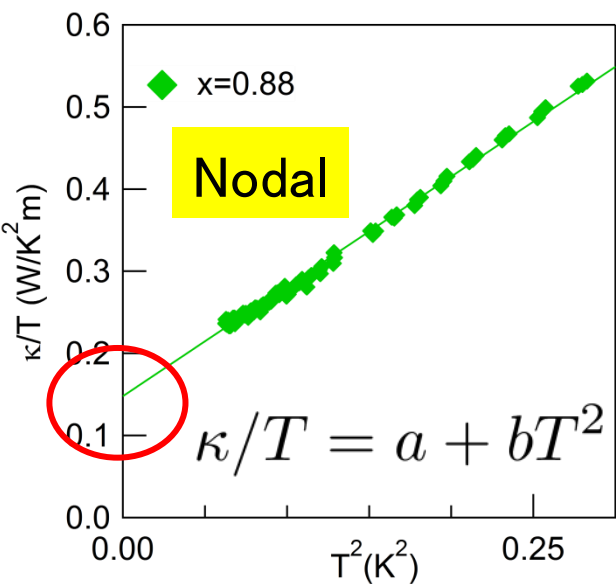
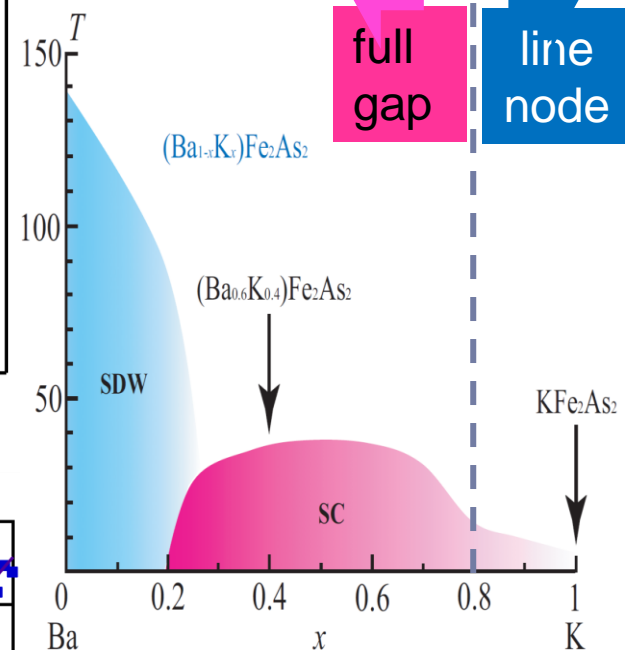
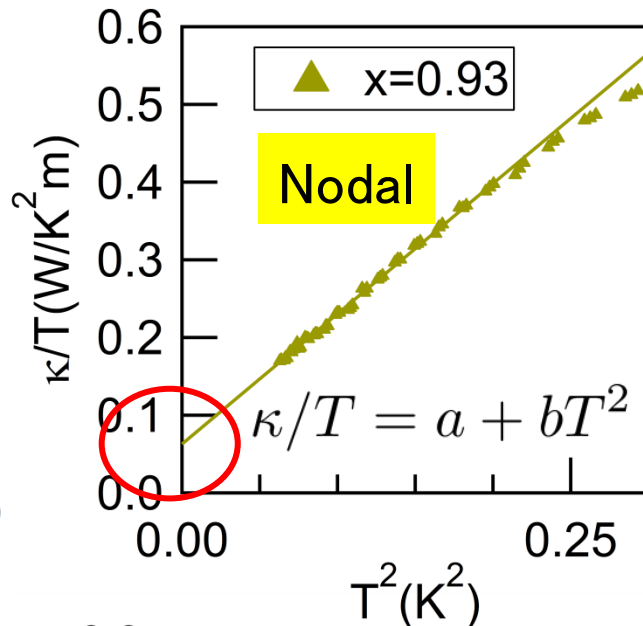
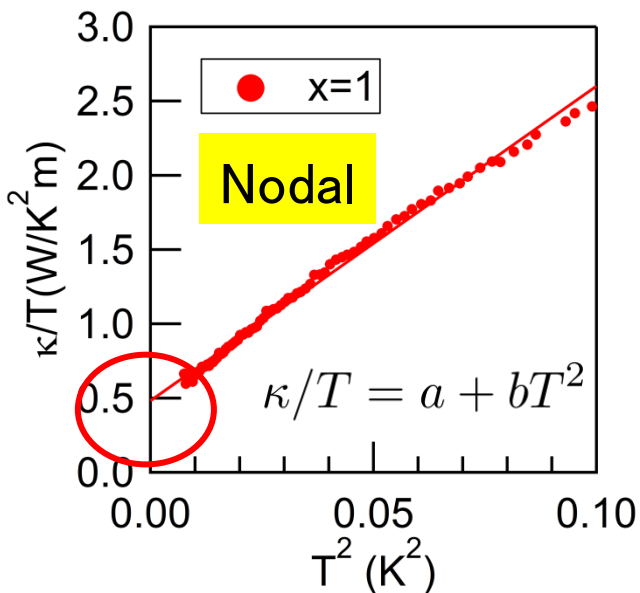
D. Watanabe *et al.* PRB (2014)

Boundary

$0.76 < x < 0.88$

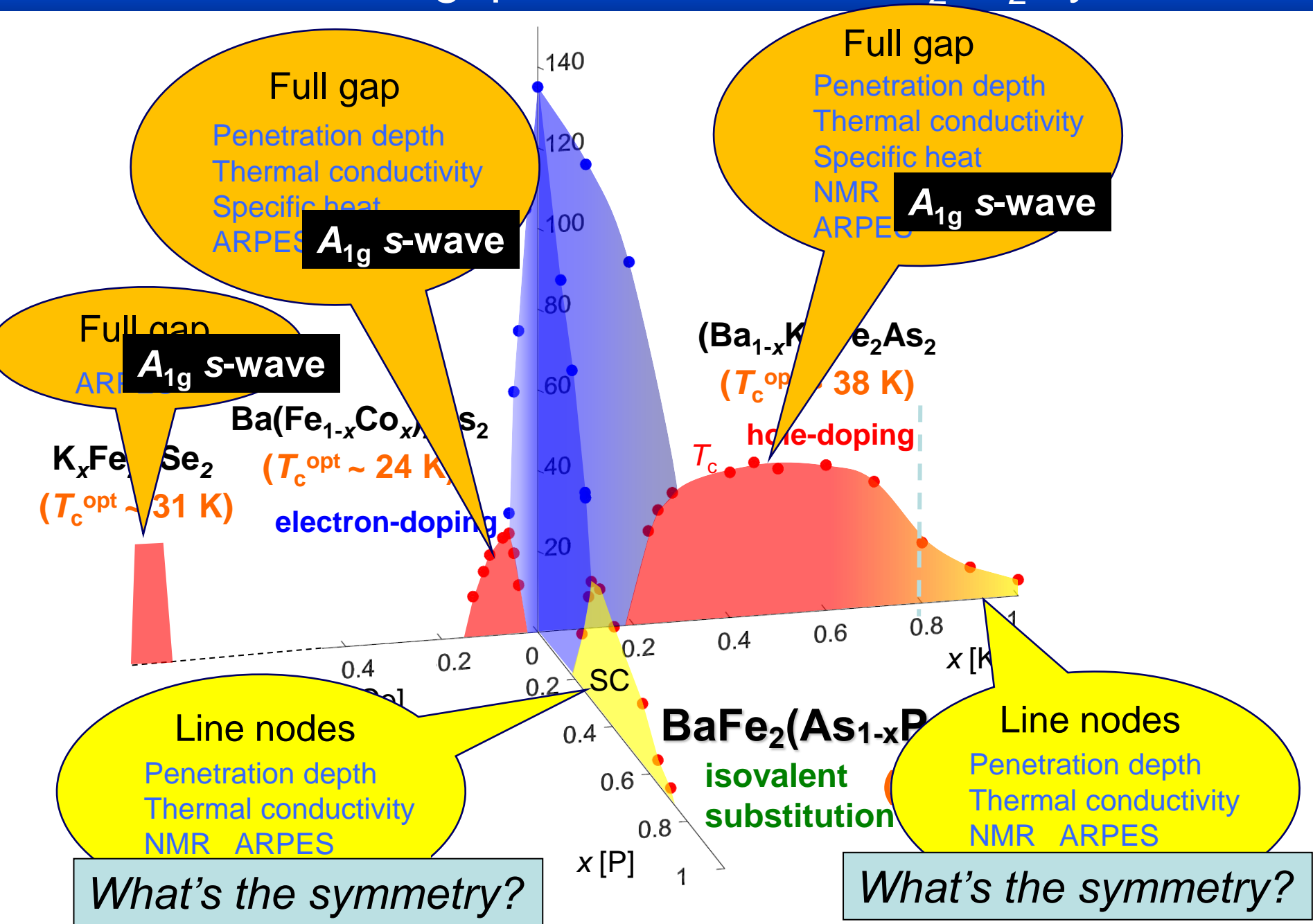
full gap

line node



The gap structure changes at  $x \sim 0.8$ .

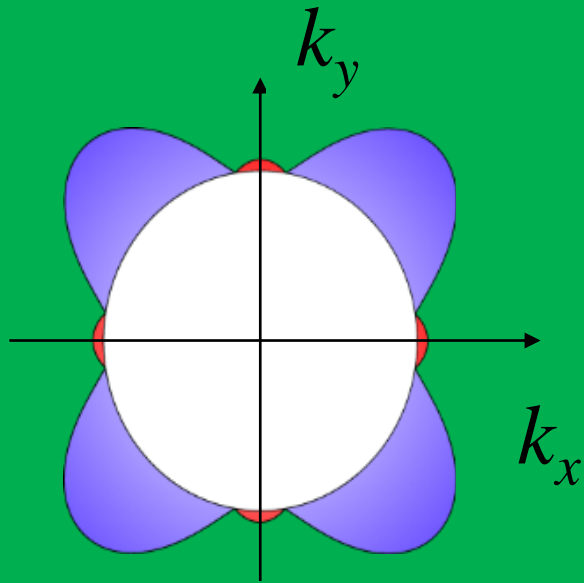
# Non-universal gap structure in $\text{BaFe}_2\text{As}_2$ systems





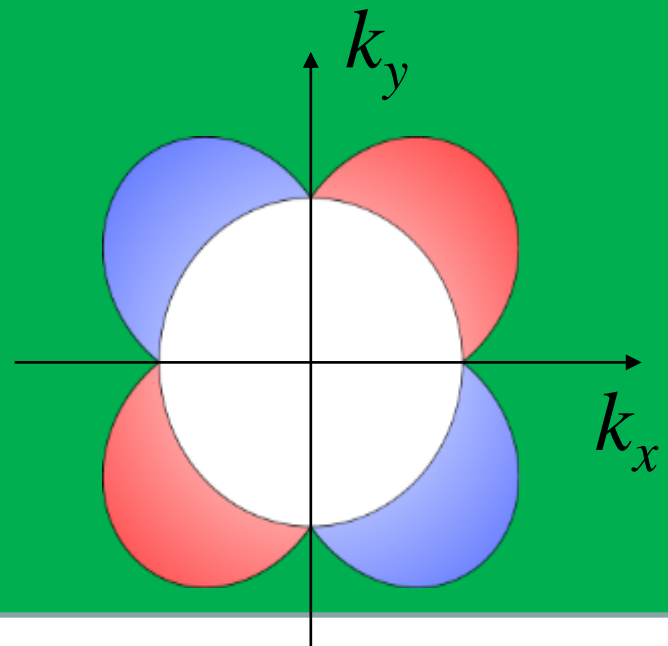
# Non-universal gap structure in $\text{BaFe}_2\text{As}_2$ systems

**s-wave ( $A_{1g}$ )**  
**Nodes: Accidental**



or

**d-wave ( $B_{1g}$  or  $B_{2g}$ )**  
**Nodes: Symmetry-protected**



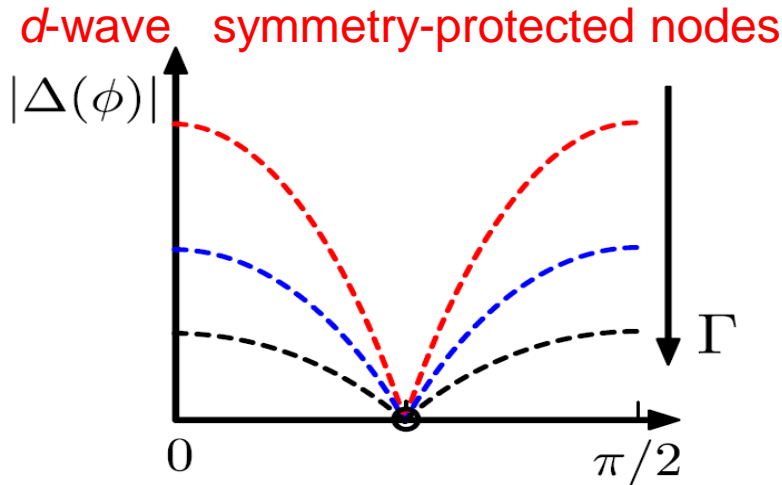
*What's the symmetry?*

*What's the symmetry?*

# Are the nodes accidental or symmetry protected?

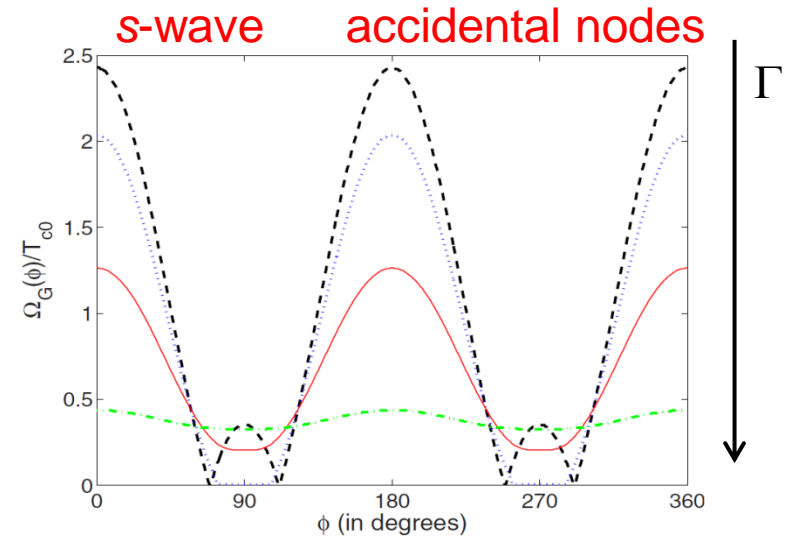
Impurity scattering dependence of gap structure can be a powerful probe of symmetry

$\Gamma$  : impurity scattering rate



J-Ph Reid *et al.*, Supercond. Sci. Technol. **25**,084013 (2012).

Nodes are robust against disorder



V. Mishra *et al.*, PRB **79**, 094521 (2009).

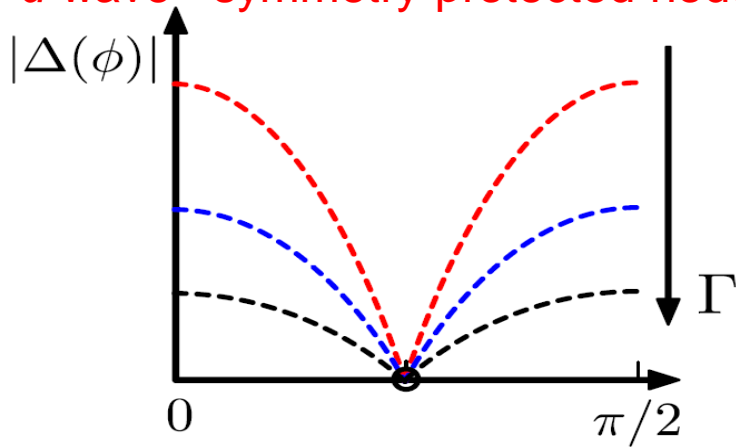
Nodes can be lifted by disorder

# Are the nodes accidental or symmetry protected?

Impurity scattering dependence of gap structure can be a powerful probe of symmetry

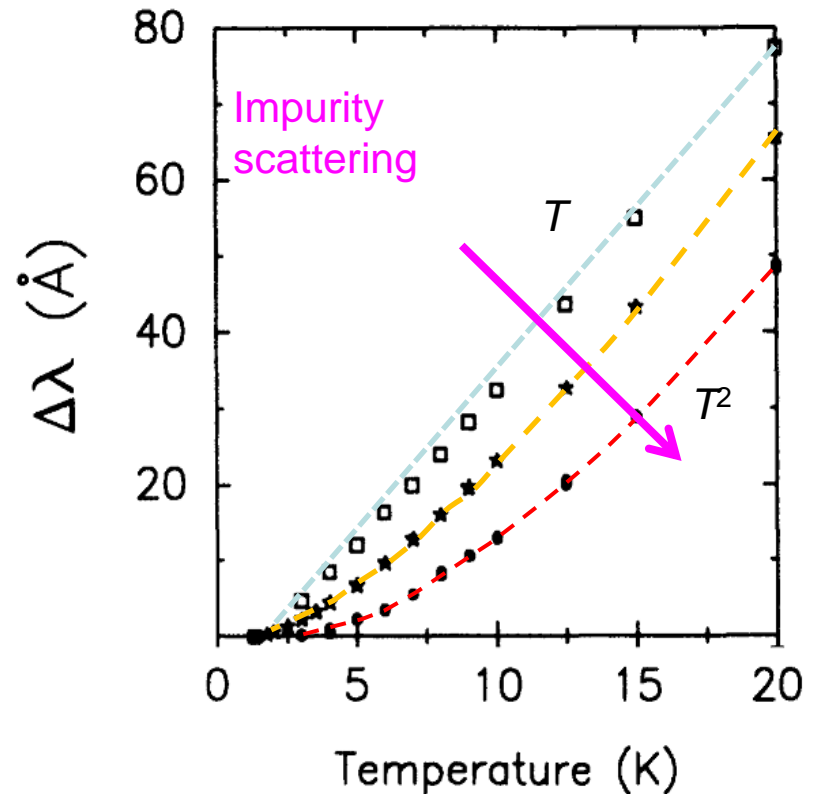
$\Gamma$  : impurity scattering rate

*d*-wave symmetry-protected nodes



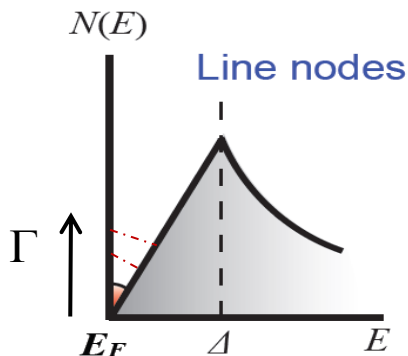
J-Ph Reid *et al.*, Supercond. Sci. Technol. **25**,084013 (2012).

Zn doped  $\text{YBa}_2\text{Cu}_3\text{O}_{6.95}$



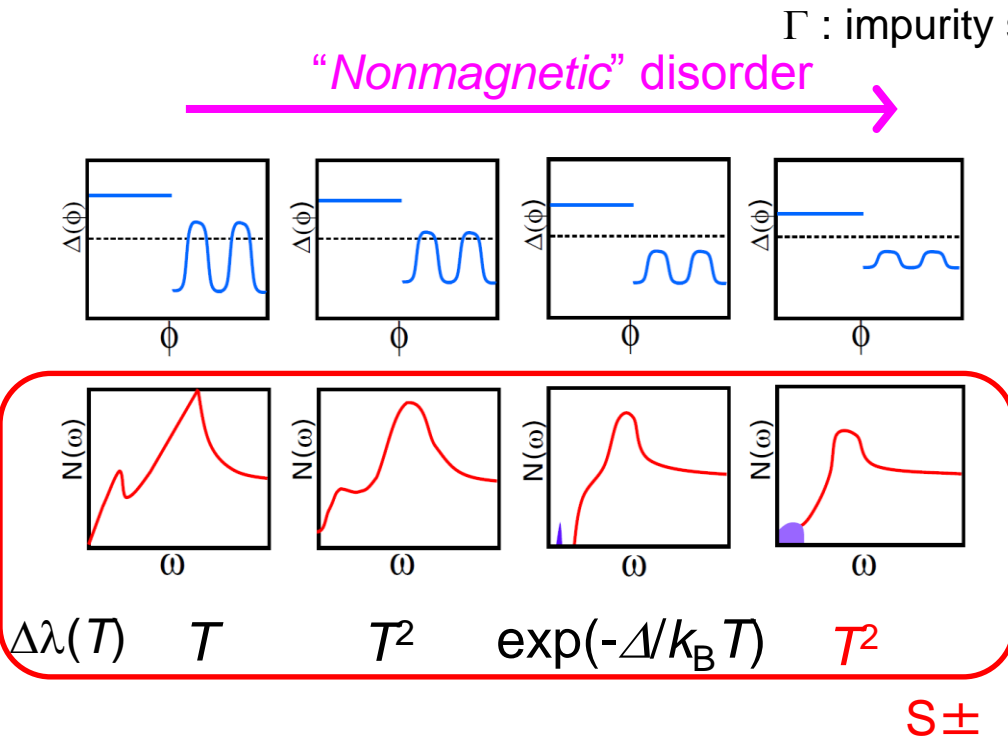
D. A. Bonn *et al.*, PRB **50**,4051 (1993).  
 P. J. Hirschfeld and N. Goldenfeld, PRB **48**, 4219 (1993).

Nodes are robust against disorder

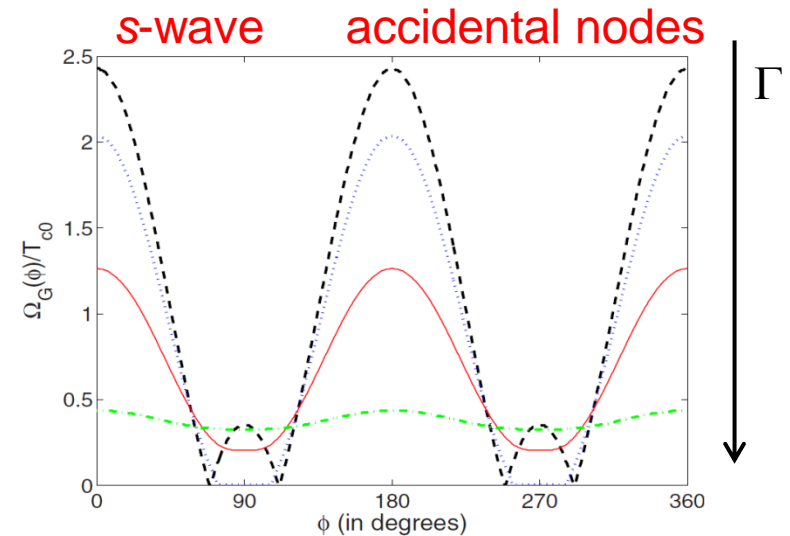


# Are the nodes accidental or symmetry protected?

Impurity scattering dependence of gap structure can be a powerful probe of symmetry



Y. Wang *et al.*, PRB **87**, 094504 (2013).

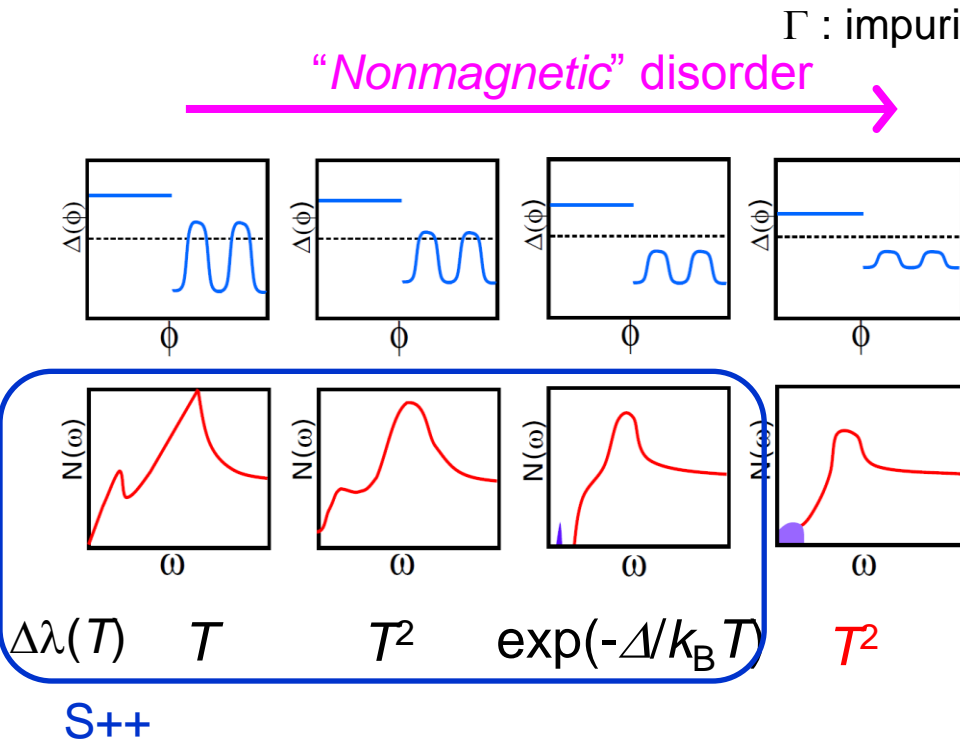


V. Mishra *et al.*, PRB **79**, 094521 (2009).

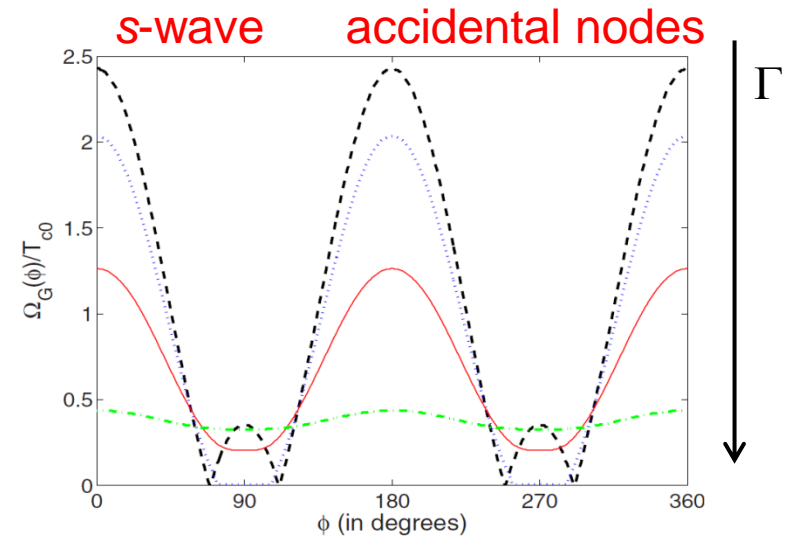
Nodes can be lifted by disorder

# Are the nodes accidental or symmetry protected?

Impurity scattering dependence of gap structure can be a powerful probe of symmetry



Y. Wang *et al.*, PRB **87**, 094504 (2013).

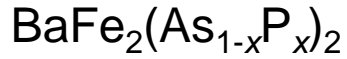


V. Mishra *et al.*, PRB **79**, 094521 (2009).

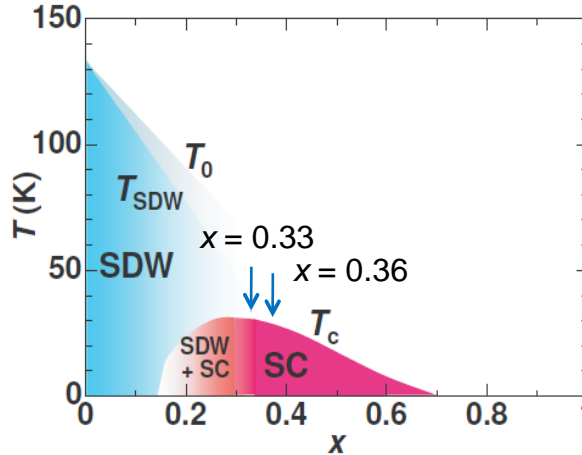
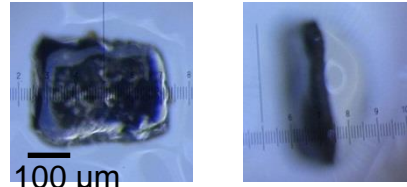
**Nodes can be lifted by disorder**

# Introducing controlled point defects by electron irradiation

## Single crystals



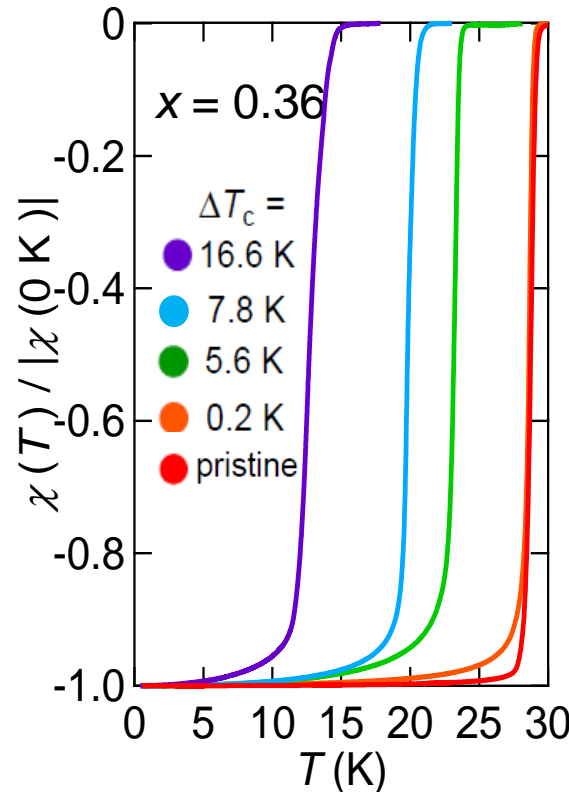
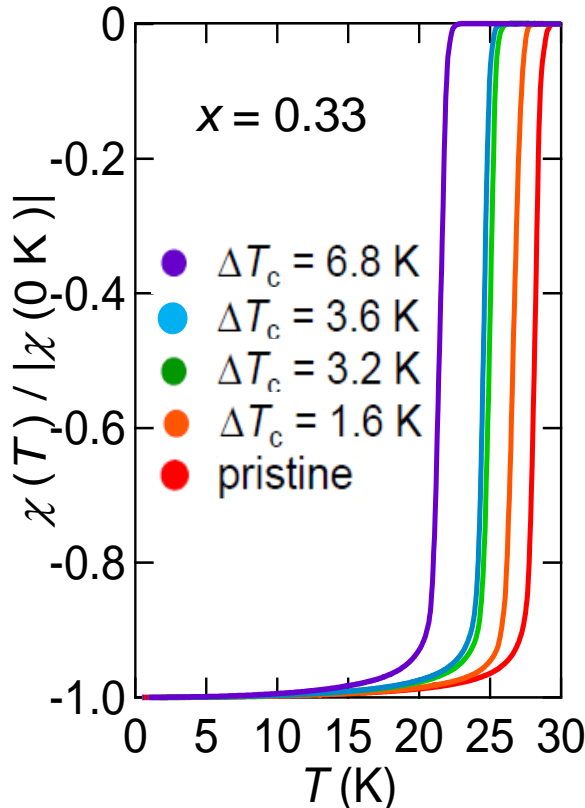
$x = 0.33, 0.36$



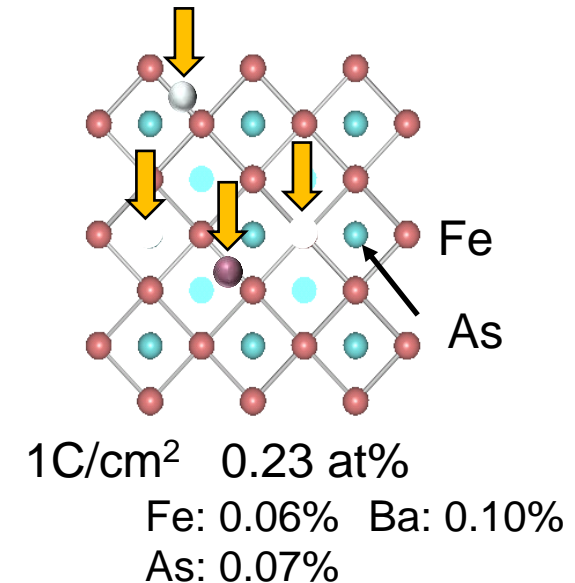
## Electron irradiation

$T = 20 \text{ K}$     $2.5 \text{ MeV}$

- ✓ No change of lattice constants
- ✓ No significant change of carrier density
- ✓ Controlled disorder on the same sample



## Point defects

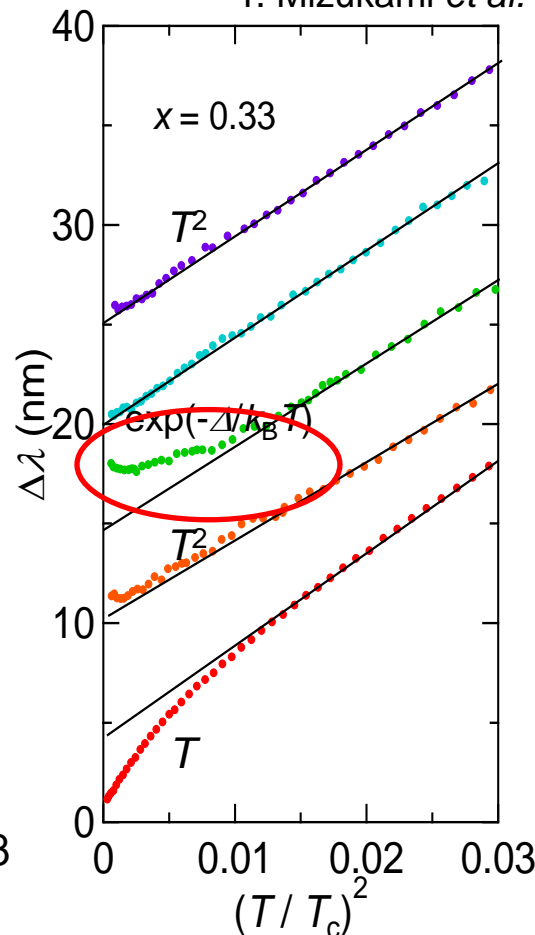
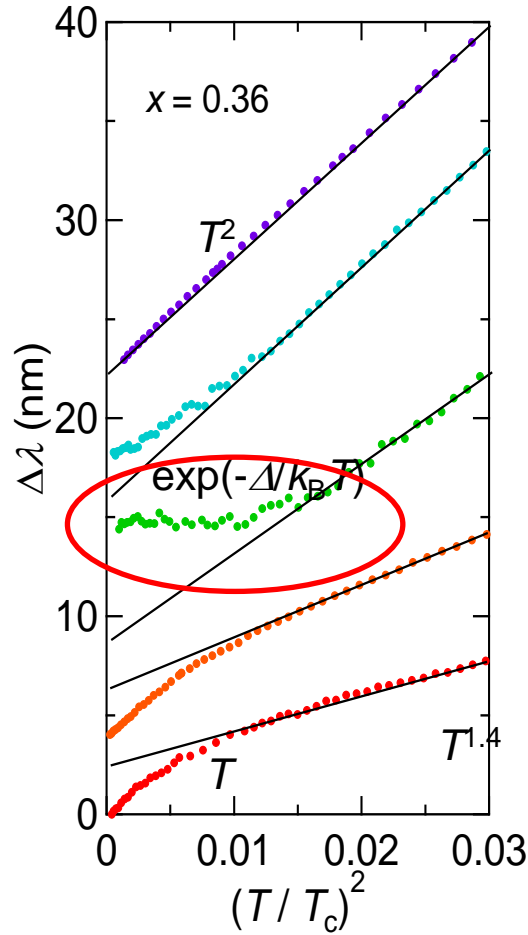


Sharp SC transitions

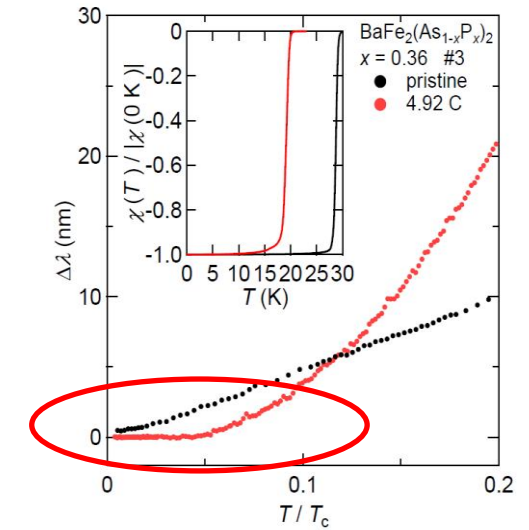
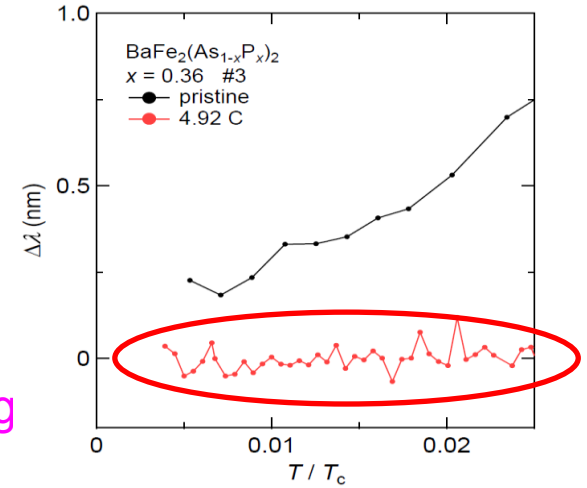
Homogeneous point defects

# Observation of node lifting by electron irradiation

Y. Mizukami *et al.*



Impurity scattering

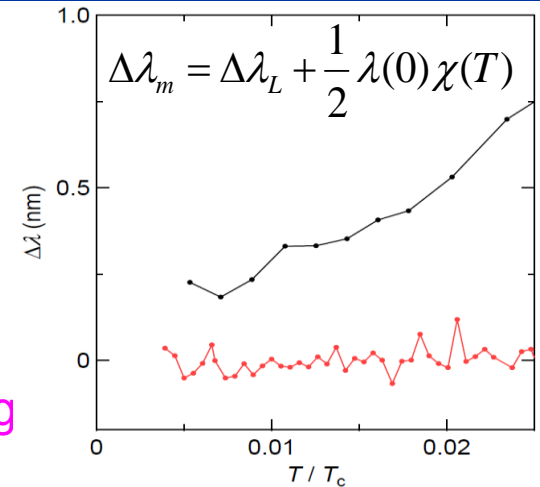
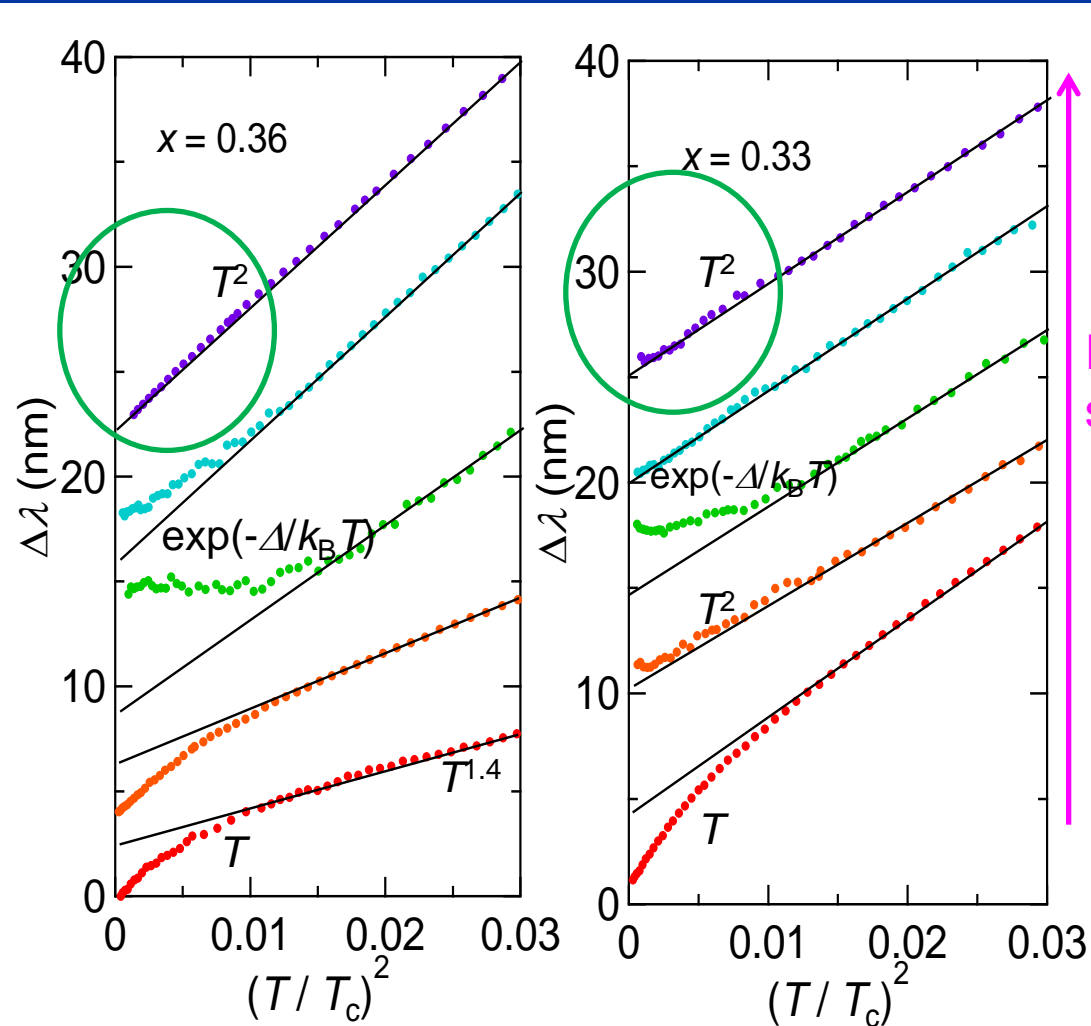


$\Delta\lambda$  changes with irradiation as  $T \rightarrow \exp(-\Delta/k_B T)$

Disorder-induced transformation from (line) nodal to nodeless state: Node is not symmetry protected  
**Bulk evidence for s-wave ( $A_{1g}$ ) symmetry**

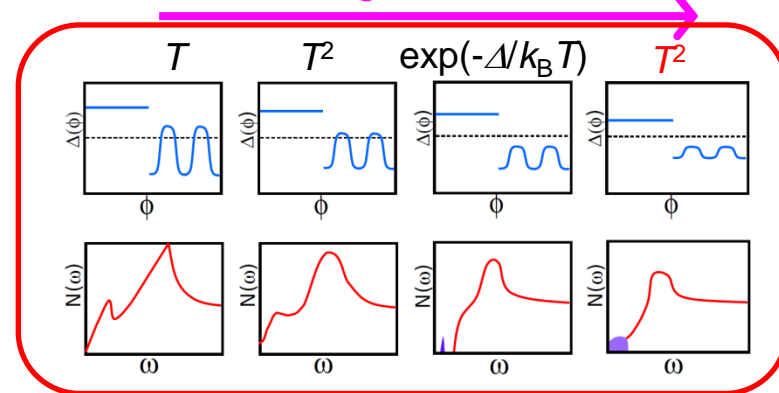


# Observation of node lifting by disorder



no evidence of Curie upturn  
down to  $\sim 80$  mK  
magnetic moment of point disorder  
is smaller than  $\sim 0.2-0.4\mu_B$

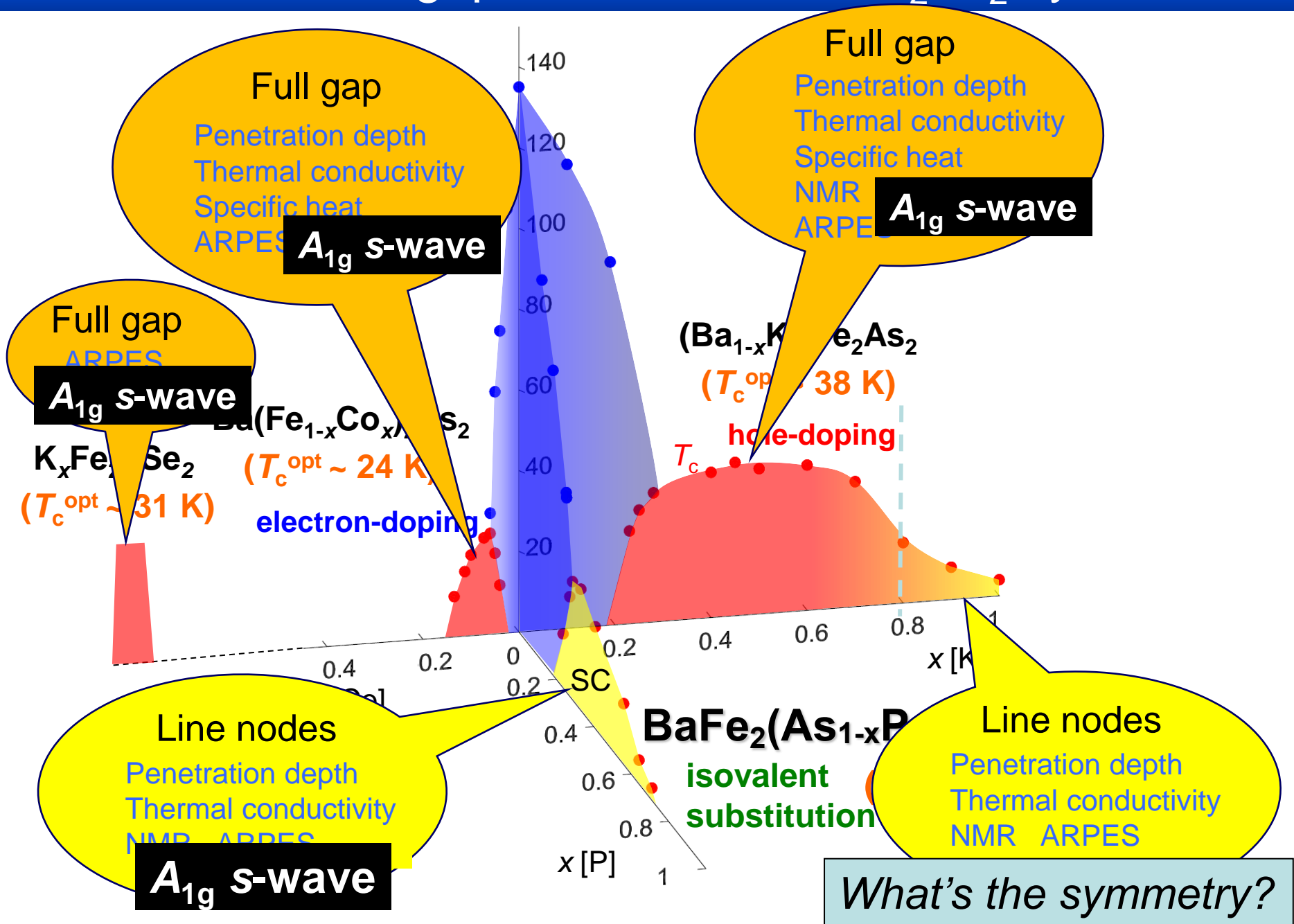
“Nonmagnetic” disorder



$\Delta\lambda$  changes with irradiation as  
 $T \rightarrow T^2 \rightarrow \exp(-\Delta/k_B T) \rightarrow T^2$

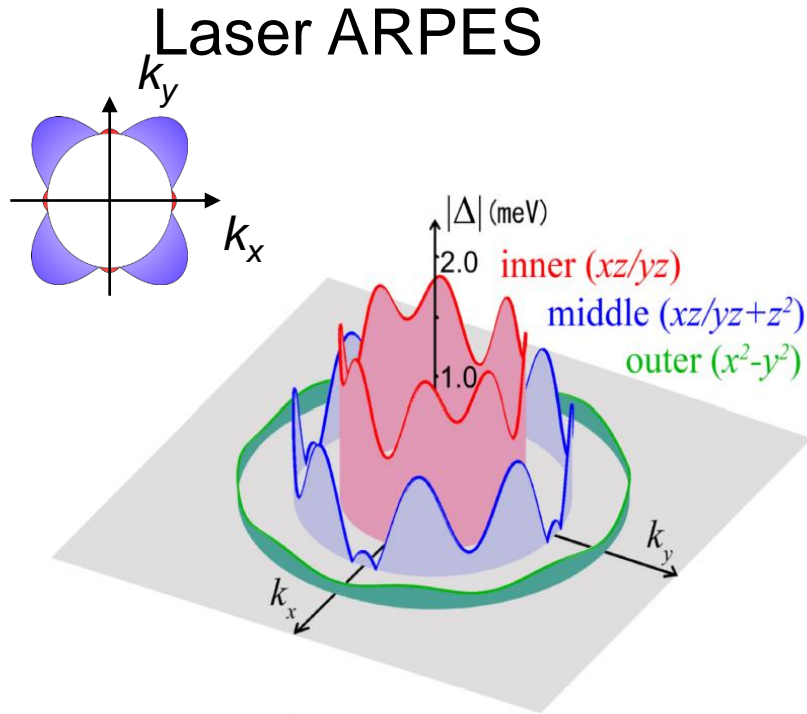
Y. Mizukami *et al.*

# Non-universal gap structure in BaFe<sub>2</sub>As<sub>2</sub> systems



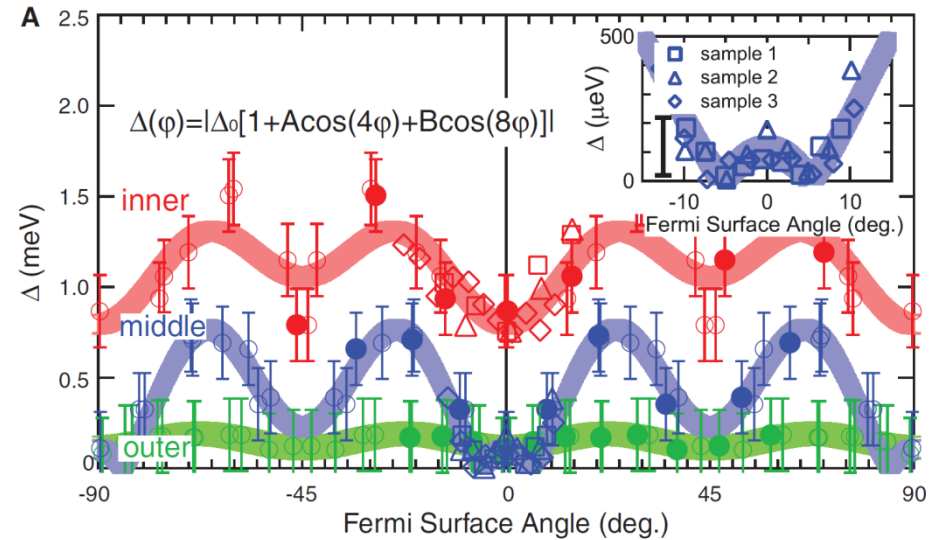
# Gap symmetry in $\text{KFe}_2\text{As}_2$

## Nodal s-wave



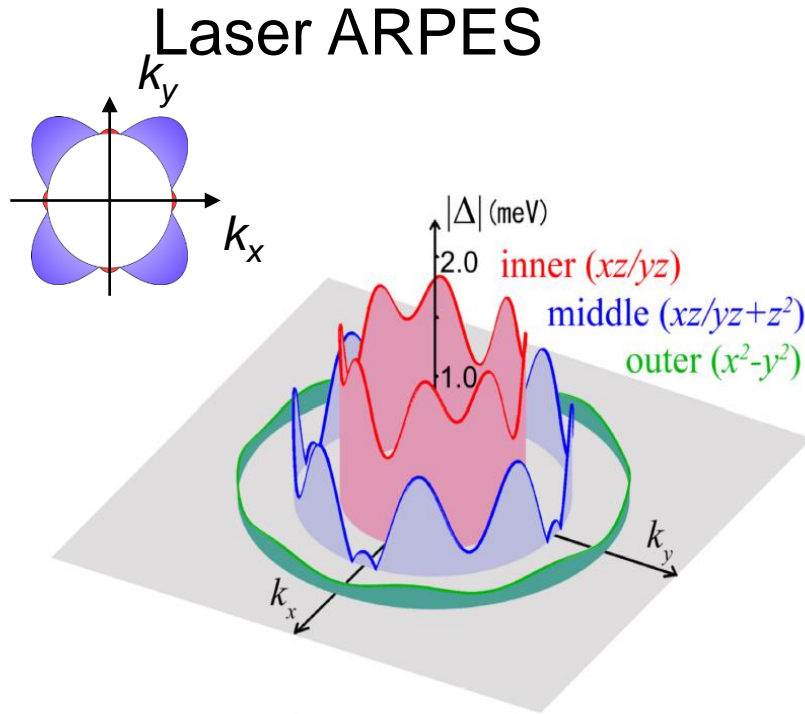
K. Okazaki *et al.*, Science (2012).

## Octet-Line Node



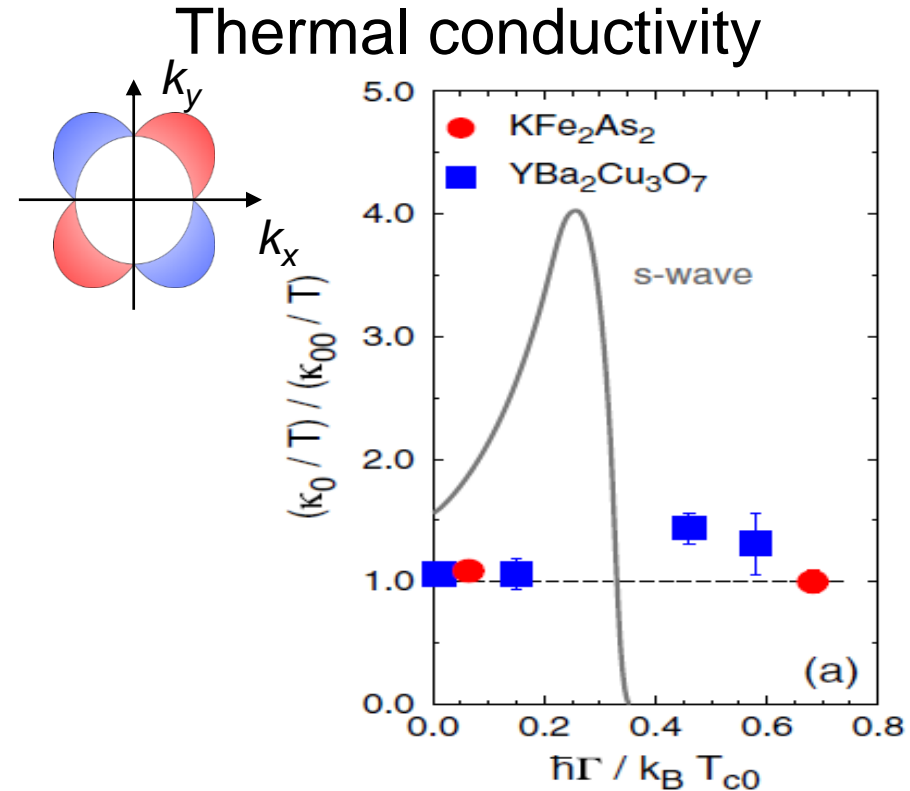
# Gap symmetry in $\text{KFe}_2\text{As}_2$

## Nodal s-wave



K. Okazaki *et al.*, Science (2012).

## d-wave

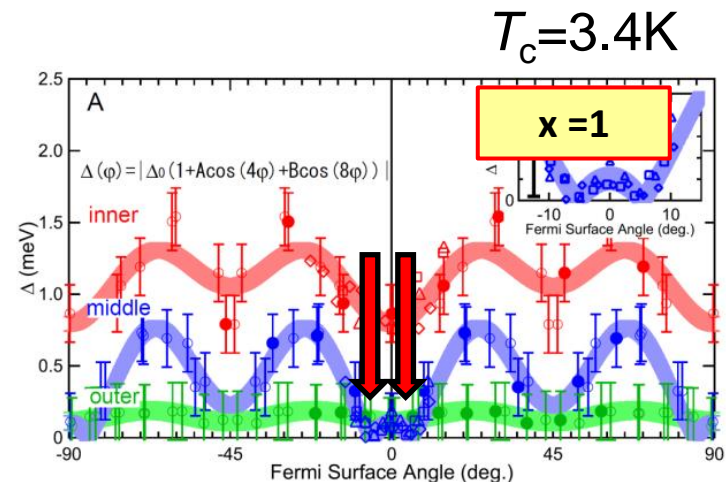
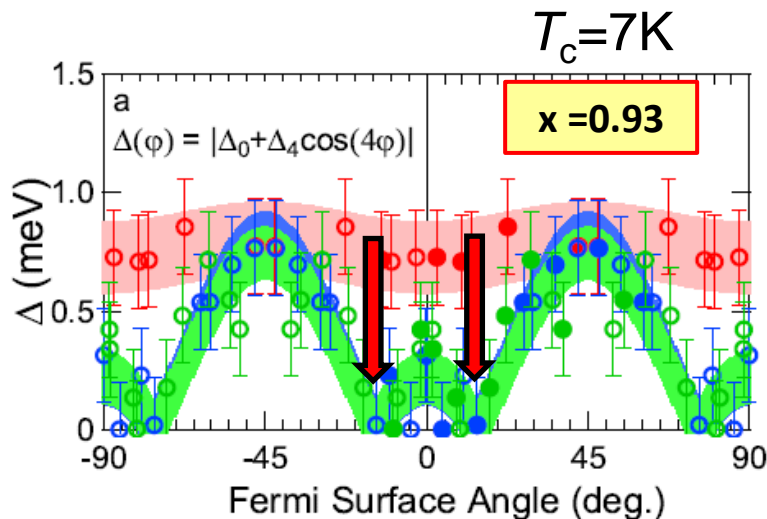
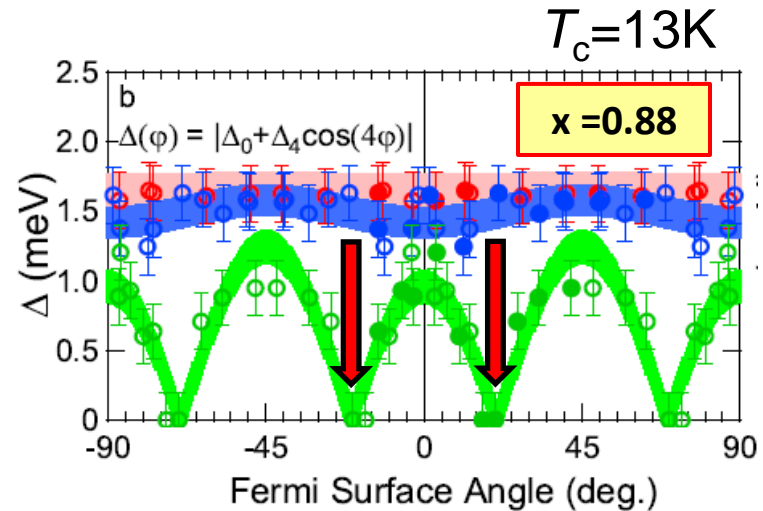
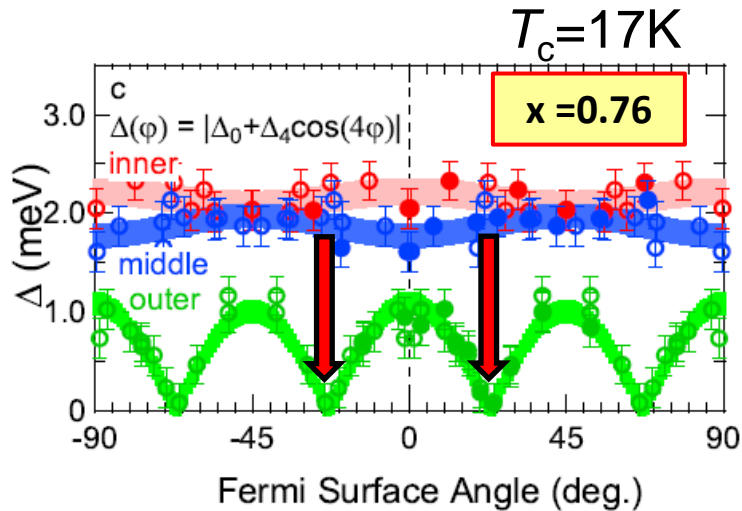


J.P.Reid *et al.* PRL (2012)

## Specific heat

F. Hardy *et al.* JPSJ (2013)

# Doping evolution of SC gap structure in $(\text{Ba}_{1-x}\text{K}_x)\text{Fe}_2\text{As}_2$



No discontinuous change of the gap function with doping.

K. Okazaki *et al.*, Science 337, 1314 (2012)

Y. Ota *et al.*, (submitted) arXiv:1307.7922

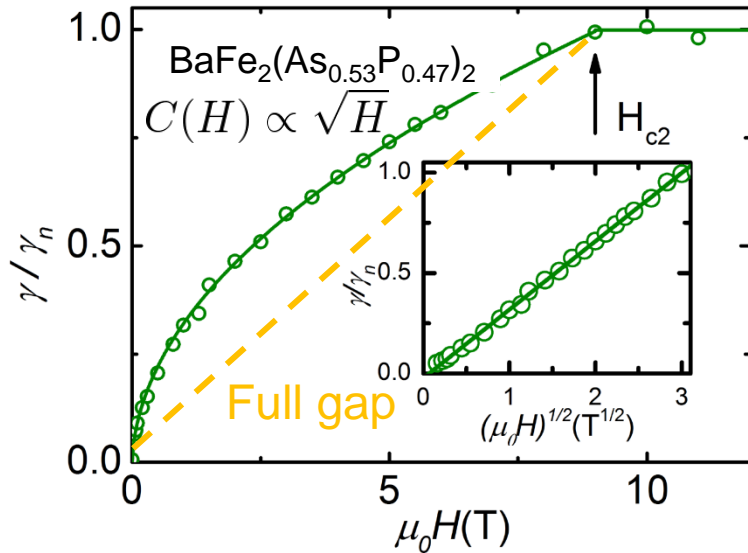






# Nodal structure of $\text{BaFe}_2(\text{As}_{1-x}\text{P}_x)_2$

## Specific heat

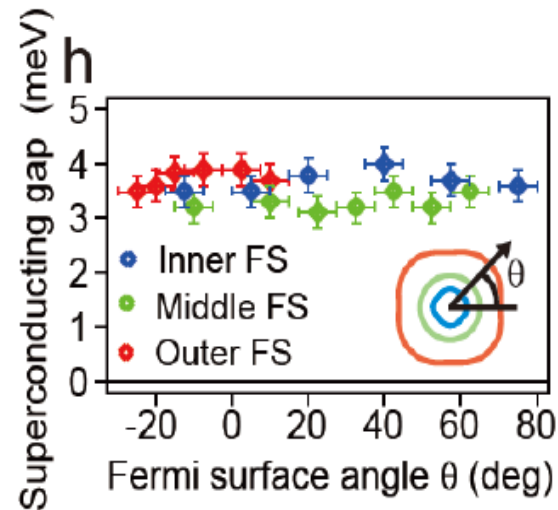
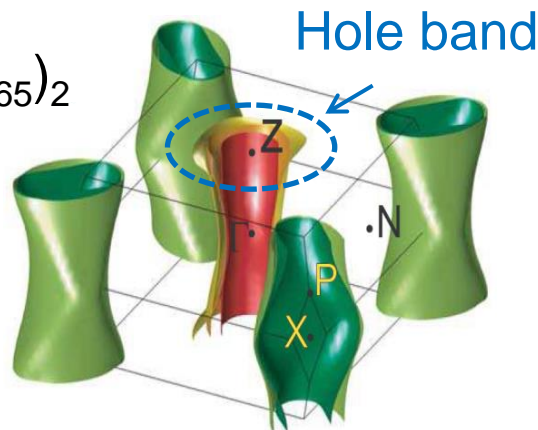


$$C(H) \propto \sqrt{H} \quad \text{up to } H_{c2}$$

Line nodes in all FSs

## Laser ARPES

$\text{BaFe}_2(\text{As}_{0.35}\text{P}_{0.65})_2$   
 $(T_c = 30 \text{ K})$



Hole



Horizontal

Full gap in all three hole bands around Z-point

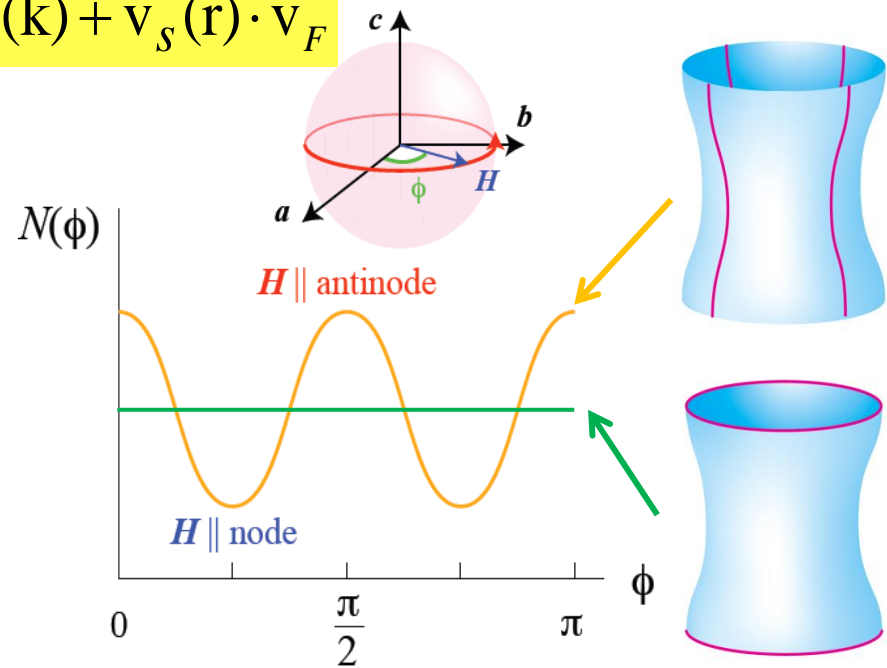
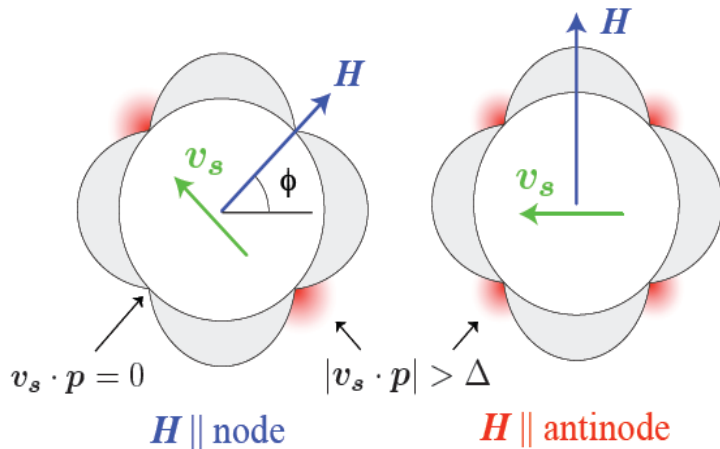
# Where is the line node ?

## Pinpointing line node by angle-resolved thermal conductivity

Doppler shift

$$E'(\mathbf{k}, \mathbf{r}) = E(\mathbf{k}) + \mathbf{v}_S(\mathbf{r}) \cdot \mathbf{v}_F$$

Angular dependent density of states



Fourfold oscillation, minima for  $H \parallel \text{node}$

Quasiparticles are not generated at nodal locations where  $\mathbf{v}_F \parallel \mathbf{H}$  ( $\mathbf{v}_S \cdot \mathbf{v}_F = 0$ )

theory

- I.Vekhter *et al.* 1999-2002
- K.Maki *et al.* 2000-2004
- P.Thalmeier *et al.* PRB (01)
- H.Kusunose JPSJ (04)
- T. Nakai *et al.* PRB (04)
- L.Tewordt and Fay PRB (05)
- A.B. Vorontsov and I.Vekhter, PRL (06), PRB (07)
- Y. Nagai and N. Hayashi, PRL (08)
- G.R. Boyd *et al.* PRB (09)

review

- Y. Matsuda *et al.* J. Phys. C 18, R705 (06)

### Pnictide

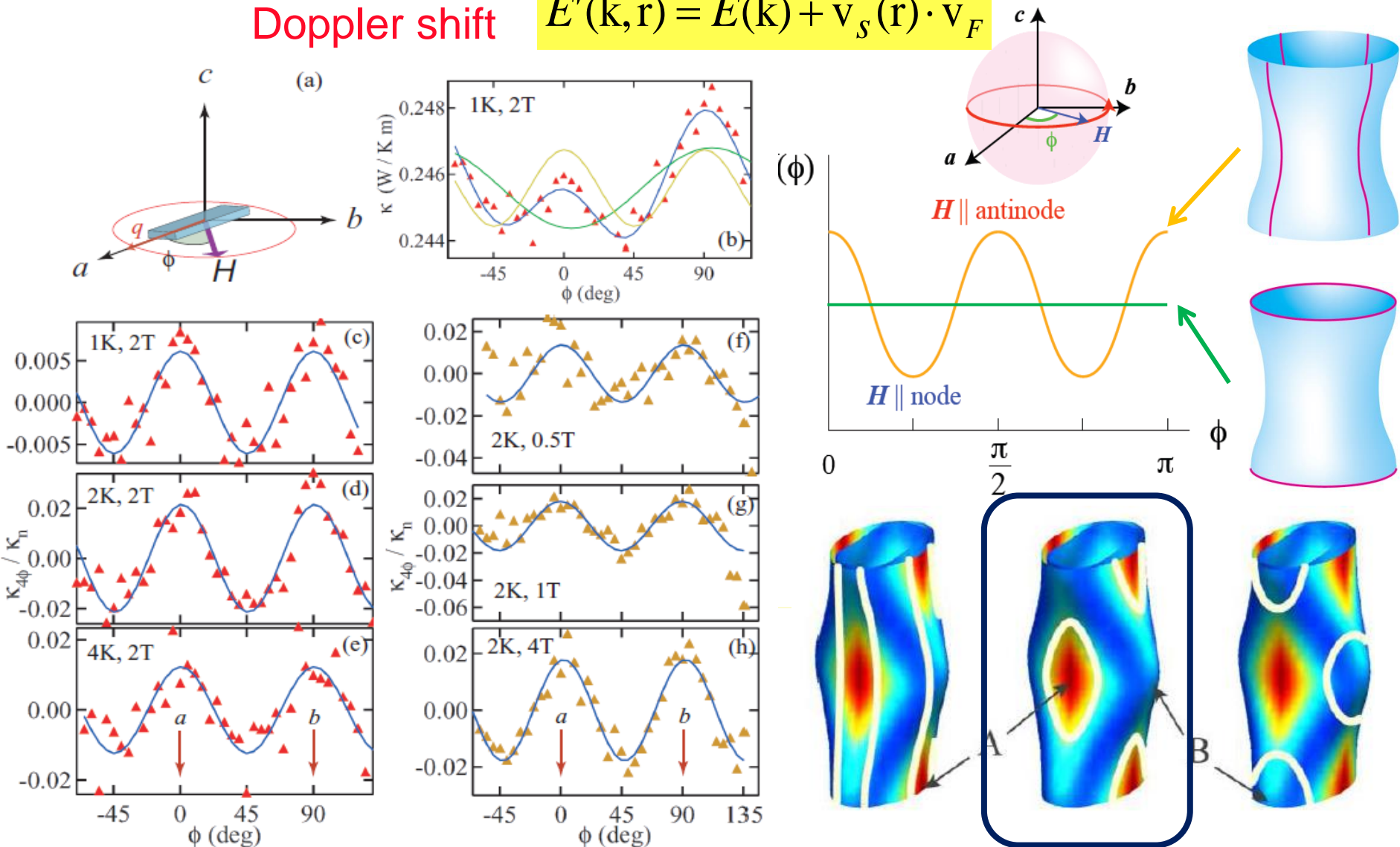
- A.B. Vorontsov and I.Vekhter, PRL (10)
- S. Graser *et al.* PRB (08)
- A.V. Chubukov and I. Eremin, PRB (10)

# Where is the line node ?

## Pinpointing line node by angle-resolved thermal conductivity

Doppler shift

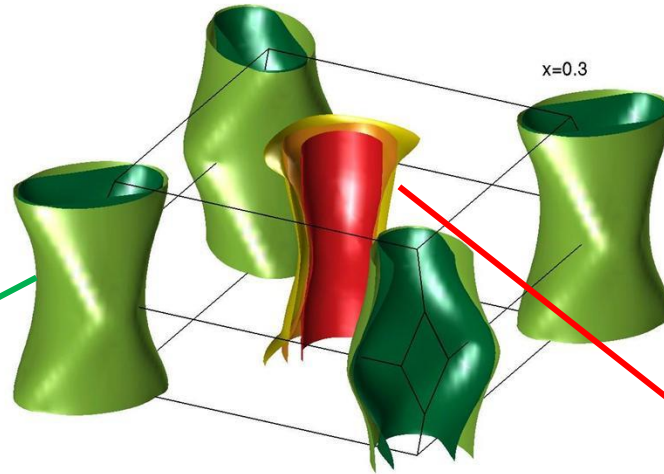
$$E'(\mathbf{k}, \mathbf{r}) = E(\mathbf{k}) + \mathbf{v}_S(\mathbf{r}) \cdot \mathbf{v}_F$$



# Nodal structure of $\text{BaFe}_2(\text{As}_{1-x}\text{P}_x)_2$

$\text{BaFe}_2(\text{As}_{0.3}\text{P}_{0.70})_2$   
( $T_c=31$  K)

Electron



Hole



Nodal loop



Horizontal lines

# What is the implication of line node?

Line node → Presence of repulsive pairing interaction

Accidental line node (not symmetry protected)

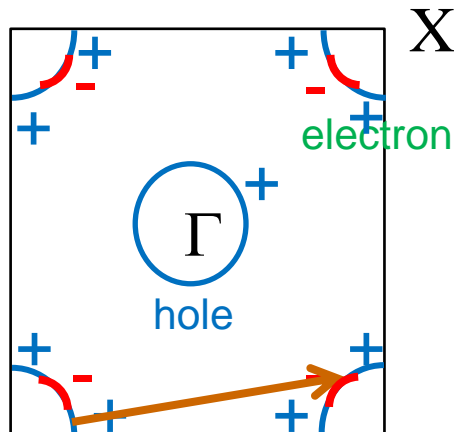
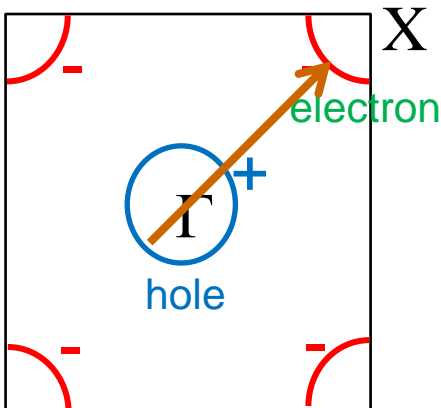
→ Presence of two (or more) competing pairing interactions

Possible scenarios

## 1) Frustration

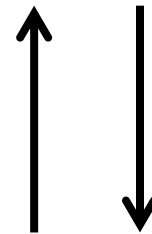
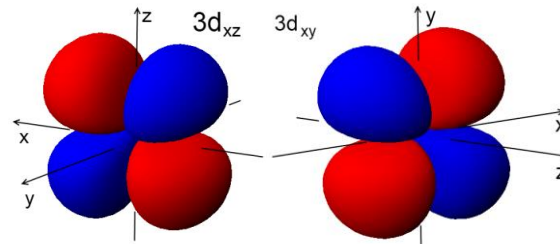
$el-h$ : repulsive  $S_{+-}$

$el-el$ : repulsive



## 2) Competition

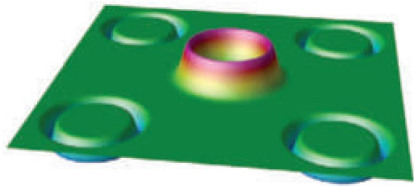
Orbital : attractive  $S_{++}$  Spin : repulsive  $S_{+-}$



# Summary: Superconducting gap structure

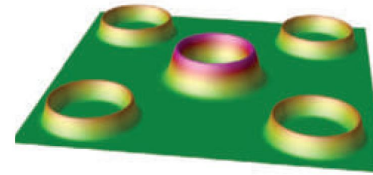
Full gap superconductivity

$S_{+-}$



Repulsive  
Spin fluctuations

$S_{++}$



Attractive  
Orbital fluctuations

No conclusive experimental evidence so far

Some pnictides have line nodes

Presence of repulsive pairing interaction

Line node is accidental (not symmetry protected)

Presence of two (or more) competing pairing interactions

# Physics of iron-based high temperature superconductors (III)

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Yuji Matsuda



*Department of Physics  
Kyoto University  
Kyoto, Japan*

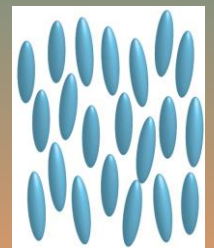
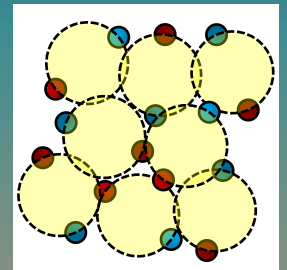




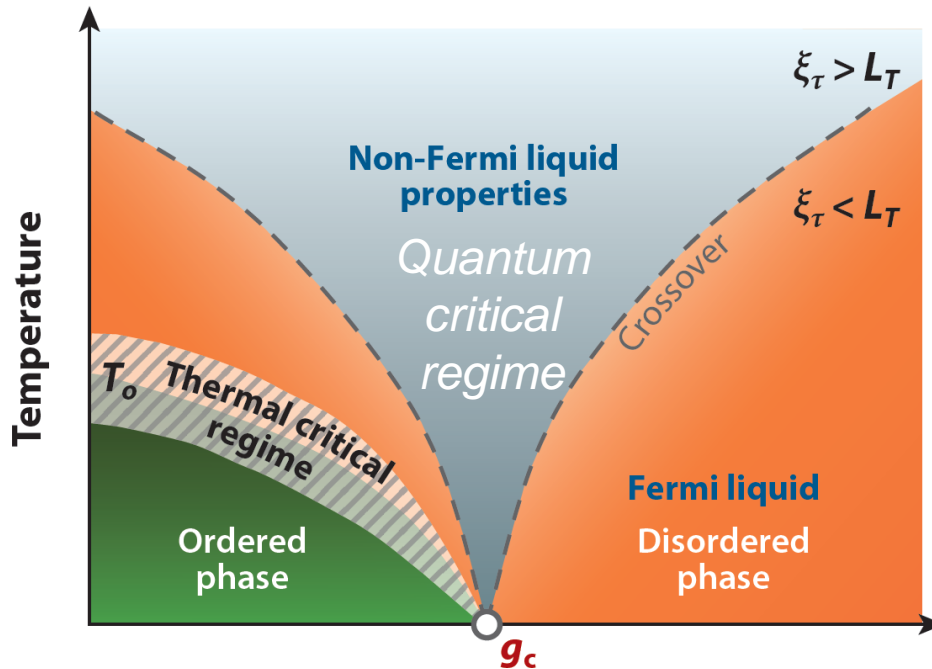
# Physics of iron-based high- $T_c$ superconductors

## Selected recent topics

1. Quantum critical point
2. BCS-BEC crossover and a novel high field SC phase
3. Nematicity



# Quantum Critical Point (QCP)



**Control parameter  $g$**   
**(Quantum critical point)**

$g$ : pressure, chemical substitution, magnetic field

S. Sachdev, Quantum Phase Transitions

Quantum time scale

$$\xi \propto |g - g_c|^\nu \quad \xi_\tau \propto \xi^z$$

Thermal time scale

$$L_T = \frac{\hbar}{k_B T}$$

$$\xi_\tau < L_T$$

QP excitations are well defined

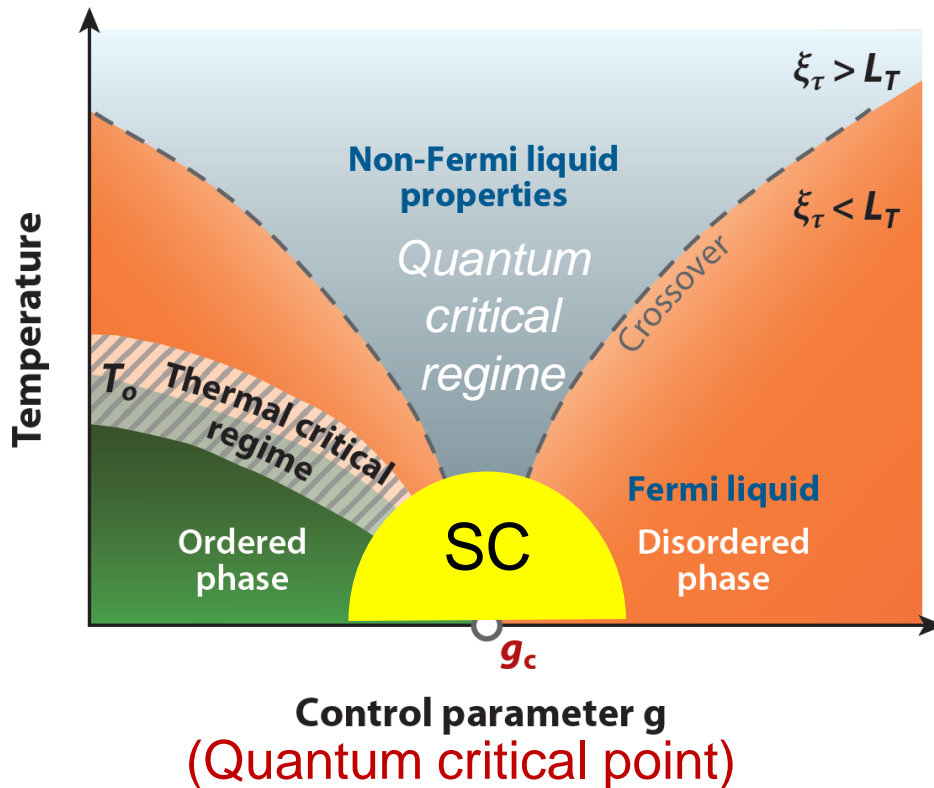
$$\xi_\tau > L_T$$

Physical properties are seriously influenced by QCP at  $g=g_c$ .

Ordinary phase transition – driven by thermal fluctuations

Quantum phase transition – driven by zero temperature quantum fluctuations associated with Heisenberg's Uncertainty Principle

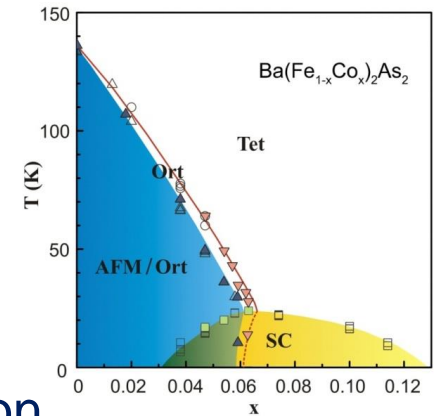
# Quantum Critical Point (QCP)



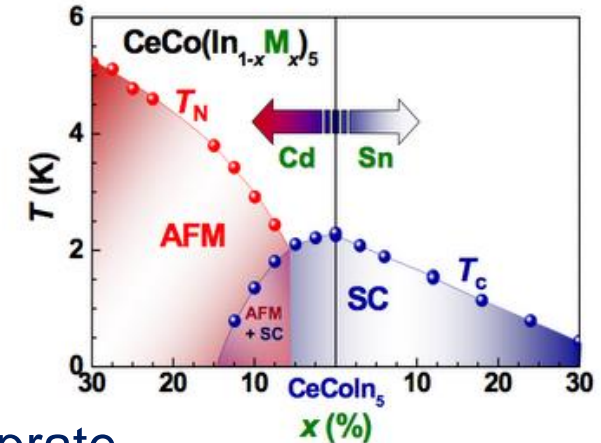
$g$ : pressure, chemical substitution, magnetic field

S. Sachdev, Quantum Phase Transitions

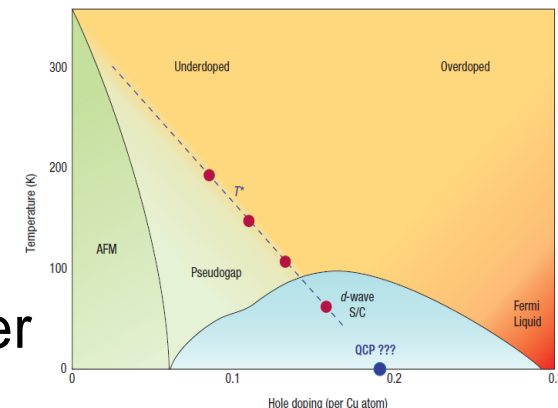
## Fe-pnictide



## Heavy Fermion



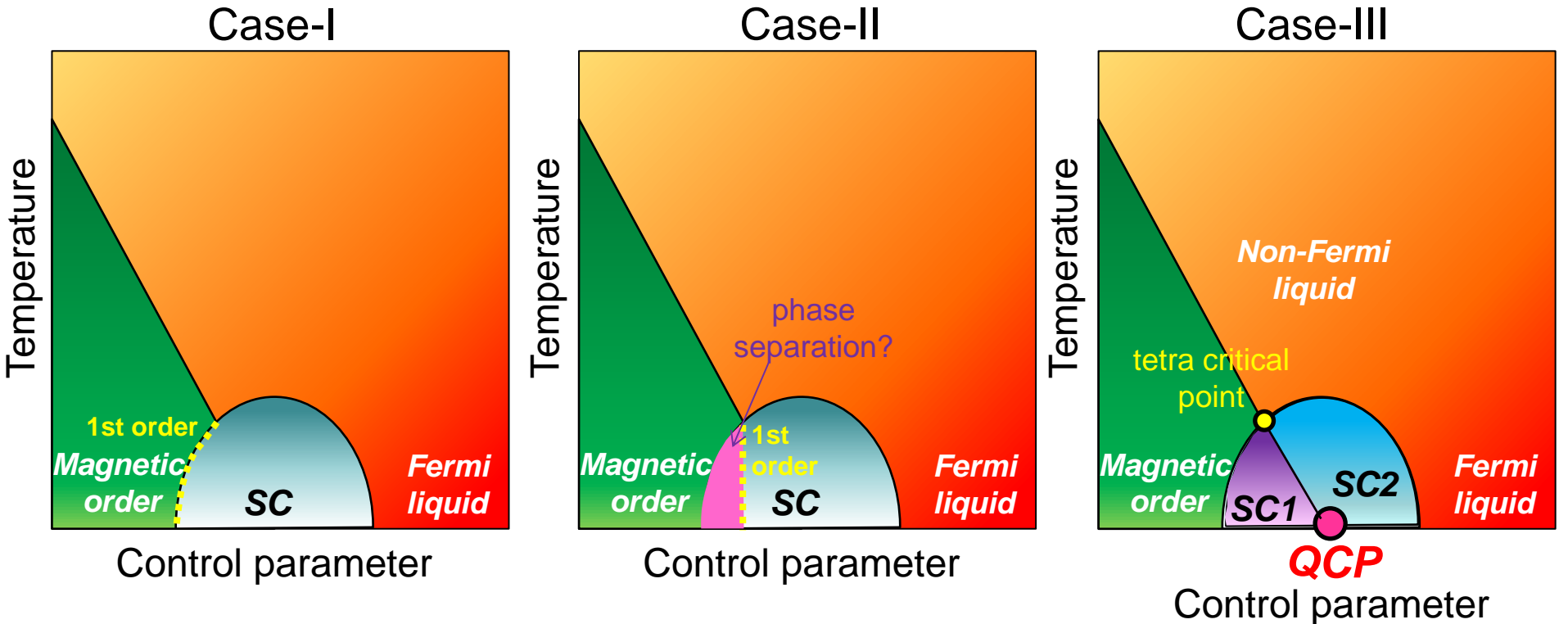
## Cuprate



Does the QCP lie beneath the SC dome?

1. Mechanism of superconductivity
2. non-Fermi liquid properties
3. Coexistence of SC and magnetic (exotic) order

# What lies beneath the SC dome?



*Criticality avoided by the transition to the SC state*

Origin of non-Fermi liquid properties, if observed, is not clear.

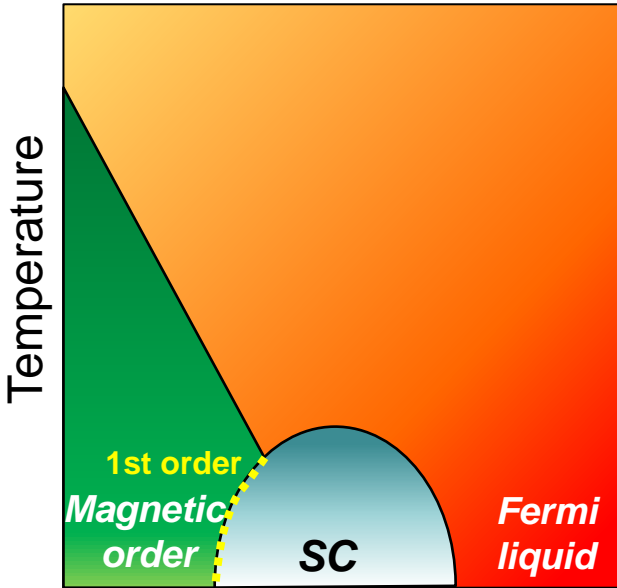
*QCP lying beneath the SC dome*

1. Non-Fermi liquid properties
2. Mechanism of unconventional SC
3. Microscopic coexistence of SC and magnetic (exotic) order

# What lies beneath the SC dome?

*QCP hidden in the SC dome has been highly controversial*

Case-I

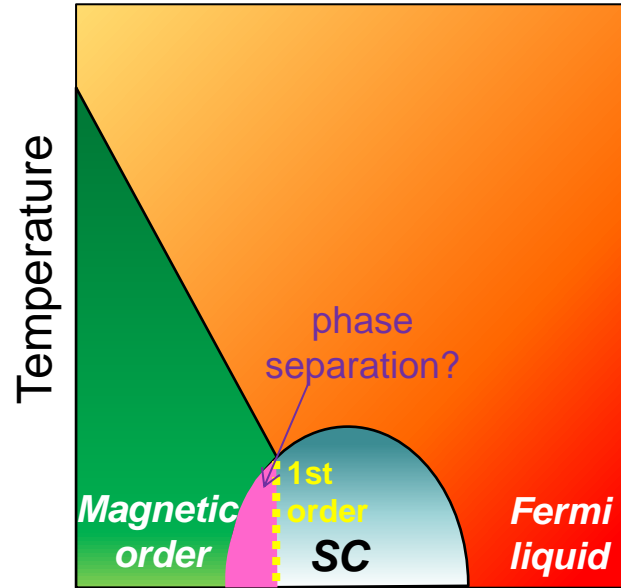


Control parameter

$\text{CeIn}_3, \text{CePd}_2\text{Si}_2$

NMR

Case-II



Control parameter

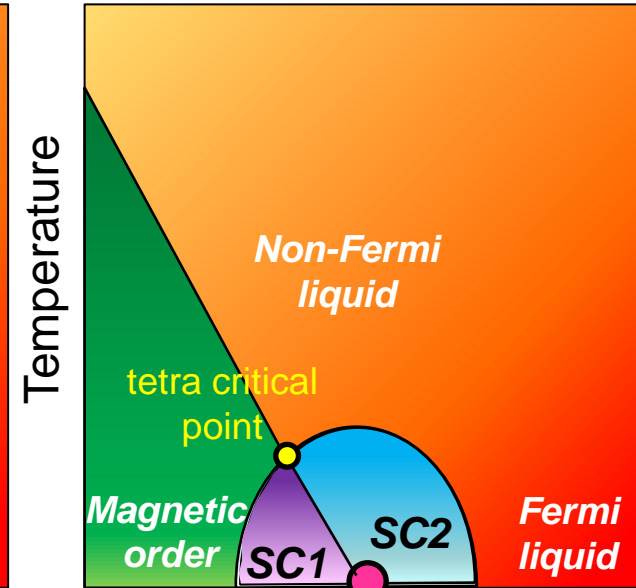
$\text{CeRhIn}_5$

Specific heat

T. Park *et al.* Nature (06)

G. Knebel *et al.* Phys. Rev. B (06)

Case-III



Control parameter

**QCP**

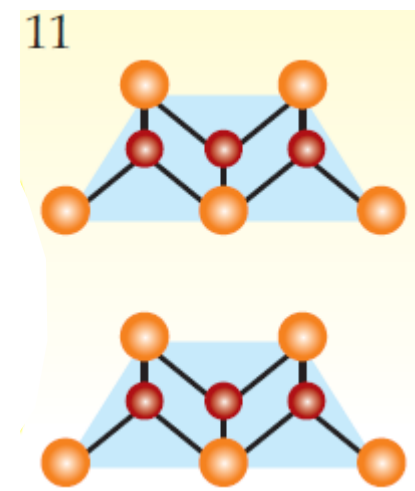
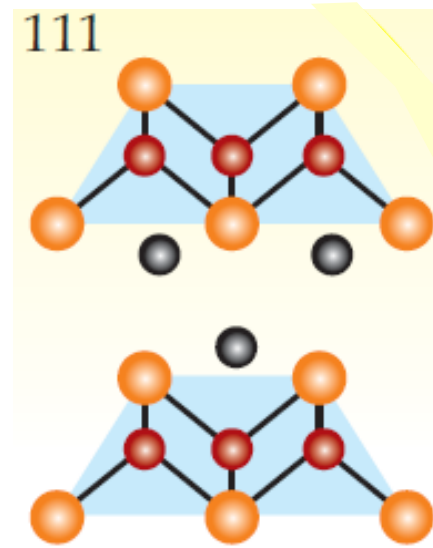
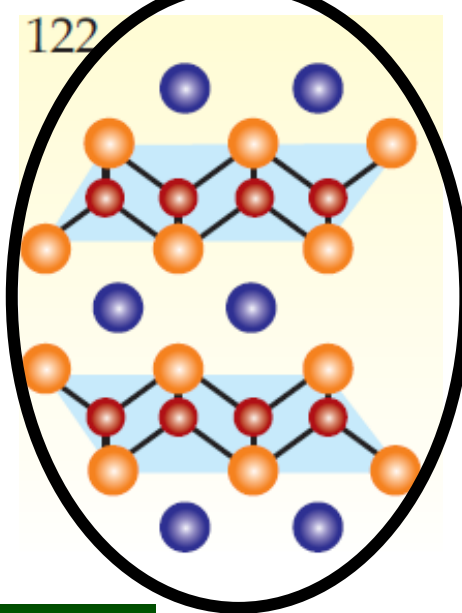
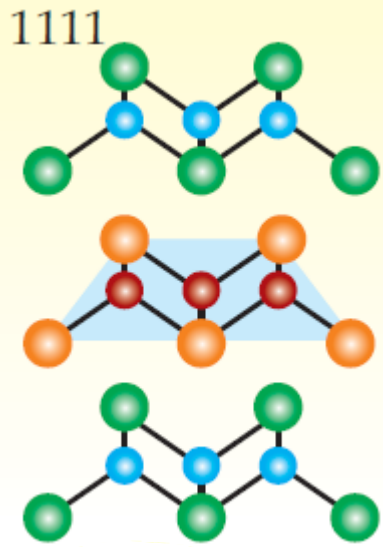
*Other heavy fermions ??*

*Pnictides ??*

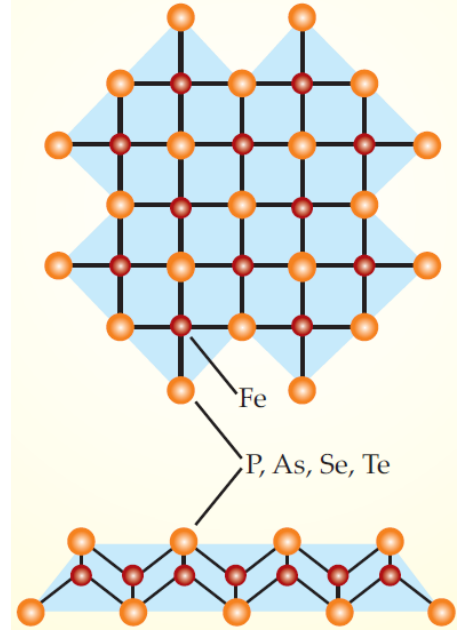
*Cuprates ??*

T. Kawasaki *et al.* J. Phys. Soc. Jpn (04)

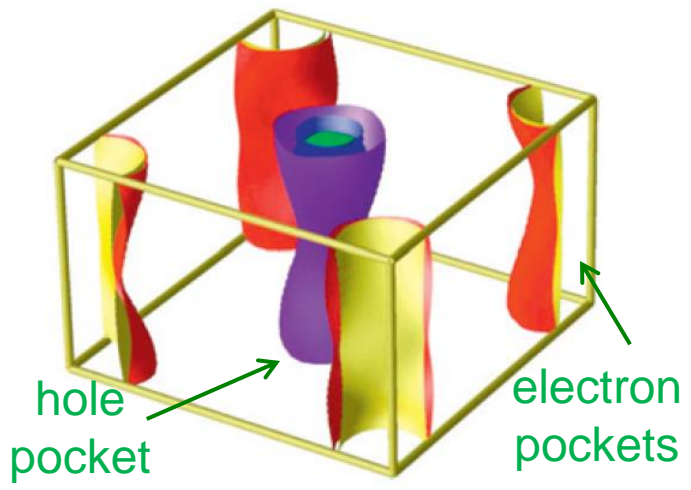
# Fe-based high- $T_c$ superconductors



2D square lattice of Fe



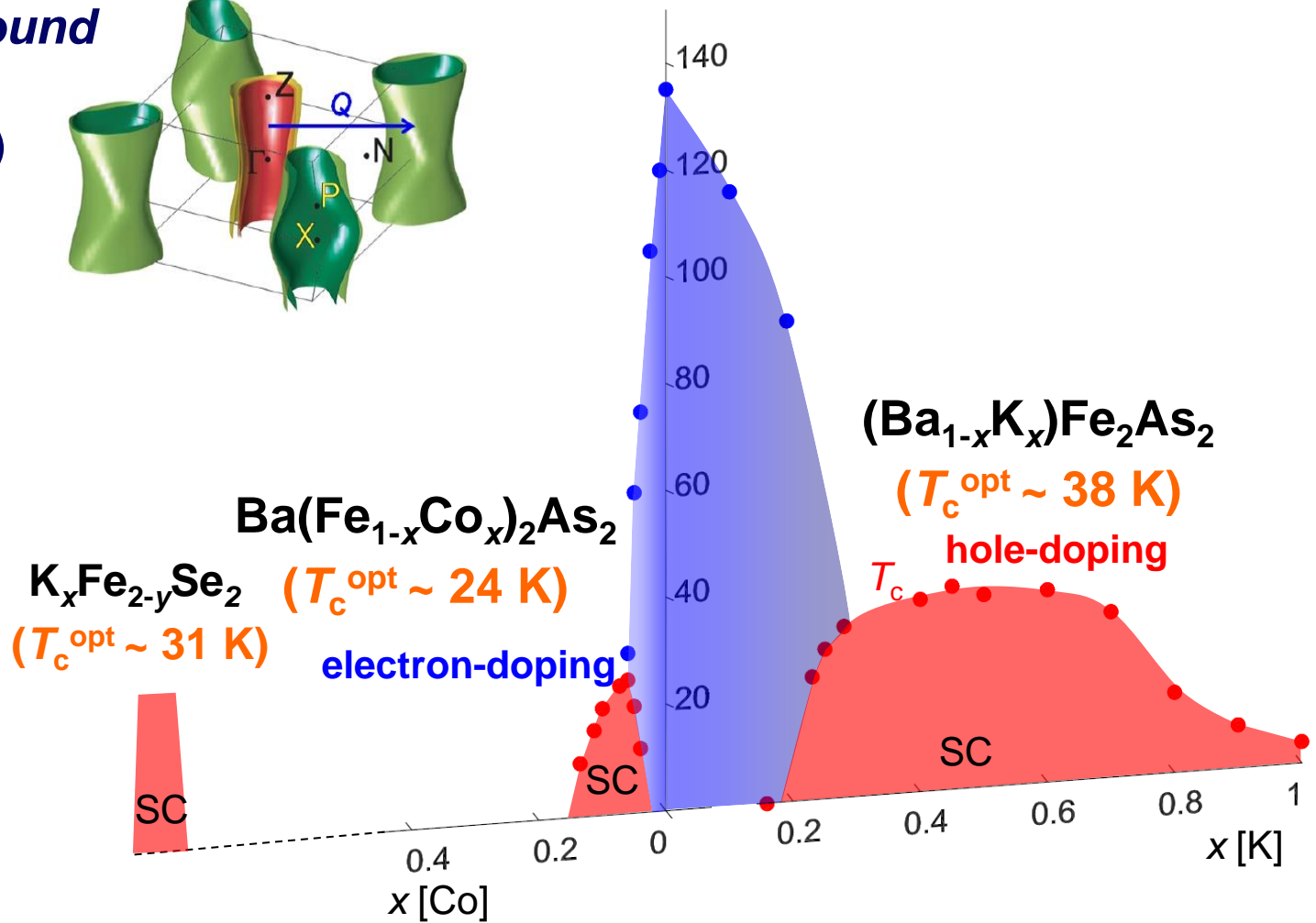
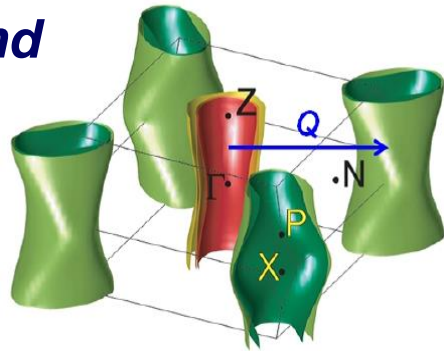
Well separated electron and hole sheets



# Superconductivity in BaFe<sub>2</sub>As<sub>2</sub> systems

Parent compound

BaFe<sub>2</sub>As<sub>2</sub>  
(AF Metal)

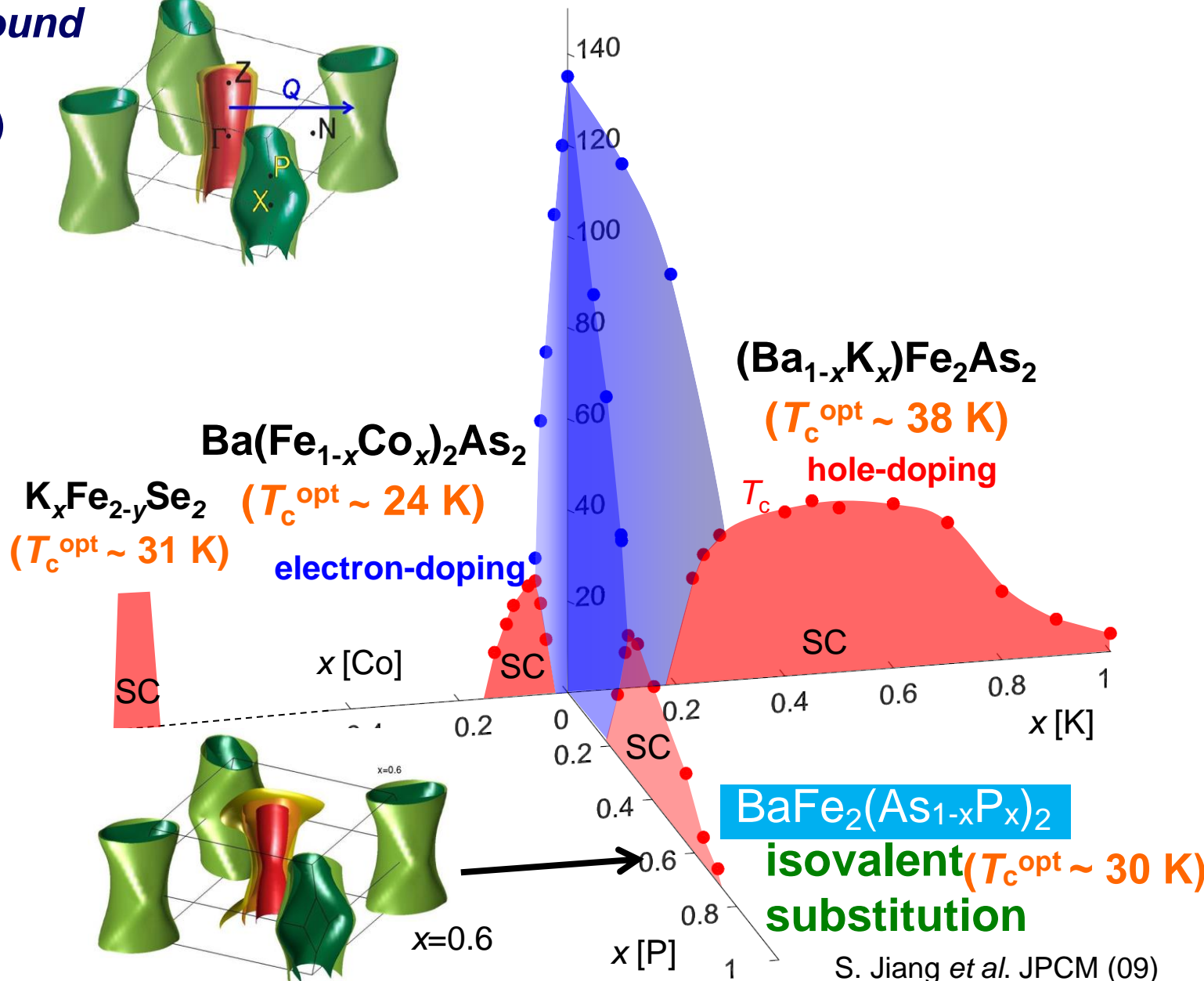
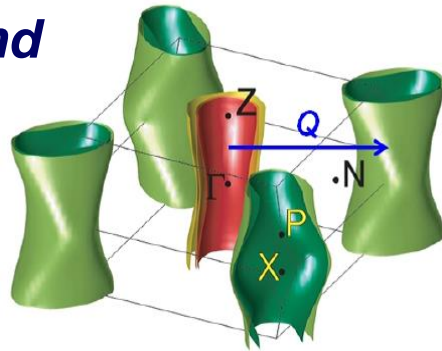




# Superconductivity in BaFe<sub>2</sub>As<sub>2</sub> systems

Parent compound

BaFe<sub>2</sub>As<sub>2</sub>  
(AF Metal)

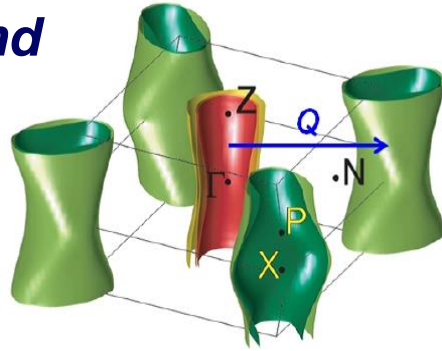


Ground state can be tuned without doping carriers

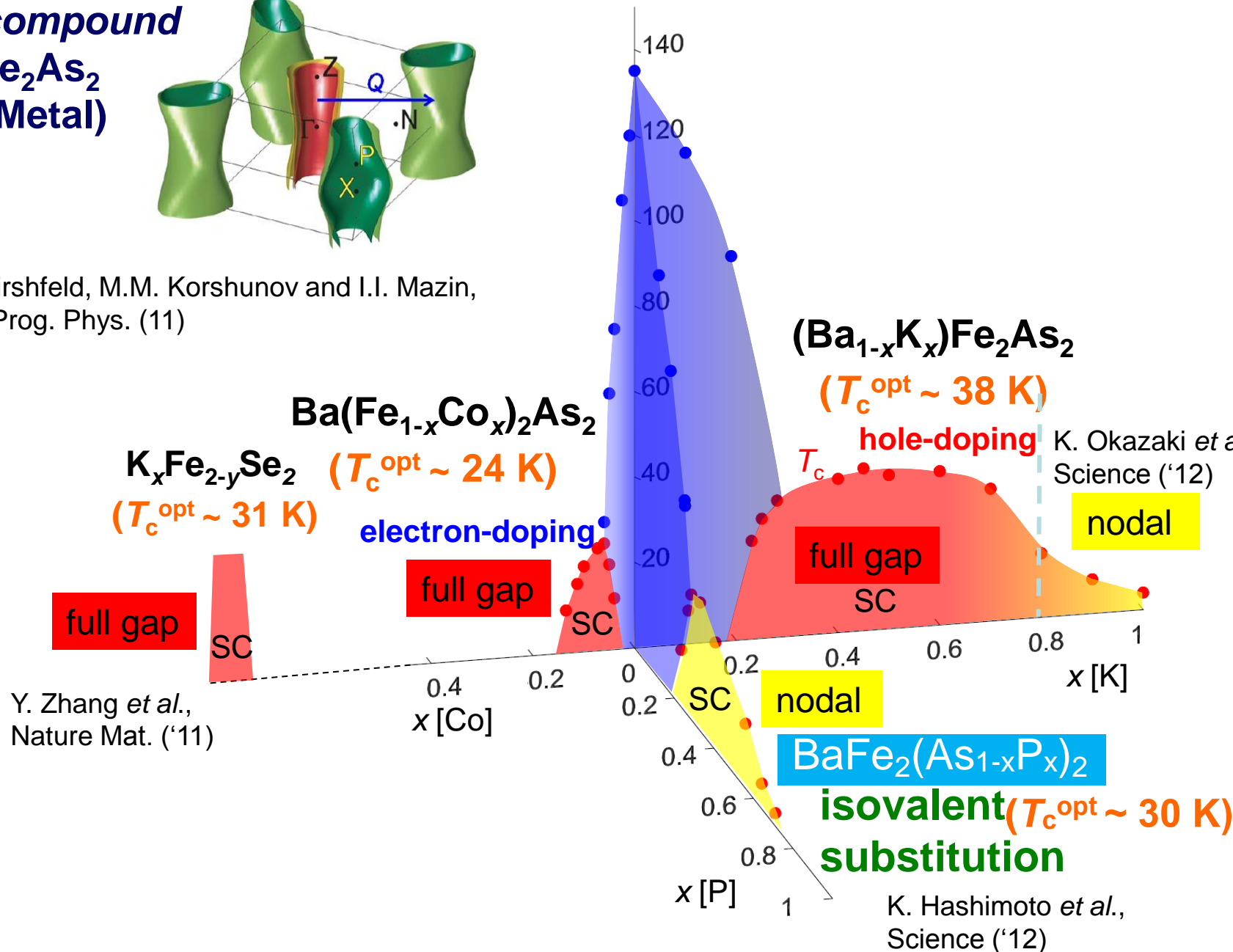
# Superconductivity in BaFe<sub>2</sub>As<sub>2</sub> systems

Parent compound

BaFe<sub>2</sub>As<sub>2</sub>  
(AF Metal)



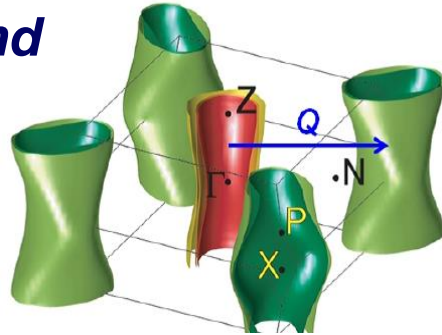
P.J. Hirshfeld, M.M. Korshunov and I.I. Mazin,  
Rep. Prog. Phys. (11)



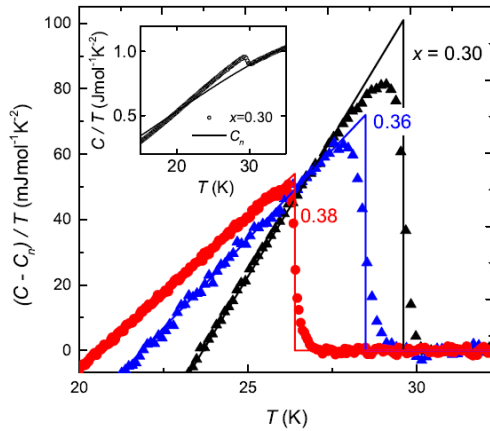
# BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub> : a clean system

Parent compound

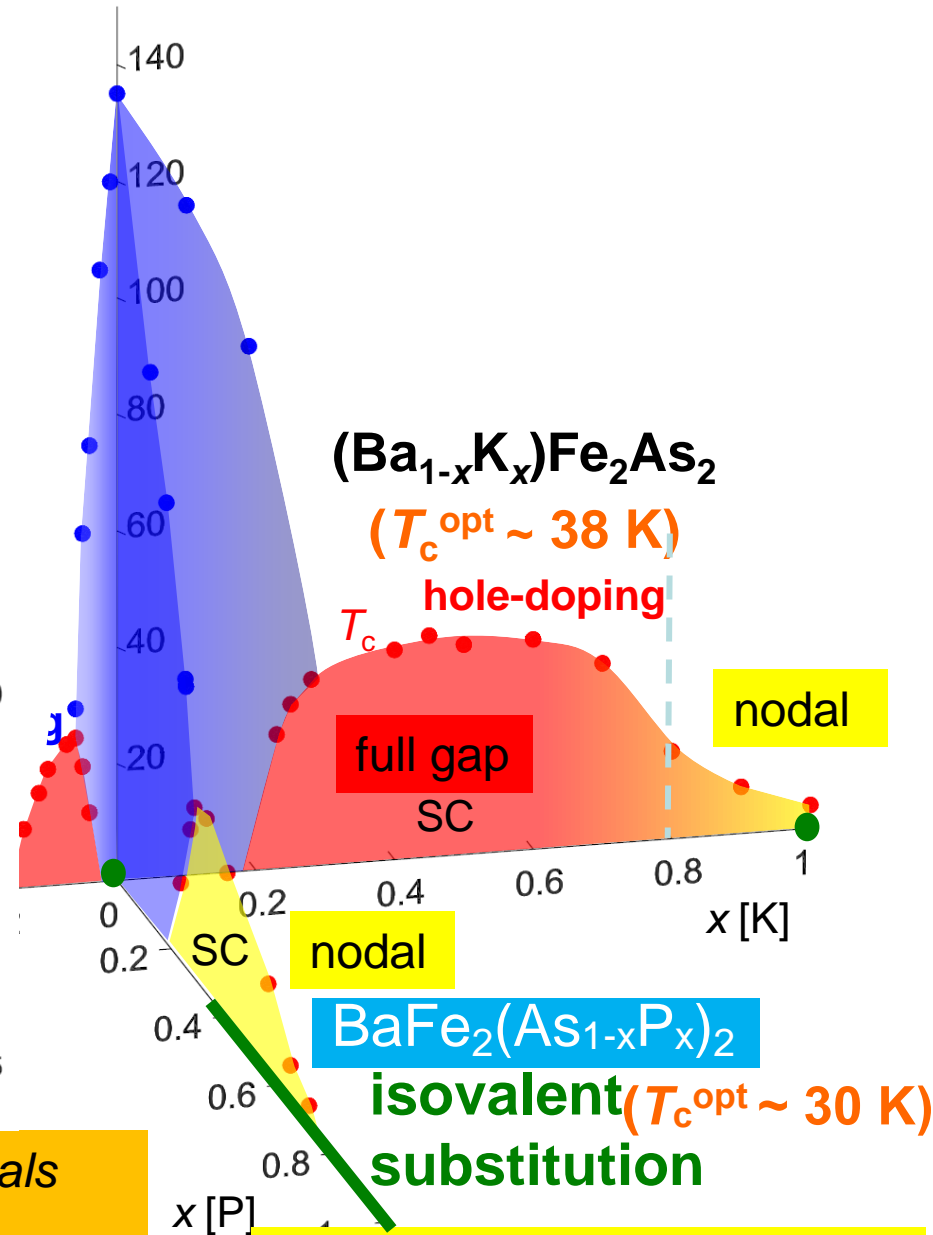
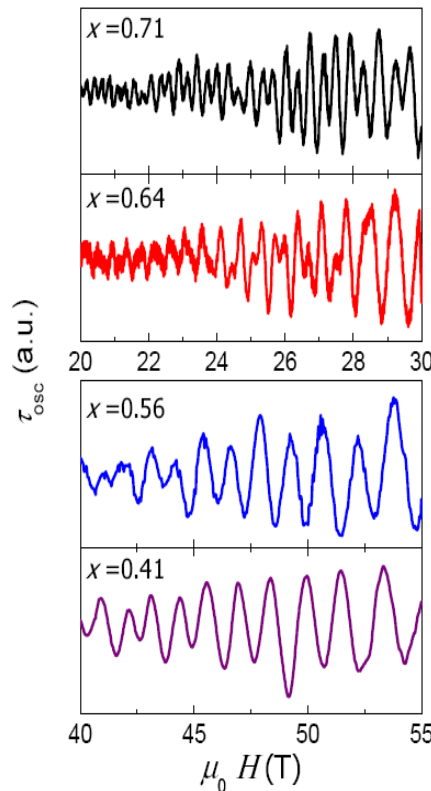
BaFe<sub>2</sub>As<sub>2</sub>  
(AF Metal)



BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>



H. Shishido *et al.* PRL (10)  
J.G. Analytis *et al.* PRL (11)  
P. Walmsley *et al.* PRL (13)



(Ba<sub>1-x</sub>K<sub>x</sub>)Fe<sub>2</sub>As<sub>2</sub>

(*T<sub>c</sub>*<sup>opt</sup> ~ 38 K)

hole-doping

full gap

SC

nodal

BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>

isovalent (*T<sub>c</sub>*<sup>opt</sup> ~ 30 K)

substitution

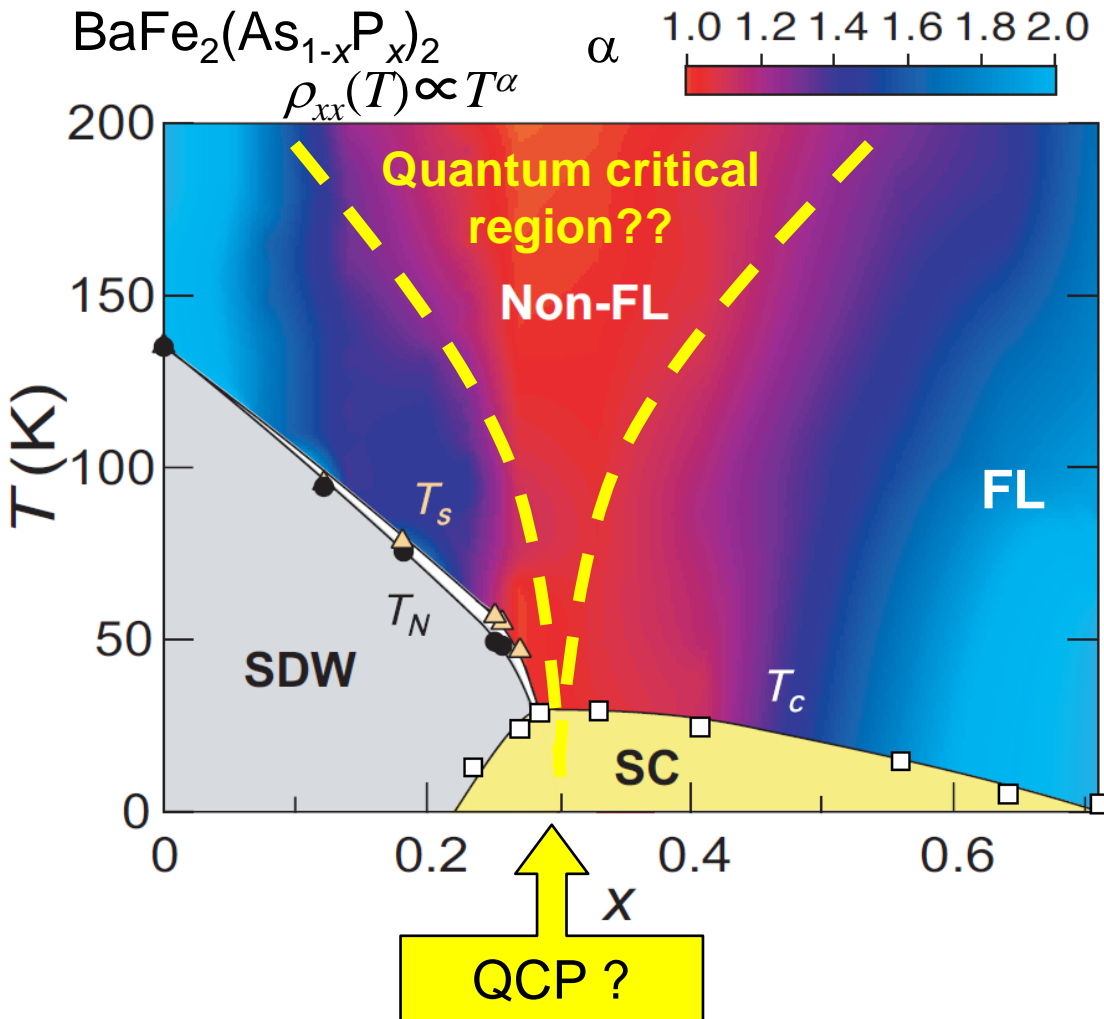
Quantum oscillations

Clean and homogeneous single crystals have been available.

# Quantum phase transition lurking inside the superconducting dome

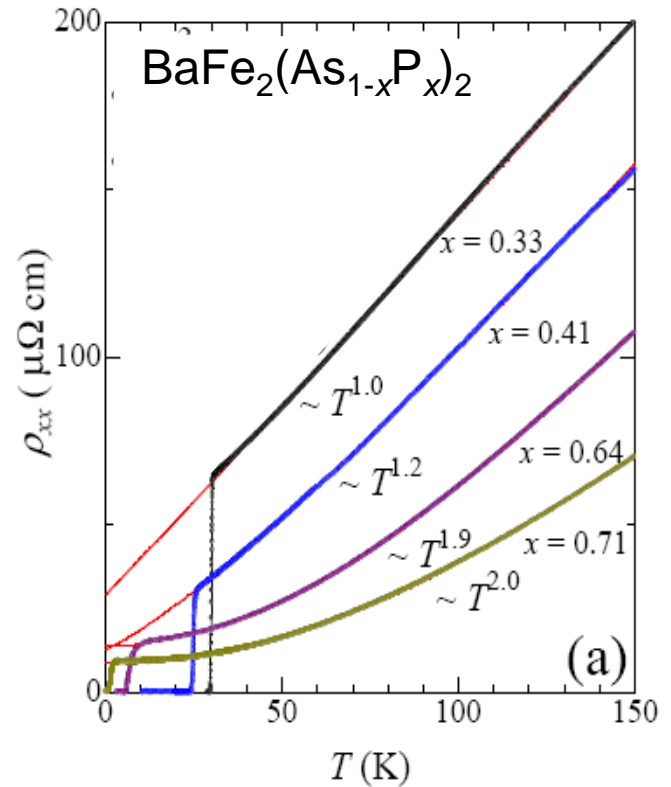
Influence of quantum critical fluctuations on  
*normal* and *superconducting* electrons

# Doping evolution of the transport property



S. Kasahara *et al.*, PRB **81**, 184519 (10)

A.E. Böhrer *et al.* Phys. Rev. B **86**, 094521 (12)



$T$ -linear resistivity at  $x=0.33$  just beyond SDW end point ( $x_c=0.3$ )

Hallmark of non-Fermi liquid

$T^2$ -dependence at  $x=0.71$

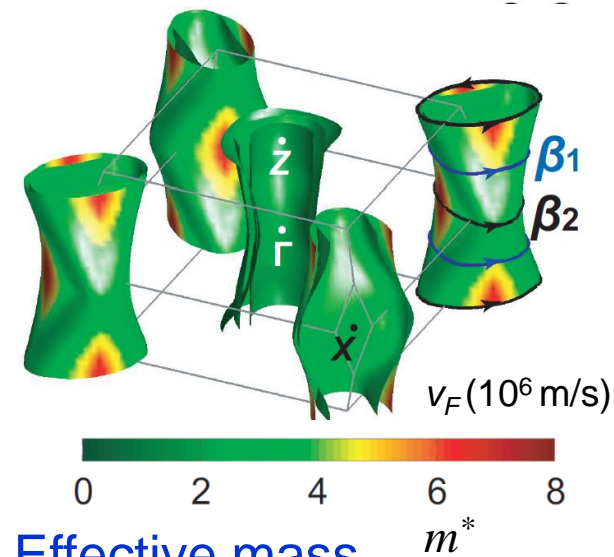
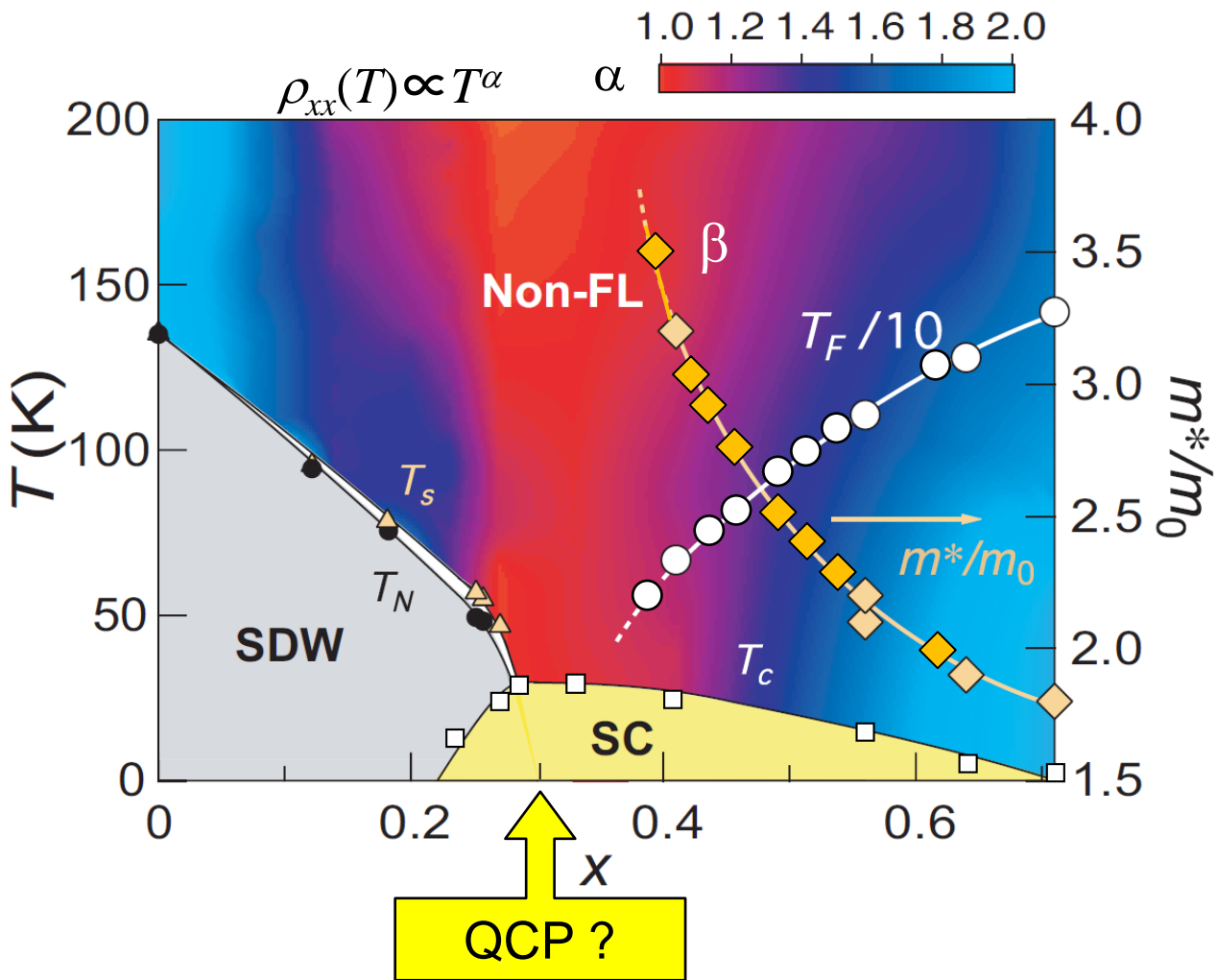
Fermi-liquid behavior

See also

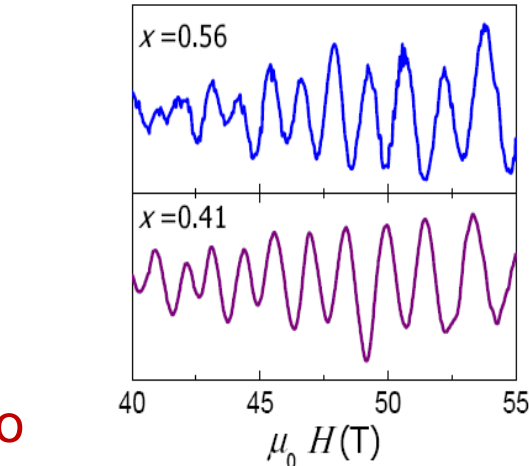
S. Sachdev and B. Keimer, Physics Today (11)

J. Dai, Q. Si, J.-X. Zhu, and E. Abrahams, PNAS (09)

# Fermi surface and mass renormalization



$T_F = \hbar e F / m^* k_B$

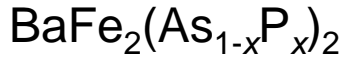


As  $x$  is tuned towards the maximum  $T_C$ ,

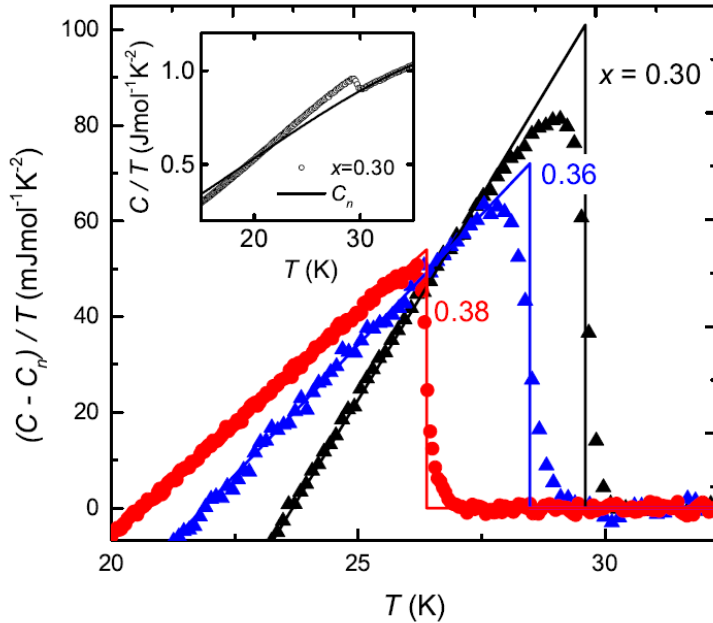
Effective mass  $m^*$  is strongly enhanced

Fermi temperature  $T_F = \hbar e F / m^* k_B$  tends to zero

# Doping evolution of the specific heat jump at $T_c$



P. Walmsley *et al.* PRL(13)

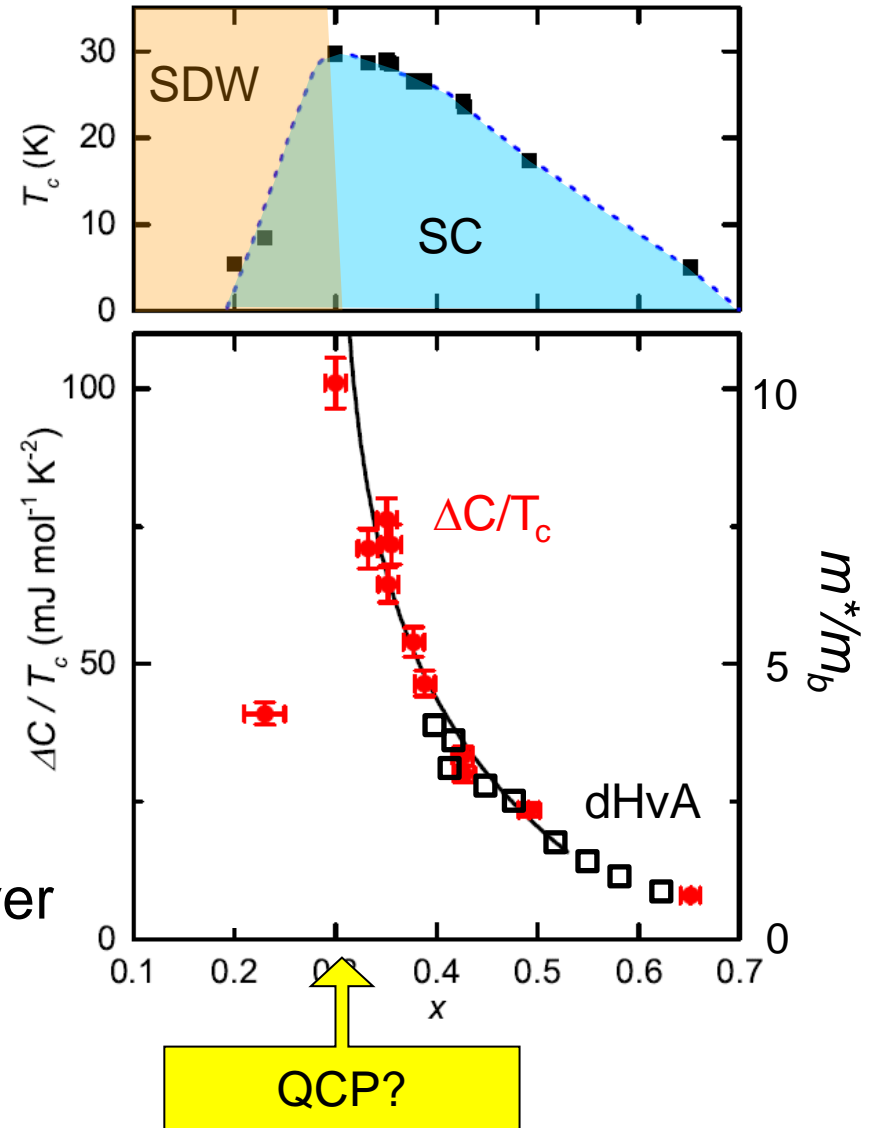


$$\frac{\Delta C}{T_c} \propto \gamma \propto m^*$$

The uniform mass enhancement over the Fermi surface

Strong mass enhancement at  $x=0.30$

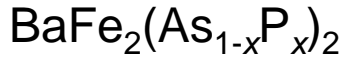
$$\gamma \sim 70 \text{ mJ/K}^2\text{mol}$$



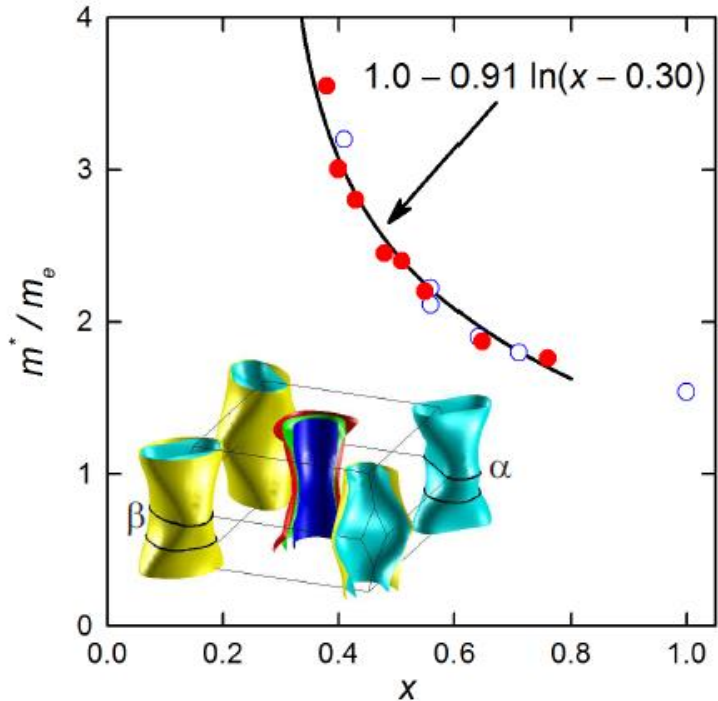
QCP?



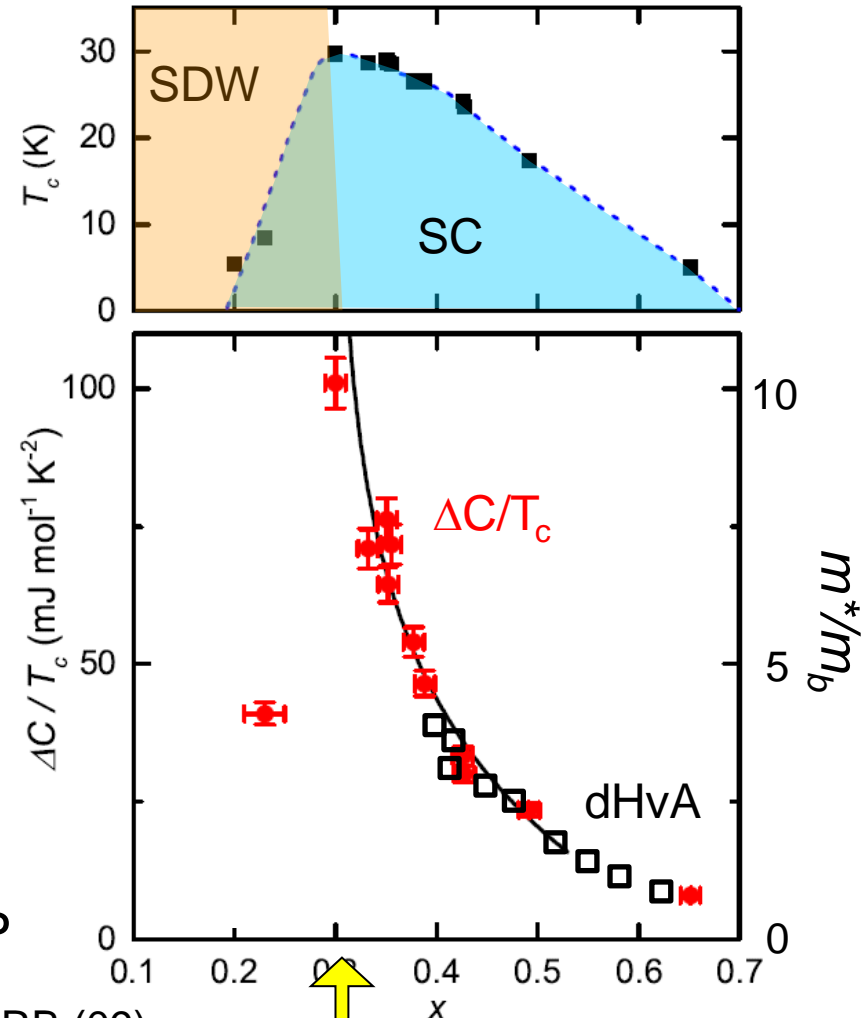
# Doping evolution of the specific heat jump at $T_c$



P. Walmsley *et al.* PRL(13)



$$\frac{m^*}{m_b} = c_0 + c_1 \ln(x - x_c)$$



expected x-dependence close to a QCP

$$\Delta C/T_c \propto T_c^2$$

S. L. Bud'ko *et al.* PRB (09)  
J. Zaanen PRB (09)

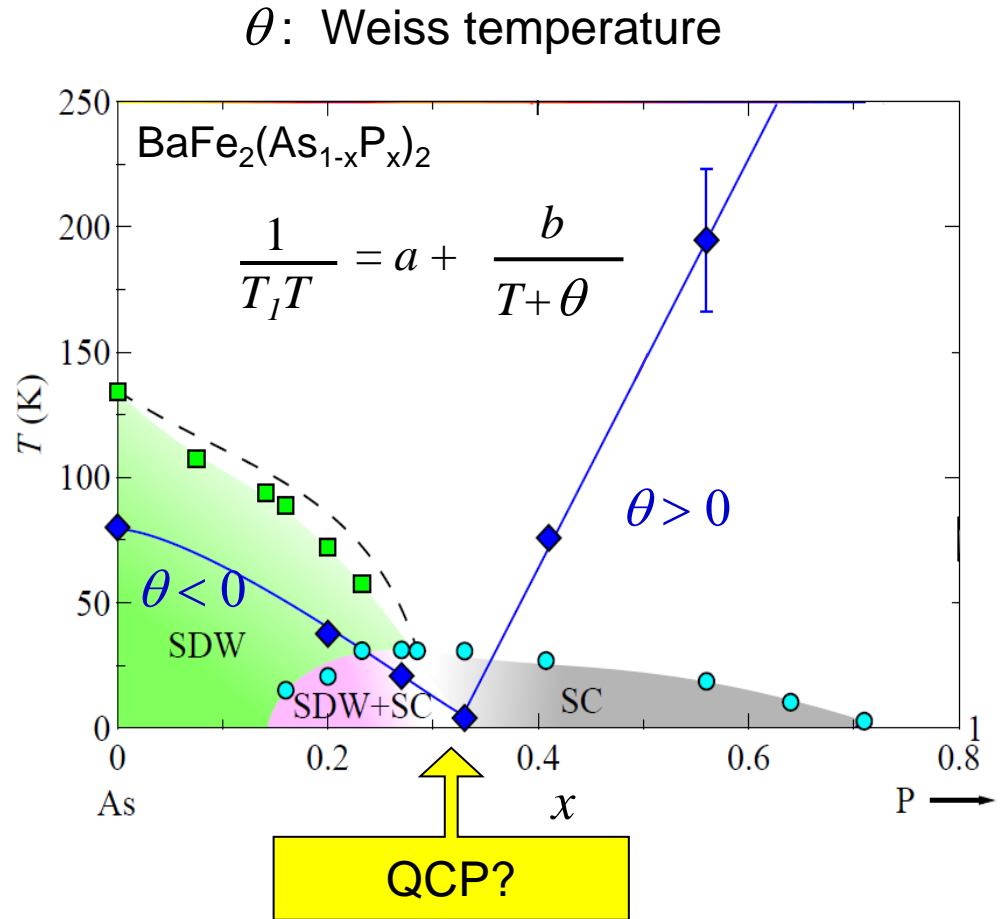
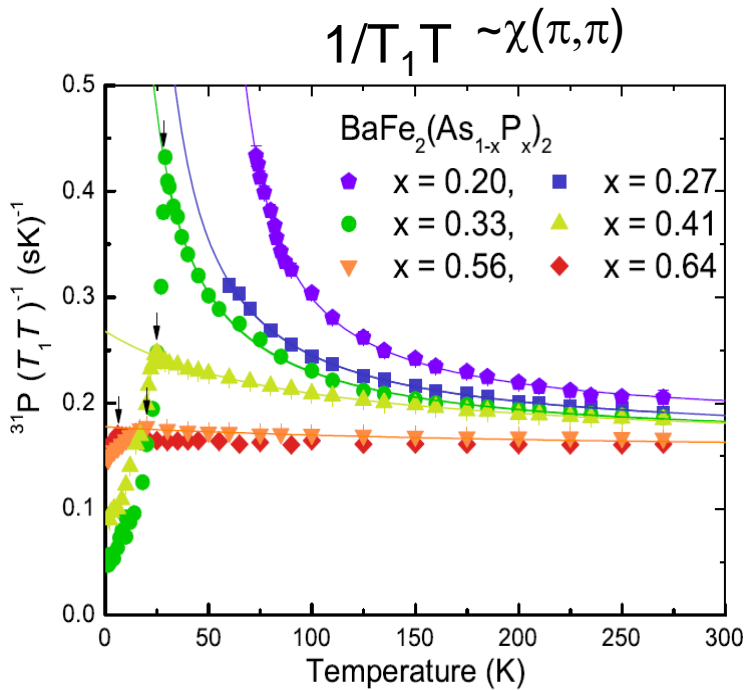
$$\Delta C/T_c \propto T_c^{5-6}$$

for  $30\text{K} > T_c > 23\text{K}$

present results

QCP?

# Doping evolution of the magnetic fluctuations ( $^{31}\text{P}$ NMR)



$\theta$  goes to zero at  $x \sim 0.3$

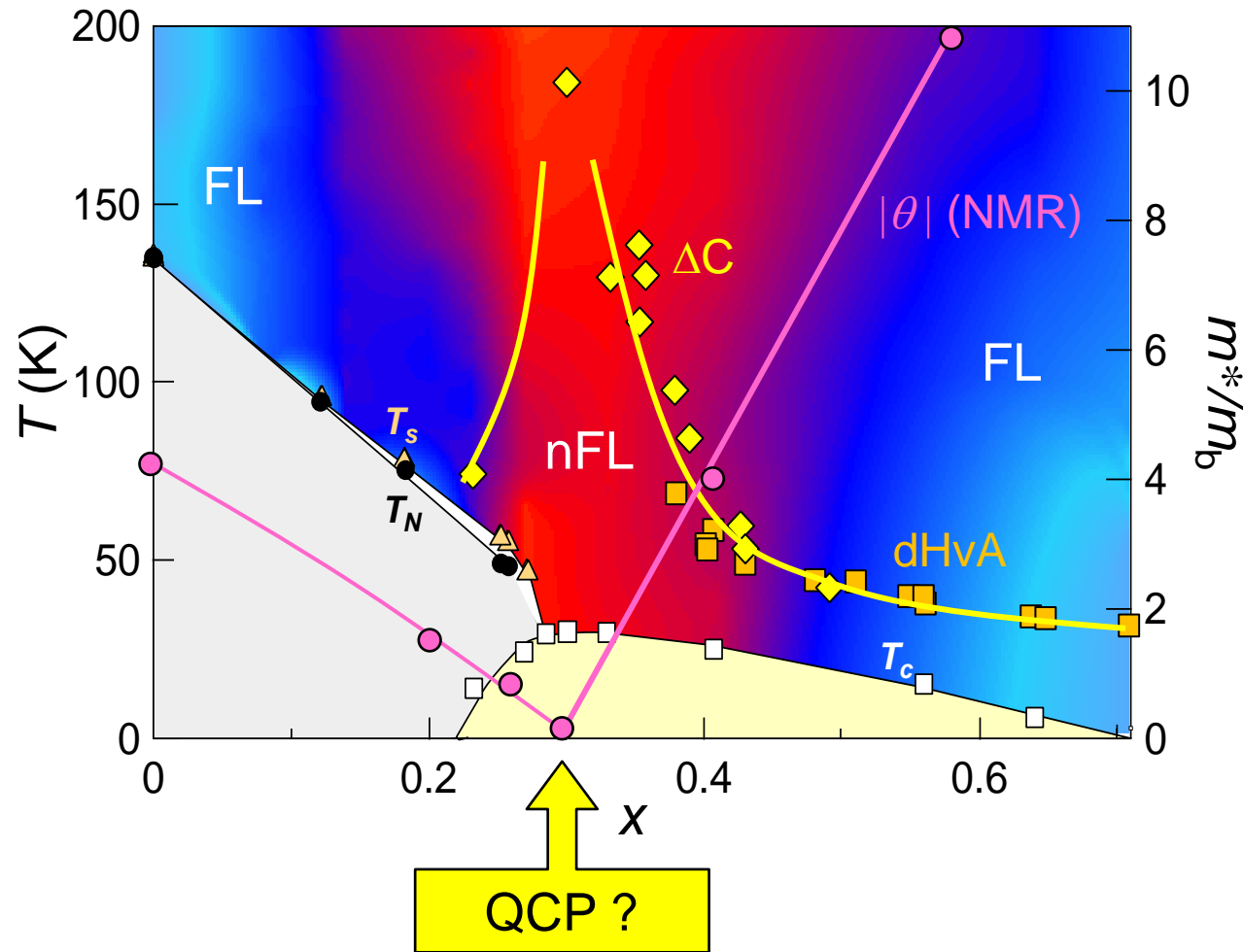
Dynamical susceptibility diverse at  $T = 0$  K.

# Doping evolution of normal electrons

$$\rho_{xx}(T) \propto T^\alpha$$

$\alpha$

As  $x$  is tuned towards the maximum  $T_c$  at  $x=0.30$



*Hallmark of non-Fermi liquid behavior*

Resistivity

*Effective mass  $m^*$  is strongly enhanced*

dHvA

Specific heat

*Weiss temperature goes to zero*

NMR

We need evidence at zero temperature and zero field.

# Quantum phase transition lurking inside the superconducting dome

Influence of quantum critical fluctuations on  
*normal and superconducting electrons*

# Doping evolution of the London penetration depth at $T=0$

London penetration depth  $\lambda_L$  is the quantity that can probe the electronic structure **at zero temperature limit.**

$$\lambda_L^{-2}(0) = \frac{\mu_0 n_s e^2}{m^*}$$

Number of superfluid  
Mass of superfluid

1. Tunnel diode oscillator (13MHz, 70 mK)

Al coated method

2. Microwave surface impedance

Rutile cavity resonator (5 GHz,  $Q \sim 10^6$ , 350 mK)

3. Nodal superconducting gap structure

Line node

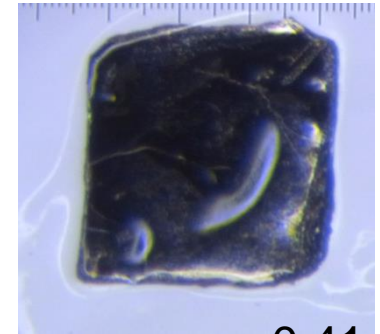
$$\frac{\delta\lambda_L(T)}{\lambda_L(0)} \approx \frac{\ln 2}{\Delta} k_B T$$

# Determination of the London penetration depth at $T=0$

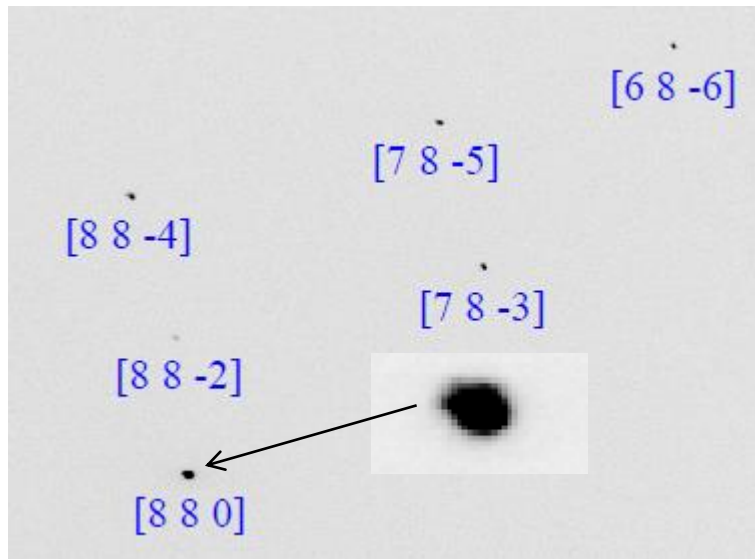
## Very small single crystals

Typical crystal size  $\sim 200 \times 200 \times 10 \mu\text{m}^3$   
Rectangular shape  
Cleaved just before the measurements

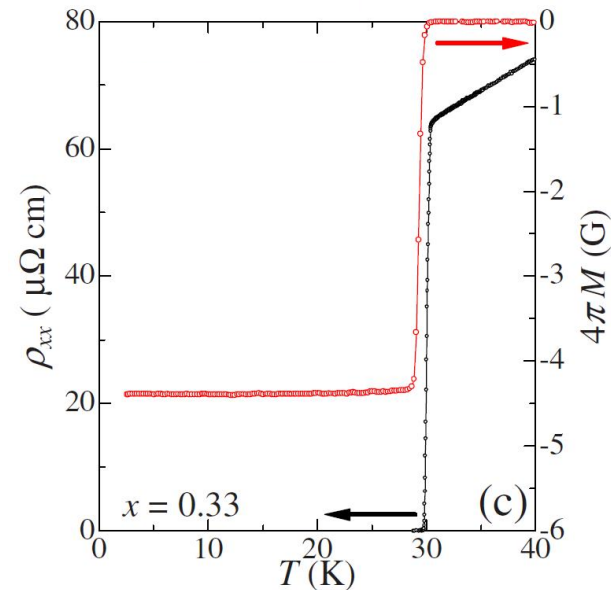
$225.9 \times 217.6 \times 10 \mu\text{m}^3$



$x=0.41$



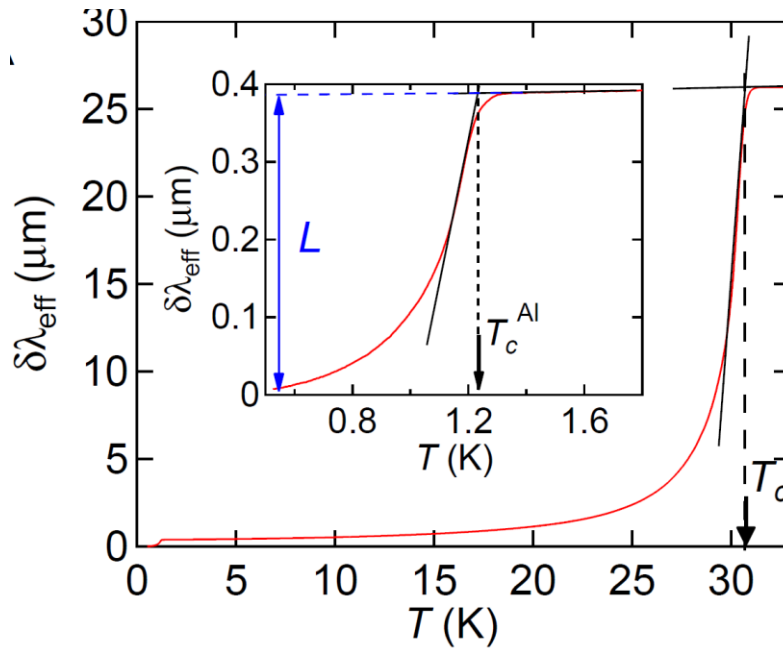
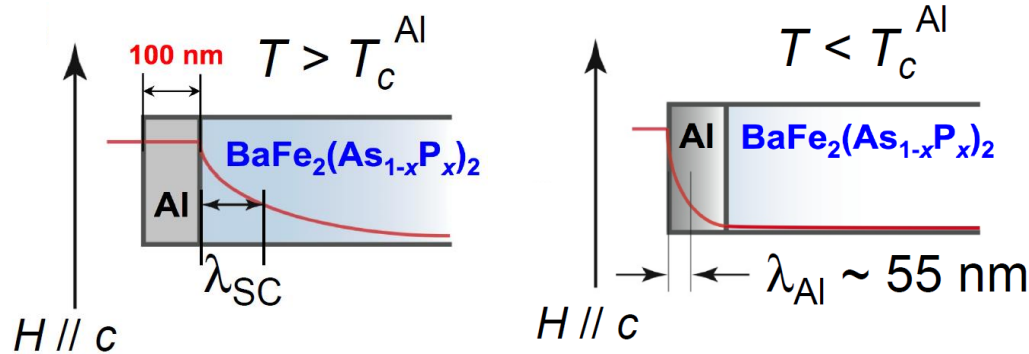
Synchrotron X-ray diffraction pattern shows high crystalline quality



Sharp SC transition  
Nearly perfect Meissner state with negligibly small non-SC region

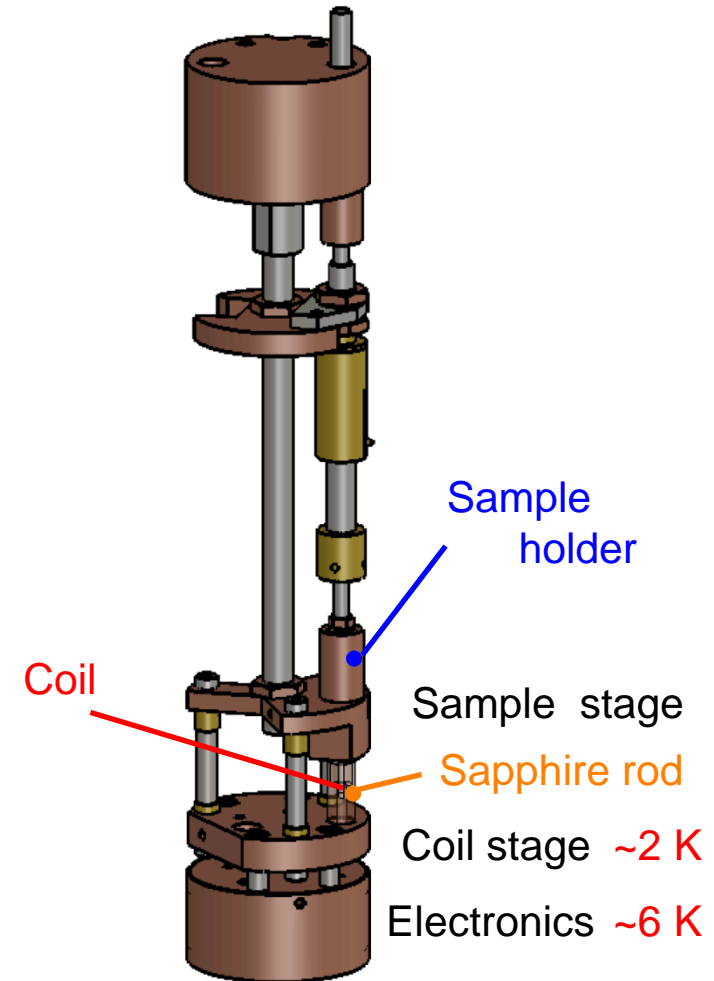
# Determination of the London penetration depth at $T=0$

## 1. Al coated method (Tunnel diode oscillator, 13MHz)



$$\lambda_{\text{eff}}(T) = \lambda_{\text{Al}}(T) \frac{\lambda(T) + \lambda_{\text{Al}}(T) \tanh \frac{t}{\lambda_{\text{Al}}(T)}}{\lambda_{\text{Al}}(T) + \lambda(T) \tanh \frac{t}{\lambda_{\text{Al}}(T)}}$$

$^3\text{He}/^4\text{He}$  mixing chamber



Error bar of  $\lambda_L(0)$  :  $\pm 15\%$



# Determination of the London penetration depth at $T=0$

## 2. Microwave surface impedance

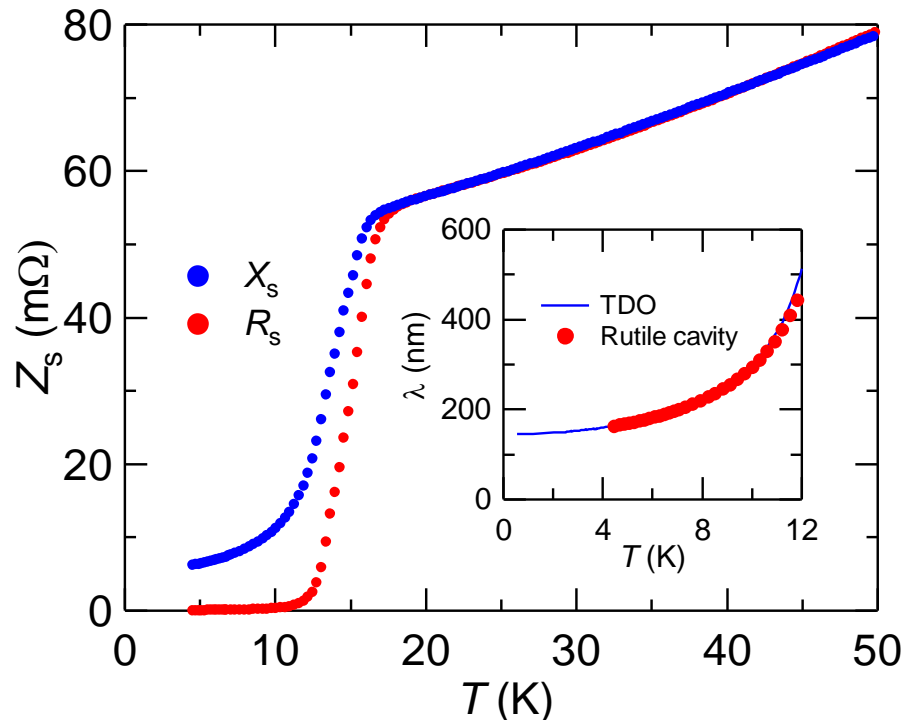
$$R_s = G_1 \left( \frac{1}{2Q_s} - \frac{1}{2Q_0} \right) \quad X_s = G_2 \left( -\frac{f_s - f_0}{f_0} \right) + C$$

Normal state

$$R_s = X_s$$

Superconducting state

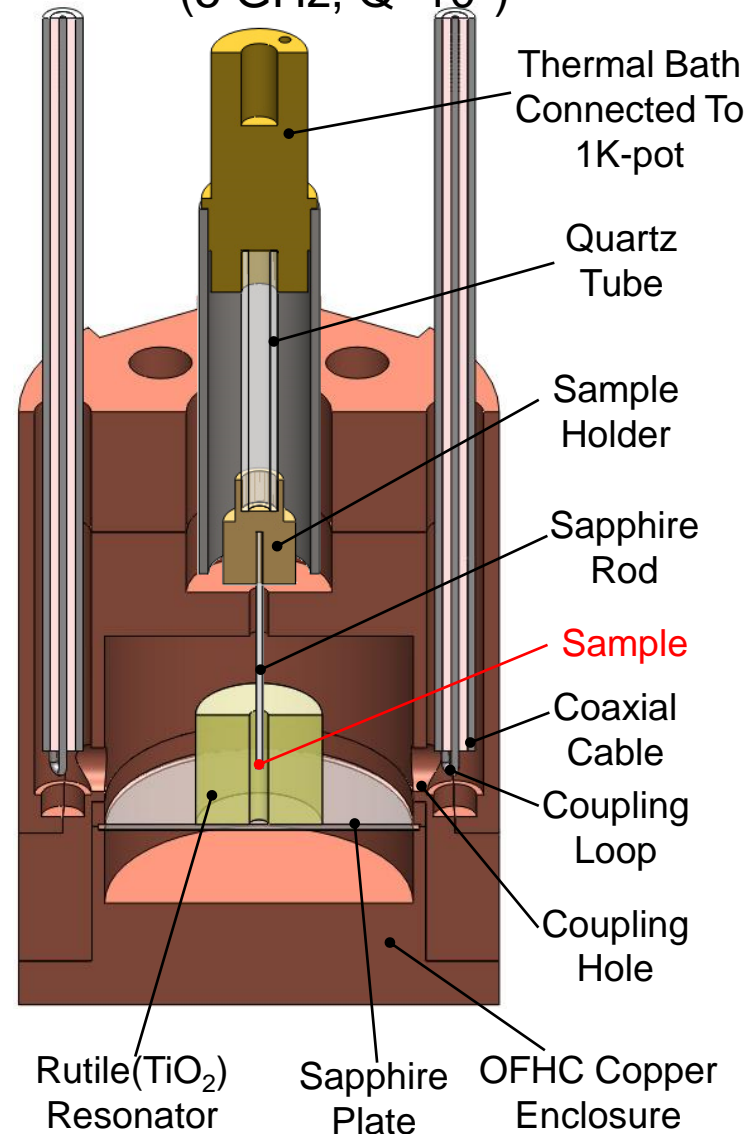
$$\lambda_{ab} = \frac{X_s}{\mu_0 \omega}$$



$$R_s(0) < 10^{-3} R_s(T > T_c)$$

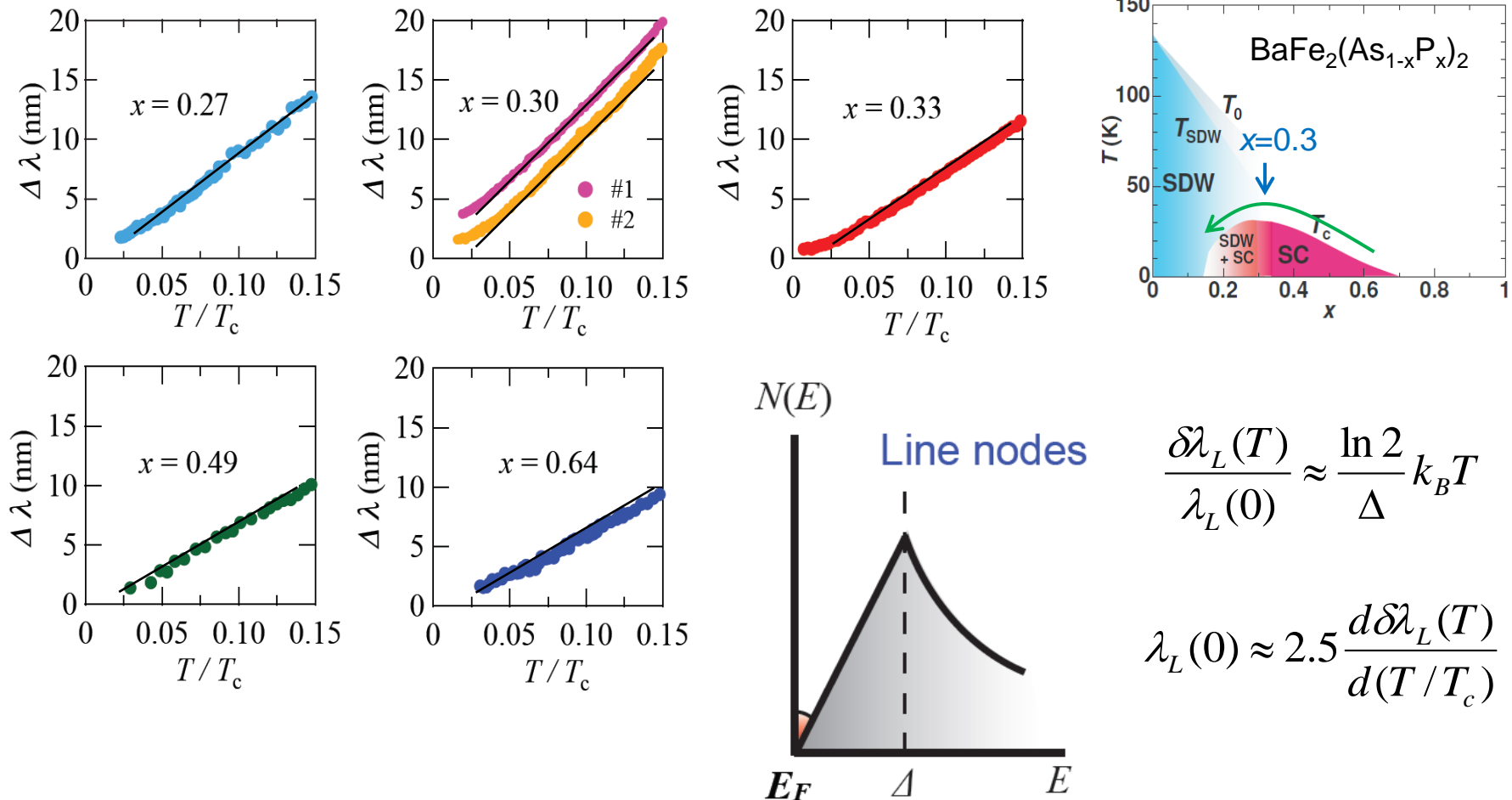
Error bar of  $\lambda_L(0)$ :  $\pm 15\%$  W.A. Huttema *et al.* Rev. Sci. Instrum (06)

## Rutile cavity resonator (5 GHz, $Q \sim 10^6$ )



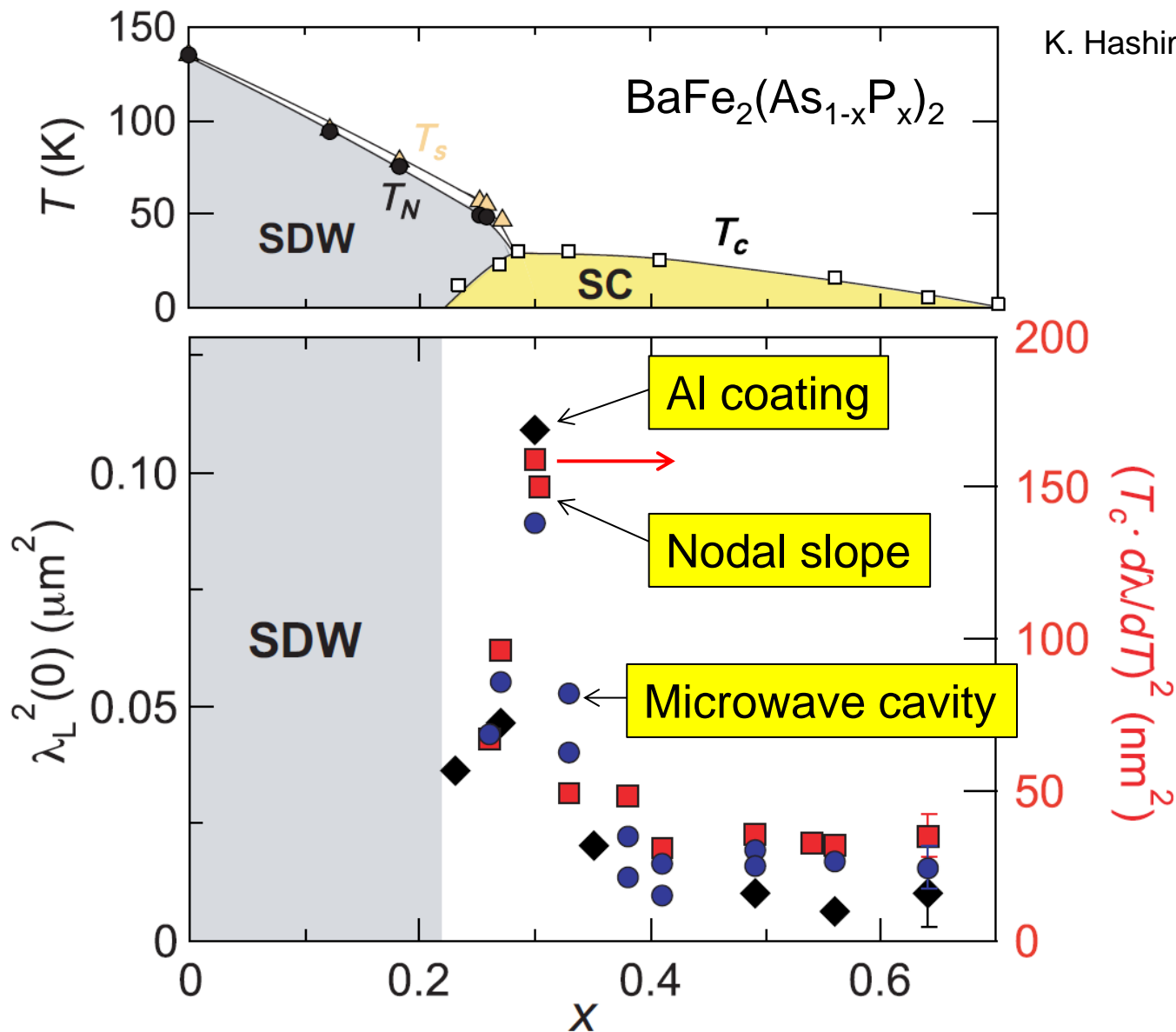
# Determination of the London penetration depth at $T=0$

## 3. Nodal superconducting gap structure



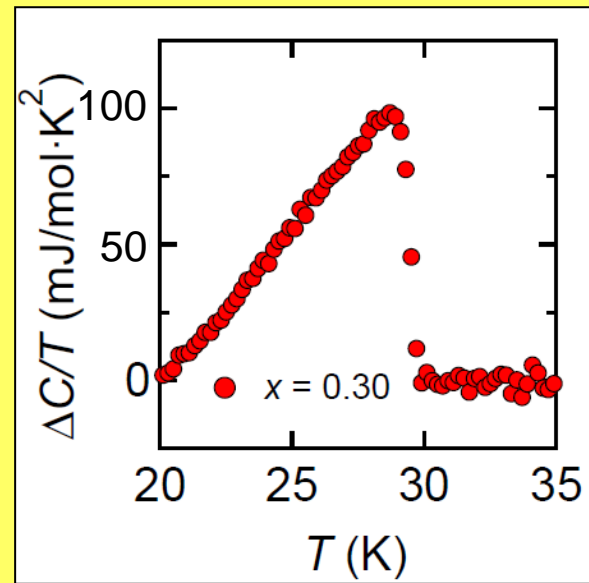
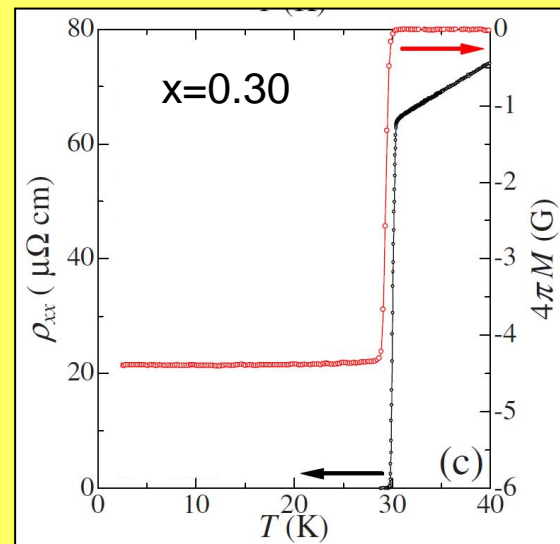
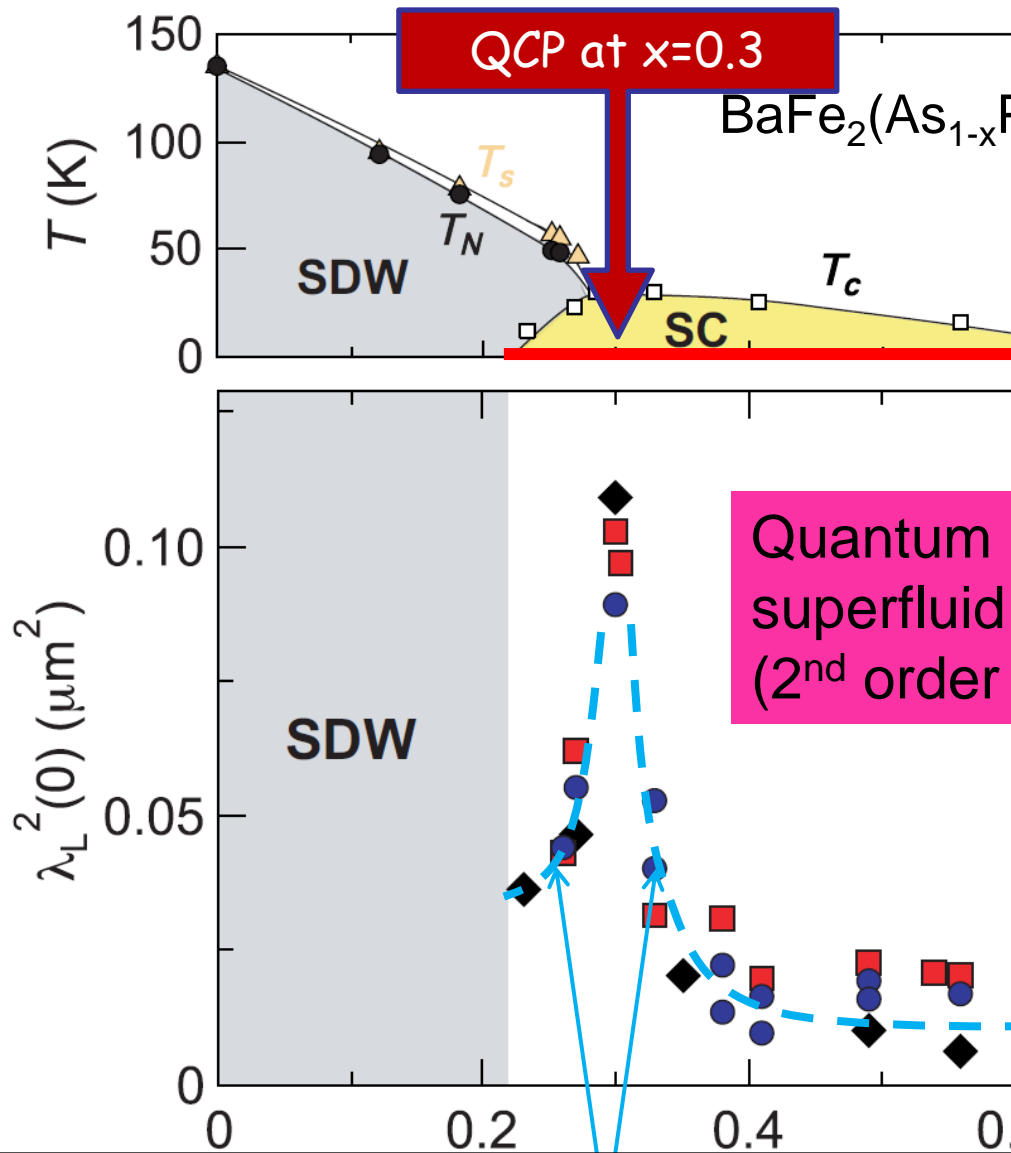
Error bar of  $\lambda_L(0) \pm 10\%$

# Doping evolution of the London penetration depth at $T=0$



All three methods give very similar  $x$ -dependence

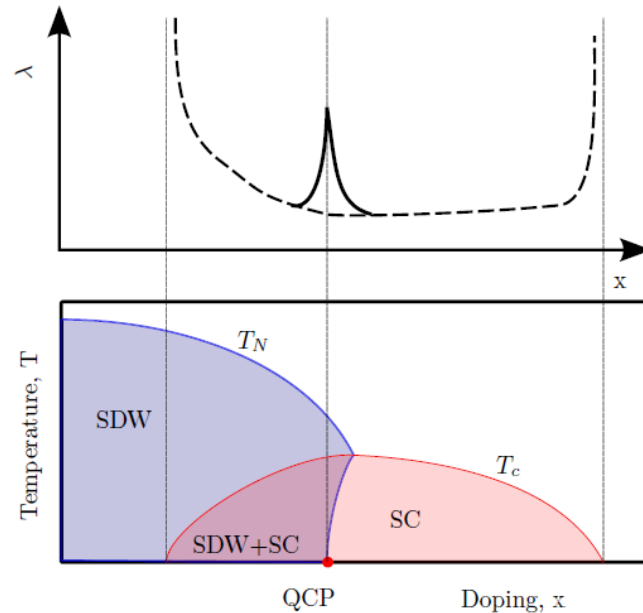
# Doping evolution of the London penetration depth at $T=0$



Striking enhancement of  $\lambda_L^2(0)$  on approaching

The data represents the behavior at the zero temperature limit.

# Singularity of the London penetration depth at QCP



## 1) Mass renormalization of superfluid by critical magnetic fluctuations

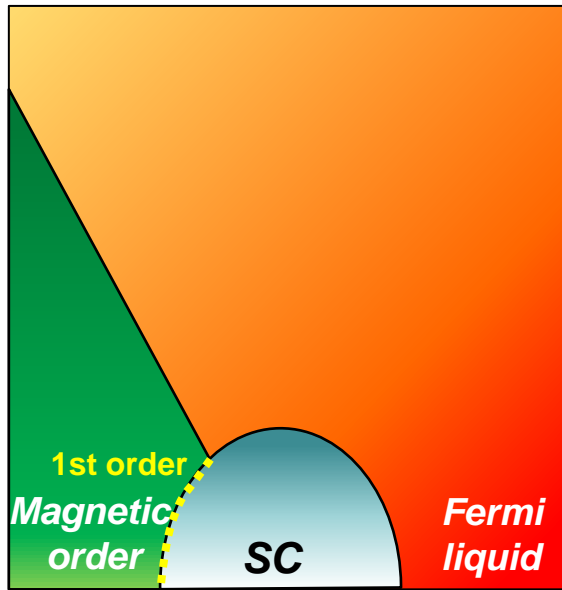
A. Levchenko, M. G. Vavilov, M. Khodas, and A. V. Chubukov, PRL (13)  
T. Nomoto and H. Ikeda, PRL (13)

## 2) SDW fluctuations + nematic order

D. Chowdhury, B. Swingle, E. Berg, and S. Sachdev, PRL (13)

# What lies beneath the SC dome?

Case-I



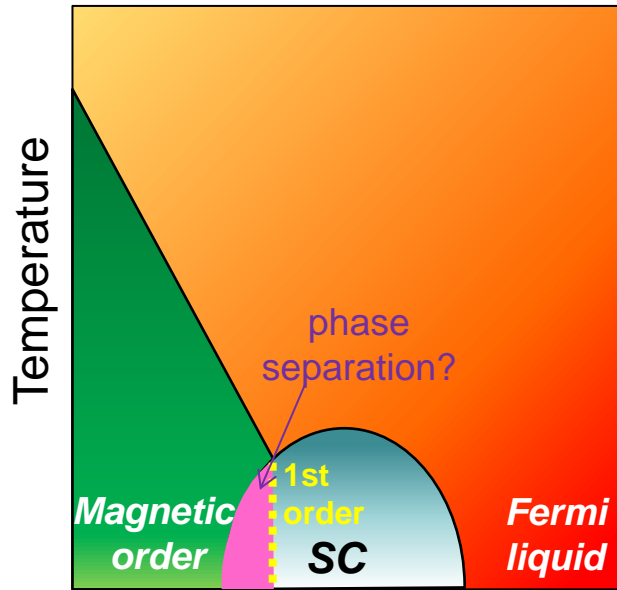
Control parameter



NMR

T. Kawasaki *et al.* J. Phys. Soc. Jpn (04)

Case-II



Control parameter



Specific heat

T. Park *et al.* Nature (06)

G. Knebel *et al.* Phys. Rev. B (06)



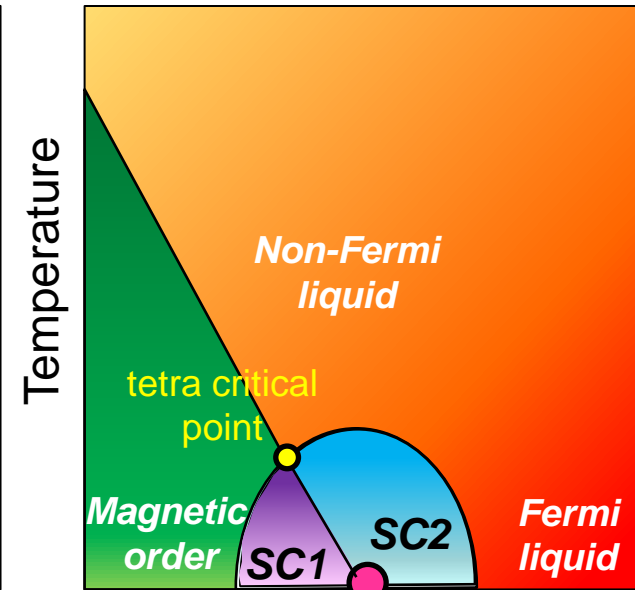
Neutron

Xingye Lu *et al.* PRL (13)



No anomaly in  $\lambda_L$

Case-III



Control parameter

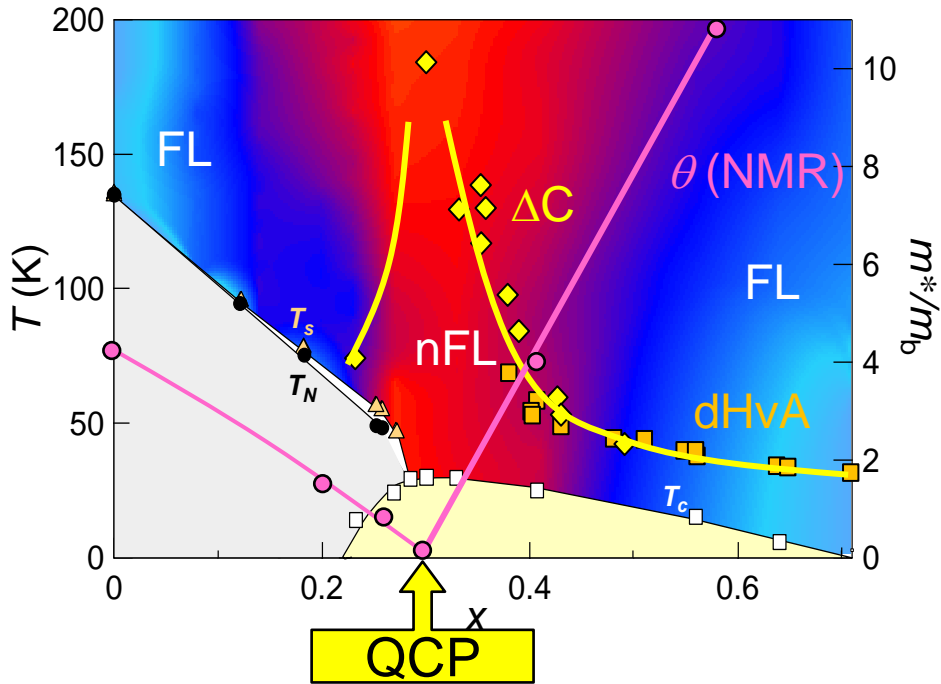
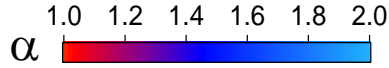


K. Hashimoto *et al.* Science (12)

# QCP lies beneath the dome

Normal electrons

$$\rho_{xx}(T) \propto T^\alpha$$



Hallmark of non-Fermi liquid behavior

S. Kasahara *et al.* PRB (10)

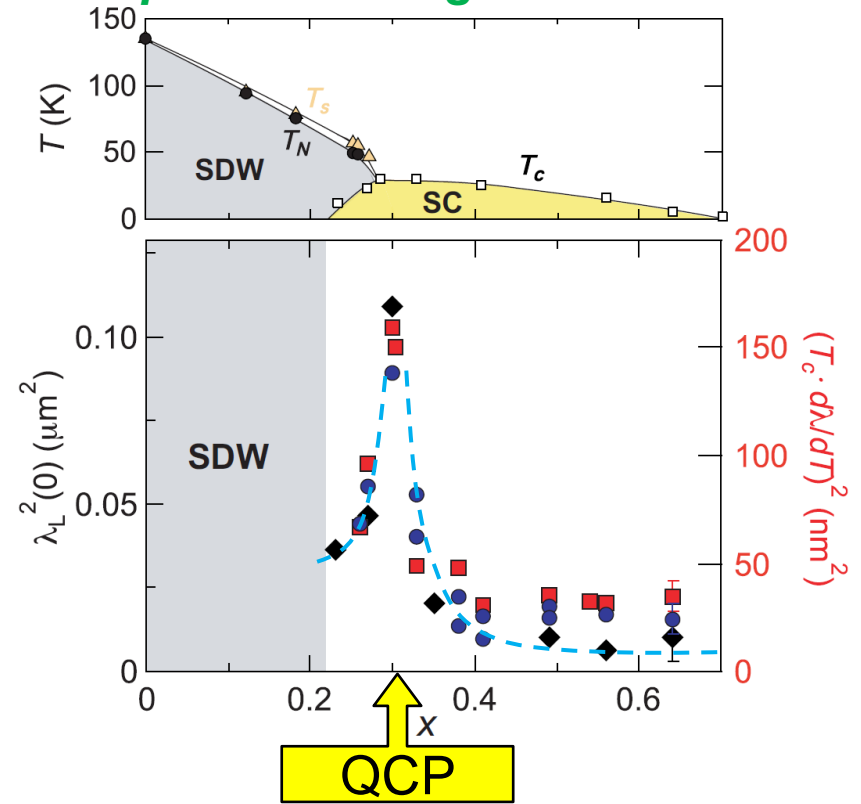
Enhancement of normal electron mass

H. Shishido *et al.* PRL (10), P. Walmsley *et al.* PRL(13)

Vanishing of Weiss temperature

Y. Nakai *et al.* PRL (10)

Superconducting electrons



Striking enhancement of superfluid mass

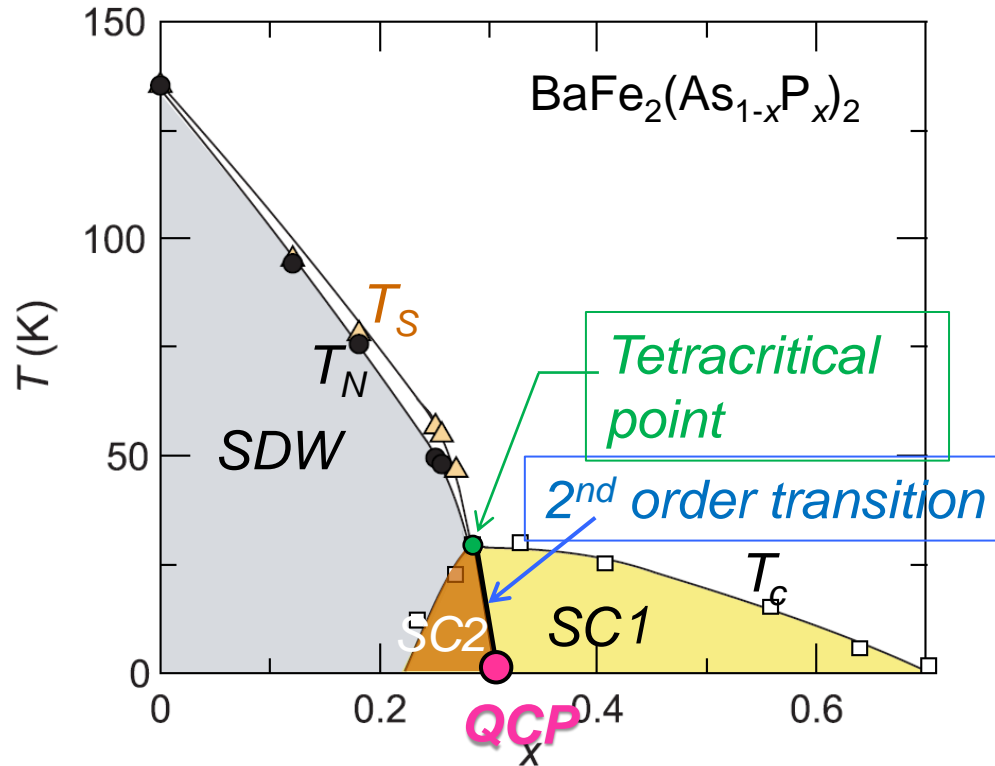
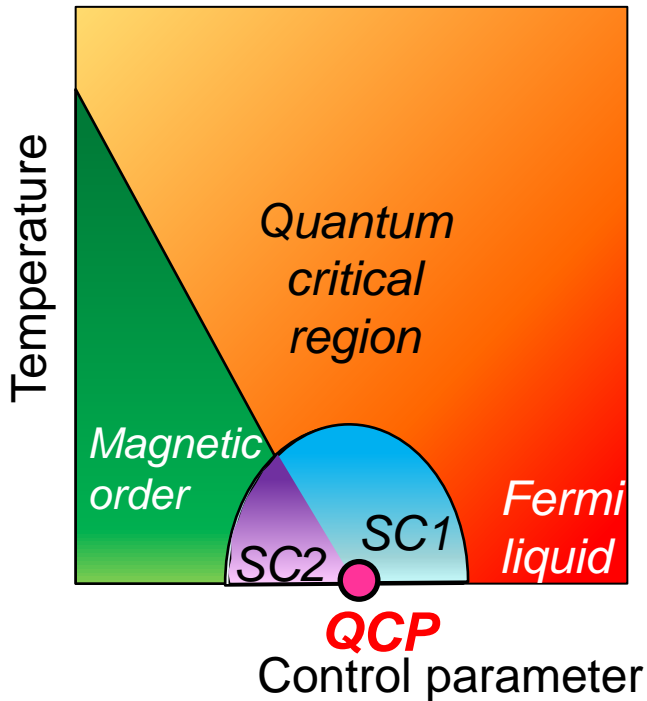
K. Hashimoto *et al.* Science (12), PNAS (13)

QCP lies beneath the superconducting dome

T. Shibauchi, A. Carrington and Y. Matsuda, Annu. Rev. Condens. Matter Phys. 5, 113 (14)

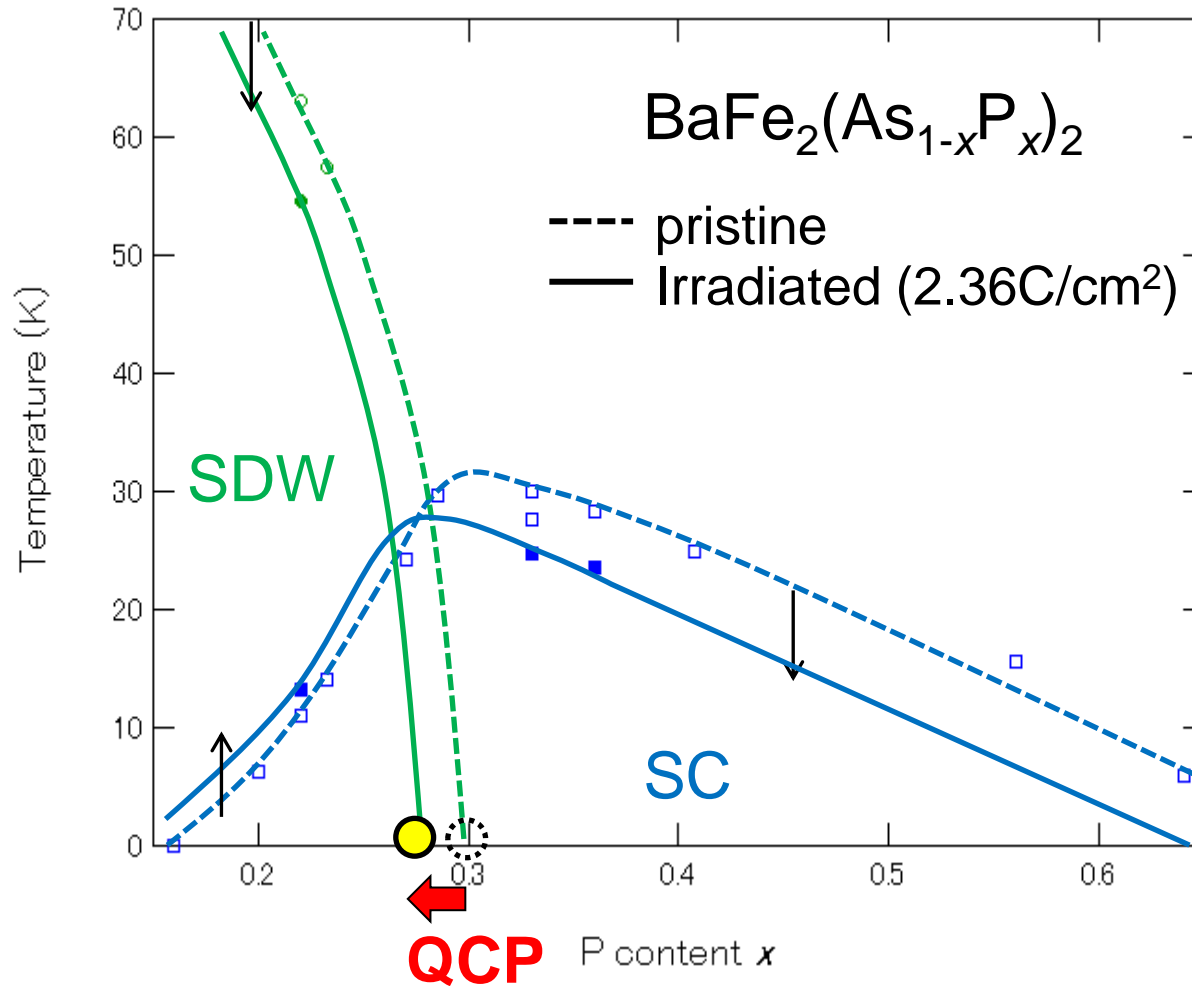


# QCP lies beneath the dome



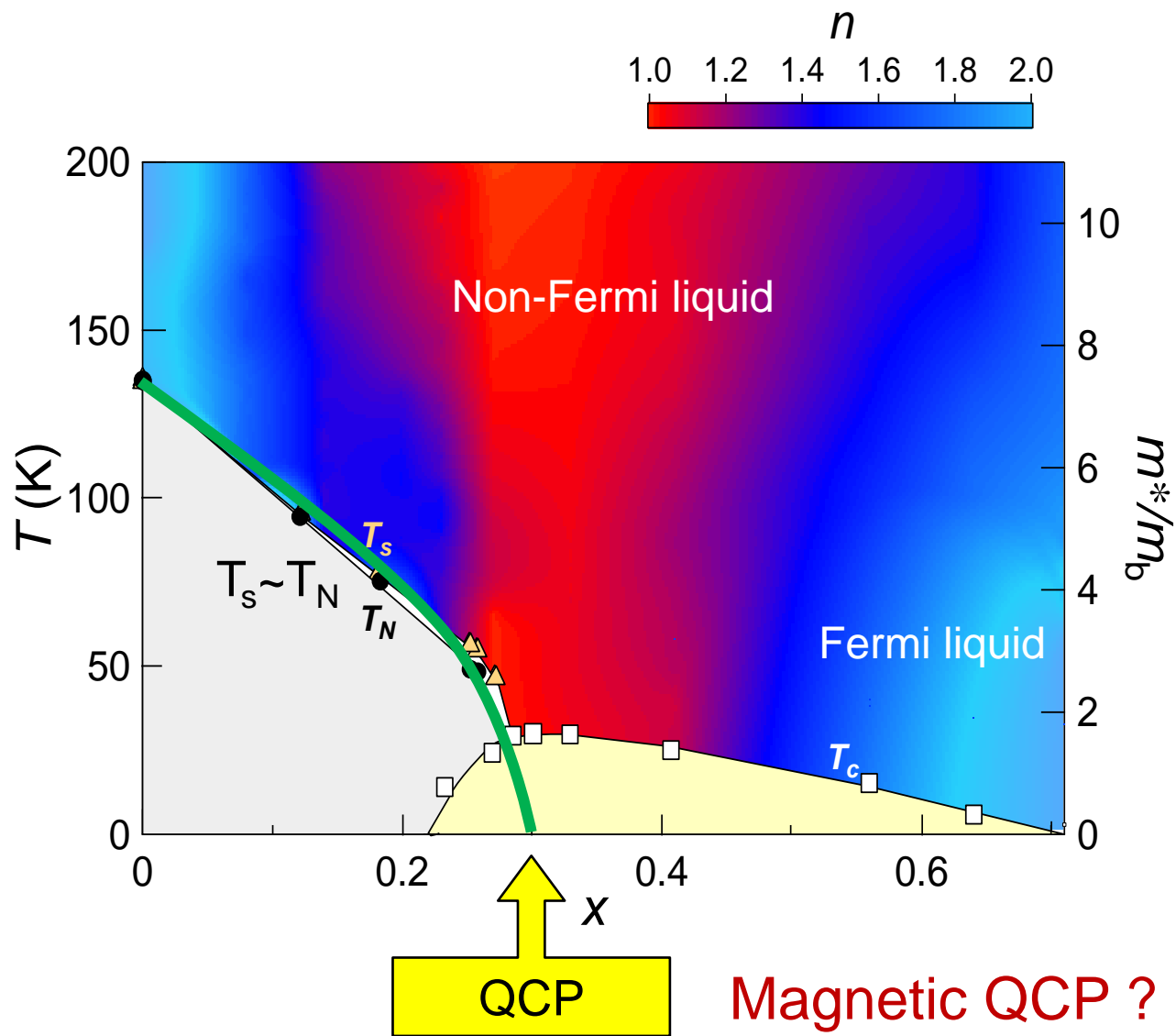
1. The QCP is the origin of the non-Fermi liquid behavior above  $T_c$ .
2. Microscopic coexistence of superconductivity and SDW.
3. The quantum critical fluctuations help to enhance the high- $T_c$  superconductivity.

# Changes in the phase diagram by point disorder

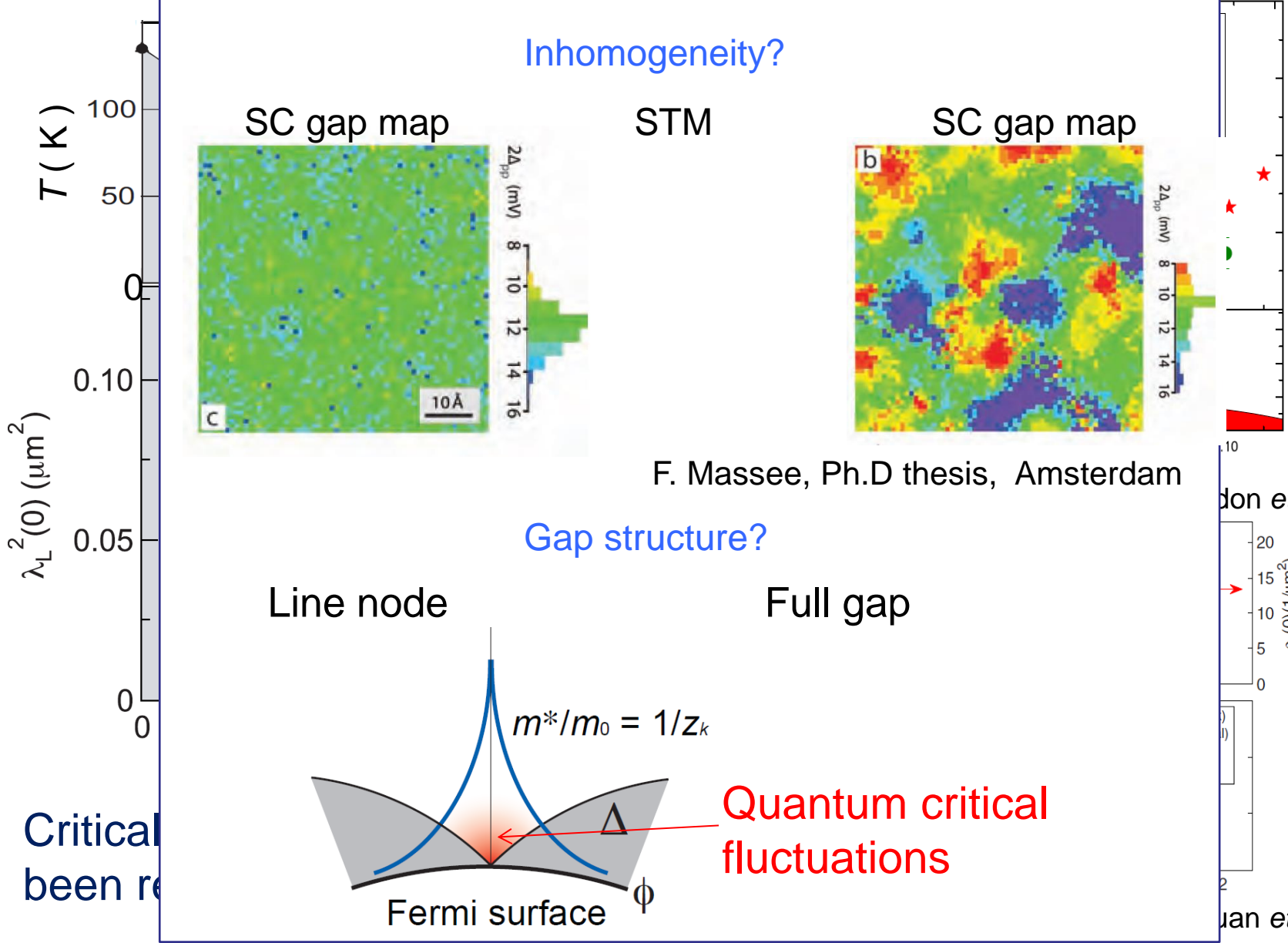
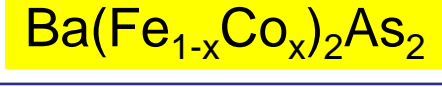
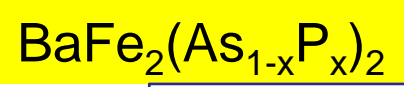


Suppression of SDW moves the QCP toward left, which can consistently explain the shift of SC dome. **A close link between the QCP and SC.**

Quantum critical fluctuations are definitely important for the high- $T_c$  superconductivity



# Doping evolution of the London penetration depth at $T=0$

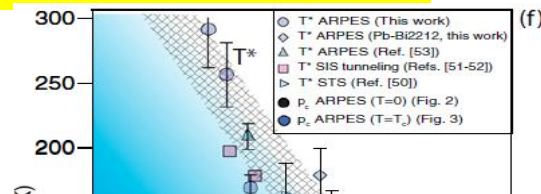


# Doping evolution of the London penetration depth at $T=0$

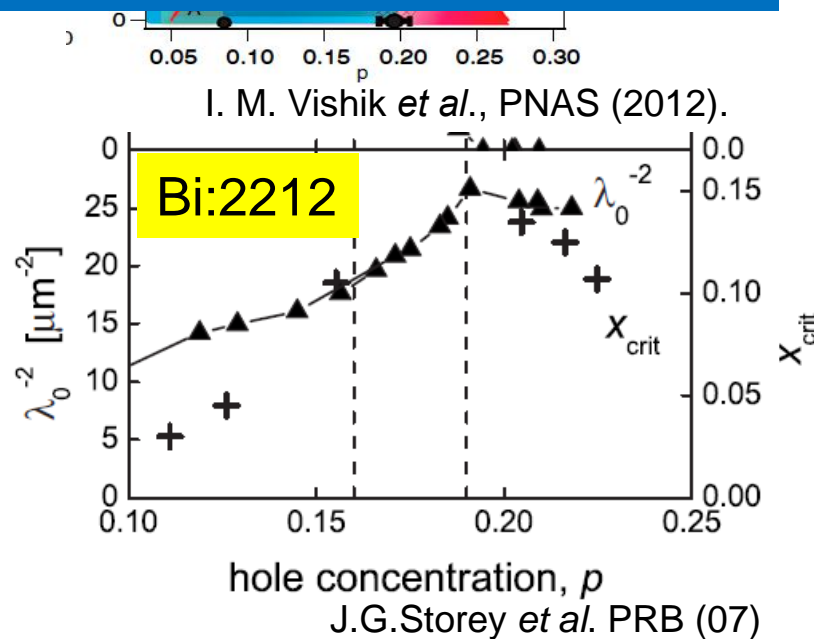
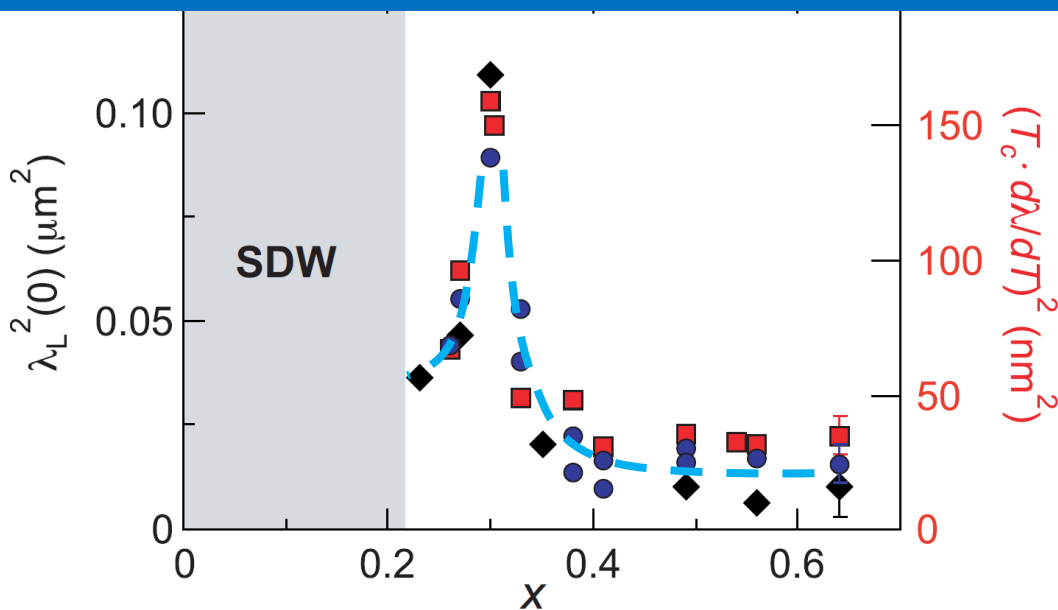
**BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub>**



**High- $T_c$  cuprates**



Superfluid density  $n_s/m^*$  at (putative) QCP  
 Contrasting behavior between pnictides and cuprates



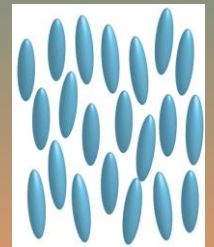
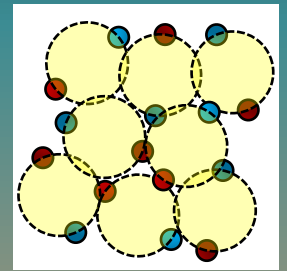
Bi:2212 : broad maximum in  $1/\lambda_L^2(0)$  (enhancement of  $n_s/m^*$ ) at  $p \sim 0.19$

BaFe<sub>2</sub>(As<sub>1-x</sub>P<sub>x</sub>)<sub>2</sub> : sharp peak in  $\lambda_L^2(0)$  (suppression of  $n_s/m^*$ ) at  $x=0.3$

# Physics of iron-based high- $T_c$ superconductors

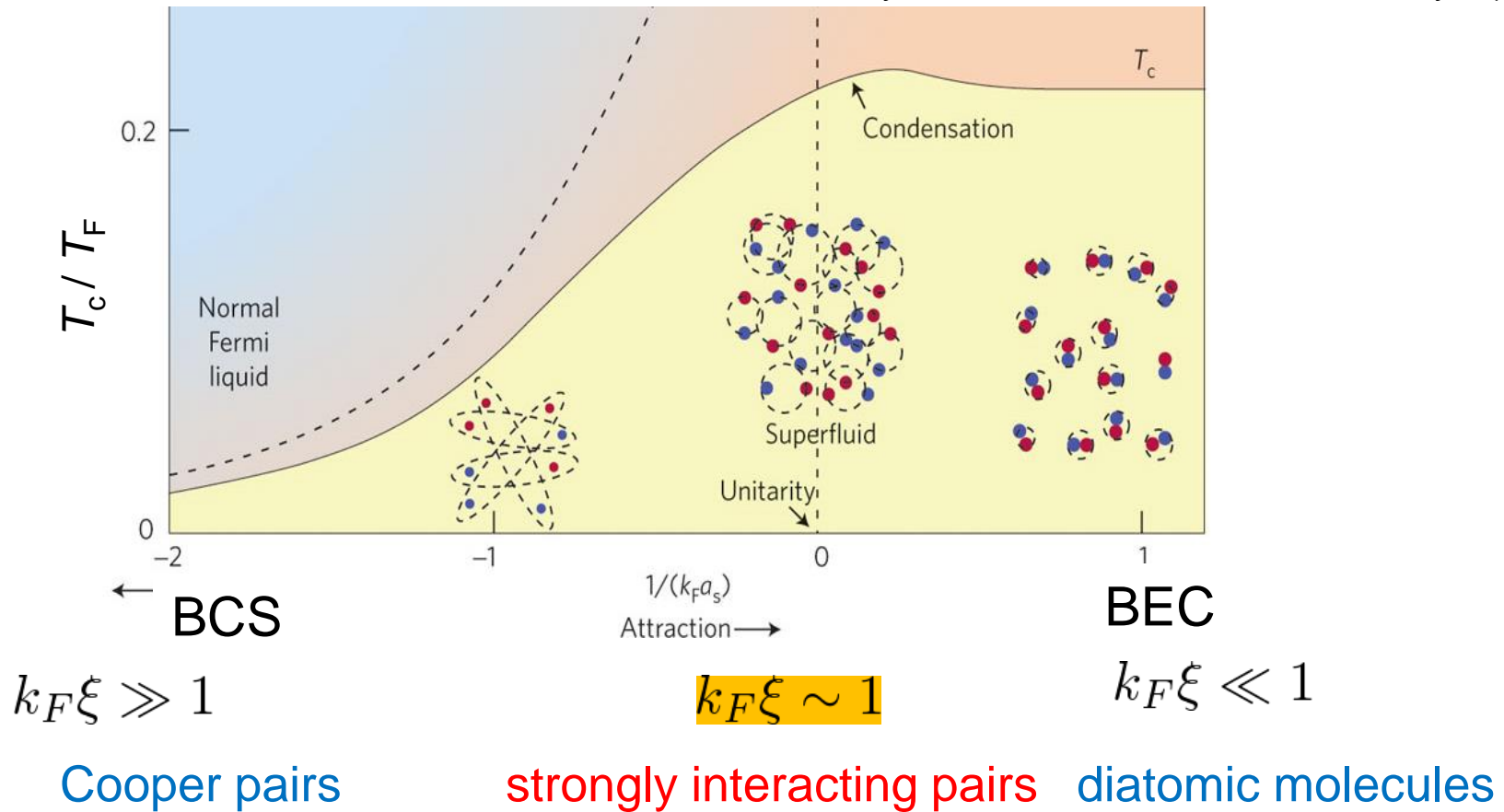
## Selected recent topics

1. Quantum critical point
2. BCS-BEC crossover and a novel high field SC phase
3. Nematicity



# BCS-BEC crossover

M. Randeria, E. Taylor, Annu. Rev. Condens. Matter Phys. (14)



$$\frac{\Delta}{\varepsilon_F} \sim \frac{T_c}{T_F} \sim \frac{1}{\xi k_F}$$

Conventional superconductors

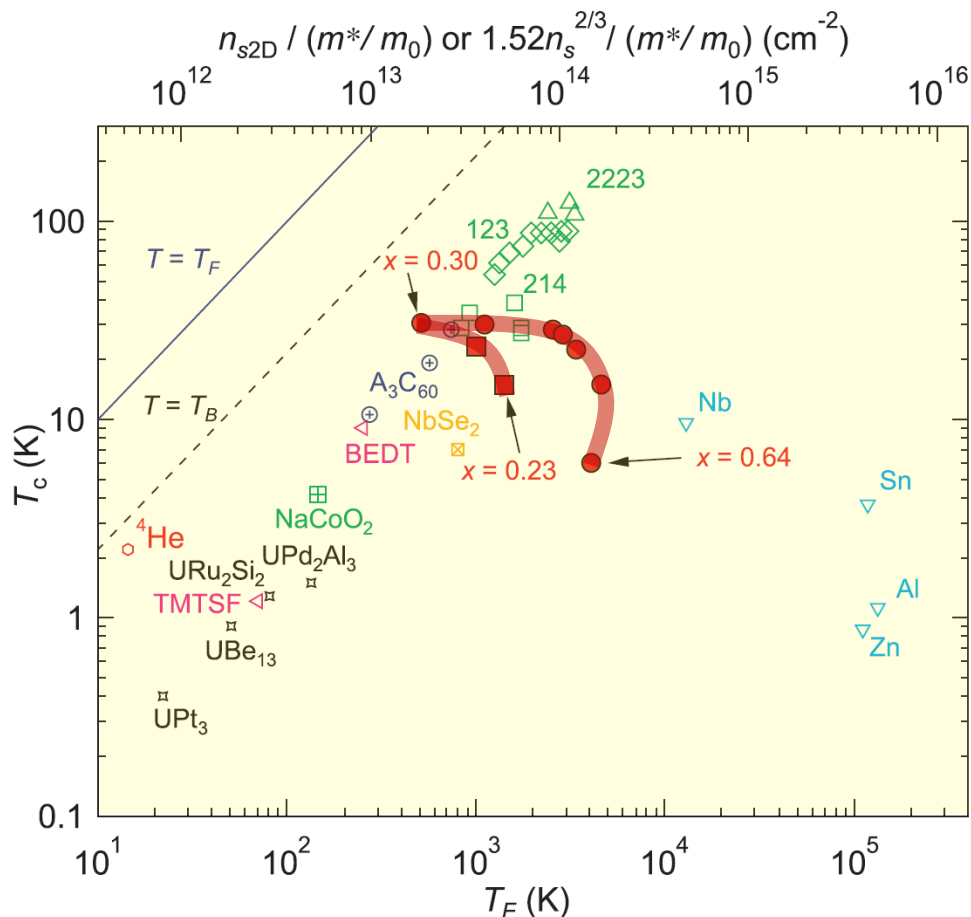
$$\Delta/\varepsilon_F \sim 10^{-4} - 10^{-5}$$

High- $T_c$  cuprates

$$\Delta/\varepsilon_F \sim 10^{-2} - 10^{-3}$$



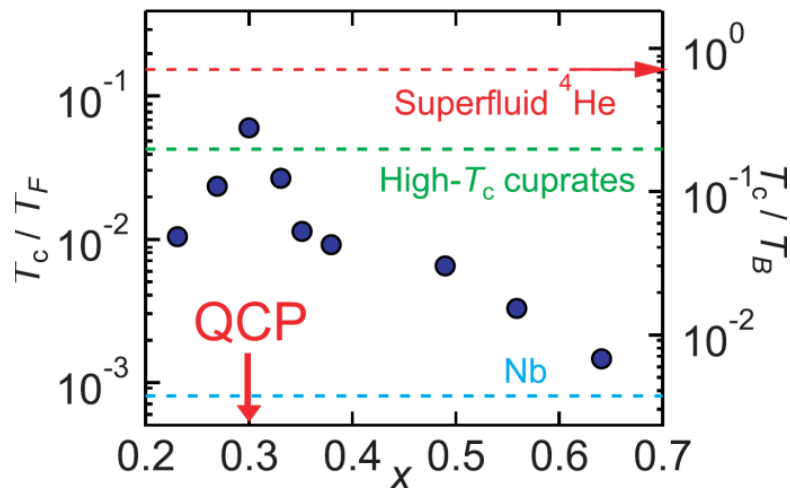
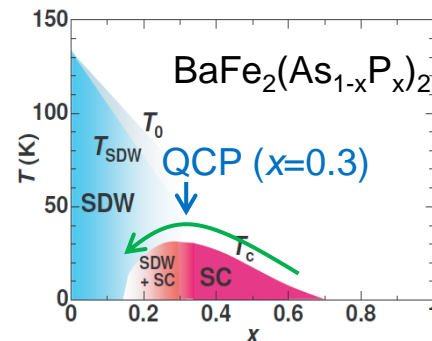
# Doping evolution of the superfluid density



The strongest pairing interaction at the QCP.



High- $T_c$  SC is driven by the QCP

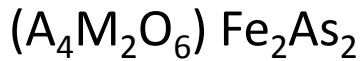
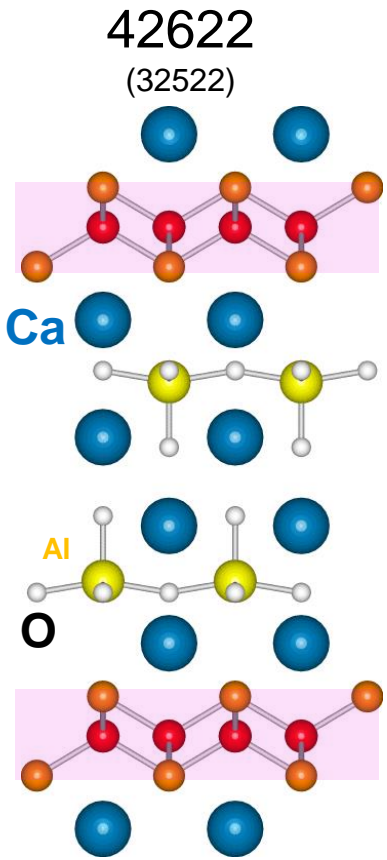
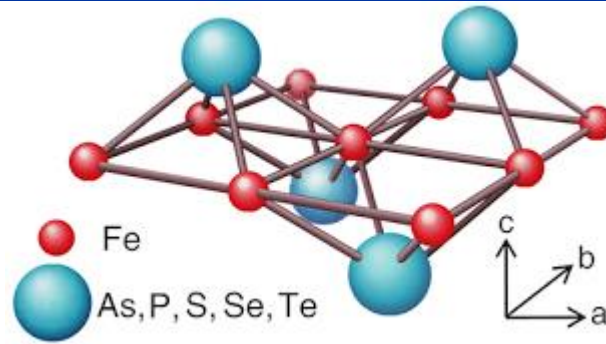


$T_c / T_B = 1/4$  at the QCP  
40% of superfluid  ${}^4\text{He}$



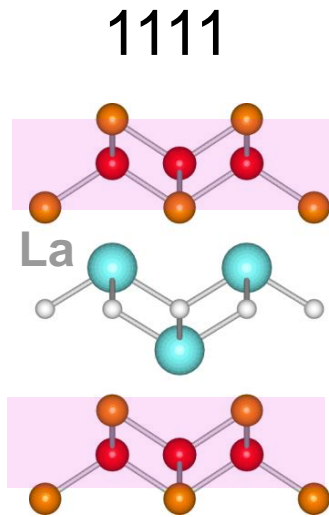
A possible crossover towards the BEC driven by quantum criticality

# Fe-based high- $T_c$ superconductors



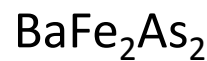
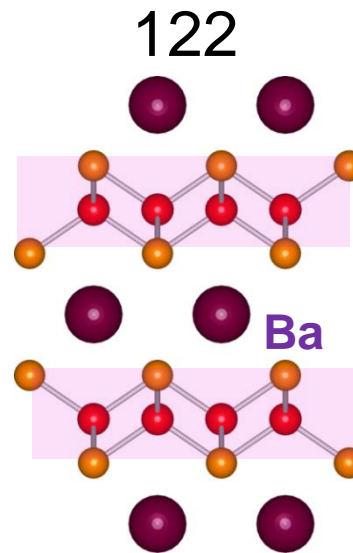
$T_c(\text{max})=47\text{K}$

Zhu et al.(2009)  
Ogino et al. (2009)



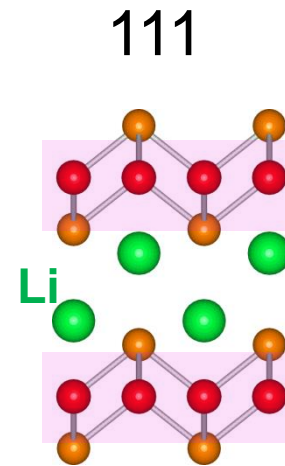
$T_c(\text{max})=55\text{K}$

Y. Kamihara et al.(2008)



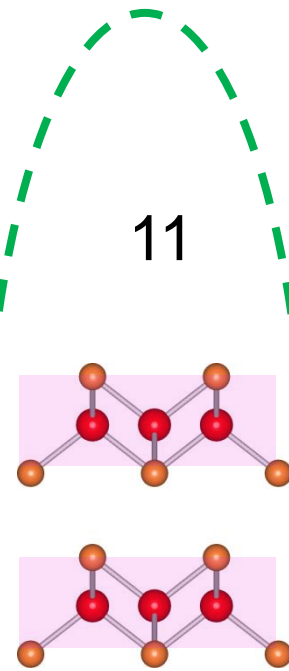
$T_c(\text{max})=38\text{K}$

M. Rotter et al.(2008)



$T_c=18\text{K}$

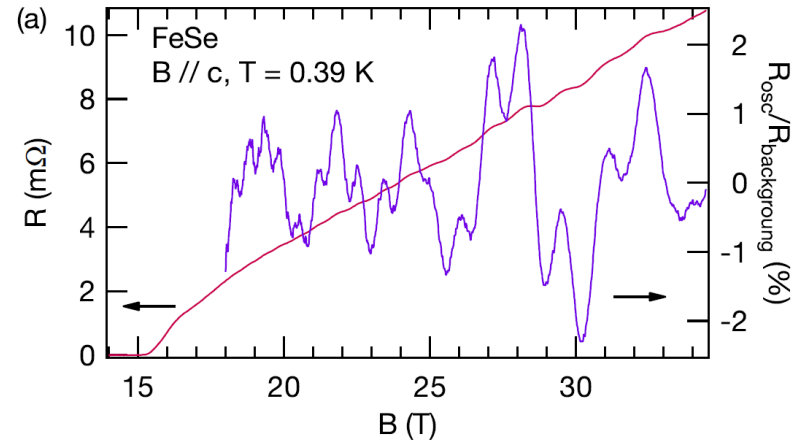
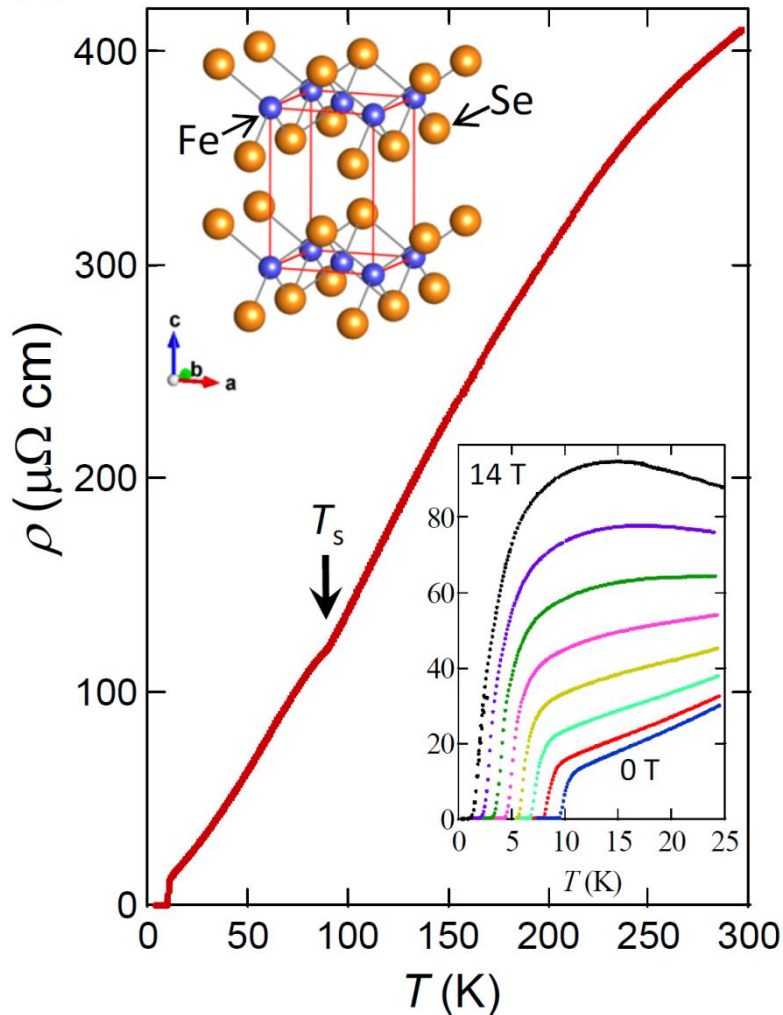
X.C.Wang et al.(2008)



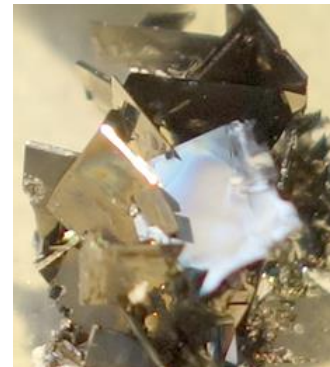
$T_c=9\text{K}$

F.C.Hsu et al.(2008)

# FeSe: A candidate system near BCS-BEC crossover



- ✓ 1:1 stoichiometry within experimental error  
A. Böhrer et al. PRB (2013).
- ✓ Small residual resistivity & large RRR
- ✓ Large magnetoresistance, SdH oscillations

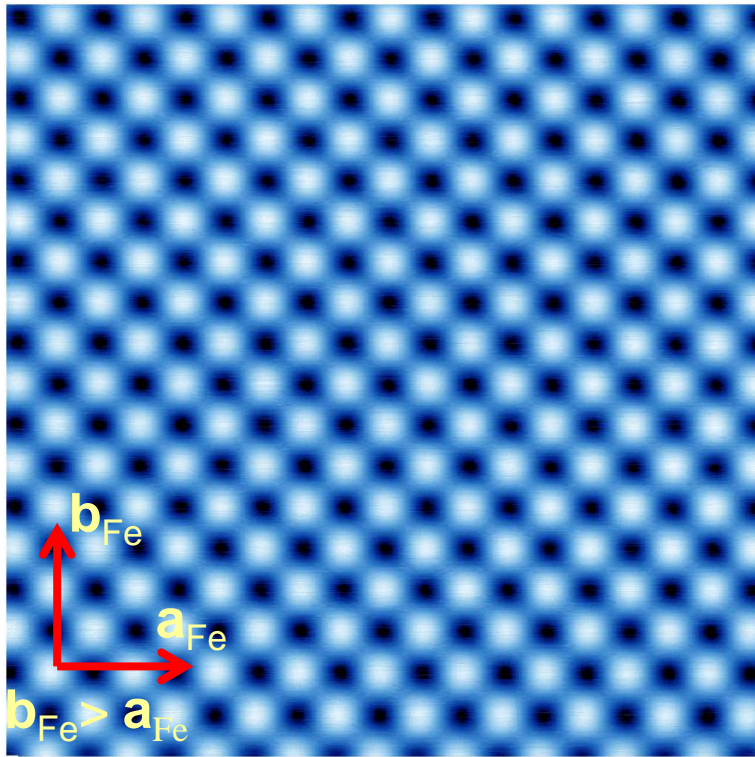


# High quality single crystals of FeSe

## STM topographic image of FeSe

+95 mV/100 pA

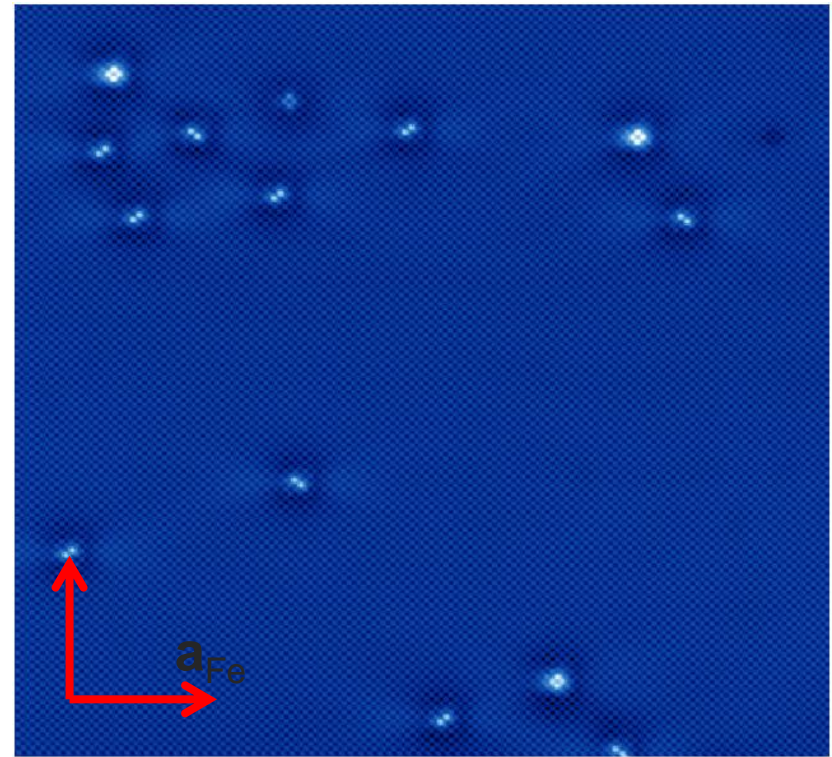
$T \sim 0.4$  K



5 nm

+95 mV/100 pA

$T \sim 1.5$  K



45 nm

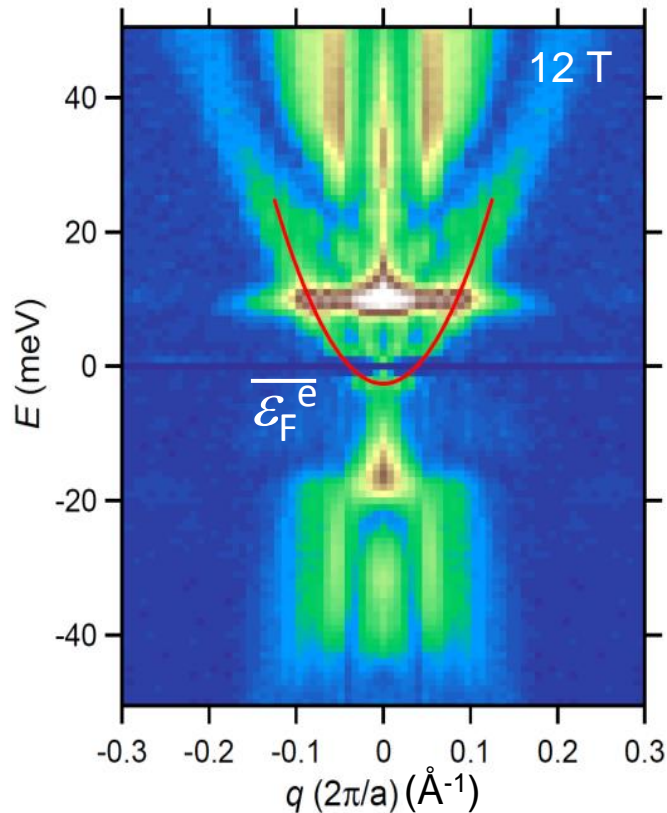
- ✓ Surface Se lattice
- ✓ Low defect density ( $< 1/5,000$  unit cells) **Extremely clean Xtals**



# Extremely small Fermi energy : QPI

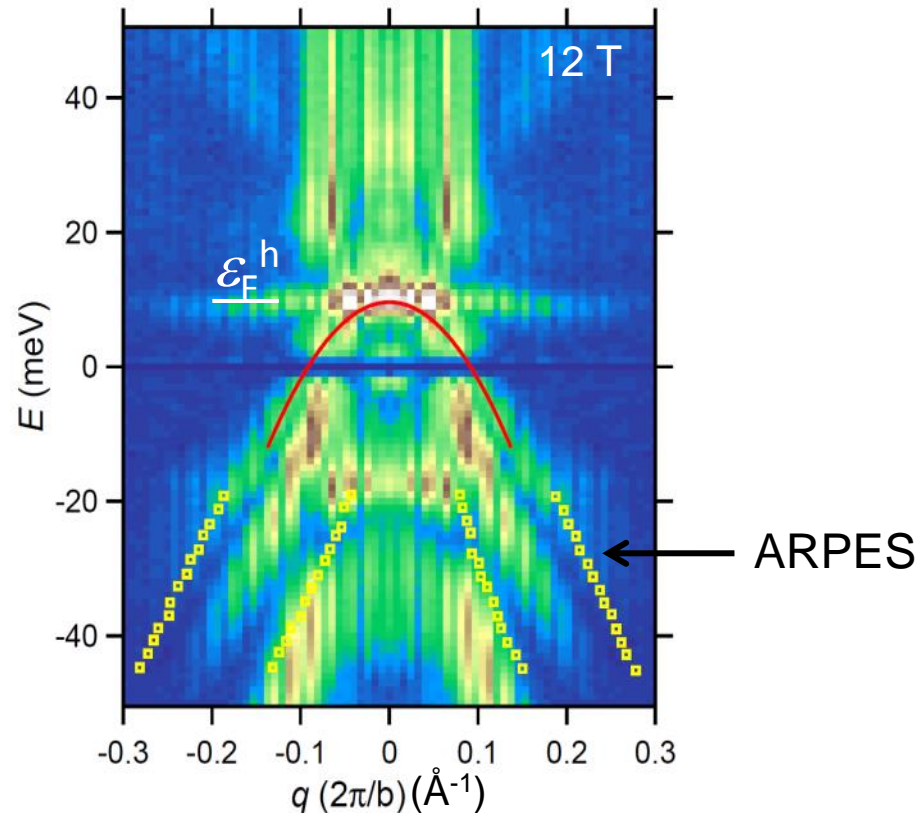
Band dispersion curves obtained by QPI (Quasi Particle Interference) of STM

S. Kasahara *et al.*,



Electron band

$$\varepsilon_F \sim 3 \text{ meV}$$

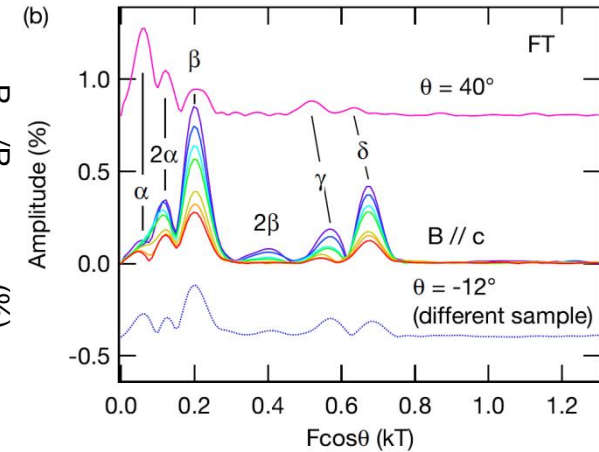
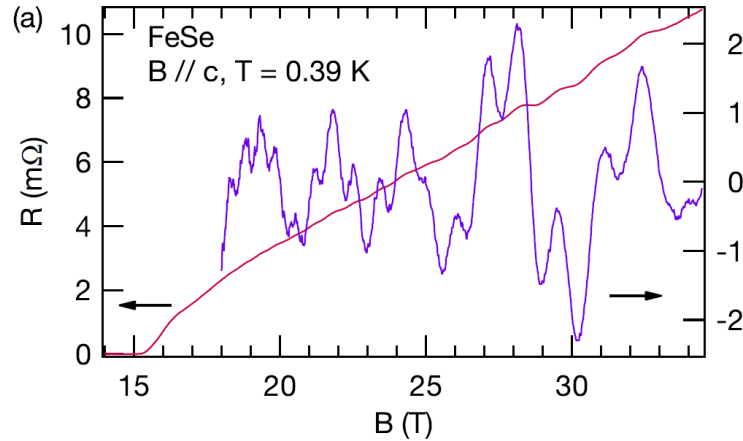
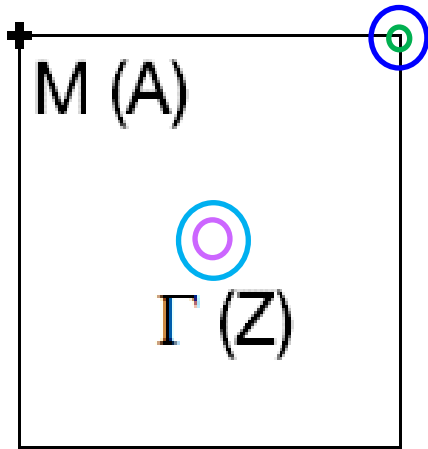


Hole band

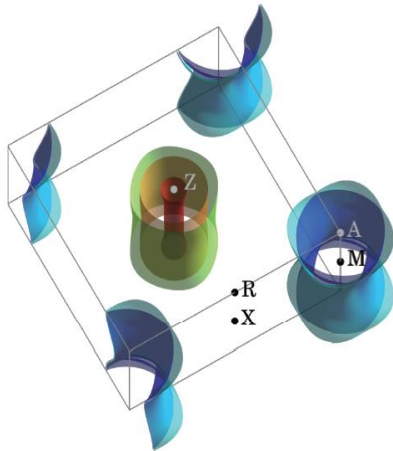
$$\varepsilon_F \sim 10 \text{ meV}$$

# Extremely small Fermi energy: Quantum oscillations

T. Terashima et al., arXiv.1405.7749.



Only two Fermi surface sheets



LDA

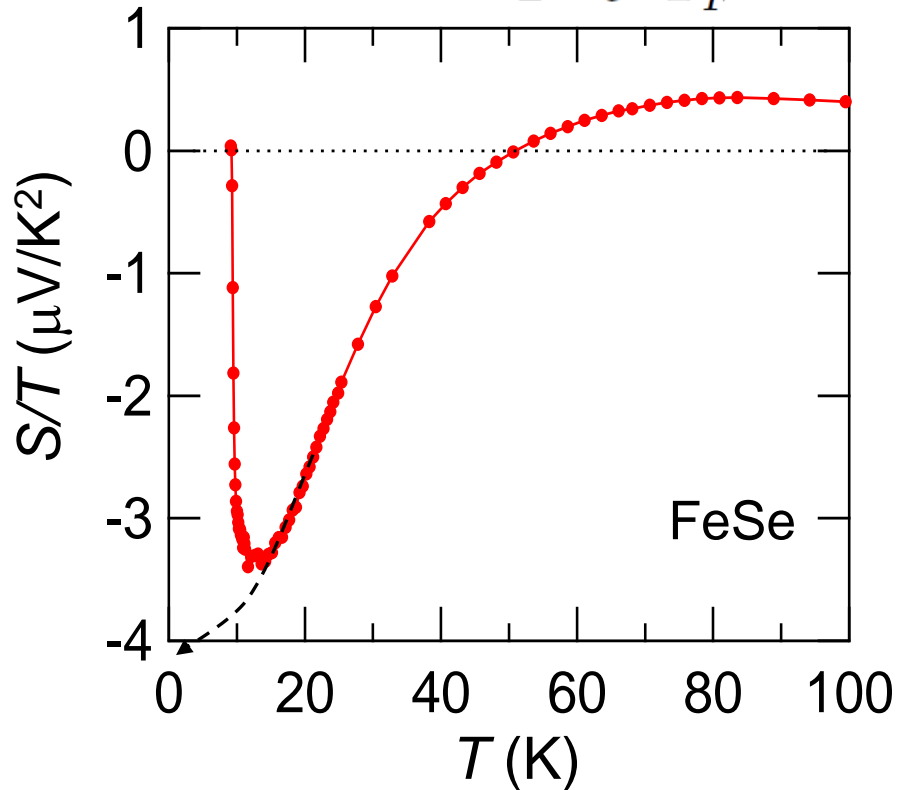
Branch	$F$ (kT)	$m^*/m_e$	$A$ (%BZ)	$k_F$ ( $\text{\AA}^{-1}$ )	$E_F$ (meV)
$\alpha^a$	0.06	1.9(2)	0.20	0.043	3.5
$\beta$	0.20	4.5(5)	0.69	0.078	5.1
$\gamma$	0.57	7.0(7)	2.0	0.13	9.4
$\delta$	0.67	4.8(5)	2.3	0.14	16

✓ Extremely small Fermi surface and Fermi energy.

# Extremely small Fermi energy

Seebeck coefficient

$$S/T = \pm \frac{\pi^2 k_B}{2} \frac{1}{e} \frac{1}{T_F}$$

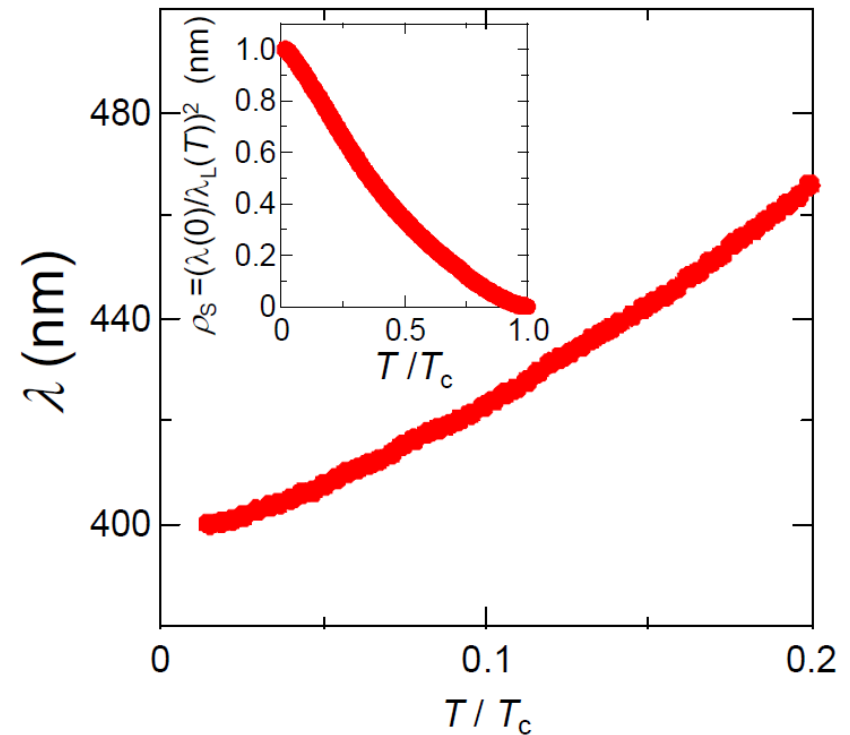


$T_F \sim 100$  K

(The upper limit for the electron band)

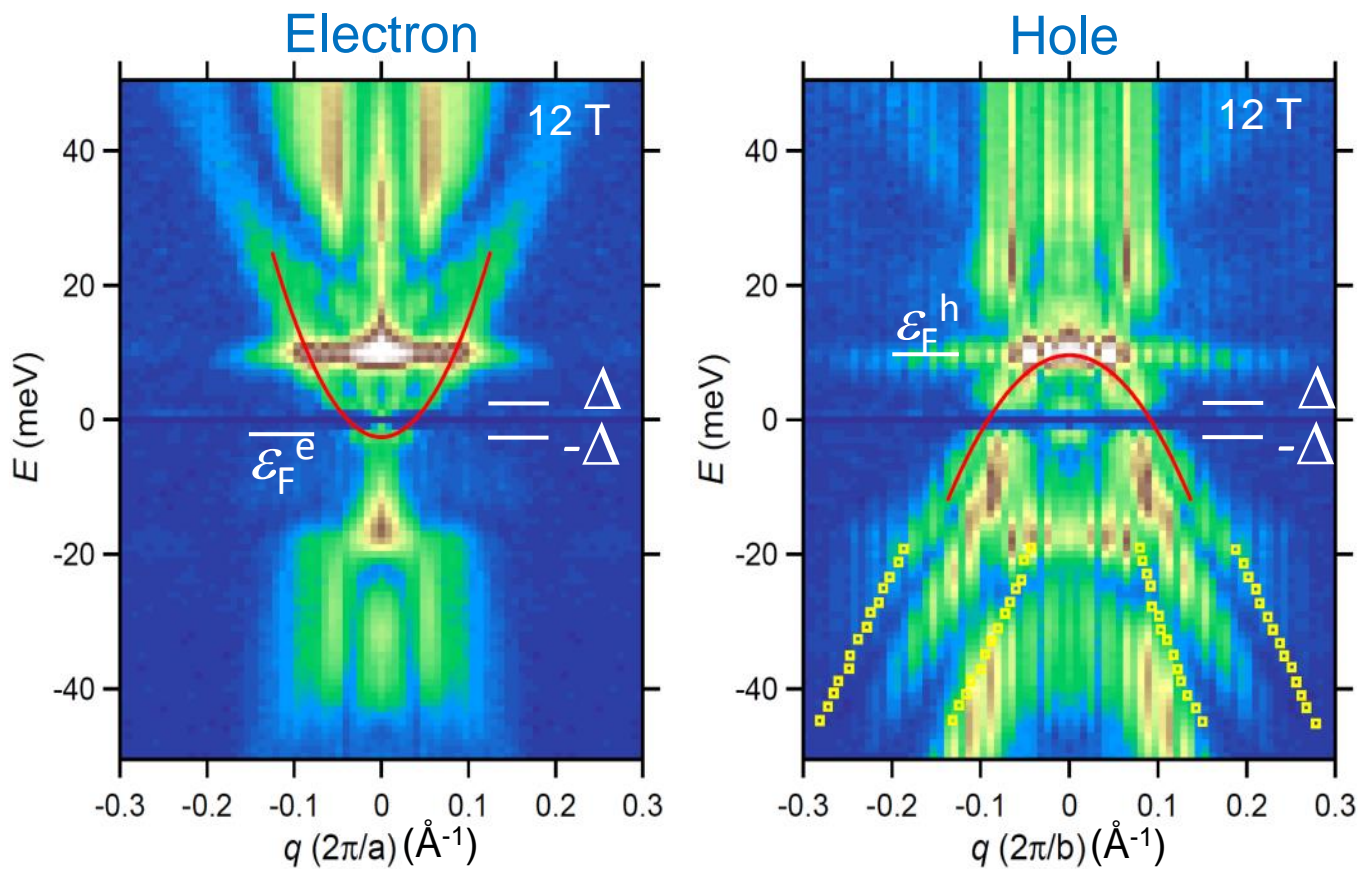
Penetration depth

$$\varepsilon_F = \frac{\pi \hbar^2 d}{\mu_0 e^2} \lambda_L^{-2}(0)$$



$T_F \sim 100$  K

# A possible BCS-BEC crossover regime, $\varepsilon_F \sim \Delta$



$$\Delta \sim 2.5 \text{ meV}$$

Conventional superconductors

$$\Delta/\varepsilon_F \sim 10^{-4} - 10^{-5}$$

High- $T_c$  cuprates

$$\Delta/\varepsilon_F \sim 10^{-2} - 10^{-3}$$

$$\Delta/\varepsilon_F^e \sim 1$$

$$\Delta/\varepsilon_F^h \sim 0.3$$

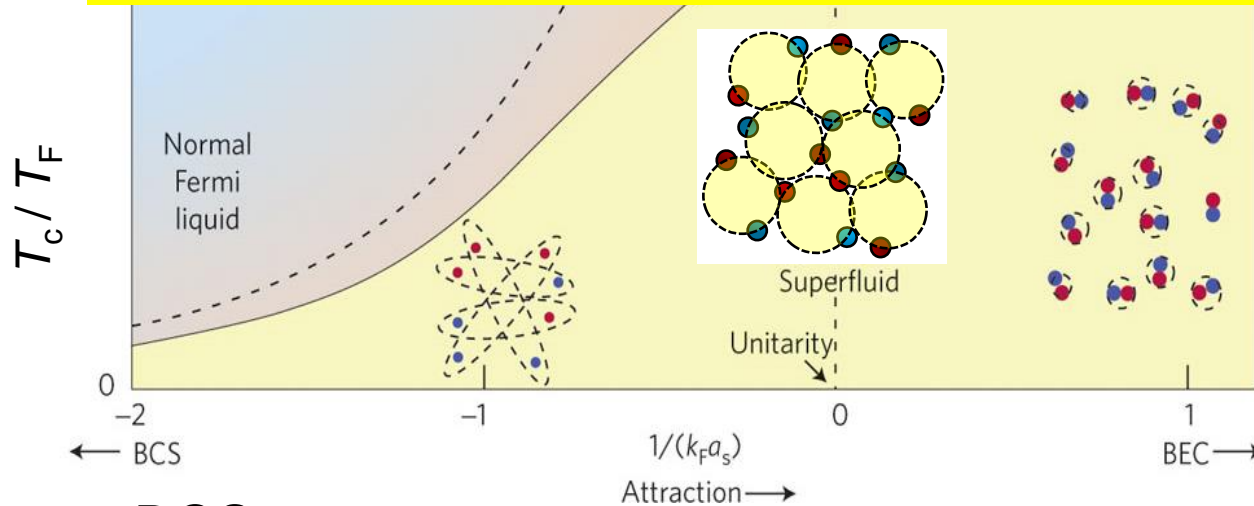
Never realized in any other superconductors!

cf. Cold atoms



# BCS-BEC crossover

FeSe is in the BCS-BEC crossover regime  
Close to unitary Fermi gas?



M. Randeria, E. Taylor,  
Annu. Rev. Condens.  
Matter Phys. (14)

BCS

$$k_F \xi \gg 1$$

Cooper pairs

$$k_F \xi \sim 1$$

strongly interacting pairs

BEC

$$k_F \xi \ll 1$$

diatomic molecules

$$\frac{\Delta}{\varepsilon_F} \sim \frac{T_c}{T_F} \sim \frac{1}{\xi k_F}$$

FeSe

$$\Delta/\varepsilon_F^e \sim 1$$

$$\Delta/\varepsilon_F^h \sim 0.3$$

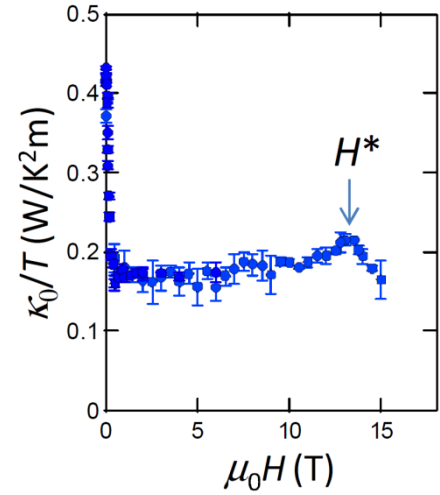
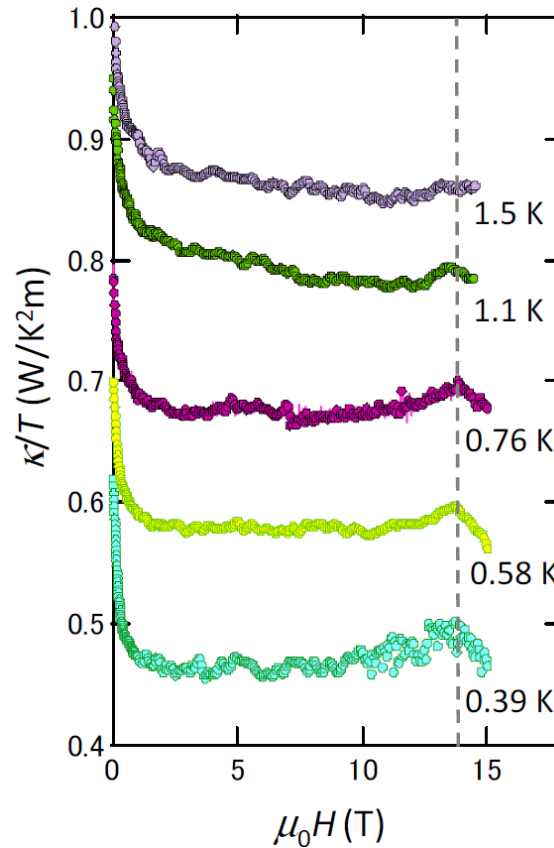
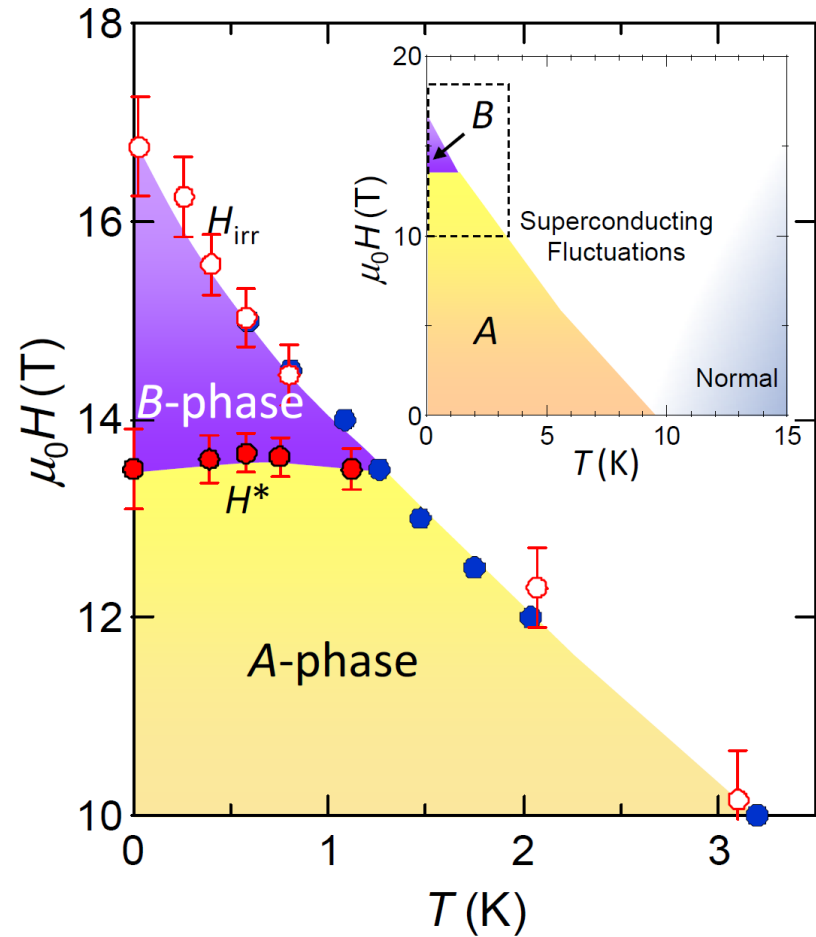
Conventional superconductors

$$\Delta/\varepsilon_F \sim 10^{-4} - 10^{-5}$$

High- $T_c$  cuprates

$$\Delta/\varepsilon_F \sim 10^{-2} - 10^{-3}$$

# A new high-field superconducting phase

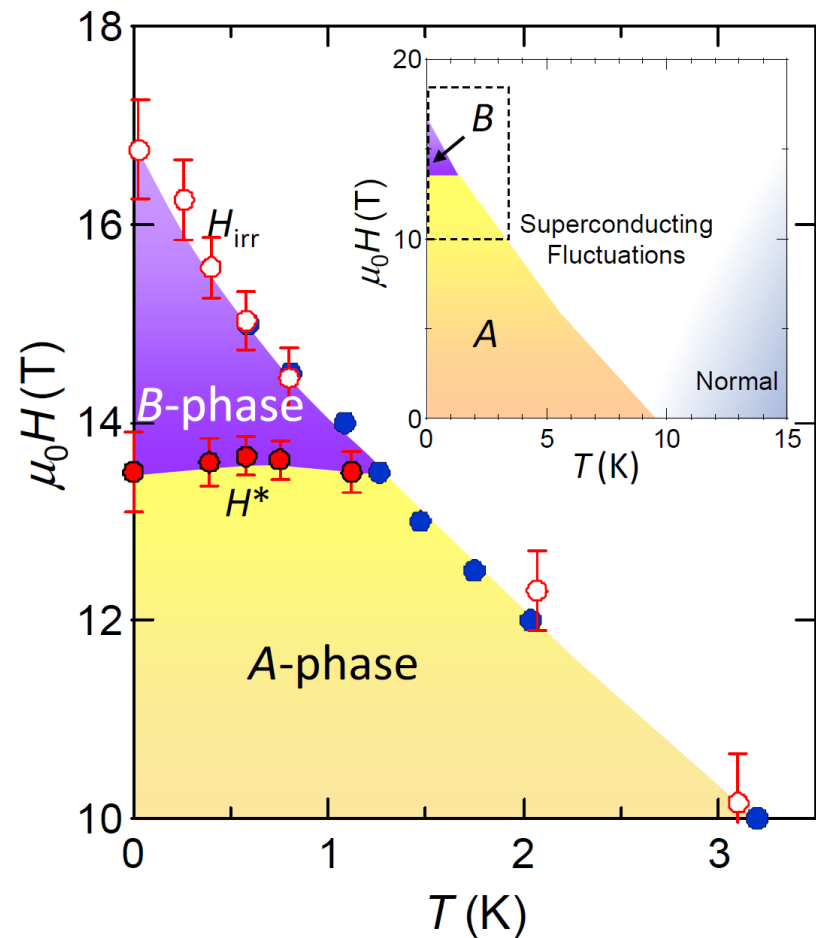


$$\varepsilon_F \sim \Delta \sim \mu_B H$$

Fermi ~ Gap ~ Zeeman

B-phase is induced by strong spin imbalance of the unitary Fermi gas

# A new high-field superconducting phase

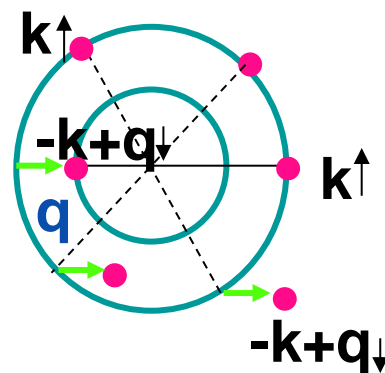


$$\varepsilon_F \sim \Delta \sim \mu_B H$$

Fermi ~ Gap ~ Zeeman

Highly spin-polarized phase

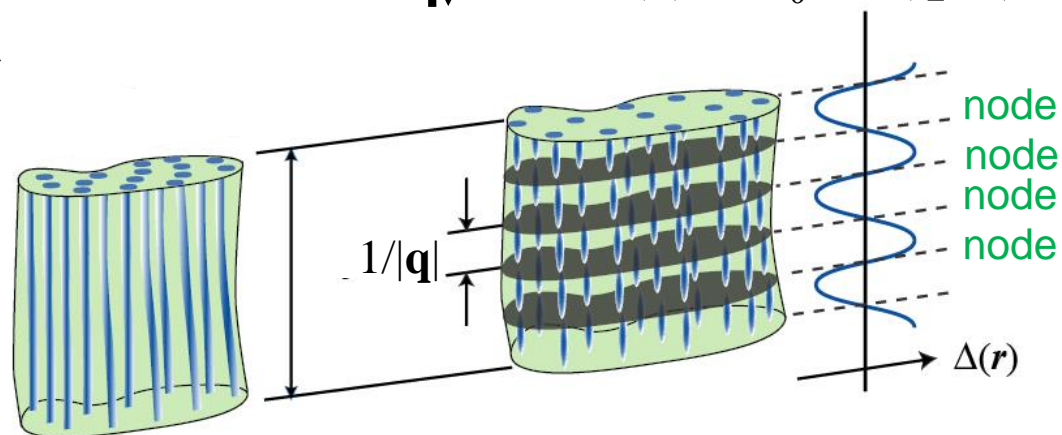
FFLO state ?



$$(\mathbf{k}\uparrow, -\mathbf{k} + \mathbf{q}\downarrow)$$

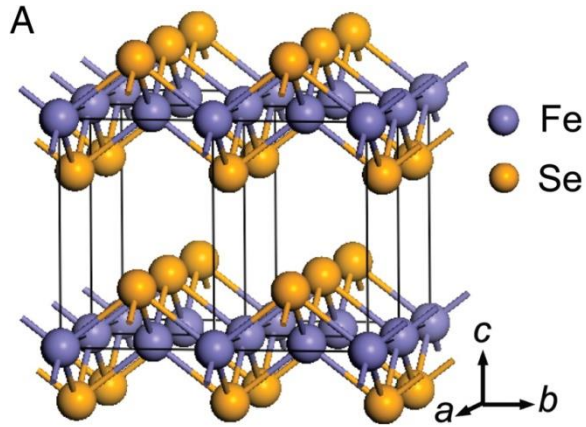
*pairing between Zeeman split parts of the Fermi surface*

$$\Delta(\mathbf{r}) = \Delta_0 \cos(\mathbf{q} \cdot \mathbf{r})$$

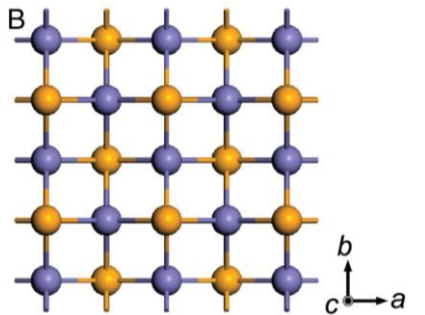


High- $T_c$  superconductivity  
in single layer FeSe

# High- $T_c$ superconductivity in FeSe

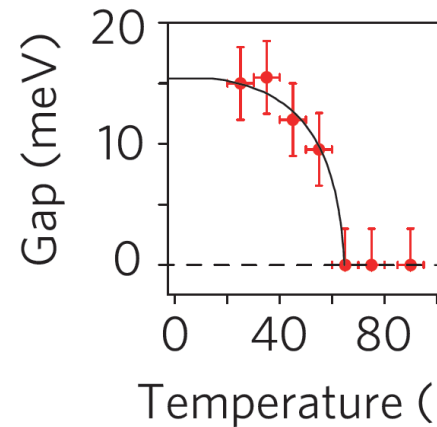
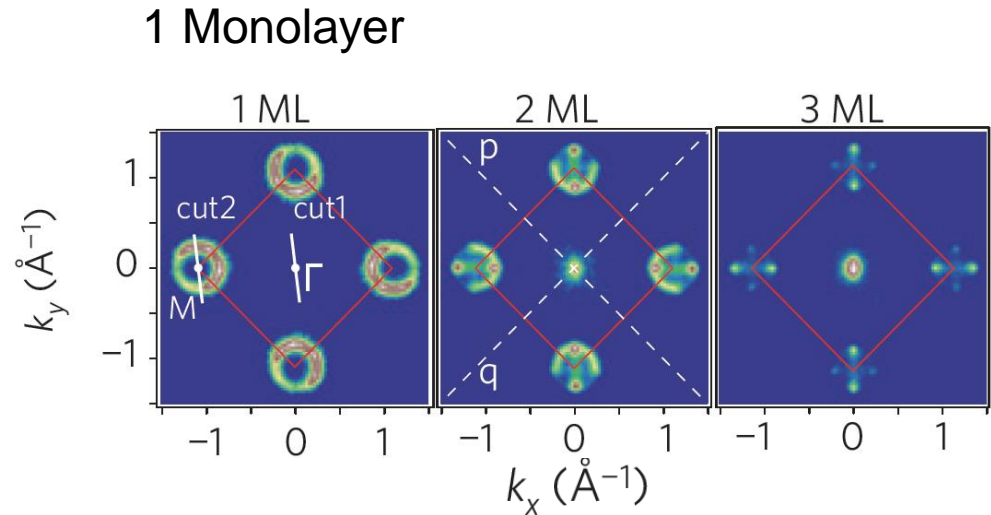


F.-C. Hsu *et al.*,  
PNAS **105**, 14262 (2008).



FeSe/SrTiO<sub>3</sub>

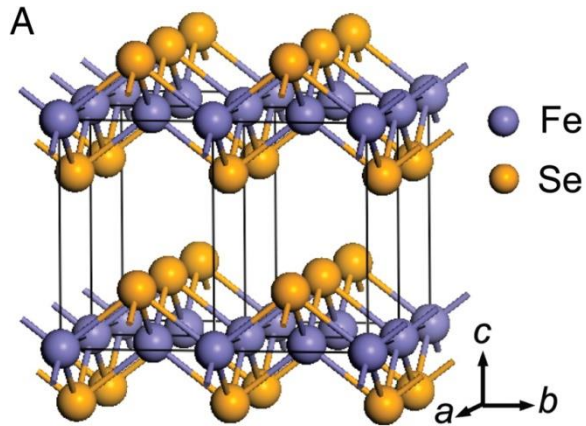
ARPES



$T_c = 65\text{K}??$

S.Tan *et al.* Nature Mat. 12, 634 (2013).

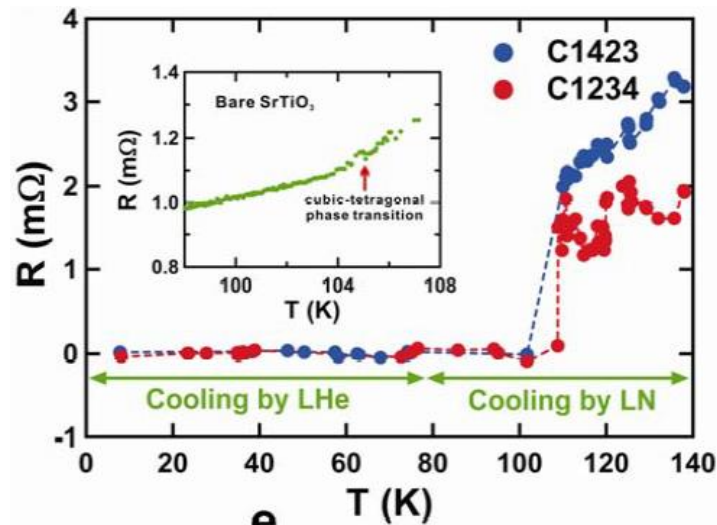
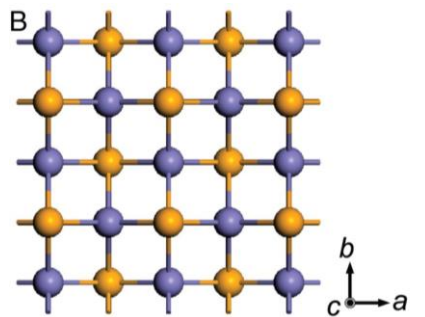
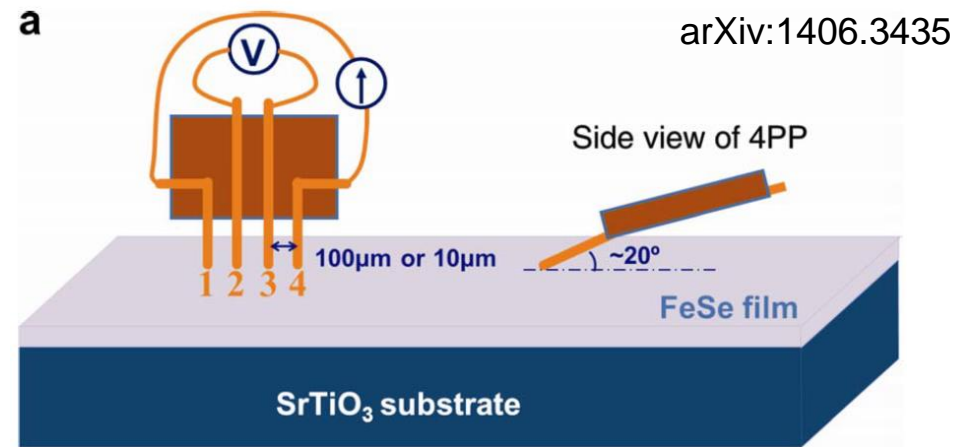
# High- $T_c$ superconductivity in FeSe



F.-C. Hsu *et al.*,  
PNAS **105**, 14262 (2008).

## Superconductivity in single-layer films of FeSe with a transition temperature above 100 K

Jian-Feng Ge<sup>1</sup>, Zhi-Long Liu<sup>1</sup>, Canhua Liu<sup>1\*</sup>, Chun-Lei Gao<sup>1</sup>, Dong Qian<sup>1</sup>, Qi-Kun Xue<sup>2\*</sup>, Ying Liu<sup>1,3</sup>, Jin-Feng Jia<sup>1\*</sup>

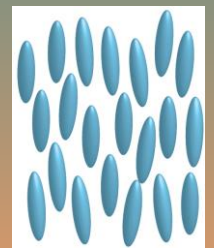
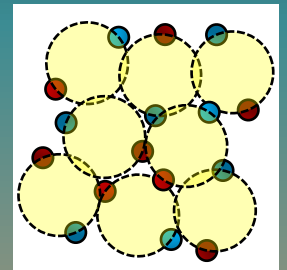


$T_c = 110$  K????

# Physics of iron-based high- $T_c$ superconductors

## Selected recent topics

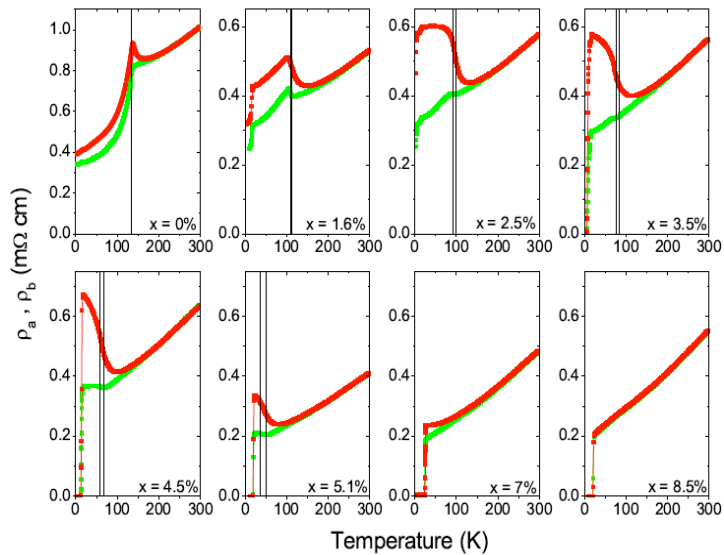
1. Quantum critical point
2. BCS-BEC crossover and a novel high field SC phase
3. Nematicity



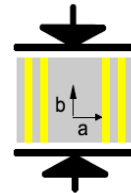


# Experiments suggesting in-plane anisotropy at $T > T_s$

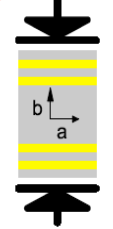
★ **Resistivity** J. Chu *et al.* Science (10). **Detwinned by uniaxial pressure**



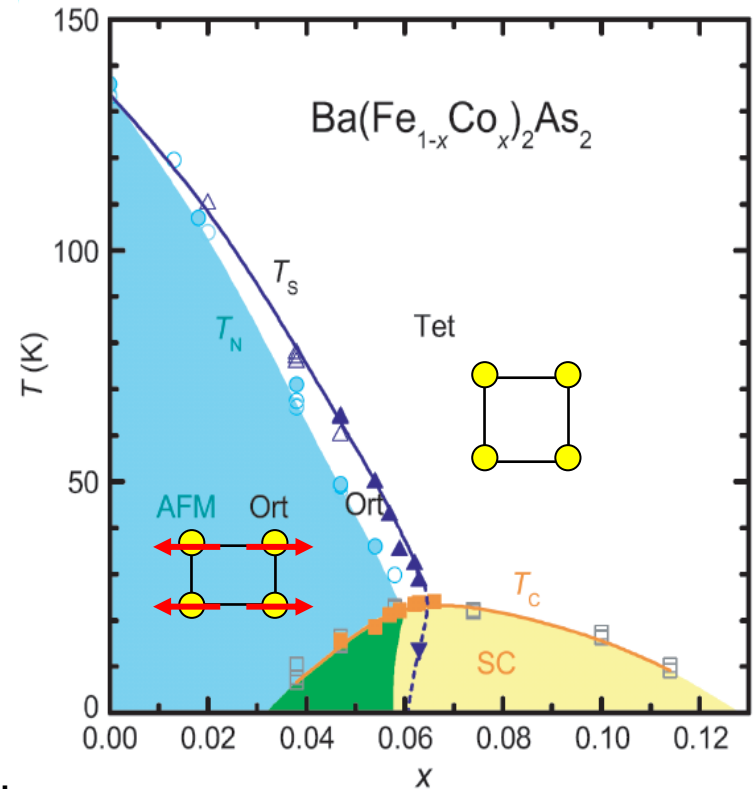
$\rho_a$  Configuration



$\rho_b$  Configuration



$\rho_b > \rho_a$  above  $T_s$



★ **Optical Conductivity**

A. Dusza *et al.*, EPL (11).

★ **Neutron**

M. Nakajima *et al.*, PNAS (11).

★ **X-Ray**

J. Zhao *et al.*, Nature Phys. (09).

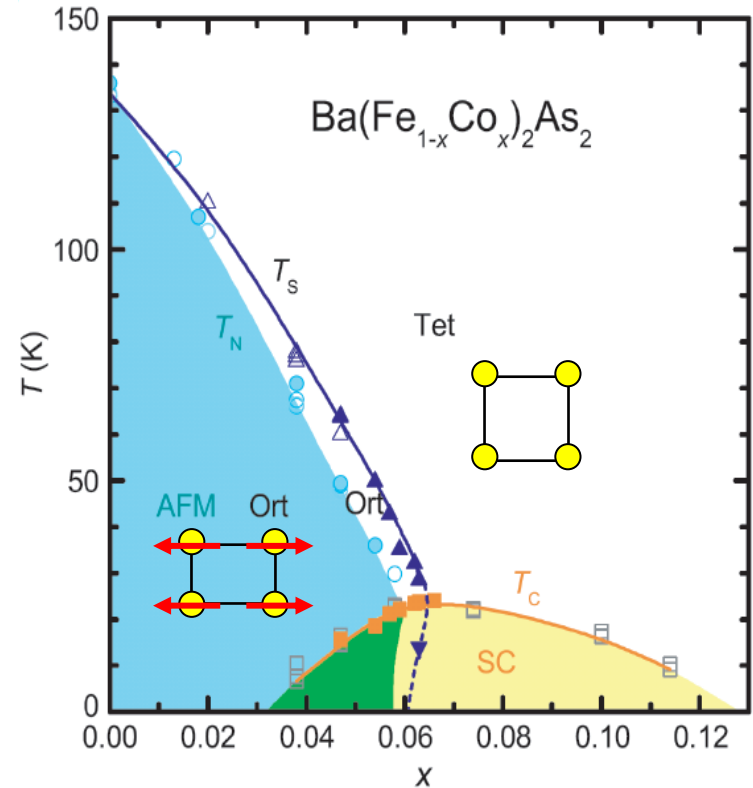
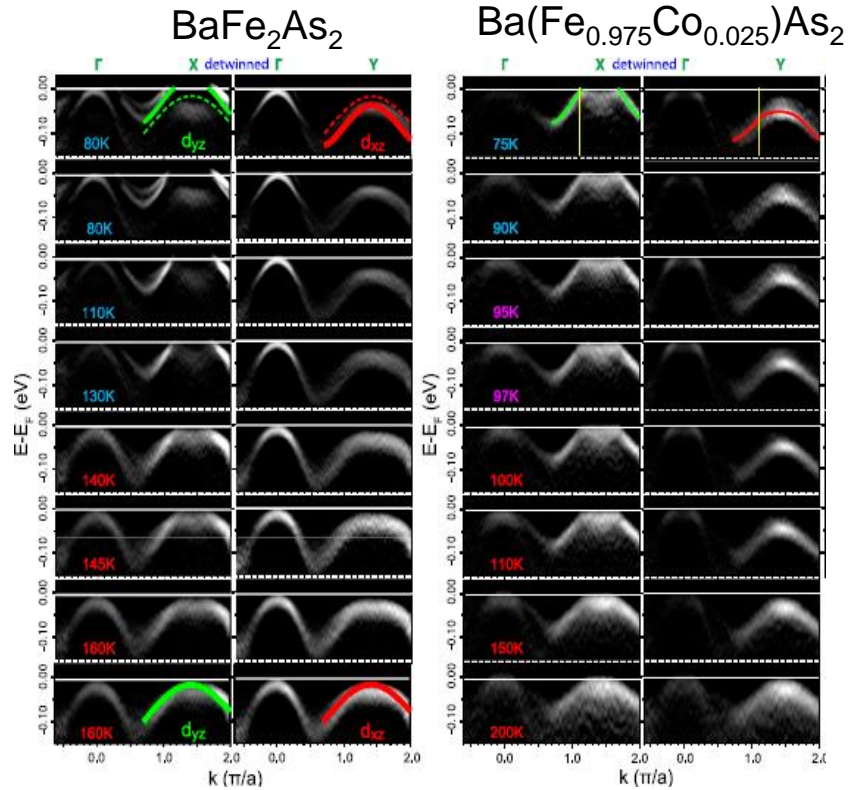
L. W. Harriger *et al.* PRB (11).

E.C. Blomberg *et al.* PRB (12)

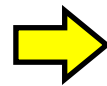
# Experiments suggesting in-plane anisotropy at $T > T_s$

## Detwinned by uniaxial pressure

★ ARPES M. Yi *et al.*, PNAS (11).



Nematicity appears above  $T_s$  in crystals under uniaxial strain.



Experiments using thermodynamic probe with no uniaxial stress.

# Microcantilever torque magnetometry

## Micro-chip cantilever

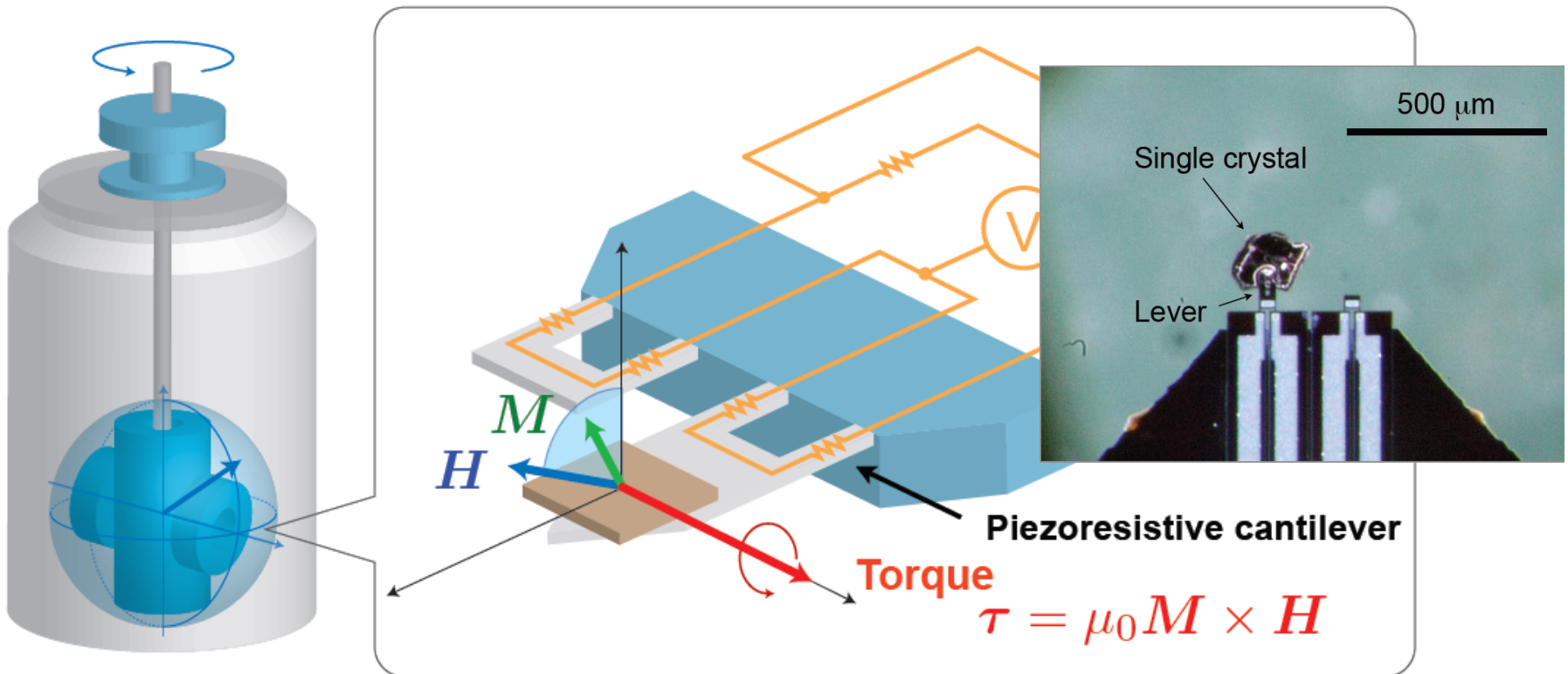
Very high sensitivity

torque  $5 \times 10^{-12}$  e.m.u.  
SQUID  $10^{-8}$  e.m.u.

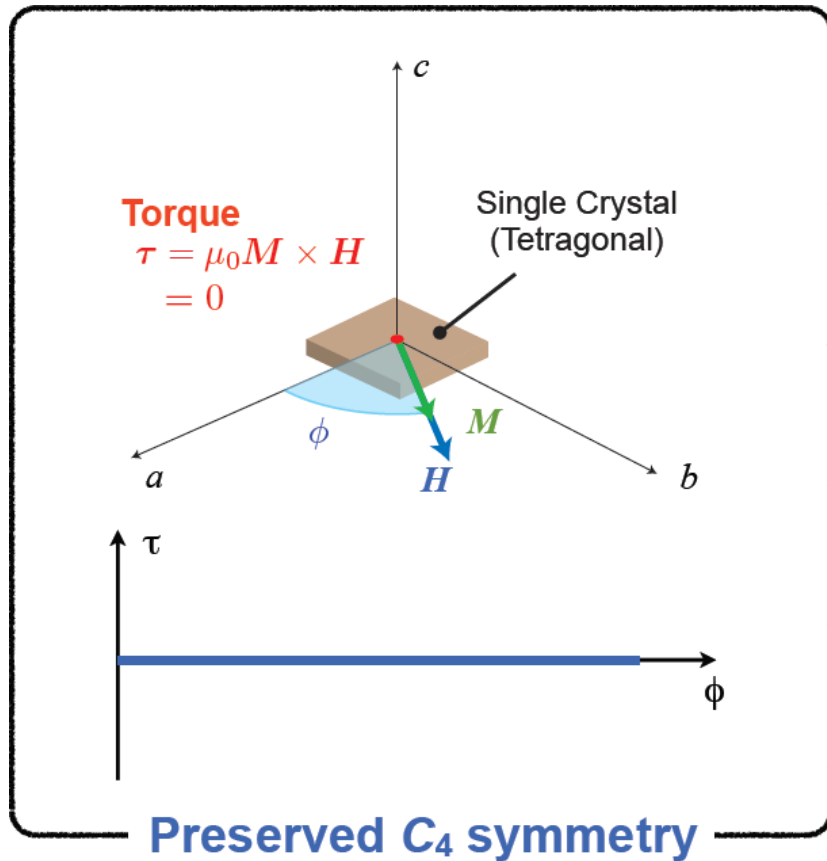
at  $\mu_0 H = 4$  T

## Vector magnet and mechanical rotator system

We can rotate  $H$  continuously within the  $ab$  plane with a misalignment less than 0.01 deg.



# What the magnetic torque tells us



$$\text{Torque} \quad \tau = \mu_0 \mathbf{M} \times \mathbf{H}$$

Angle derivative of the free energy

$$\tau(\phi) = -\frac{\partial F_{eq}(\mathbf{H})}{\partial \phi}$$

Direct probe of the  
**magnetic anisotropy**

$$\tau = \frac{1}{2} \mu_0 H^2 V [(\chi_{aa} - \chi_{bb}) \sin 2\phi - 2\chi_{ab} \cos 2\phi]$$

$$\chi_{aa} = \chi_{bb}, \quad \chi_{ab} = 0 \quad \rightarrow \quad \tau = 0$$

# What the magnetic torque tells us

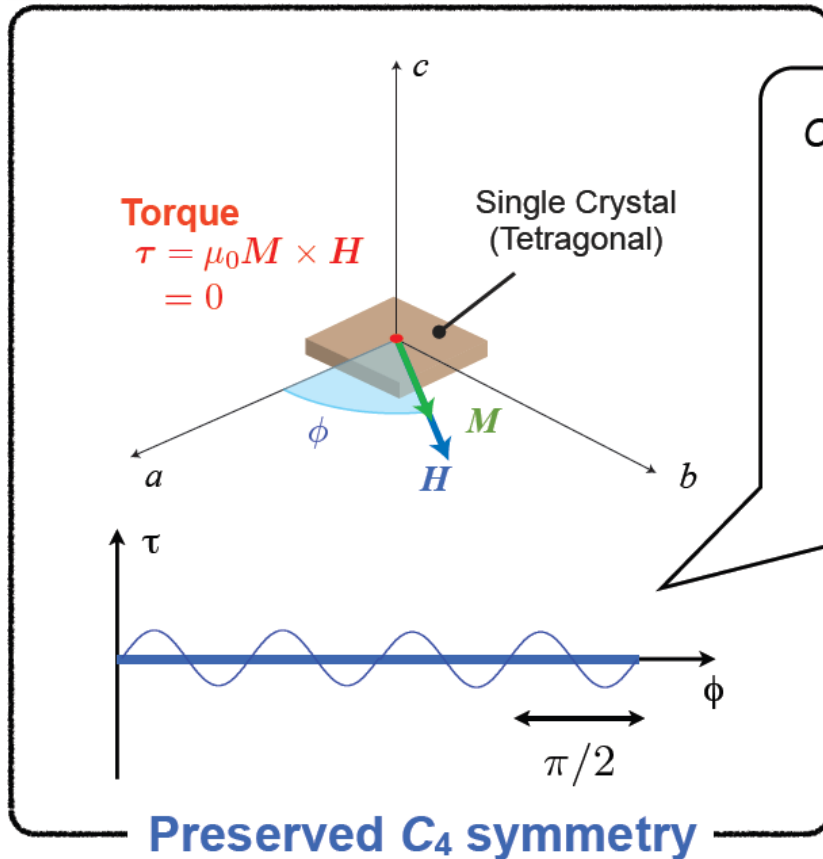
## Nonlinear susceptibility

$C_4$  symmetry in the  $ab$  plane: 4-fold oscillation

$$M_i = \chi_{ij} H_j + \chi_{ijkl}^{(3)} H_j H_k H_l + \dots$$

$\tau = 0$        $\tau \propto \sin 4\phi$

**No 2-fold oscillation**



$$\tau_{2\phi} = \frac{1}{2} \mu_0 H^2 V [(\chi_{aa} - \chi_{bb}) \sin 2\phi - 2\chi_{ab} \cos 2\phi]$$

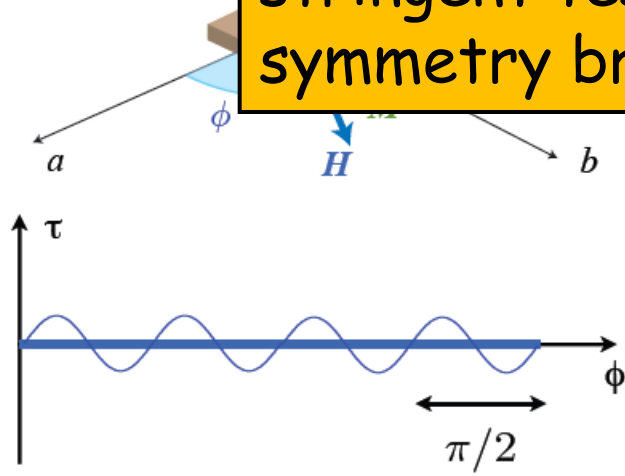
$$\chi_{aa} = \chi_{bb}, \quad \chi_{ab} = 0$$

# What the magnetic torque tells us

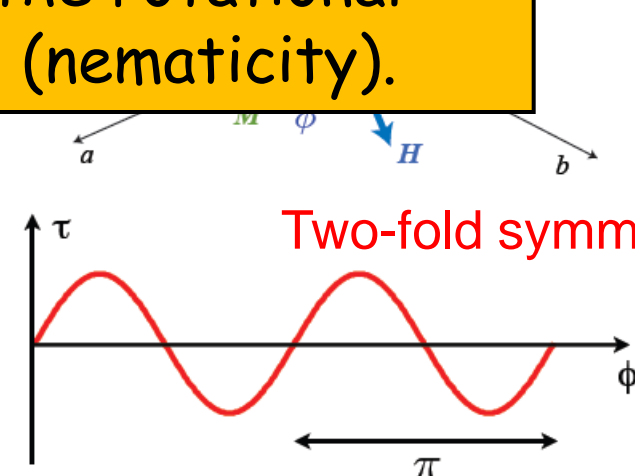
If rotational symmetry is broken, twofold oscillation appears in  $\tau(\phi)$ .

Torque measurements provide a stringent test for the rotational symmetry breaking (nematicity).

Torque  
 $\tau = \mu_0 \mathbf{M} \times \mathbf{H}$   
 $= 0$



Preserved  $C_4$  symmetry



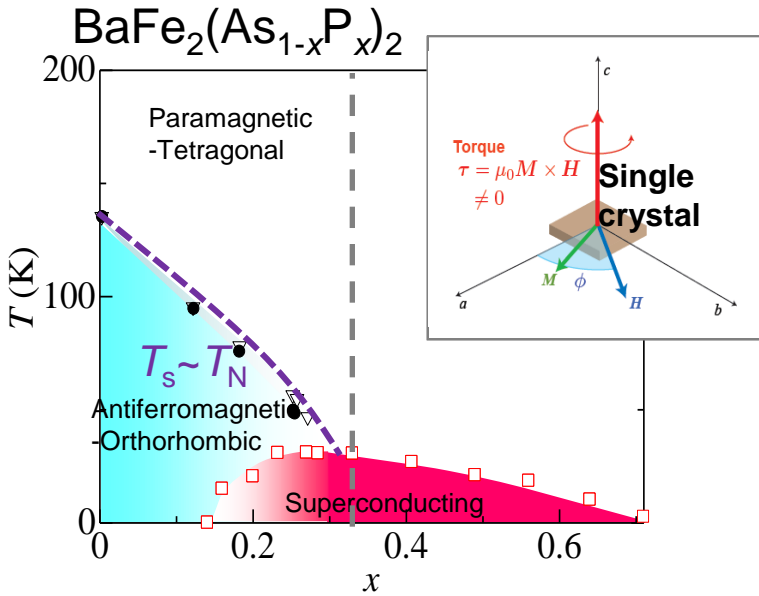
Broken  $C_4$  symmetry

$$\tau_{2\phi} = \frac{1}{2} \mu_0 H^2 V [(\chi_{aa} - \chi_{bb}) \sin 2\phi - 2\chi_{ab} \cos 2\phi]$$

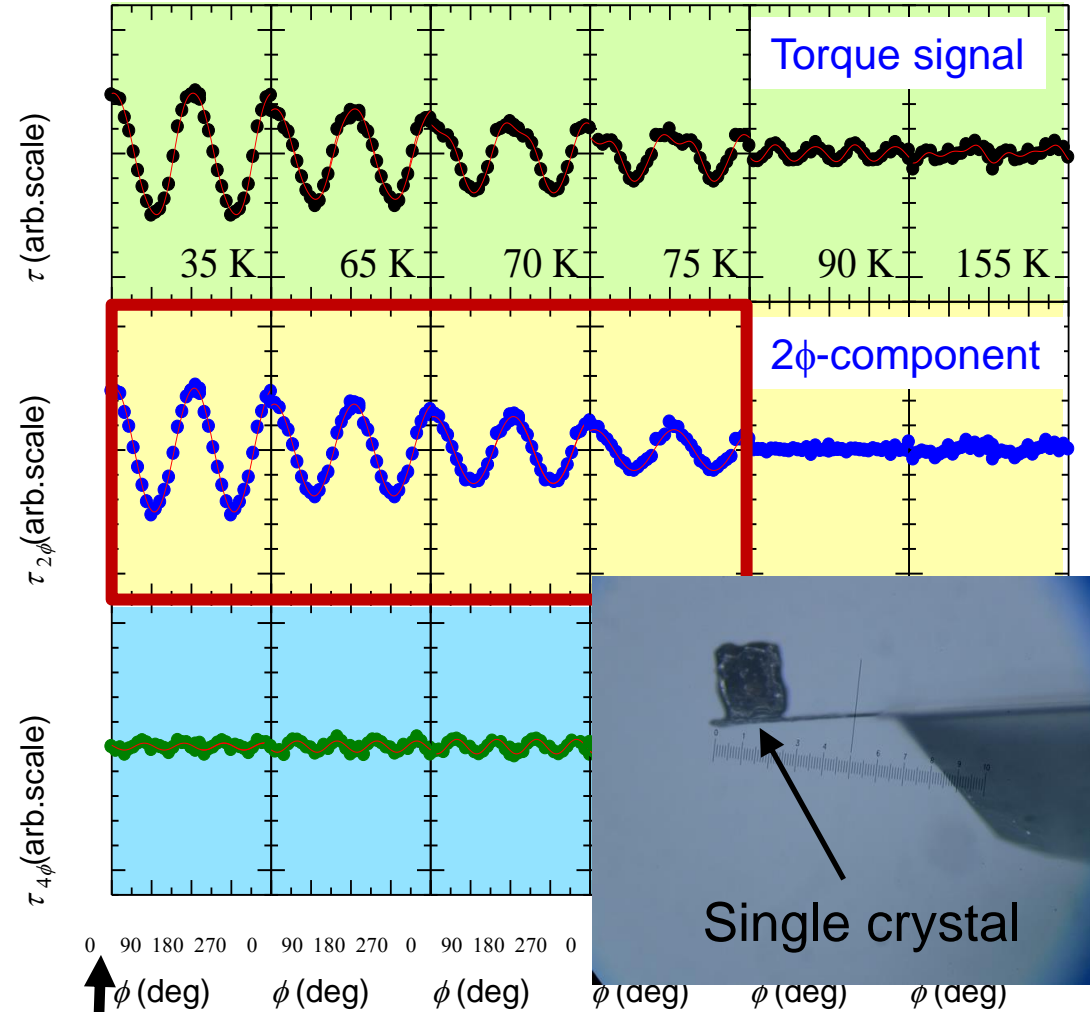
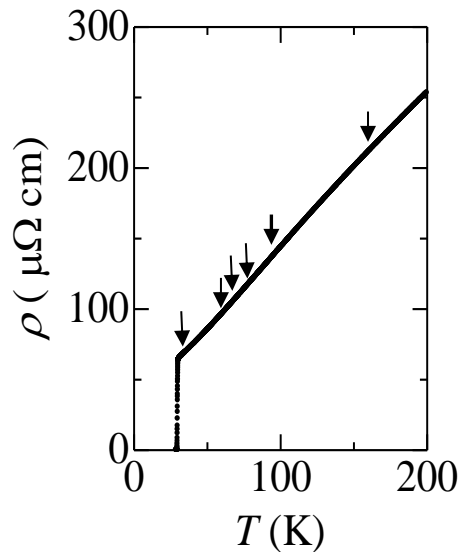
$\chi_{aa} = \chi_{bb}$  and  $\chi_{ab} = 0$

$\chi_{aa} \neq \chi_{bb}$  and/or  $\chi_{ab} \neq 0$

# In-plane torque magnetometry: a test of nematicity



$x = 0.33$  (no structural and magnetic transitions)



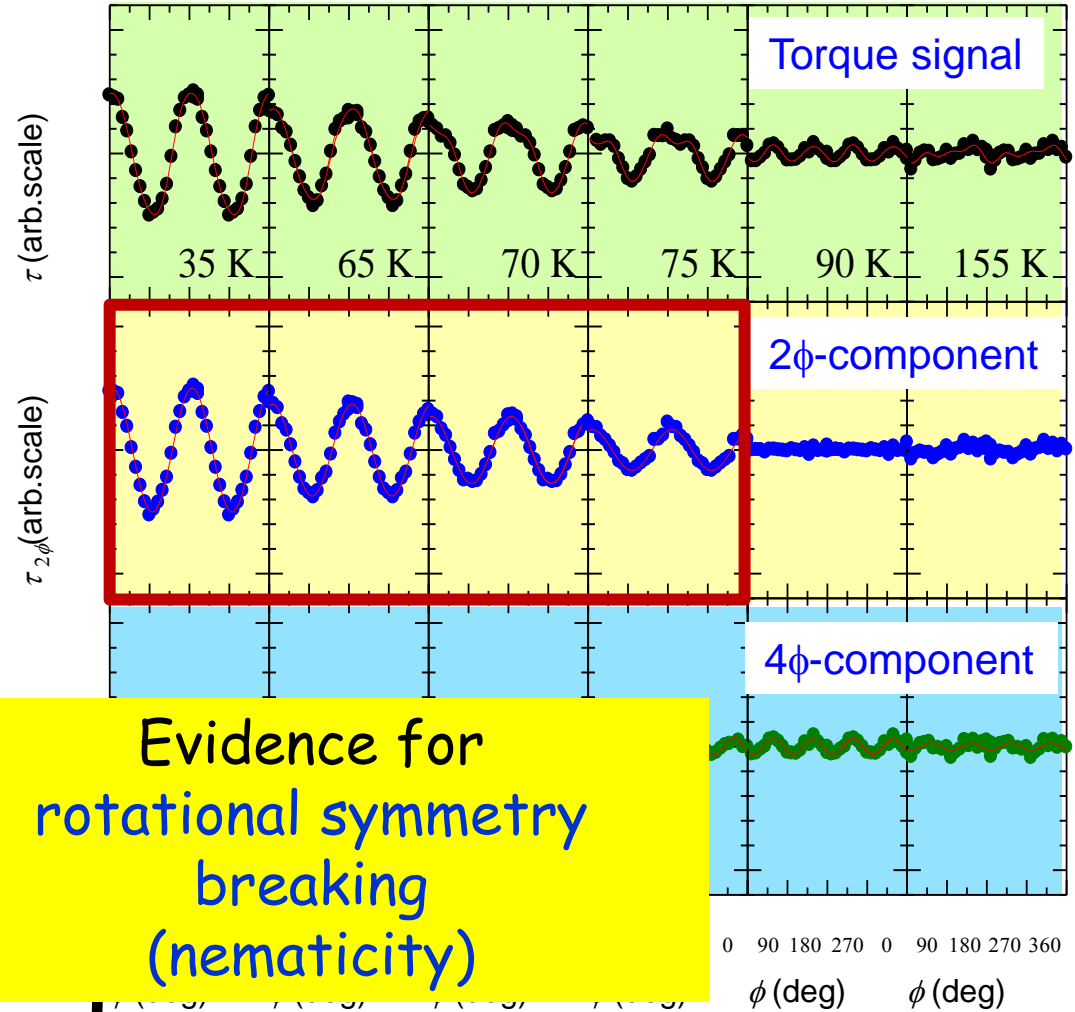
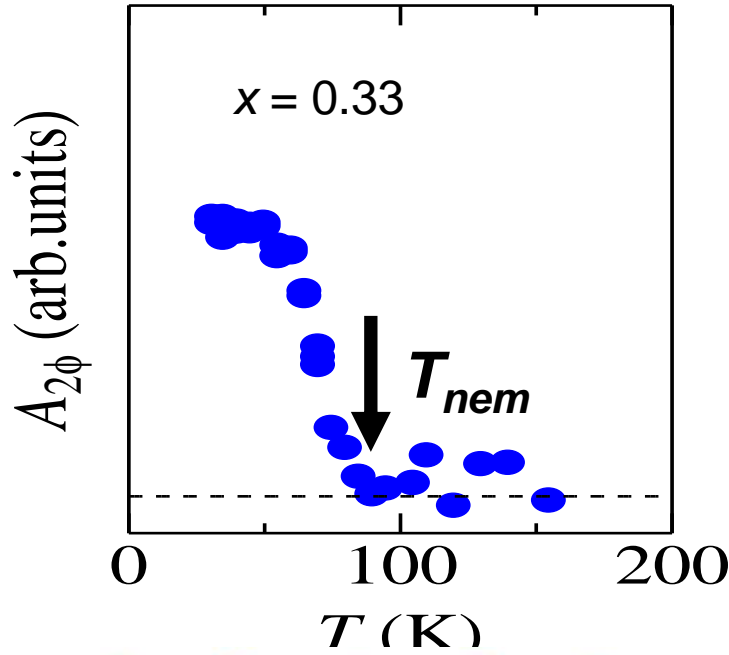
$[100]_T$

(Typical crystal dimensions: 70 x 70 x 30  $\mu\text{m}^3$ )

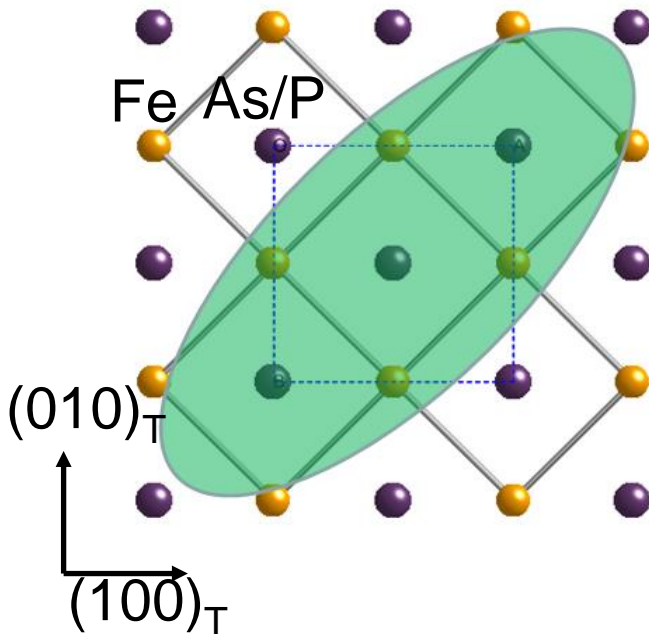
**-2 $\phi$  component at low temperatures**



# In-plane torque magnetometry: a test of nematicity



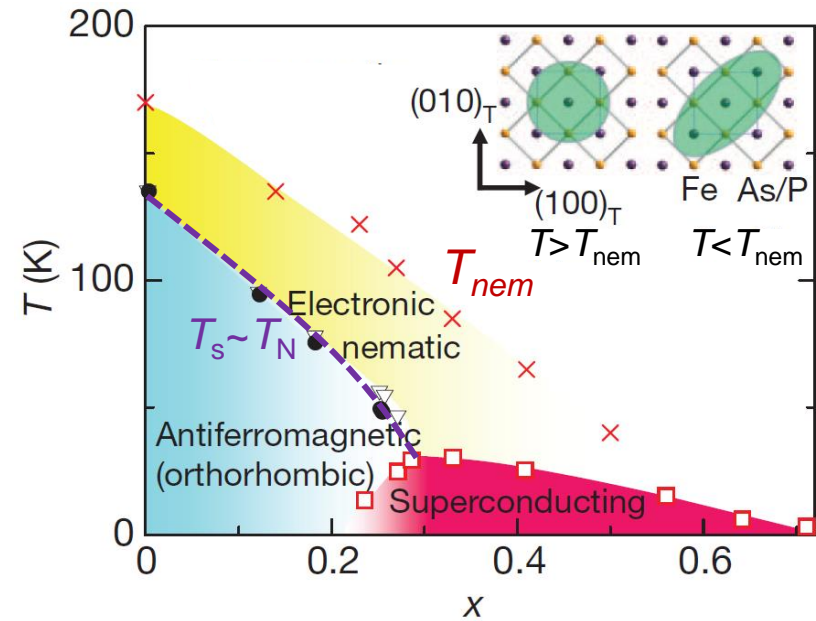
Evidence for rotational symmetry breaking (nematicity)



$$\tau = \frac{1}{2} \mu_0 H^2 V [(\chi_{aa} - \chi_{bb}) \sin 2\phi - 2\chi_{ab} \cos 2\phi]$$

$$\chi_{ab} \neq 0$$

# Phase diagram: Nematicity



S. Kasahara *et al.* Nature (2012)

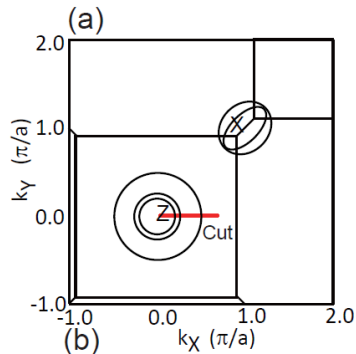
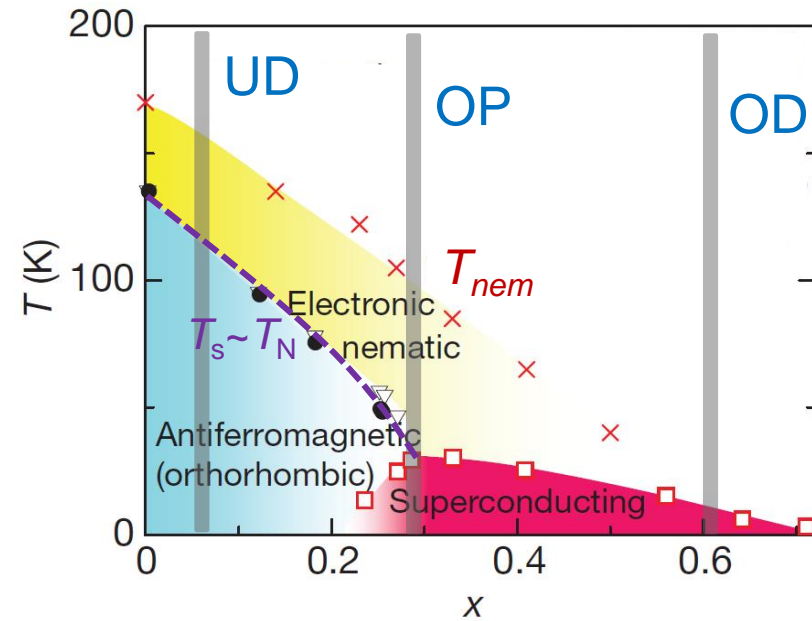
Electronic nematic phase persists over a wide range of doping.

Both AFM and SC states are within the nematic phase.

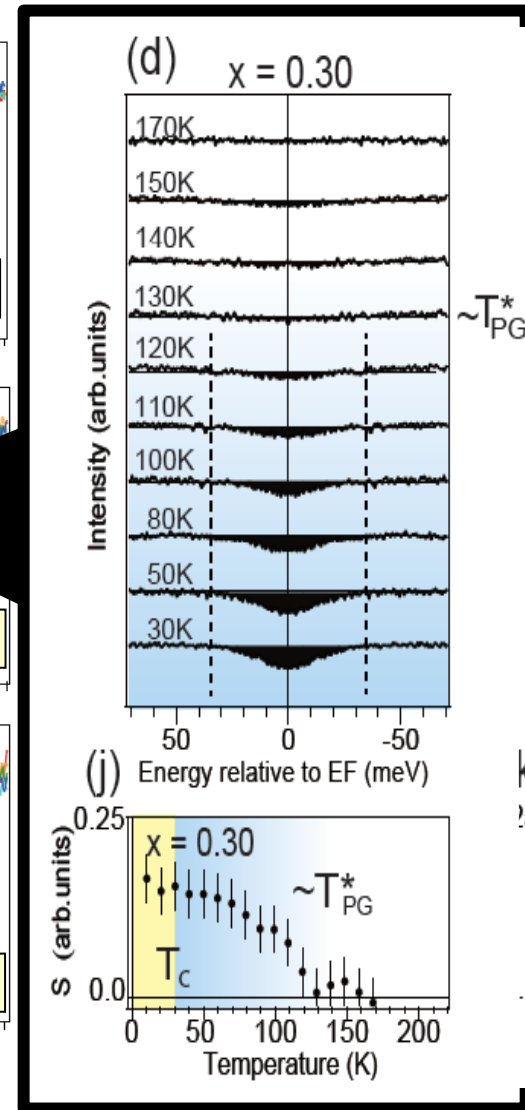
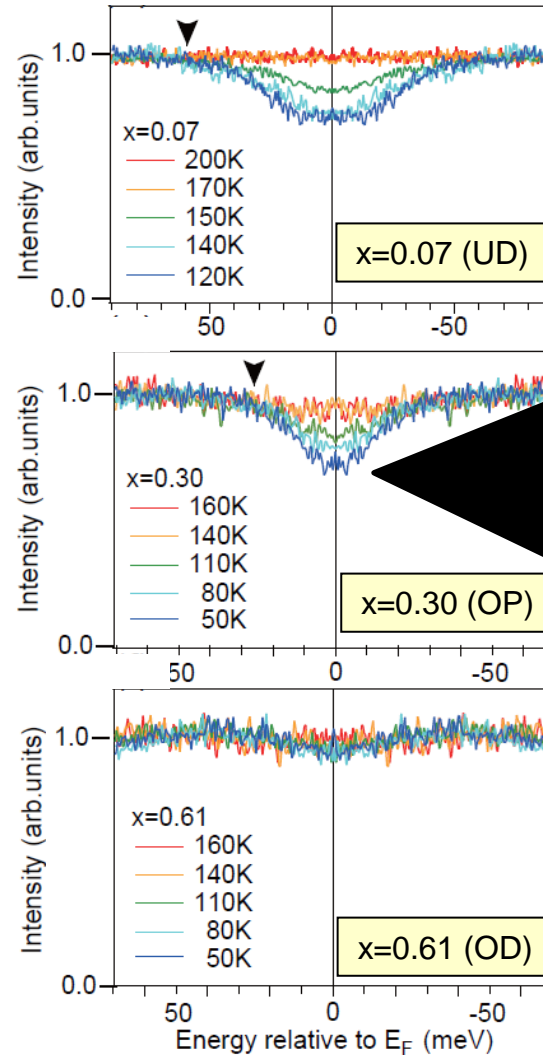
# Pseudogap

Laser ARPES in  $\text{BaFe}_2(\text{As}_{1-x}\text{P}_x)_2$

T. Shimojima *et al.*, Phys. Rev. B (2014).



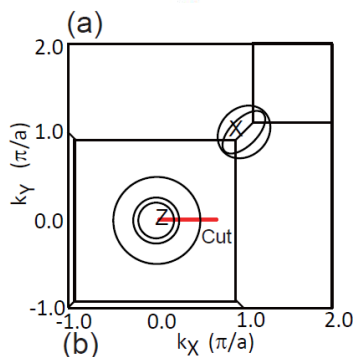
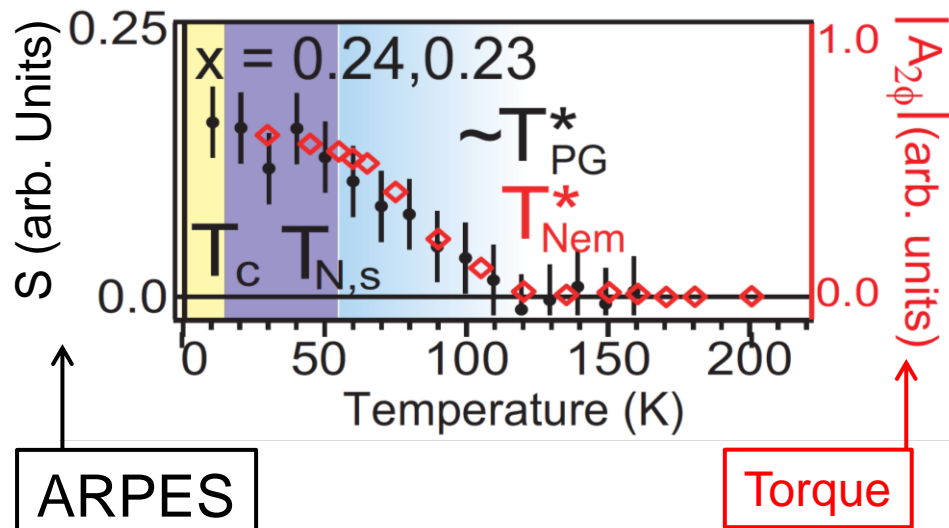
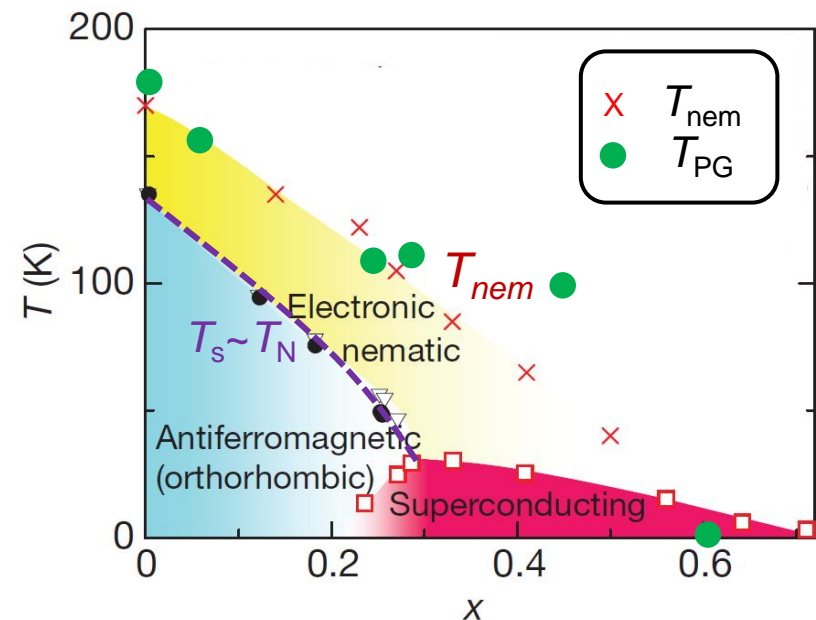
Outer hole band in Z plane



# Pseudogap

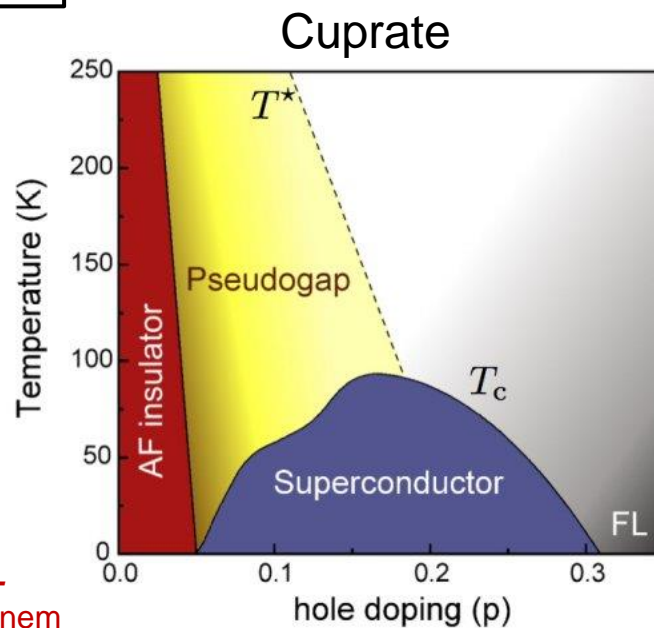
## Laser ARPES in $\text{BaFe}_2(\text{As}_{1-x}\text{P}_x)_2$

T. Shimojima *et al.*, Phys. Rev. B (2014).



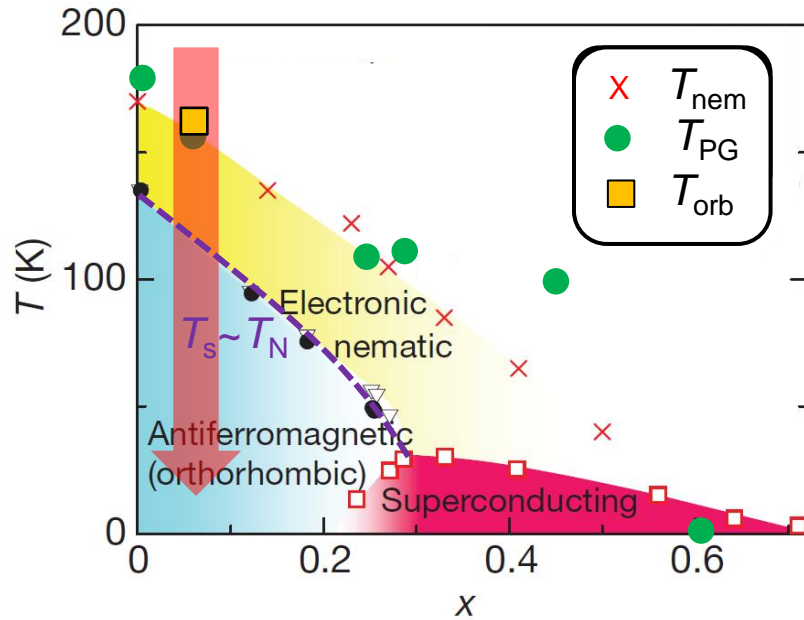
Outer hole band in Z plane

Pseudogap formation at  $T_{PG} \sim T_{nem}$

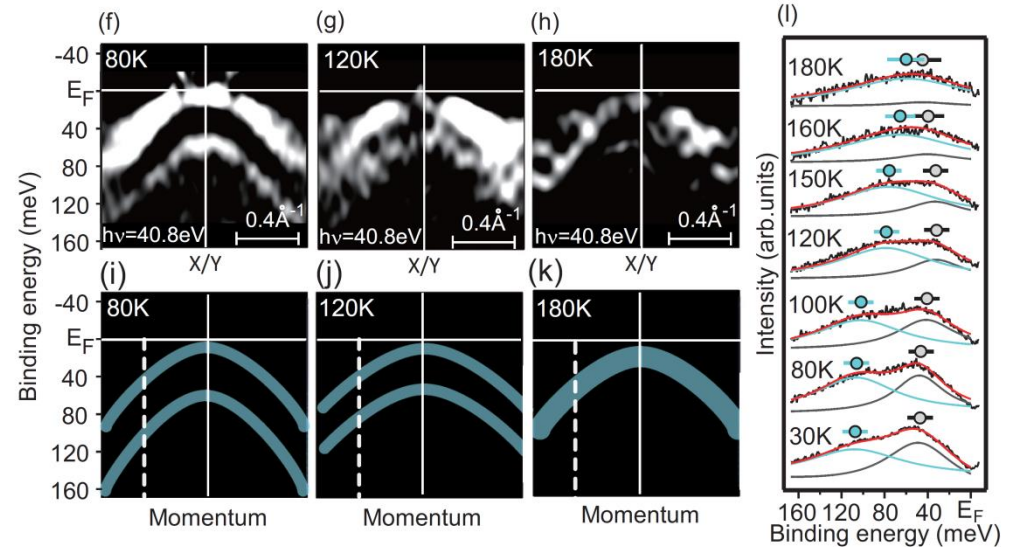


# Anisotropic electronic occupation in $zx/yz$ orbitals

T. Shimojima *et al.*, Phys. Rev. B (2014).



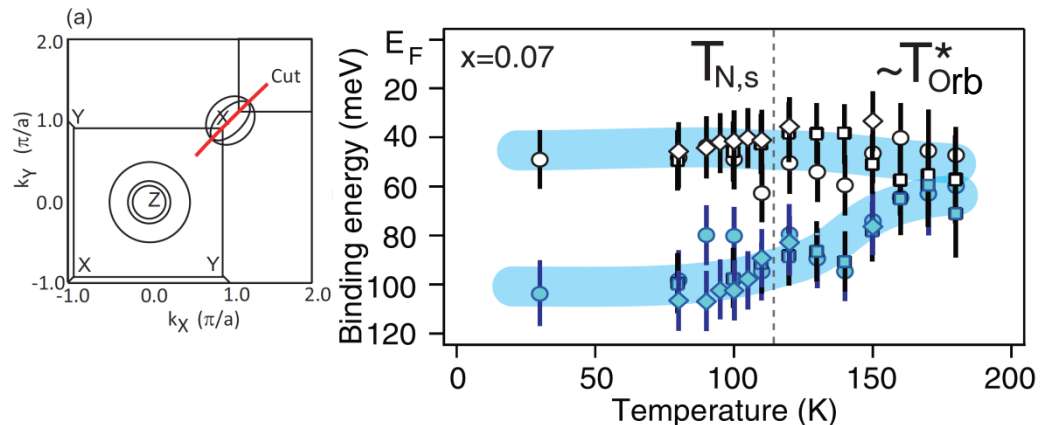
Inequivalent energy shifts for  $xz/yz$  orbitals below  $T_{orb}$



orbital ordering?

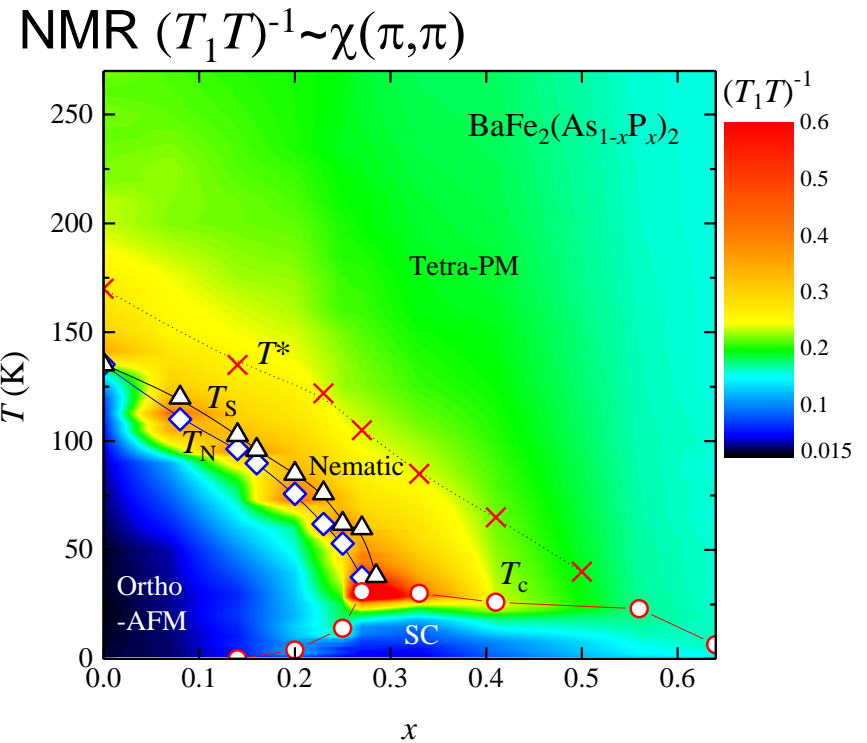
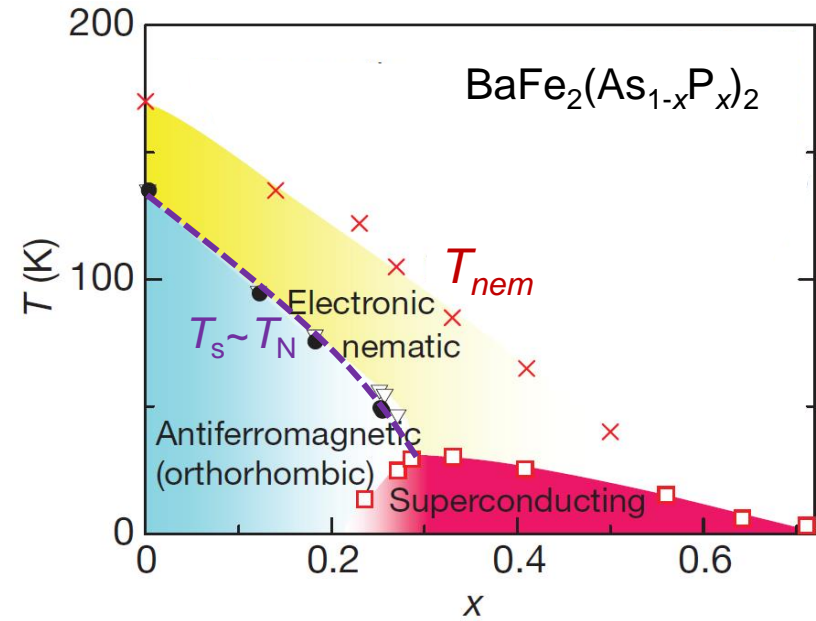
Nematic transition  $T_{nem}$   
 Pseudogap formation  $T_{PG}$   
 Orbital ordering  $T_{orb}$

$$T_{nem} \sim T_{PG} \sim T_{orb}$$

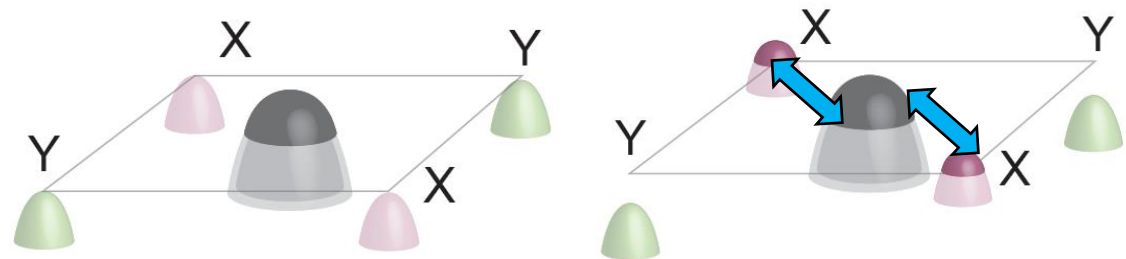


# Nematicity and AFM fluctuations

Y. Nakai et al., PRB **87**, 174507 (2013)



The nematicity enhances AFM fluctuations.

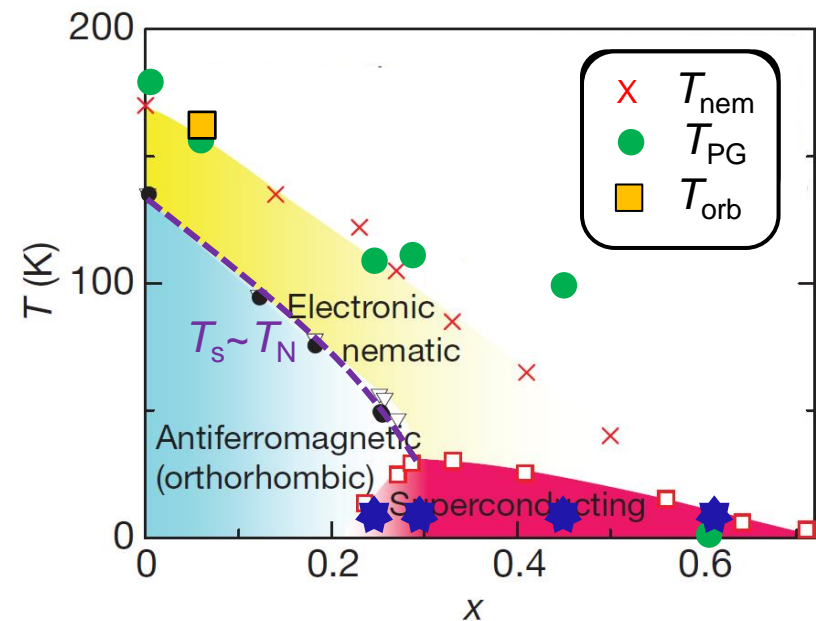




# Coexistence of orbital degeneracy lifting and superconductivity

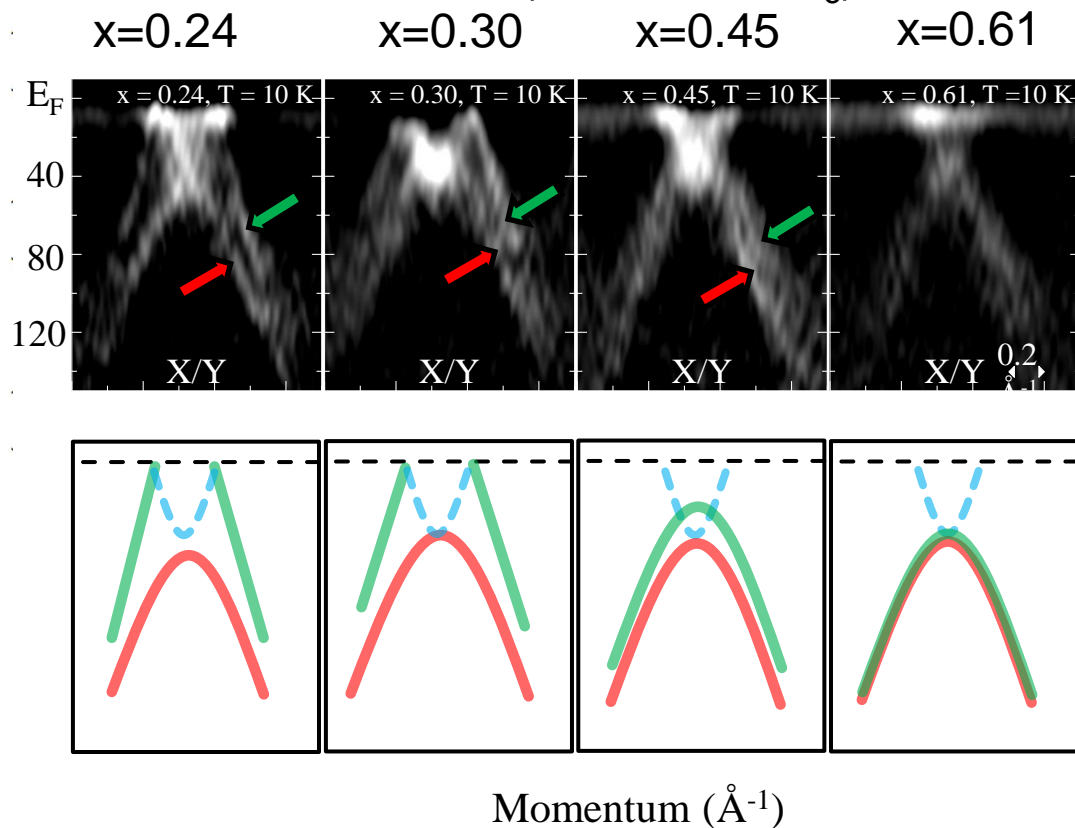
T. Sonobe *et al.*, unpublished

$T=10$  K (well below  $T_c$ )



Nematic transition  $T_{nem}$   
 Pseudogap formation  $T_{PG}$   
 Orbital ordering  $T_{orb}$

$$T_{nem} \sim T_{PG} \sim T_{orb}$$

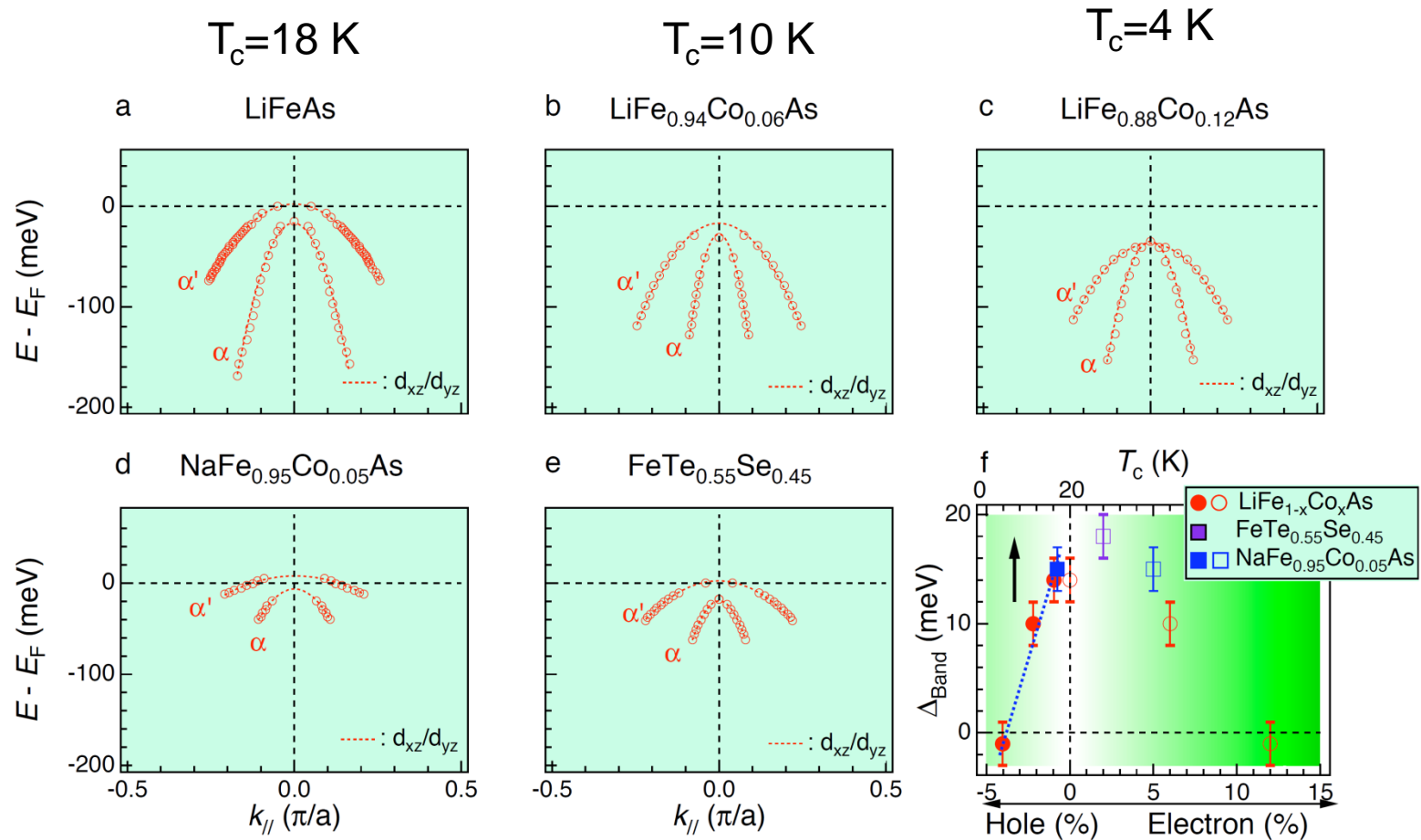


Anisotropy in  $zx/yz$  orbitals persists in the SC dome

Relationship between nematicity and superconductivity



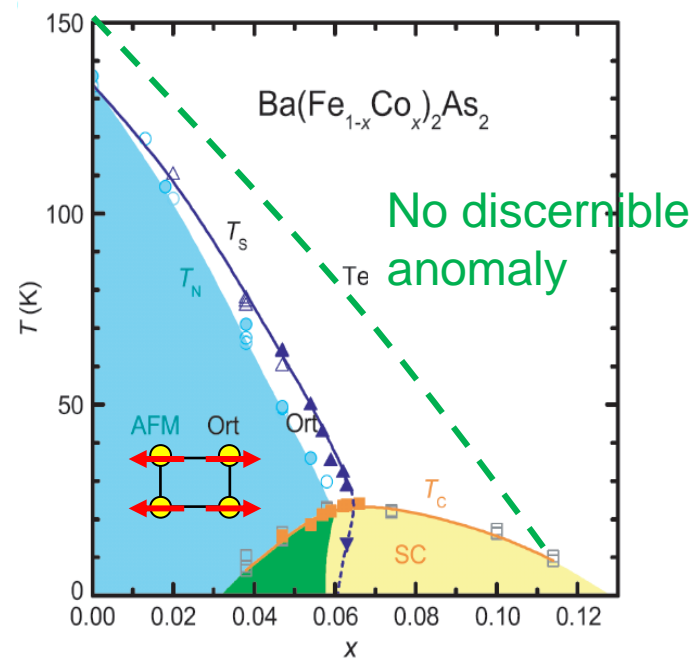
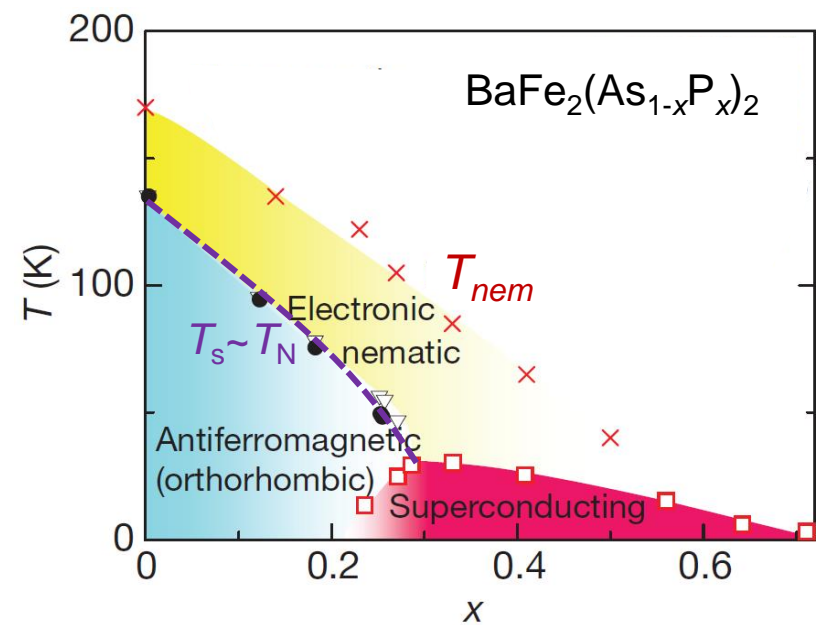
# Coexistence of orbital degeneracy lifting and superconductivity



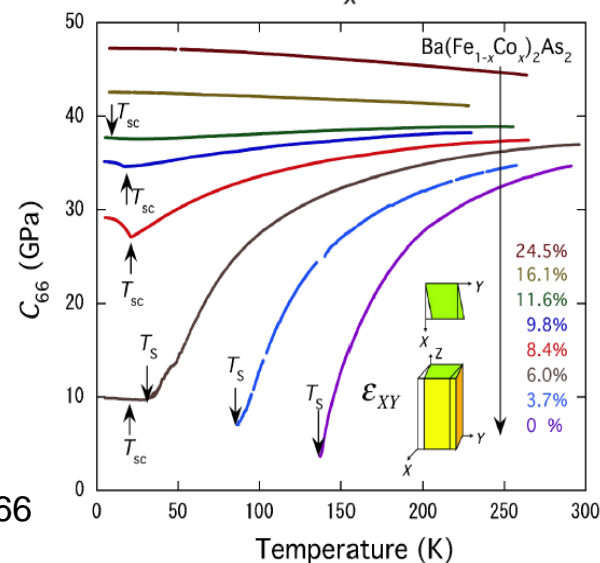
H. Miao *et al.* arXiv:1310.4601

Relationship between nematicity and superconductivity

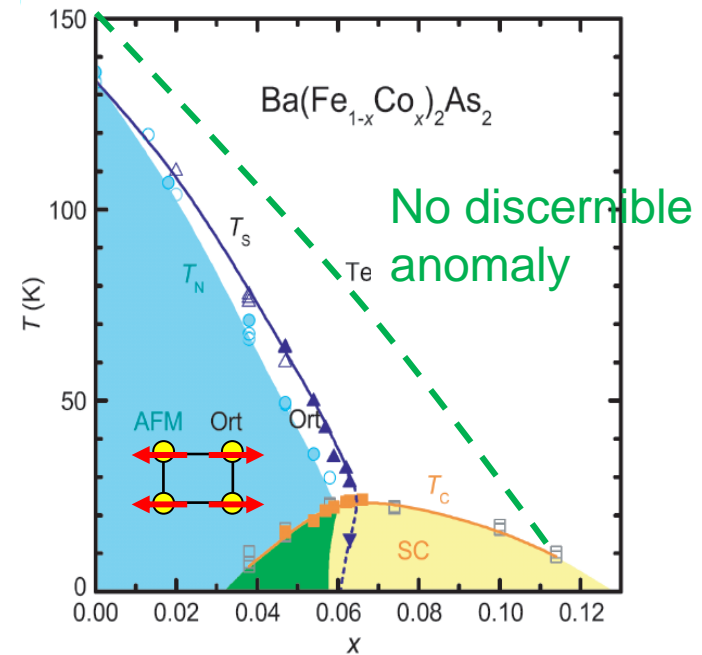
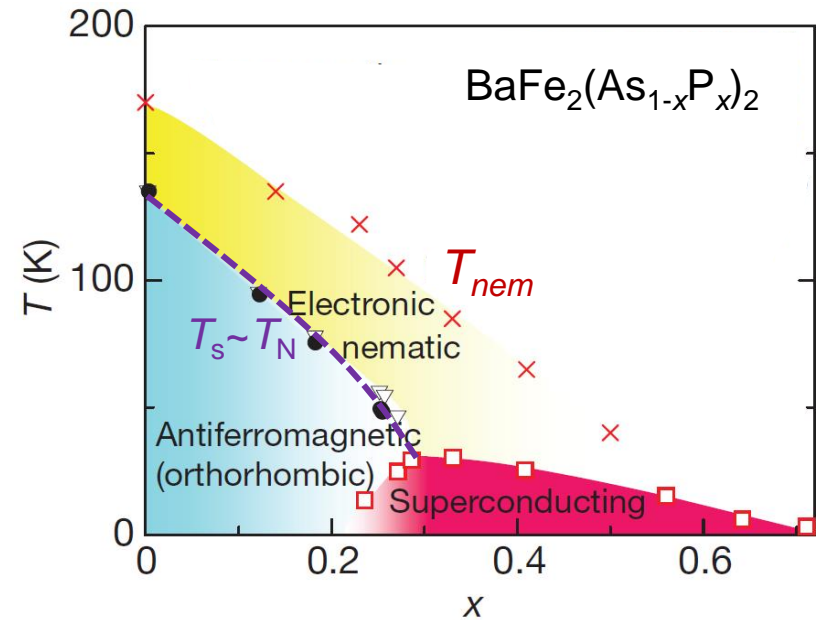
# Phase diagram



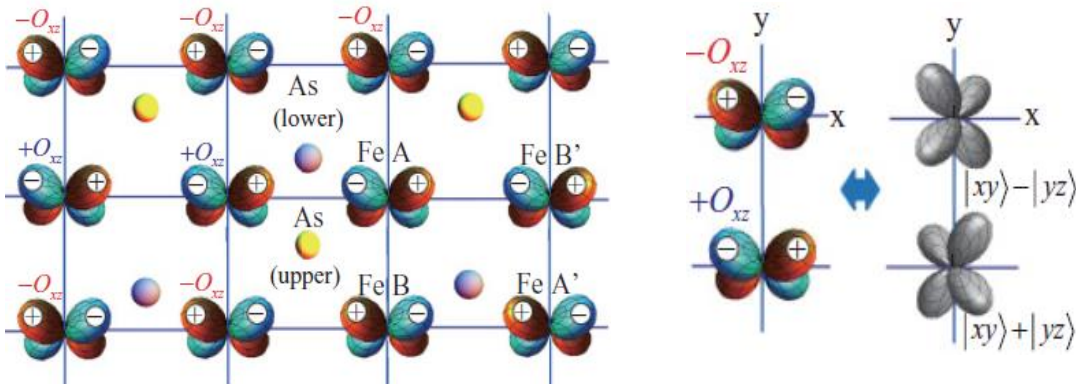
Elastic constant  $C_{66}$



# Phase diagram



Antiferro type orbital ordering  
( $O_{xz}$  antiferro-quadrupole (AFQ) ordering)



H. Kontani *et al.*, Phys. Rev. B (2011).

$q \neq 0$  AF orbital ordering may be difficult to detect by long wave length ( $q=0$ ) probes, such as elastic constant.

# 1. Quantum critical point lies beneath the SC dome

1. QCP is definitely important for the high- $T_c$  superconductivity
2. The QCP is the origin of the non-Fermi liquid behavior.
3. Microscopic coexistence of superconductivity and SDW.

Magnetic QCP or orbital QCP?

# 2. BCS-BEC crossover in FeSe

A new highly spin-polarized phase

# 3. Nematicity in Iron pnictide

Nematic transition  $T_{\text{nem}}$

Pseudogap formation  $T_{\text{PG}}$

Orbital ordering  $T_{\text{orb}}$

$$T_{\text{nem}} \sim T_{\text{PG}} \sim T_{\text{orb}}$$

Is nematicity important for the superconductivity?

What is the origin of the nematicity, spin or orbital?

