

# Cold fermions, Feshbach resonance, and molecular condensates (II)

D. Jin JILA, NIST and the University of Colorado



- I. Cold fermions
  - II. Feshbach resonance
  - III. BCS-BEC crossover
- (Experiments at JILA)

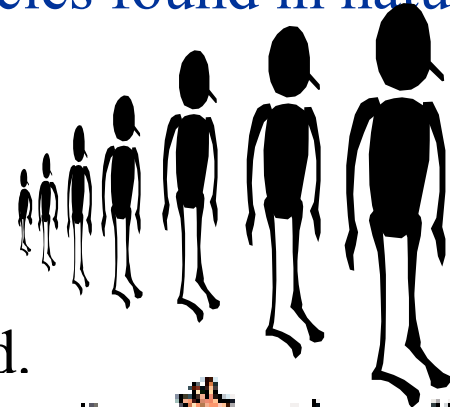
\$\$ NSF, NIST, Hertz

# I. Cold Fermions

# Quantum Particles

- There are two types of quantum particles found in nature - **bosons and fermions.**

Bosons like to do the same thing.

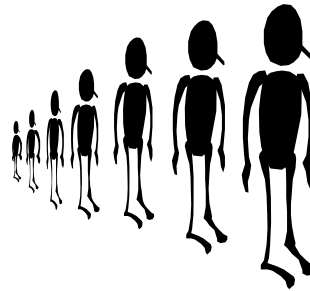


Fermions are independent-minded.



- Atoms, depending on their composition, can be either.  
**bosons:**  $^{87}\text{Rb}$ ,  $^{23}\text{Na}$ ,  $^7\text{Li}$ ,  $\text{H}$ ,  $^{39}\text{K}$ ,  $^4\text{He}^*$ ,  $^{85}\text{Rb}$ ,  $^{133}\text{Cs}$   
**fermions:**  $^{40}\text{K}$ ,  $^6\text{Li}$

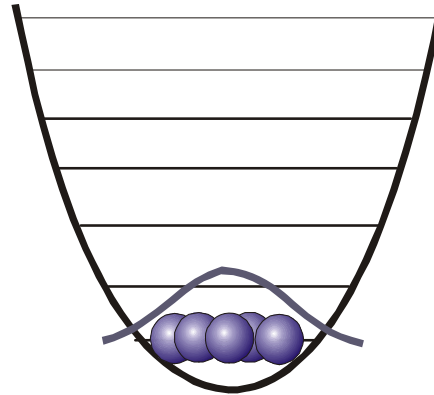
# Bosons



☺ integer spin

☺  $\Psi_{1,2} = \Psi_{2,1}$

Atoms in a  
harmonic  
potential.



Bose-Einstein condensation

1995

other bosons: photons, liquid  $^4\text{He}$

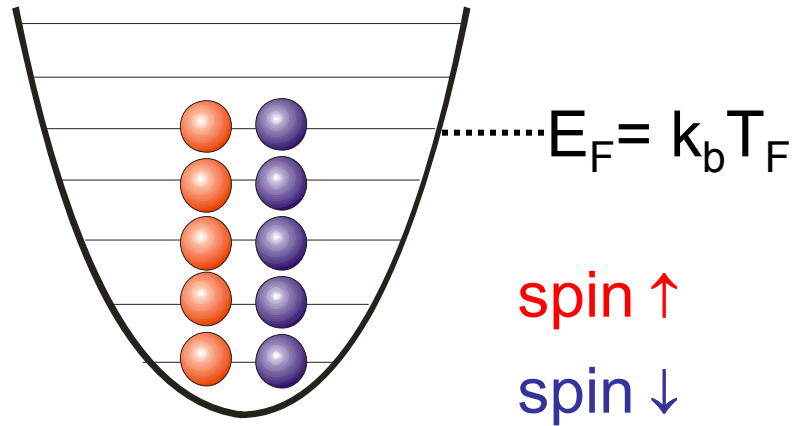
# Fermions



☹ half-integer spin

☹  $\Psi_{1,2} = -\Psi_{2,1}$  (Pauli exclusion principle)

$T = 0$



Fermi sea of atoms

1999

other fermions: protons, electrons, neutrons

# Quantum gases

Bosons

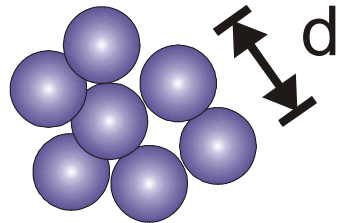
$T_C$

BEC phase transition

Fermions

$T_F$

Fermi sea of atoms gradually emerges for  $T < T_F$



$$\lambda_{\text{deBroglie}} \sim d$$

ultralow T

# Fermionic atoms

$^{40}\text{K}$

**Jin, JILA**

Inguscio, LENS

$^6\text{Li}$

Hulet, Rice

Salomon, ENS

Thomas, Duke

Ketterle, MIT

Grimm, Innsbruck

others in progress...

Future: Cr, Sr, Yb,  
radioactive isotopes Rb,  
metastable  $^3\text{He}$ ,  $^3\text{Ne}$

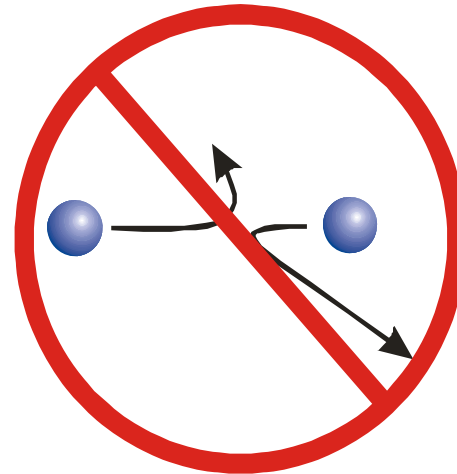
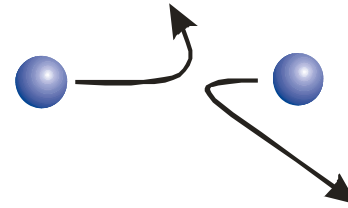
...

# Cooling fermions

Evaporative cooling requires collisions,



but at low  $T$  identical fermions stop colliding .



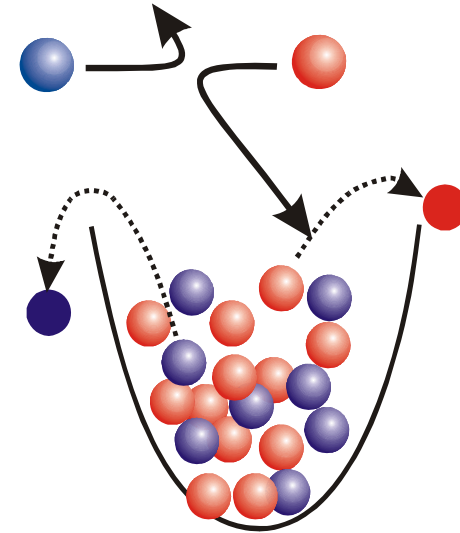


# Cooling strategies for fermions

## Simultaneous cooling

evaporate atoms in two spin-states

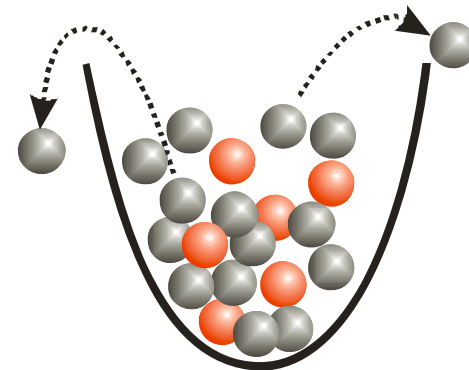
- magnetic trap  $^{40}\text{K}$
- optical trap  $^6\text{Li}$



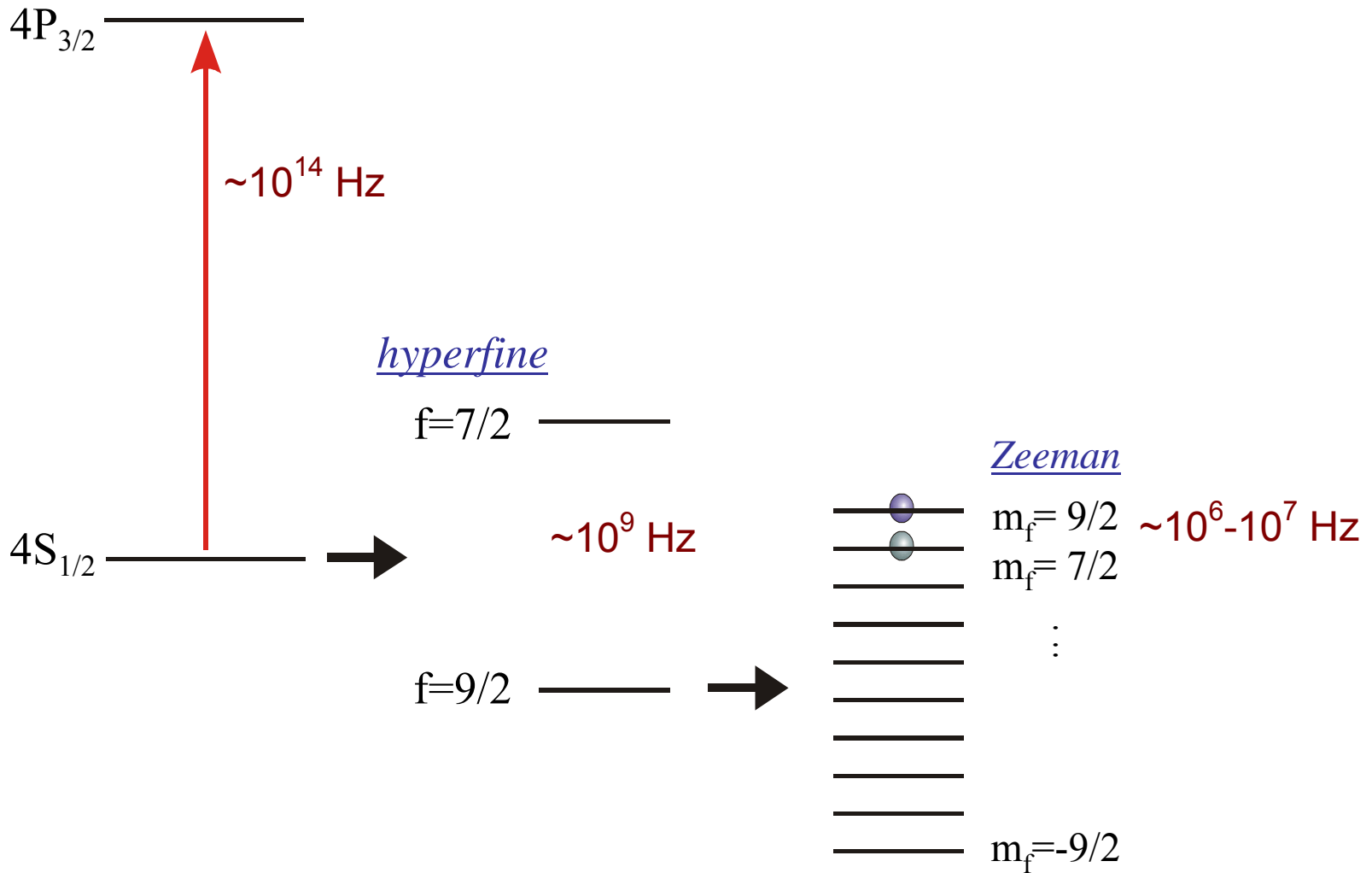
## Sympathetic cooling

evaporate bosonic atoms and cool fermionic atoms via thermal contact

- two isotopes  $^7\text{Li} + ^6\text{Li}$
- two species  $^{87}\text{Rb} + ^{40}\text{K}$   
 $^{23}\text{Na} + ^6\text{Li}$



# $^{40}\text{K}$ spin-states



# More on spin-states

 spin “↑”

Energy splitting is 10's MHz.

$T = 1 \mu\text{K}$  corresponds to 20 kHz.

 spin “↓”

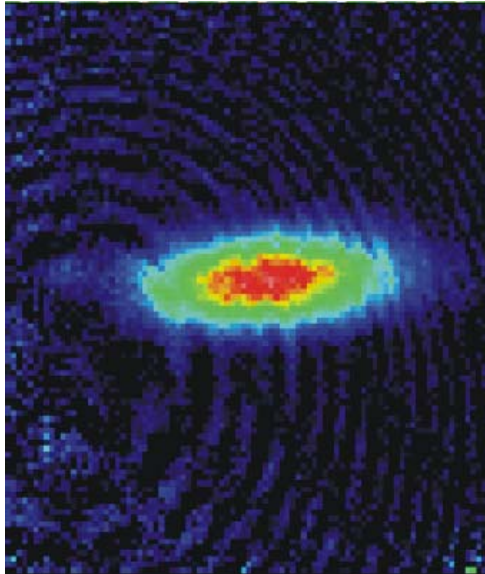
➤ spin degree of freedom is frozen



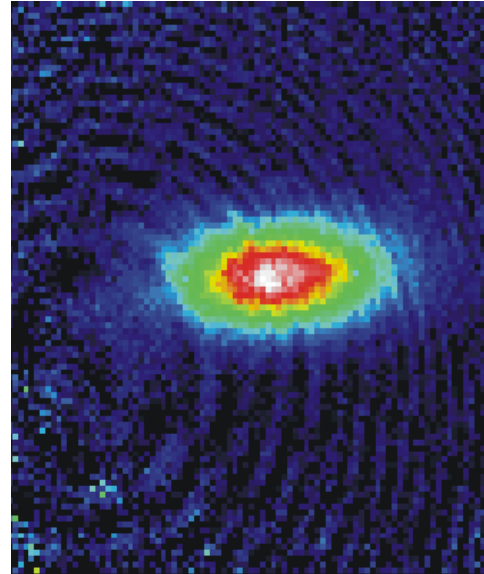
# Collision measurement

1. Add energy in one dimension of trap
2. Watch thermal relaxation

before

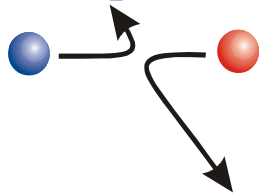


after relaxation



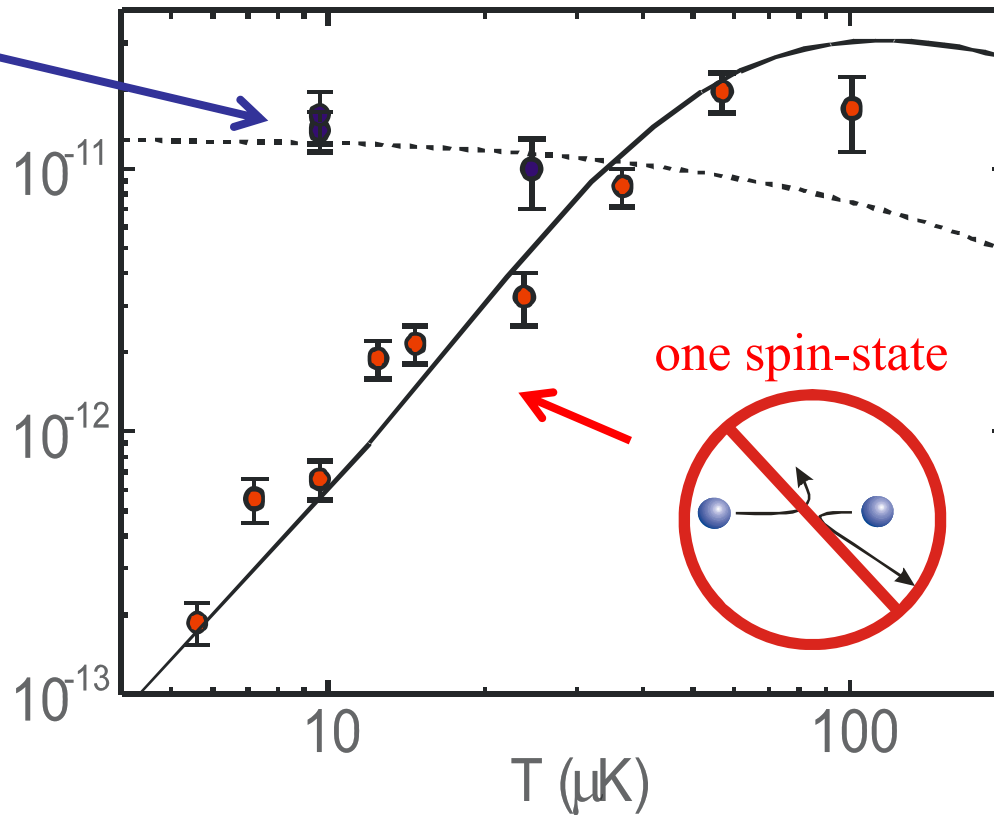
# Collisions and Fermions

two spin-states



elastic collision  
cross section

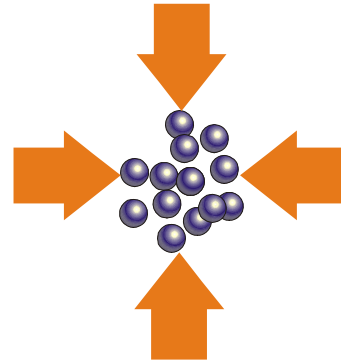
$\sigma$  (cm<sup>2</sup>)



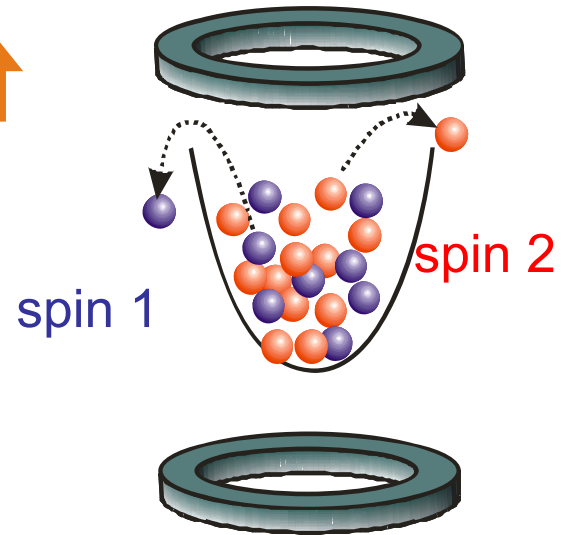
# Cooling a gas of $^{40}\text{K}$ atoms

## 1. Laser cooling and trapping

300 K to 1 mK,  $\sim 10^9$  atoms

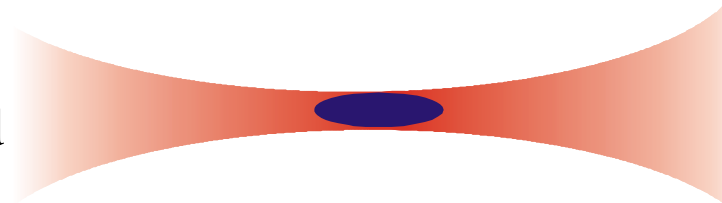


1 mK to 1  $\mu\text{K}$ ,  $\sim 10^8 \rightarrow 10^6$  atoms



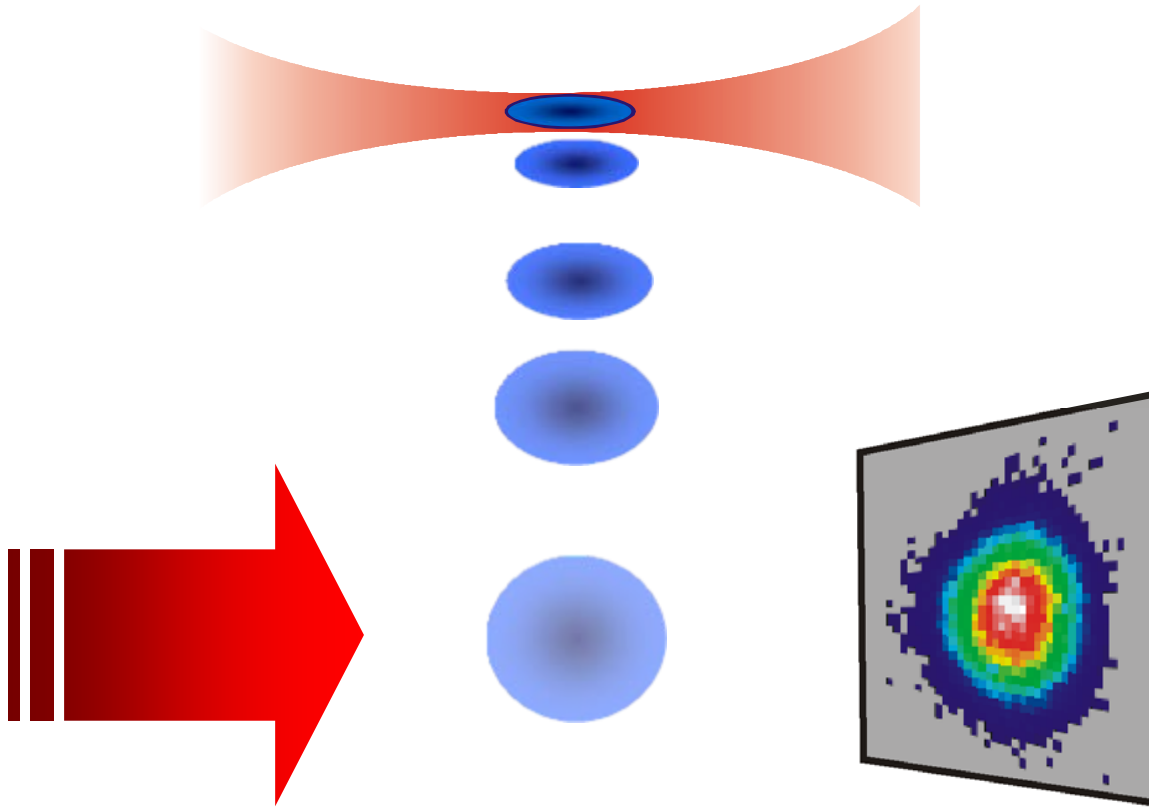
1  $\mu\text{K}$  to 50 nK,  $10^6 \rightarrow 10^5$  atoms

- can confine any spin-state
- can apply arbitrary B-field



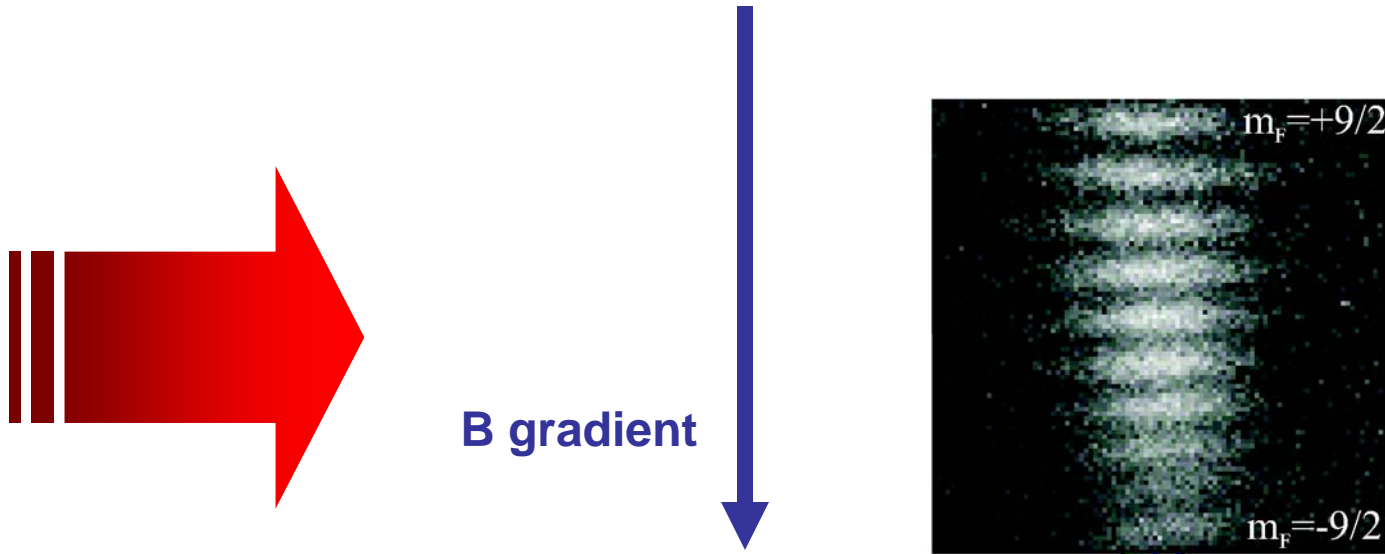
# Probing the ultracold gas

Time-of-flight absorption imaging



# Stern-Gerlach imaging

Time-of-flight absorption imaging

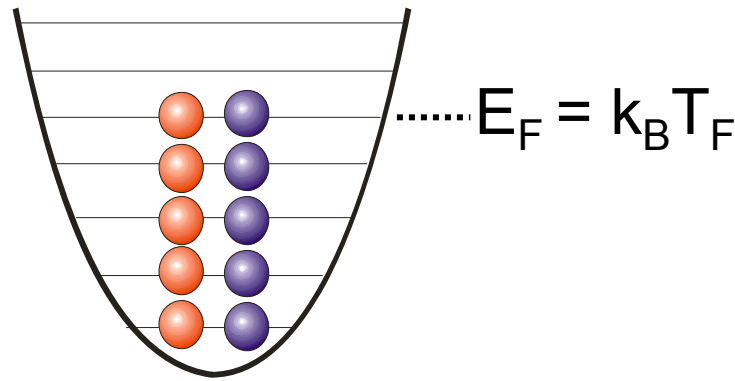




# Quantum degenerate atomic Fermi gases

1999:  **$^{40}\text{K}$**  JILA

$^6\text{Li}$  - Rice, Duke, ENS, MIT, Innsbruck;  $^{40}\text{K}$  - LENS, ETH Zurich

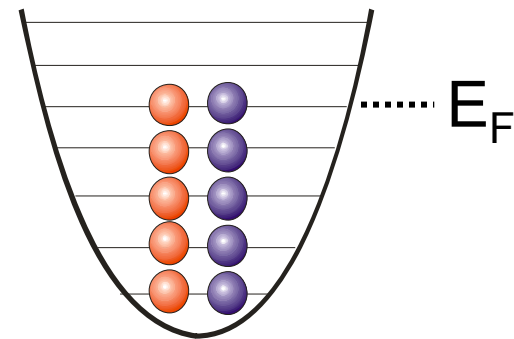
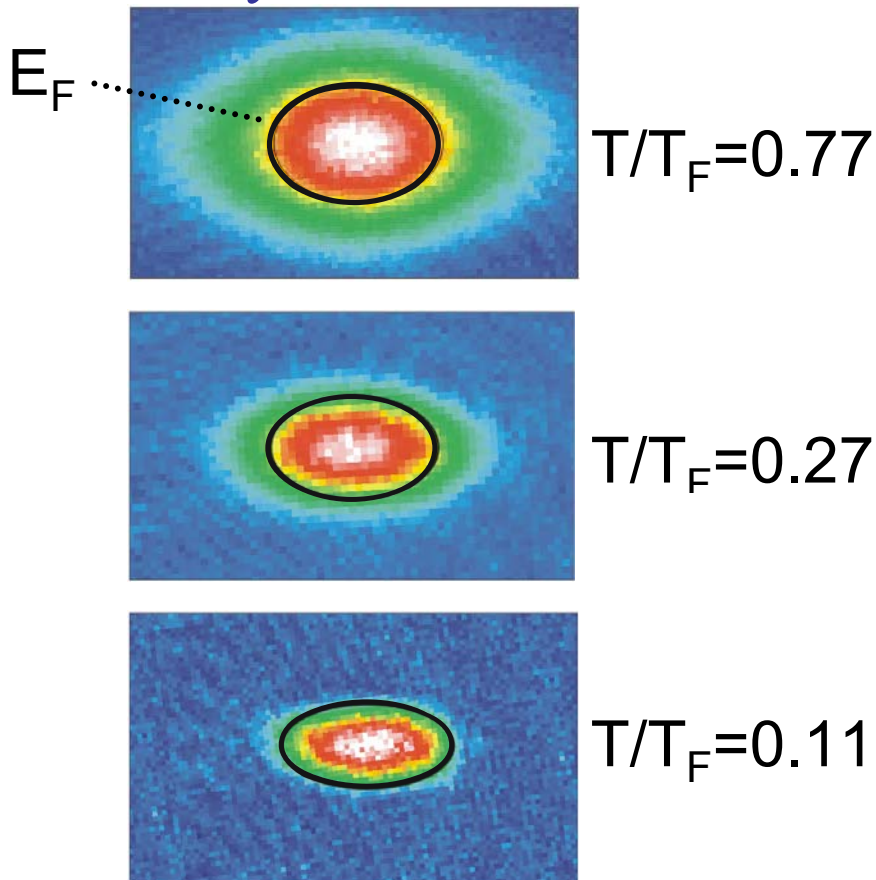


Fermi sea of atoms

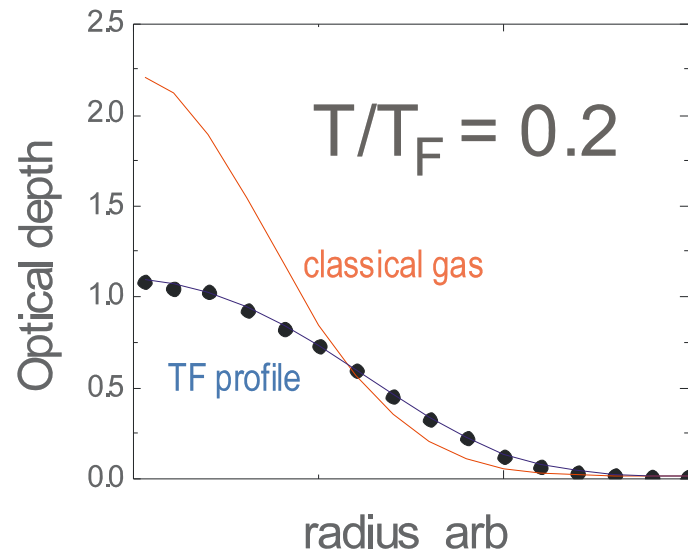
- $T \sim 0.05 T_F$
- low temperature, low density:  
 $T \sim 100 \text{ nK}$ ,  $n \sim 10^{13} \text{ cm}^{-3}$

# Quantum degeneracy

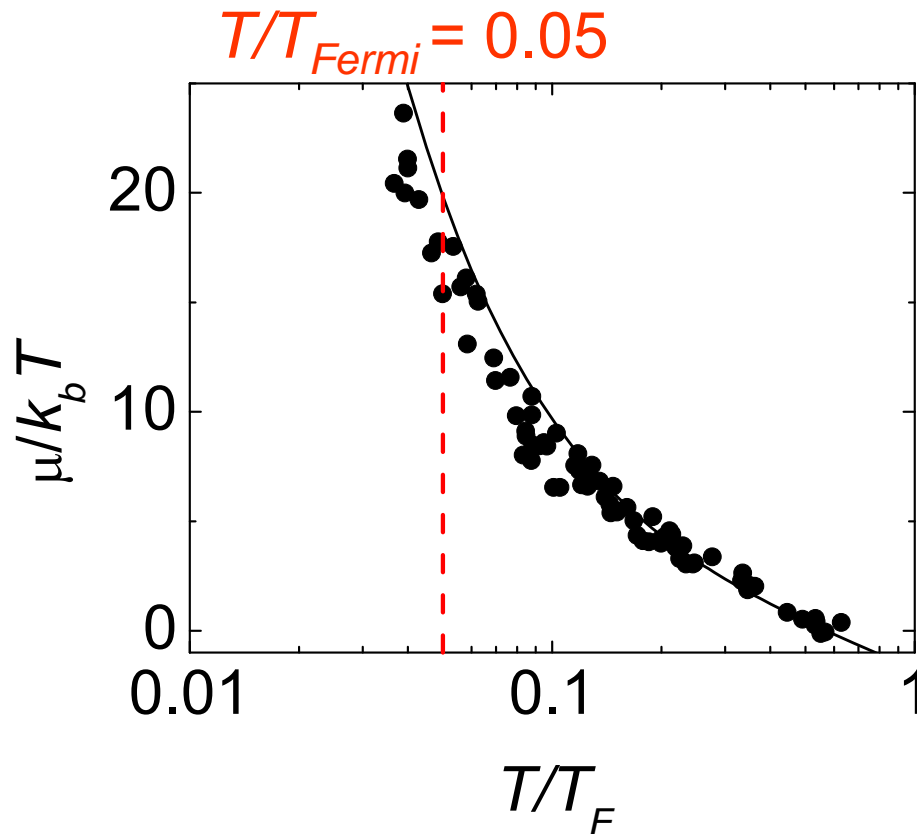
velocity distributions



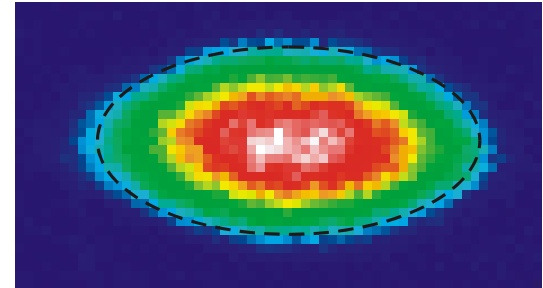
Fermi sea of atoms



# Quantum degeneracy



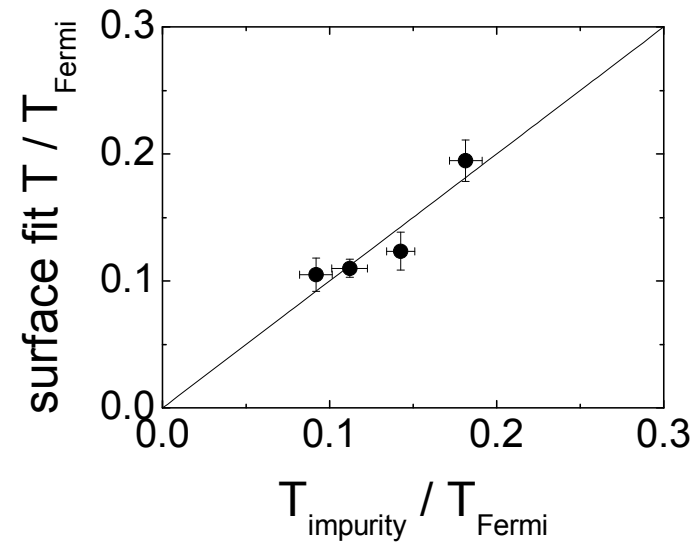
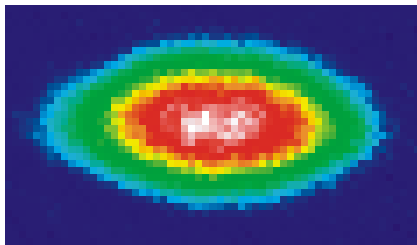
$N = 4 \cdot 10^5$ ,  $T = 16$  nK  
 $T/T_{Fermi} = 0.05$



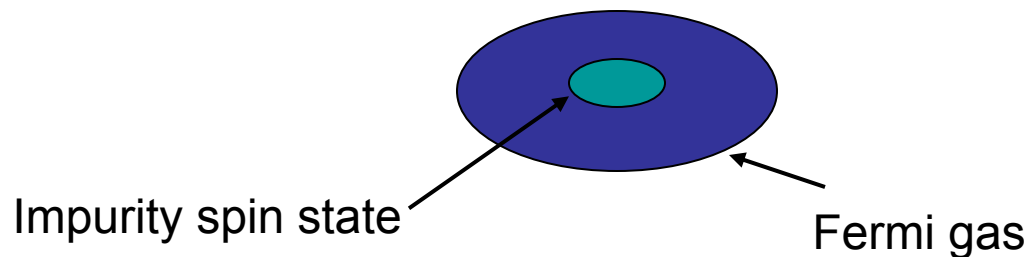
# Fermi gas thermometry

Determine temperature from

(1) surface fit to expanded cloud



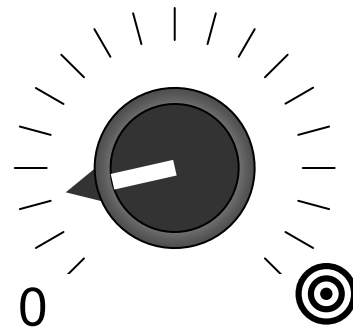
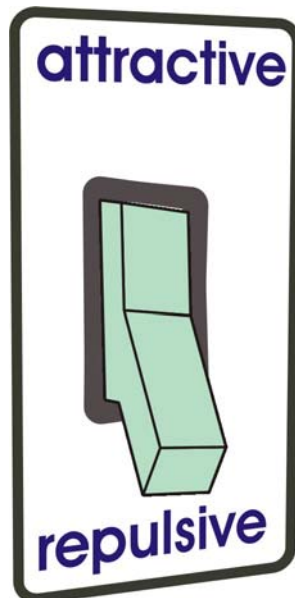
(2) an embedded  
non-degenerate gas



# II. Feshbach resonance

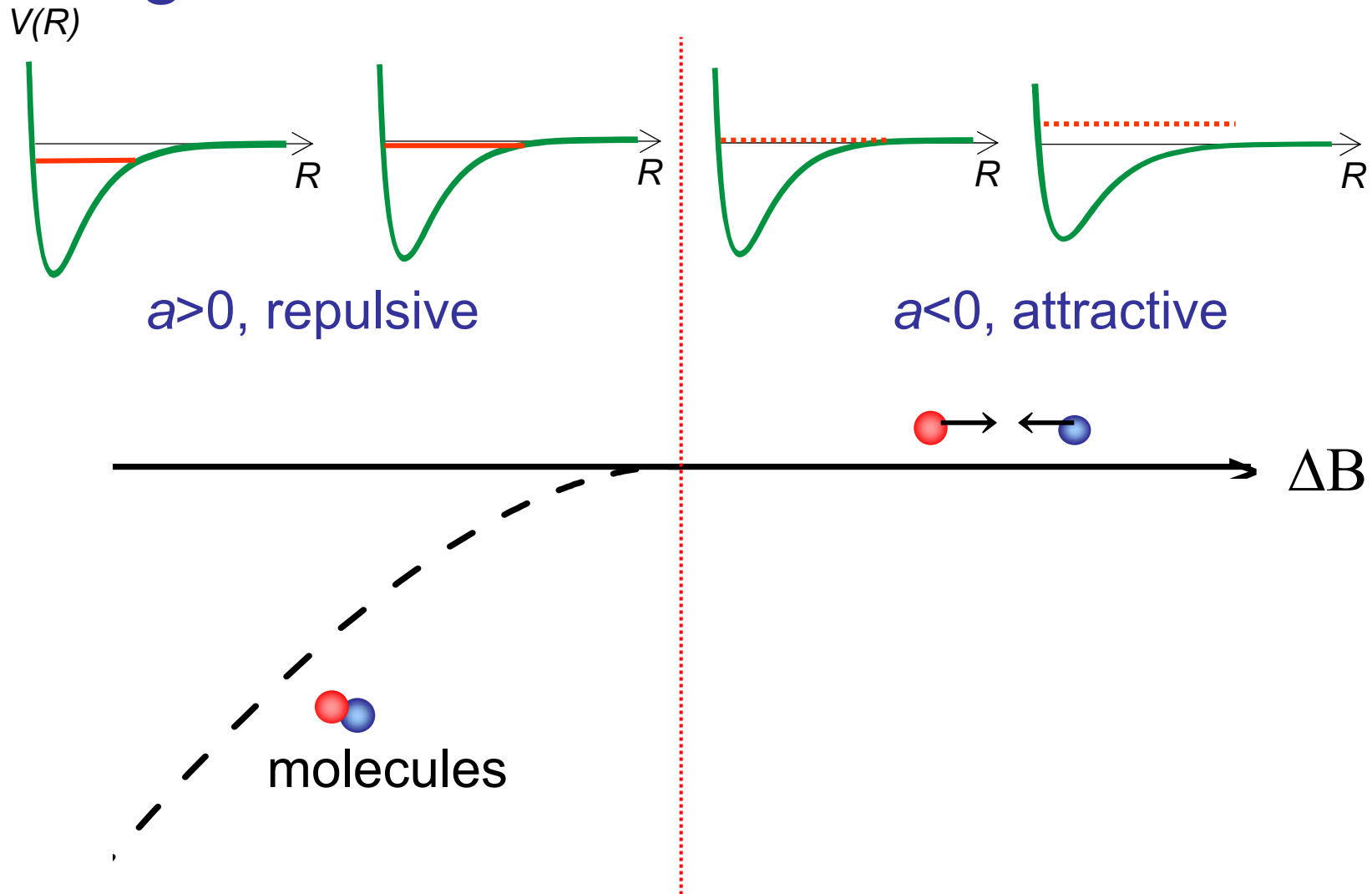
# Interactions

- Interactions are characterized by the s-wave scattering length,  $a$ 
  - $a > 0$  repulsive,  $a < 0$  attractive
  - Large  $|a| \rightarrow$  strong interactions
- In an ultracold atomic gas, we can control  $a$ !

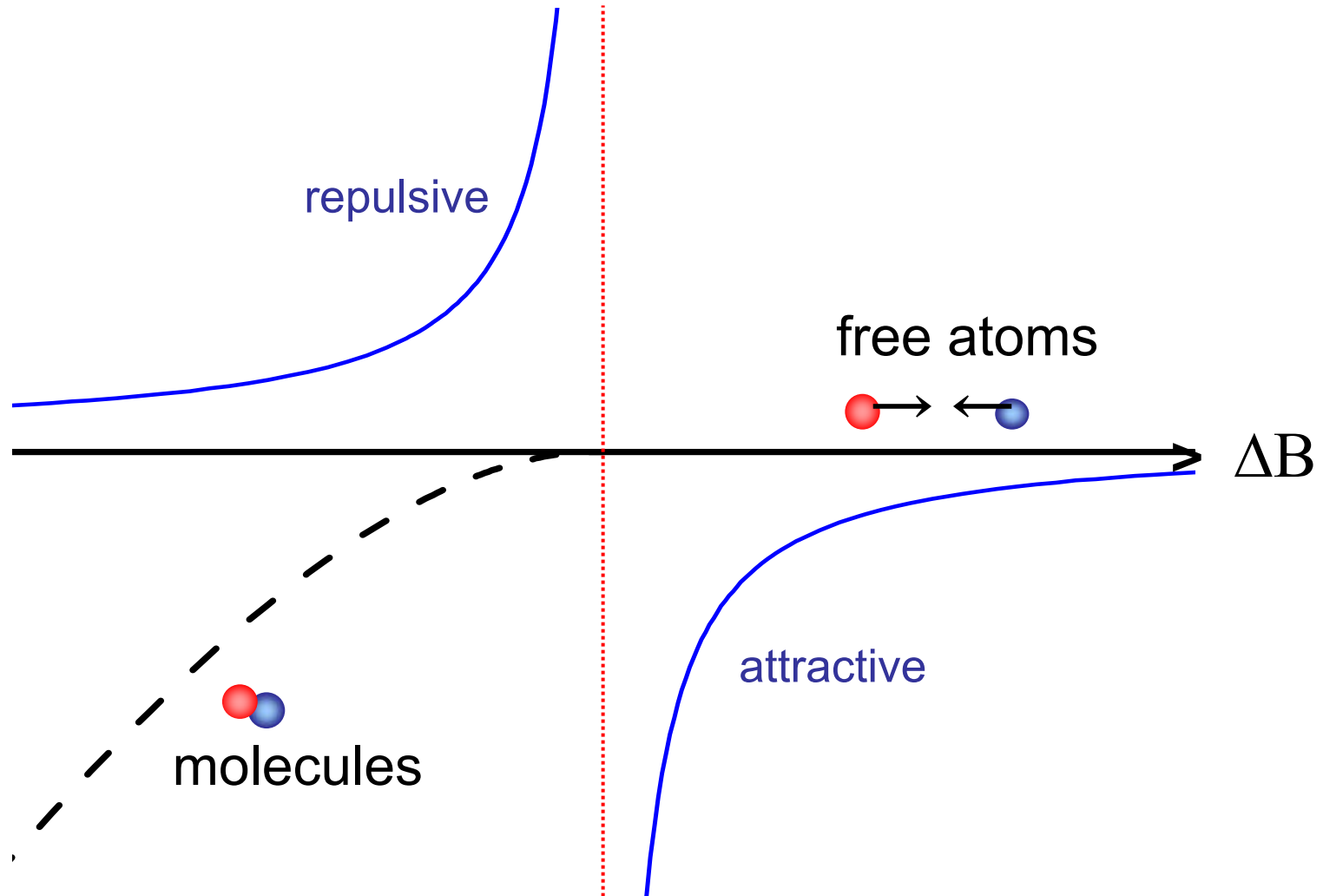


*scattering length*

# Magnetic-field Feshbach resonance



# Magnetic-field Feshbach resonance

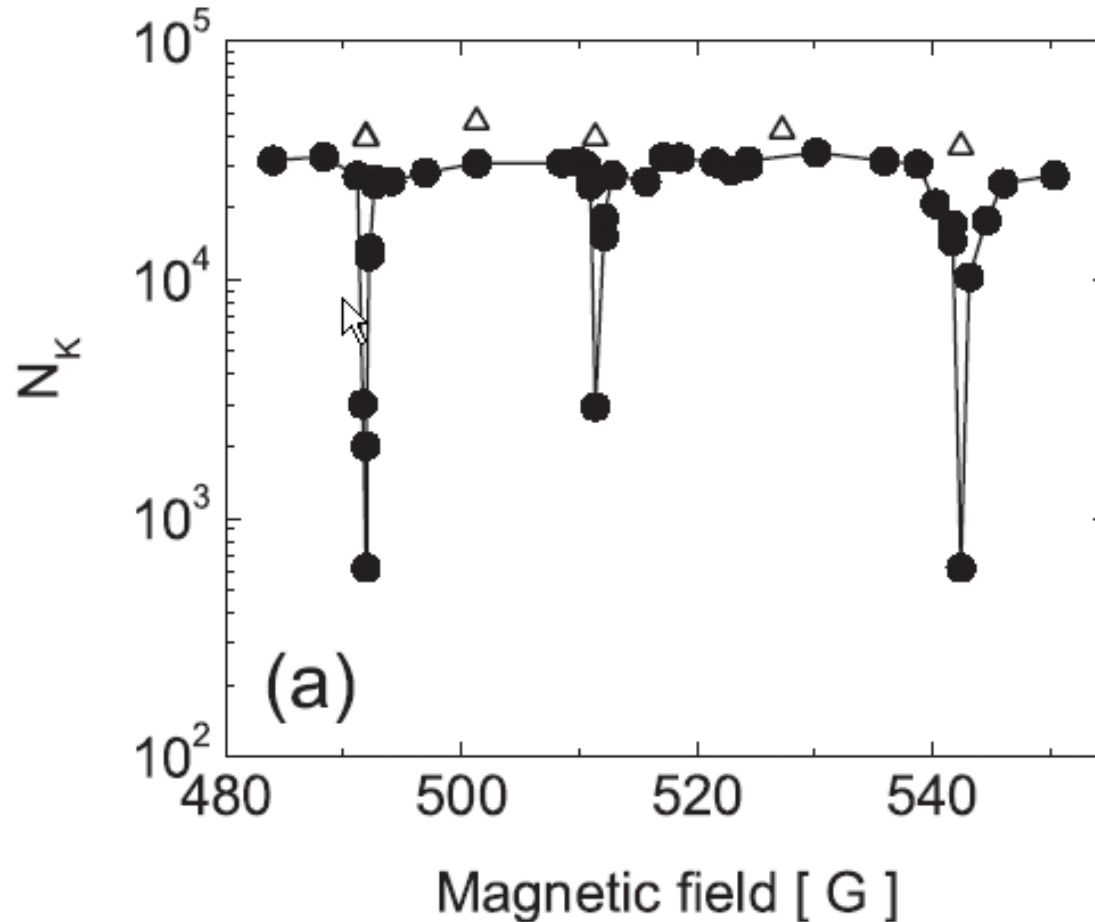




# Experimental observation

## 1. Trap Loss (3-body inelastic collisions)

three  $^{87}\text{Rb}$ - $^{40}\text{K}$  Feshbach resonances:

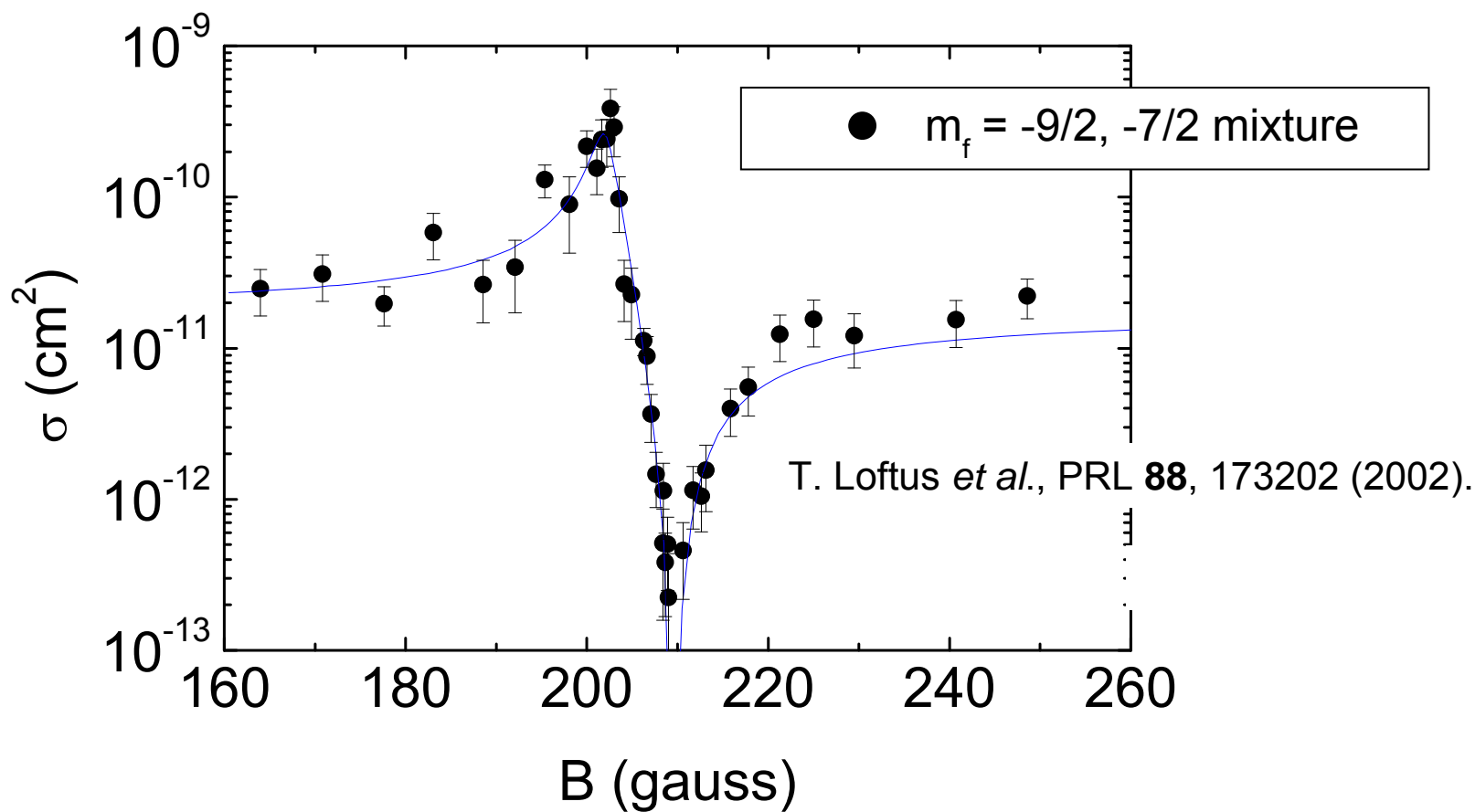


S. Inouye et al.,  
cond-mat, 2004.

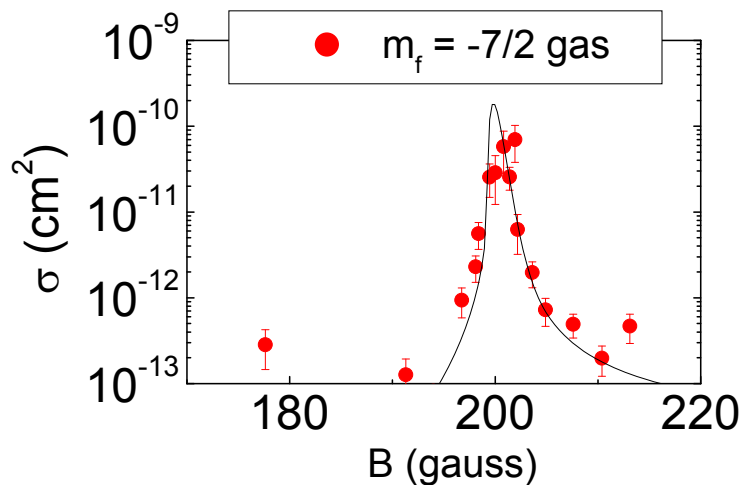


# Experimental observation

## 2. Elastic collision rate ( $\sigma=4\pi a^2$ )

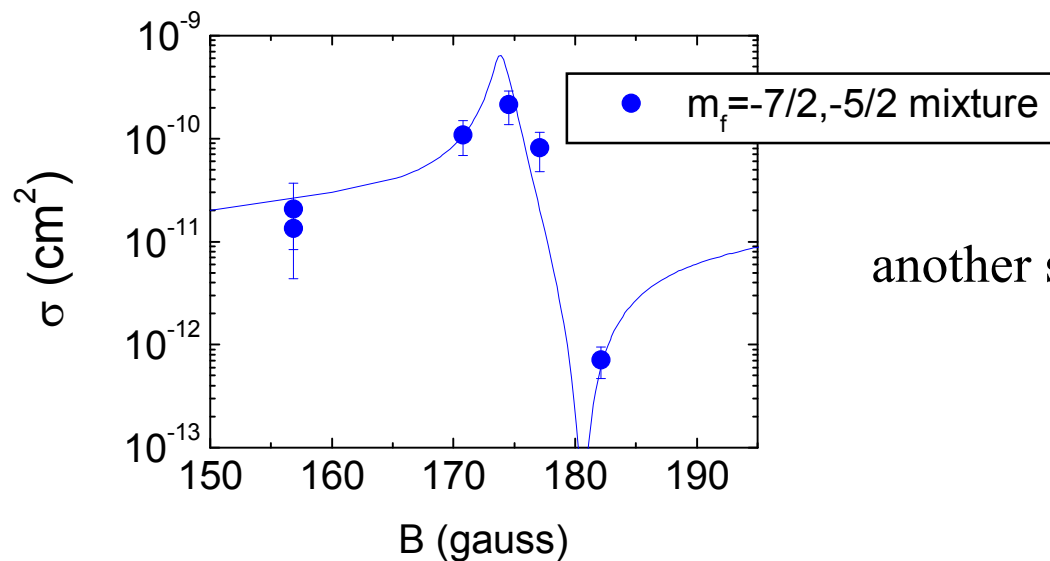


# More $^{40}\text{K}$ resonances



a p-wave resonance!

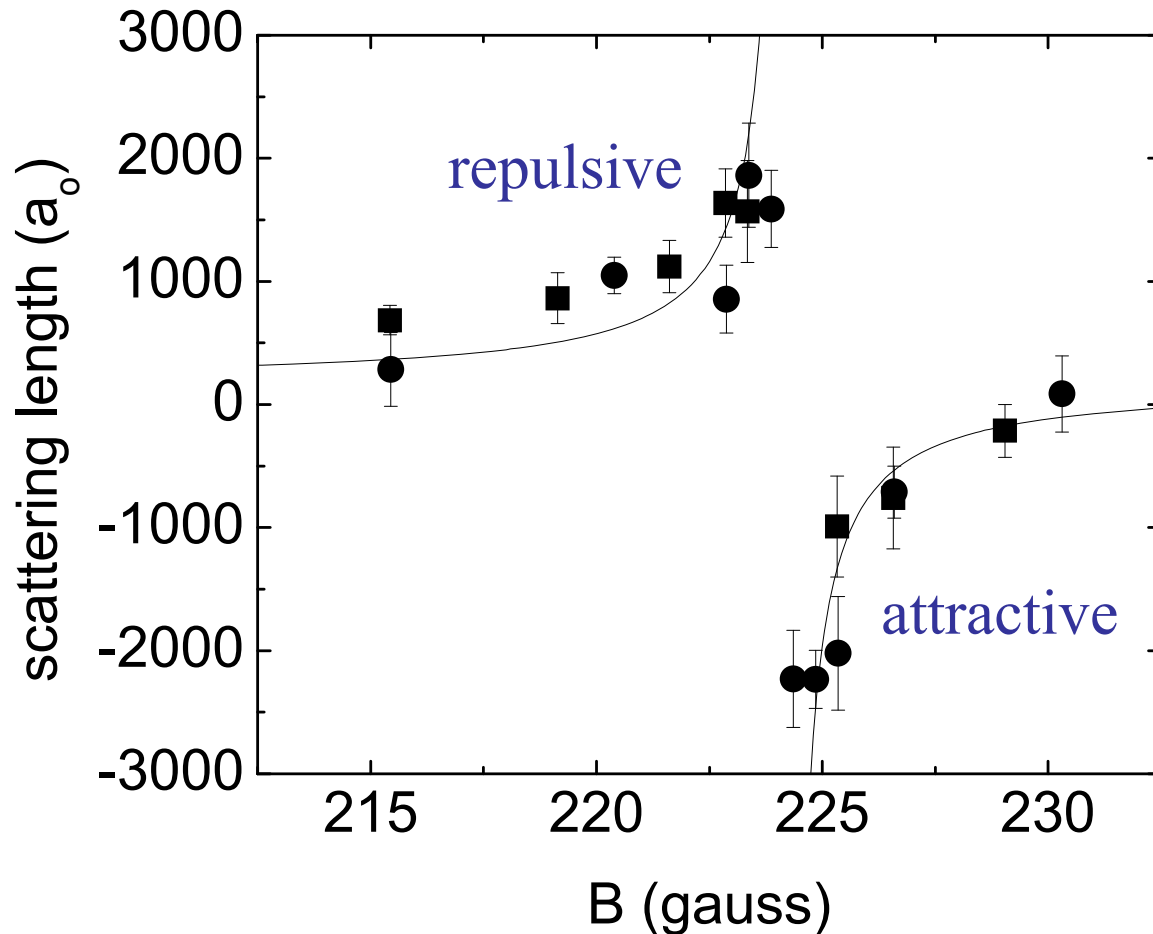
C. A. Regal *et al.*, PRL **90**, 053201 (2003)



another s-wave resonance

# Experimental observation

## 3. Interaction energy (RF spectroscopy)



Feshbach  
resonance between  
 $m_f = -9/2, -5/2$

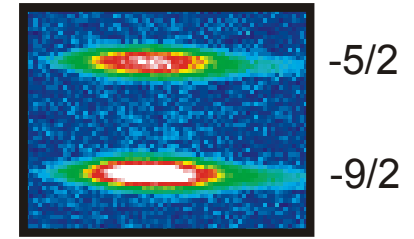
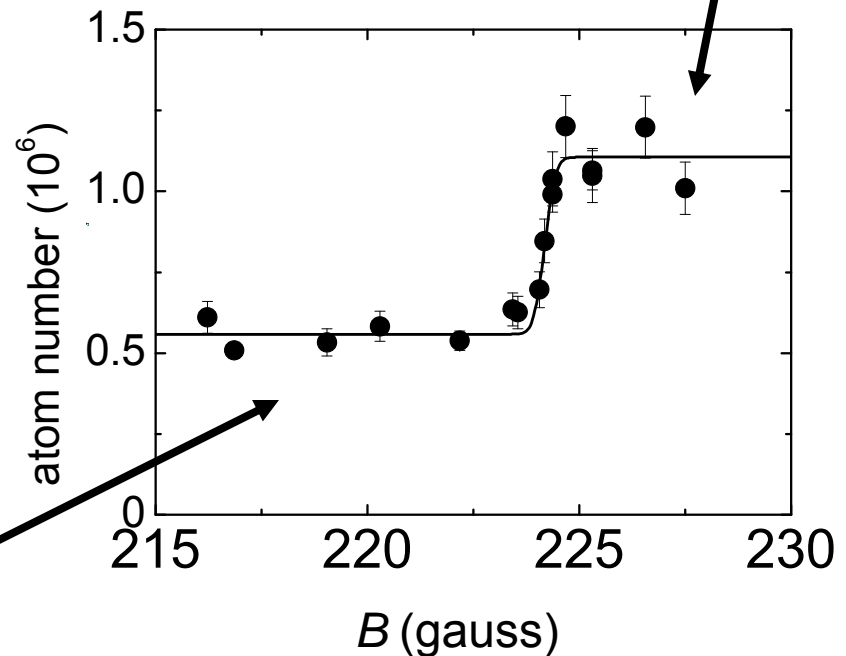
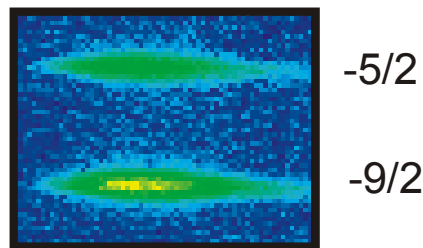
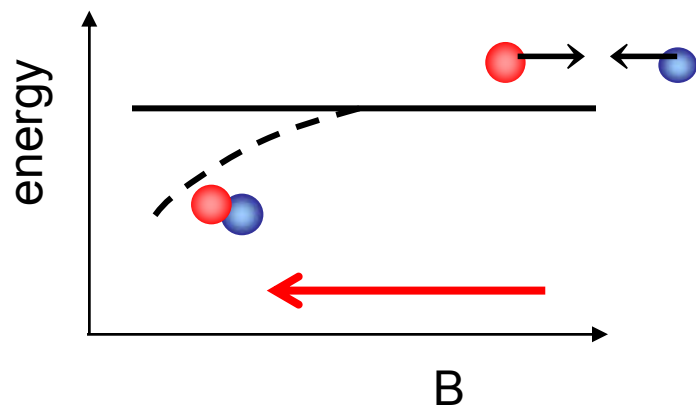
Use  $\Delta v \sim n_9 a_{59}$

C. A. Regal and D. S. Jin,  
PRL, (2003)

# Experimental observation

## 4. Molecule creation

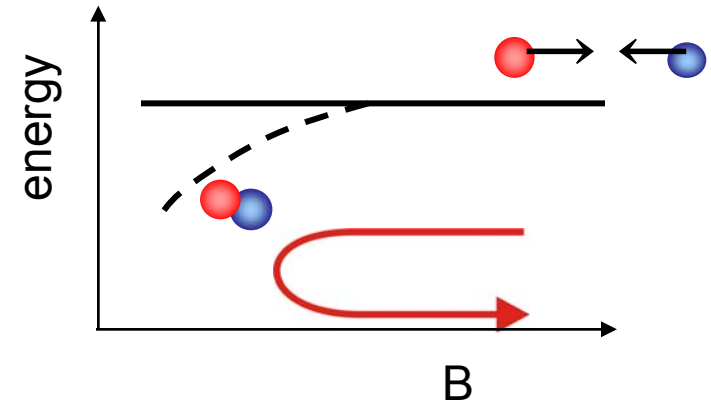
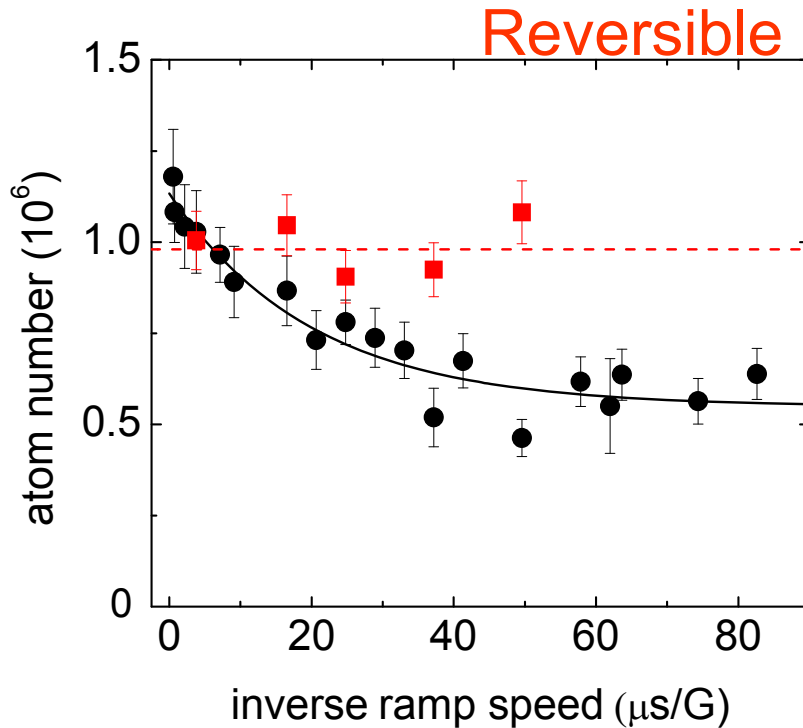
Ramp across Feshbach resonance from high to low B



C. A. Regal et al., *Nature* 424, 47 (2003).

Motivation: E. A. Donley et al., *Nature* 417, 529 (2002)

# Magnetic field sweep rate



Similar experiments:

Bosons

Innsbruck

Garching

JILA

Fermions

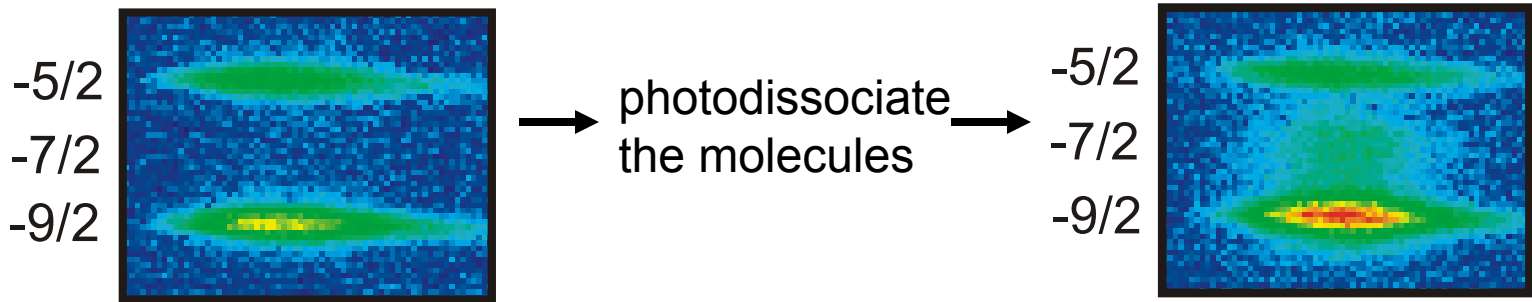
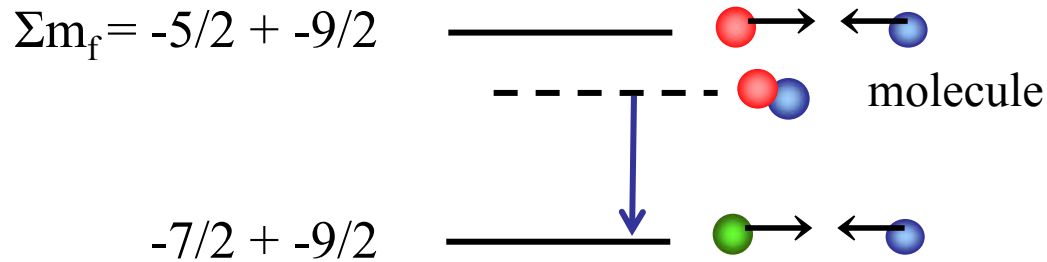
Rice

ENS

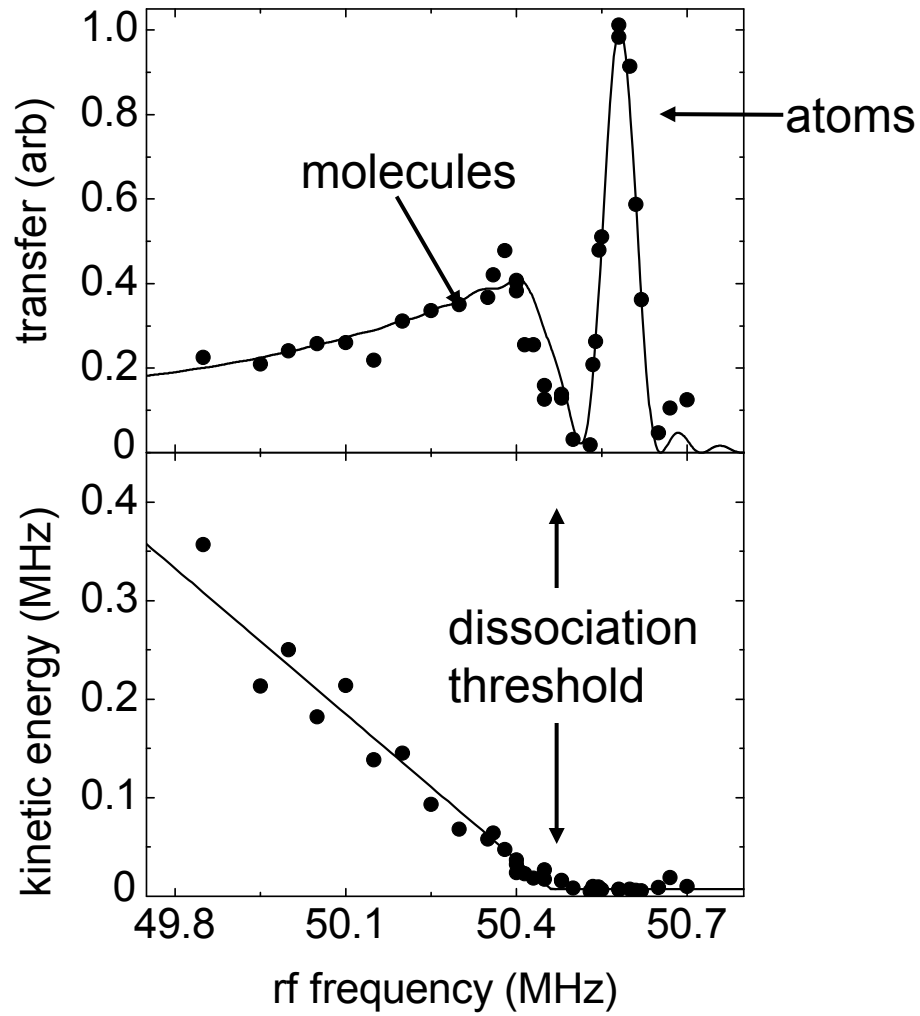
Innsbruck

# Molecule detection

- Apply RF near the atomic  $m_f = -5/2$  to  $m_f = -7/2$  transition

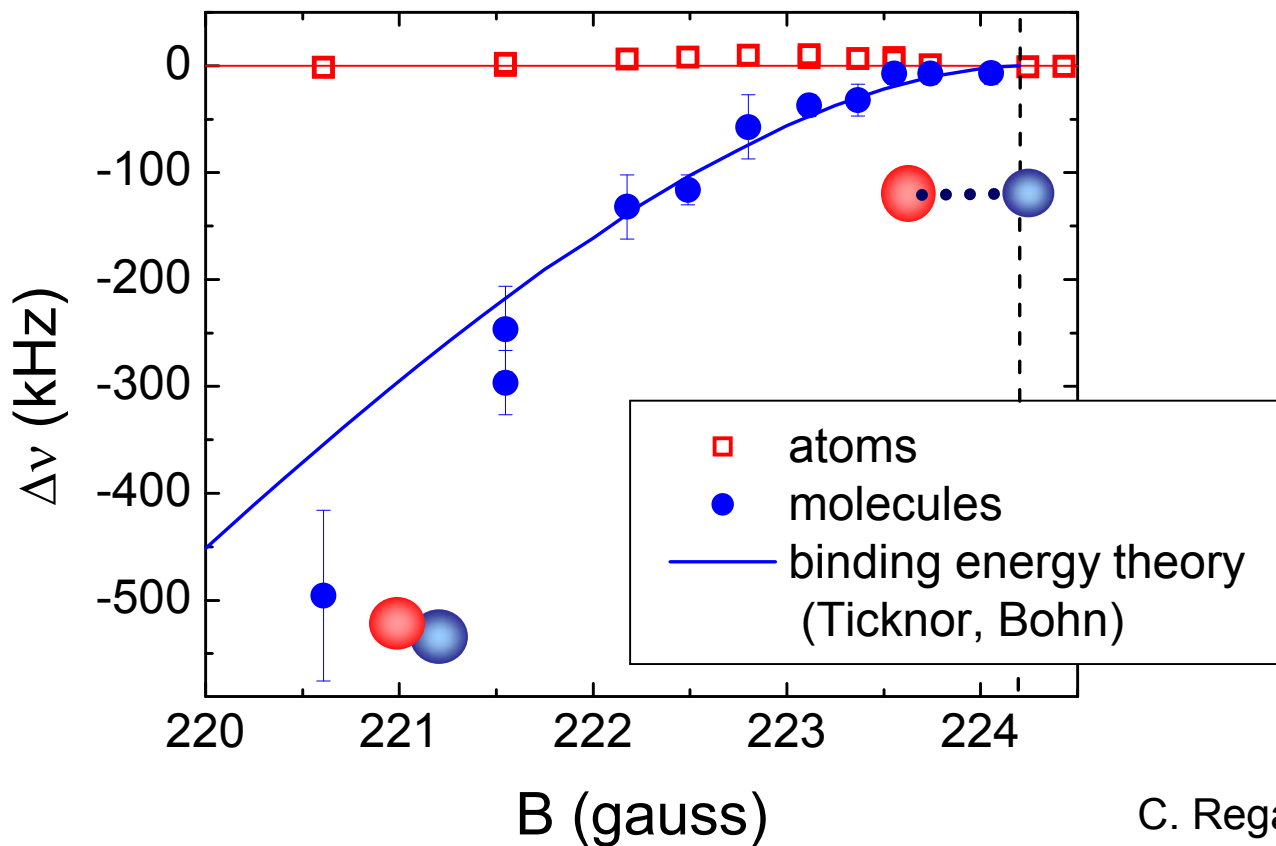


# Molecule detection





# Molecule binding energy

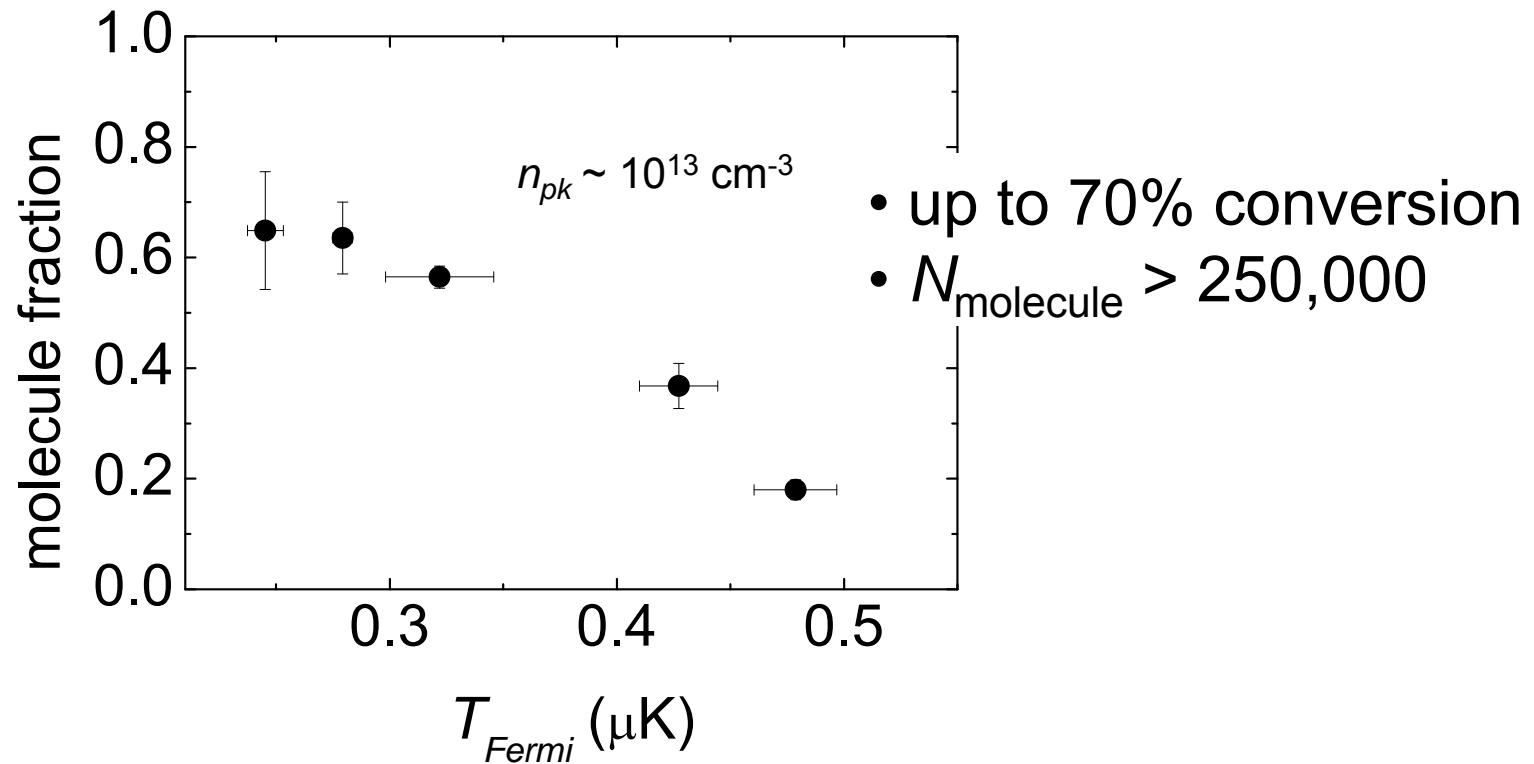


C. Regal *et al.*  
Nature 424, 47 (2003)

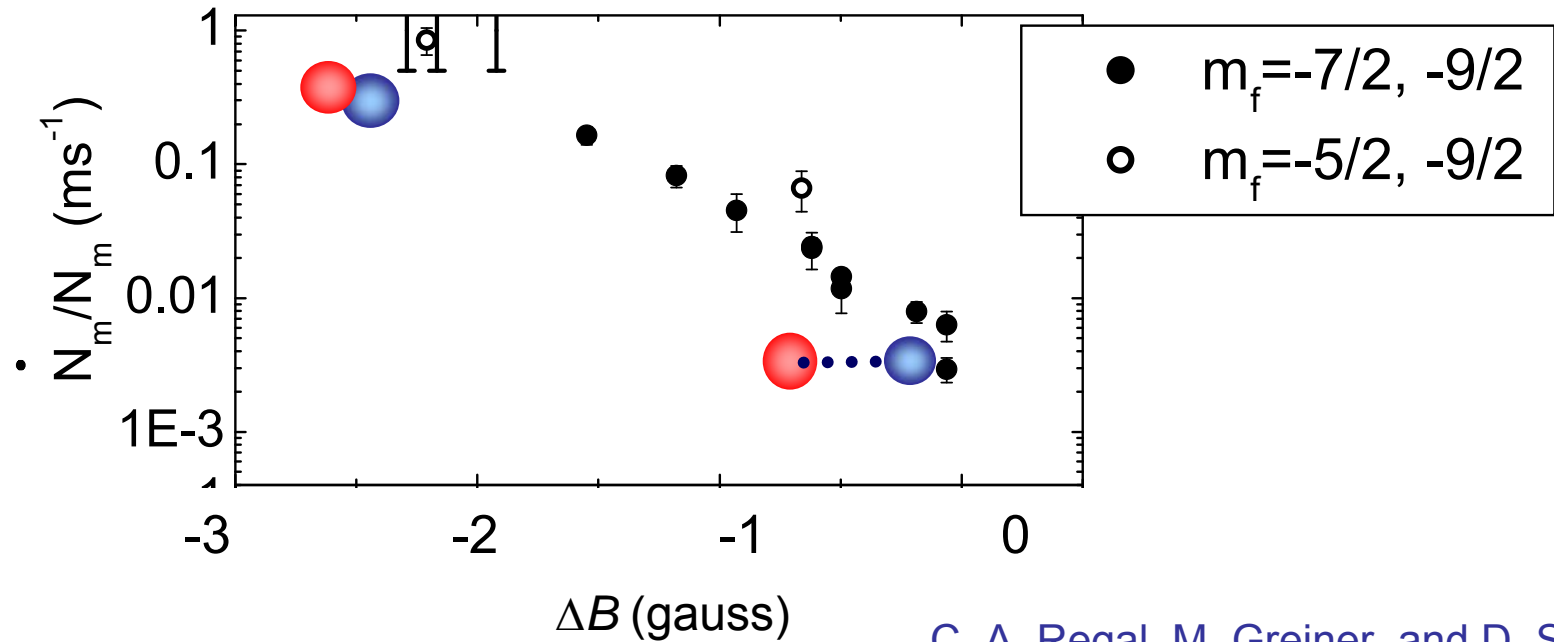
➤ extremely weakly bound !

# Molecule conversion efficiency

- depends strongly on energy of Fermi gas



# Molecule decay rate



C. A. Regal, M. Greiner, and D. S. Jin, PRL **92**, 083201 (2004)

Theory prediction: D.S. Petrov, C. Salomon, G.V. Shlyapnikov, cond-mat/0309010 (2003)

Expts: Rice, ENS, Innsbruck, JILA

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- (Experiments at JILA)

\$\$ NSF, NIST, Hertz

# III. BCS-BEC crossover

# Bose-Einstein condensation

BEC shows up in condensed matter, nuclear physics, elementary particle physics, astrophysics, and atomic physics.

Cooper pairs  
of electrons in  
superconductors

$^4\text{He}$  atoms  
in superfluid  
liquid He

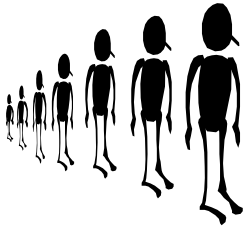
Excitons, biexcitons  
in semiconductors

Alkali atoms  
in ultracold  
atom gases

$^3\text{He}$  atom pairs  
in superfluid  
 $^3\text{He-A,B}$

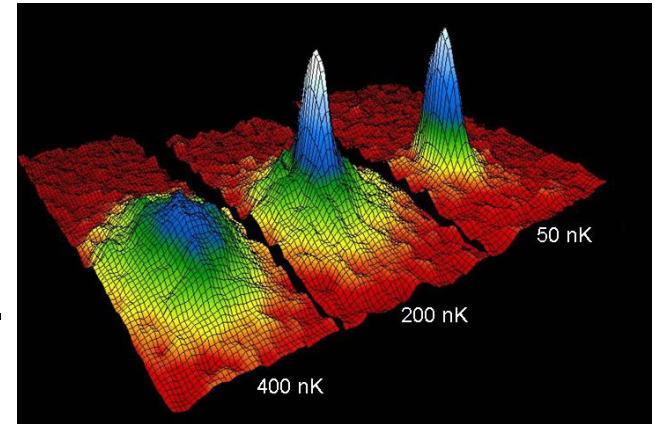
Neutron pairs,  
proton pairs in nuclei  
And neutron stars

Mesons in  
neutron star  
matter

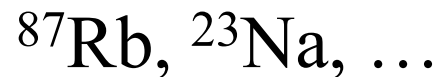


# Bosons and Fermions

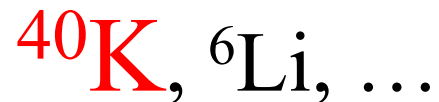
- Condensation requires bosons.
- Material bosons are composite particles, made up of fermions.



➤ For a gas of bosonic atoms, the underlying fermion degrees of freedom are not accessible.



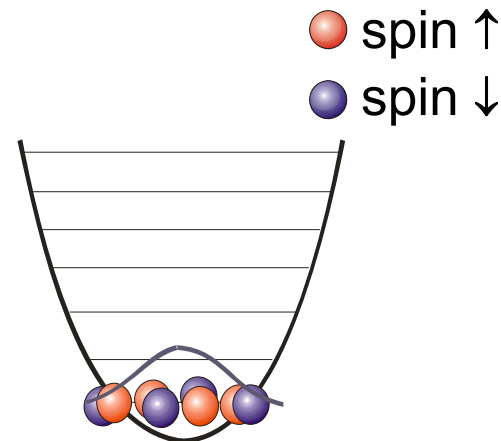
➤ By starting with a gas of fermionic atoms we can explore how bosonic degrees of freedom emerge.



# Making condensates with fermions

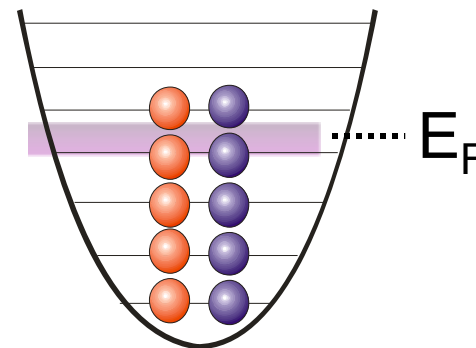
## ➤ BEC of diatomic molecules

1. Bind fermions together.
2. BEC



## ➤ BCS superconductivity/superfluidity

Condensation of Cooper pairs of atoms  
(pairing in momentum space,  
near the Fermi surface)

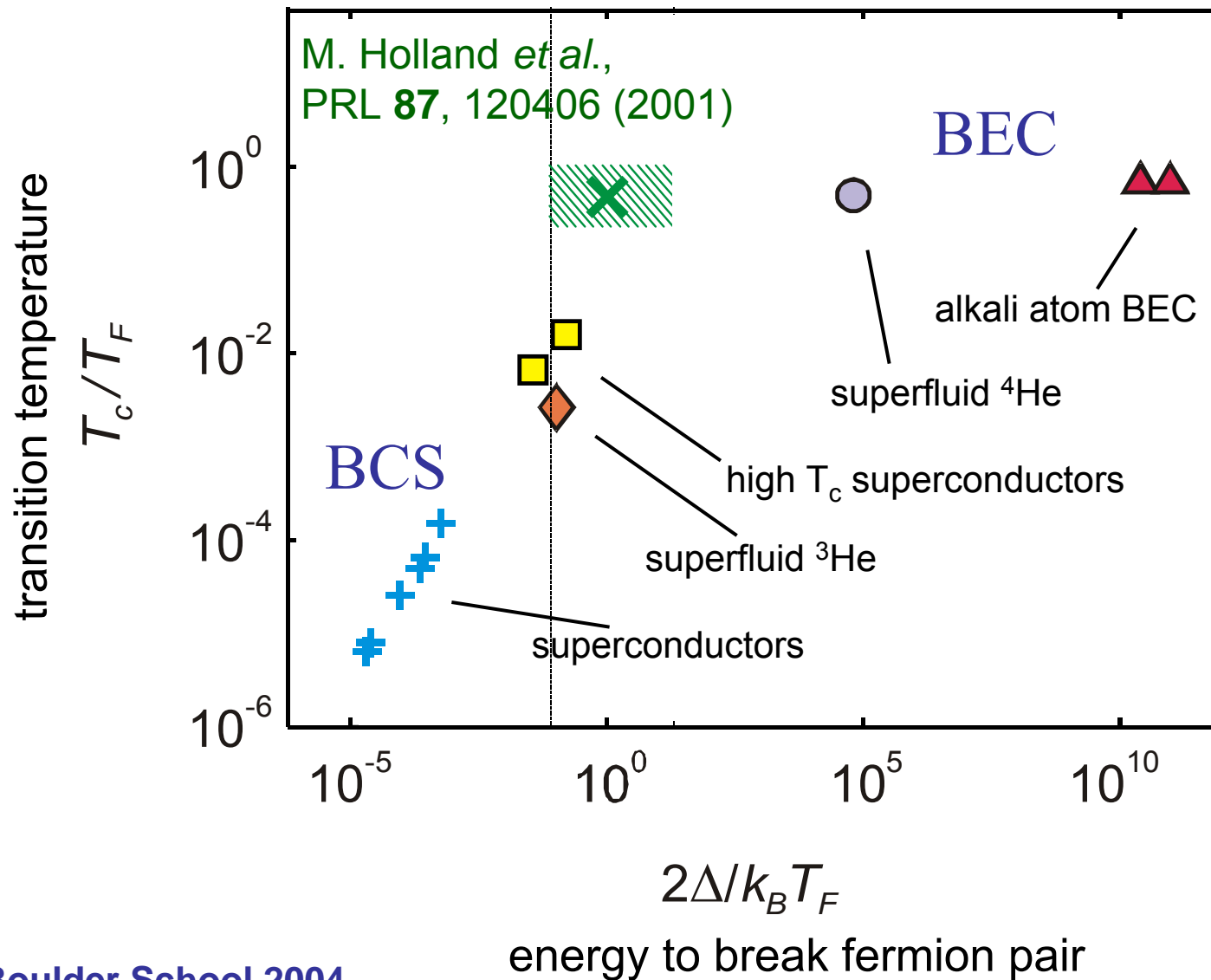


## ➤ Something in between?

BCS-BEC crossover



# BCS-BEC landscape



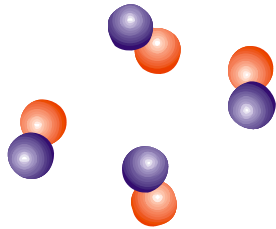
# Pairing and Superfluidity

→ Spin is additive: Fermions can pair up and form effective bosons:

$$\Psi(1, \dots, N) = \hat{A} [ \phi(1,2) \phi(3,4) \dots \phi(N-1,N) ]$$

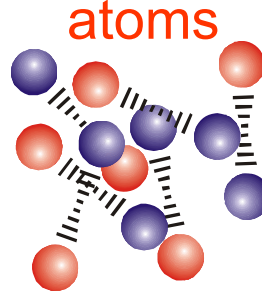
● spin ↑  
● spin ↓

Molecules of fermionic atoms



**BEC** of weakly bound molecules

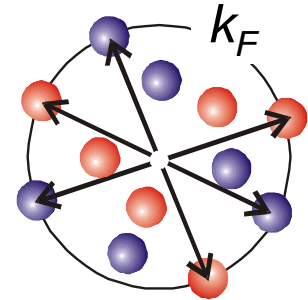
Generalized Cooper pairs of fermionic atoms



**BCS - BEC crossover**



Cooper pairs



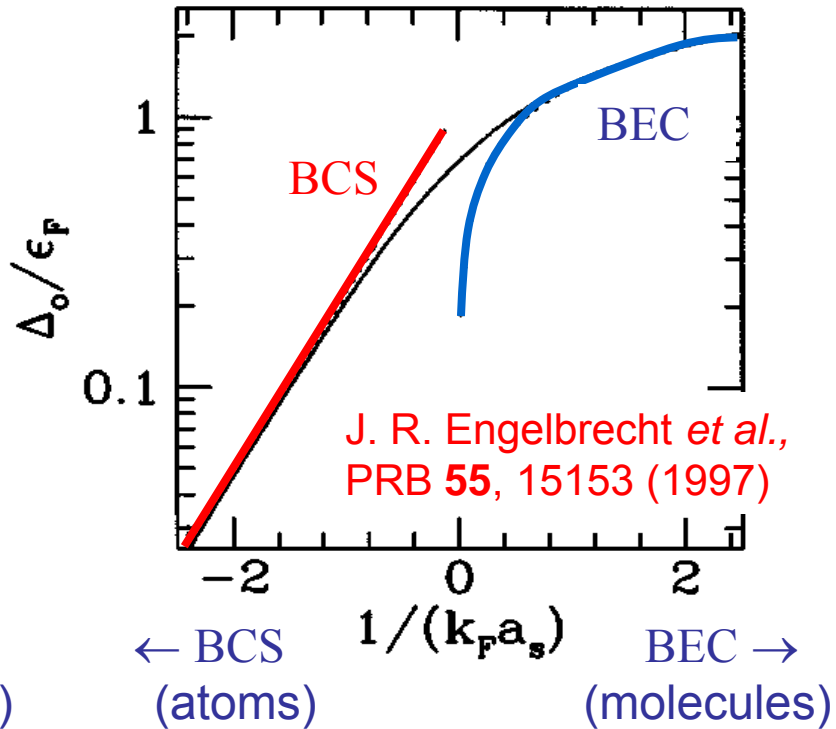
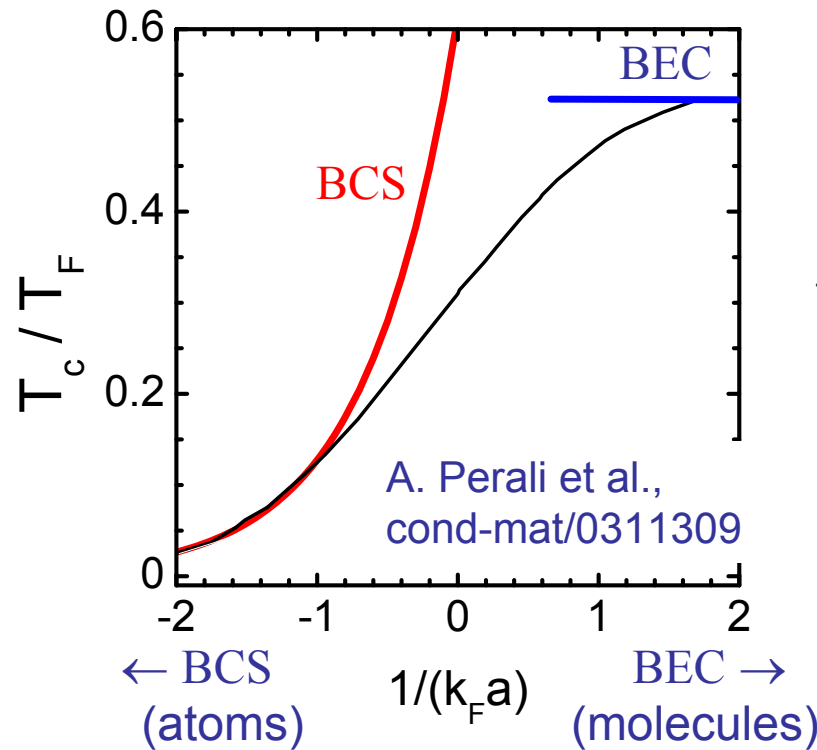
**BCS** superconductivity  
Cooper pairs: correlated momentum-space pairing

**BCS-BEC crossover for example:**

Eagles, Leggett, Nozieres and Schmitt-Rink, Randeria, Strinati, Zwirger, Holland, Timmermans, Griffin, Levin ...  
Boulder School 2004

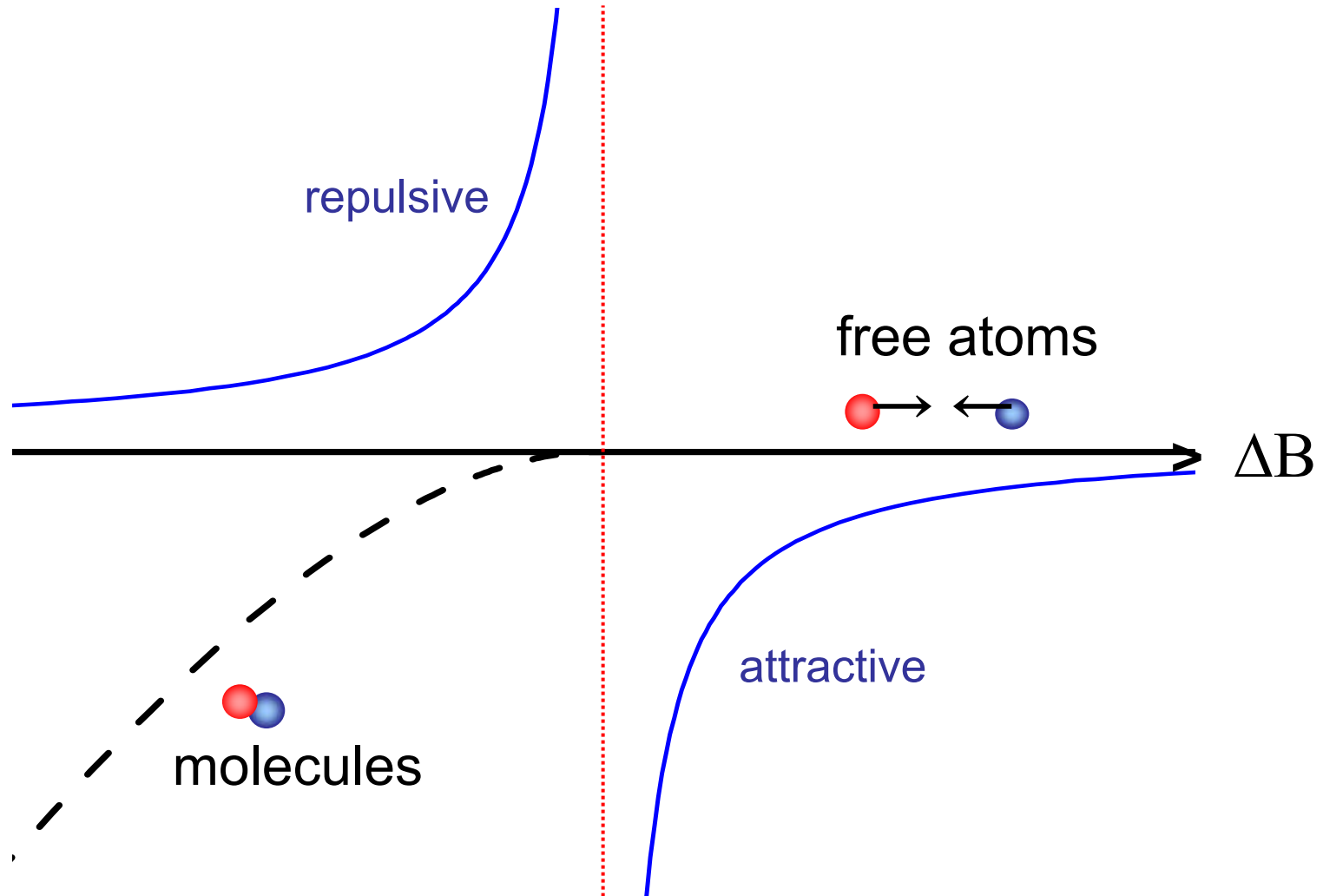
# BCS-BEC crossover

Predict a smooth connection between BCS and BEC

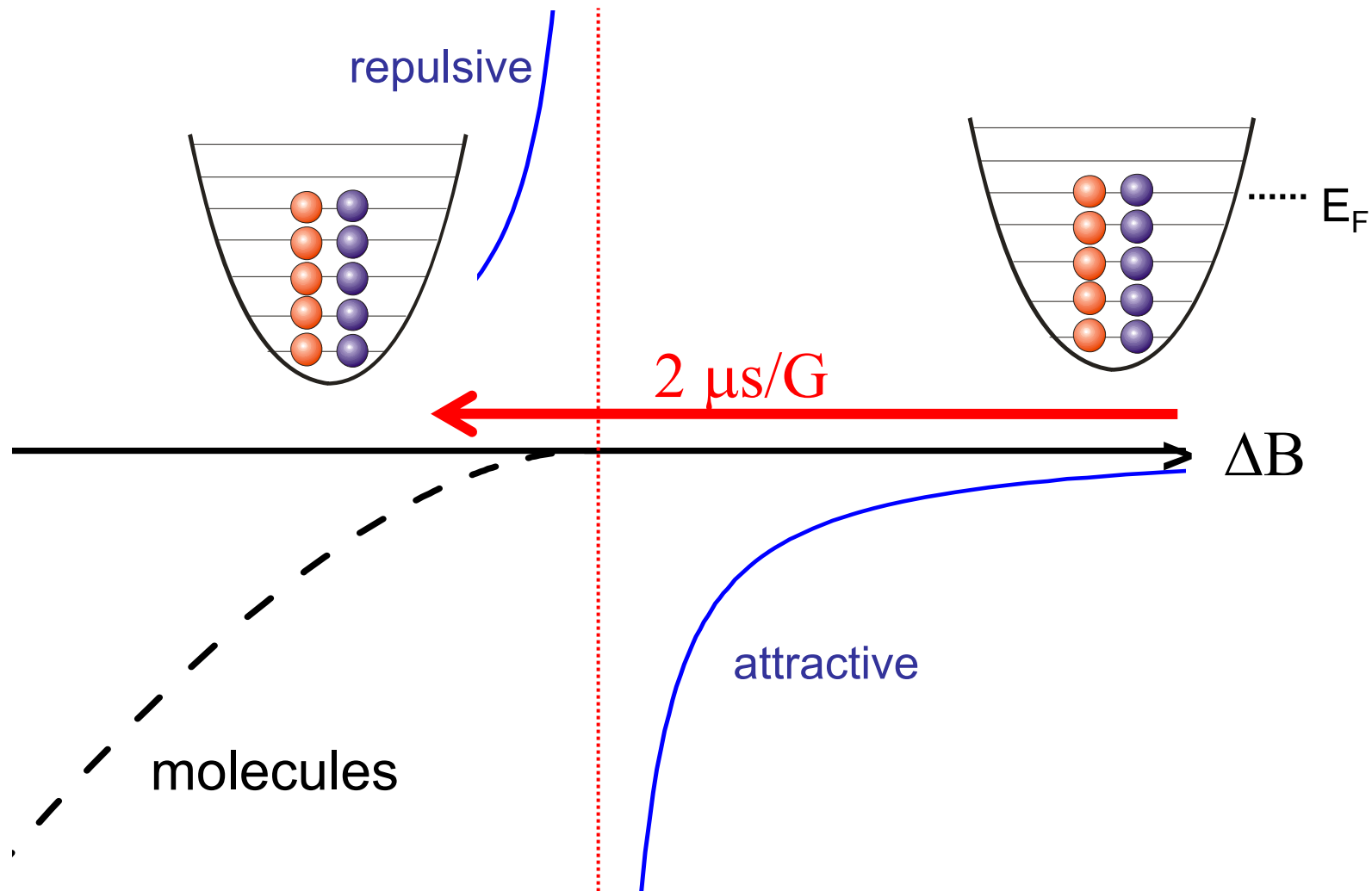


partial list: Eagles, Leggett, Nozieres and Schmitt-Rink, Randeria, Haussman, Strinati, Holland, Timmermans, Griffin, Levin, ...

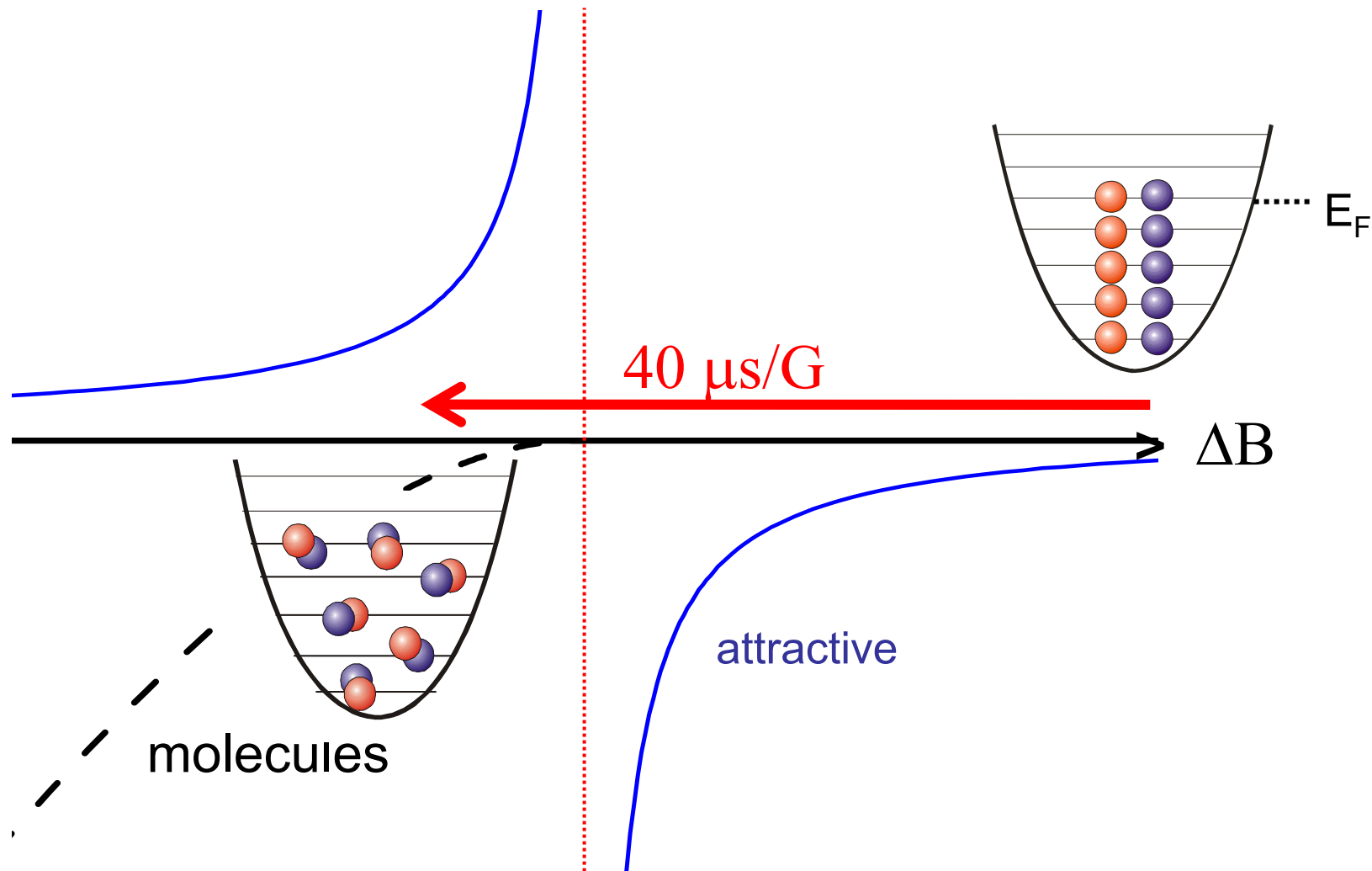
# Magnetic-field Feshbach resonance



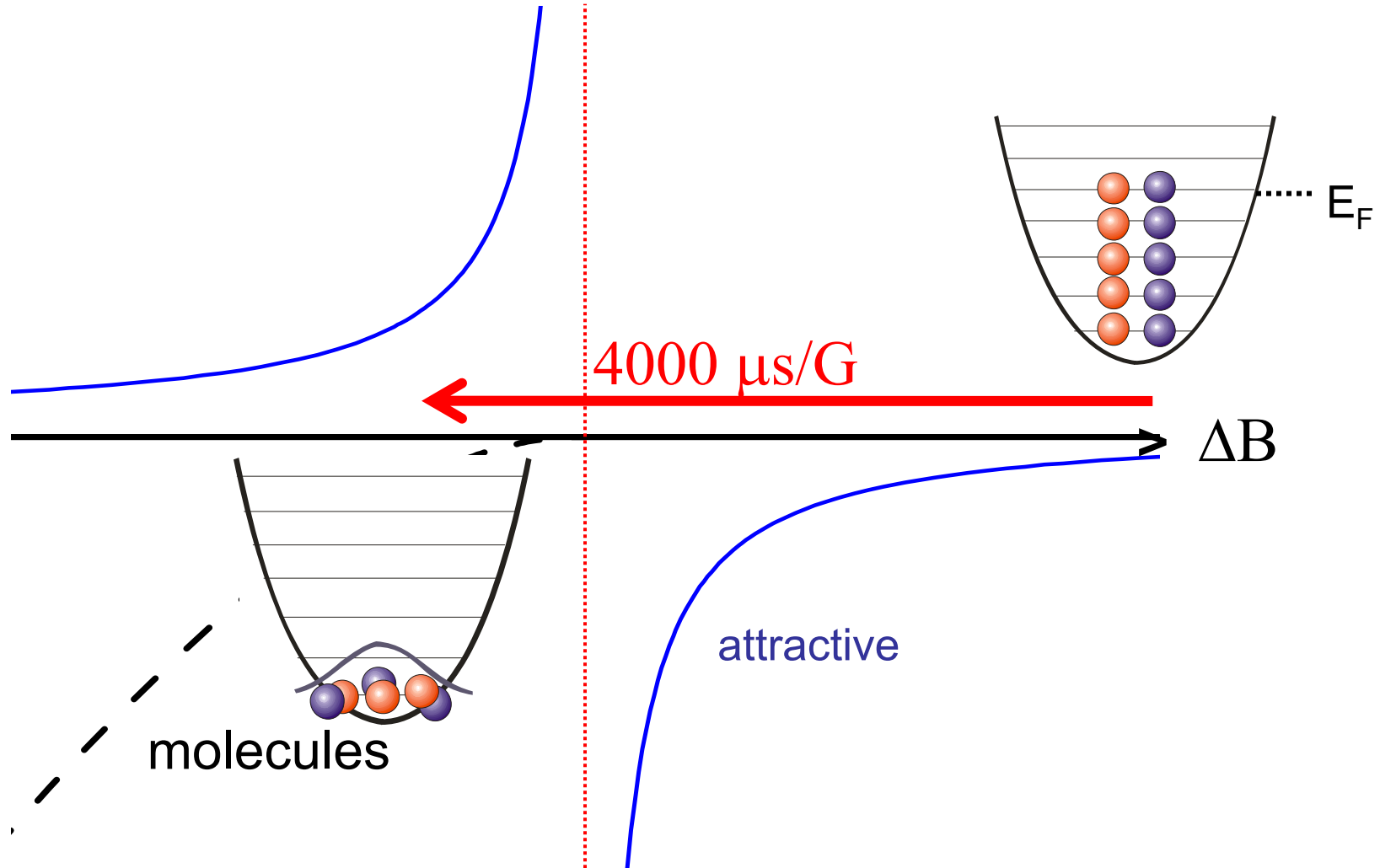
# Changing the interaction strength in real time: FAST



# Changing the interaction strength in real time: SLOW



# Changing the interaction strength in real time: SLOWER



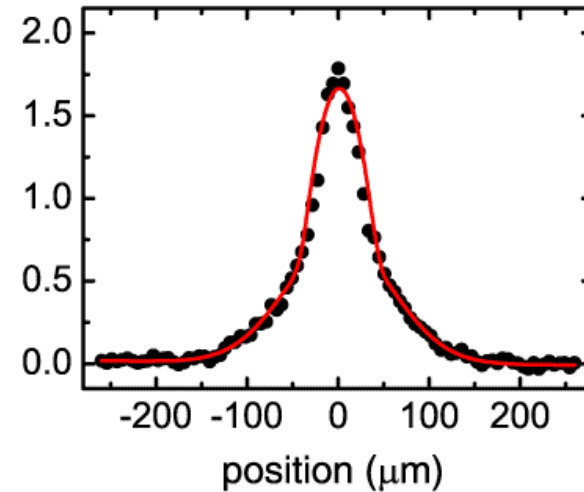
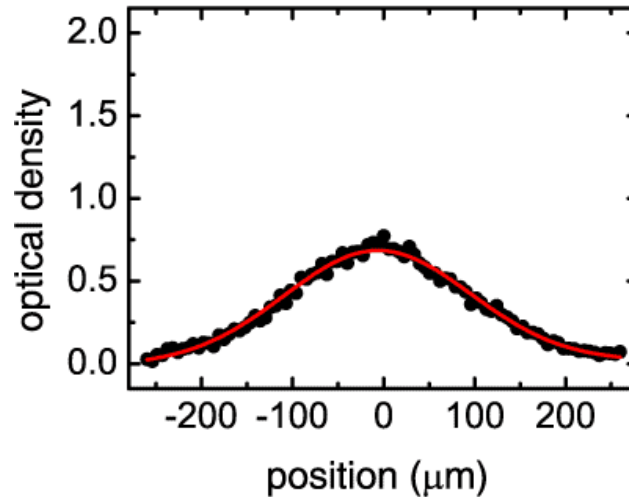
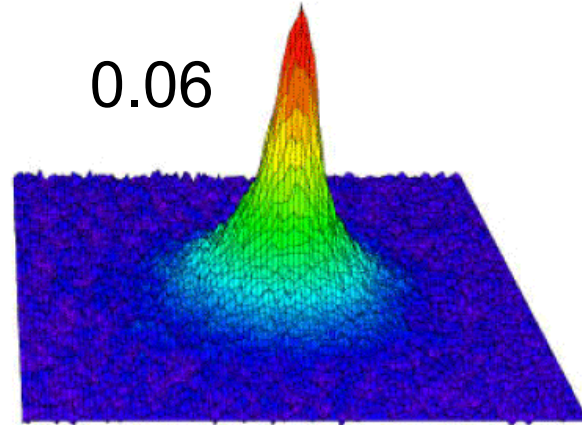
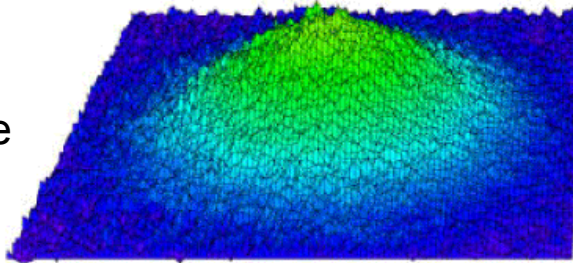
Cubizolles *et al.*, PRL **91**, 240401 (2003); L. Carr *et al.*, cond-mat/0308306

# Molecular Condensate

initial  $T/T_F$ : 0.19

0.06

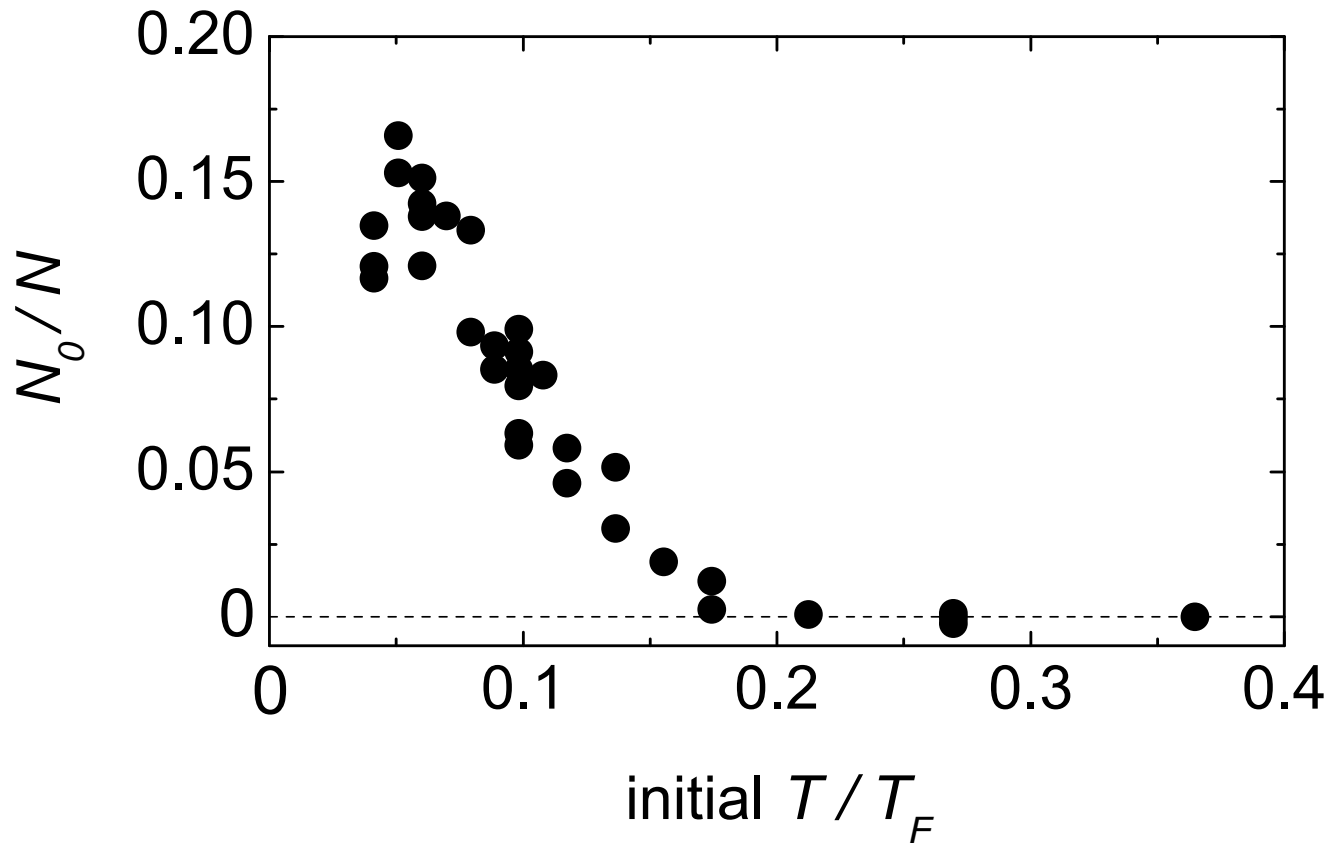
Time of flight  
absorption image



M. Greiner, C.A. Regal, and D.S. Jin, *Nature* **426**, 537 (2003).

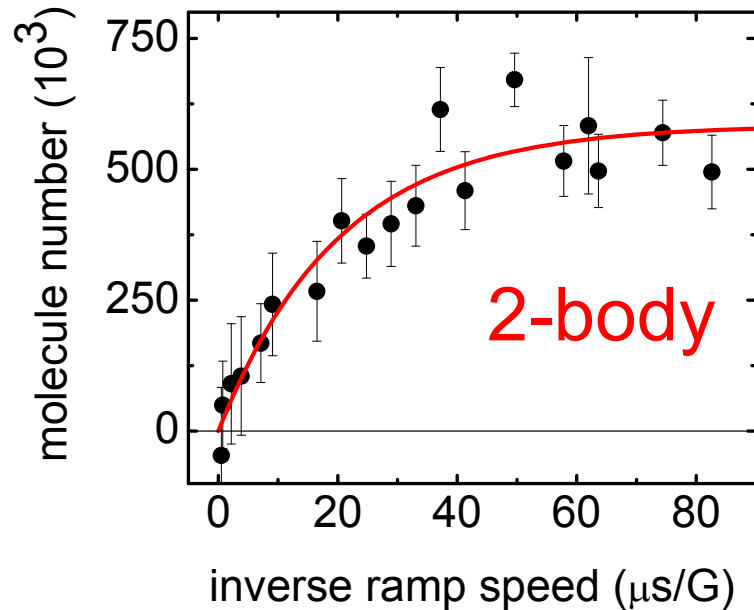
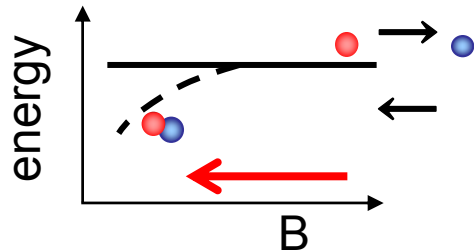


# A BEC from a Fermi Sea!

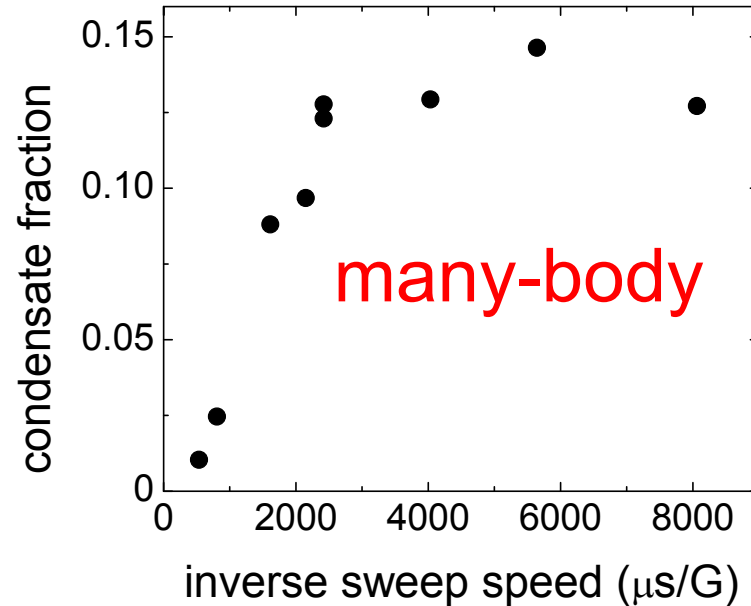
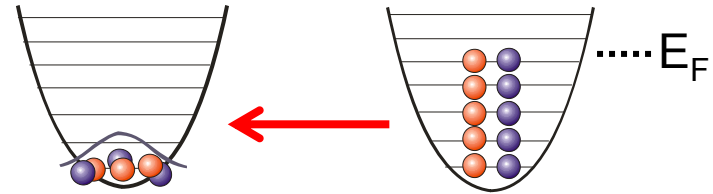


# Timescales

## Creating molecules

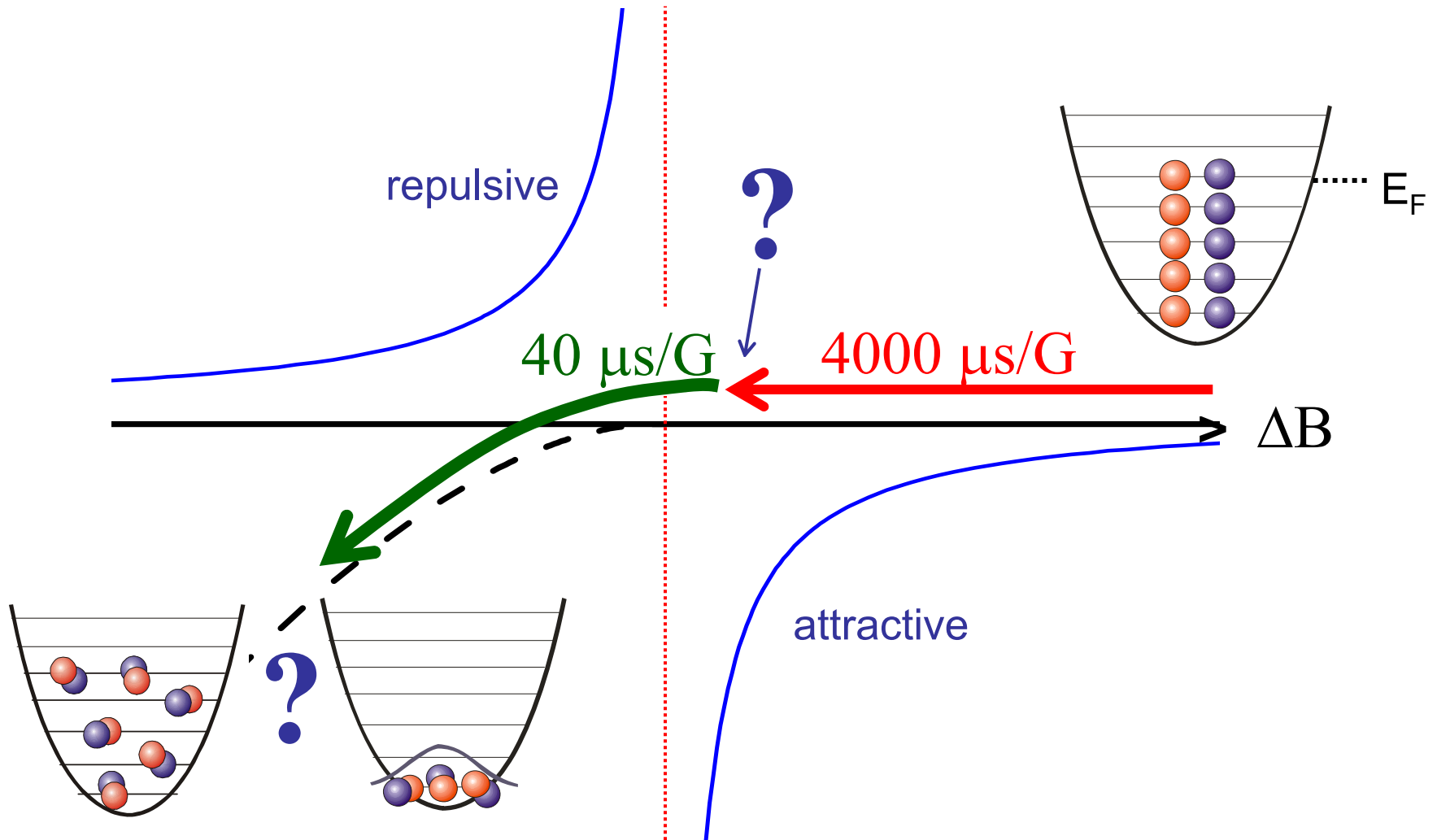


## Creating molecular BEC

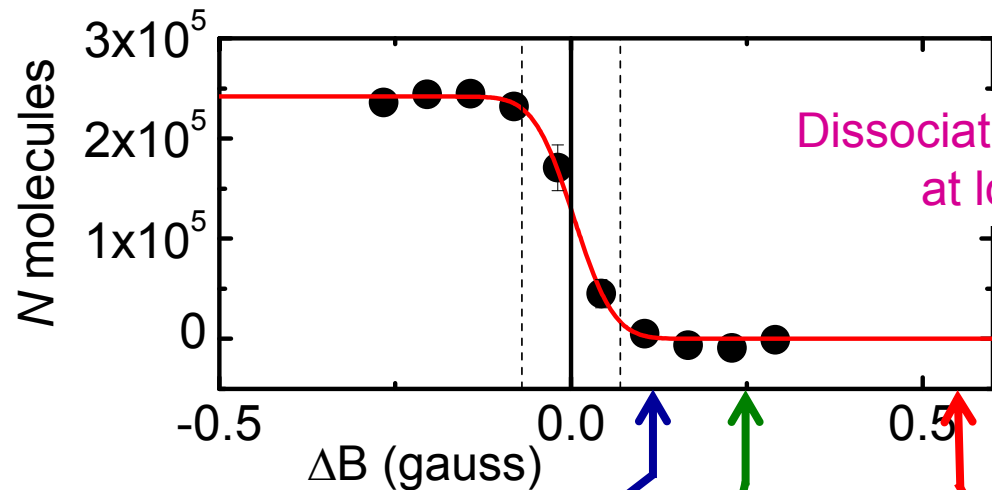


➤ two orders of magnitude difference in timescales!

# Observing a Fermi condensate

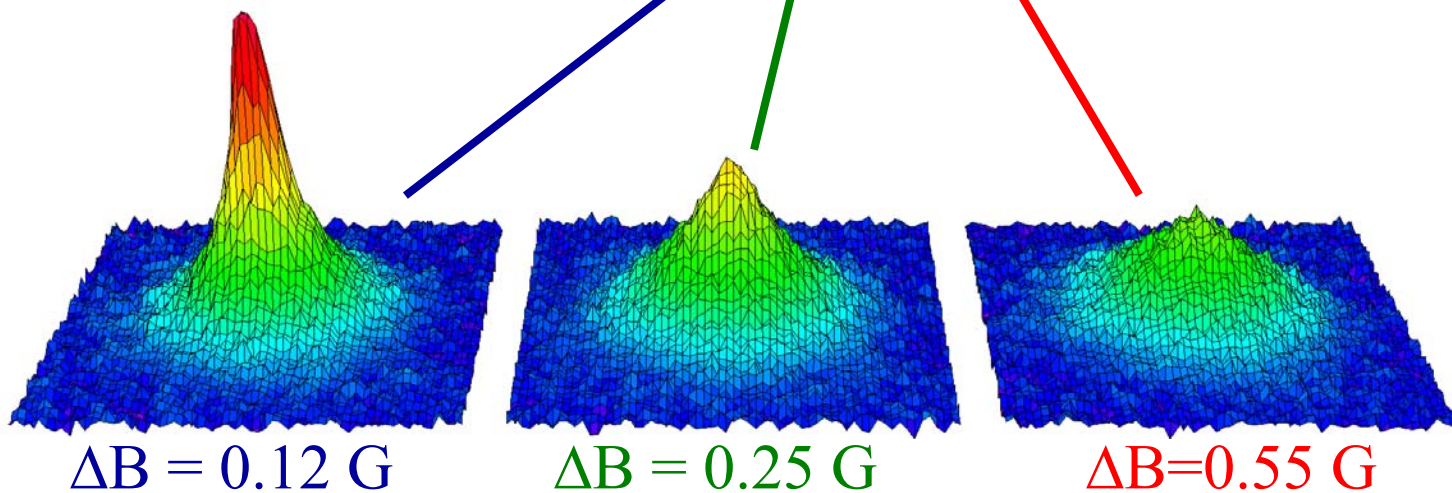


# Condensates w/o a two-body bound state



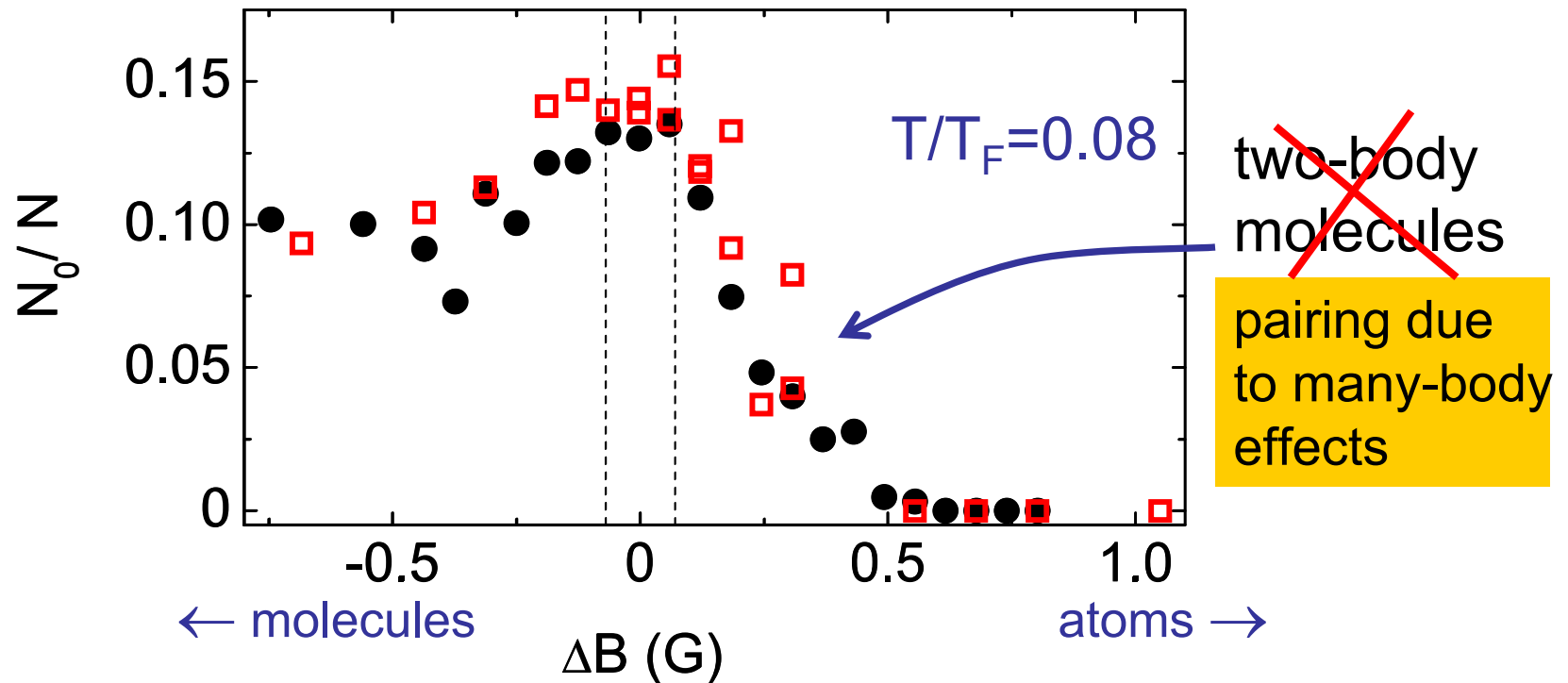
Dissociation of molecules  
at low density

C. Regal, M. Greiner,  
and D. S. Jin, PRL **92**,  
040403 (2004)



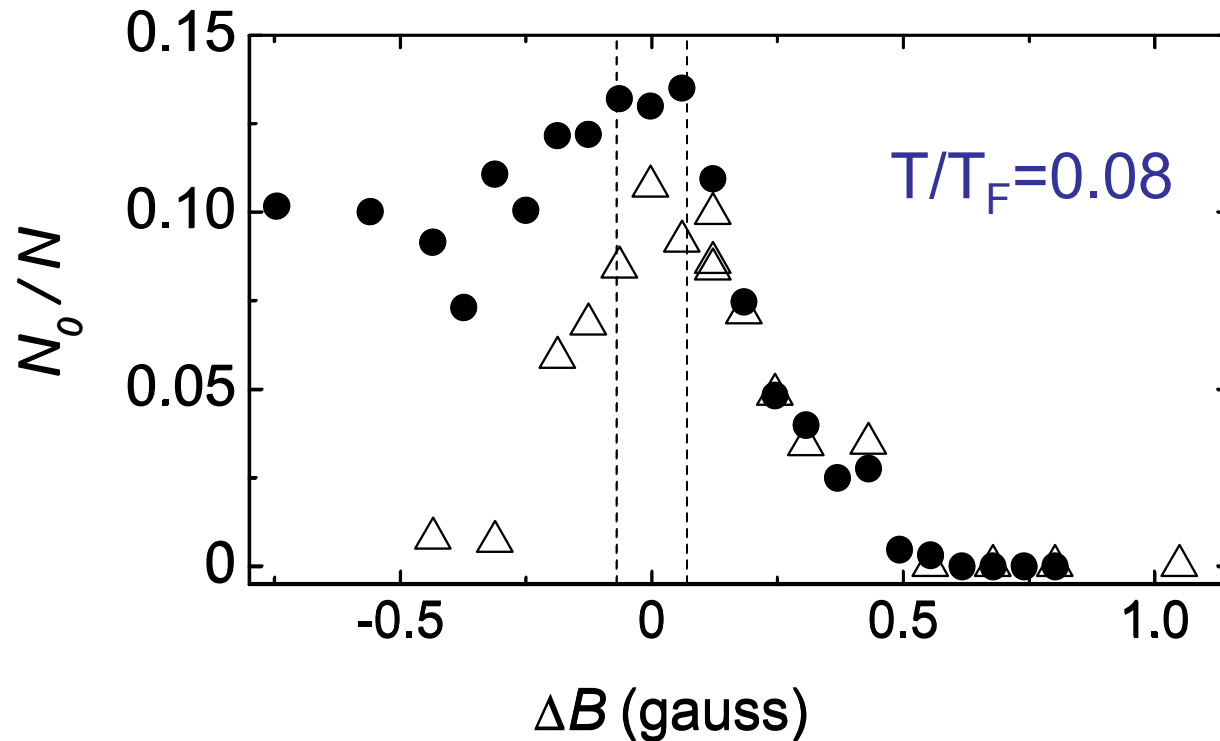
$$T/T_F = 0.08$$

# Fermionic condensate



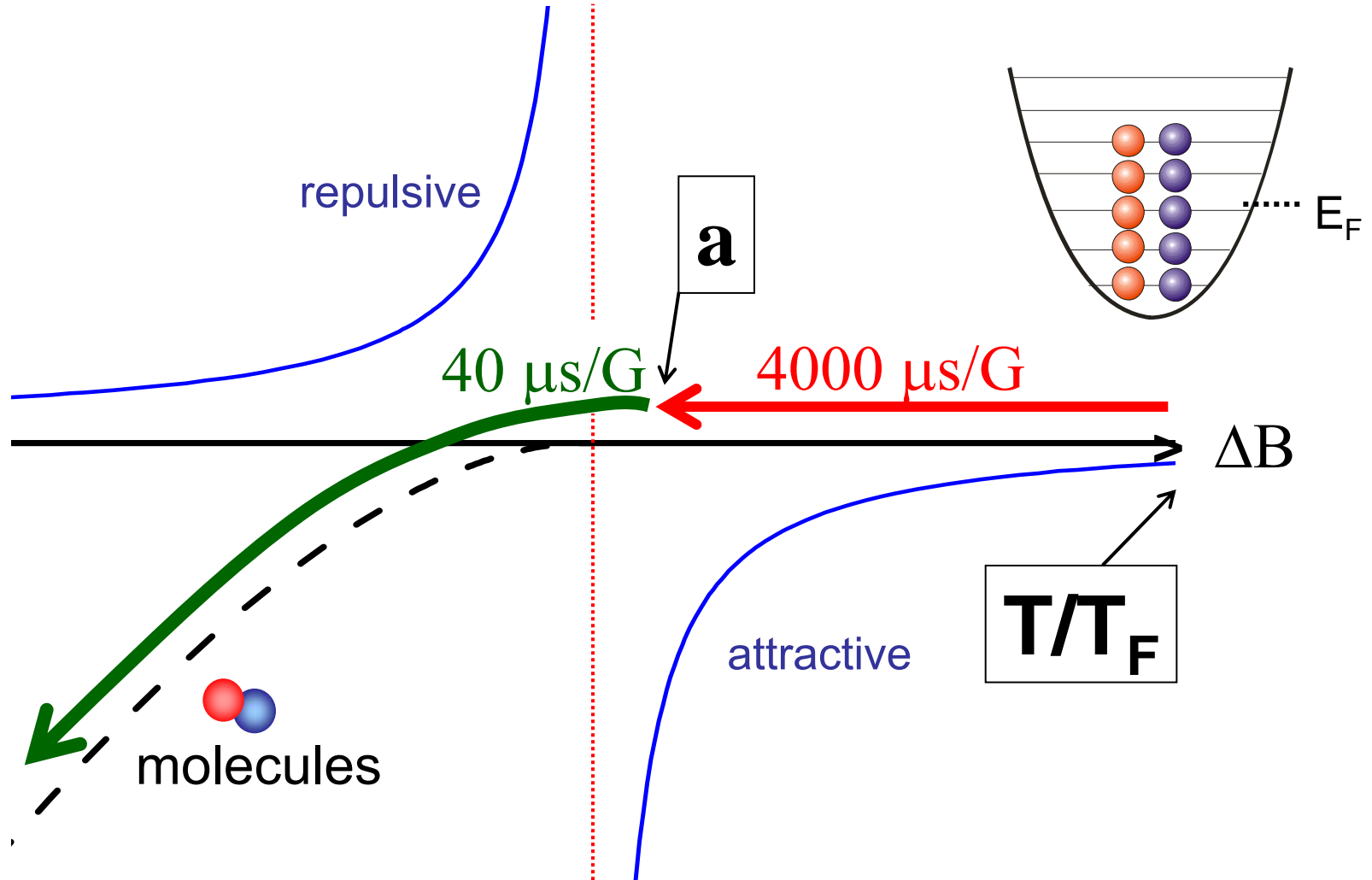
- Clearly see condensation on the “atom-side” of the resonance!

# Fermionic condensate

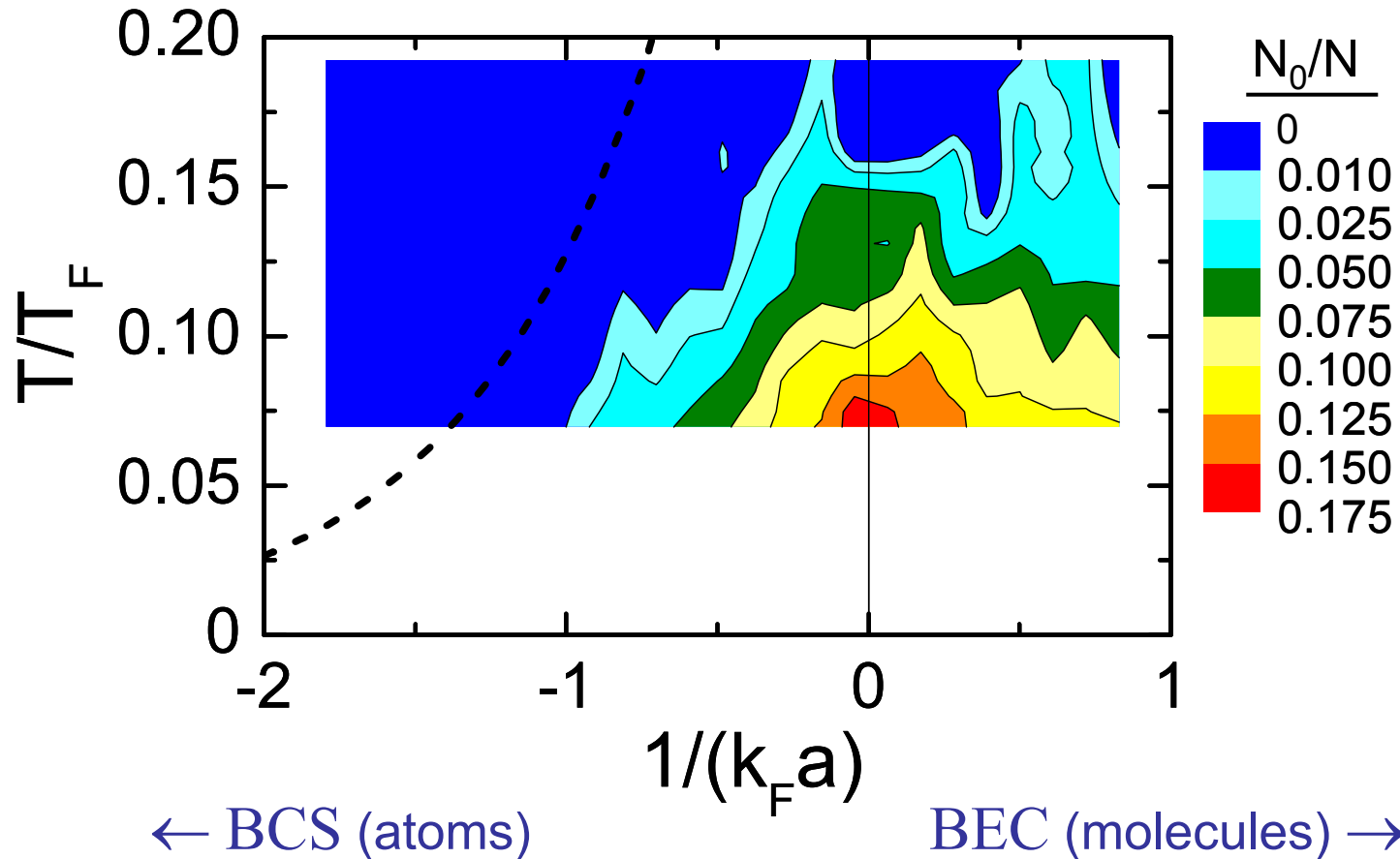


- Clearly see condensation on the “atom-side” of the resonance!
- Condensate lives much longer near resonance than in BEC limit.

# Mapping out a phase diagram



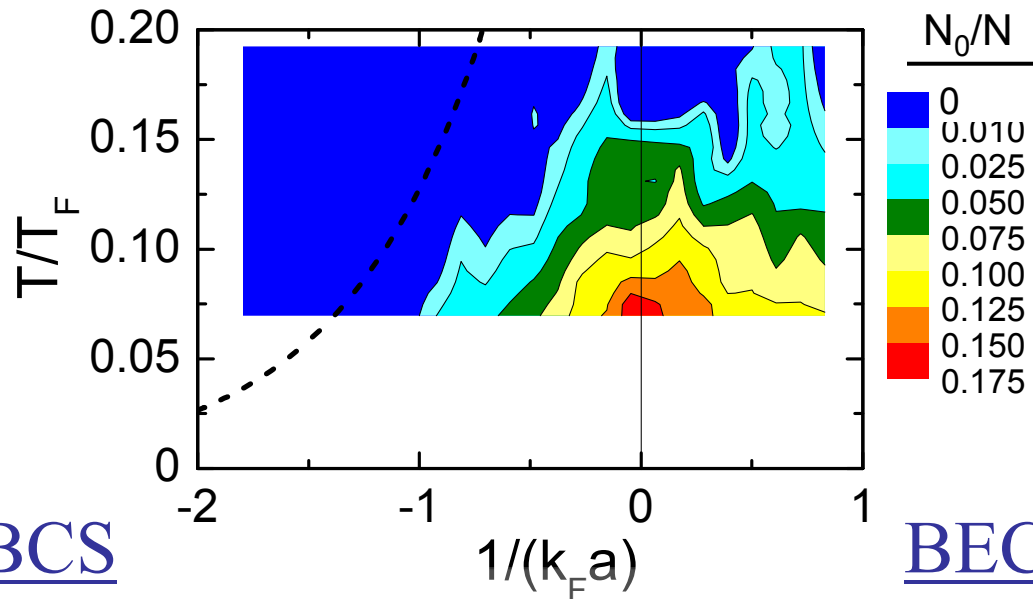
# BCS-BEC Crossover



C. Regal, M. Greiner, and D. S. Jin, PRL **92**, 040403 (2004)



# BCS-BEC Crossover



←BCS

Cooper pairs:

collective, many-body effect  
weakly bound  
(pairing in momentum-space)  
pair size  $\gg n^{-1/3}$

$$T_c/T_F \ll 1$$

$$T_{\text{pairing}} = T_c$$

Fermion excitations

BEC→

diatomic molecules:

two-body effect  
tightly bound  
(pairing in real space)  
pair size  $\ll n^{-1/3}$

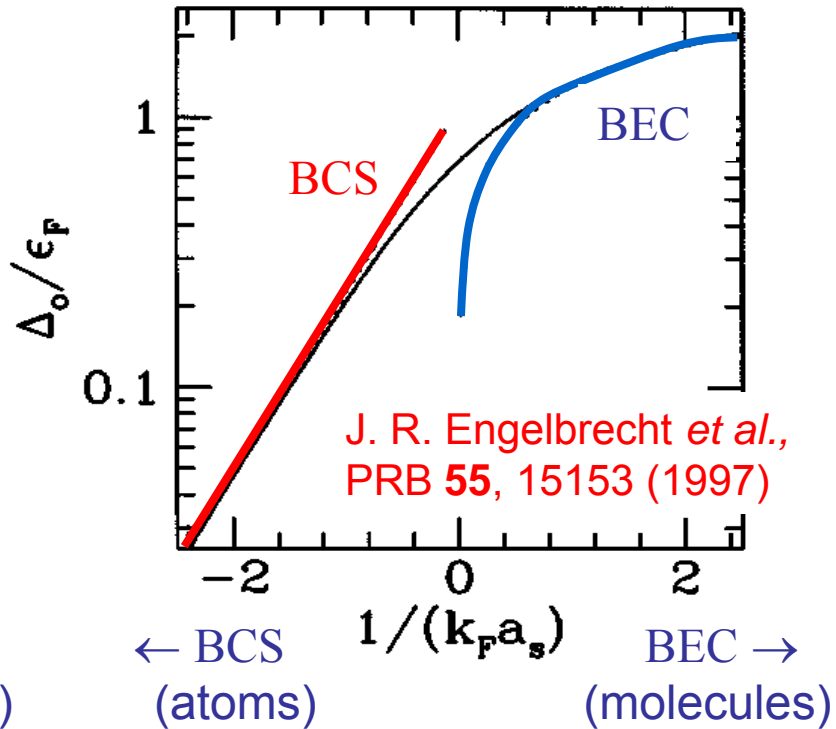
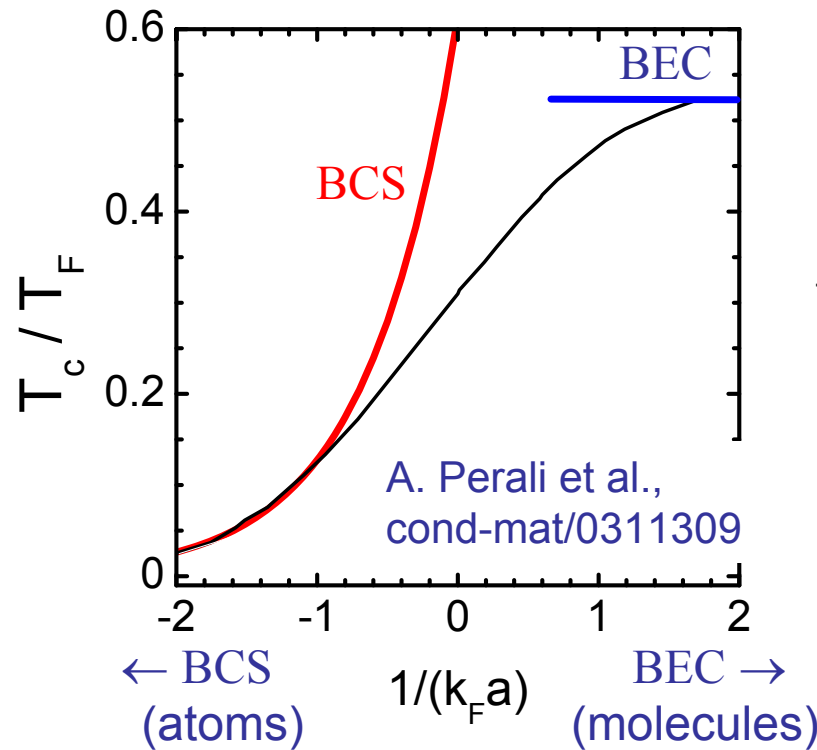
$$T_c/T_F \sim 1$$

$$T_{\text{pairing}} \gg T_c$$

Boson excitations

# BCS-BEC crossover

Predict a smooth connection between BCS and BEC

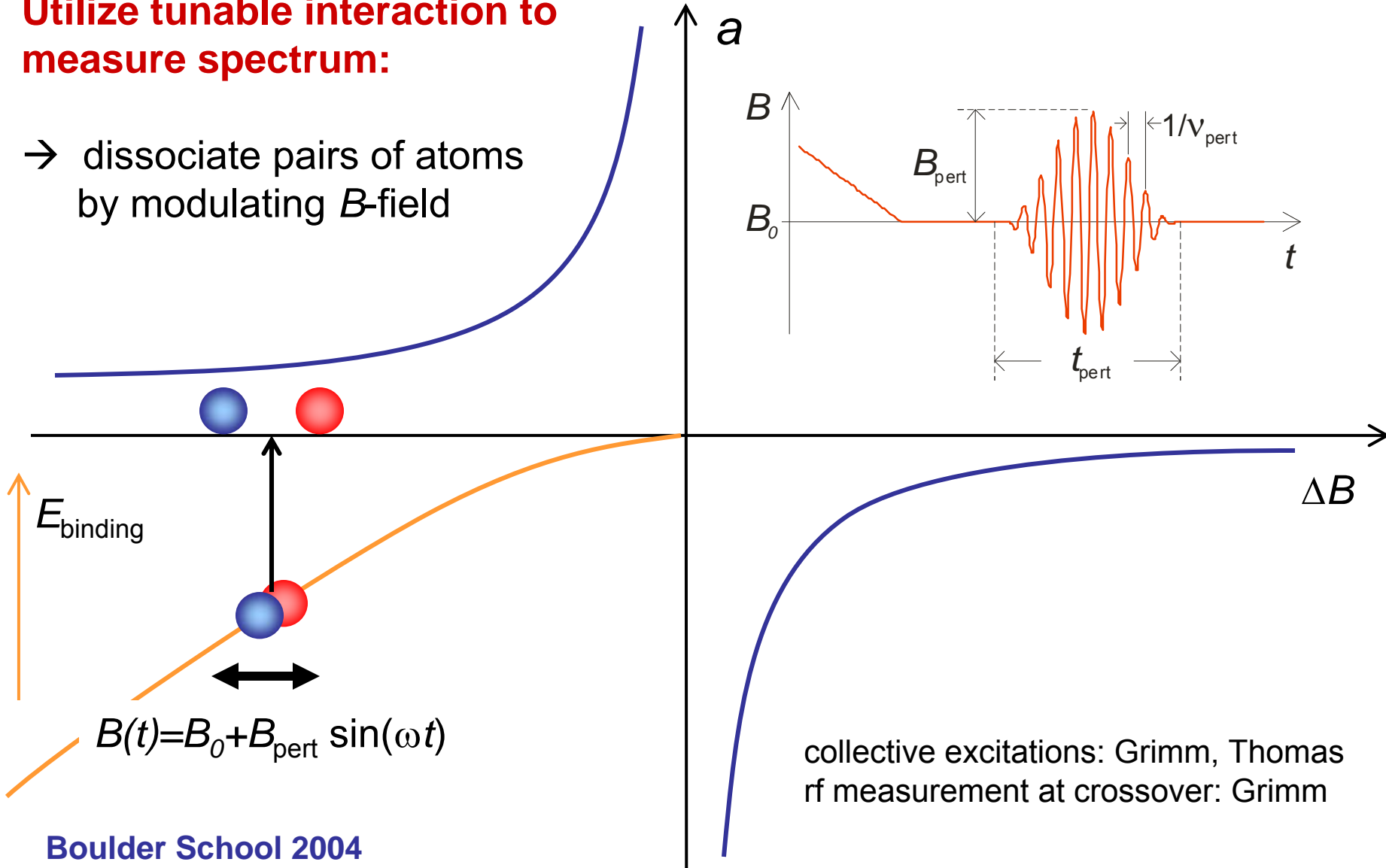


partial list: Eagles, Leggett, Nozieres and Schmitt-Rink, Randeria, Haussman, Strinati, Holland, Timmermans, Griffin, Levin, ...

# Measuring the excitation spectrum

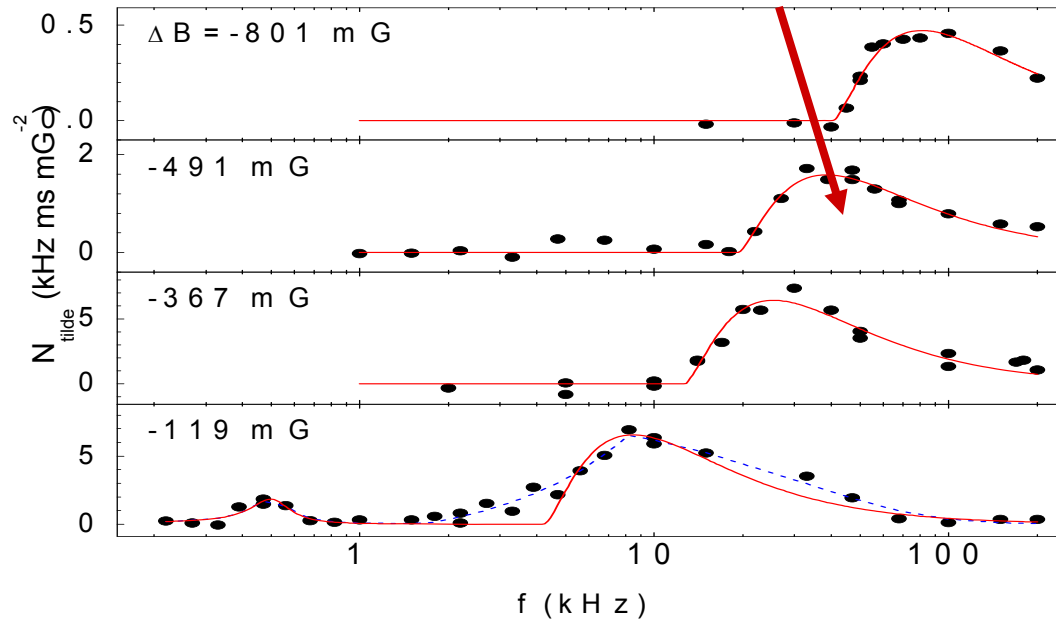
Utilize tunable interaction to measure spectrum:

→ dissociate pairs of atoms by modulating  $B$ -field



# Excitation spectrum: BEC side

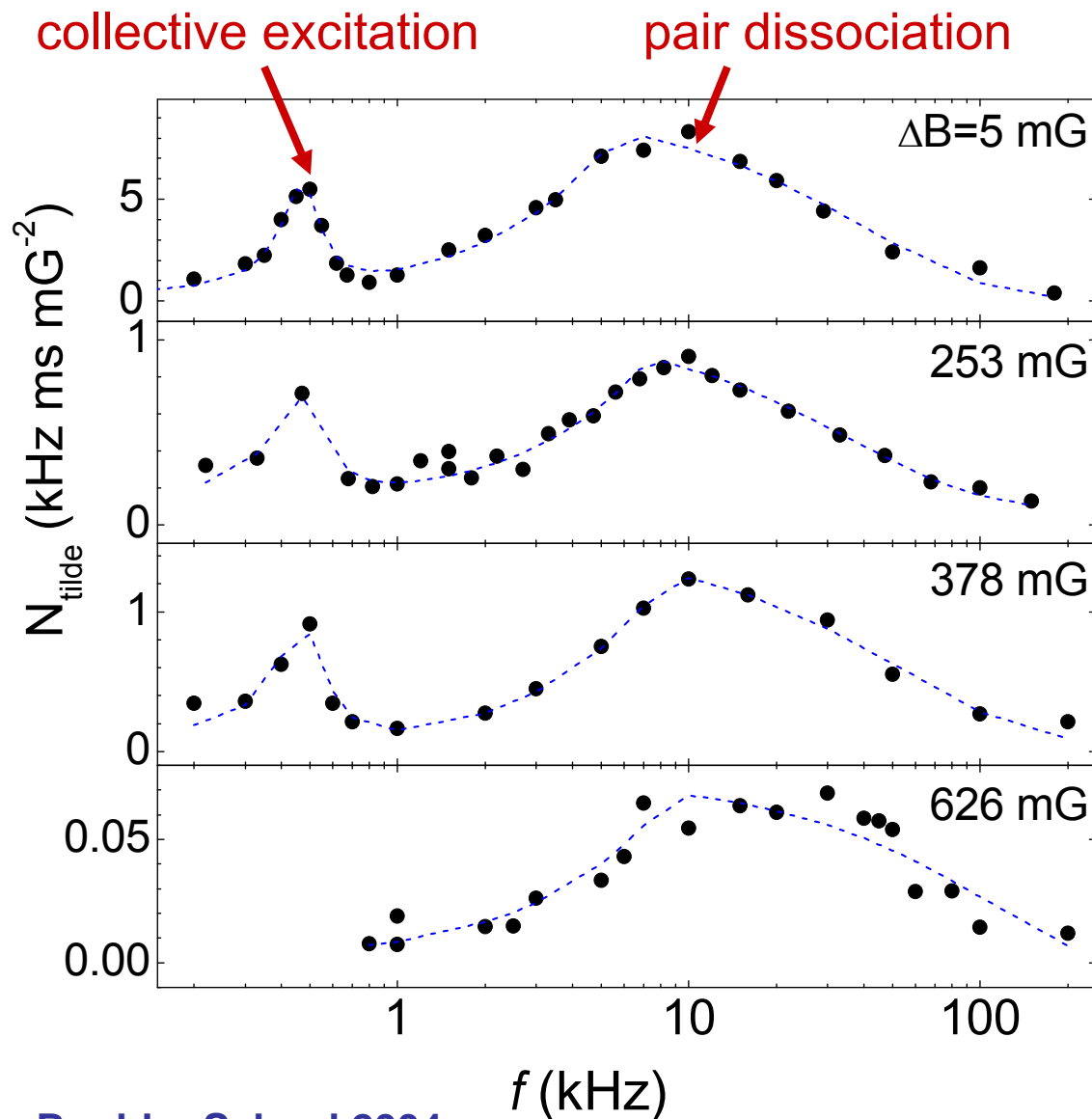
dissociation threshold: molecule binding energy  $E_B/h$



**single particle  
excitation spectrum:**

- molecule dissociation

# Excitation spectrum: BCS side

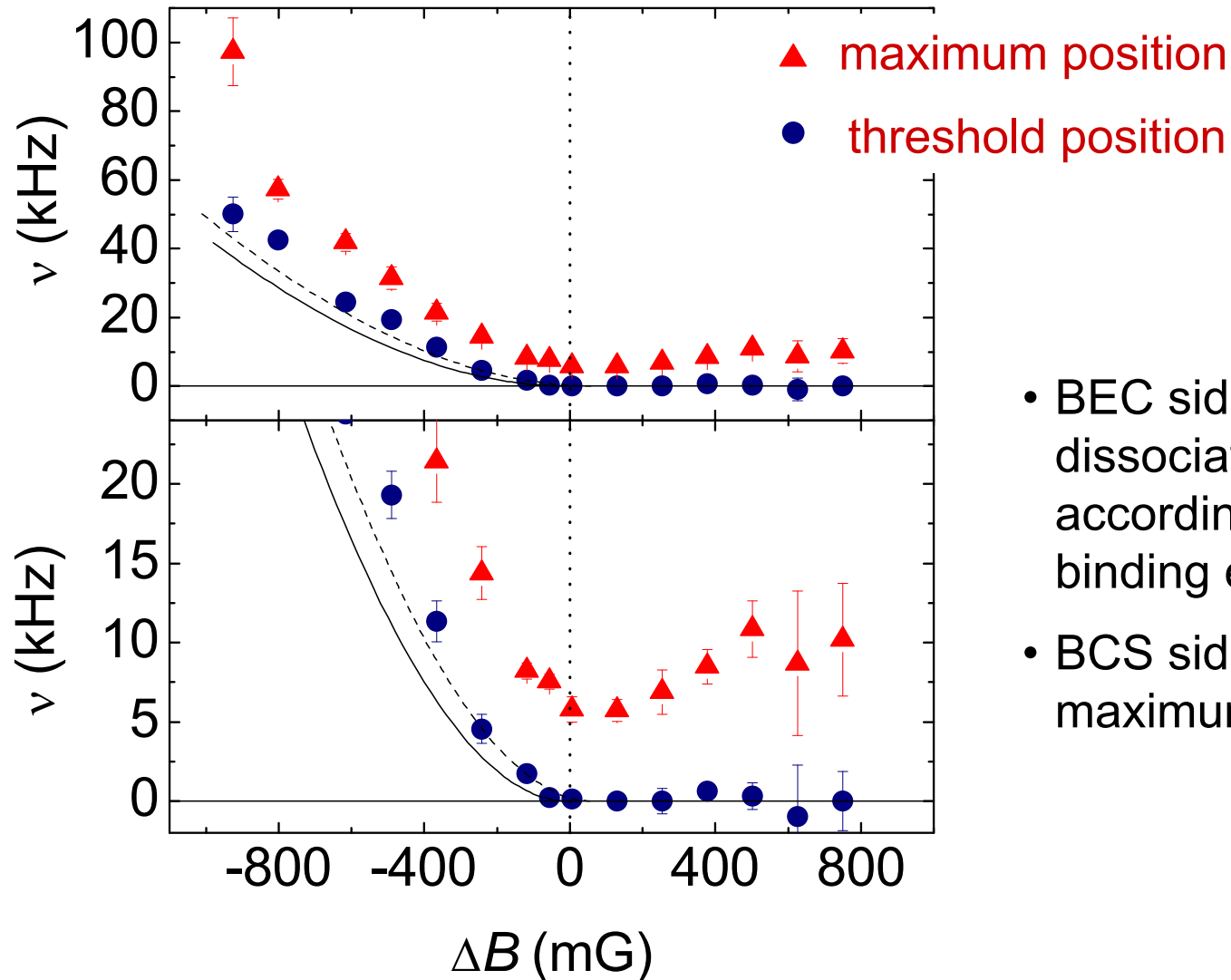


**excitation spectrum**

→ shows pairing

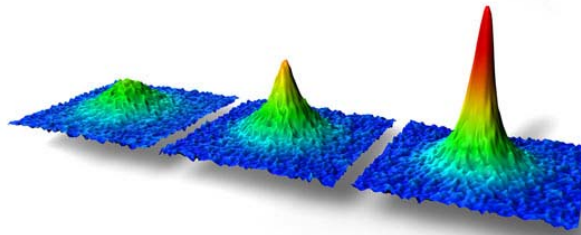
→ containing information about crossover regime,  
**no theoretical model available yet**

# Excitation spectrum



- BEC side: dissociation threshold according to molecule binding energy
- BCS side: nonzero maximum  $\rightarrow$  pairing

# Conclusion



➤ An atomic Fermi gas provides experimental access to the BCS-BEC crossover region.

- Fermi gas  $\leftrightarrow$  molecular BEC interconversion has been explored.

- Condensates of fermionic atom pairs have been achieved !

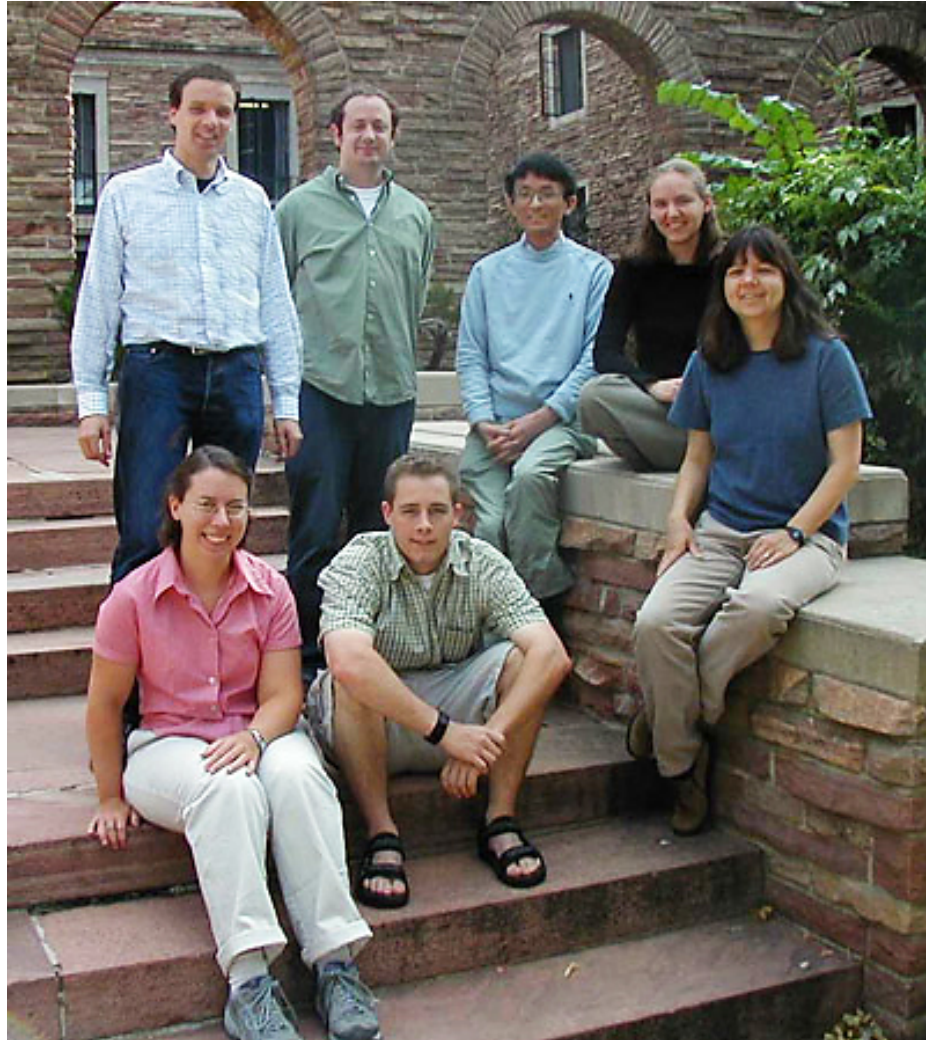
- “Cooper pairs” with strong interactions
- “BEC” with extremely weakly bound molecules

Next...

Many opportunities for further experimental and theoretical work ...

# Current group members:

**M. Greiner**  
J. Goldwin  
S. Inouye  
**C. Regal**  
J. Smith  
M. Olsen





The End.