

Next up: vortices as a window to the “normal” state...

And other things I would like to get to today:

- comparison of charge order in several cuprates
- internal form factor of charge order
- Fermi surface
- nematicity in cuprates & pnictides
- bosons

# Superconductivity Tunneling Milestones



1960: gap measurement (Pb)

1965: boson energies & coupling (Pb)

1985: charge density wave ( $\text{TaSe}_2$ )

1989: vortex lattice ( $\text{NbSe}_2$ )

1997: single atom impurities (Nb)

2002: quasiparticle interference

→ band structure & gap symmetry (BSCCO)

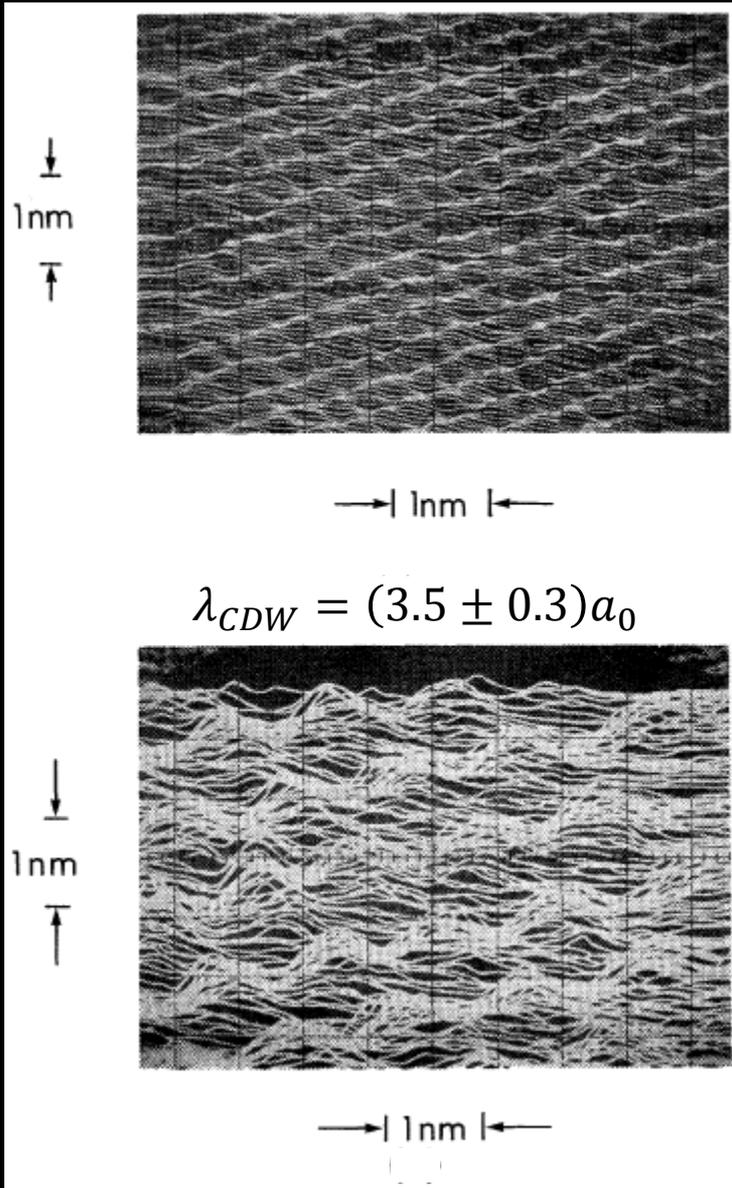
2009: phase-sensitive gap measurement (Na-CCOC)

2010: intra-unit-cell structure (BSCCO)

# 1985: charge density wave

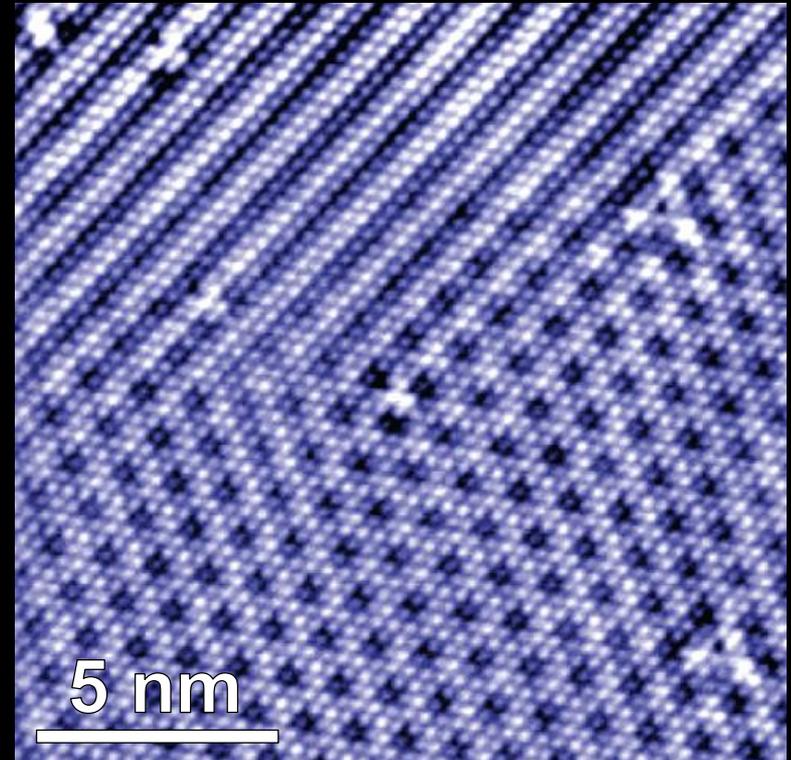


TaSe<sub>2</sub> (T<sub>c</sub>=133 mK)



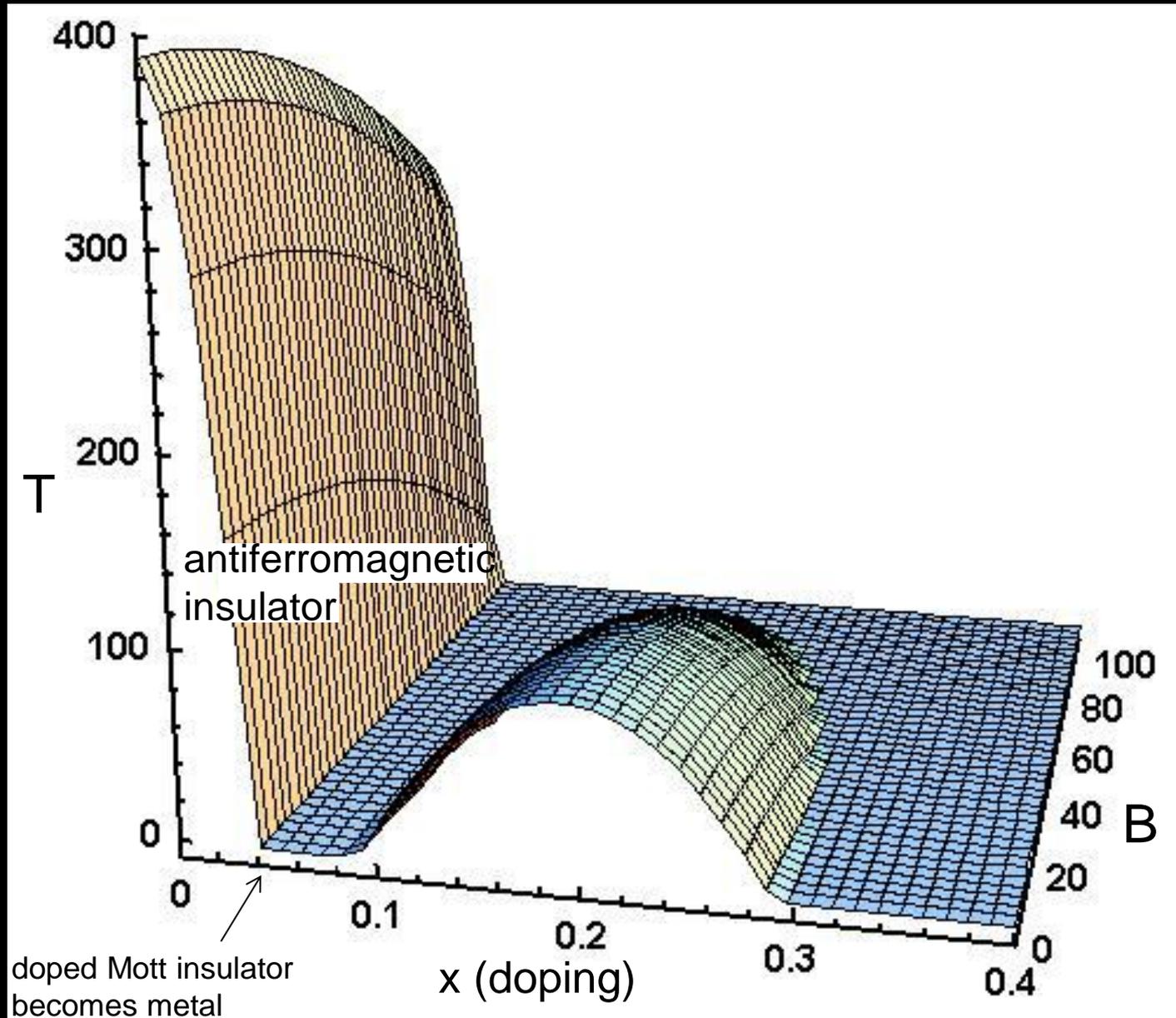
Coleman, PRL 55, 394 (1985)

2013: quantum phase transition between  
1D & 2D CDW phases in NbSe<sub>2</sub>

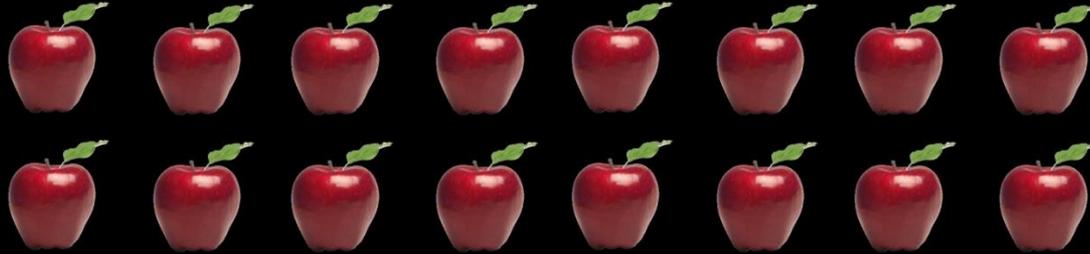


Soumyanarayanan & JEH, PNAS 110, 1623 (2013)

# Cuprate Phase Diagram



# Mott Transition



localized



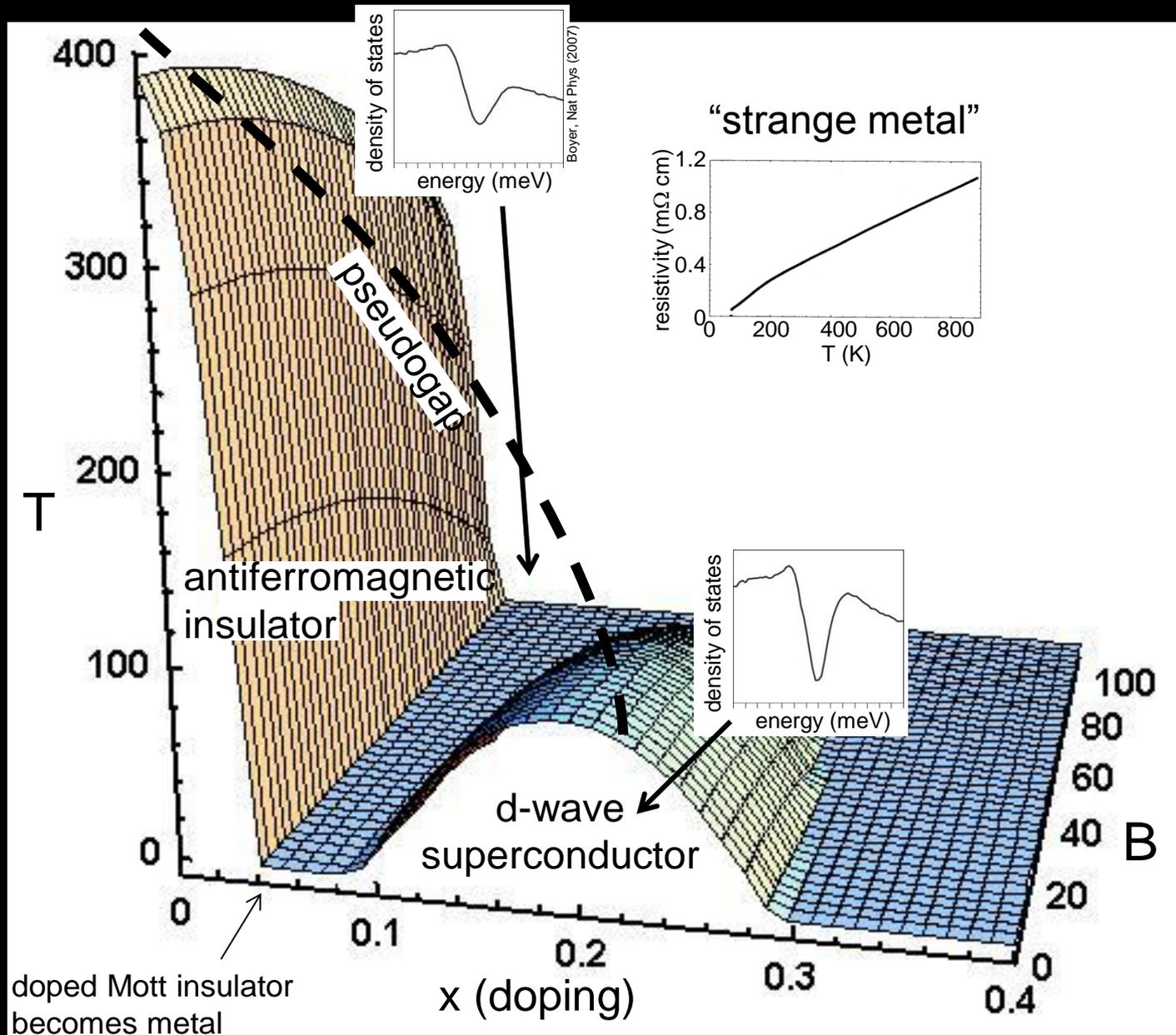
delocalized



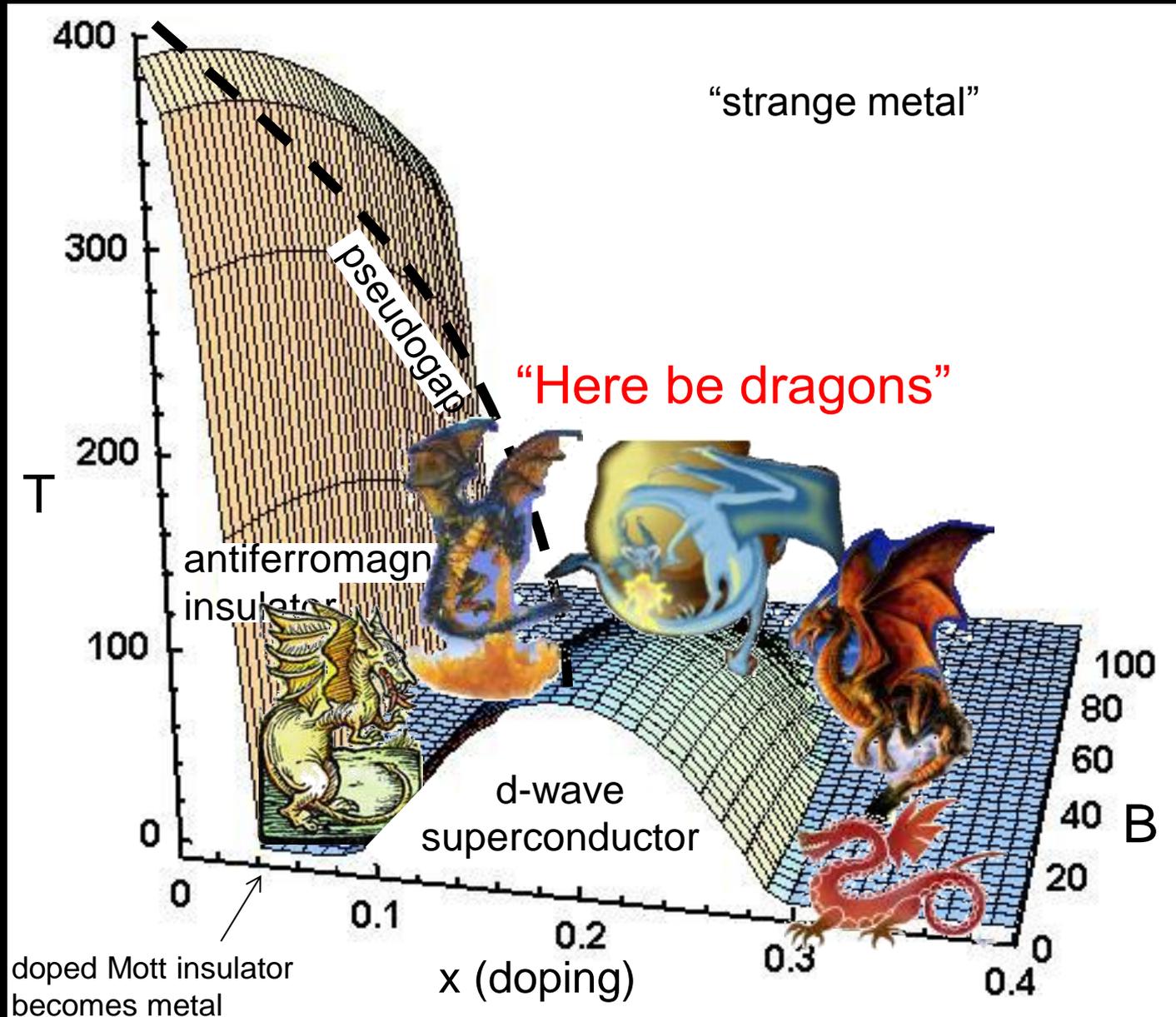
further delocalized



# Cuprate Phase Diagram



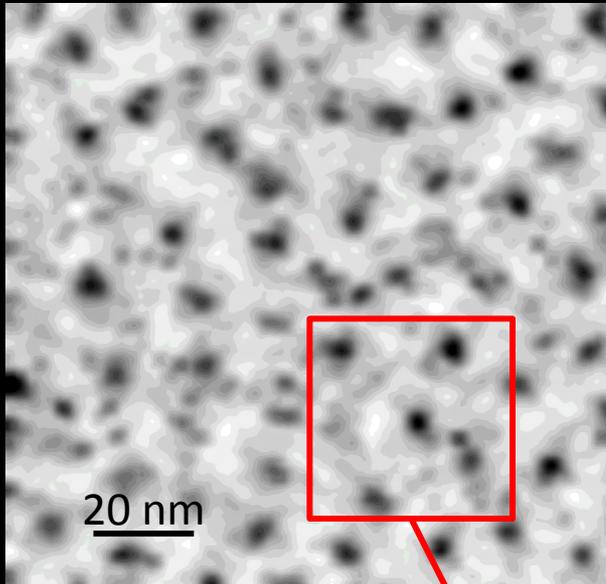
# Cuprate Phase Diagram



# Look back at those Bi2212 vortices...

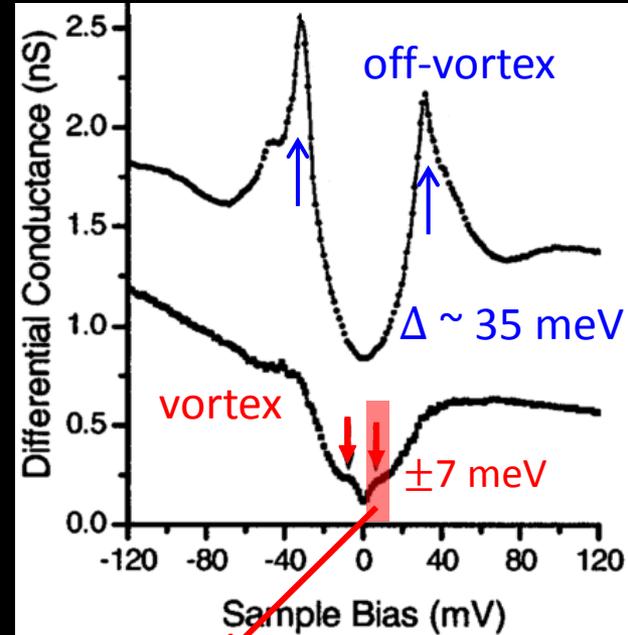


BSCCO



Pan, PRL 85, 1536 (2000)

zoom in

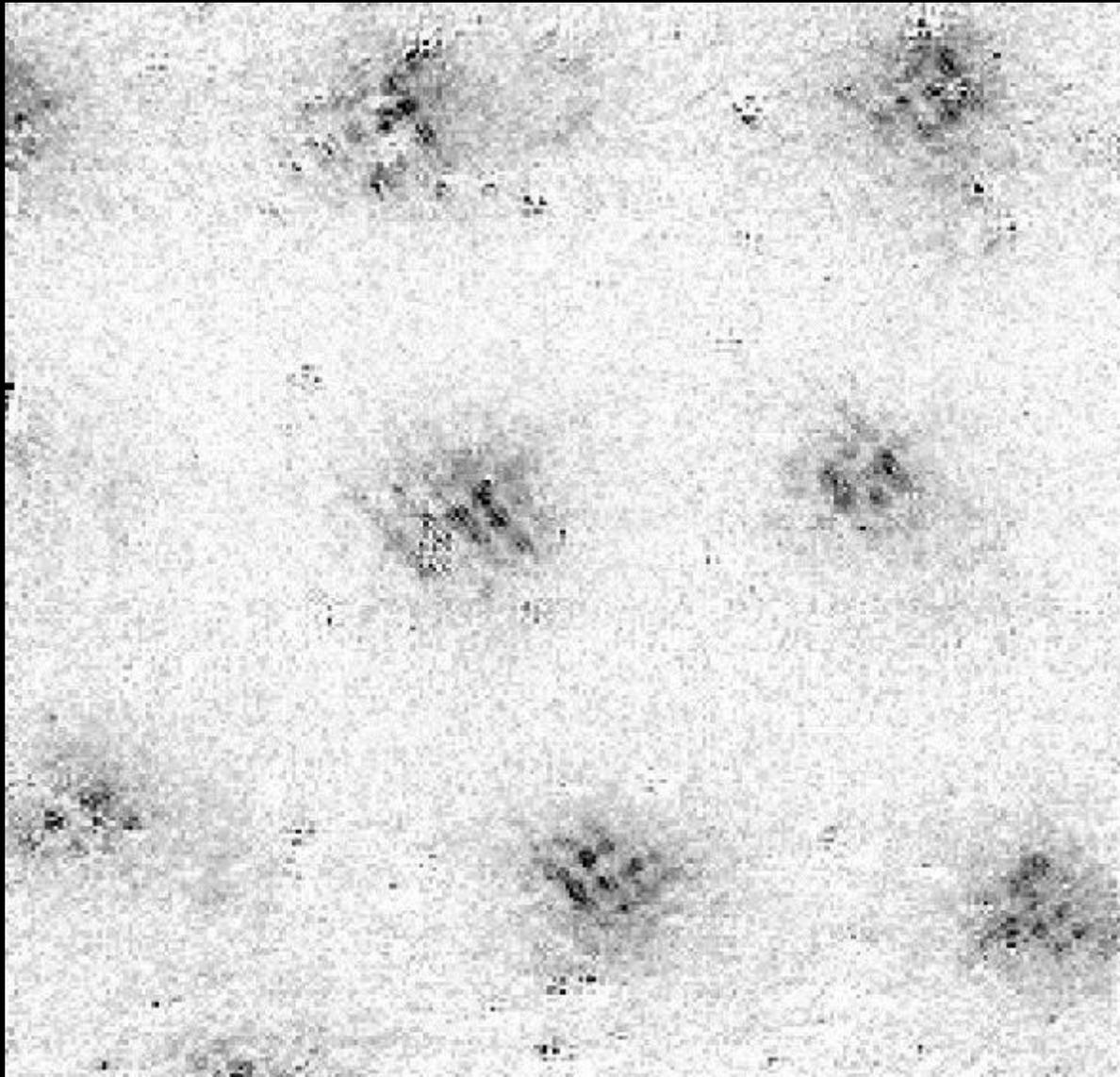


integrate over the core state energy range

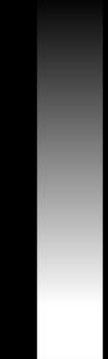
# Bi2212: Vortex-induced checkers



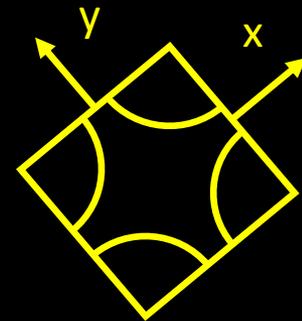
560 Å



2 pA

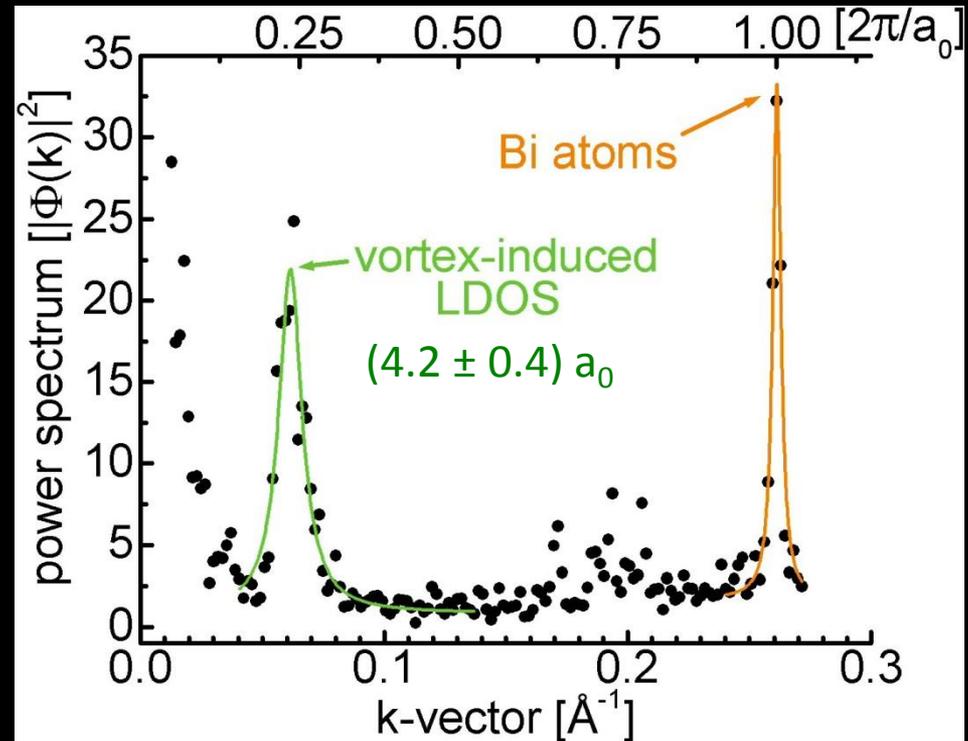
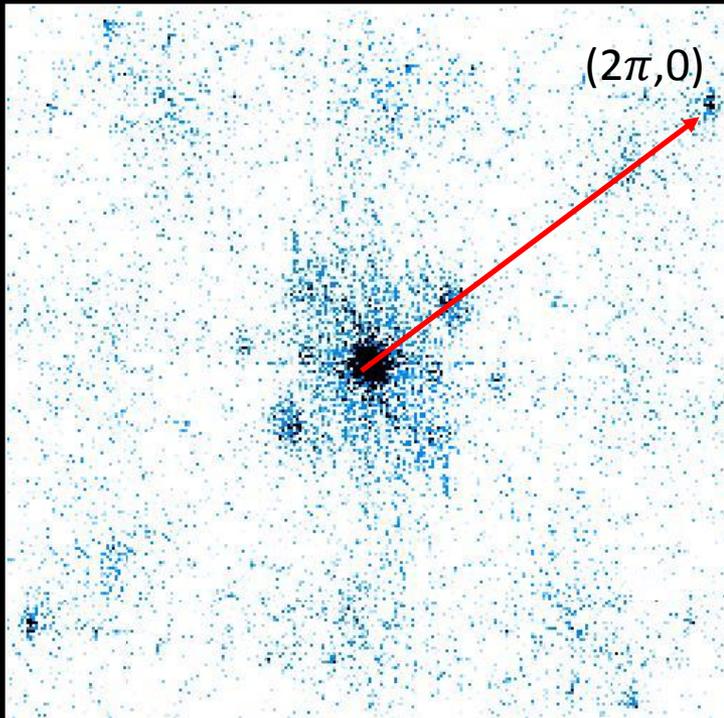


0 pA



*Hoffman, Science 266, 455 (2002)*

# Bi2212 vortices: Fourier transform



One might conclude that these core state are non-dispersive because they were identified by energy integration (!)

But vortex diameter is  $D \sim 100 \text{ \AA} \sim 25a_0$  in diameter.  
The  $q$ -space resolution is therefore  $\delta q = 2\pi/D \sim 4\% (2\pi/a_0)$   
→ too coarse to resolve band structure dispersion

# Bi2212: Destroy SC $\rightarrow$ Static Order?

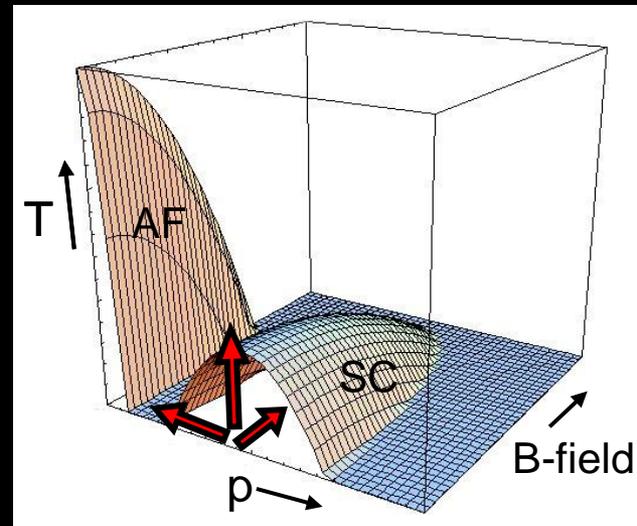


Suppression of Superconductivity in optimal Bi2212:

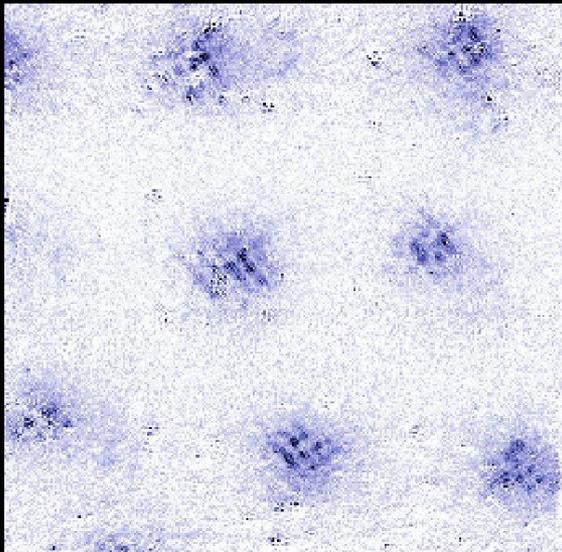
$\rightarrow$  Pseudogap Spectra

$\rightarrow$  “checkerboard” LDOS Modulations

$\rightarrow$  Incommensurate:  $4.3a_0$ ,  $4.5a_0$ ,  $4.6a_0$

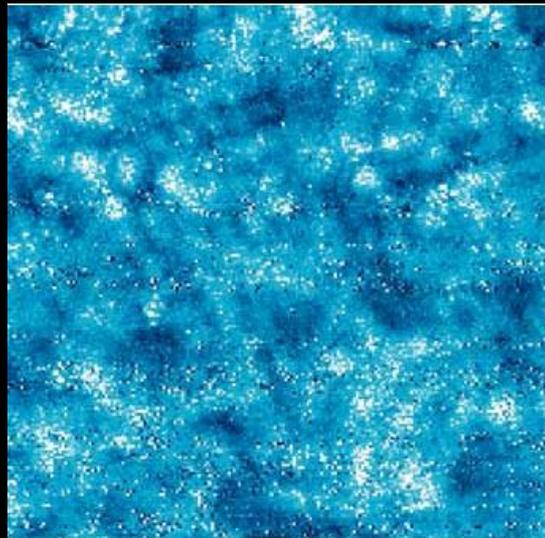


$B = 5T$  ( $E = 7 \text{ meV}$ )



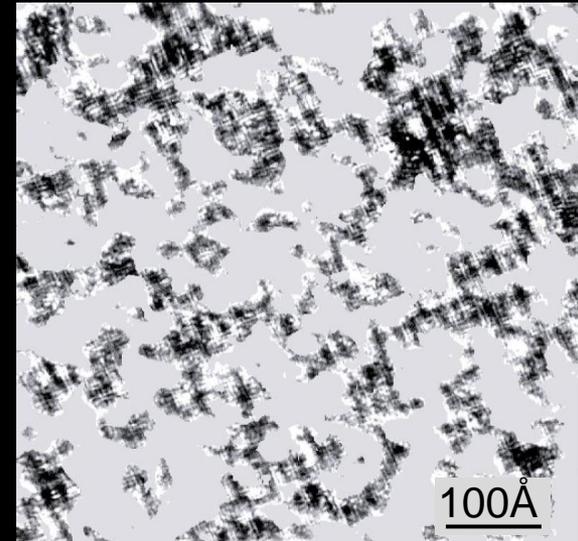
J. Hoffman, ... J.C. Davis  
*Science* 295, 466 (2002)

$T = 100K$  ( $E < \Delta$ )



M. Vershinin, ... A. Yazdani  
*Science* 303, 1995 (2004)

$\Delta > 65 \text{ meV}$  ( $E > 65 \text{ meV}$ )

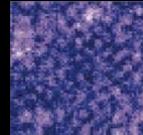


K. McElroy, ... J.C. Davis  
*PRL* 94, 197005 (2005)

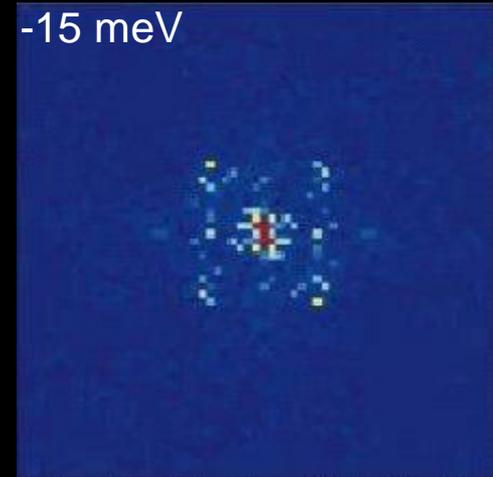
# Superconducting State: Dispersing vs. Static?



Real space:  
(160 Å)<sup>2</sup>



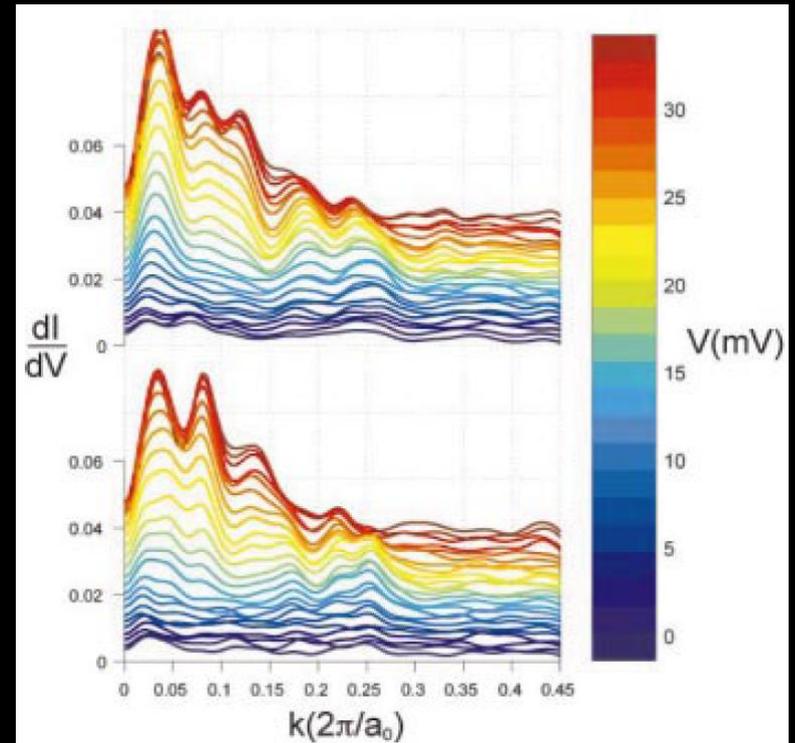
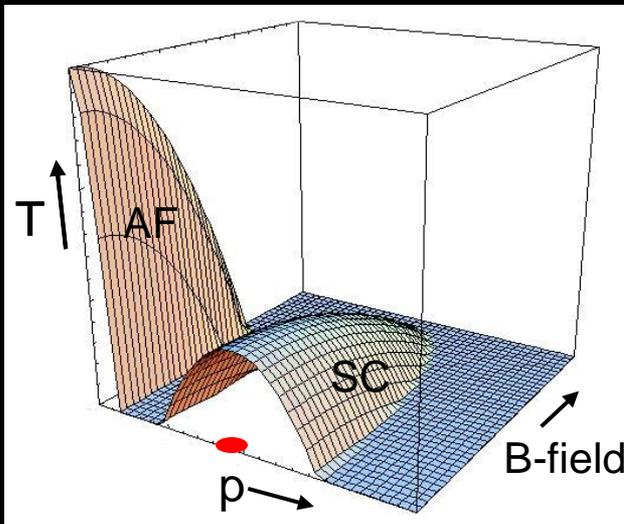
q-space: 2.4% BZ resolution  
-15 meV



Setup:  $V_{\text{sample}} = -200 \text{ meV}$ ,  $R = 2 \text{ G}\Omega$

Howald, ... Kapitulnik  
*PRB* 67, 014533 (2003).

Claim: static order in low-energy (sub-gap) DOS in the superconducting state.



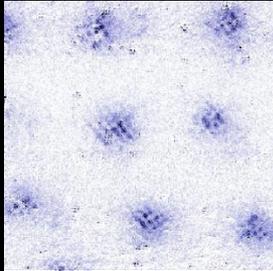
# Another Cuprate for STM: $\text{Na}_x\text{Ca}_{2-x}\text{CuO}_2\text{Cl}_2$



Motivation: previous reports of static checkerboards occurred in small areas (vortices, underdoped areas) & in very disordered BSCCO. Need cleaner, lower  $T_c$  sample.

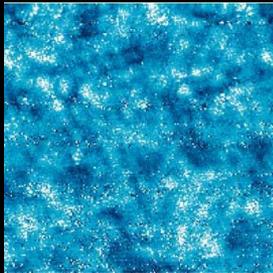
vortices:

- small area



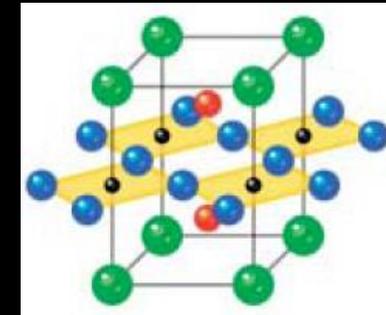
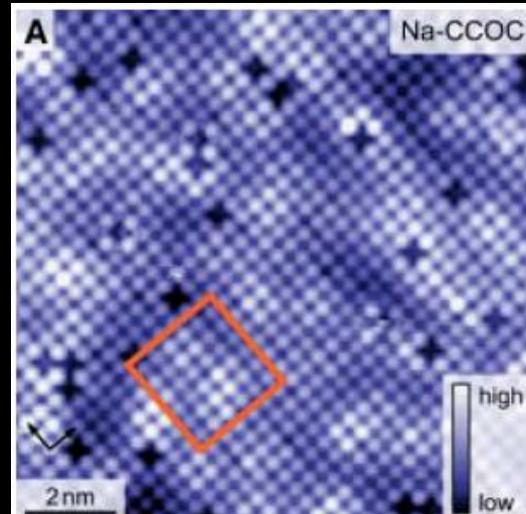
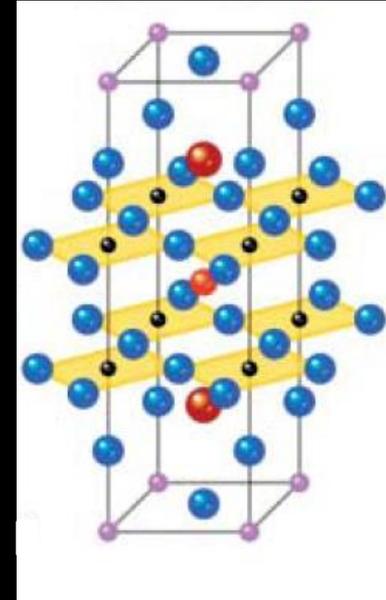
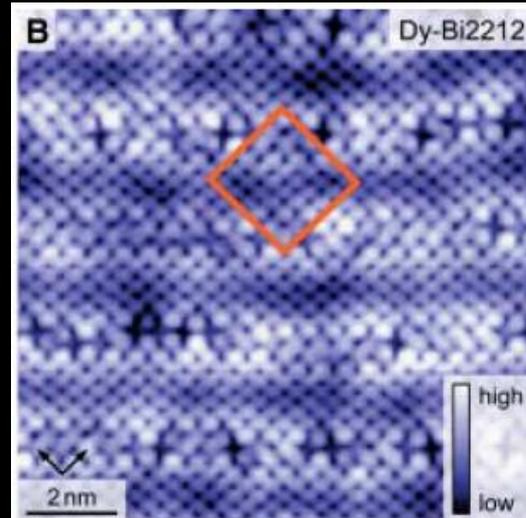
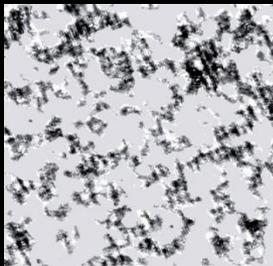
>  $T_c$ :

- low E resolution
- large spatial disorder

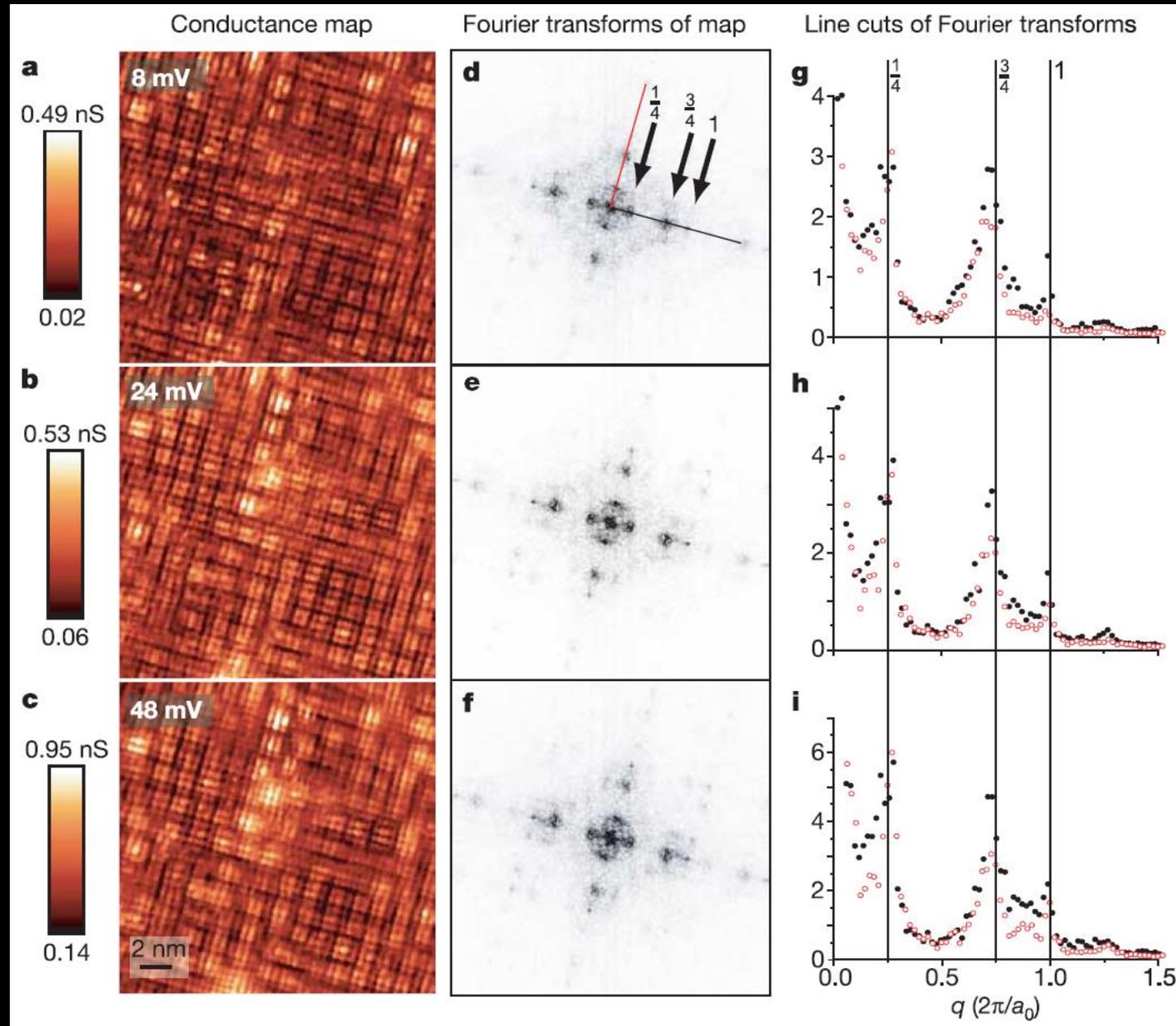


low p:

- small area
- spatial disorder



# $\text{Na}_x\text{Ca}_{2-x}\text{CuO}_2\text{Cl}_2$ checkerboard does not disperse



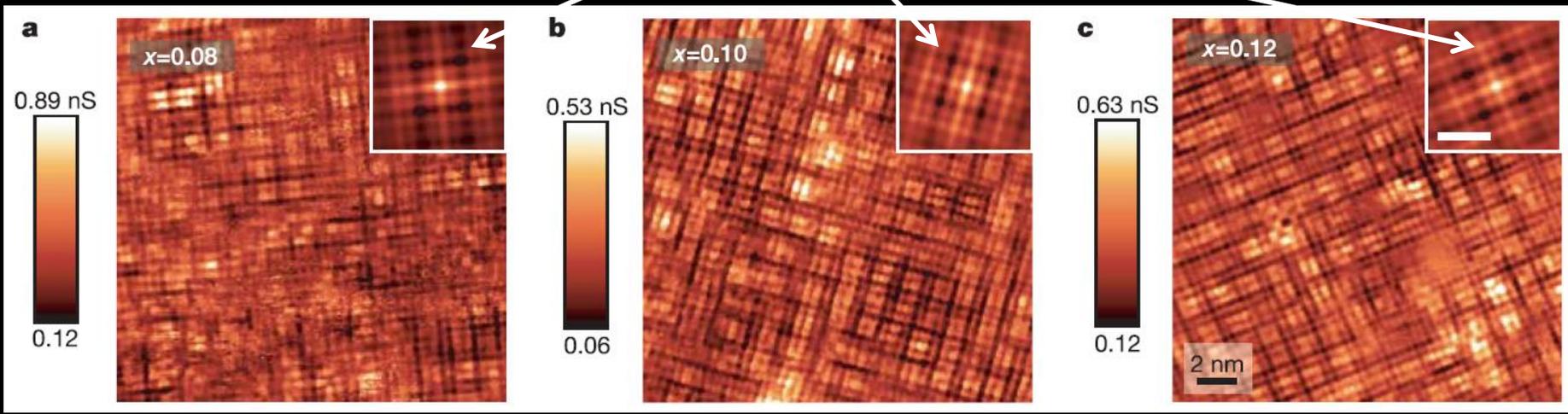
$x = 0.12$   
 $T_c = 20 \text{ K}$

Experiment:  
 $T = 100 \text{ mK}$



# $\text{Na}_x\text{Ca}_{2-x}\text{CuO}_2\text{Cl}_2$ checkerboard does not depend on doping

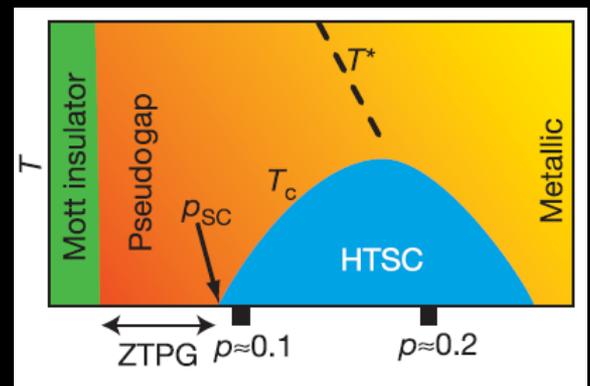
autocorrelation shows 4-unit-cell plaquette,  
with 3 internal maxima,  
for all 3 dopings



$T_c = 0 \text{ K}$

$T_c = 15 \text{ K}$

$T_c = 20 \text{ K}$



Setup:  $V_{\text{sample}} = +200 \text{ meV}$ ,  $R = 2 \text{ G}\Omega$

# Checkerboard comparison: Na-CCOC vs. BSCCO

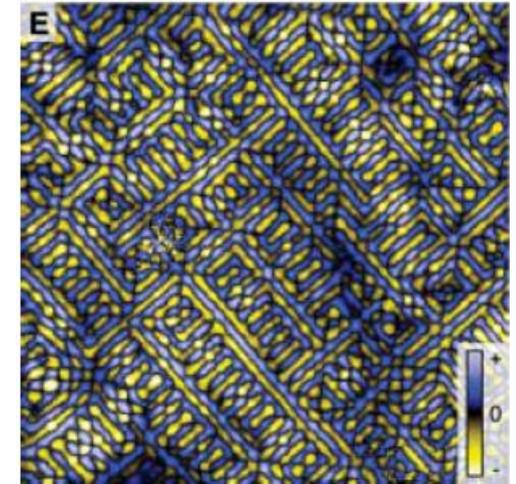
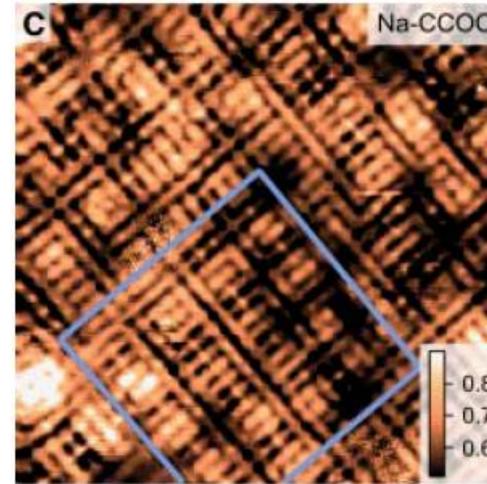
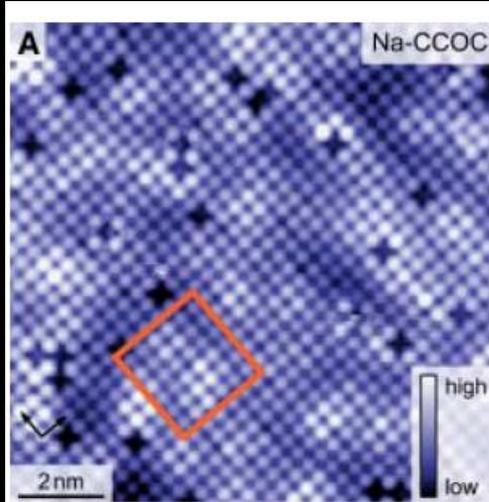


Topography

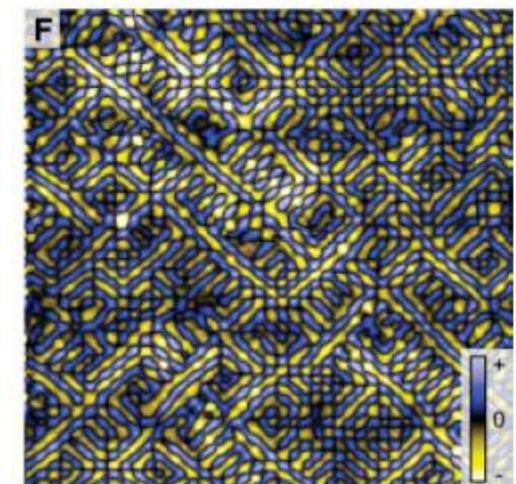
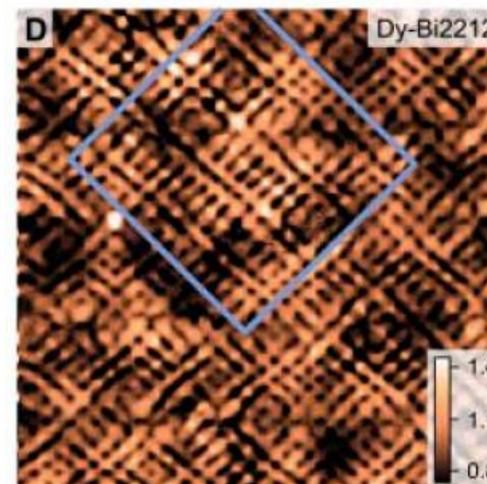
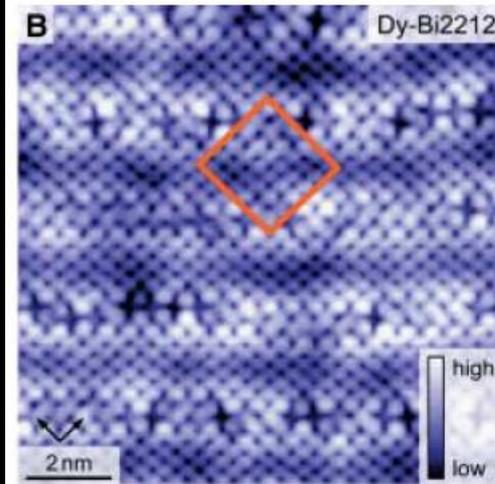
R-map (150 meV)

Laplacian:  $\nabla^2(R)$

Na-CCOC  
 $x = 0.12$   
 $T_c = 21$  K



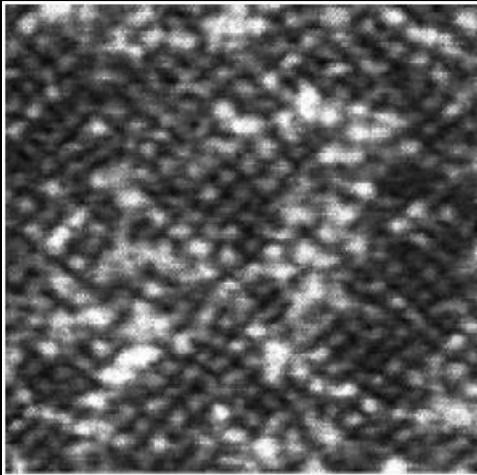
Dy-BSCCO  
 $p \sim 0.08$   
 $T_c = 45$  K



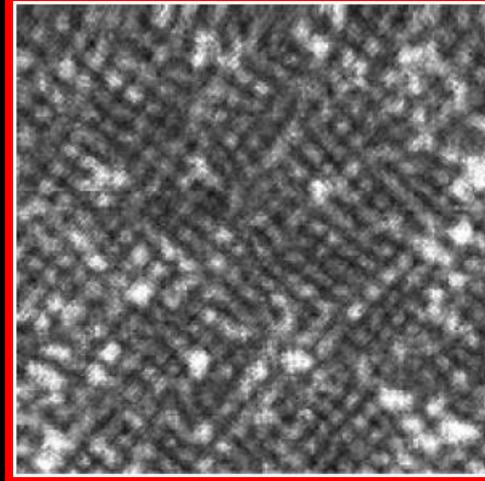
# Bi-2201: charge density wave



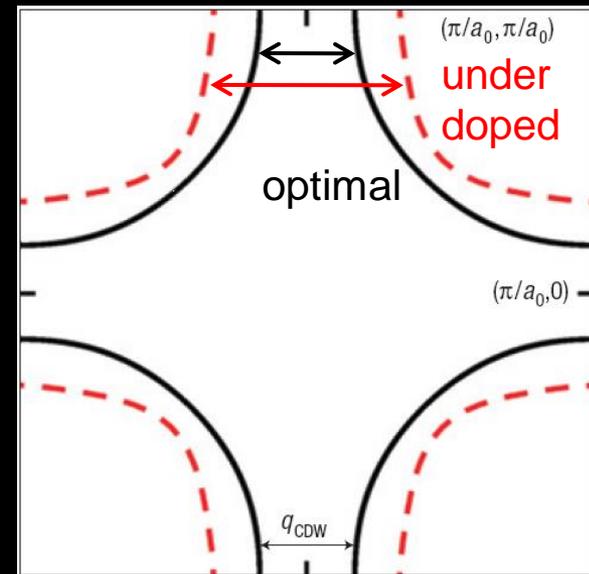
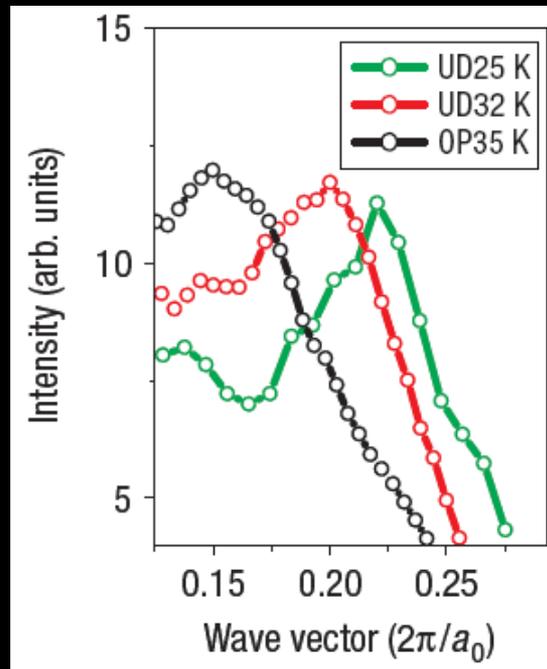
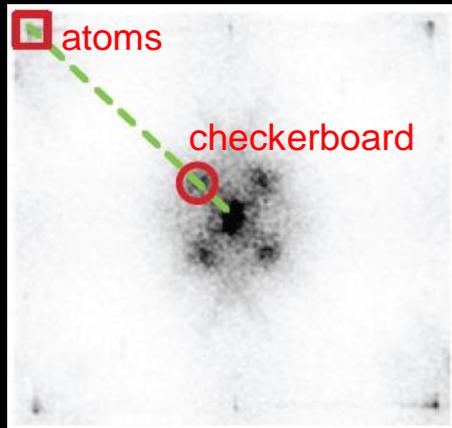
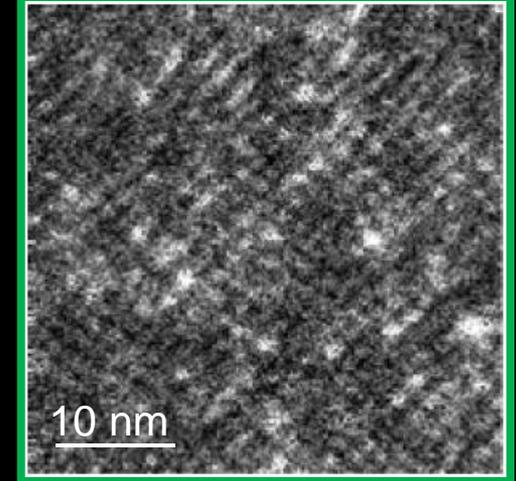
OP,  $T_c = 35$  K



UD,  $T_c = 32$  K



UD,  $T_c = 25$  K



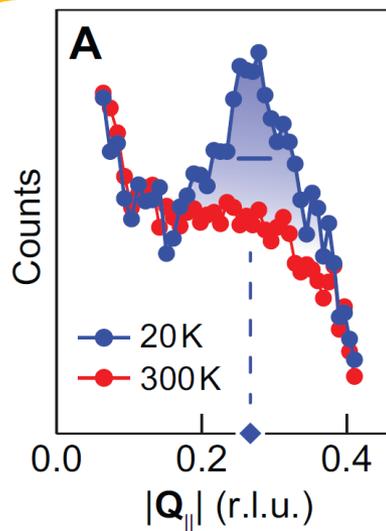
# Bulk charge order



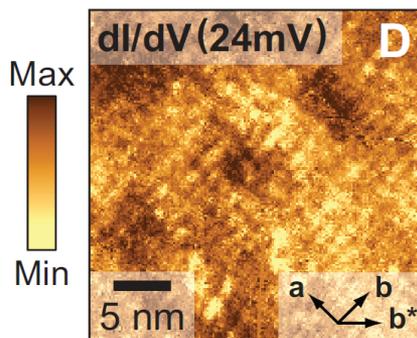
NMR { Wu+Julien, *Nature* 477, 191 (2011)  
(YBCO) { Wu+Julien, *Nat. Comm.* 4, 2113 (2013)

REXS { Ghiringhelli, *Science* 337, 821 (2012)  
(YBCO) { Chang, *Nat. Phys.* 8, 871 (2012)

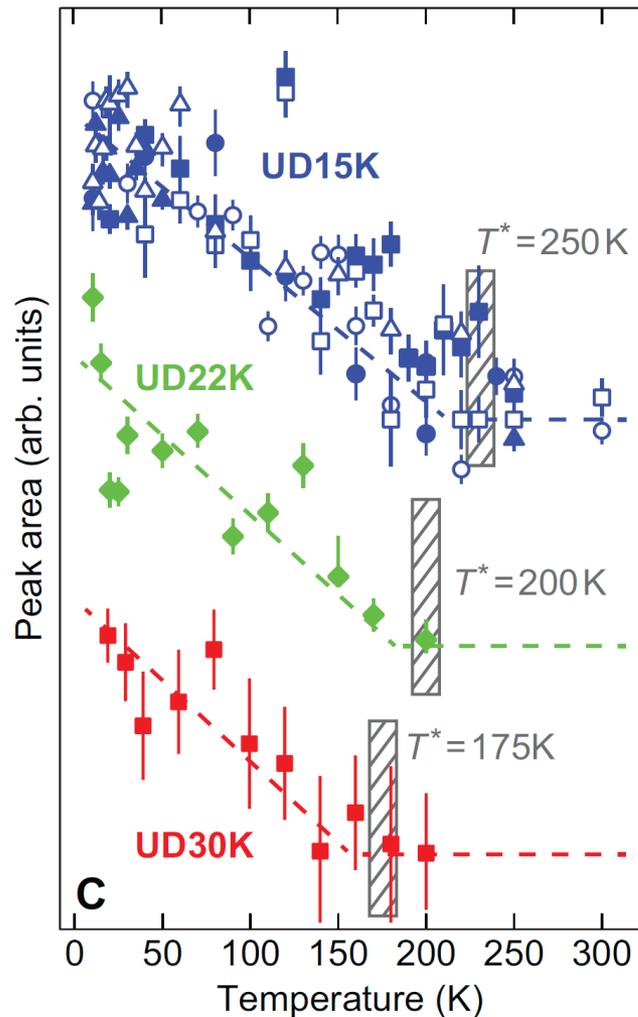
**Bi2201: First ever reconciliation of surface and bulk charge order!**



Resonant  
X-ray  
Scattering



Scanning  
Tunneling  
Microscopy



Riccardo Comin *et al*, *Science* 343, 390 (2014)

# Charge Order Questions



1. What is the doping,  $T$ , and  $B$  dependence of charge order?
2. Is the charge order = pseudogap, or within PG?
3. Are we within the CDW phase or just disorder-pinned fluctuations?
4. Does charge order compete with superconductivity?
5. What is the wavevector of charge order – where is it living on FS?
6. What is the energy dependence of charge order?
7. Is charge order responsible for small FS?
8. Is it 1D or 2D? Does it have some internal form factor?

# Charge Order Questions

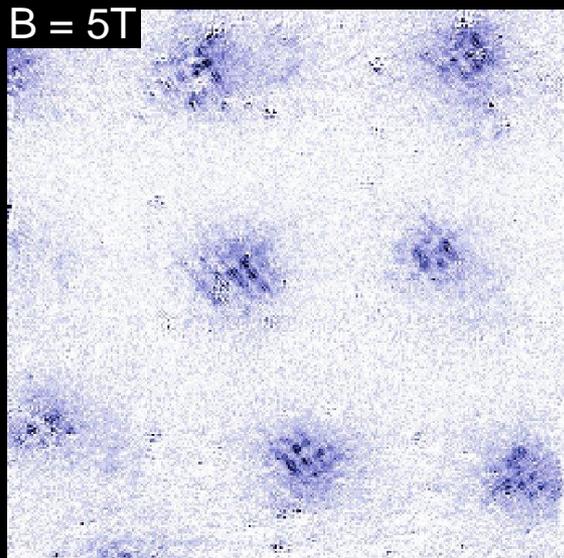


1. What is the doping, T, and B dependence of charge order?  
**strongest near  $p=1/8$ , and in applied B**
2. Is the charge order = pseudogap, or within PG?  
**appears to be within the PG**
3. Are we within the CDW phase or just disorder-pinned fluctuations?  
**YBCO can be long-range-ordered; BSCCO is pinned fluctuations?**
4. Does charge order compete with superconductivity?  
**yes! (vortex cores, dip in dome, etc.)**
5. What is the wavevector of charge order – where is it living on FS?  
**varies continuously w/ doping; connects AFBZ hotspots**
6. What is the energy dependence of charge order?  
**hard to say... maybe strongest at +E, maybe strongest at  $\Delta_{PG}$**
7. Is charge order responsible for small FS?  
**Bi2212: claim is yes; Bi2201: CDW constant while FS evolves**
8. Is it 1D or 2D? Does it have some internal form factor?  
**local 1D patches? d-wave form factor**

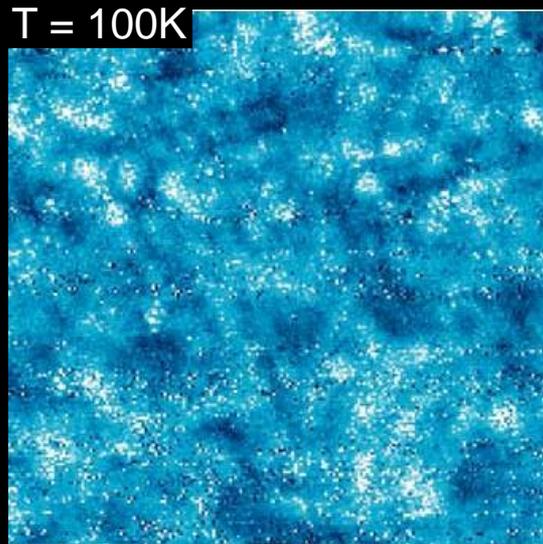
# Doping, B, and T dependence?



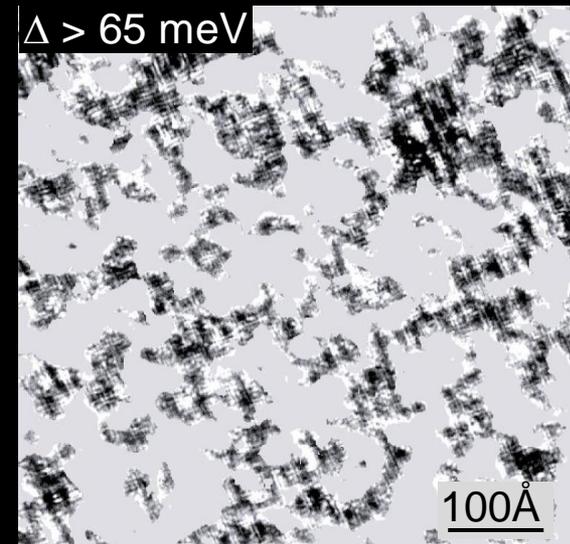
Bi2212: strengthens when SC is suppressed



Hoffman *Science* 295, 466 (2002)

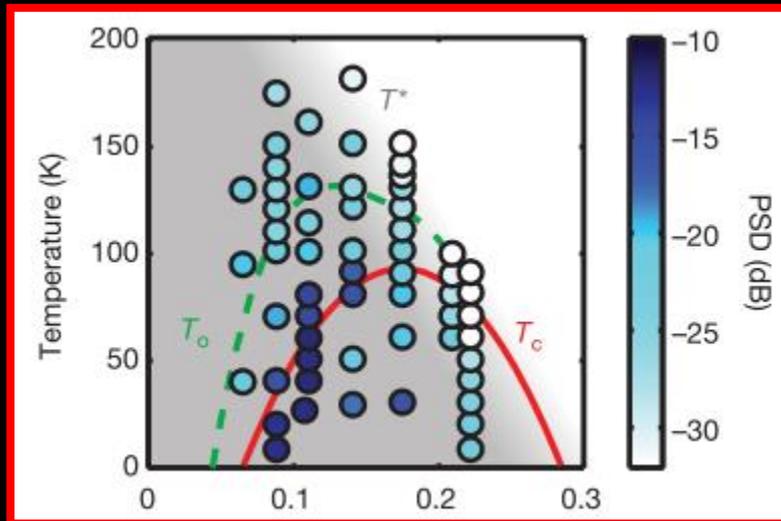


Vershinin, *Science* 303, 1995 (2004)

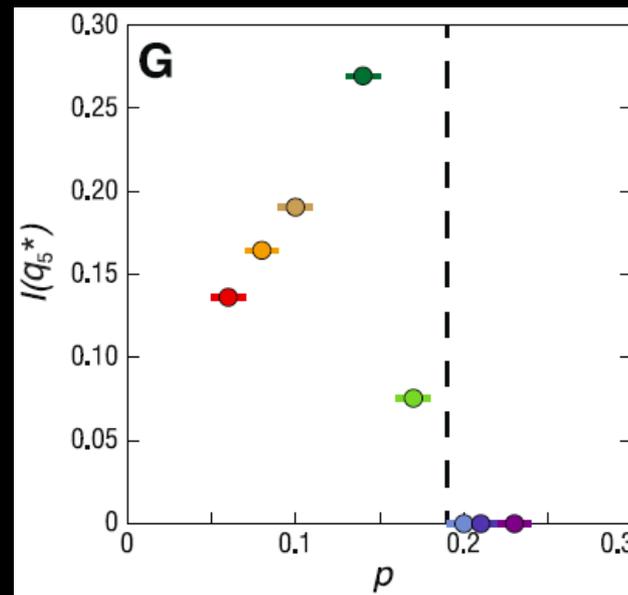


McElroy, *PRL* 94, 197005 (2005)

But: CDW dies gradually or abruptly near  $p=0.19$



Parker+Yazdani, *Nature* (2010)

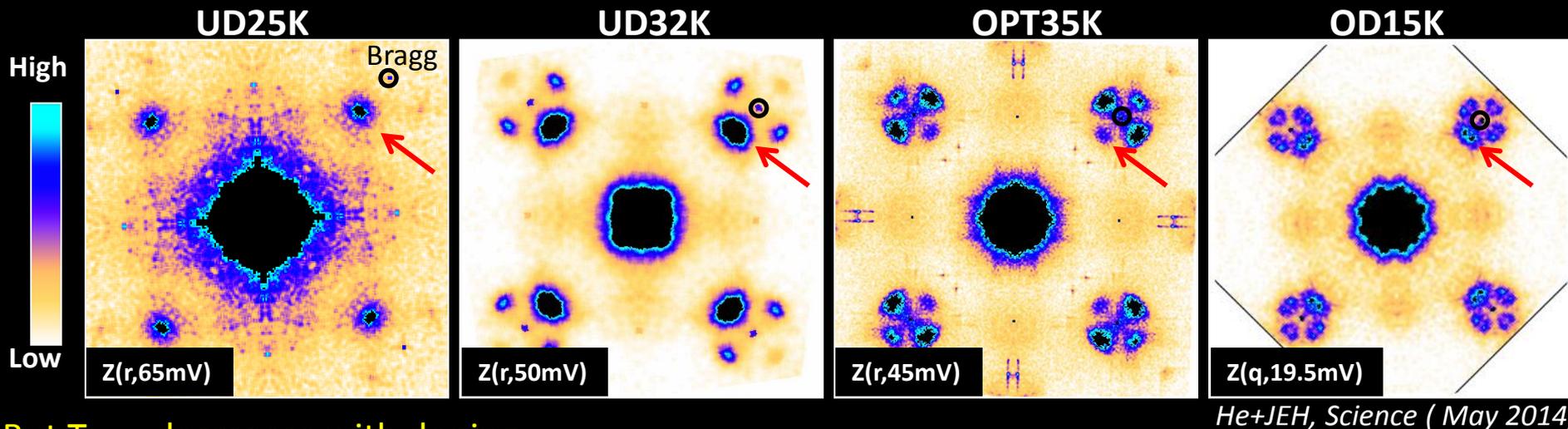


Fujita, *Science* (2014)

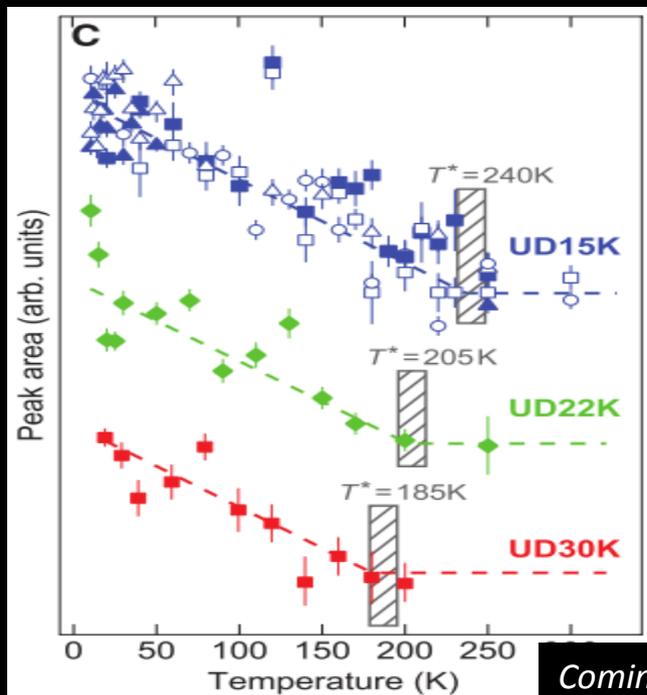
# Doping, B, and T dependence?



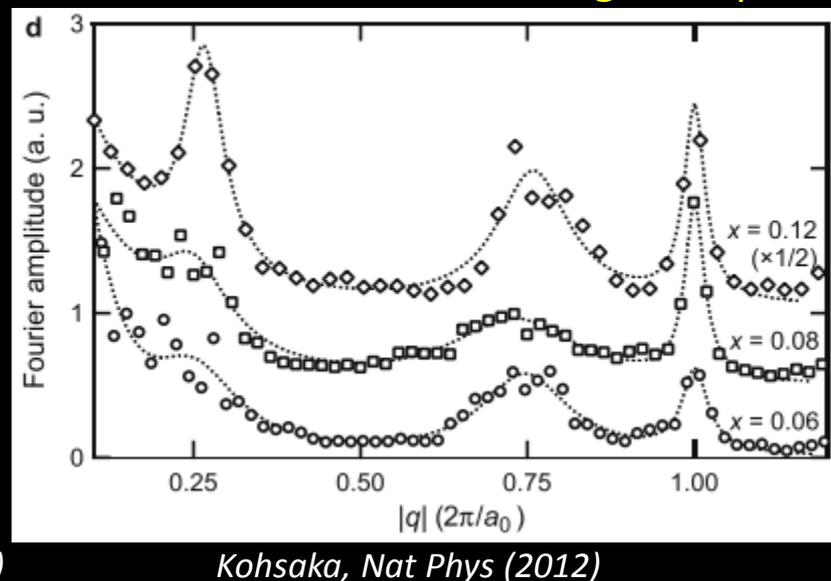
Bi2201: at T=6K, CDW is present at all dopings, no obvious trend in strength or lengthscale



But  $T_{\text{onset}}$  decreases with doping



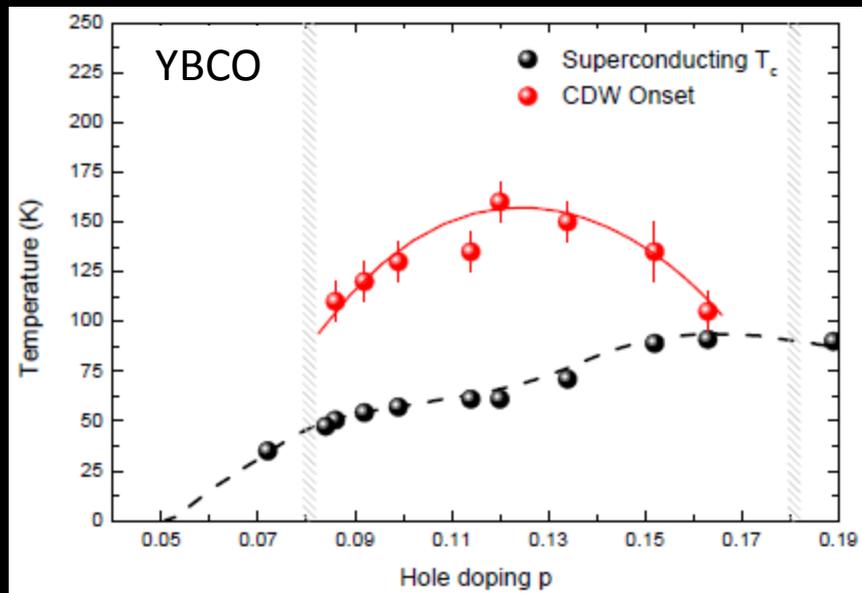
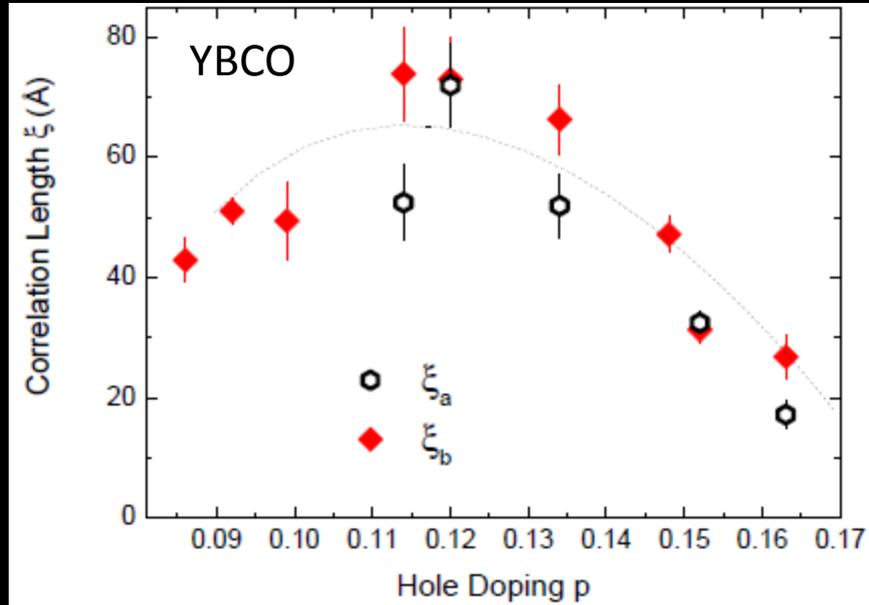
Na-CCOC: CDW present at  $p=0.06-0.12$ ; strongest at  $p=0.12$



# Doping, B, and T dependence?



YBCO (from XRD):

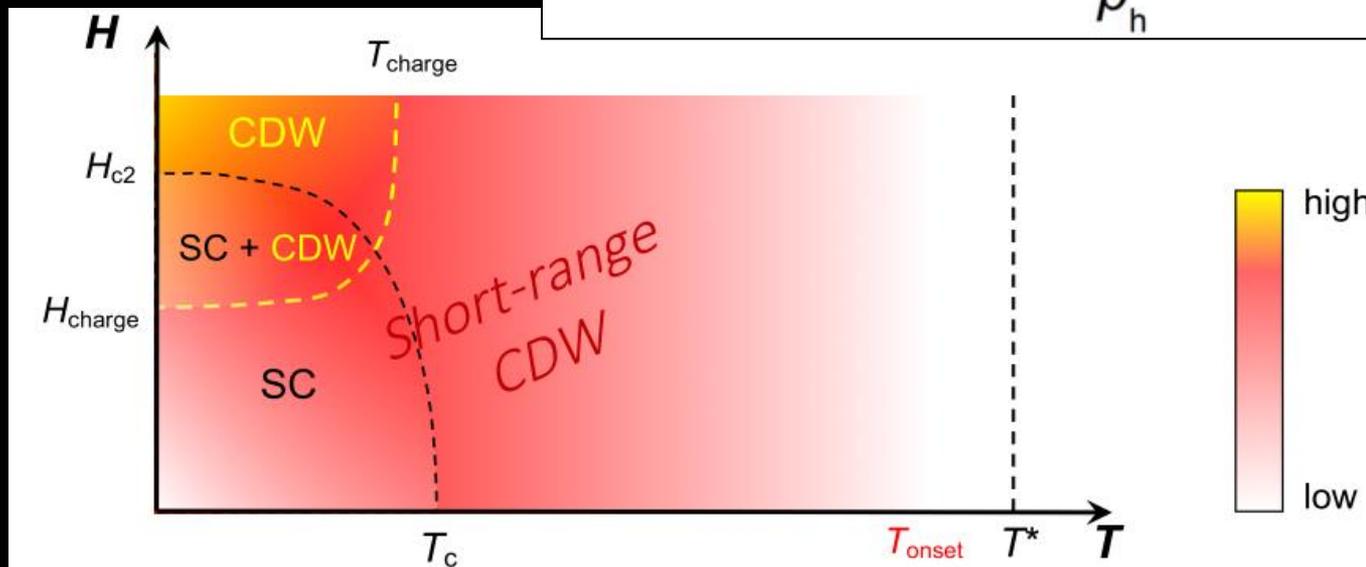
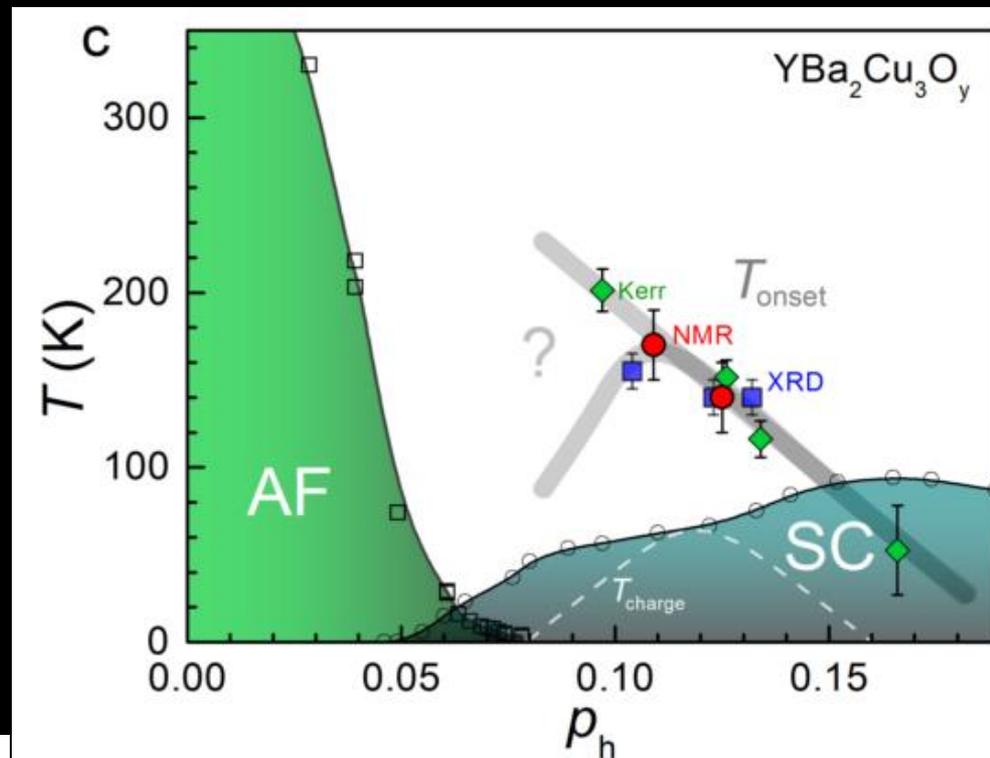


Blanco-Canosa, arxiv: 1406.1595

# Doping, B, and T dependence?



YBCO (from NMR):  
distinguishes between  
 $T_{CDW}$  (long-range order)  
and  $T_{onset}$



# Charge Order Questions



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3. Are we within the CDW phase or just disorder-pinned fluctuations?  
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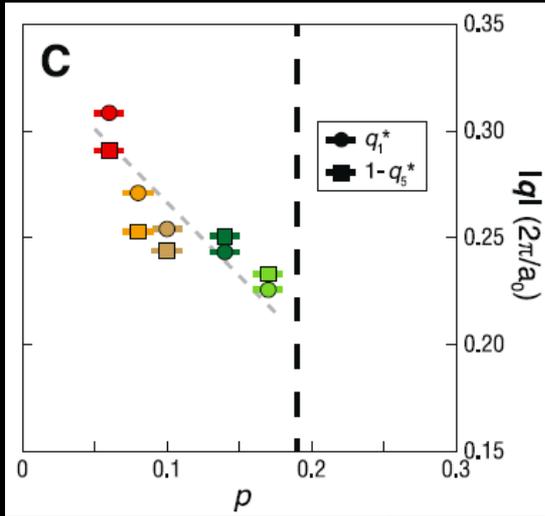


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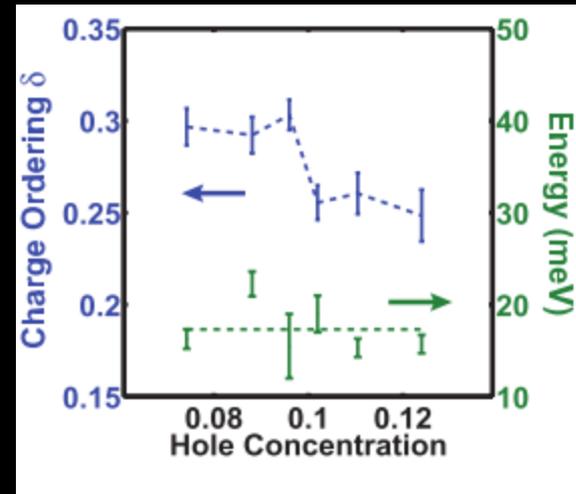
# Wavevector of CDW?



## Bi2212: continuous evolution vs. step function with doping

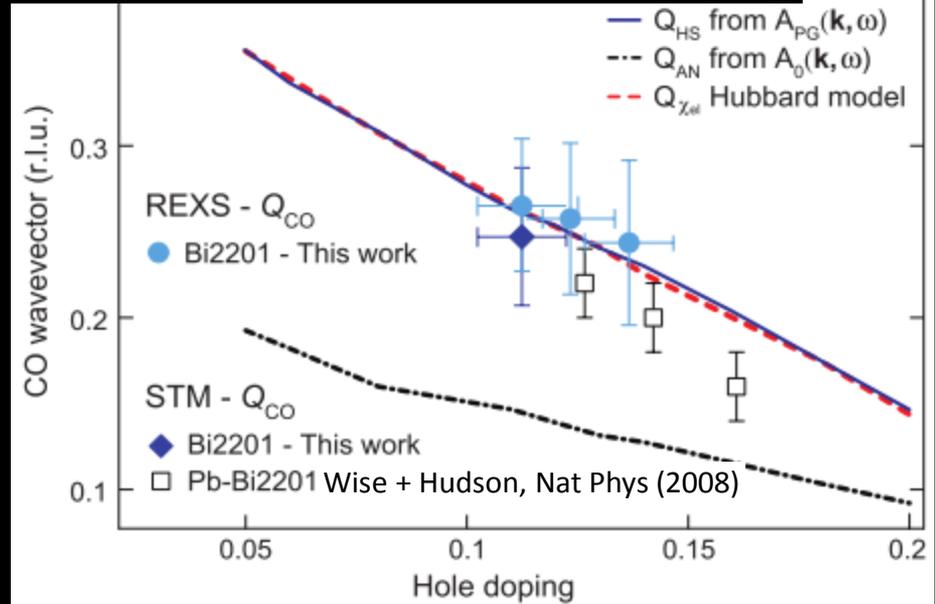


Fujita+Davis, *Science* (May 2014)



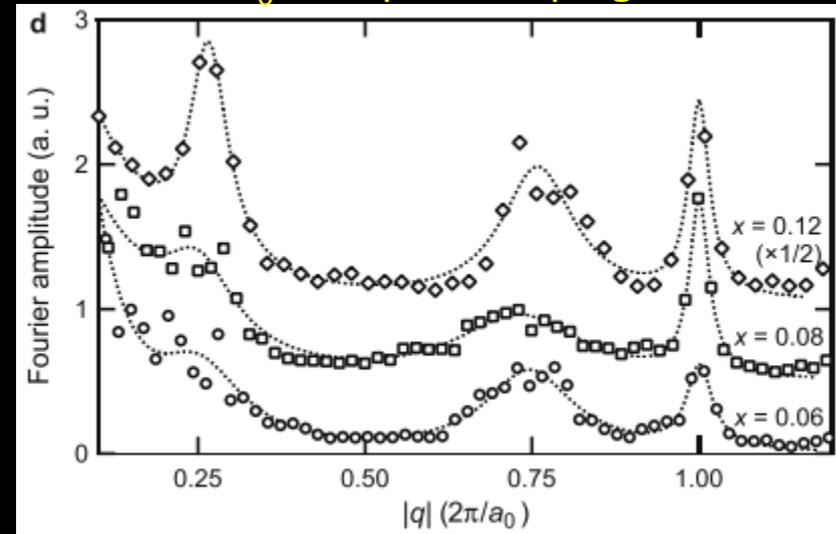
da Silva Neto+Yazdani, *Science* (Jan 2014)

## Bi2201: continuous evolution w/ doping



Comin+JEH, *Science* (Jan 2014)

## Na-CCOC: $4a_0$ , indept. of doping



Kohsaka, *Nat Phys* (2012)

# CDW is hotspot wavevector, not antinodal nesting



Bi2201  
OPT35K

5mV

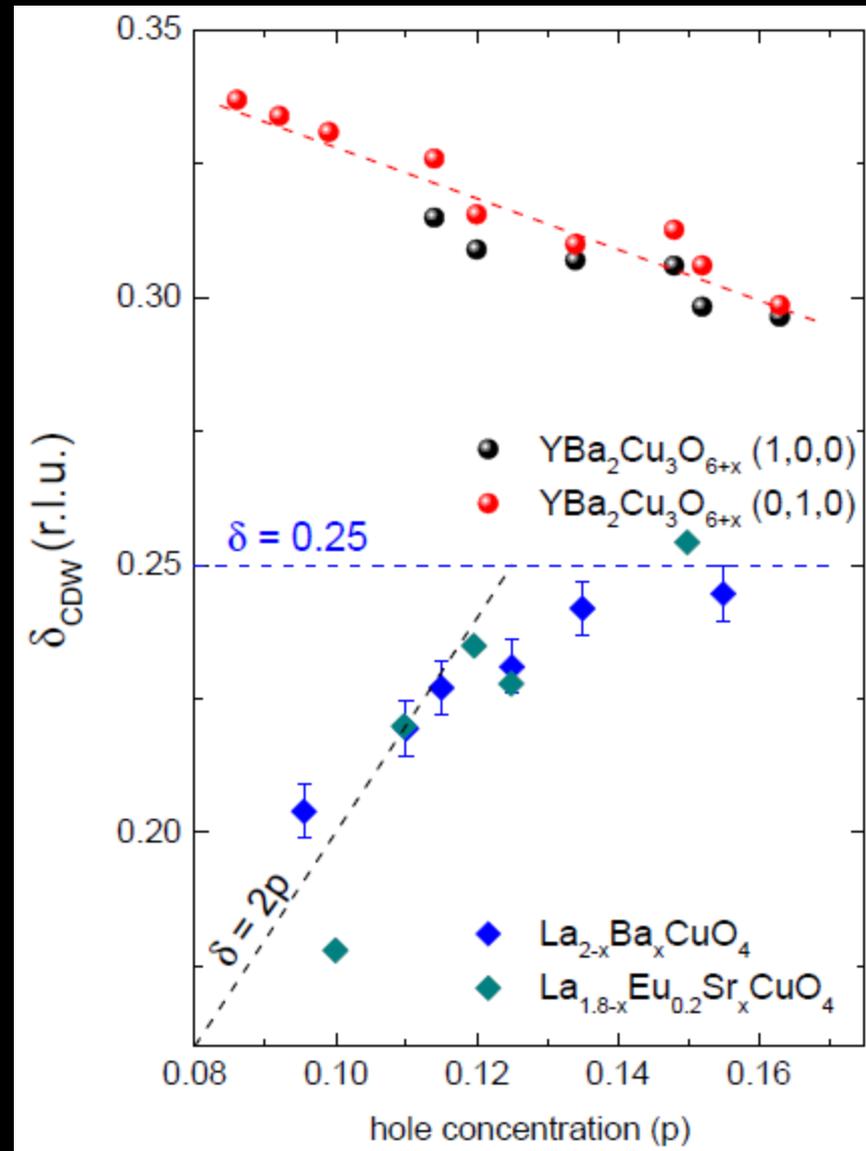
50mV

Red lines passing  
through antinodal FS  
at low energy...

do not pass through  
the Bragg reflections of  
the smectic near  $\Delta_{PG}$

→ charge order wavevector is the AFBZ hotspot wavevector,  
not the antinodal nesting vector

# YBCO, LSCO, LBCO from bulk probes

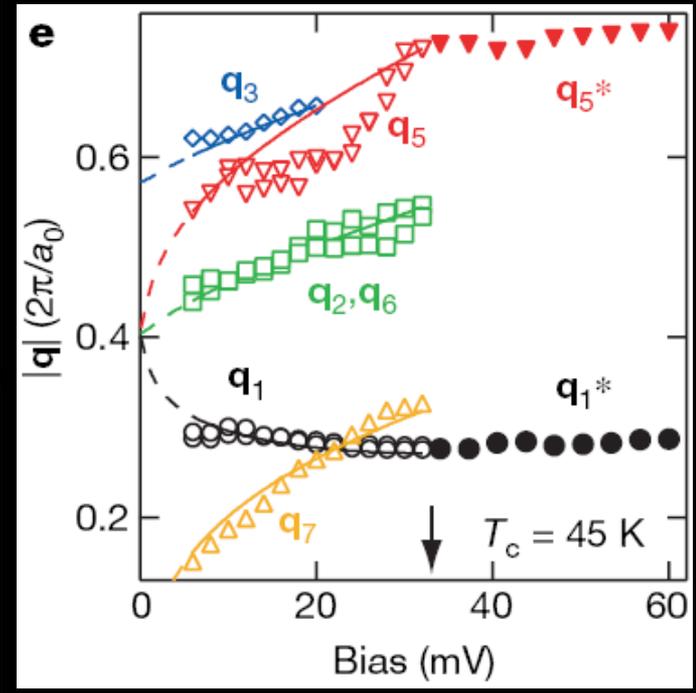
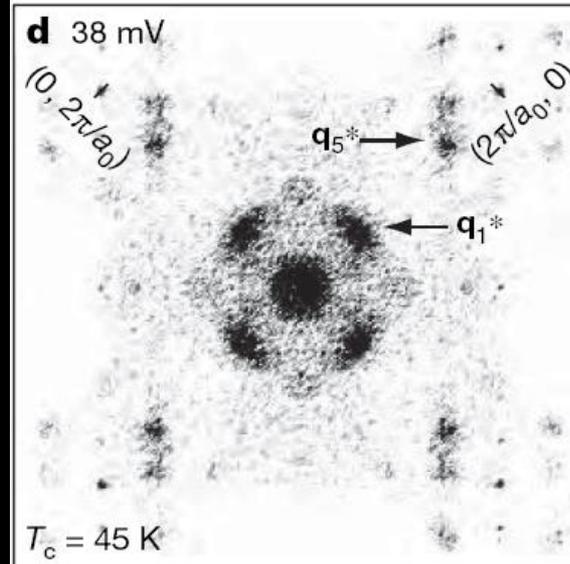
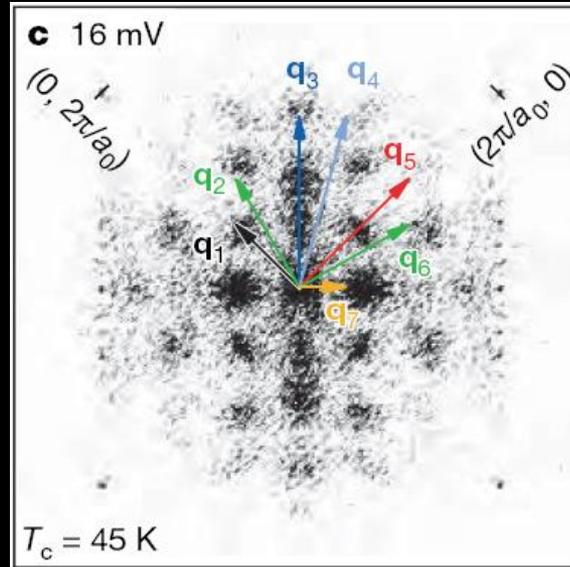
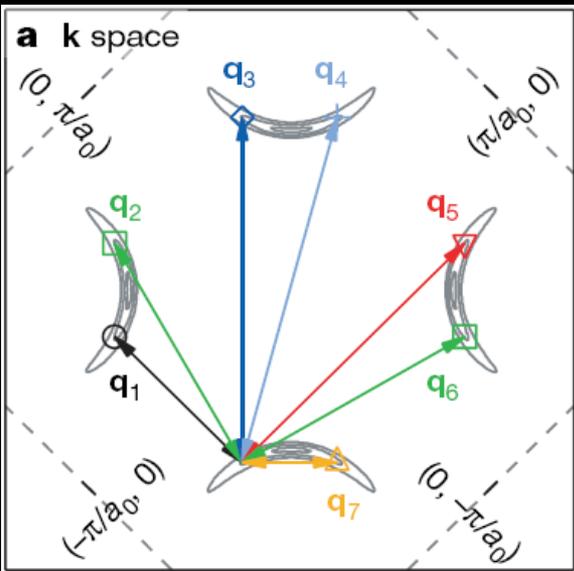


# Charge Order Questions



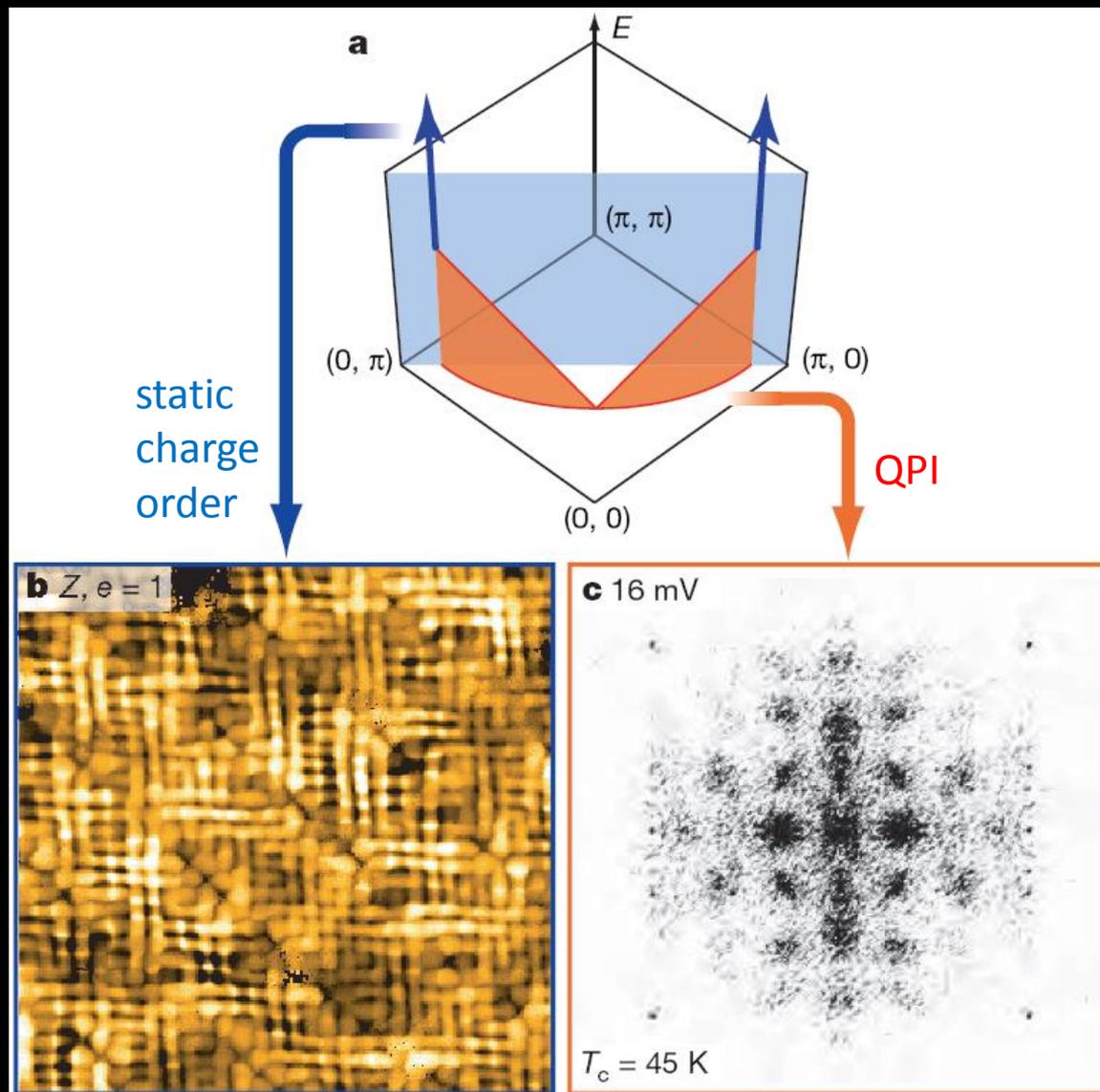
1. What is the doping,  $T$ , and  $B$  dependence of charge order?  
strongest near  $p=1/8$ , and in applied  $B$
2. Is the charge order = pseudogap, or within PG?  
appears to be within the PG
3. Are we within the CDW phase or just disorder-pinned fluctuations?  
YBCO can be long-range-ordered; BSCCO is pinned fluctuations?
4. Does charge order compete with superconductivity?  
yes! (vortex cores, dip in dome, etc.)
5. What is the wavevector of charge order – where is it living on FS?  
varies continuously w/ doping; connects AFBZ hotspots
6. What is the energy dependence of charge order?  
hard to say... maybe strongest at  $+E$ , maybe strongest at  $\Delta_{PG}$
7. Is charge order responsible for small FS?  
Bi2212: claim is yes; Bi2201: CDW constant while FS evolves
8. Is it 1D or 2D? Does it have some internal form factor?  
local 1D patches? d-wave form factor

# Bi-2212: Energy crossover: dispersing $\rightarrow$ static



$q1^*$ ,  $q5^*$  are static at high E

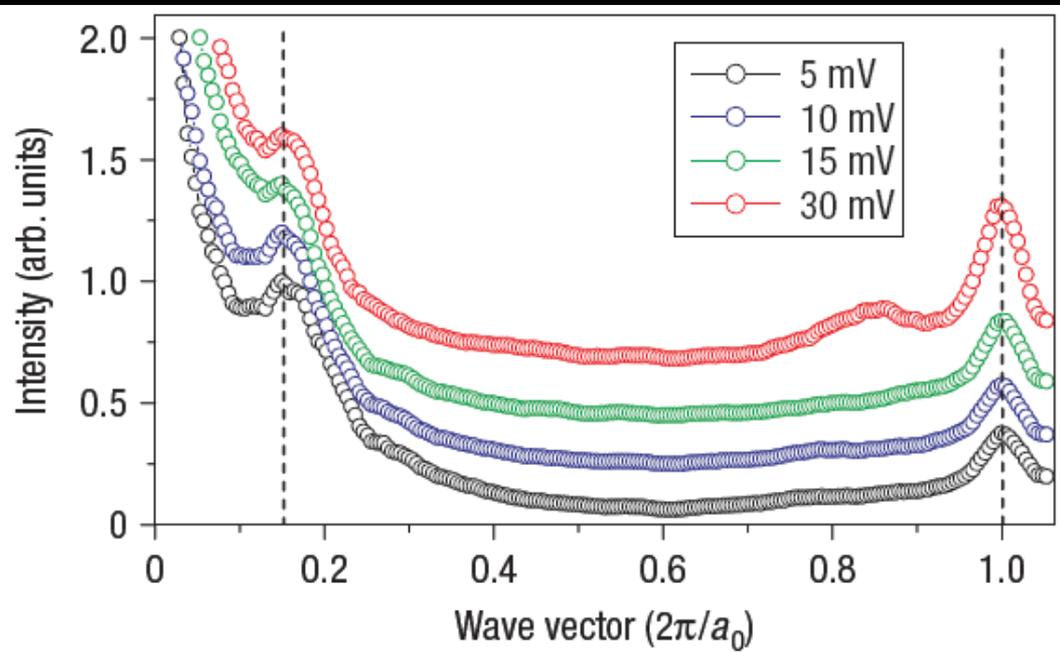
# Bi2212: 2 energy scales



# Bi2201 energy dependence



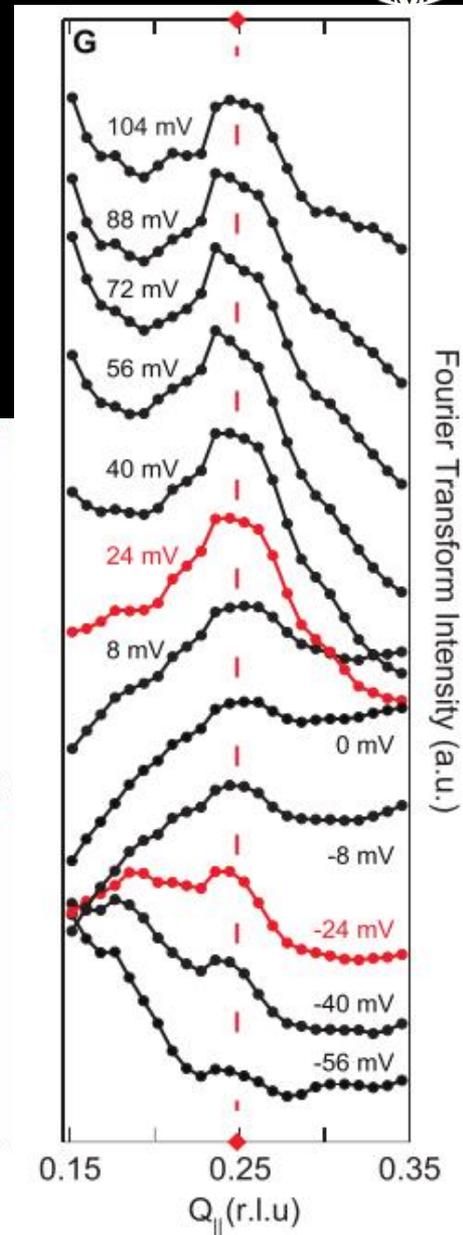
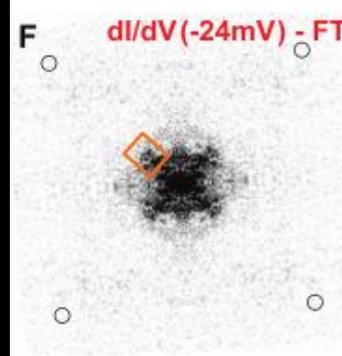
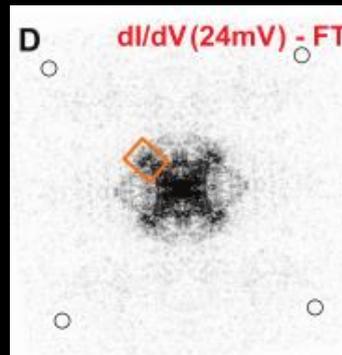
Pb-Bi2201



Wise, Nat Phys (2008)

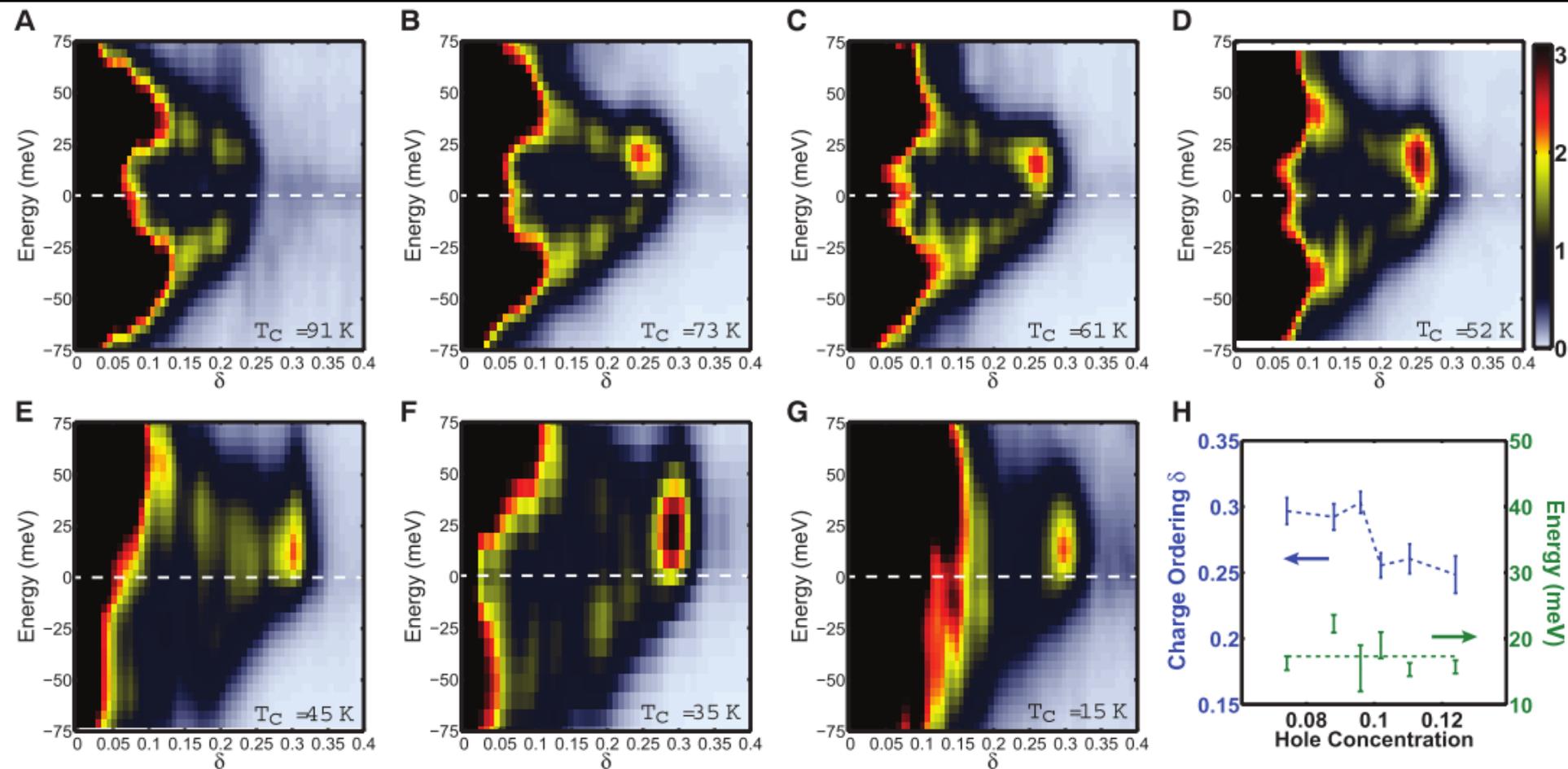
Bi2201

(-200 mV setup)



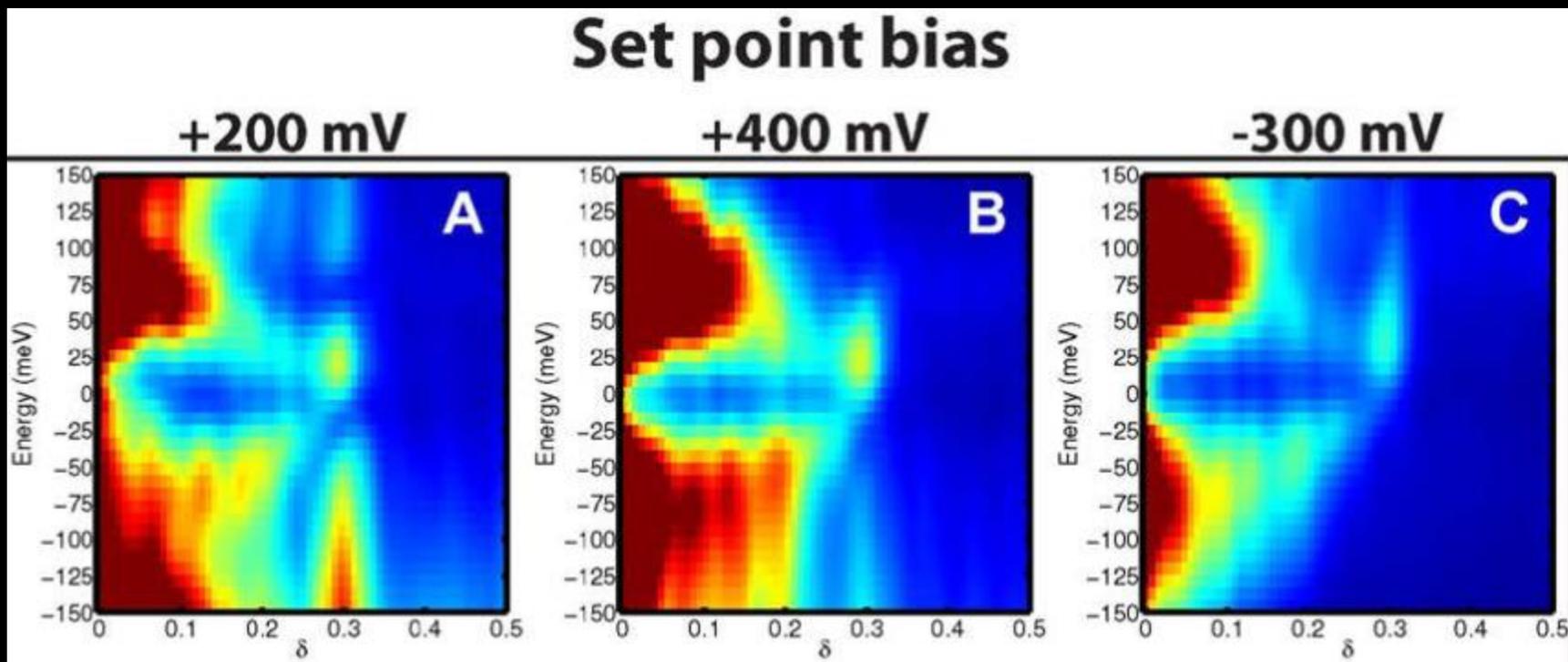
Comin, Science (Jan 2014)

# Bi2212: CDW energy dependence?



(what setpoints are used?)

# Bi2212: CDW energy dependence?



(which sample is this?)

# Charge Order Questions

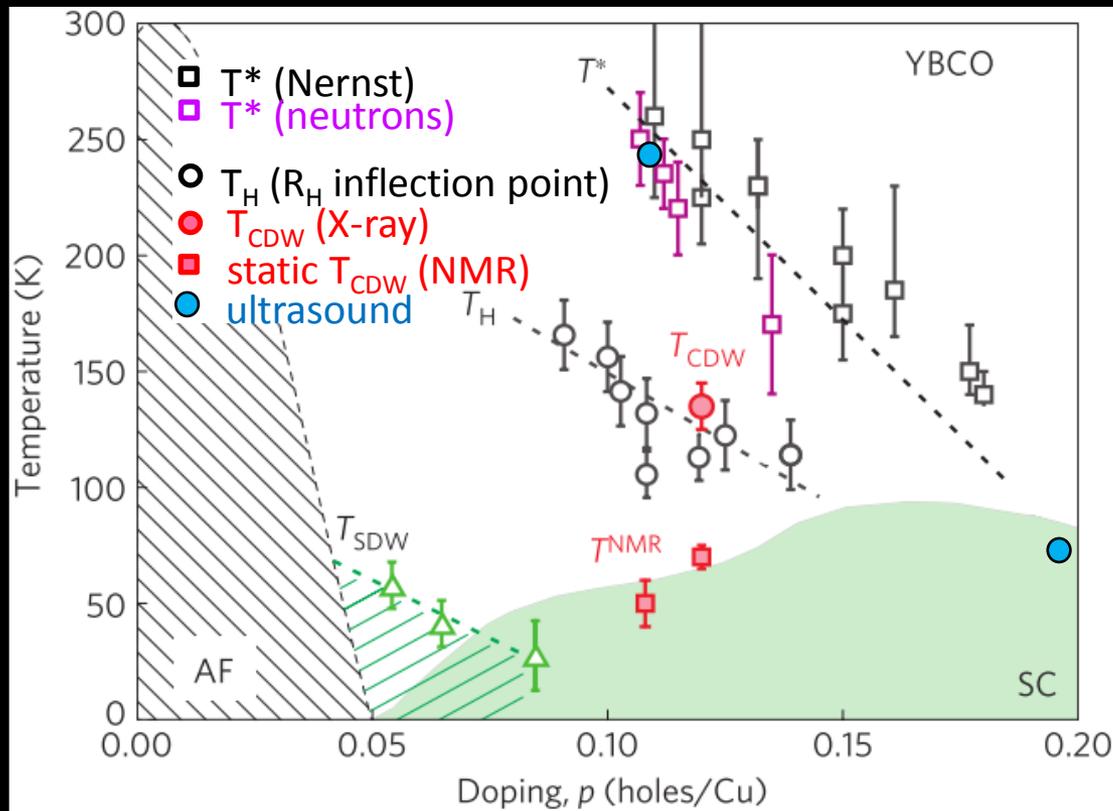


1. What is the doping,  $T$ , and  $B$  dependence of charge order?  
strongest near  $p=1/8$ , and in applied  $B$
2. Is the charge order = pseudogap, or within PG?  
appears to be within the PG
3. Are we within the CDW phase or just disorder-pinned fluctuations?  
YBCO can be long-range-ordered; BSCCO is pinned fluctuations?
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yes! (vortex cores, dip in dome, etc.)
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Bi2212: claim is yes; Bi2201: CDW constant while FS evolves
8. Is it 1D or 2D? Does it have some internal form factor?  
local 1D patches? d-wave form factor

# Fermi Surface vs. Pseudogap ?

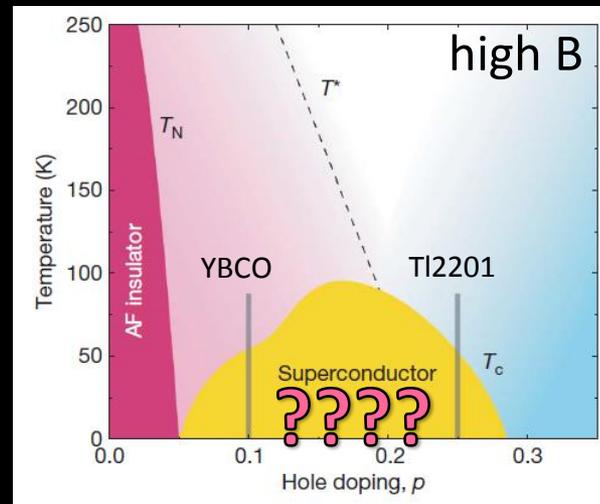


## Pseudogap & Charge order



- X-rays: Chang + Forgen + Hayden, Nat Phys 8, 871 (2012)*
- neutrons: Li + Greven, Nature 455, 372 (2008)*
- Nernst: Daou + Taillefer, Nature 463, 519 (2010)*
- Hall: LeBoeuf + Taillefer, PRB 83, 054506 (2011)*
- NMR: Wu + Julien, Nature 477, 191 (2011)*
- ultrasound: Shekhter + Ramshaw, Nature 498, 75 (2013)*

## Fermi surface

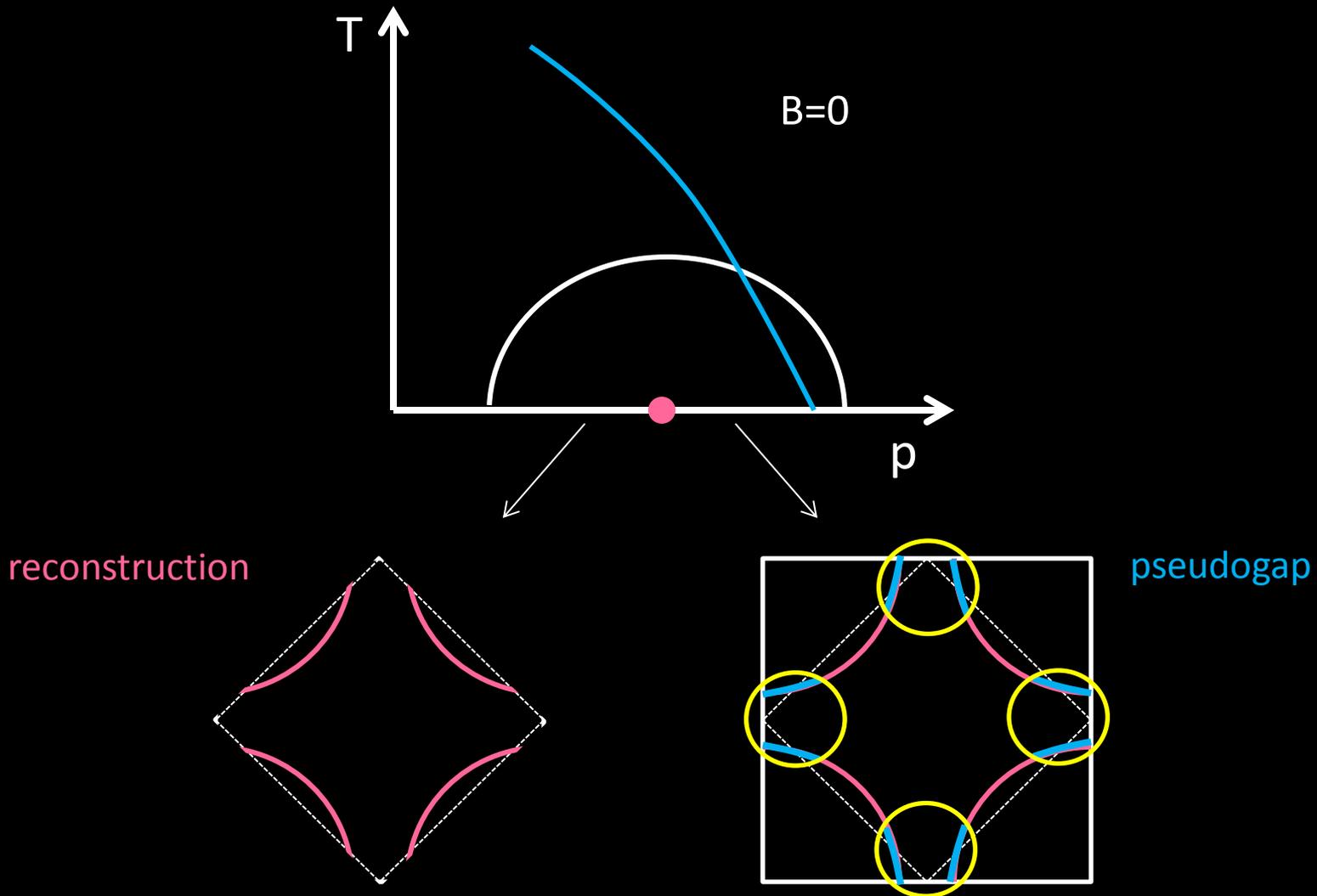


- Doiron-Leyraud, Nature 447, 565 (2007)*
- Vignolle, Nature 455, 952 (2008)*

# Our Conclusions (STM on Bi2201)



## 1. Fermi surface reconstruction $\neq$ pseudogap



## 2. Superconductivity coexists with pseudogap at the antinode

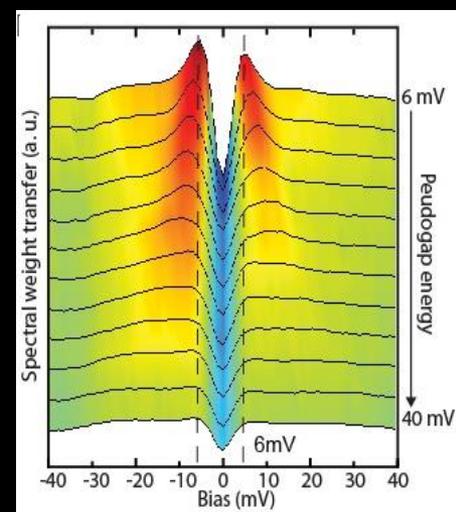
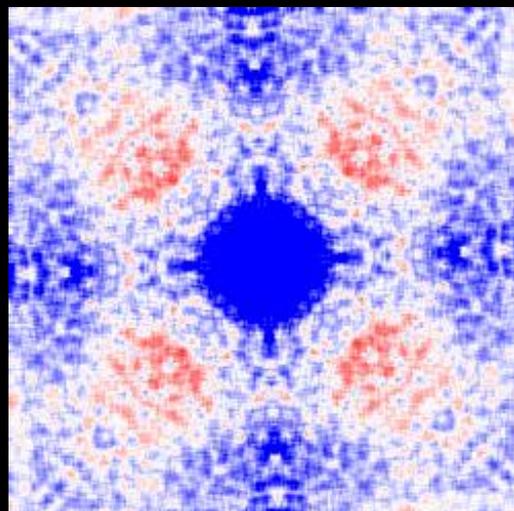
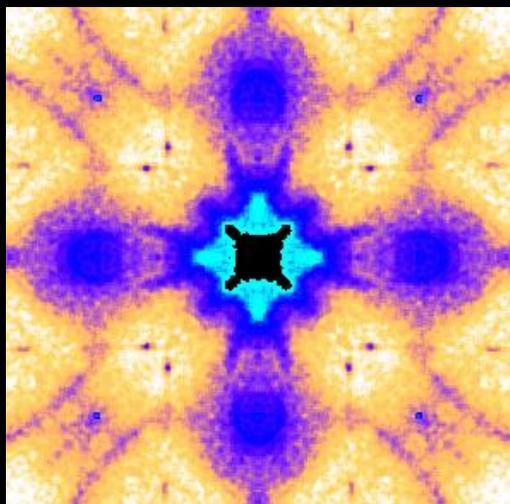
## 1. Where is the Fermi surface reconstruction?

Answer: coincides with QCP near optimal doping at  $B=0$

## 2. What is the role of the pseudogap?

Answer:

- separate occurrence
- coexists with superconductivity at the antinode
- causes decoherence at the nanoscale

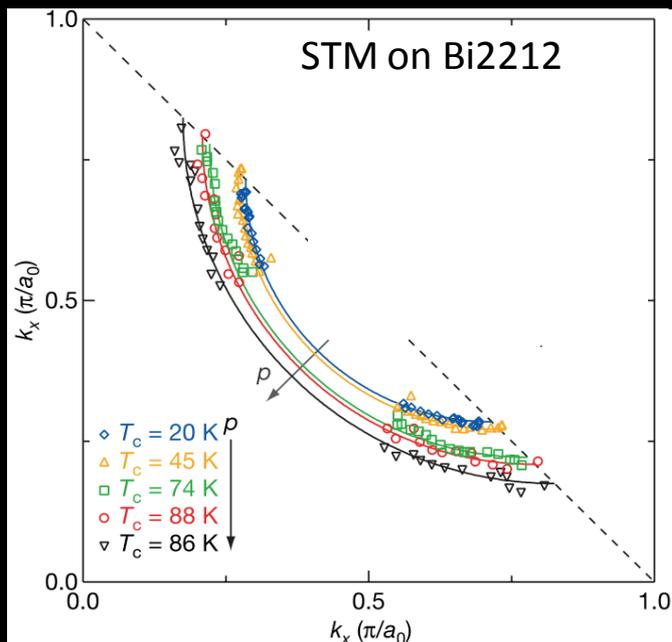


arxiv:1305.2778, He et al, *Science*, May 9 (2014)

# Intro to Fermi arc phenomenology in Bi2212

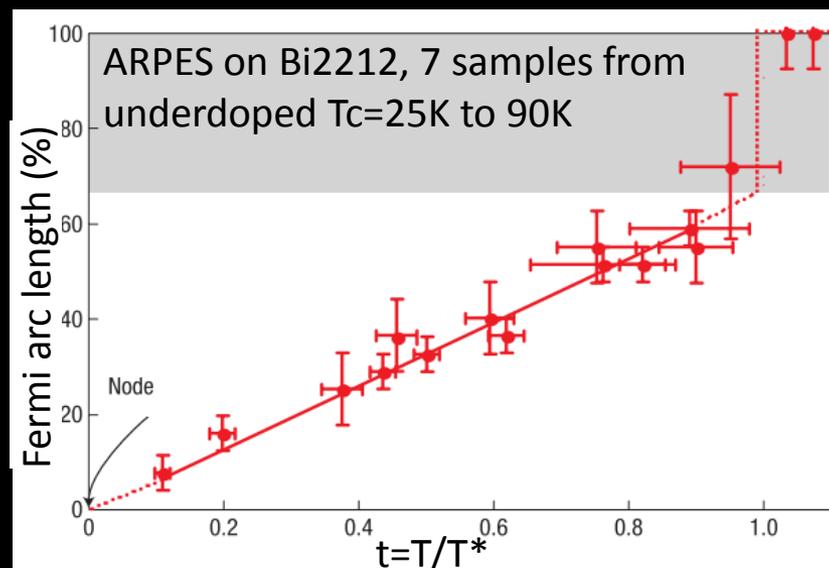


## Arc cuts off at AFBZ

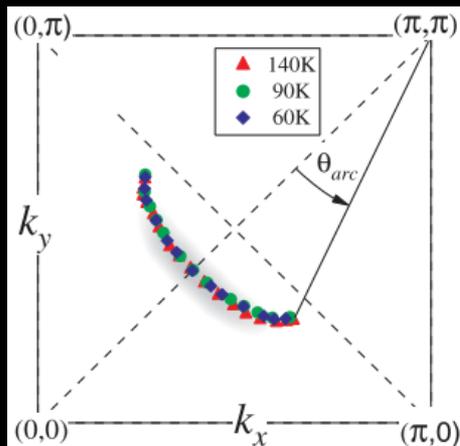
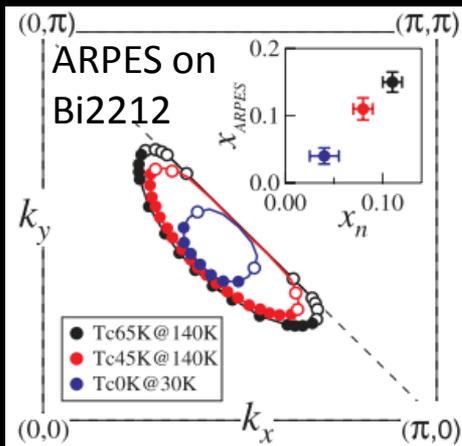


Kohsaka + JC Davis, Nature 454, 1072 (2008)

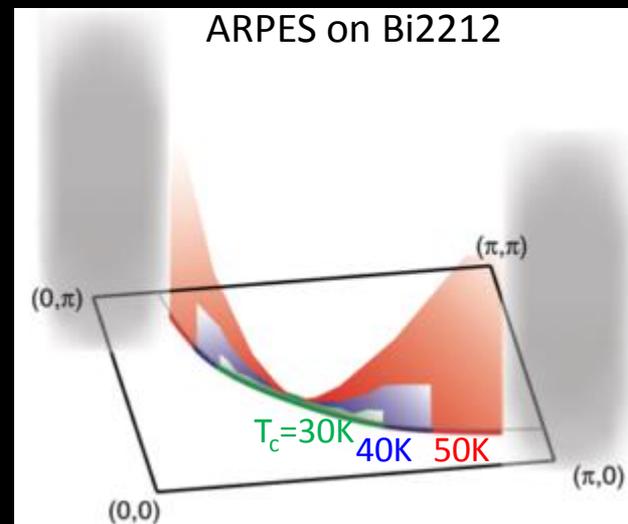
## Arc length evolves with $T, \rho$



Kanigel + Norman + Campuzano, Nat Phys 2, 447 (2006)

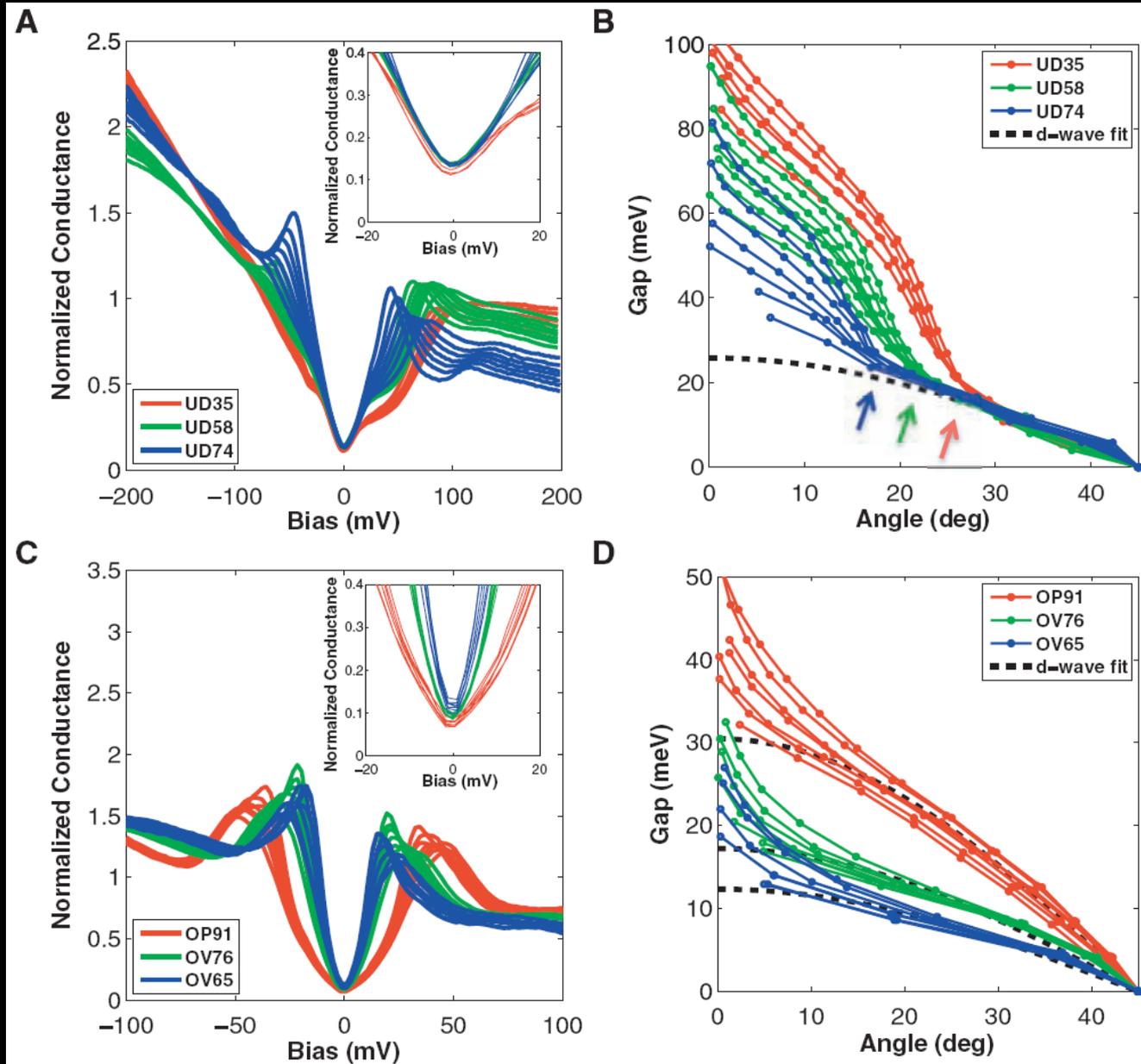


Yang + PD Johnson, PRL 107, 047003 (2011)



Tanaka + ZX Shen, Science 314, 1910 (2006)

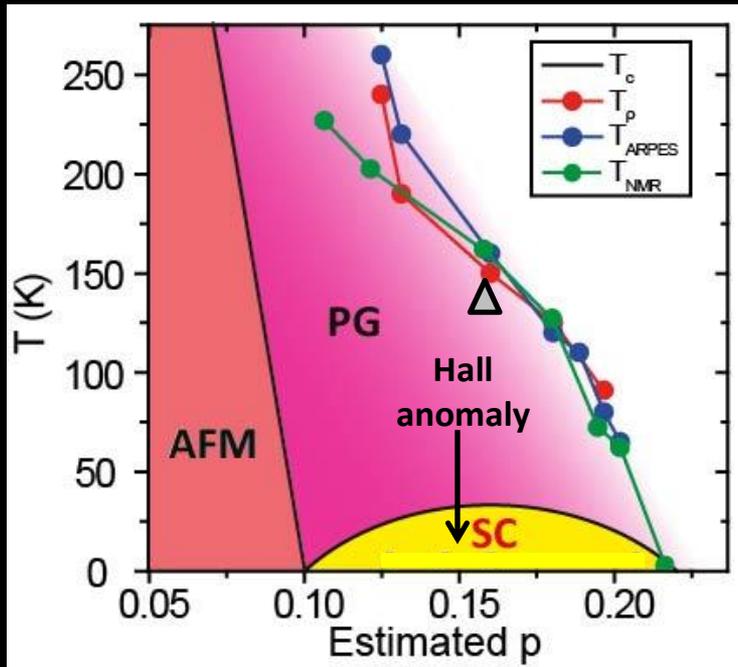
# Bi2212 k-space info, a different way



# Motivation to study Pb-doped Bi2201

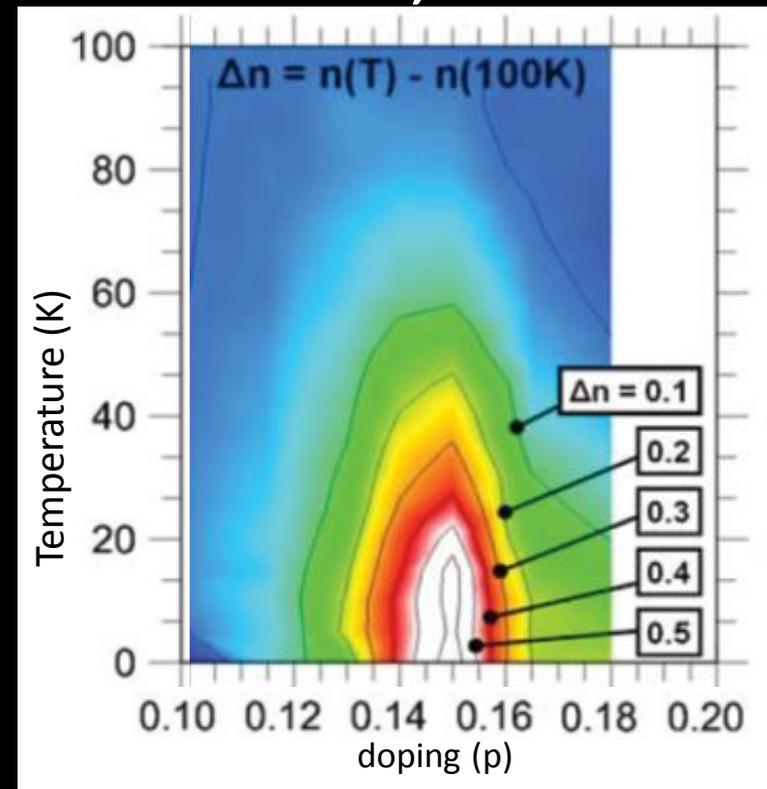


- No supermodulation or bilayer splitting artifacts
- Well-characterized pseudogap persists throughout the phase diagram
- Evidence for a quantum critical point near optimal doping (at high B)



- resistivity,  $B=0$ , Kondo, *Nat Phys* 7, 21 (2010)
- ARPES,  $B=0$ , Kondo, *Nat Phys* 7, 21 (2010)
- NMR,  $B=28-43T$ , Zheng, *PRL* 94, 047006 (2005)
- △ Kerr, ARPES, time-resolved reflectivity  
He + Kivelson + Kapitulnik + Orenstein + ZX Shen, *Science* 331, 1579 (2011)
- SC dome, Ando, *PRB* 61, R14956 (2000)

## Hall coeff, $B > 30 T$

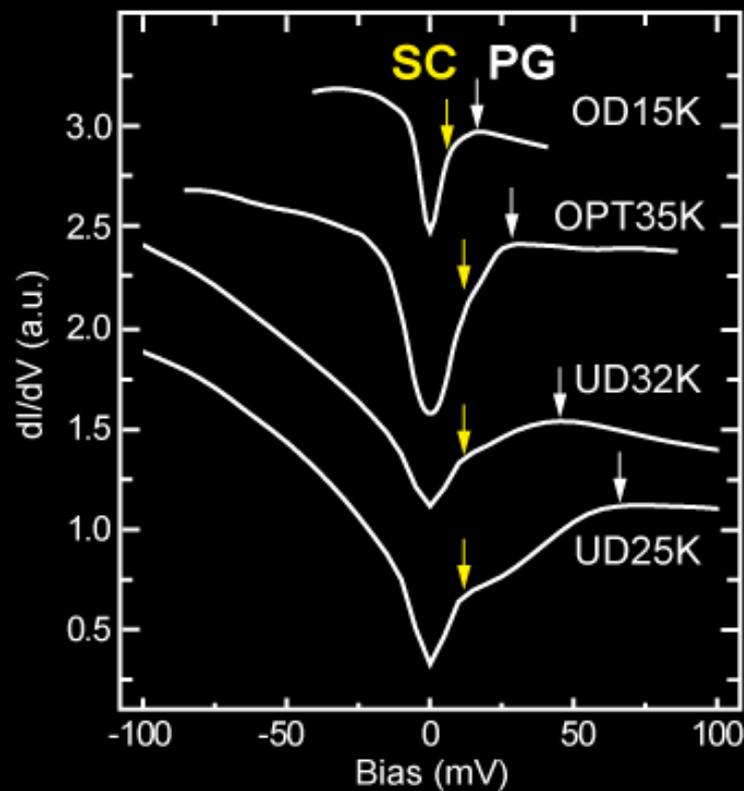
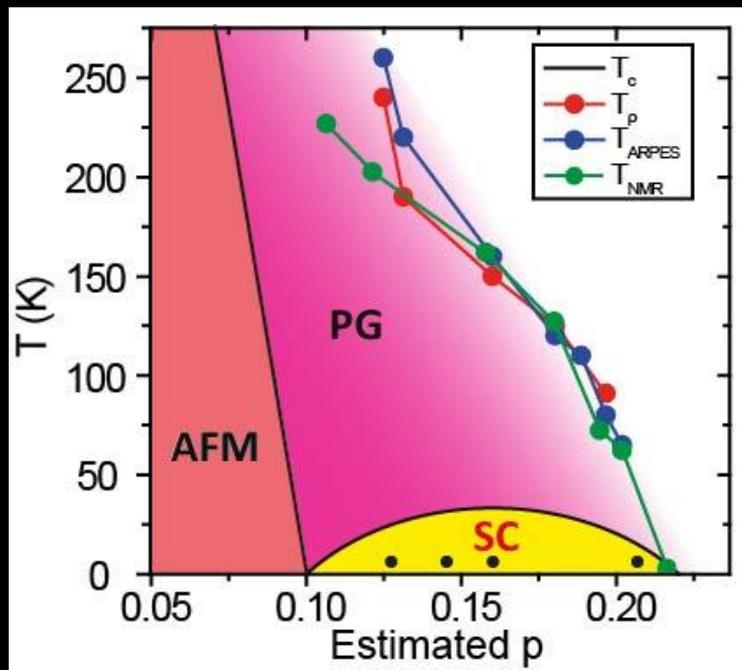


Balakirev, *Nature* 424, 912 (2003)  
Balakirev, *PRL* 102, 017004 (2009)

Does the FS reconstruct at  $B=0$  Tesla?

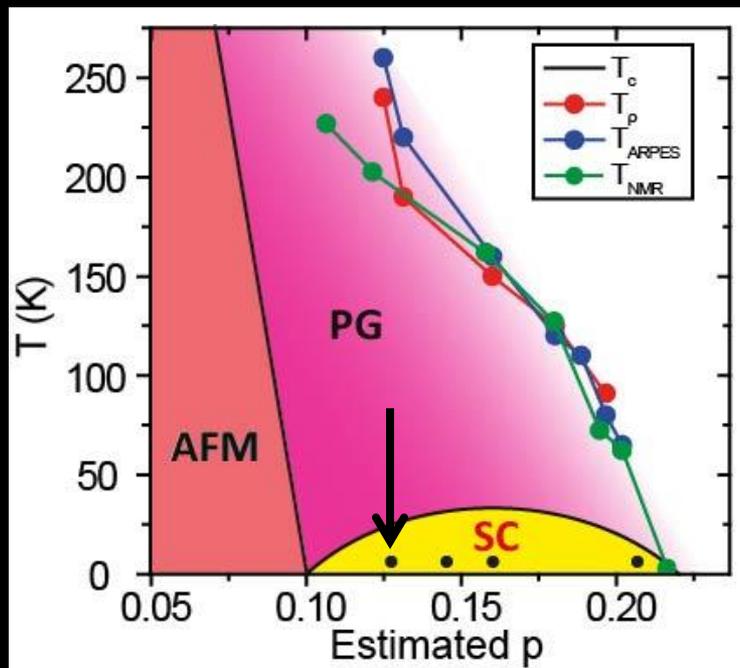
Does the FS reconstruction correspond to Hall QCP ( $p \sim 0.15$ ) or PG ( $p \sim 0.23$ )?

# STM studies of Pb-doped Bi2201



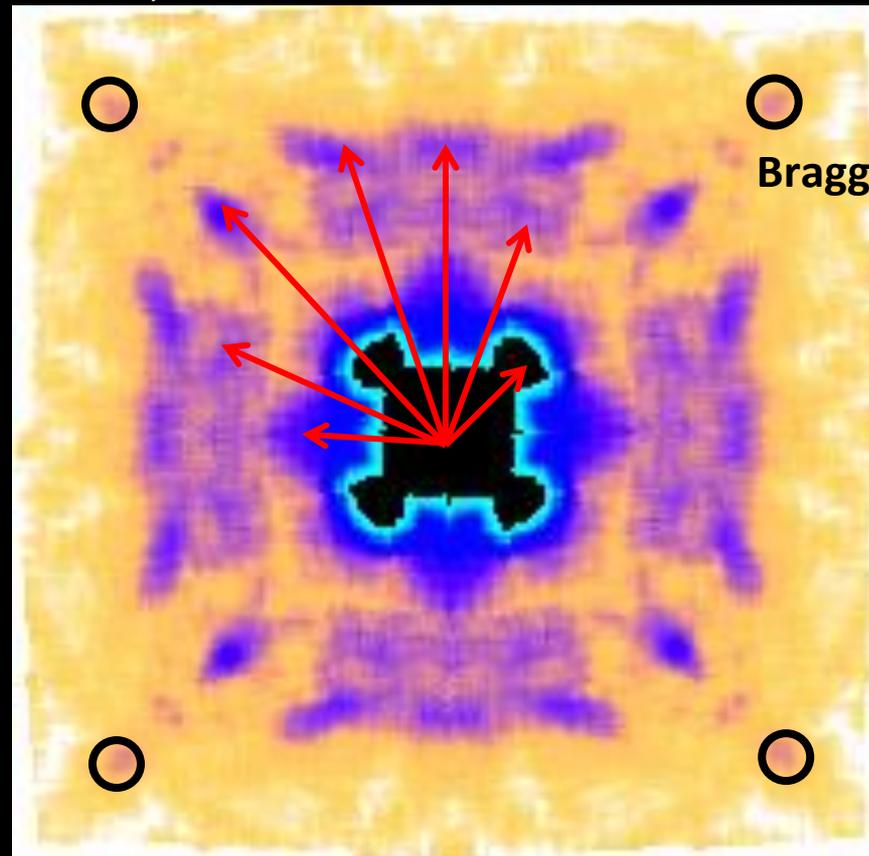
arxiv:1305.2778, to appear in *Science*, May 9 (2014)

# Octet QPI in UD25K Bi2201



Bi2201, UD25K

9mV



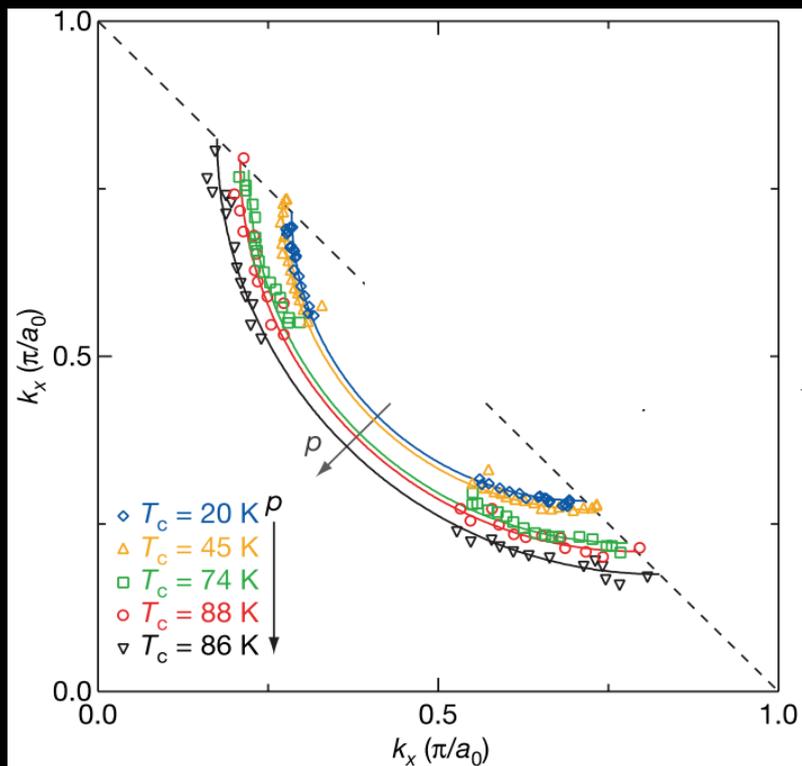
Low  High

(Fourier transform of a real space  $dI/dV$  map)

# Extinction of octet QPI

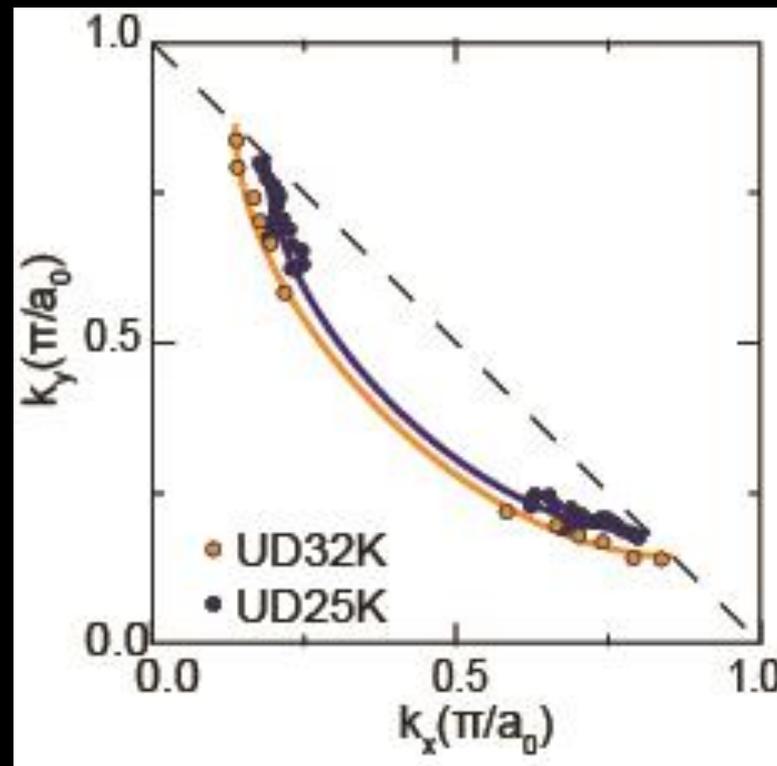


Previous work: Bi2212



Kohsaka, Nature 454, 1072 (2008)

Our data: Bi2201



arxiv:1305.2778, to appear in *Science*, May 9 (2014)

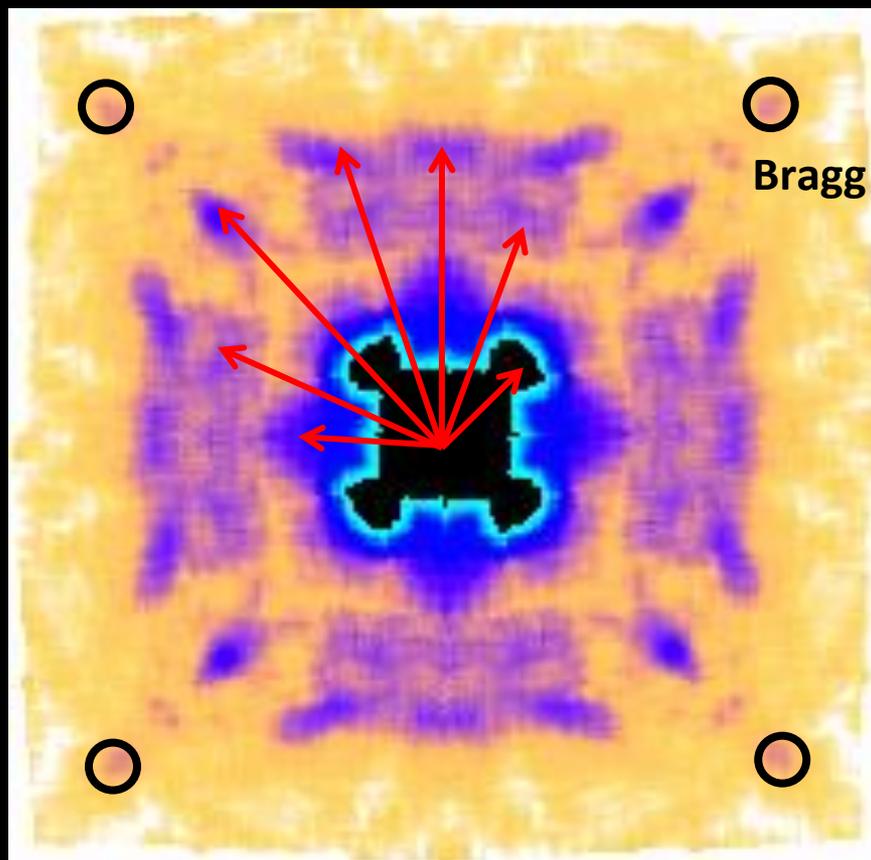


# Compare QPI in UD25K and UD32K



UD25K

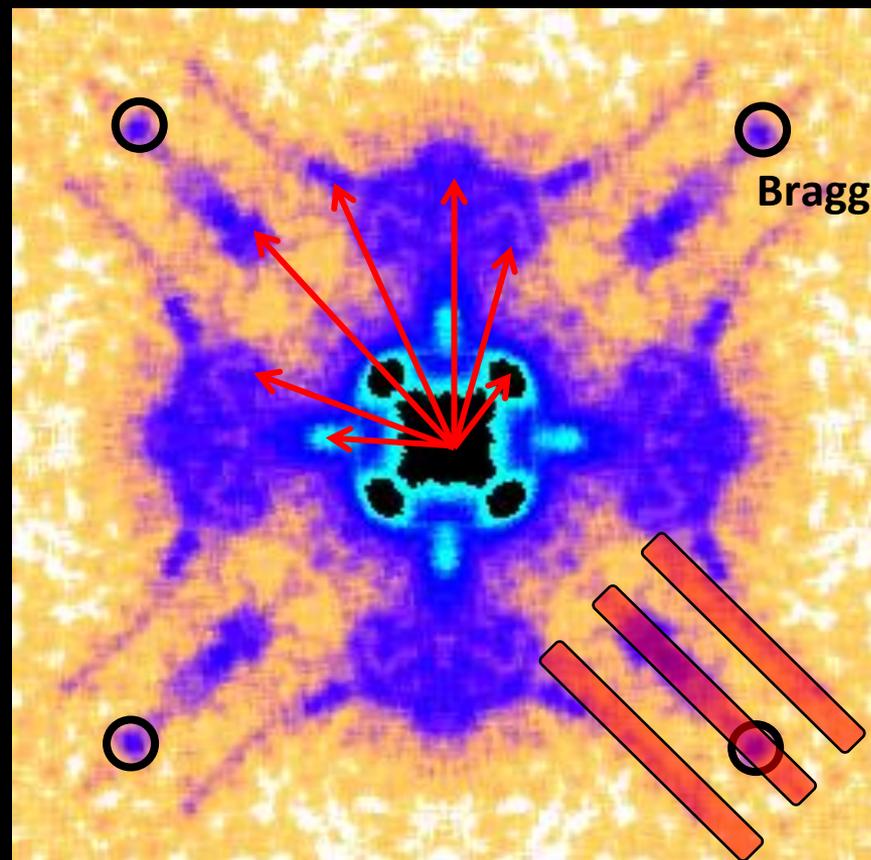
9mV



Low  High

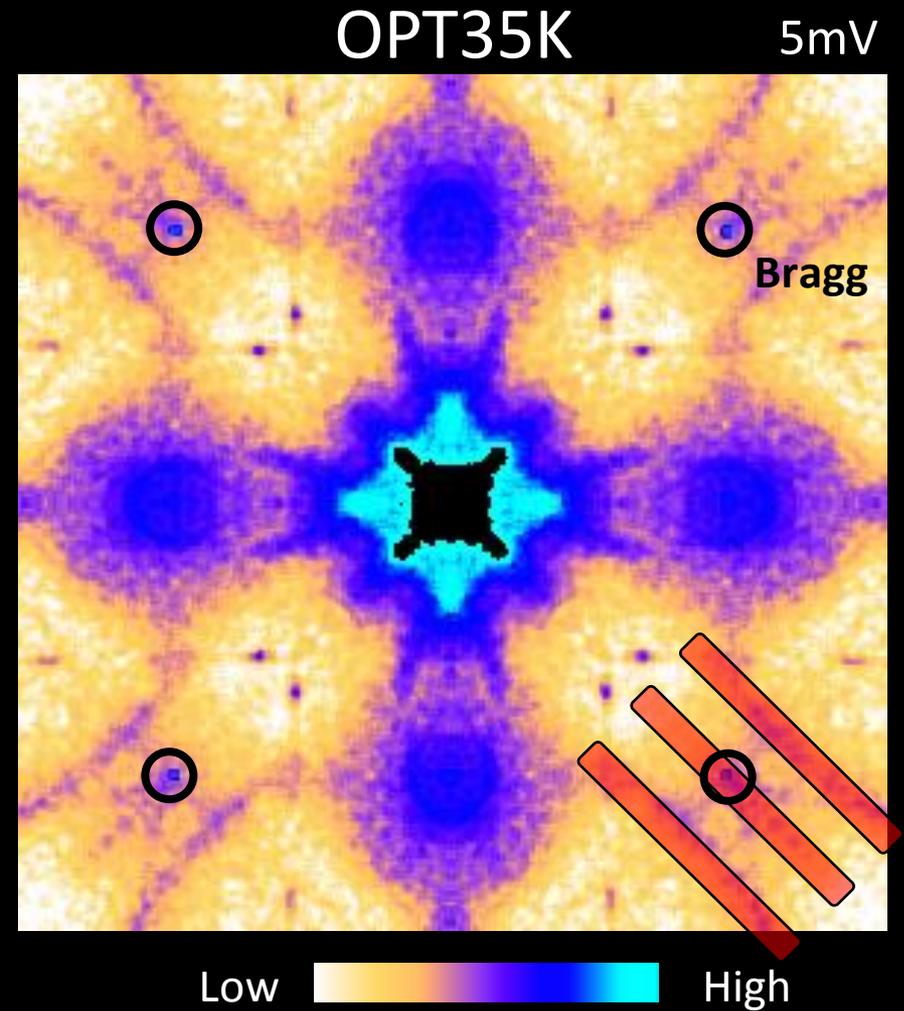
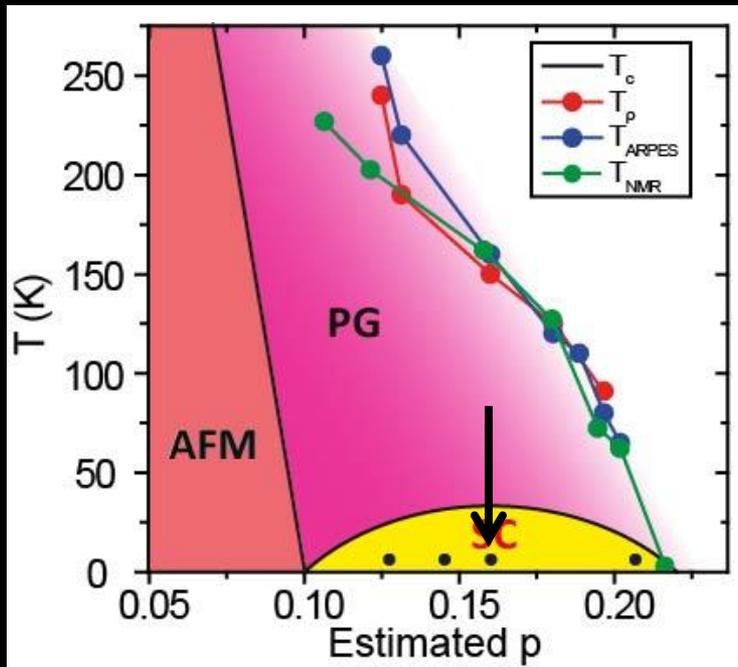
UD32K

5mV

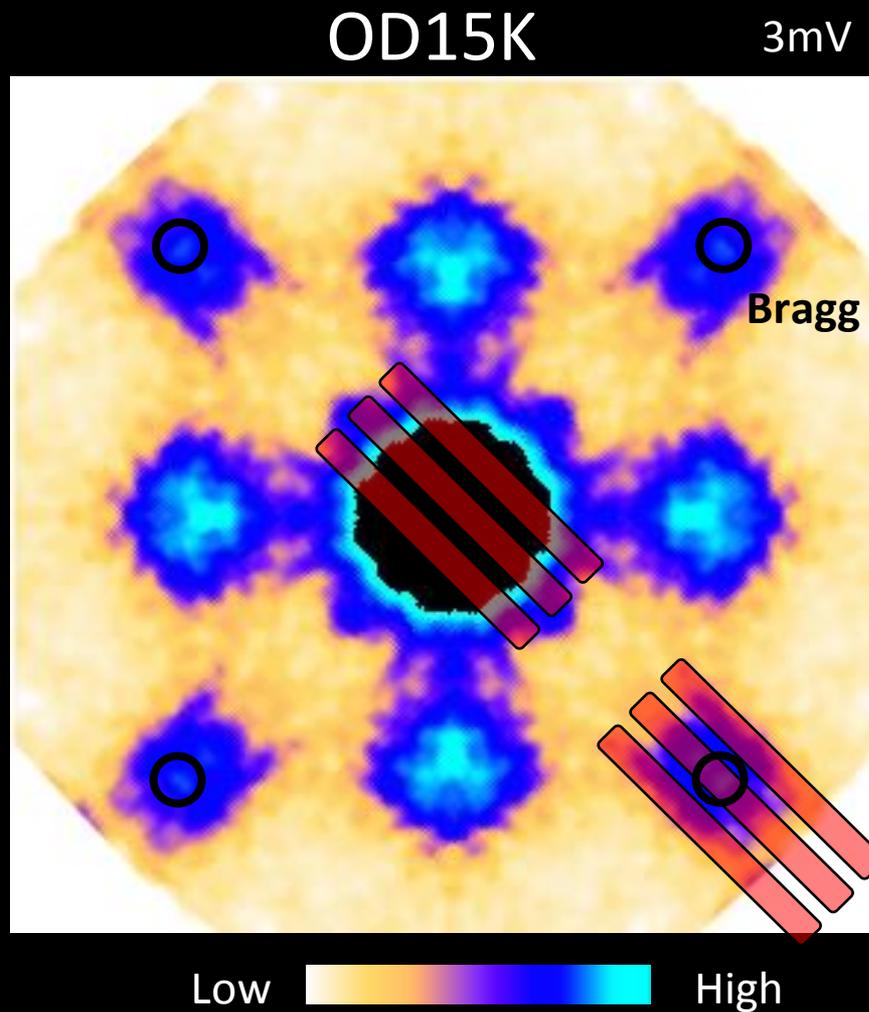
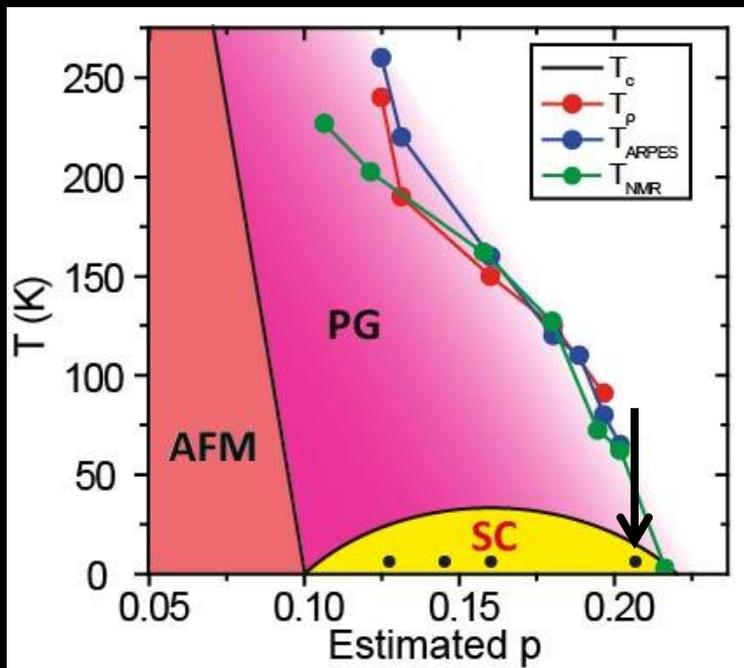


Low  High

# QPI in OPT35K



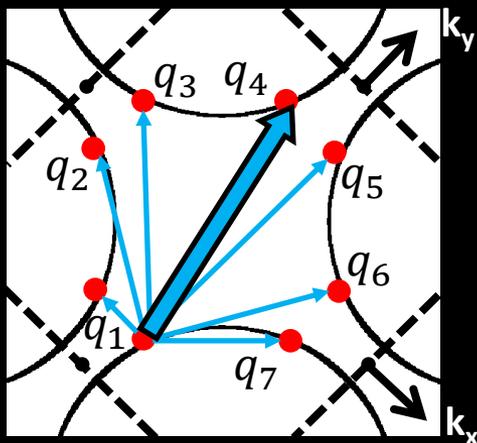
# QPI in OD15K



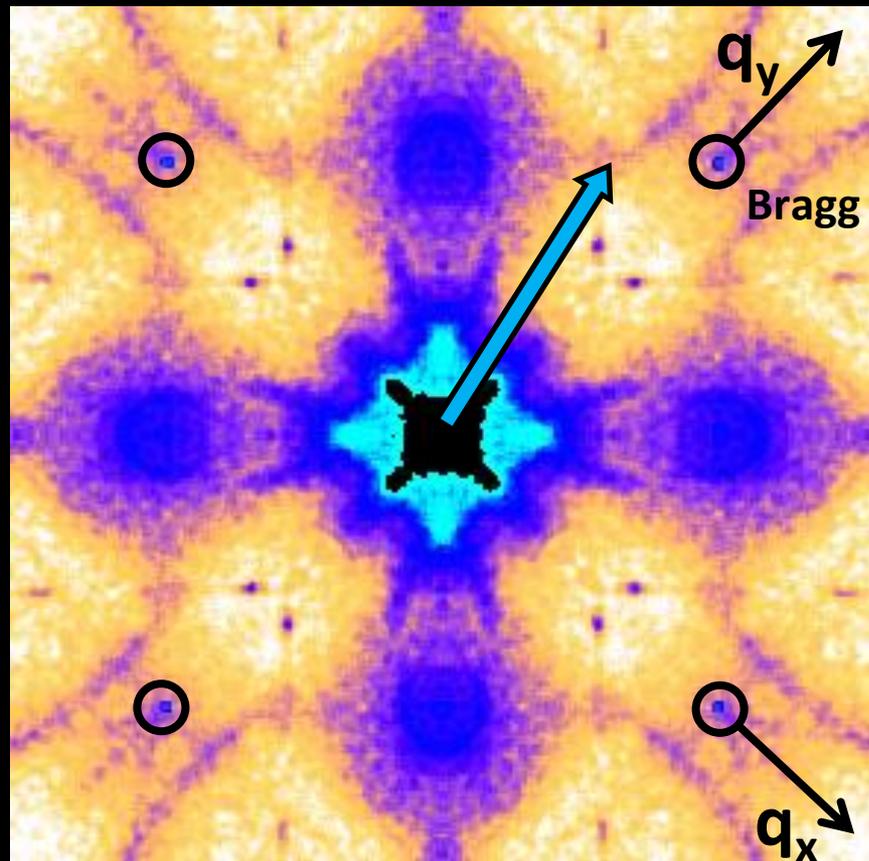
# Compare Fermi surface to QPI



k space Fermi surface



q space QPI



OPT35K 5mV

Low

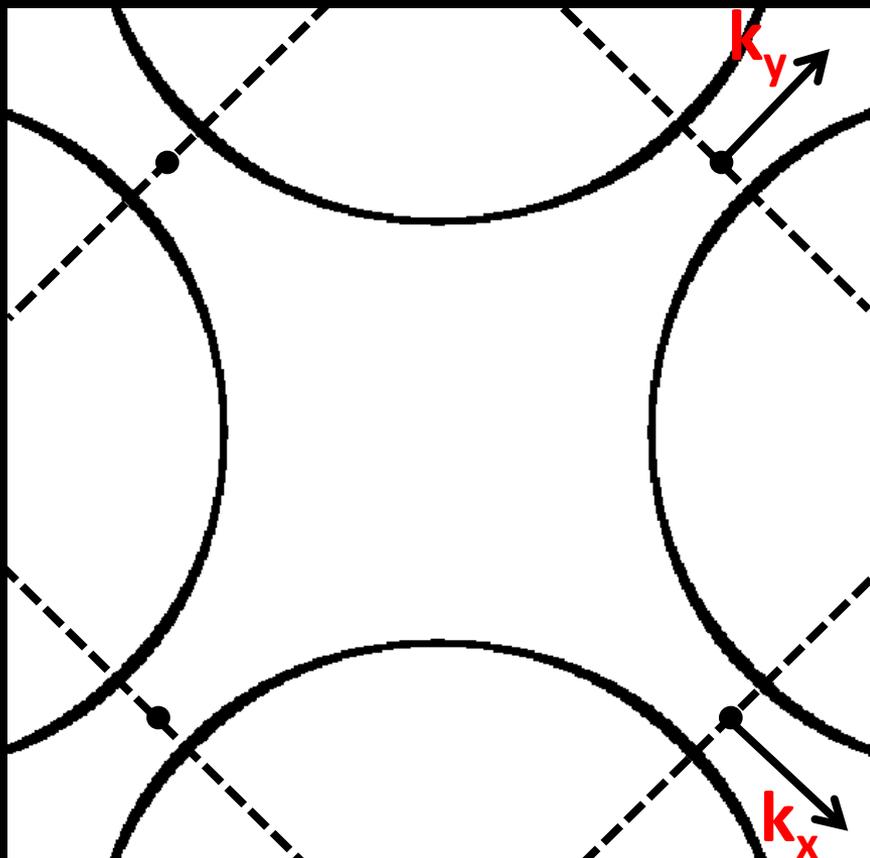
High

$q_4 = (2k_x, 2k_y)$  which follows the Fermi surface

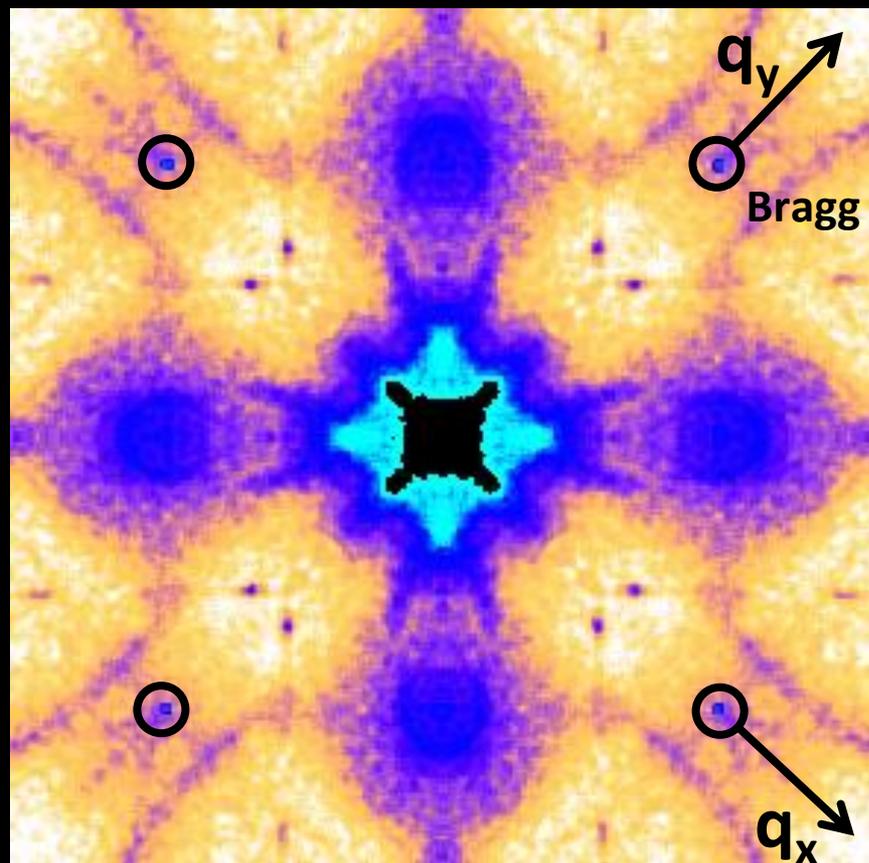
# Compare Fermi surface to QPI



2 x k space Fermi surface



q space QPI



OPT35K 5mV

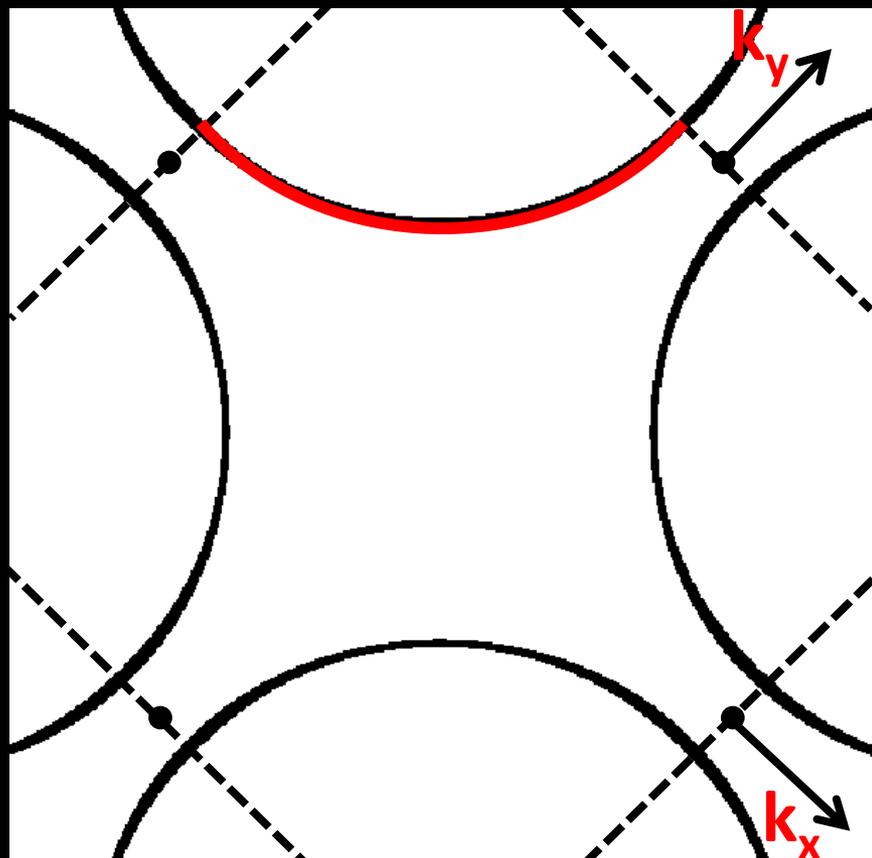
Low  High

$q_4 = (2k_x, 2k_y)$  which follows the Fermi surface

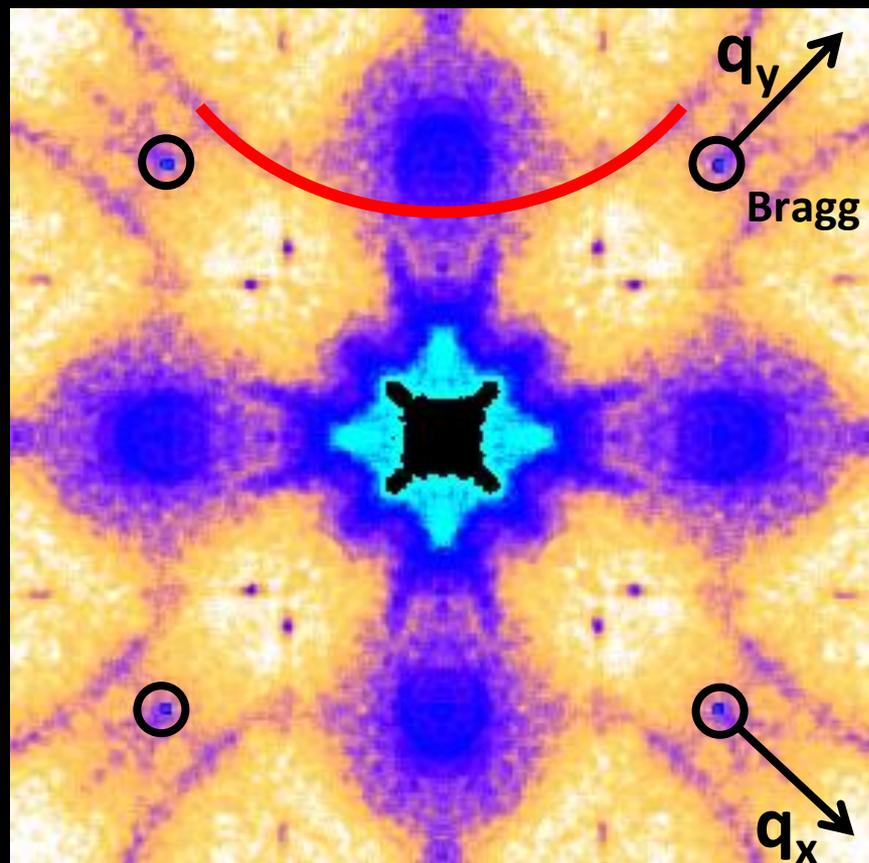
# Compare Fermi surface to QPI



2 x k space Fermi surface



q space QPI



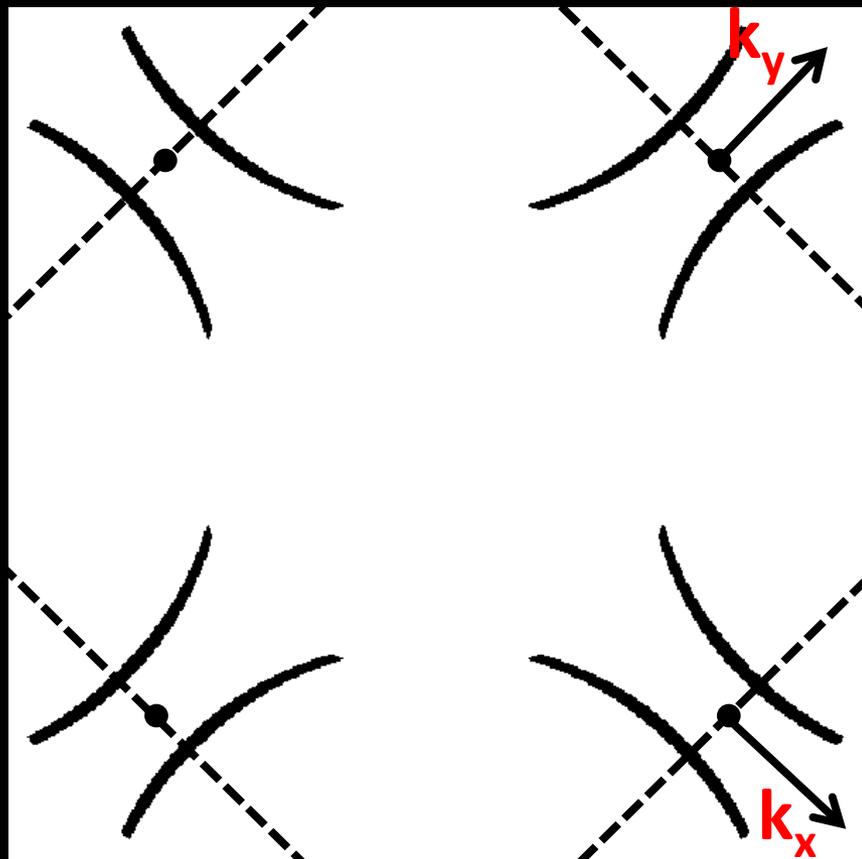
Low  High

$q_4 = (2k_x, 2k_y)$  which follows the Fermi surface

# Autocorrelate just the antinodal Fermi surface

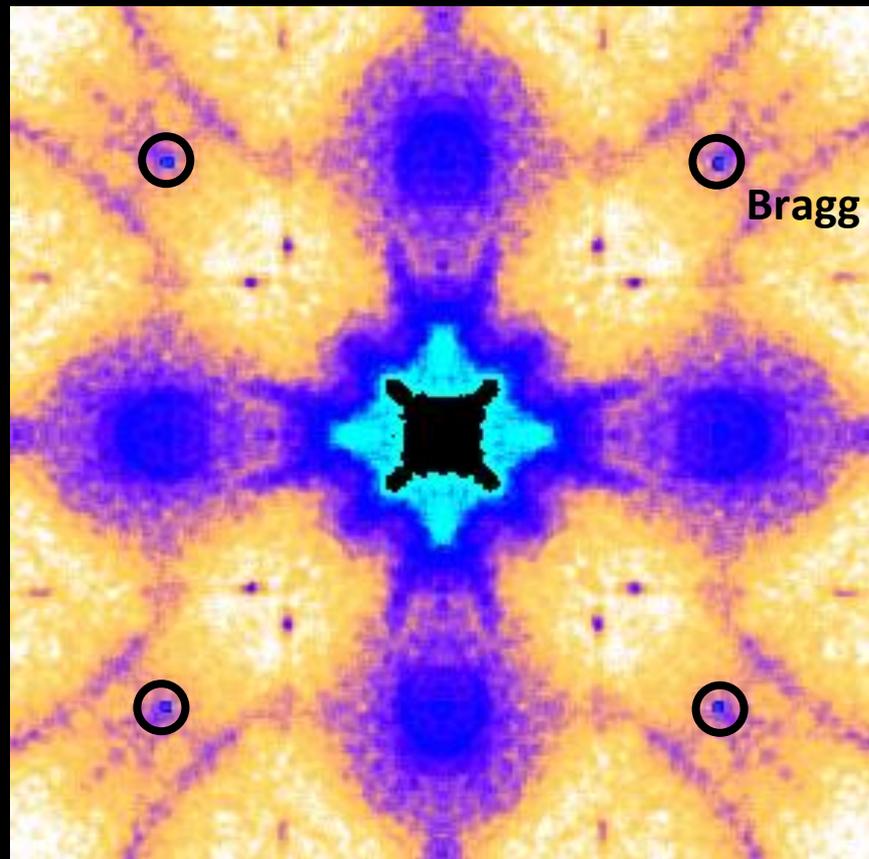


2 x Antinodal Fermi surface



q space QPI

OPT35K 5mV



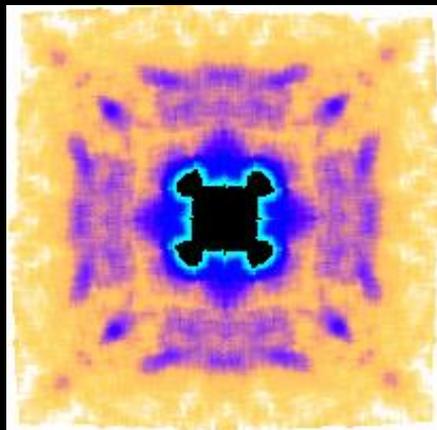
Low  High

Triplet feature comes from antinode.

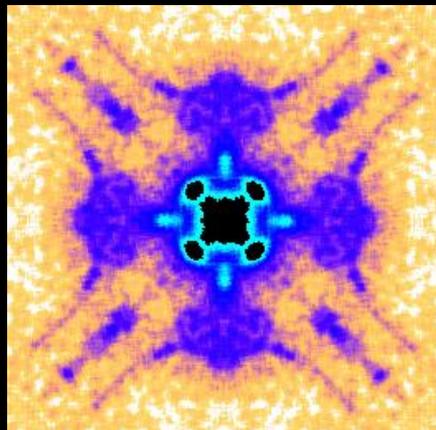
# Luttinger count



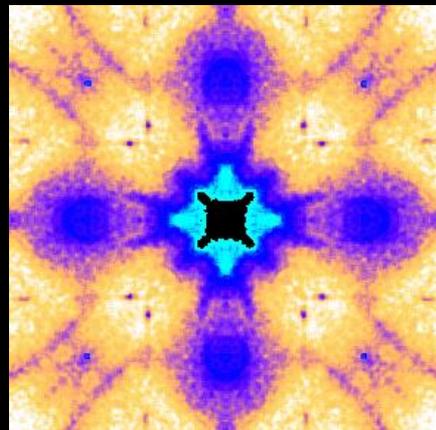
UD25K



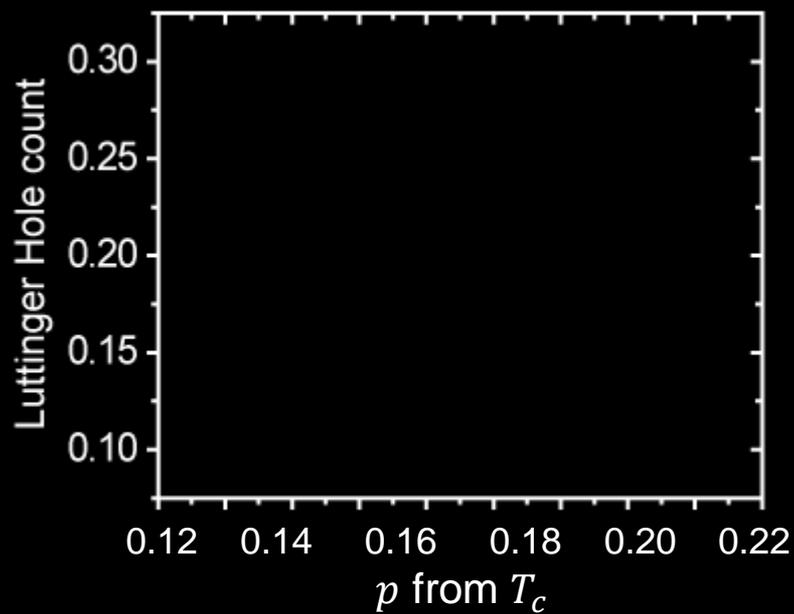
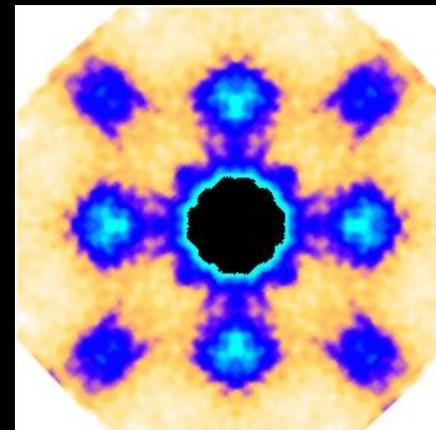
UD32K



OPT35K



OD15K

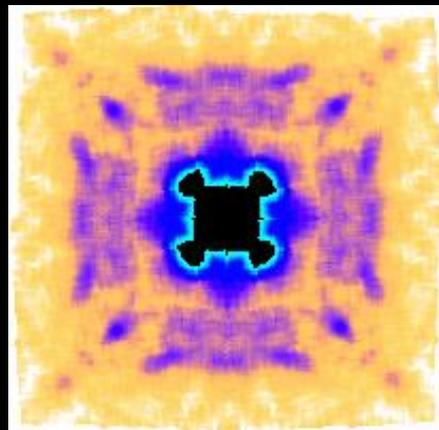


Ando, PRB 61, R14956 (2000)

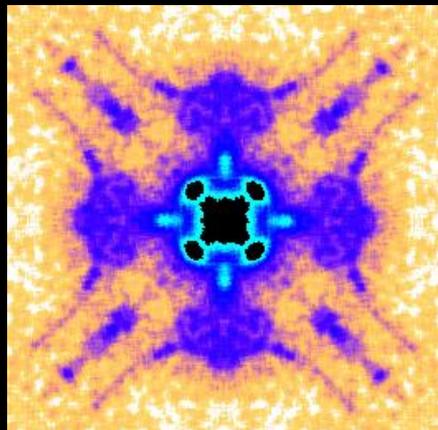
# Luttinger count



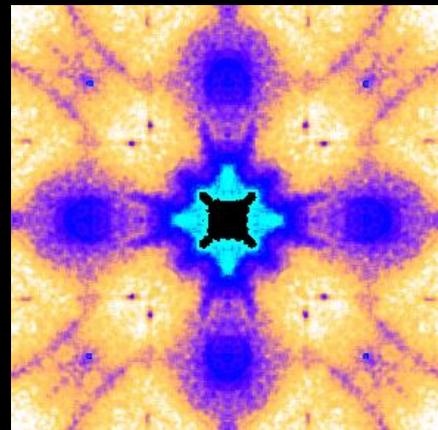
UD25K



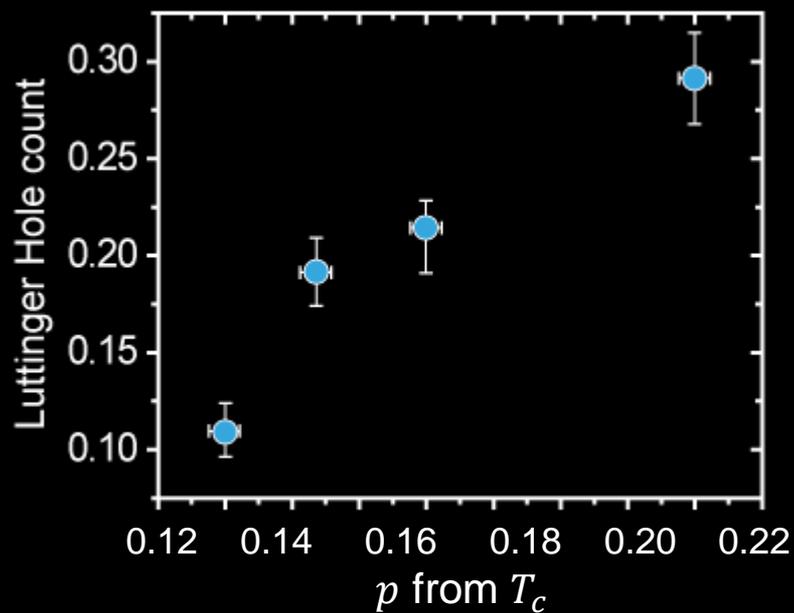
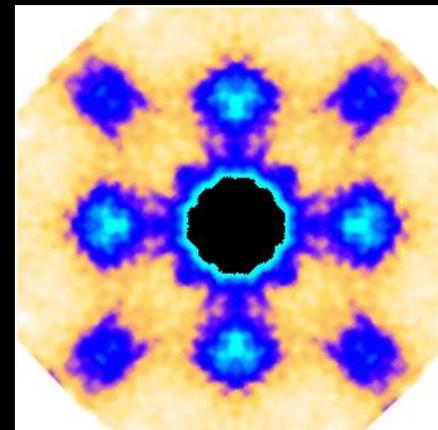
UD32K



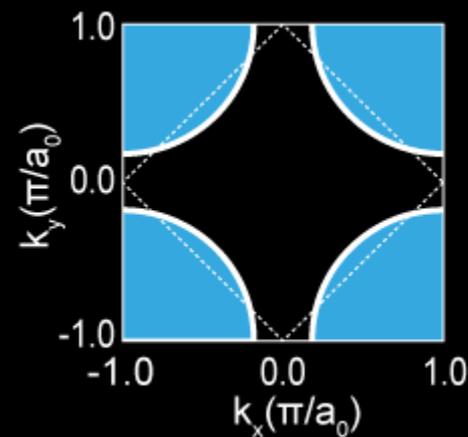
OPT35K



OD15K



Ando, PRB 61, R14956 (2000)

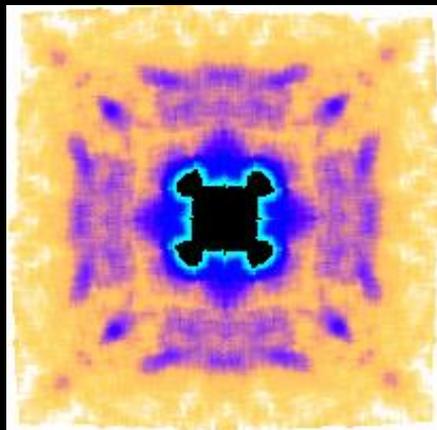


$$p_{\text{large}} = \frac{2A_{\text{blue}}}{A_{\text{BZ}}} - 1$$

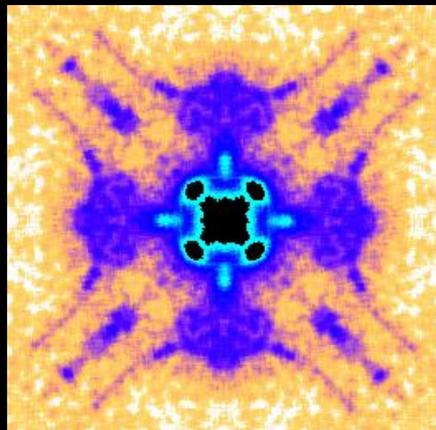
# Luttinger count



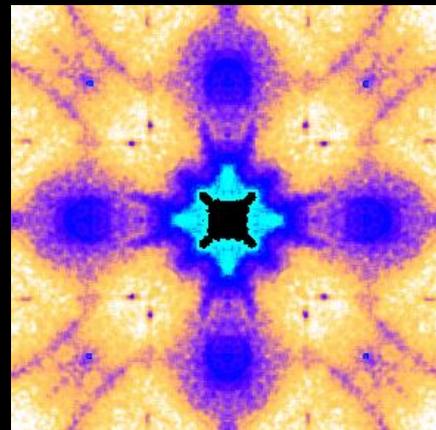
UD25K



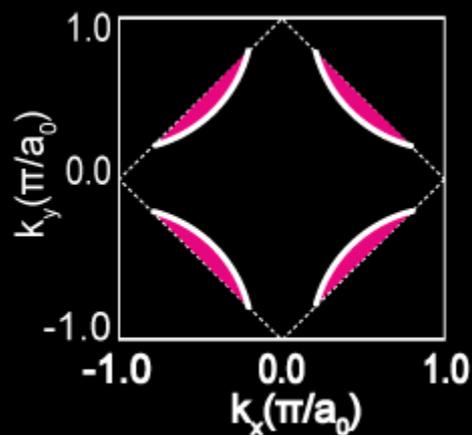
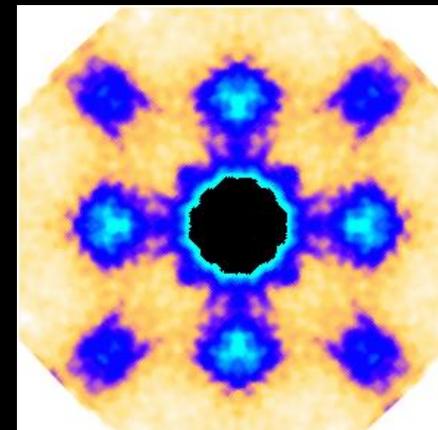
UD32K



OPT35K



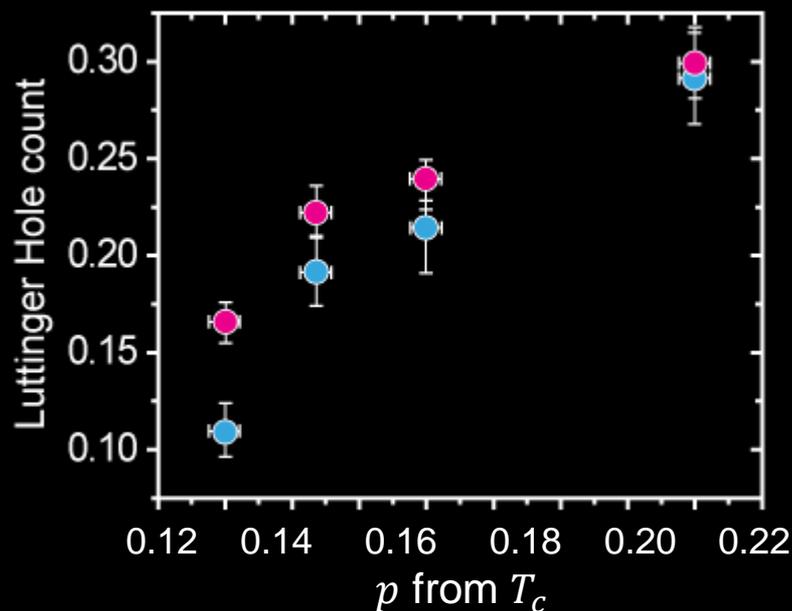
OD15K



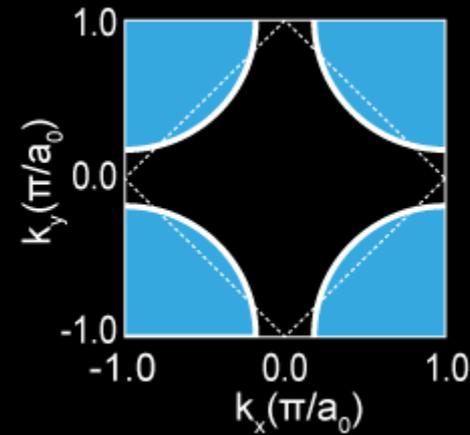
$$p_{\text{small}} = \frac{2A_{\text{pink}}}{A_{\text{BZ}}}$$

YRZ, PRB 73, 174501 (2006)

Qi + Sachdev, PRB 81, 115129 (2010)



Ando, PRB 61, R14956 (2000)

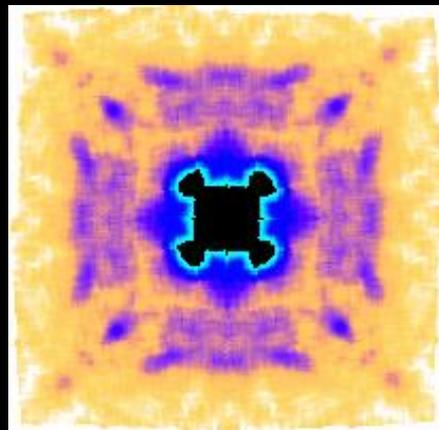


$$p_{\text{large}} = \frac{2A_{\text{blue}}}{A_{\text{BZ}}} - 1$$

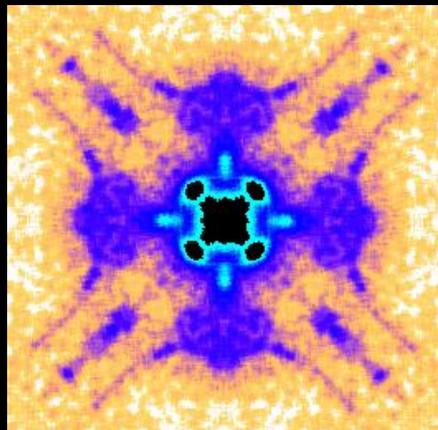
# Luttinger count



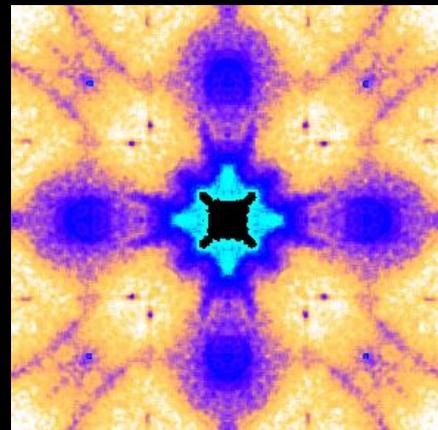
UD25K



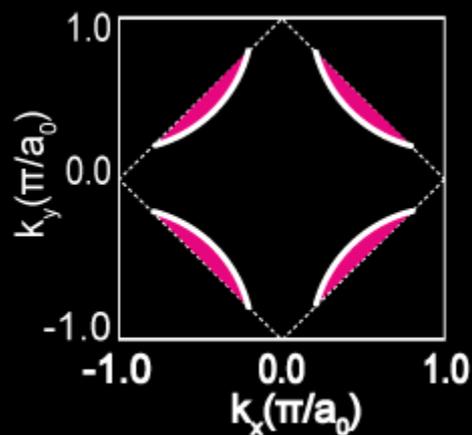
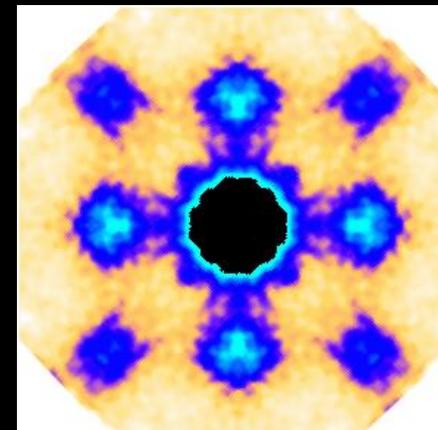
UD32K



OPT35K



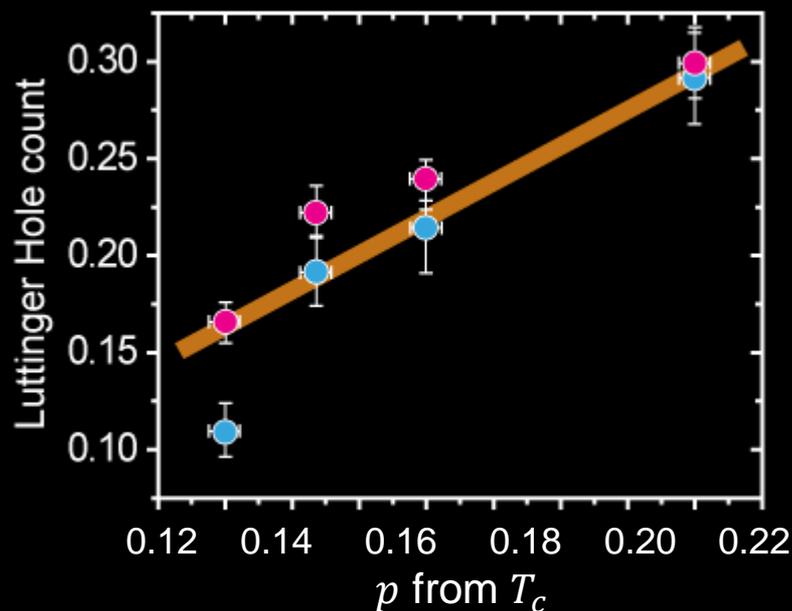
OD15K



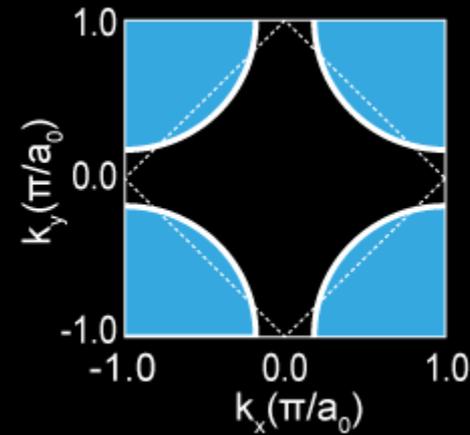
$$p_{\text{small}} = \frac{2A_{\text{pink}}}{A_{\text{BZ}}}$$

YRZ, PRB 73, 174501 (2006)

Qi + Sachdev, PRB 81, 115129 (2010)



Ando, PRB 61, R14956 (2000)

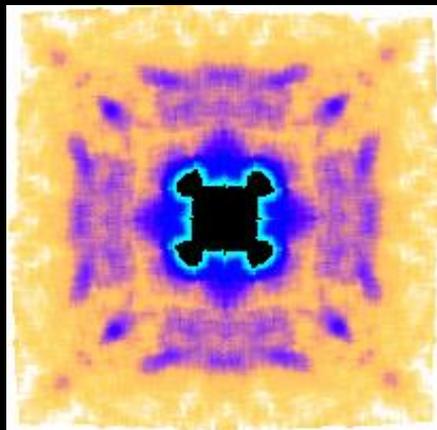


$$p_{\text{large}} = \frac{2A_{\text{blue}}}{A_{\text{BZ}}} - 1$$

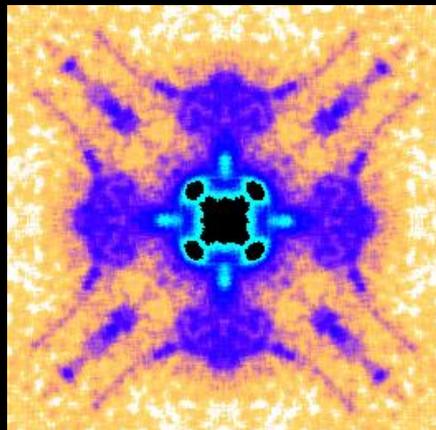
# Luttinger count



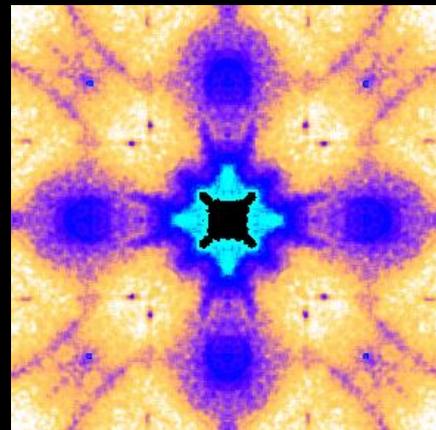
UD25K



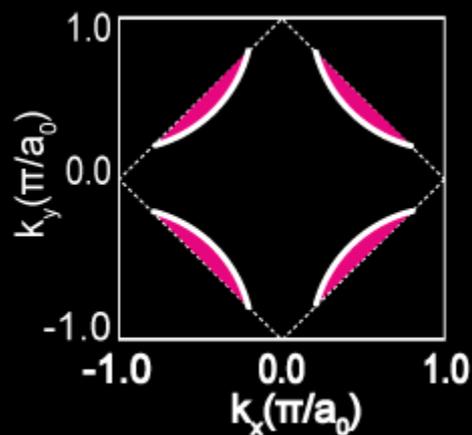
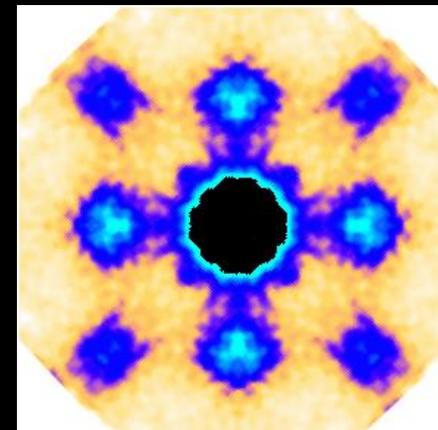
UD32K



OPT35K



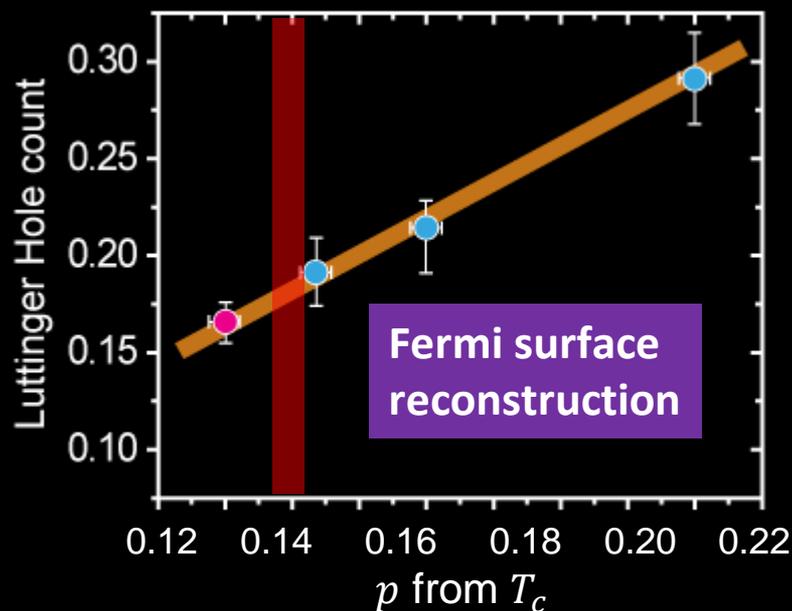
OD15K



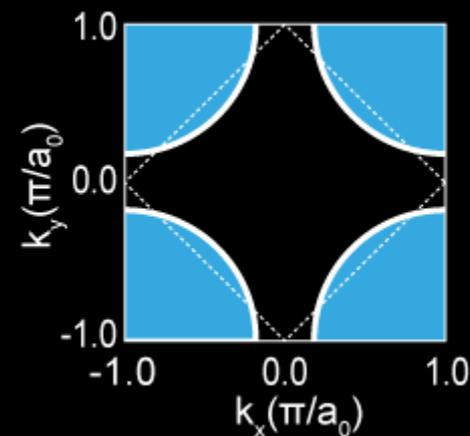
$$p_{\text{small}} = \frac{2A_{\text{pink}}}{A_{\text{BZ}}}$$

YRZ, PRB 73, 174501 (2006)

Qi + Sachdev, PRB 81, 115129 (2010)

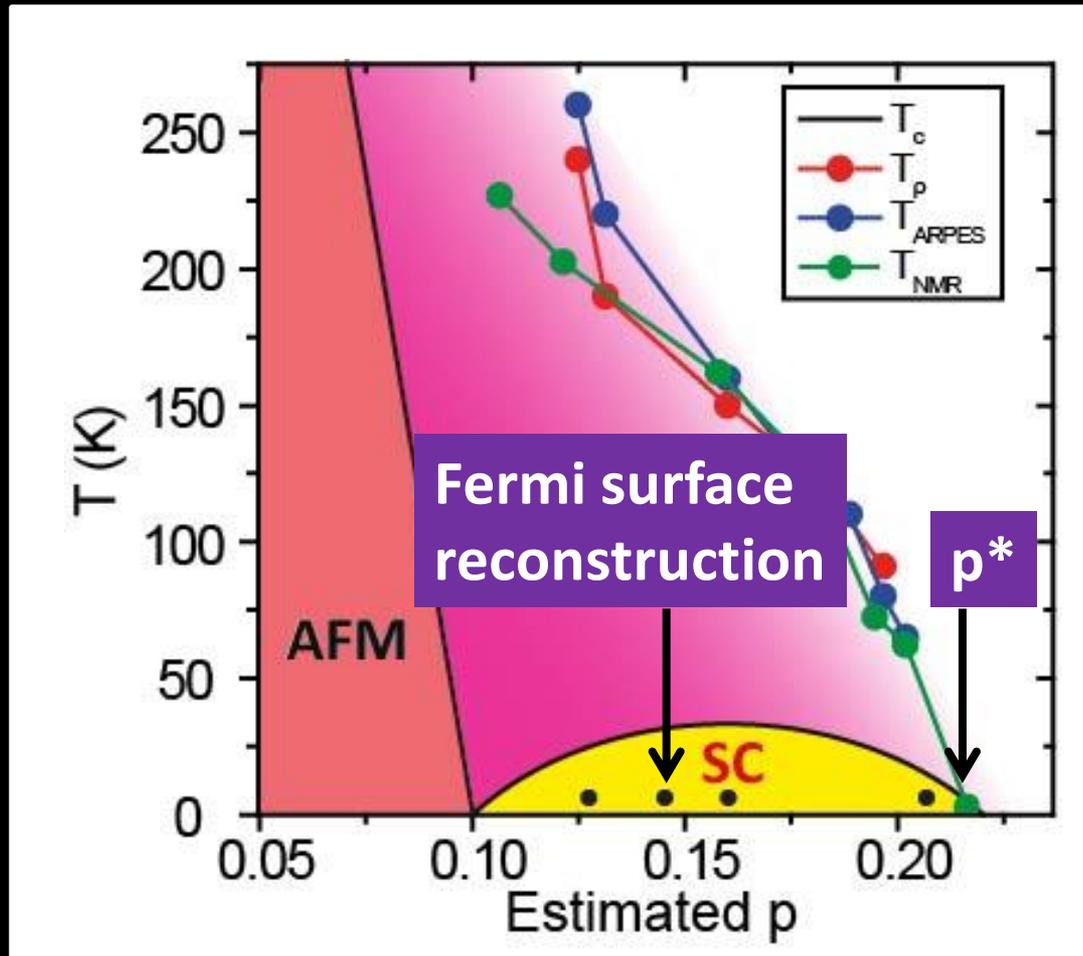


Ando, PRB 61, R14956 (2000)



$$p_{\text{large}} = \frac{2A_{\text{blue}}}{A_{\text{BZ}}} - 1$$

# FS reconstruction & pseudogap



In Bi2201,  $p^*$  does not coincide with Fermi surface reconstruction

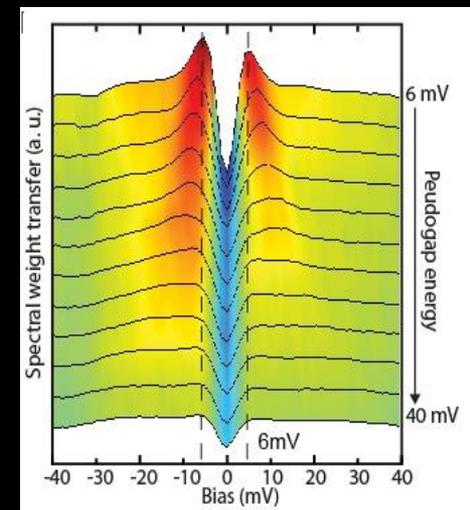
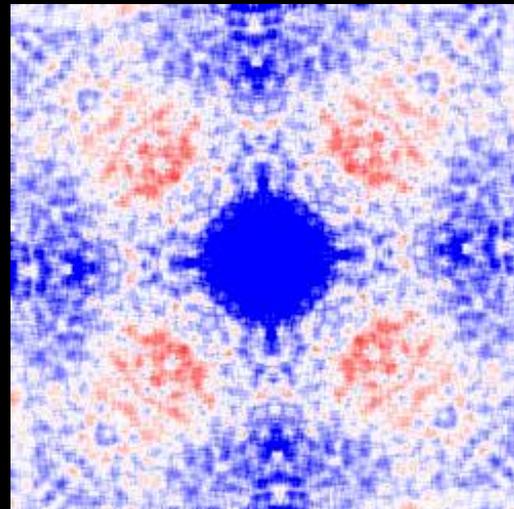
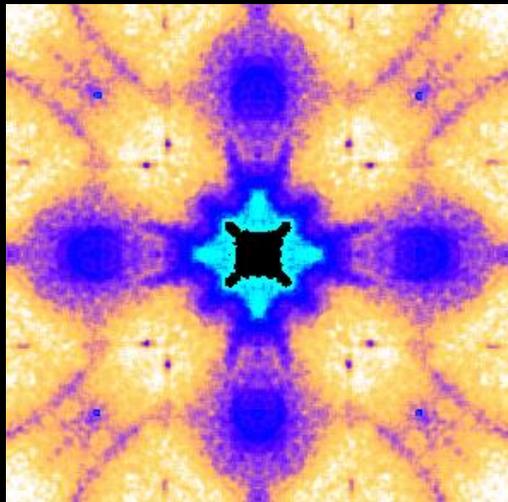
## 1. Where is the Fermi surface reconstruction?

Answer: coincides with QCP near optimal doping at  $B=0$

## 2. What is the role of the pseudogap?

Answer:

- separate occurrence
- coexists with superconductivity at the antinode
- causes decoherence at the nanoscale

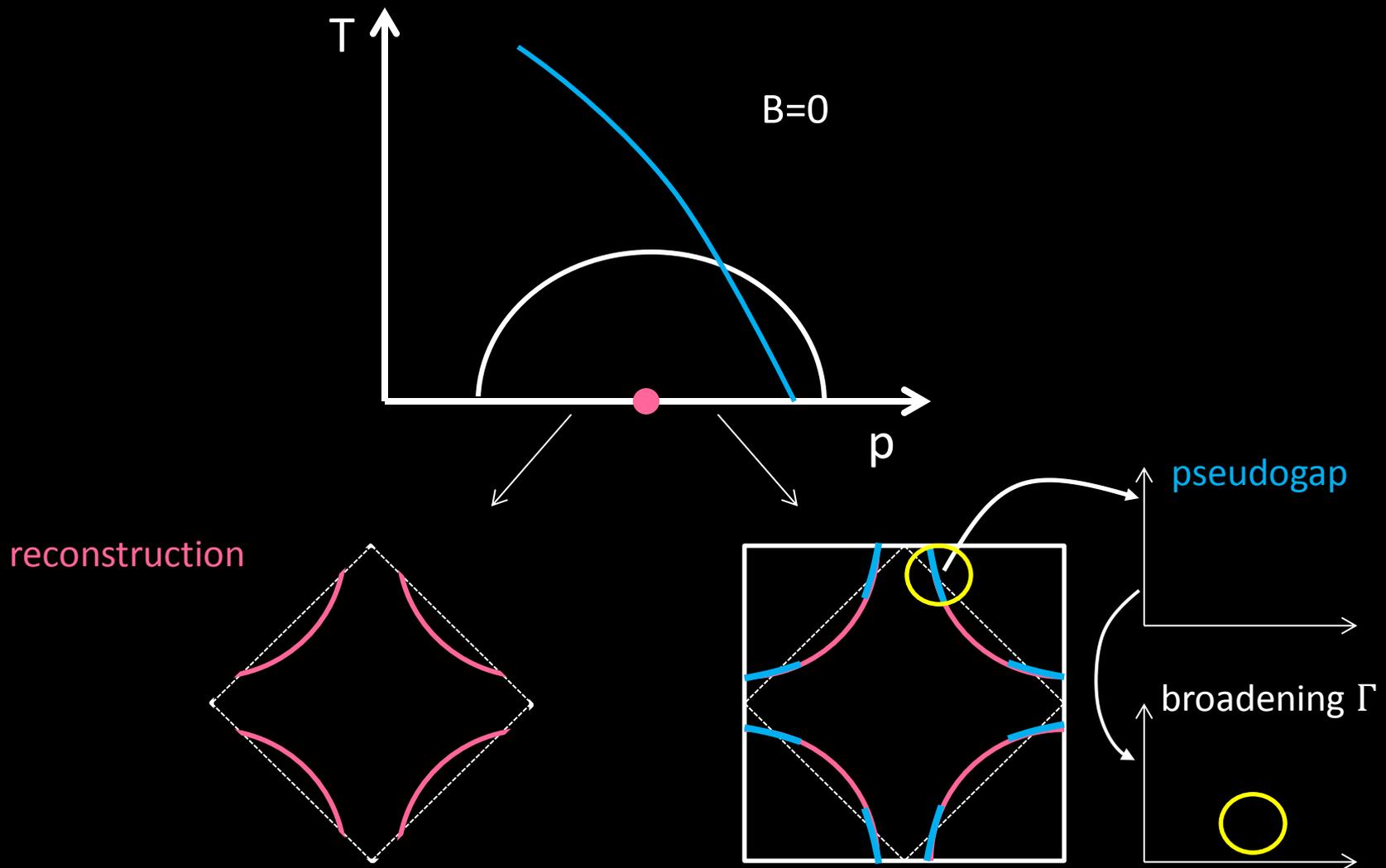


arxiv:1305.2778, He et al, *Science*, May 9 (2014)

# What about **superconductivity**?



## 1. Fermi surface reconstruction $\neq$ pseudogap

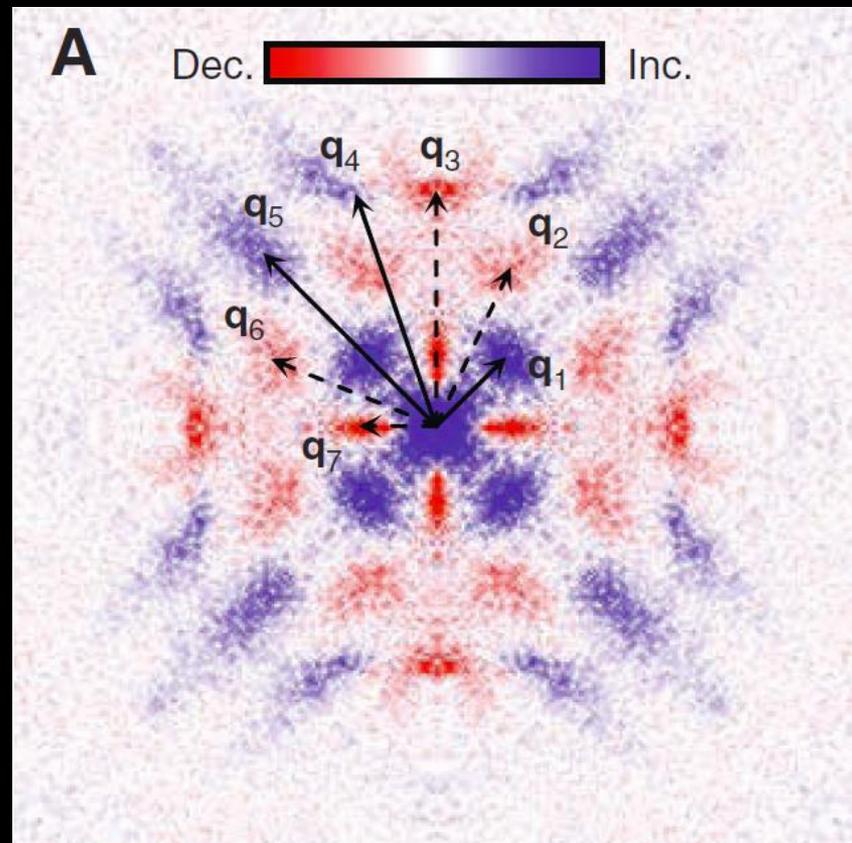
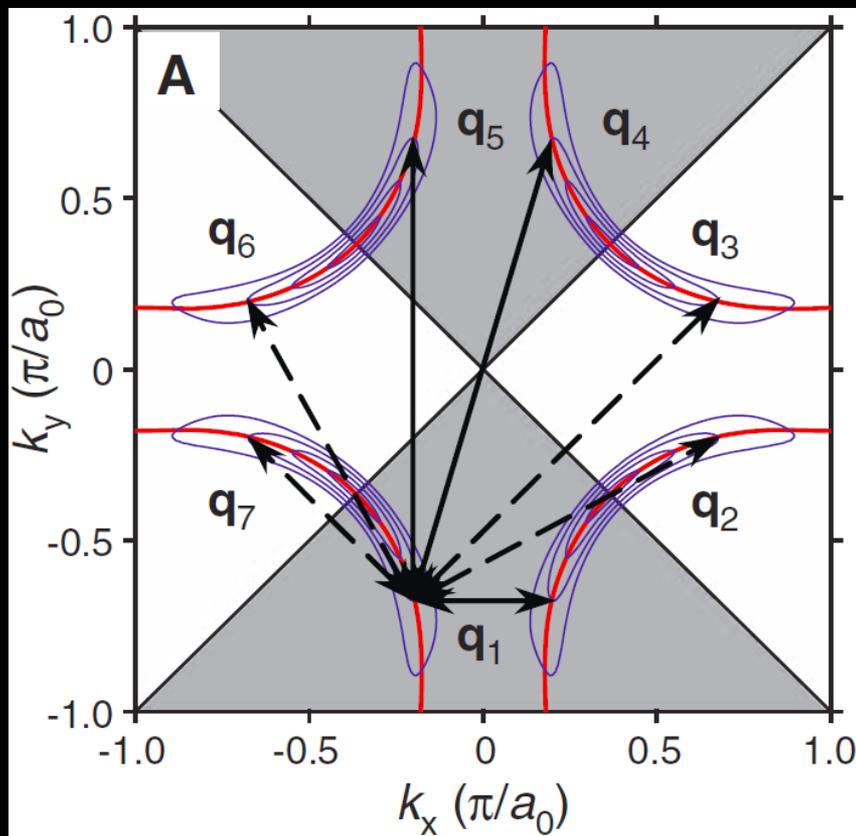


Can **superconductivity** live here too?

# $d$ -wave coherence factors in Bi2212

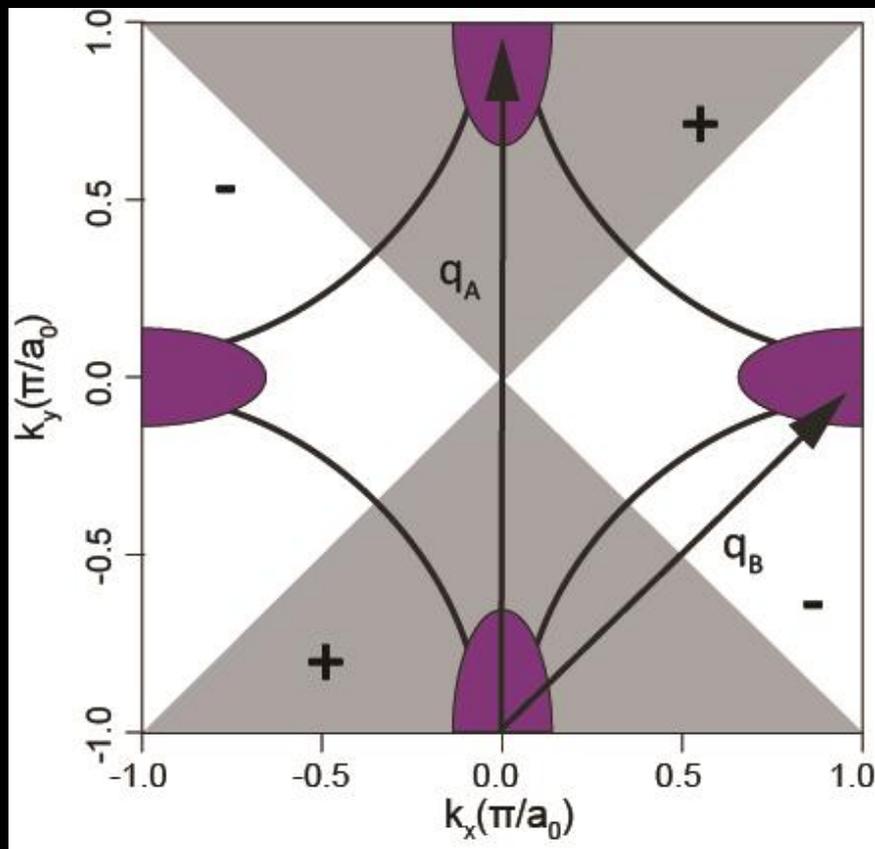


sign flipping  $\longrightarrow$  decreasing in field  
sign preserving  $\longrightarrow$  increasing in field

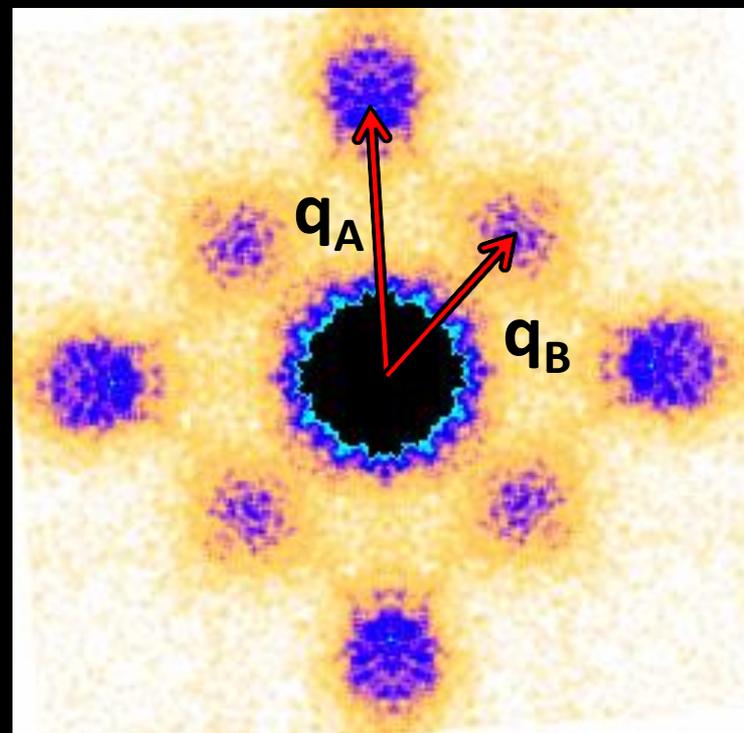


Hanaguri, et al, *Science* 323, 923 (2009)  
suggested by Tami Pereg-Barnea & Marcel Franz  
*PRB* 78, 020509 (2008)

# antinodal $d$ -wave coherence in Bi2201



OD15K 6mV, 0T

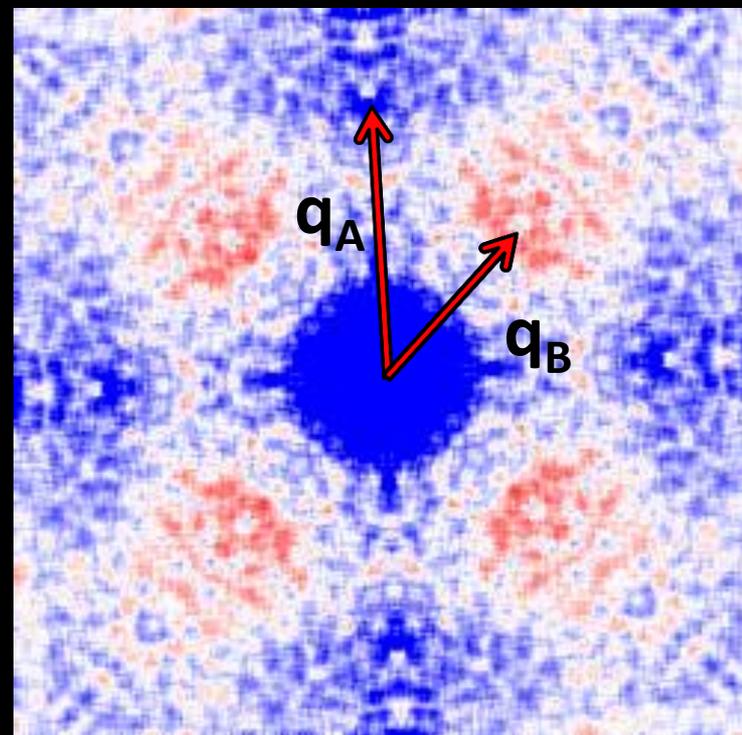
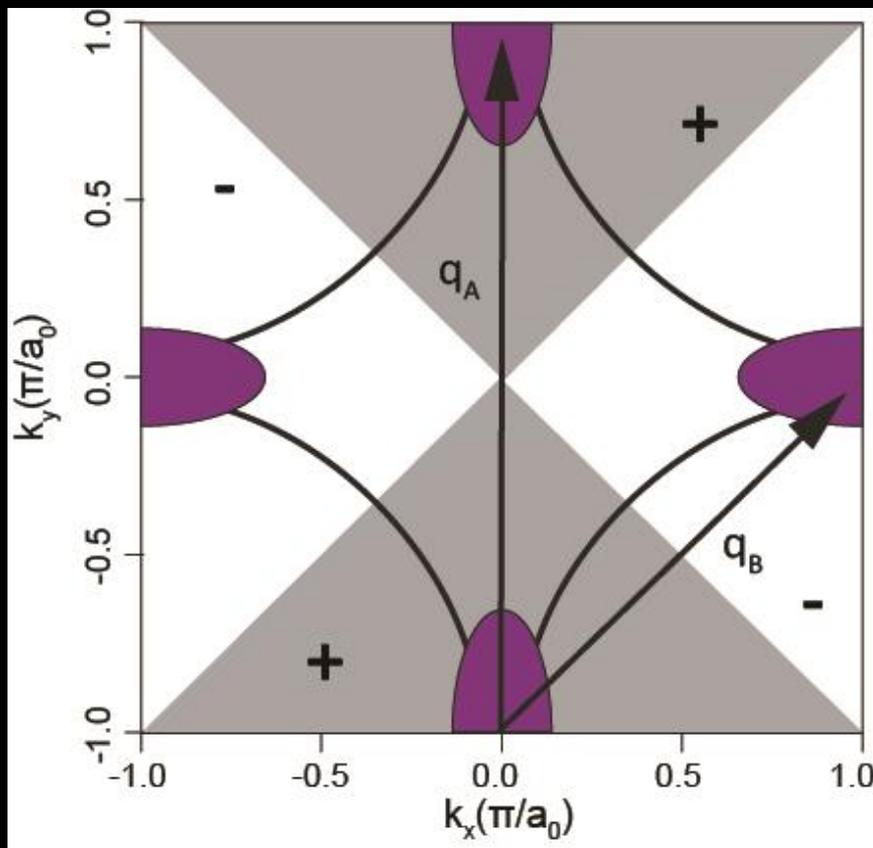


# antinodal $d$ -wave coherence in Bi2201



sign flipping  $\longrightarrow$  decreasing in field  
sign preserving  $\longrightarrow$  increasing in field

OD15K 6mV, 9T-0T



Decreasing  Increasing

Field dependence

$\longrightarrow$  Antinodal quasiparticles show  $d$ -wave coherence

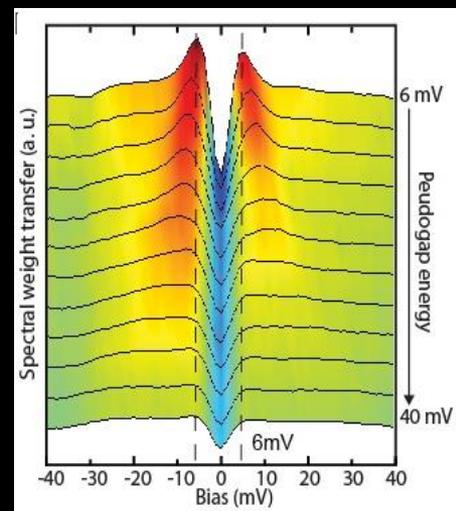
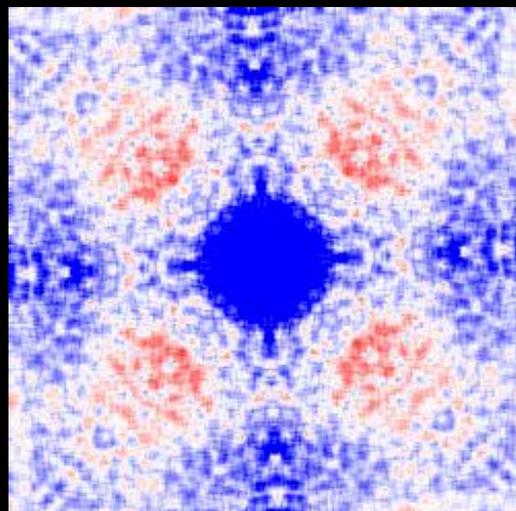
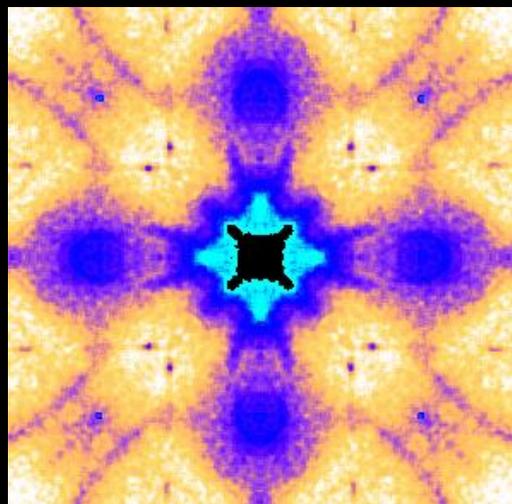
## 1. Where is the Fermi surface reconstruction?

Answer: coincides with QCP near optimal doping at  $B=0$

## 2. What is the role of the pseudogap?

Answer:

- separate occurrence
- coexists with superconductivity at the antinode
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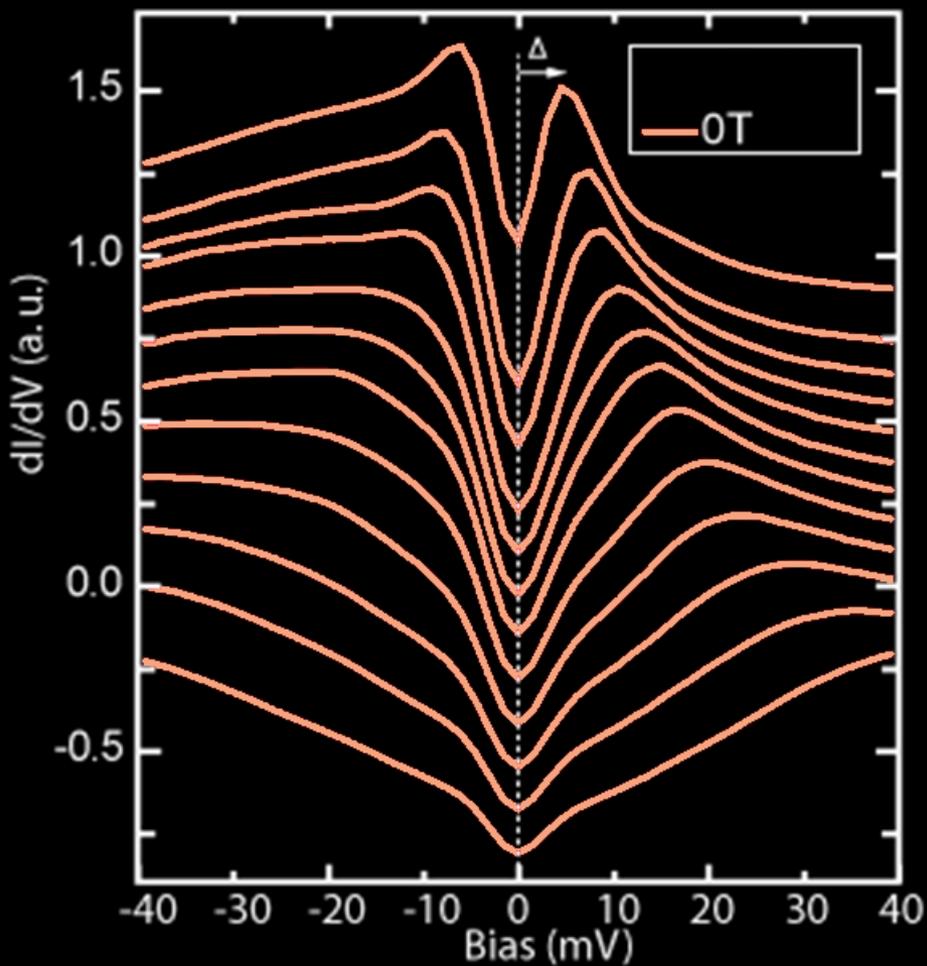
arxiv:1305.2778, to appear in *Science*, May 9 (2014)

# Two gap scenario: coexist spatially?

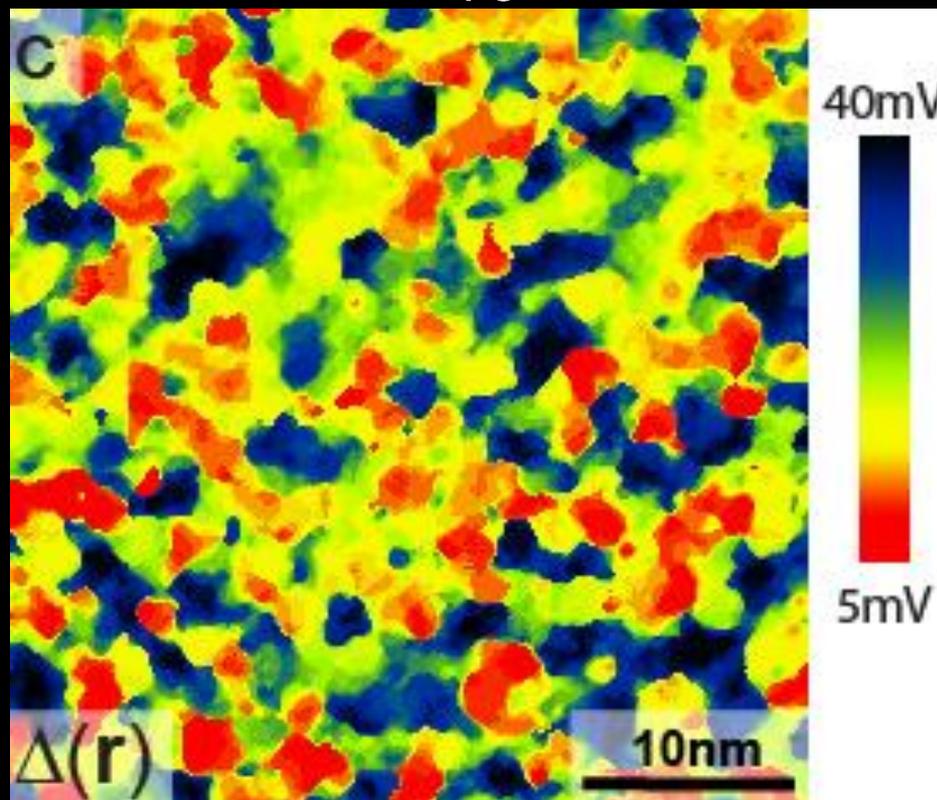
**superconductivity** vs. **pseudogap** at antinode?



OD15K



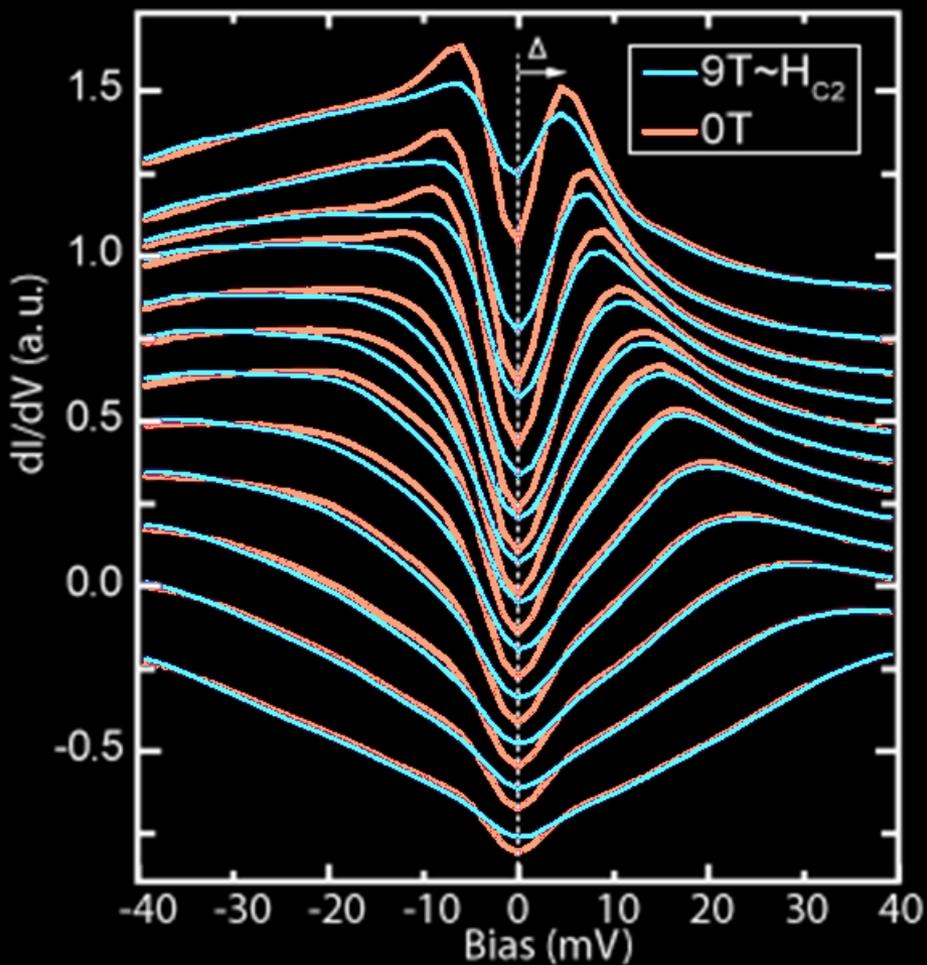
$\Delta_{PG}$



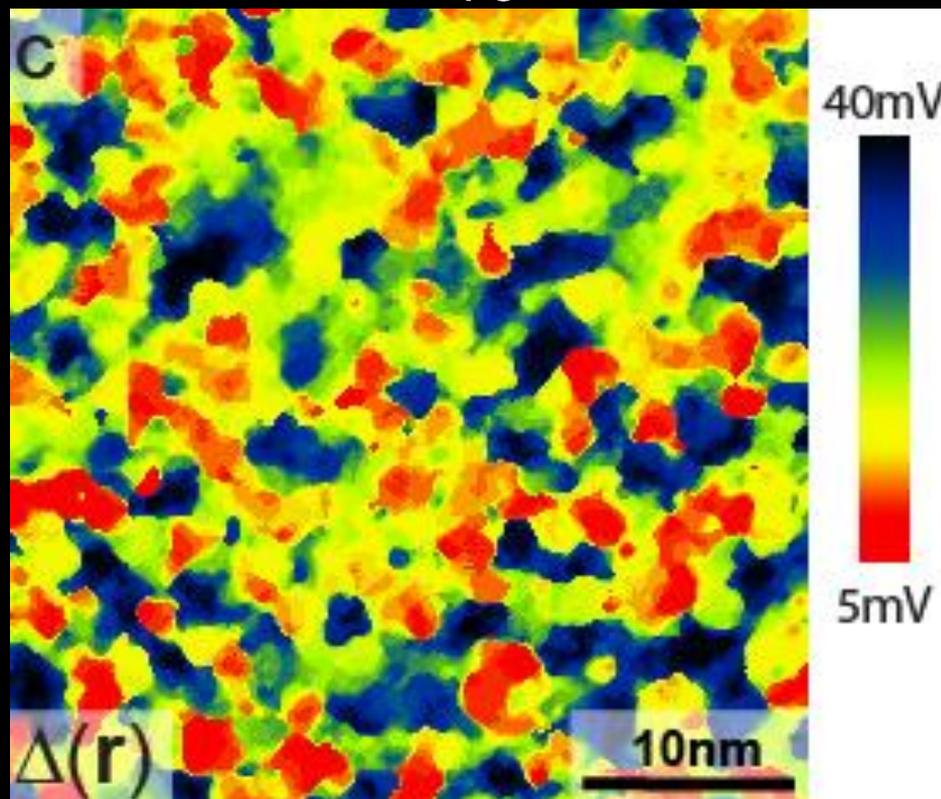
# Two gap scenario: coexist spatially?



OD15K



$\Delta_{PG}$



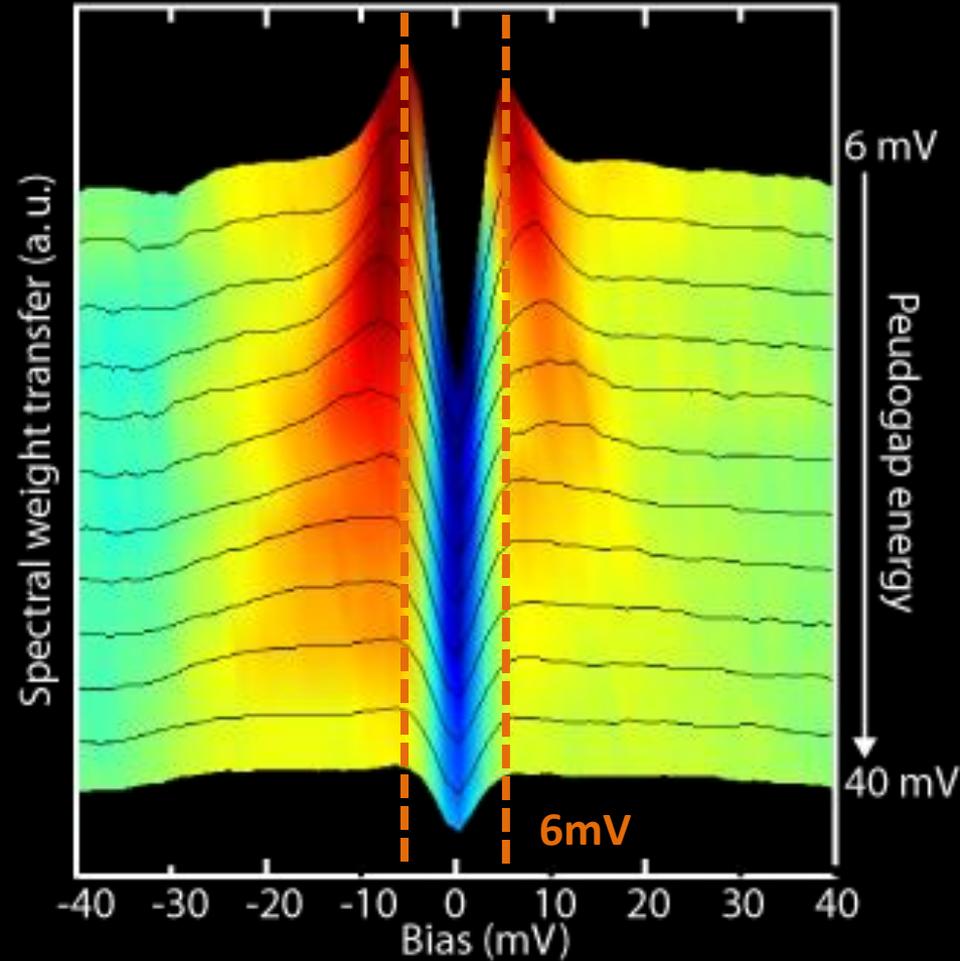
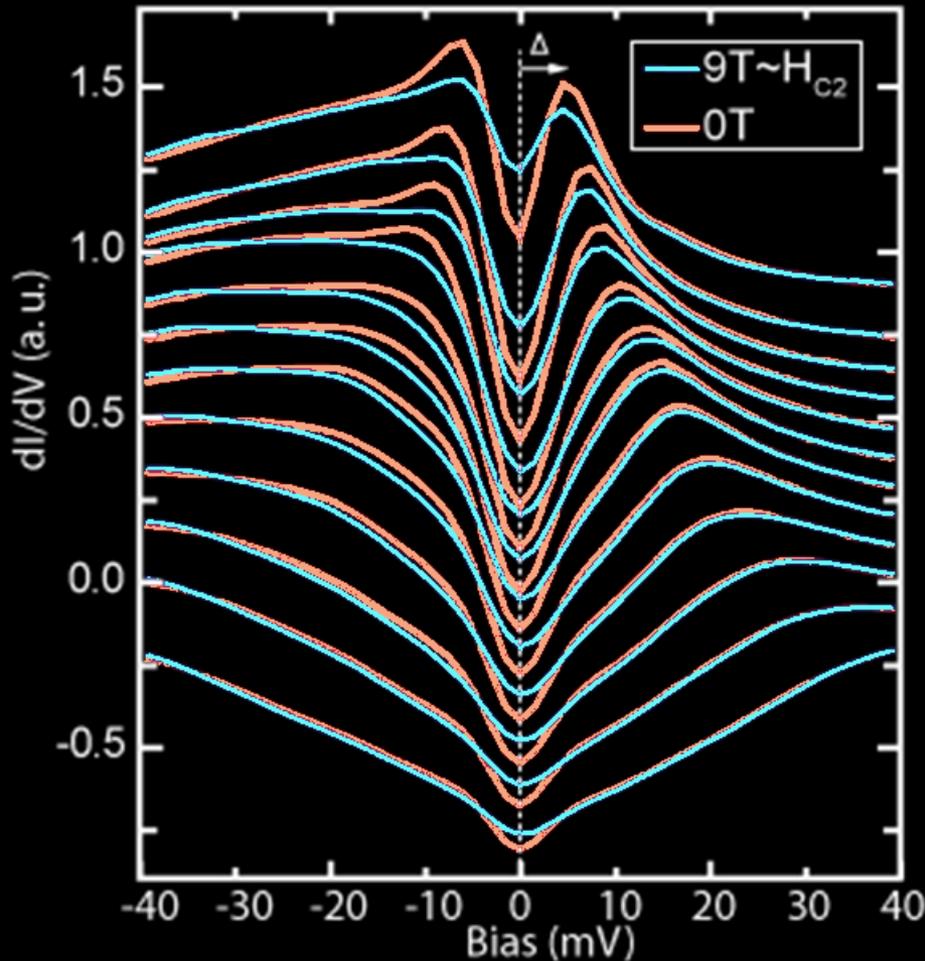
# Two gap scenario: coexist spatially?



Field-induced spectral weight transfer:

$$S(E) = g(E, 0T) - g(E, 9T)$$

OD15K



1. PG suppresses SC coherence.
2. PG does not affect SC order parameter amplitude.

# Conclusions



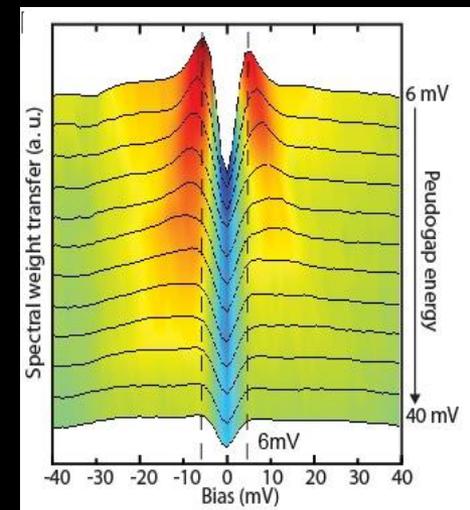
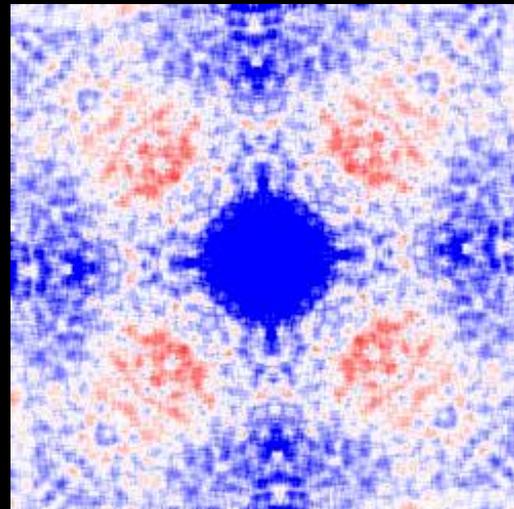
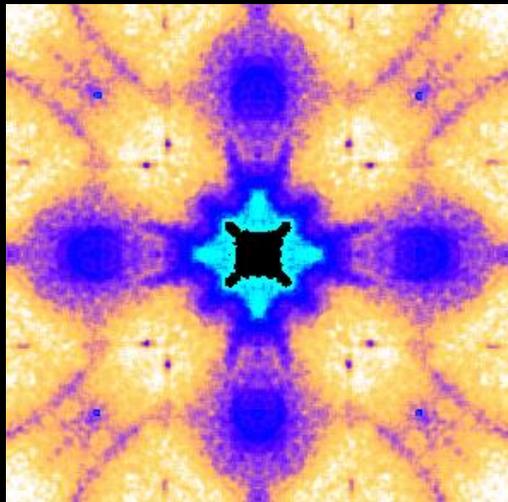
1. Where is the Fermi surface reconstruction?

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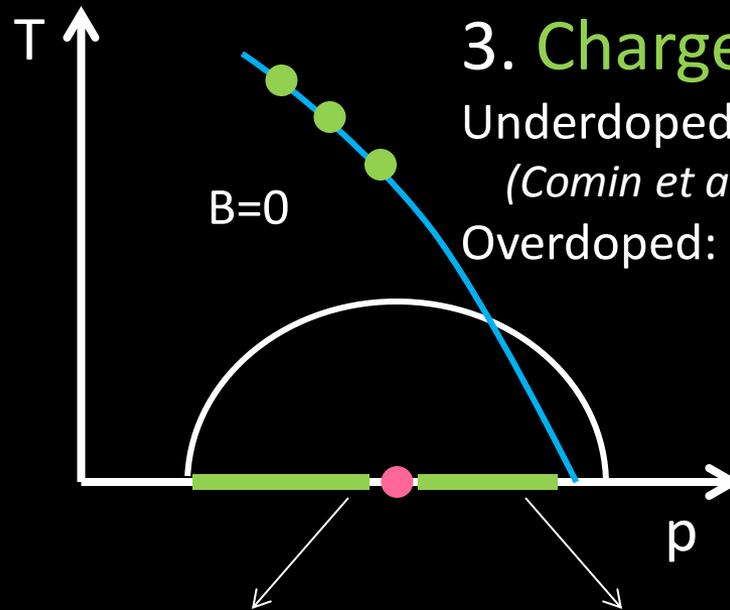


arxiv:1305.2778, to appear in *Science*, May 9 (2014)

# Conclusions (STM on Bi2201)



1. Fermi surface reconstruction  $\neq$  pseudogap

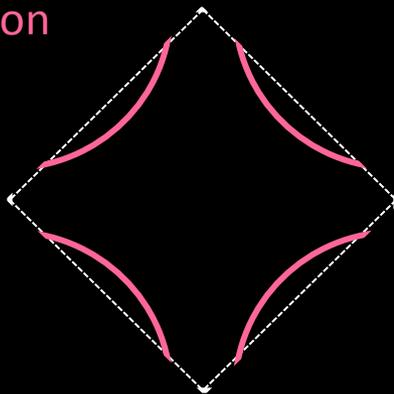


3. Charge order

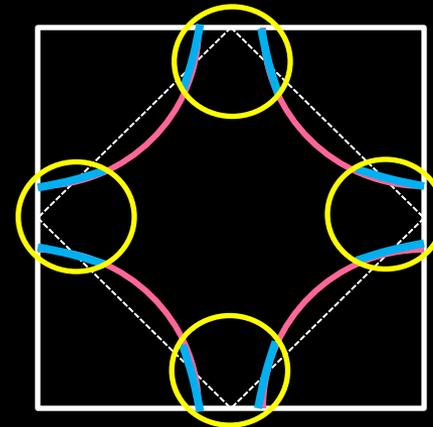
Underdoped: bulk-surface correspondence  
(Comin et al, Science 343, 390 2014)

Overdoped: visible on surface to  $p^*$

reconstruction



pseudogap

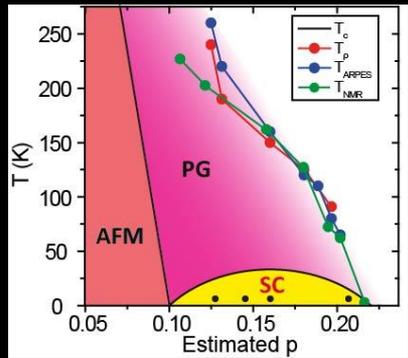


2. Superconductivity coexists with pseudogap at the antinode

# Forest of Phase Diagrams

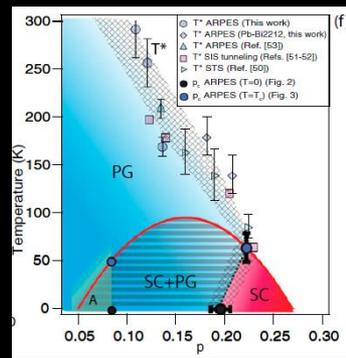


Bi2201



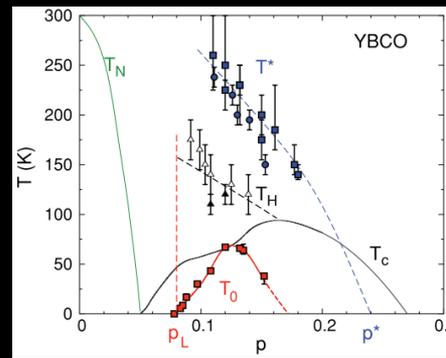
*This talk*

Bi2212



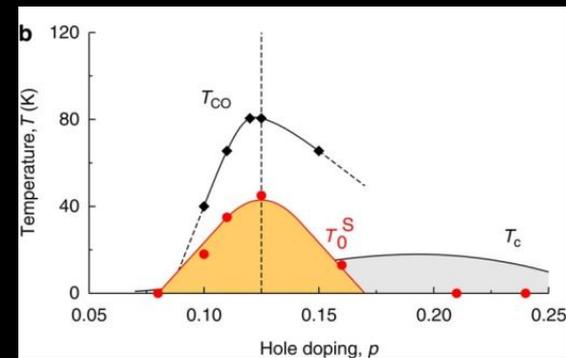
*Vishik, PNAS 2012*

YBCO

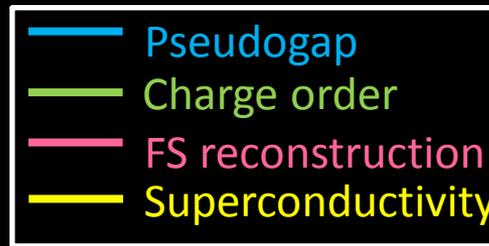


*LeBouef, PRB 2011*

Eu-LSCO



*Laliberte, Nature Comm 2012*

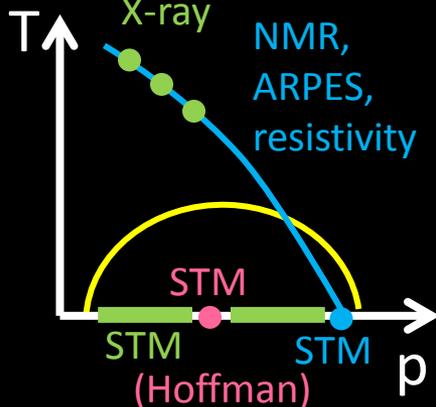


Bi2201

*Comin et al,*

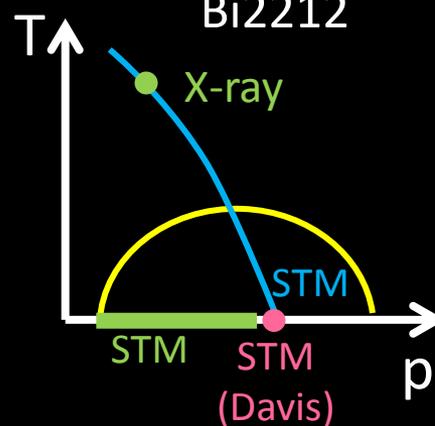
X-ray

NMR,  
ARPES,  
resistivity



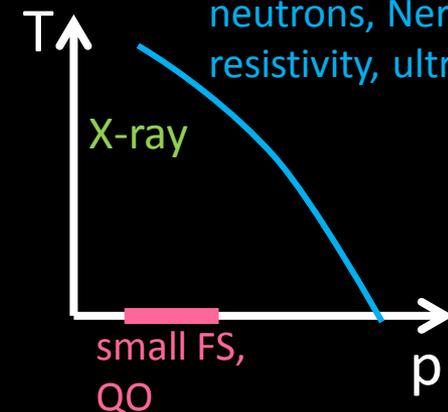
Bi2212

X-ray



YBCO & LSCO

neutrons, Nernst,  
resistivity, ultrasound



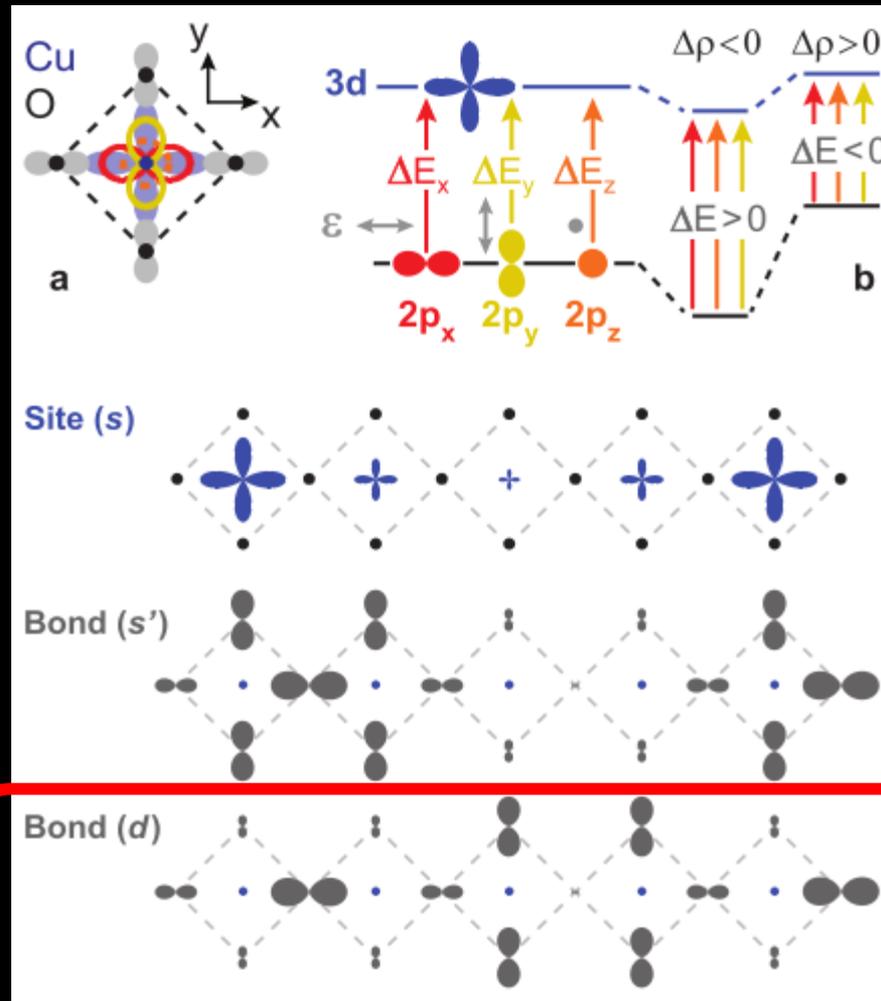
Why does Bi2212 have no fluctuating CDW regime?  
Is the  $T^*$  line in cuprates something else entirely?

# Charge Order Questions



1. What is the doping,  $T$ , and  $B$  dependence of charge order?  
strongest near  $p=1/8$ , and in applied  $B$
2. Is the charge order = pseudogap, or within PG?  
appears to be within the PG
3. Are we within the CDW phase or just disorder-pinned fluctuations?  
YBCO can be long-range-ordered; BSCCO is pinned fluctuations?
4. Does charge order compete with superconductivity?  
yes! (vortex cores, dip in dome, etc.)
5. What is the wavevector of charge order – where is it living on FS?  
varies continuously w/ doping; connects AFBZ hotspots
6. What is the energy dependence of charge order?  
hard to say... maybe strongest at  $+E$ , maybe strongest at  $\Delta_{PG}$
7. Is charge order responsible for small FS?  
Bi2212: claim is yes; Bi2201: CDW constant while FS evolves
8. Is it 1D or 2D? Does it have some internal form factor?  
local 1D patches? d-wave form factor

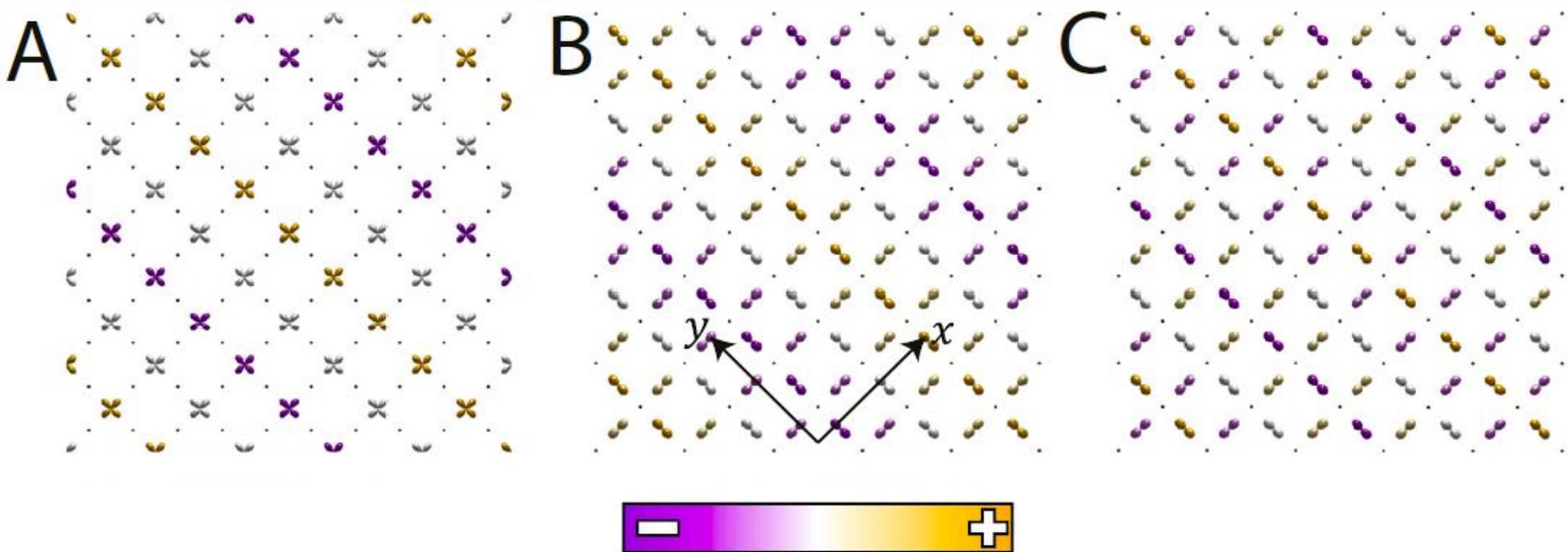
# d-wave form factor of CDW



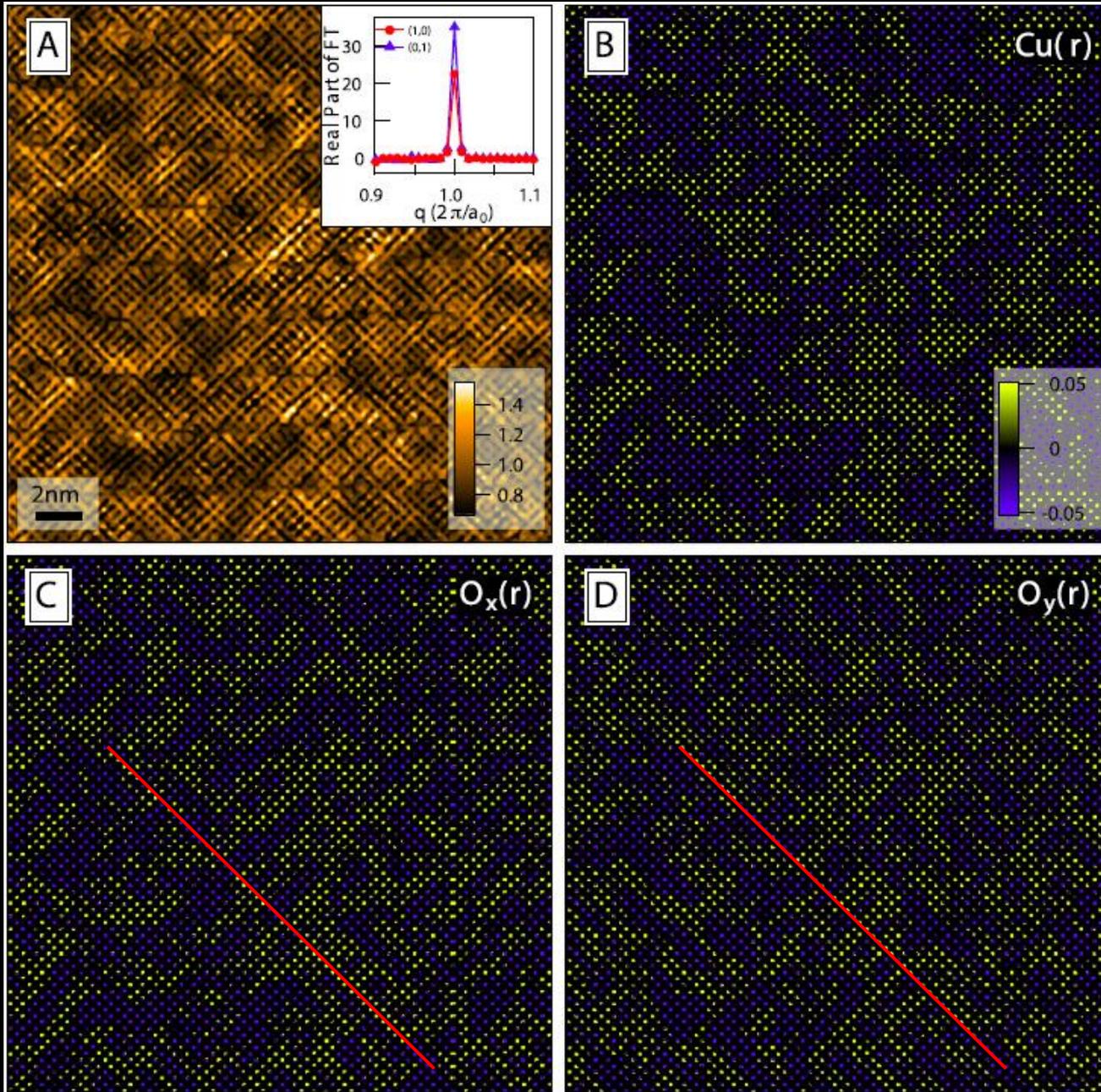
# d-wave form factor of CDW



3 possibilities (consider 1D case for simplicity)



# d-wave form factor of CDW



# Superconductivity Tunneling Milestones



1960: gap measurement (Pb)

1965: boson energies & coupling (Pb)

1985: charge density wave ( $\text{TaSe}_2$ )

1989: vortex lattice ( $\text{NbSe}_2$ )

1997: single atom impurities (Nb)

2002: quasiparticle interference

→ band structure & gap symmetry (BSCCO)

2009: phase-sensitive gap measurement (Na-CCOC)

2010: intra-unit-cell structure (BSCCO)

# 1965: tunneling measurements of phonons



VOLUME 14, NUMBER 4

PHYSICAL REVIEW LETTERS

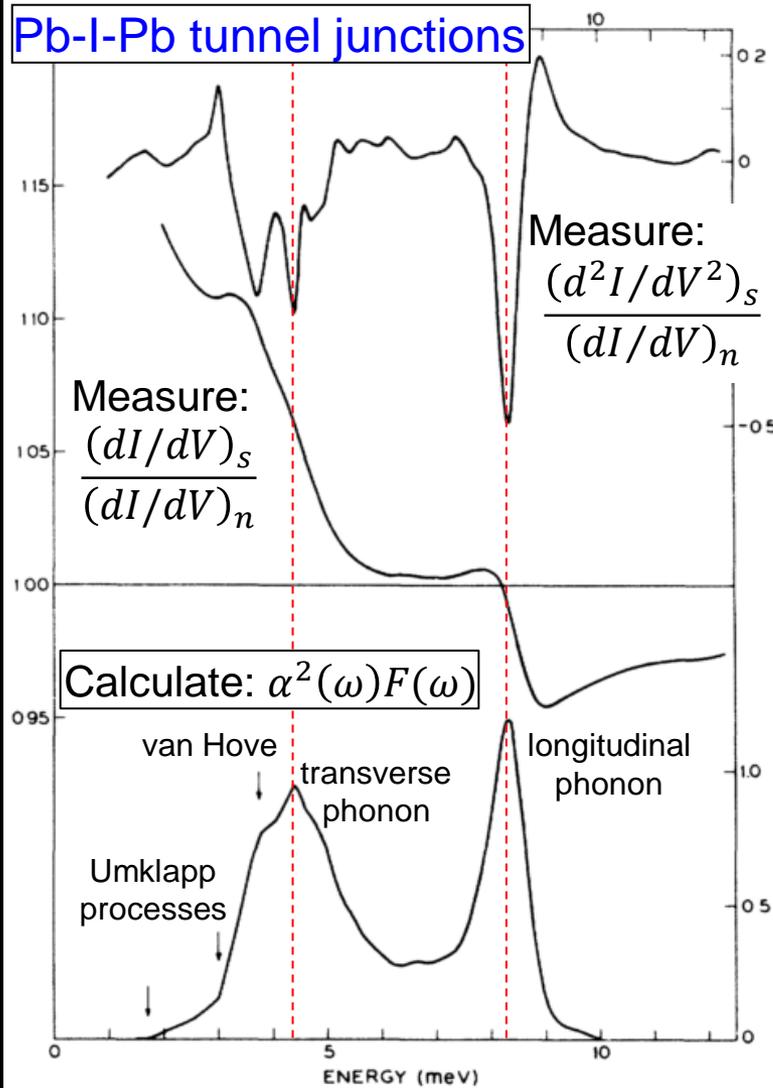
25 JANUARY 1965

## LEAD PHONON SPECTRUM CALCULATED FROM SUPERCONDUCTING DENSITY OF STATES

W. L. McMillan and J. M. Rowell

Bell Telephone Laboratories, Murray Hill, New Jersey

Pb-I-Pb tunnel junctions



$F(\omega)$  = phonon density of states  
 $\alpha^2(\omega)$  = coupling

# How to compute $\alpha^2(\omega)F(\omega)$



1. Measure  $N_s(\omega)$
2. Guess a functional form for  $\alpha^2(\omega)F(\omega)$  (recalling that they are both integrals over a full BZ)

$$F(\omega) = \sum_{\lambda} \int \frac{d^3q}{(2\pi)^3} \delta(\omega - \omega_{q\lambda})$$

$$\alpha^2(\omega)F(\omega) = \int_S d^2p \int_S' \frac{d^3p}{2\pi^2 v_F} \sum_{\lambda} g_{pp'\lambda} \times \delta(\omega - \omega_{p-p'\lambda}) / \int_S d^2p,$$

where  $g_{pp'\lambda}$  is the dressed electron-phonon coupling constant,  $\omega_{q\lambda}$  is the phonon energy for polarization  $\lambda$  and wave number  $q$  (reduced to the first zone), and  $v_F$  is the Fermi velocity. The two surface integrations are performed over the Fermi surface.

3. Plug in the guessed  $\alpha^2(\omega)F(\omega)$  to compute  $\Delta(\omega)$

$$\varphi(\omega) = \int_{\Delta_0}^{\omega_c} d\omega' \operatorname{Re} \left[ \frac{\Delta'}{(\omega'^2 - \Delta'^2)^{1/2}} \right] \times \left\{ \int d\omega_q \alpha^2(\omega_q) F(\omega_q) [D_q(\omega' + \omega) + D_q(\omega' - \omega)] - U_c \right\},$$

where  $D_q(\omega) = (\omega + \omega_q - i0^+)^{-1}$ ,  $\Delta(\omega) = \varphi(\omega)/Z(\omega)$

4. Plug in the computed  $\Delta(\omega)$  to compute  $N_s(\omega)$  and compare back to measured  $N_s(\omega)$

$$\frac{N_s(\omega)}{N(0)} = \operatorname{Re} \left\{ \frac{|\omega|}{[\omega^2 - \Delta^2(\omega)]^{1/2}} \right\}$$

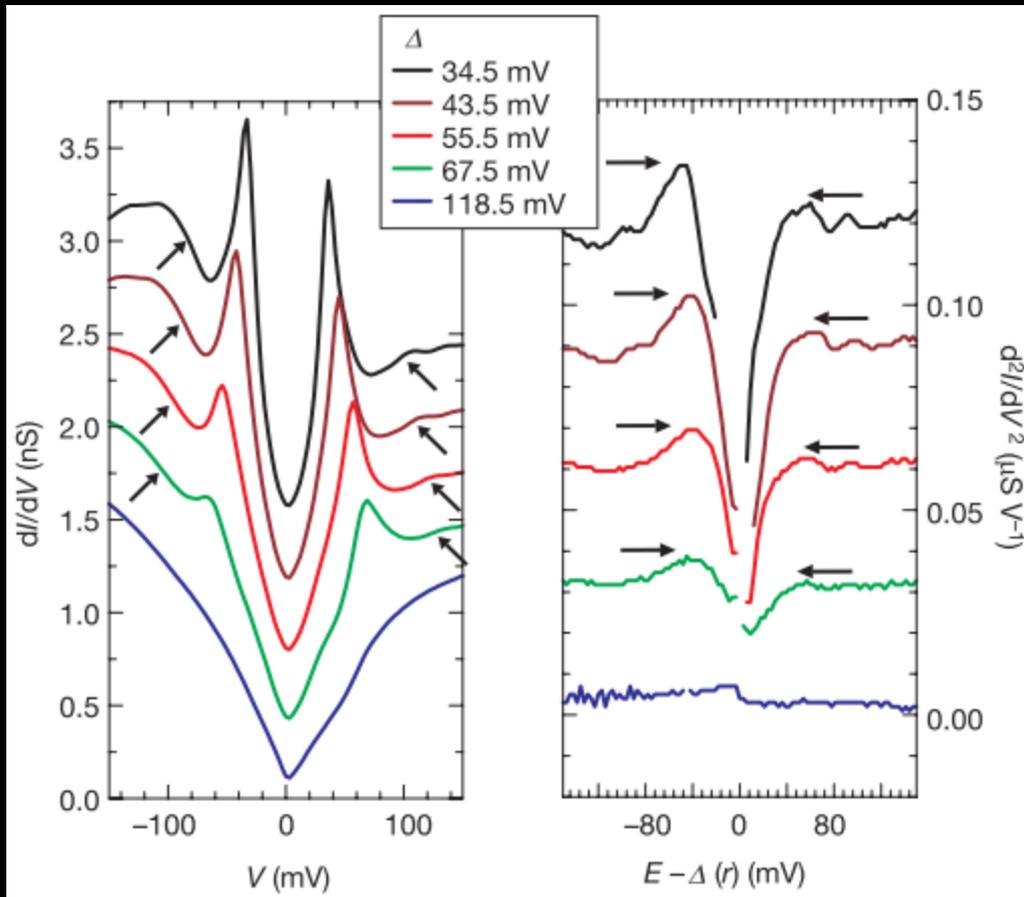
5. Compute the error and iterate

$$\delta[\alpha^2(\omega)] = \int d\omega' \left\{ \frac{\delta N(\omega')}{\delta[\alpha^2(\omega)F(\omega)]} \right\}^{-1} \times [N_s^{\text{expt}}(\omega') - N_s^{\text{calc}}(\omega')]$$

# Electron-boson coupling in cuprates

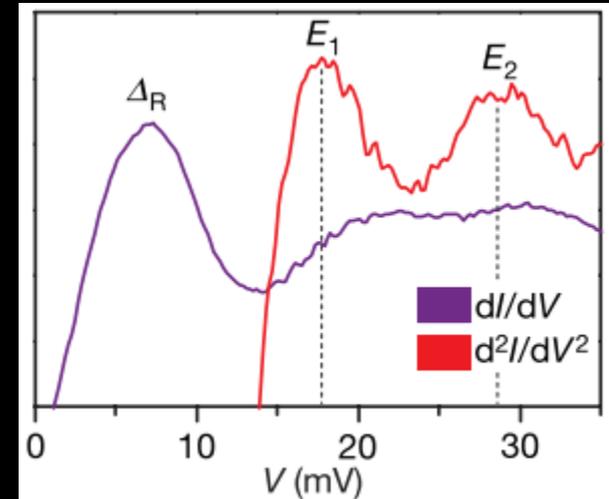


$\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+d}$  ( $T_c^{\text{max}} = 91\text{K}$ )



Lee, Nature 442, 546 (2006)

$\text{Pr}_{0.88}\text{LaCe}_{0.12}\text{CuO}_4$  ( $T_c = 24\text{K}$ )



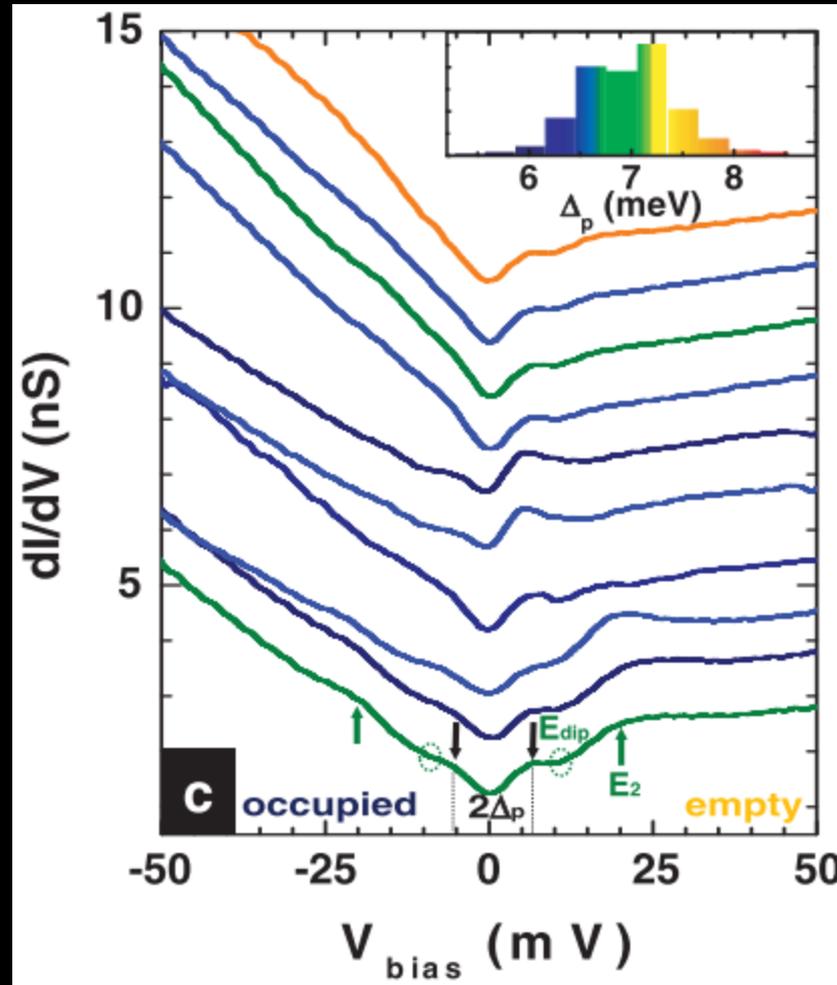
Niستمski, Nature 450, 1058 (2007)

$$\Omega = E \text{ (peak in } d^2I/dV^2) - \Delta$$

# 1111 Fe-superconductors



$\text{SmFeAsO}_{0.8}\text{F}_{0.2}$  ( $T_c=45\text{K}$ )



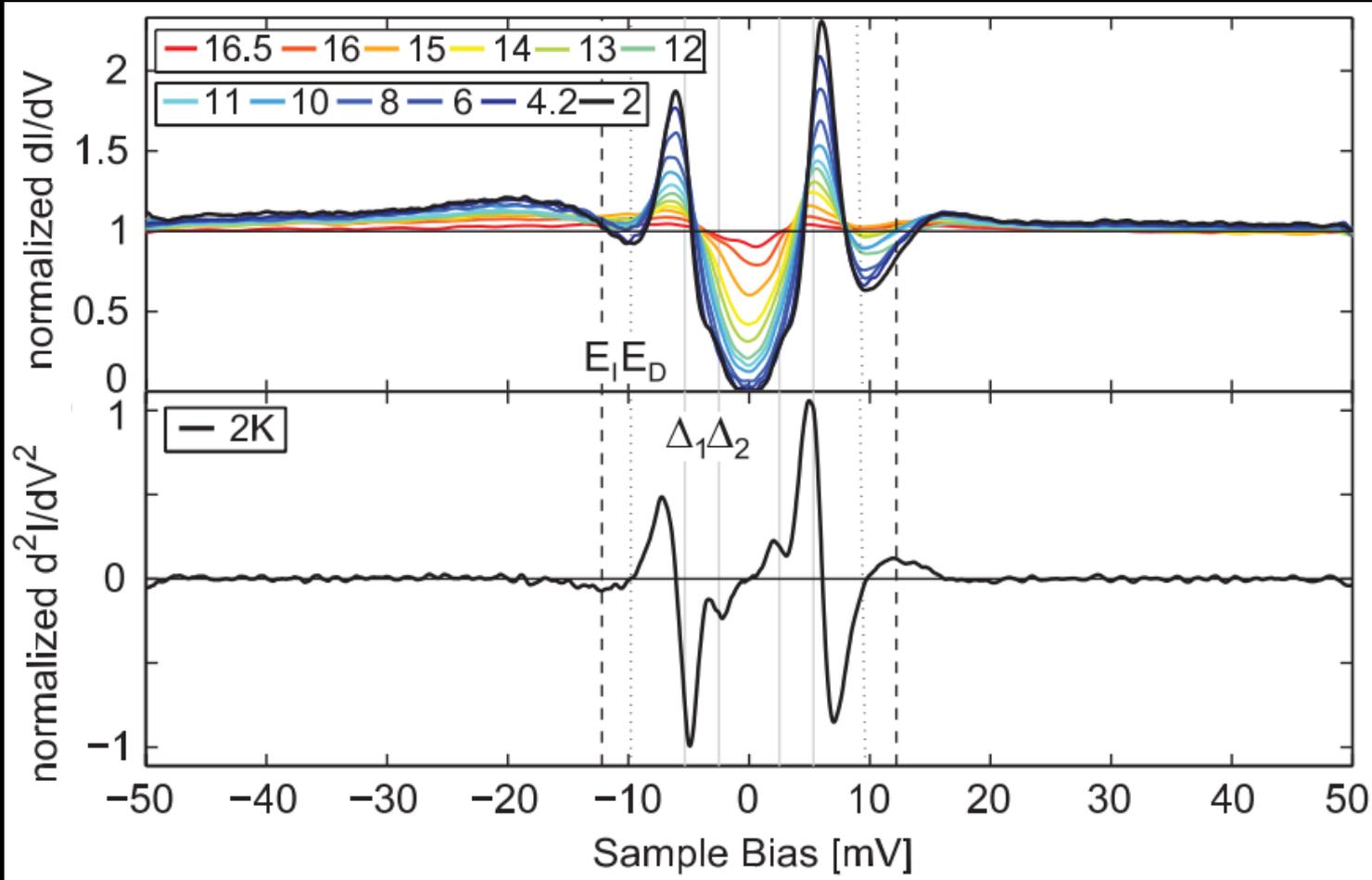
Fasano, PRL 105, 167005 (2010)

$$\Omega = E (\text{dip in } dI/dV) - \Delta$$

# 111 Fe-superconductors



LiFeAs ( $T_c=17\text{K}$ )



Chi, PRL 109, 087002 (2011)

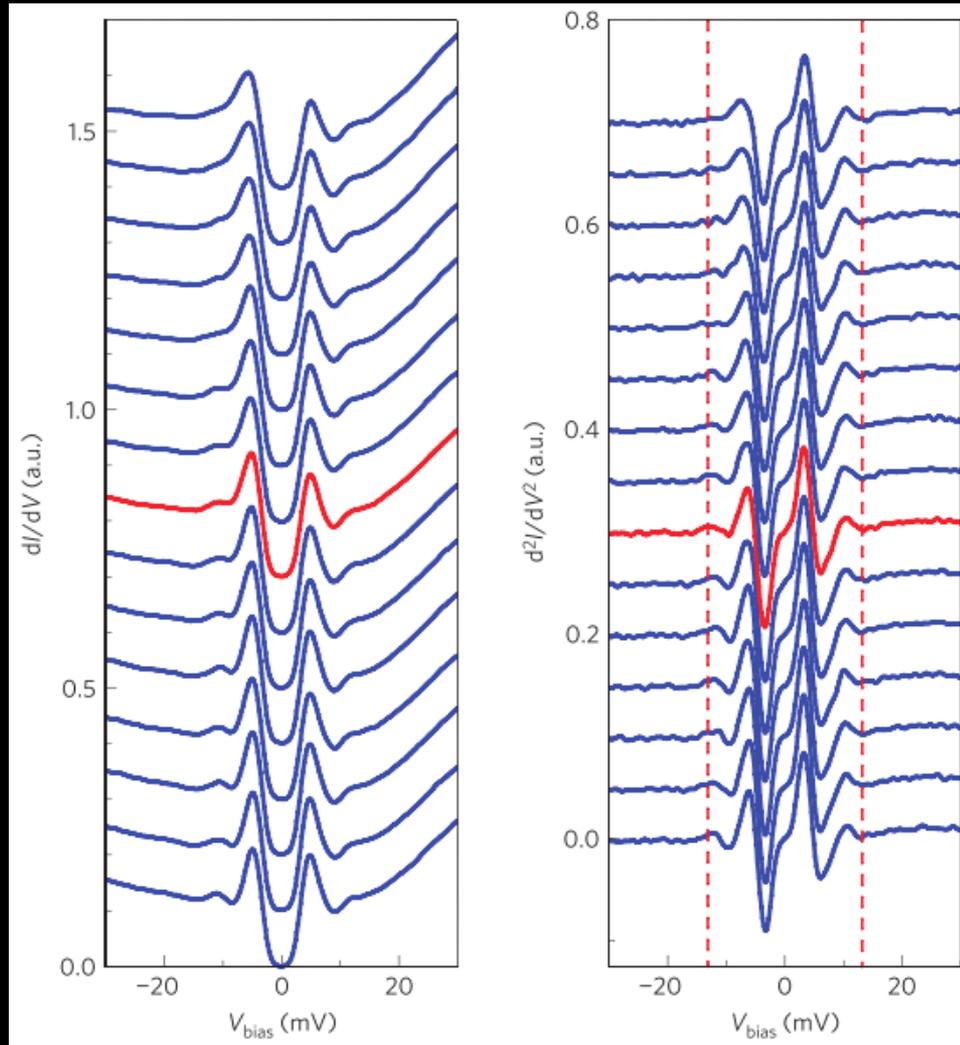
$$\Omega = E \text{ (dip in } dI/dV) - \Delta$$

# 111 Fe-superconductors



$\text{Na}(\text{Fe}_{0.975}\text{Co}_{0.025})\text{As}$  ( $T_C=21$  K)

$E$  (hump in  $dI/dV$ )  
 $= 13.3 \pm 0.8$



$E$  (dip in  $d^2I/dV^2$ )  
 $= 13.3 \pm 0.8$  (main text)  
 $= 13.5$  (figure caption)

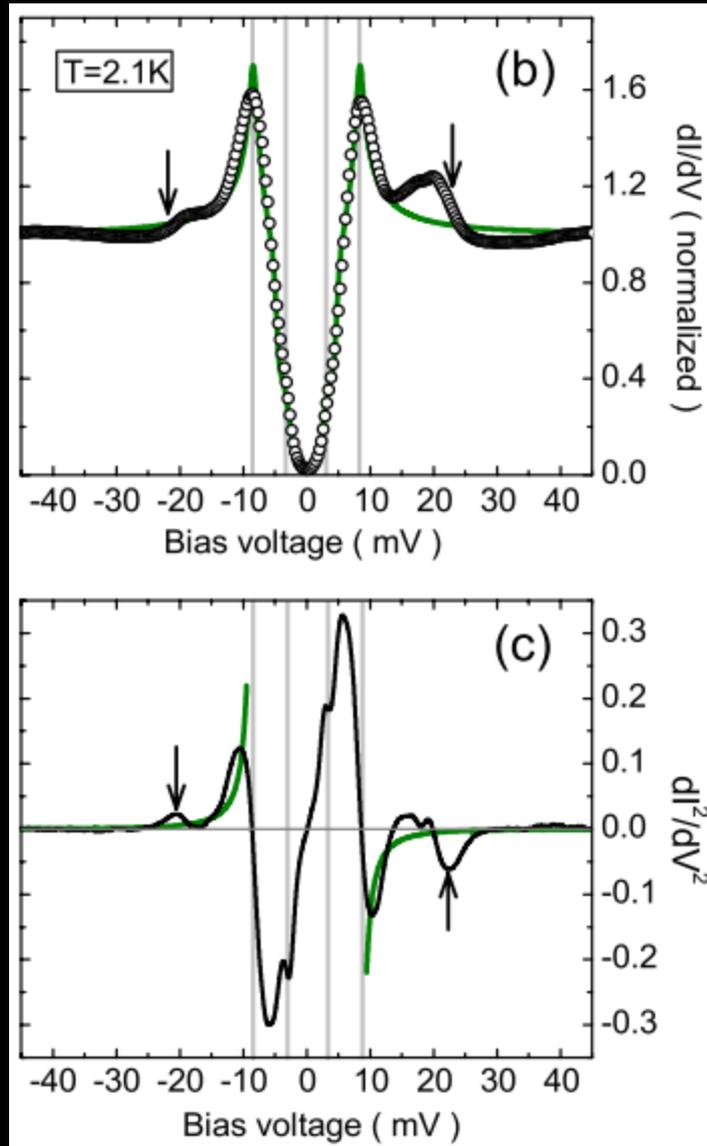
Shan, Nat Phys 9, 42 (2012)

$$\Omega = E \text{ (dip in } d^2I/dV^2) - \Delta \quad ???$$

# 122 Fe-superconductors



$\text{Ba}_{0.6}\text{K}_{0.4}\text{Fe}_2\text{As}_2$  ( $T_c=38\text{K}$ )



$$\Omega = E \text{ (dip in } d^2I/dV^2) - \Delta$$

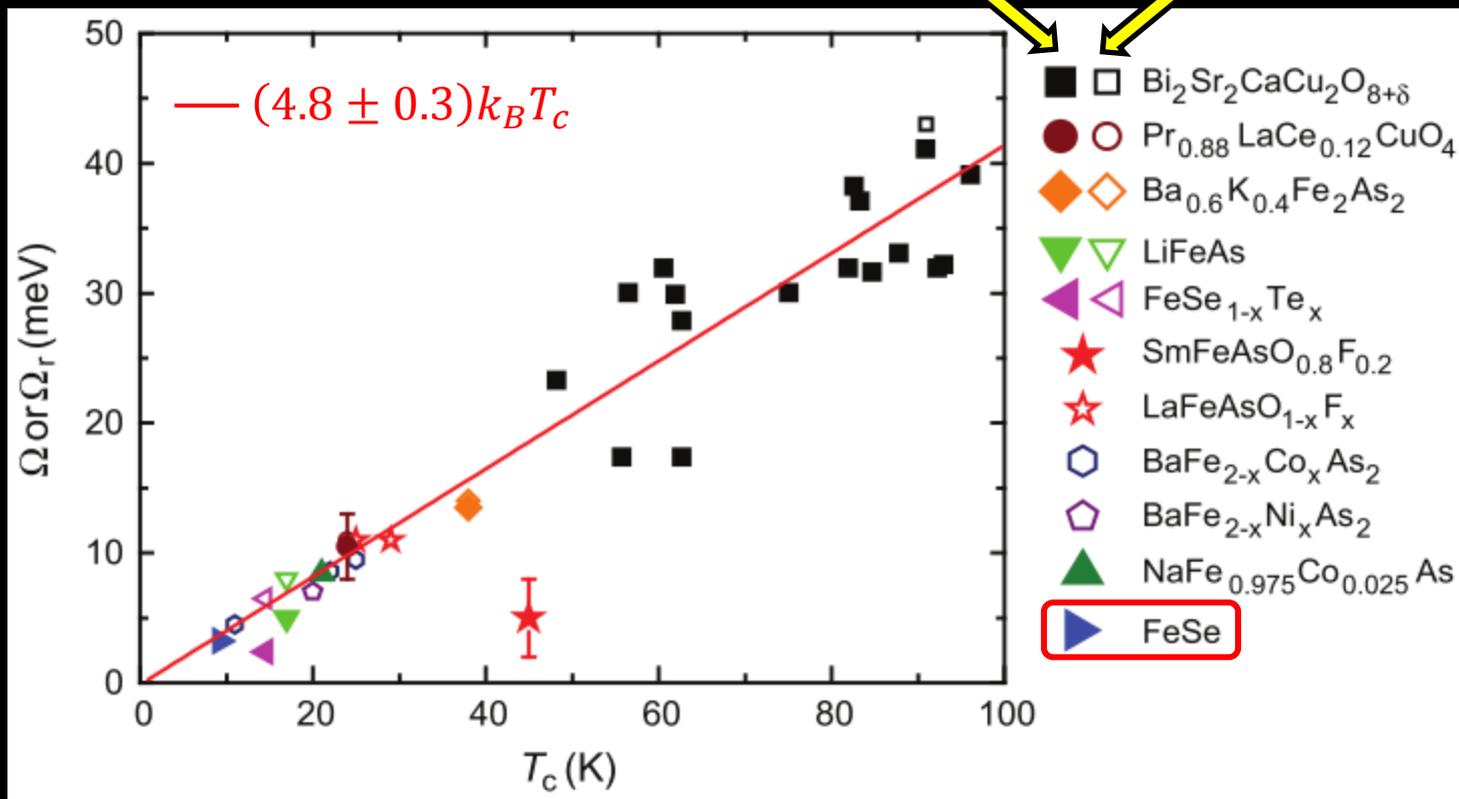
Shan, PRL 108, 227002 (2012)

# $\Omega$ in cuprates and Fe-superconductors



solid symbols =  $\Omega$   
(from STM)

open symbols =  $\Omega_r$   
(from neutron scattering)



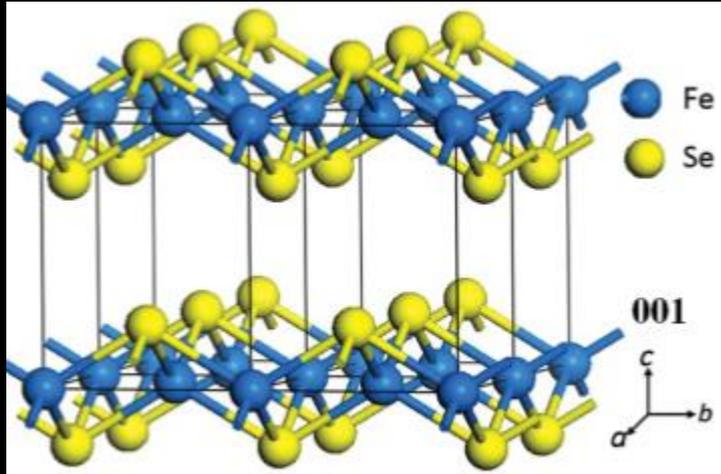
$E$  (dip in  $dI/dV$ )  
 $E$  (peak in  $d^2I/dV^2$ )  
 $E$  (dip in  $d^2I/dV^2$ )  
 $E$  (dip in  $dI/dV$ )  
 $E$  (peak in  $d^2I/dV^2$ )  
 $E$  (dip in  $dI/dV$ )  
 $E$  (dip in  $dI/dV$ )  
 $E$  (dip in  $d^2I/dV^2$ )  
 $E$  (dip in  $d^2I/dV^2$ )  
 $E$  (dip in  $d^2I/dV^2$ )  
 $E$  (peak in  $d^2I/dV^2$ )

Song + Hoffman, *Current Opinion in Solid State and Materials Science* 17, 39 (2013)

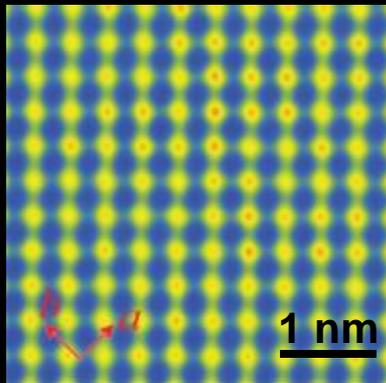
# Boson in 11 superconductor: FeSe



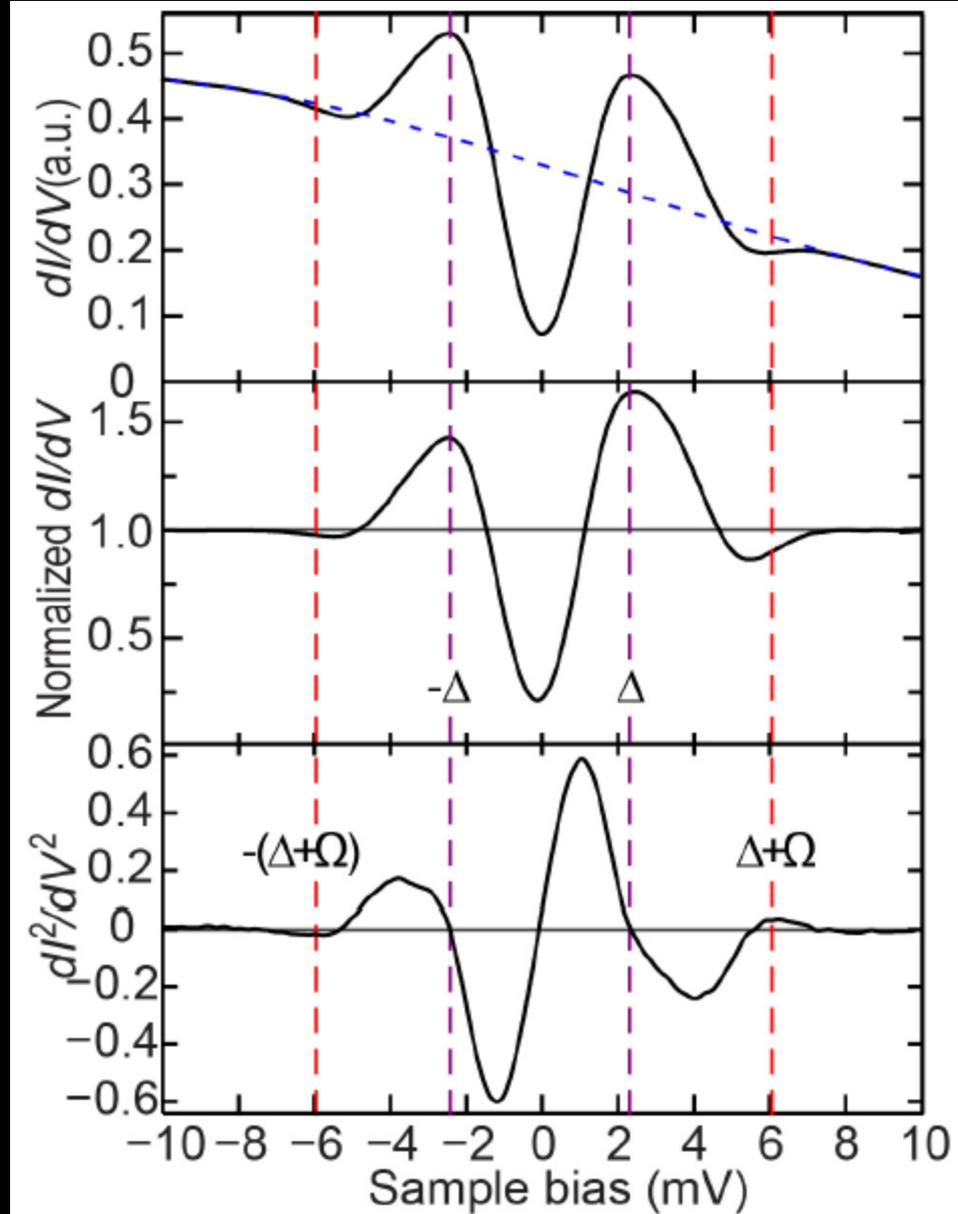
FeSe film on graphene ( $T_c \sim 8\text{K}$ )



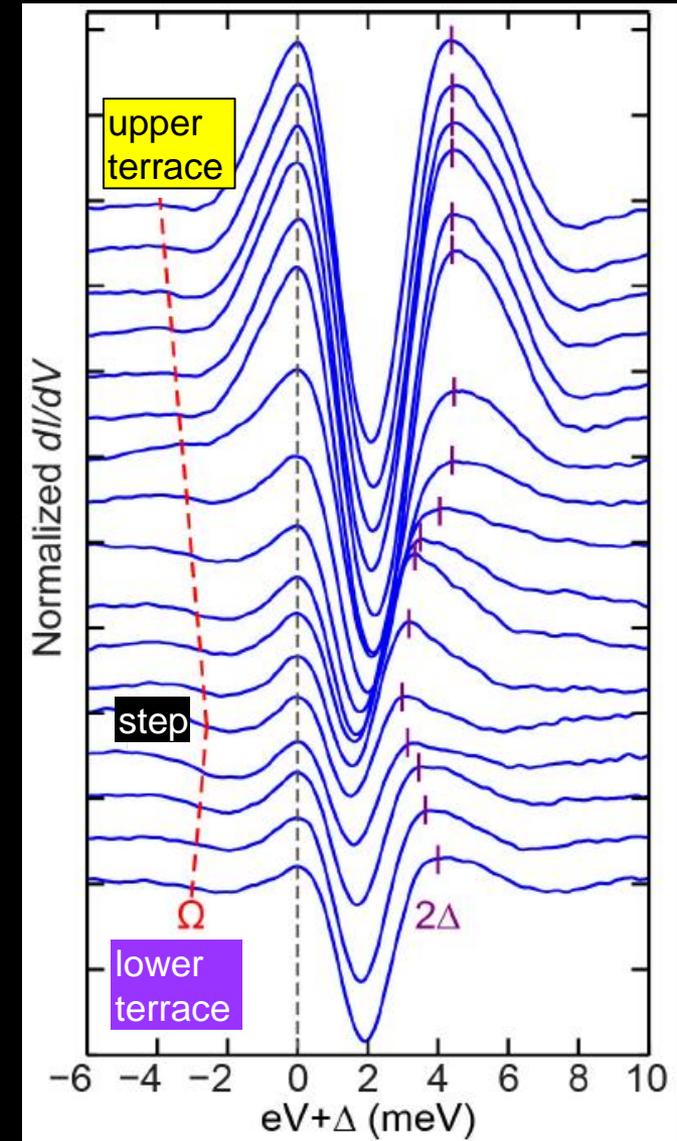
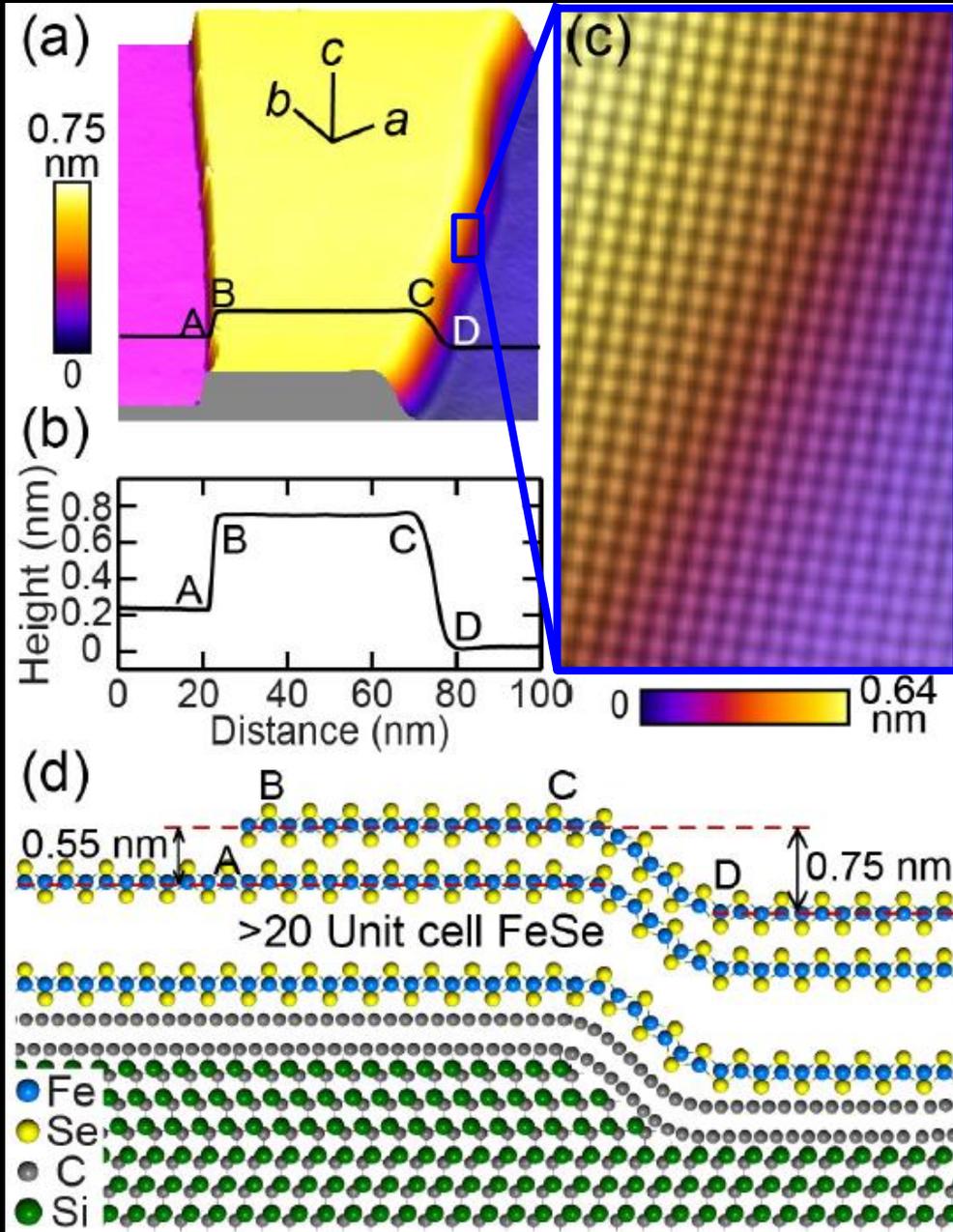
STM topography



$$\Omega = E (\text{peak in } d^2I/dV^2) - \Delta$$



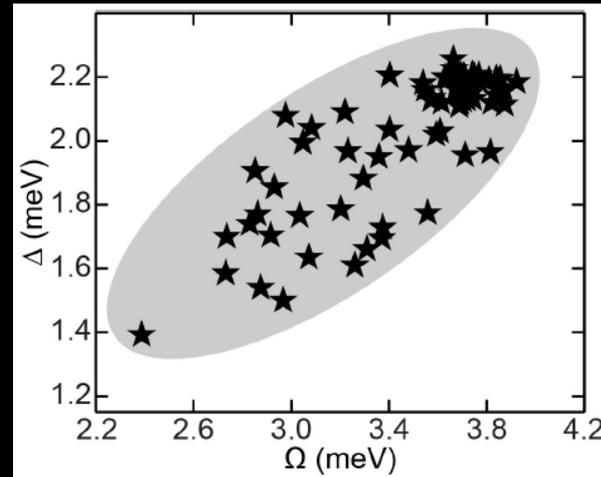
# Tensile strain reduces $\Delta$ and $\Omega$ in FeSe



# Fe-SCs: local relation between $\Delta(r)$ and $\Omega(r)$

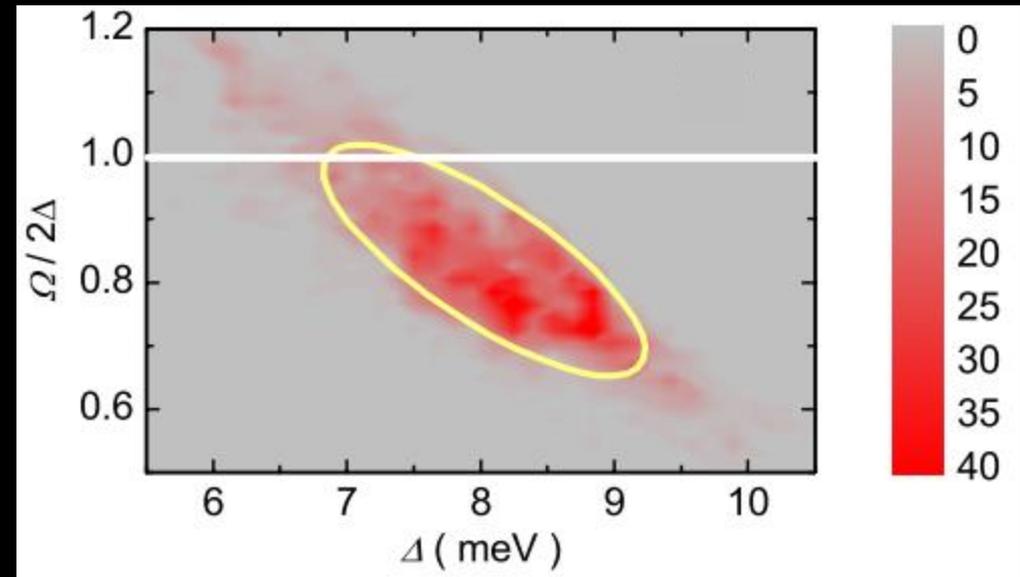


FeSe ( $T_c=8\text{K}$ )



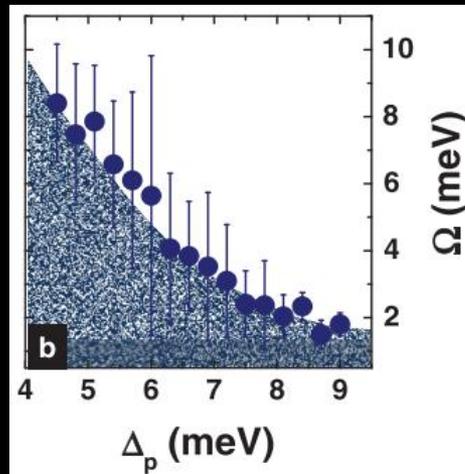
Song, arxiv:1308.2155

$\text{Ba}_{0.6}\text{K}_{0.4}\text{Fe}_2\text{As}_2$  ( $T_c=38\text{K}$ )



Shan, PRL 108, 227002 (2012)

$\text{SmFeAsO}_{0.8}\text{F}_{0.2}$  ( $T_c=45\text{K}$ )

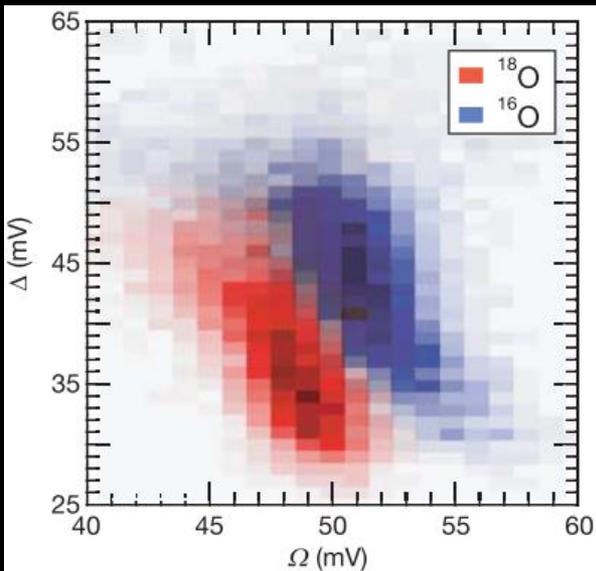


Fasano, PRL 105 167005 (2010)

# Cuprates: local relation between $\Delta(r)$ and $\Omega(r)$

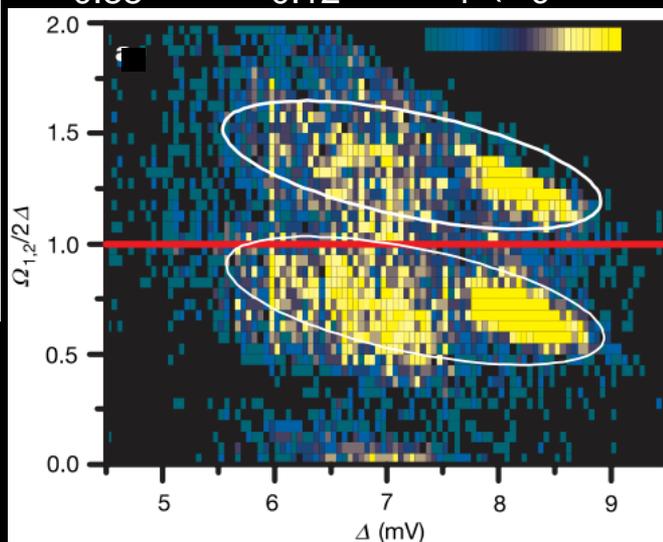


Bi-2212 ( $T_c^{\max} = 91\text{K}$ )



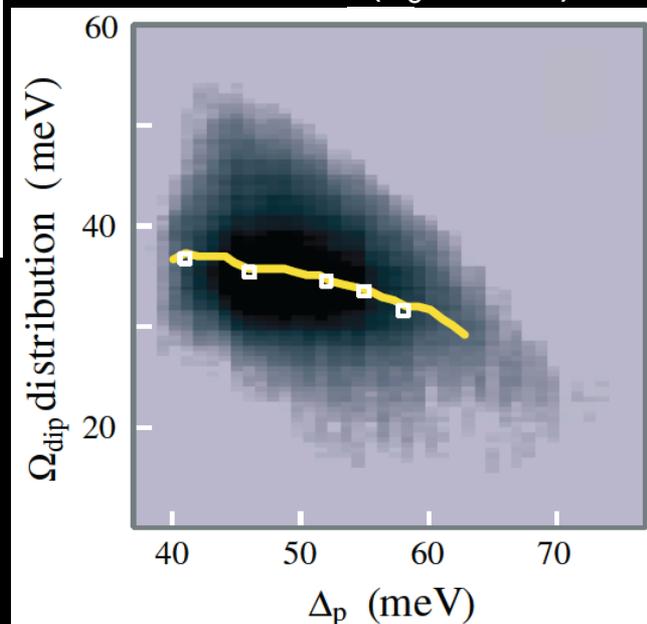
Lee, *Nature* 442, 546 (2006)

$\text{Pr}_{0.88}\text{LaCe}_{0.12}\text{CuO}_4$  ( $T_c=21\text{K}$ )



Niestemski, *Nature* 450, 1058 (2007)

Bi-2223 ( $T_c=110\text{K}$ )



Jenkins, *PRL* 103, 227001 (2009)

# Local strong-coupling pairing



Solve the local Eliashberg equations with patch size  $\sim 2\text{-}5$  nm:

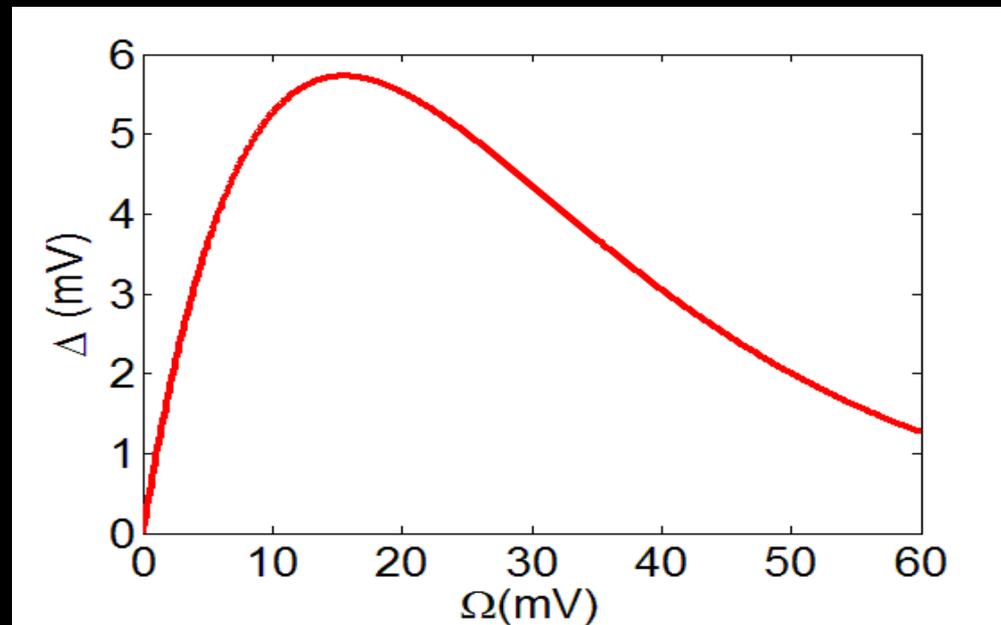
$$\Delta(r) = \Omega(r) \exp\left(\frac{-1}{N_0 g_{\text{eff}}(r)}\right)$$

$g_{\text{eff}}(r)$  = effective coupling constant

$$g_{\text{eff}}(r) = \frac{2g(r)^2}{\Omega(r)}$$

$g(r)$  = local coupling constant

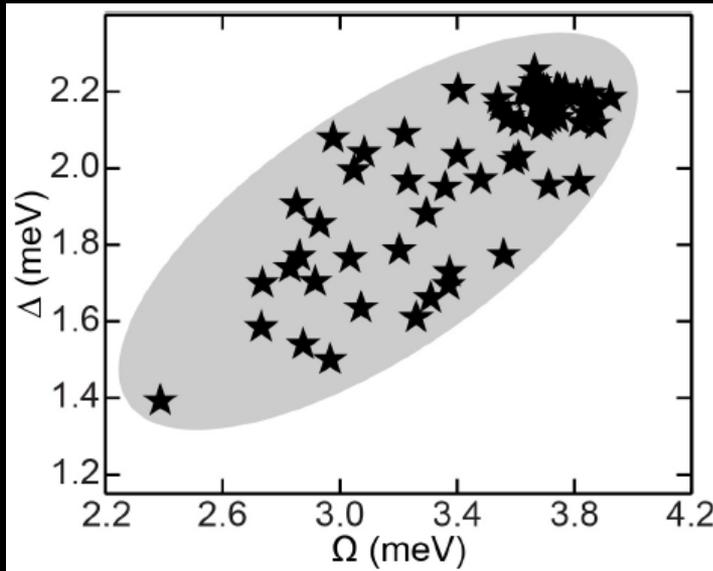
$$\Delta(r) = \Omega(r) \exp\left(\frac{-\Omega(r)}{2N_0 g(r)^2}\right)$$



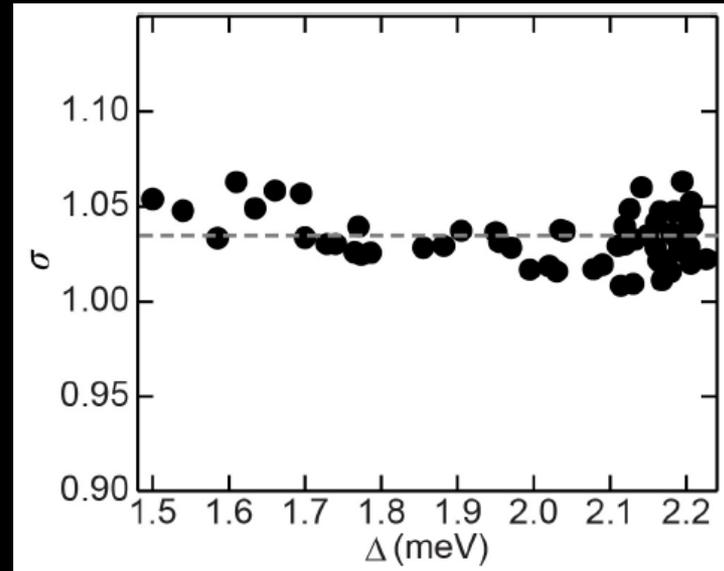
# What about $g(r)$ ?



$\Omega(r):\Delta(r) \rightarrow$  correlation



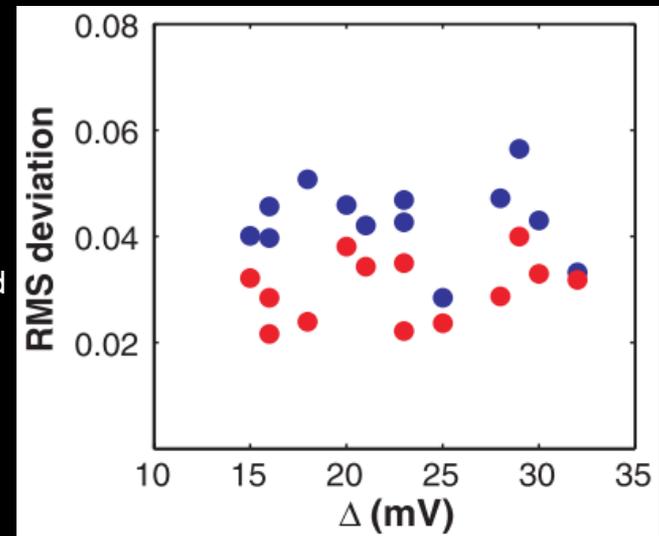
$g(r):\Delta(r) \rightarrow$  no correlation



Song, arxiv:1308.2155

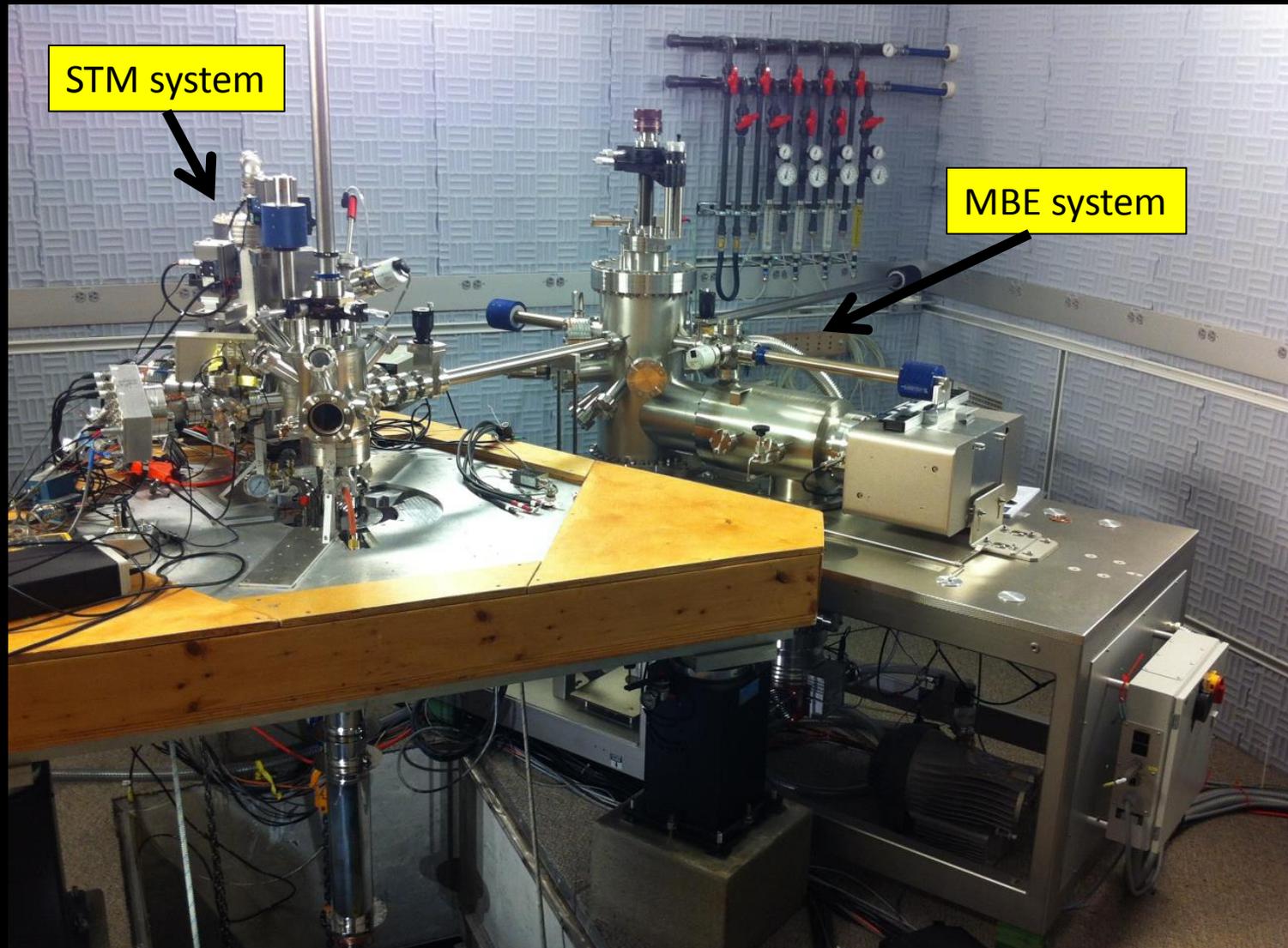
*c.f.* cuprates:

$g(r):\Delta(r) \rightarrow$  no correlation in  $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+d}$



Pasupathy, Science 320, 196 (2008)

# What's next?



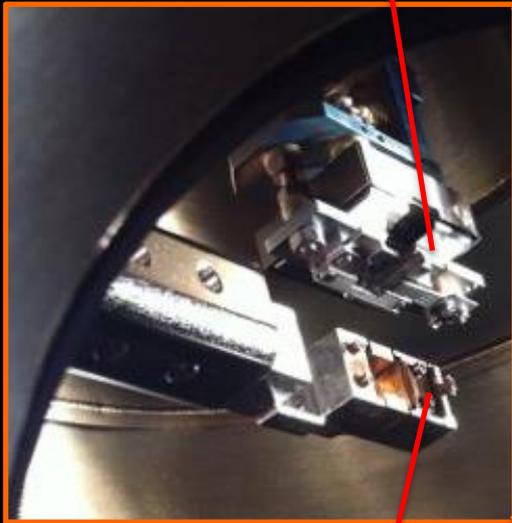
# Molecular Beam Epitaxy



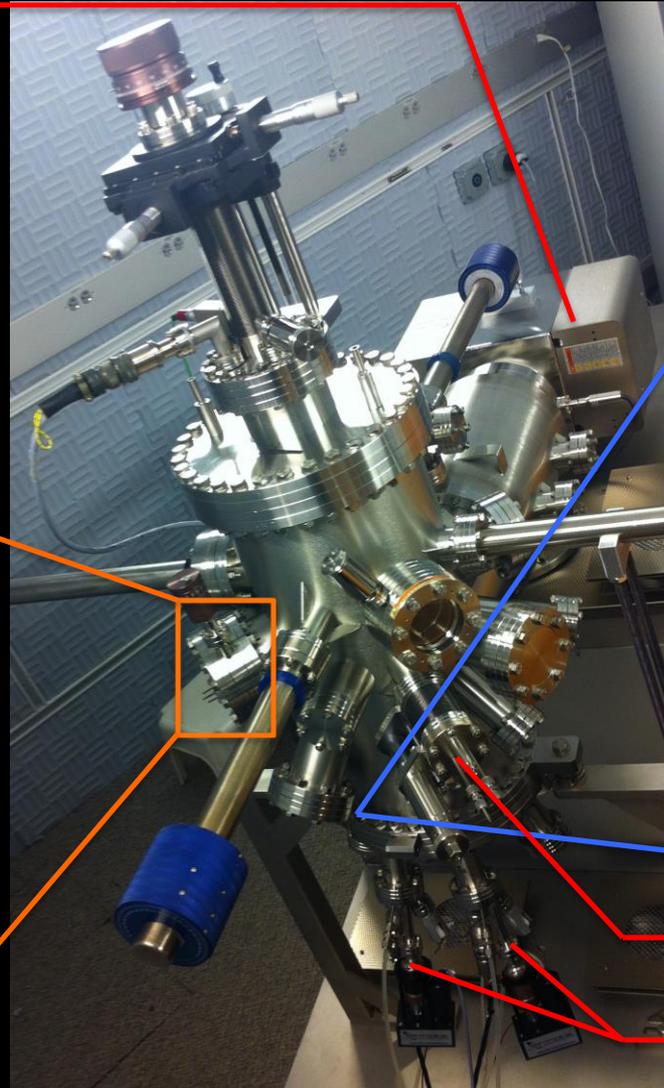
Ion getter pump and  
titanium sublimation pump  
*Base pressure:  $10^{-10}$  T*

Custom heater stage with  
Ta filament

*Through viewport:*



Homebuilt sample  
holder storage



Homebuilt evaporation  
source (Si)



Homebuilt evaporation  
source (Ta boats)

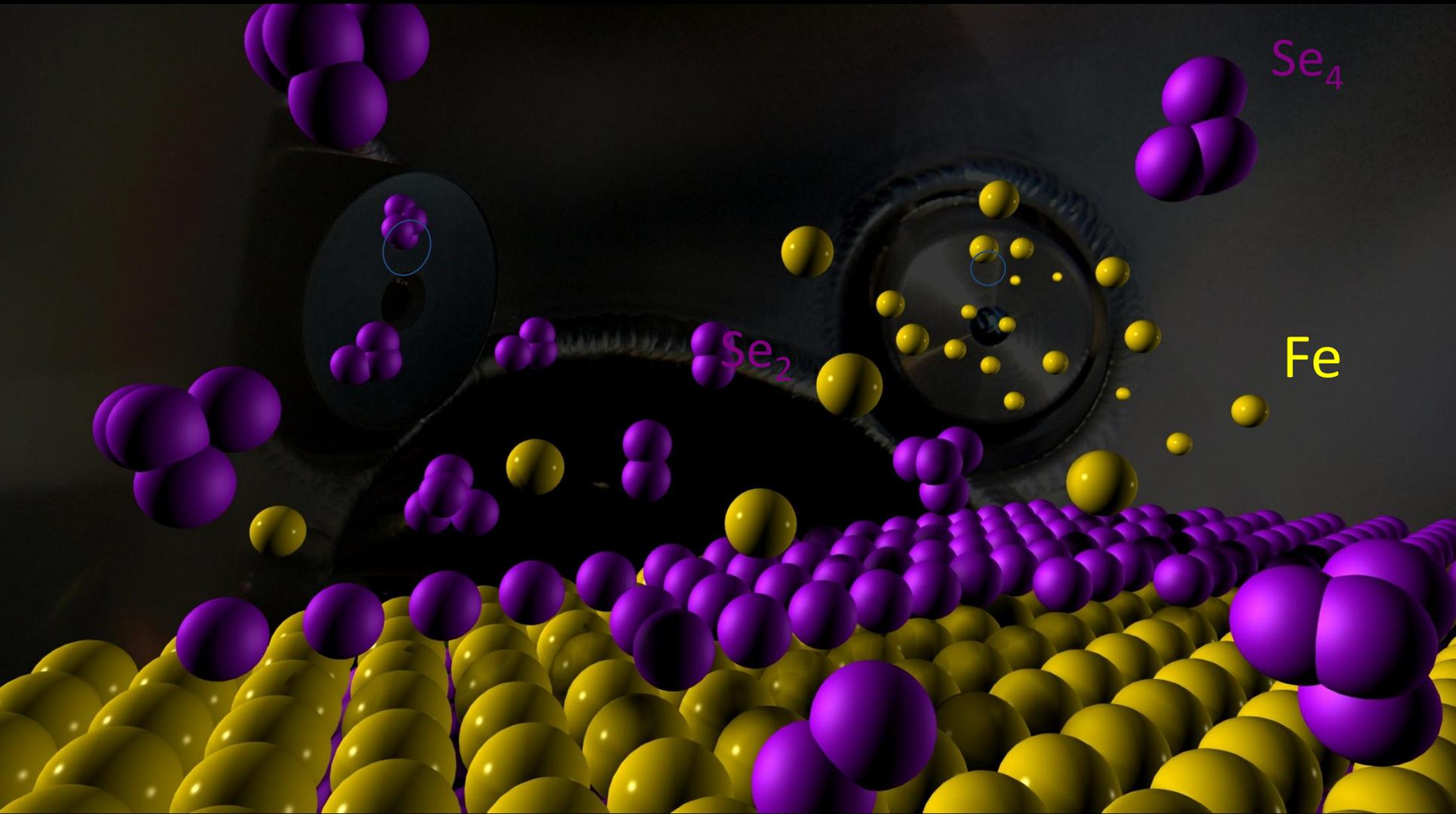


Quartz crystal monitor

Oxygen-resistant effusion  
cells

*Dennis Huang, Can-Li Song*

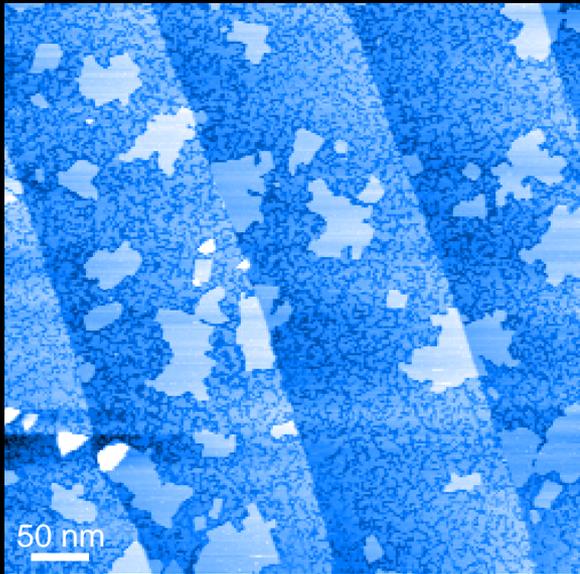
# Film Growth



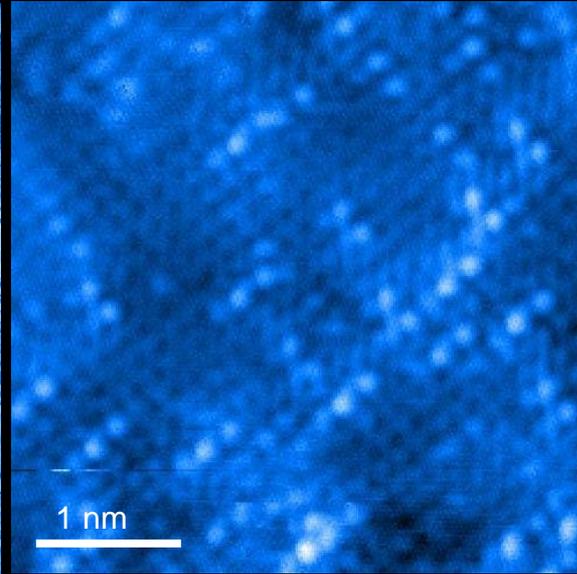
# Film Growth



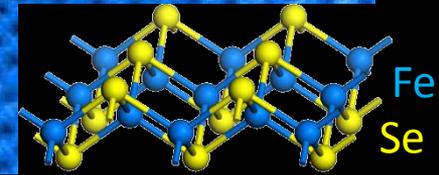
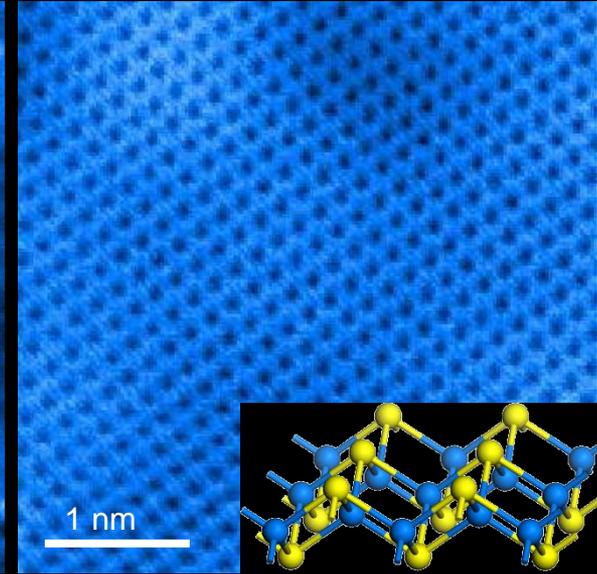
FeSe islands on SiC



as-grown: extra Se



after annealing: clean



## Systems of interest:

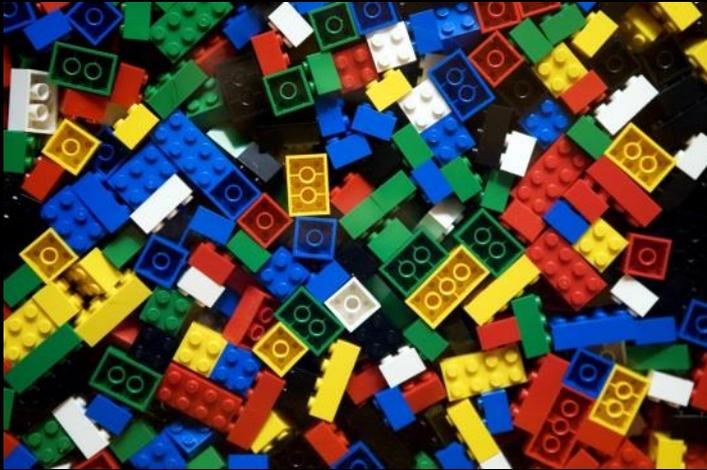
Bulk FeSe:  $T_c = 8 \text{ K}$   $\rightarrow$  FeSe on SrTiO<sub>3</sub>:  $T_c = 110 \text{ K}$

Superconductor on SmB<sub>6</sub>

Sb on superconductor

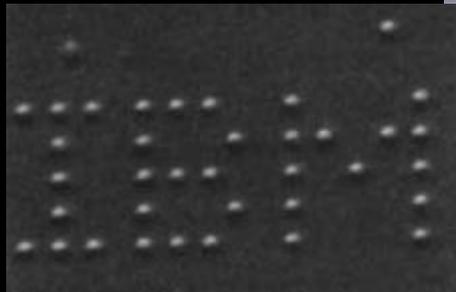
} Majorana fermion?

# Construction projects

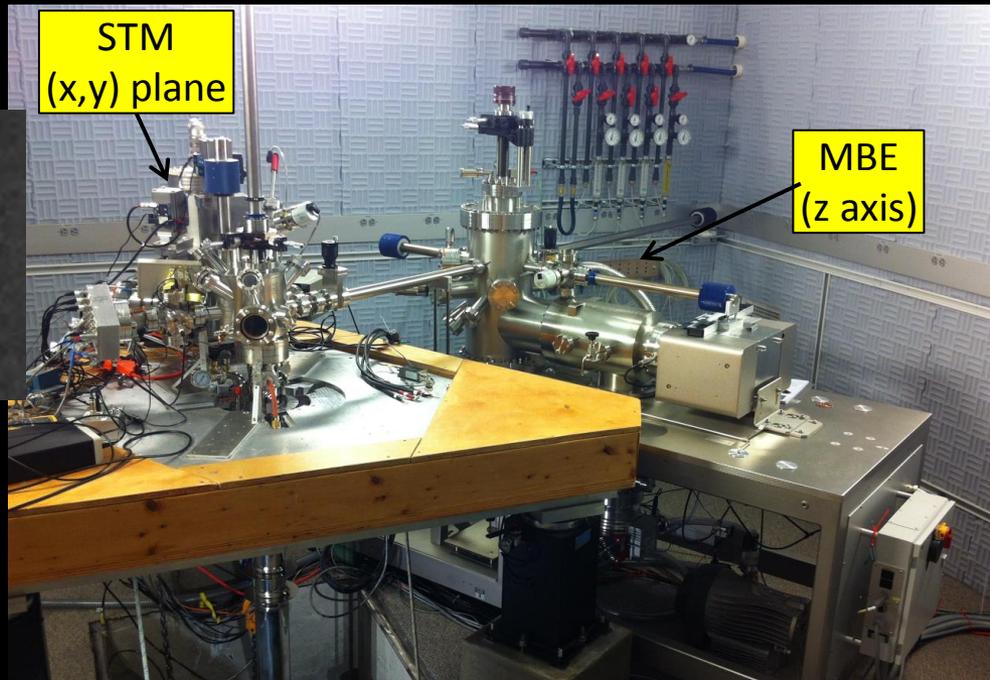


Periodic Table of the Elements

1 1IA H Hydrogen 1.00794	2 IIA He Helium 4.002602																	18 VIIIA Ar Argon 39.948																	
3 IIIA Li Lithium 6.941	4 IIA Be Beryllium 9.012182																	19 VIIA F Fluorine 18.9984032	20 VIIIA Ne Neon 20.1797																
11 IA Na Sodium 22.98976928	12 IIA Mg Magnesium 24.304	13 IIIA Al Aluminum 26.9815386	14 IVA Si Silicon 28.0855836	15 VA P Phosphorus 30.973762	16 VIA S Sulfur 32.06	17 VIIA Cl Chlorine 35.453	18 VIIIA Ar Argon 39.948																	35 VIIA Br Bromine 79.904	36 VIIIA Kr Krypton 83.80										
19 IA K Potassium 39.0983	20 IIA Ca Calcium 40.078	21 IIIB Sc Scandium 44.955912	22 IVB Ti Titanium 47.88	23 VB V Vanadium 50.9415	24 VIB Cr Chromium 51.9961	25 VIIB Mn Manganese 54.938044	26 VIII Fe Iron 55.845	27 VIII Co Cobalt 58.933195	28 VIII Ni Nickel 58.6934	29 VIII Cu Copper 63.546	30 VIII Zn Zinc 65.38	31 IIIB Ga Gallium 69.723	32 IVB Ge Germanium 72.64	33 VB As Arsenic 74.9216	34 VIB Se Selenium 78.96	35 VIIA Br Bromine 79.904	36 VIIIA Kr Krypton 83.80																	53 VIIA I Iodine 126.90547	54 VIIIA Xe Xenon 131.29
37 IA Rb Rubidium 85.4678	38 IIA Sr Strontium 87.62	39 IIIB Y Yttrium 88.905848	40 IVB Zr Zirconium 91.224	41 VB Nb Niobium 92.90638	42 VIB Mo Molybdenum 95.94	43 VIIB Tc Technetium 98.9062	44 VIII Ru Ruthenium 101.07	45 VIII Rh Rhodium 102.9055	46 VIII Pd Palladium 106.42	47 VIII Ag Silver 107.8682	48 VIII Cd Cadmium 112.411	49 IIIB In Indium 114.818	50 IVB Sn Tin 118.710	51 VB Sb Antimony 121.760	52 VIB Te Tellurium 127.6	53 VIIA I Iodine 126.90547	54 VIIIA Xe Xenon 131.29																	85 VIIA At Astatine 208.9804	86 VIIIA Rn Radon 222.01758
55 IA Cs Cesium 132.90545196	56 IIA Ba Barium 137.327	57-71 Lanthanide Series	72 IVB Hf Hafnium 178.49	73 VB Ta Tantalum 180.94788	74 VIB W Tungsten 183.84	75 VIIB Re Rhenium 186.207	76 VIII Os Osmium 190.23	77 VIII Ir Iridium 192.222	78 VIII Pt Platinum 195.084	79 VIII Au Gold 196.966569	80 VIII Hg Mercury 200.59	81 IIIB Tl Thallium 204.3833	82 IVB Pb Lead 207.2	83 VB Bi Bismuth 208.9804	84 VIB Po Polonium [209]	85 VIIA At Astatine [209]	86 VIIIA Rn Radon [222]																	117 VIIA Ts Tennessine [294]	118 VIIIA Uuo Ununoctium [294]
87 IA Fr Francium [223]	88-103 Actinide Series	104 IVB Rf Rutherfordium [261]	105 VB Db Dubnium [262]	106 VIB Sg Seaborgium [266]	107 VIIB Bh Bohrium [264]	108 VIII Hs Hassium [265]	109 VIII Mt Meitnerium [268]	110 VIII Ds Darmstadtium [271]	111 VIII Rg Roentgenium [272]	112 VIII Cn Copernicium [285]	113 IIIB Uut Ununtrium [288]	114 IVB Uuq Ununquadium [289]	115 VB Uup Ununpentium [288]	116 VIB Uuh Ununhexium [289]	117 VIIA Uus Ununseptium [289]	118 VIIIA Uuo Ununoctium [289]																	119 IA Uue Ununennium [293]	120 IIA Uuq Ununbinium [293]	
Lanthanide Series		57 La Lanthanum 138.90547	58 Ce Cerium 140.12	59 Pr Praseodymium 140.90766	60 Nd Neodymium 144.242	61 Pm Promethium [145]	62 Sm Samarium 150.36	63 Eu Europium 151.964	64 Gd Gadolinium 157.25	65 Tb Terbium 158.92534	66 Dy Dysprosium 162.50	67 Ho Holmium 164.93032	68 Er Erbium 167.259	69 Tm Thulium 168.93481	70 Yb Ytterbium 173.04	71 Lu Lutetium 174.967																			
Actinide Series		89 Ac Actinium [227]	90 Th Thorium [232]	91 Pa Protactinium [231]	92 U Uranium [238]	93 Np Neptunium [237]	94 Pu Plutonium [244]	95 Am Americium [243]	96 Cm Curium [247]	97 Bk Berkelium [247]	98 Cf Californium [251]	99 Es Einsteinium [252]	100 Fm Fermium [257]	101 Md Mendelevium [258]	102 No Nobelium [259]	103 Lr Lawrencium [260]																			



Eigler & Schweizer,  
Nature 344, 524 (1990)



→ 3D printing with atoms

# Moving to Vancouver, looking for postdocs



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