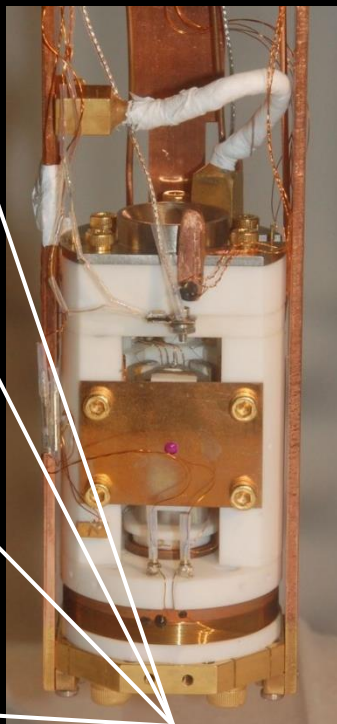


Hoffman Lab Microscopes



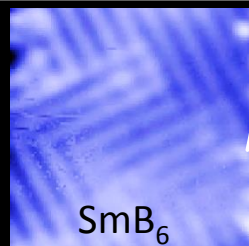
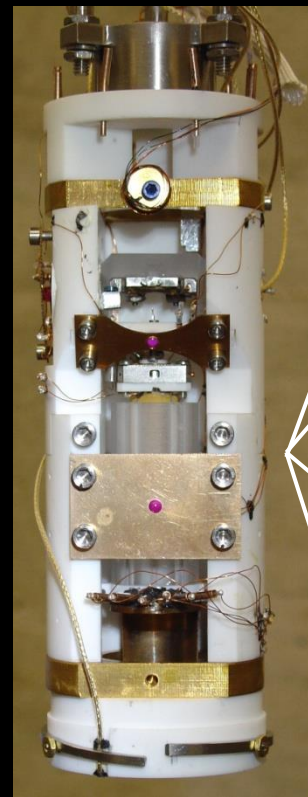
Scanning Tunneling
Microscope



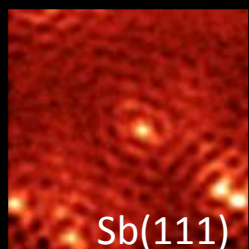
Force Microscope



STM - MBE



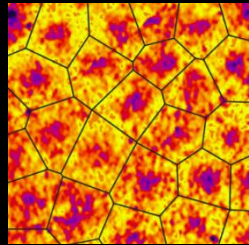
SmB_6



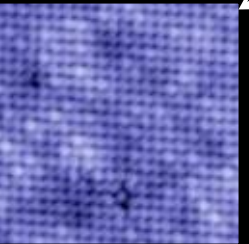
$\text{Sb}(111)$



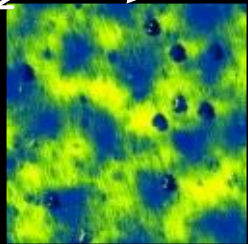
Bi_2Se_3



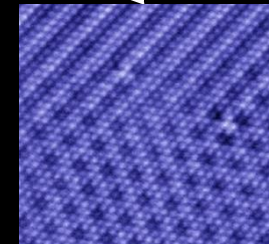
$\text{K}_x\text{Sr}_{1-x}\text{Fe}_2\text{As}_2$



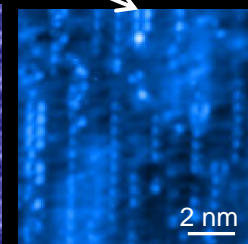
Bi-2201



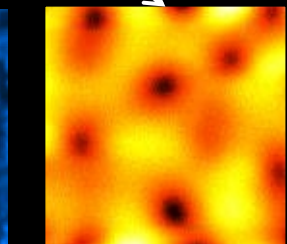
$\text{Ba}(\text{Fe}_{1-x}\text{Co}_x)_2\text{As}_2$



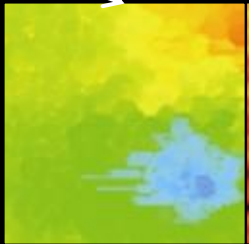
NbSe_2



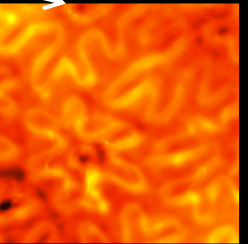
$\text{Li}_{0.9}\text{Mo}_6\text{O}_{17}$



$\text{NdFeAsO}_{1-x}\text{F}_x$



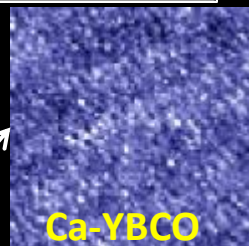
VO_2



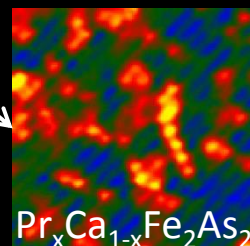
$\text{Nd}_2\text{Fe}_{14}\text{B}$



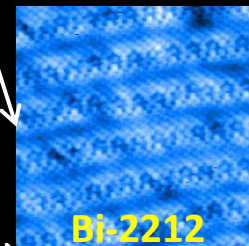
$\text{La}_2\text{SrMn}_2\text{O}_7$



Ca-YBCO



$\text{Pr}_x\text{Ca}_{1-x}\text{Fe}_2\text{As}_2$

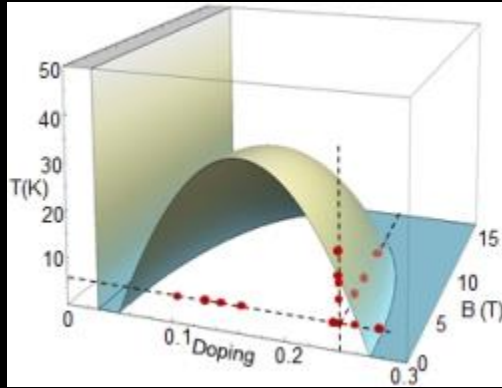


Bi-2212

High- T_c Superconductivity

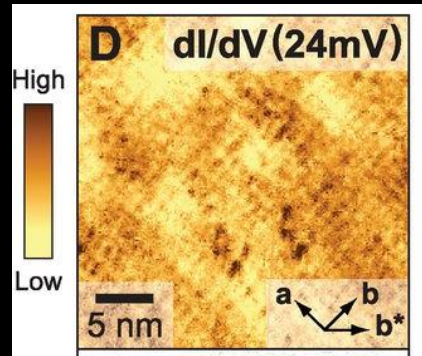


Picoscale atomic distortion



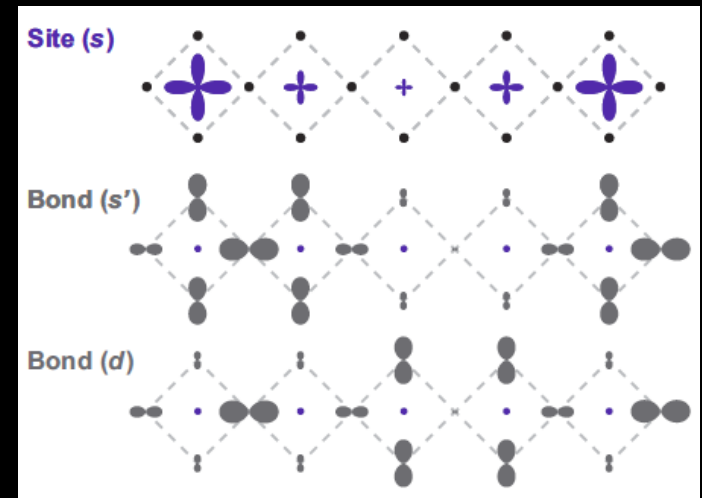
Nature Materials 11, 585 (2012)

Charge ordering



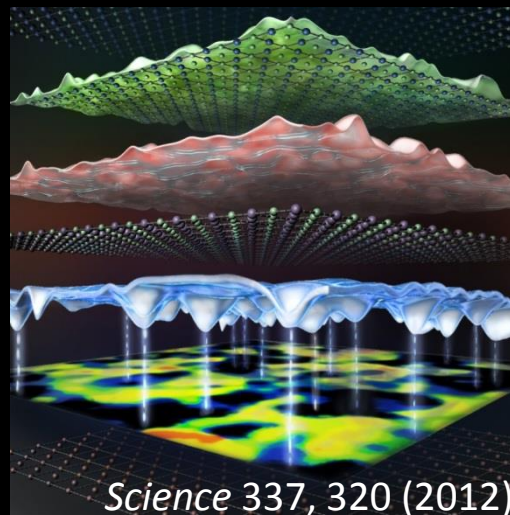
Science 343, 390 (2014)

d-wave charge ordering



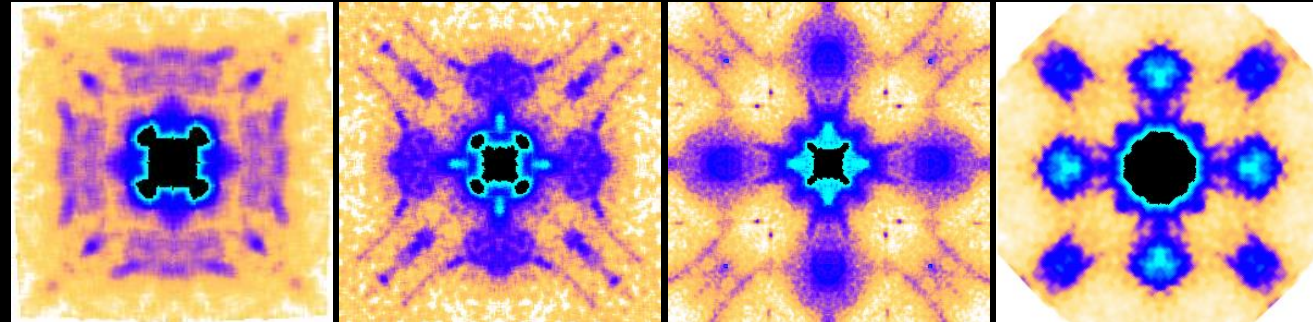
arxiv:1402.5415

Single oxygen atoms



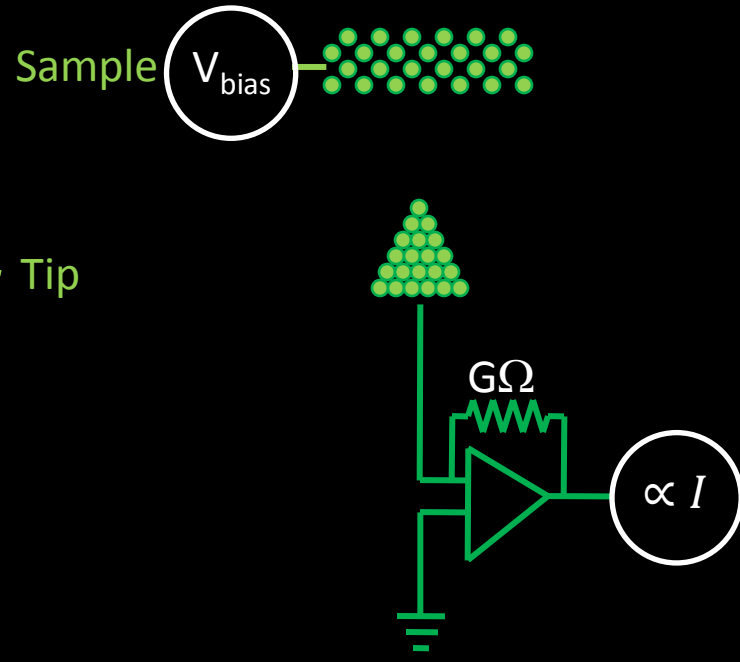
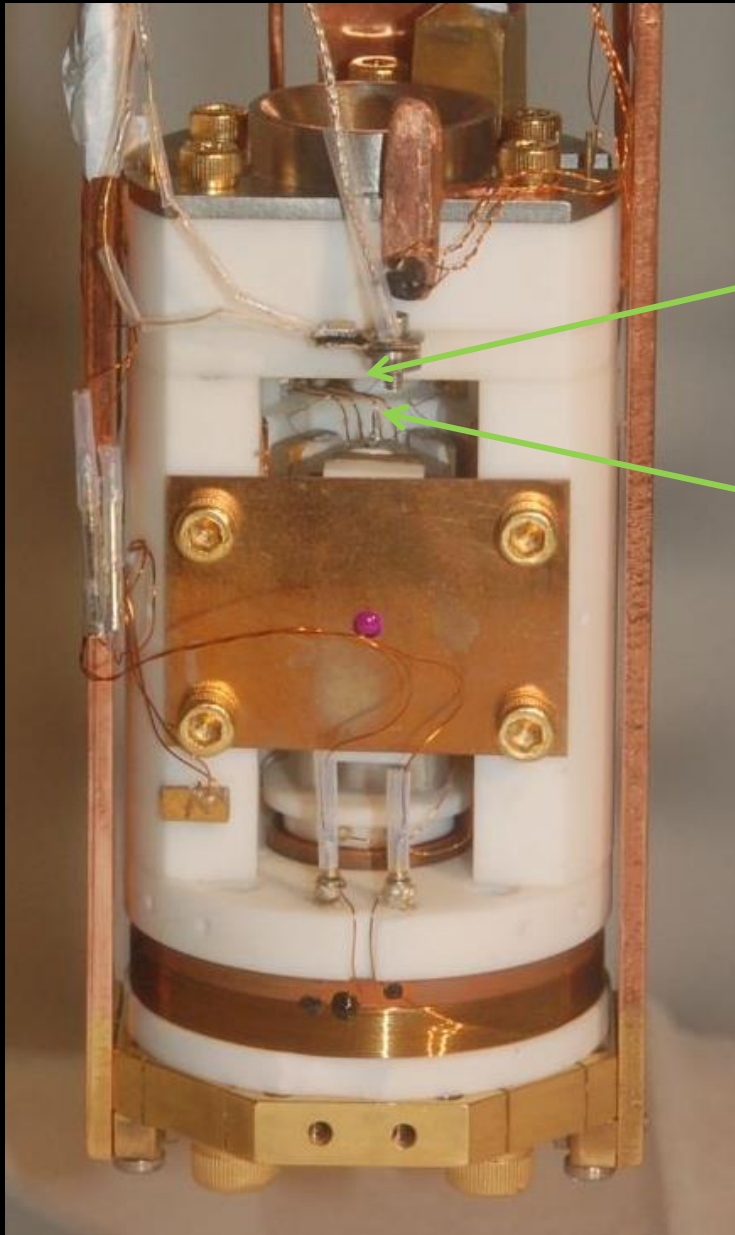
Science 337, 320 (2012)

Fermi surface transition



Science 344, 608 (2014)

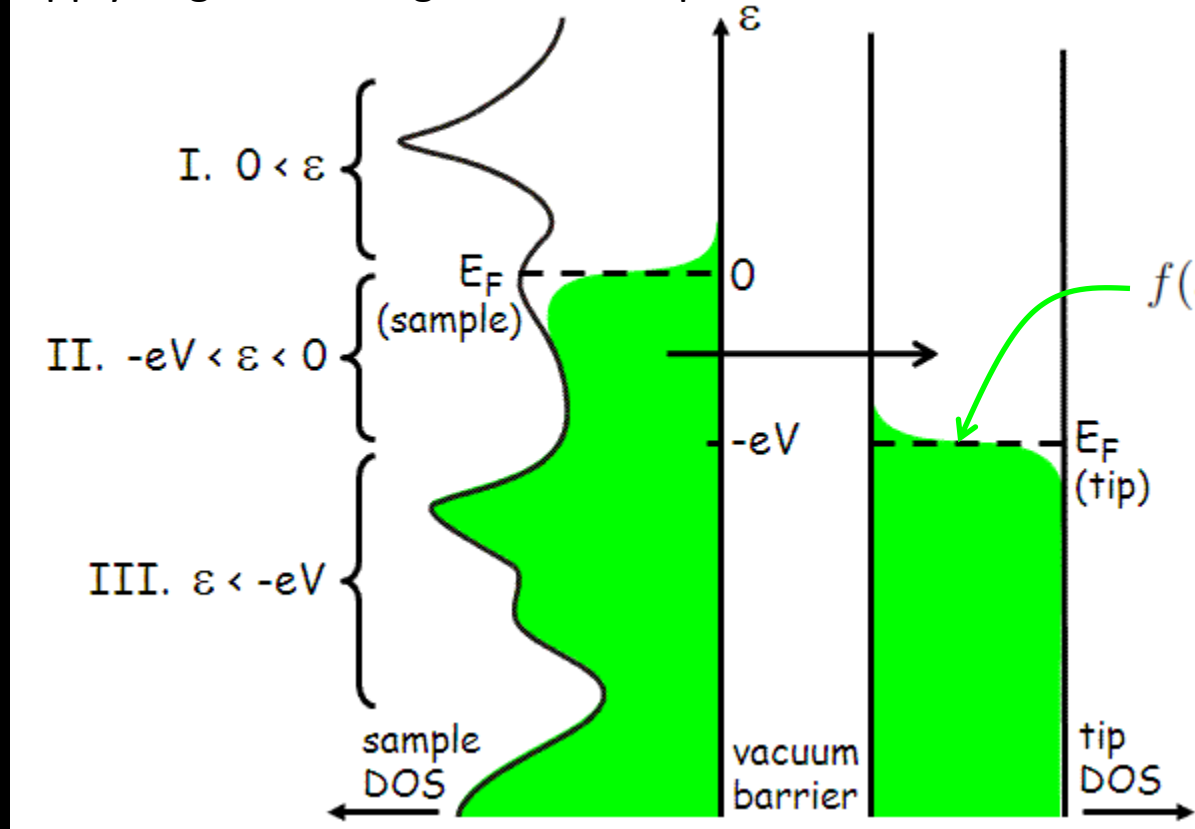
Scanning Tunneling Microscopy



Scanning Tunneling Microscopy



Apply negative voltage to the sample:



$$f(\epsilon) = \frac{1}{1 + e^{\epsilon/k_B T}}$$

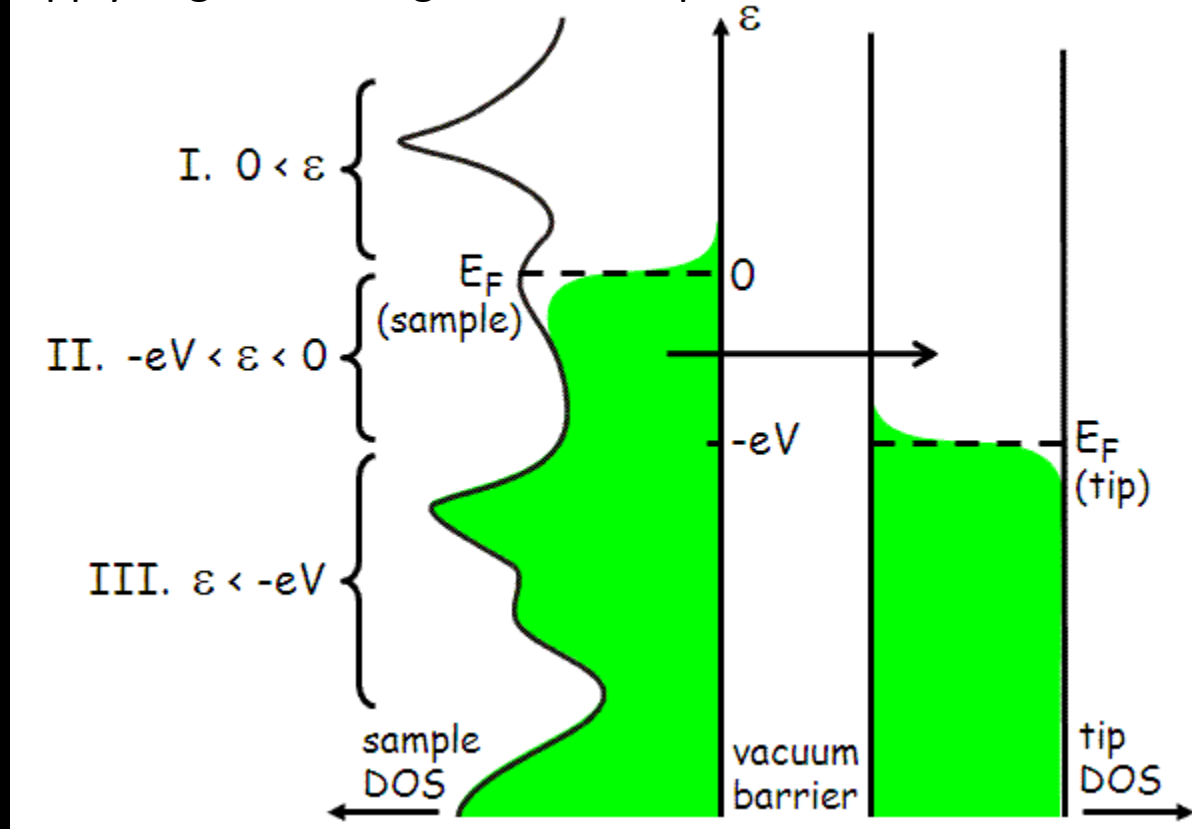
$$I_{\text{sample} \rightarrow \text{tip}} = -2e \cdot \frac{2\pi}{\hbar} |M|^2 \underbrace{(\rho_s(\epsilon) \cdot f(\epsilon))}_{\# \text{ filled sample states for tunneling from}} \underbrace{(\rho_t(\epsilon + eV) \cdot [1 - f(\epsilon + eV)])}_{\# \text{ empty tip states for tunneling to}}$$

$$I = -\frac{4\pi e}{\hbar} \int_{-\epsilon_{F(\text{tip})}}^{\infty} |M|^2 \rho_s(\epsilon) \rho_t(\epsilon + eV) \{f(\epsilon) [1 - f(\epsilon + eV)] - [1 - f(\epsilon)] f(\epsilon + eV)\} d\epsilon$$

Scanning Tunneling Microscopy



Apply negative voltage to the sample:



Assume $T \sim 0$

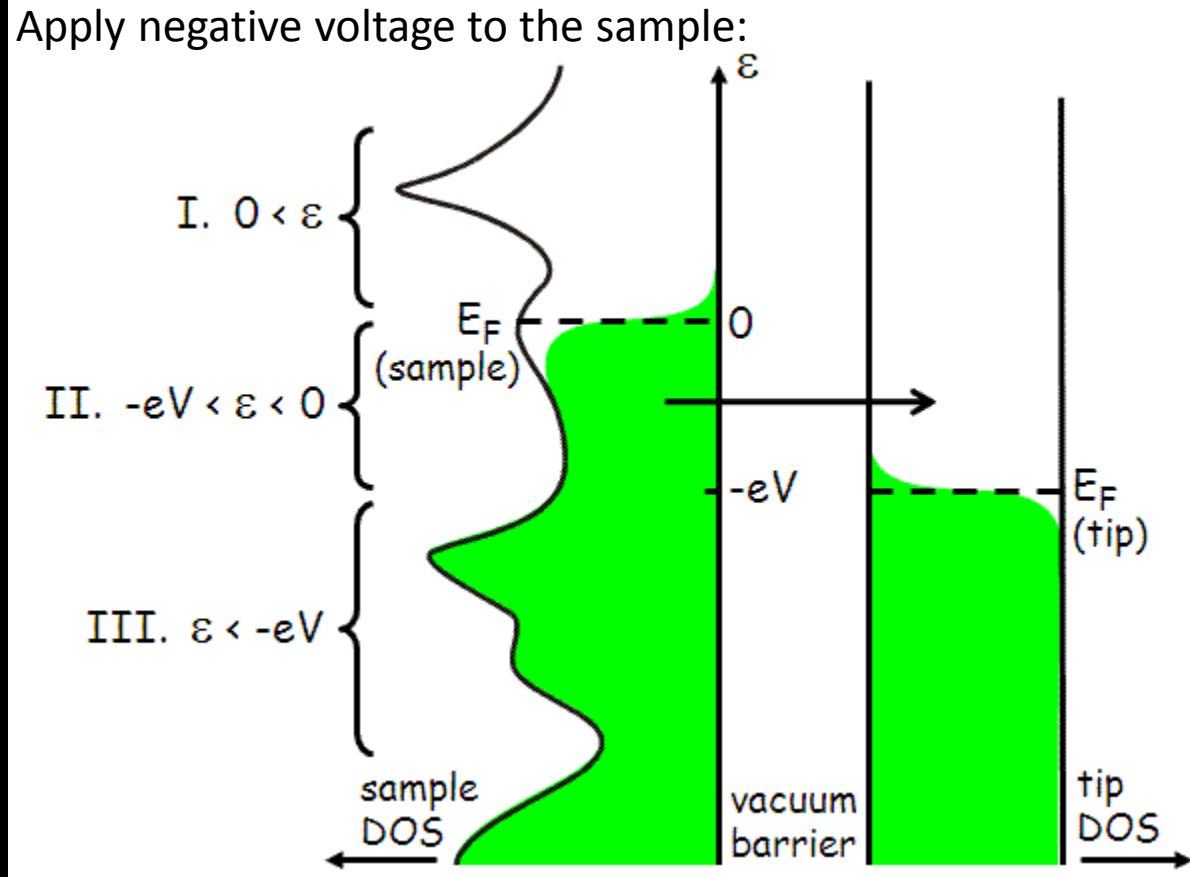
$$I \approx -\frac{4\pi e}{\hbar} \int_{-eV}^0 |M|^2 \rho_s(\epsilon) \rho_t(\epsilon + eV) d\epsilon$$

Assume tip DOS is flat

$$I \approx \frac{4\pi e}{\hbar} \rho_t(0) \int_{-eV}^0 |M|^2 \rho_s(\epsilon) d\epsilon$$

But what is $|M|^2$?

Scanning Tunneling Microscopy



WKB says that the tunneling probability through a barrier will be $|M|^2 = e^{-2\gamma}$ where:

$$\gamma = \int_0^s \sqrt{\frac{2m\varphi}{\hbar^2}} dx = \frac{s}{\hbar} \sqrt{2m\varphi}$$



$$I \approx \frac{4\pi e}{\hbar} e^{-\frac{1}{s} \sqrt{\frac{8m\varphi}{\hbar^2}}} \rho_t(0) \int_{-eV}^0 \rho_s(\varepsilon) d\varepsilon$$

s = tip-sample distance

φ = tip-sample work function

Details: Tersoff & Hamman, PRL 50, 1988 (1983)
& PRB 31, 805 (1985)

STM: setup condition



$$I_{\text{set}} = e^{-z(\vec{r})/z_0} \int_0^{eV_{\text{set}}} N(\vec{r}, \varepsilon) d\varepsilon$$

This eqn fixes $z(\vec{r})$

$$I(\vec{r}, V) = e^{-z_{\text{set}}(\vec{r})/z_0} \int_0^{eV} N(\vec{r}, \varepsilon) d\varepsilon$$

$$\frac{I_{\text{set}}}{\int_0^{eV_{\text{set}}} N(\vec{r}, \varepsilon) d\varepsilon}$$

$$\frac{dI}{dV}(\vec{r}, \varepsilon) = \frac{eI_{\text{set}}}{\int_0^{eV_{\text{set}}} N(\vec{r}, \varepsilon) d\varepsilon} \underbrace{N(\vec{r}, \varepsilon)}$$

↑ this is the raw DOS that we want

→ Define:

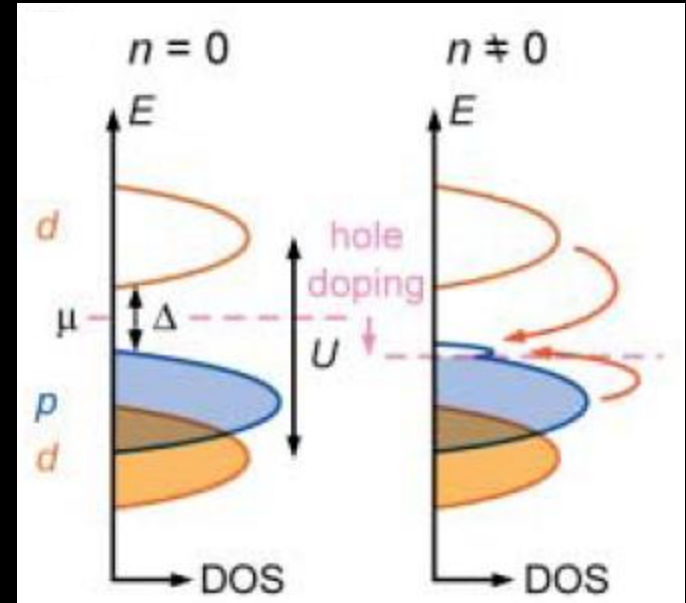
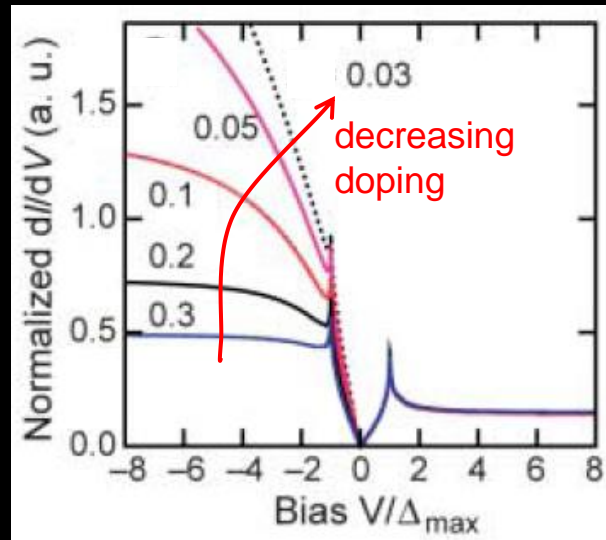
$$Z(\vec{r}, \varepsilon) = \frac{N(\vec{r}, +\varepsilon)}{N(\vec{r}, -\varepsilon)}$$

Z-maps



Theory:

$$Z(V) \equiv \frac{\bar{N}(E = +eV)}{\bar{N}(E = -eV)} \approx \frac{2n}{1+n}$$



P. W. Anderson, N. P. Ong, *J. Phys. Chem. Solids* **67**, 1 (2006).

Experiment:

$$Z(\vec{r}, V) \equiv \frac{\frac{dI}{dV}(\vec{r}, z, +V)}{\frac{dI}{dV}(\vec{r}, z, -V)}$$

R-maps



Theory:

$$R(\vec{r}) \equiv \frac{\int_0^{\Omega_c} N(\vec{r}, E) dE}{\int_{-\infty}^0 N(\vec{r}, E) dE} = \frac{2n(\vec{r})}{1 - n(\vec{r})} + \underbrace{O\left(\frac{nt}{U}\right)}_{10\%}$$

($\Omega_c \sim 1 \text{ eV}$)

Randeria, *PRL* **95**, 137001 (2005).

Experiment:

$$R(\vec{r}, V) \equiv \frac{I(\vec{r}, z, +V)}{I(\vec{r}, z, -V)} \quad (V = 150 \text{ mV})$$

Z vs. R maps

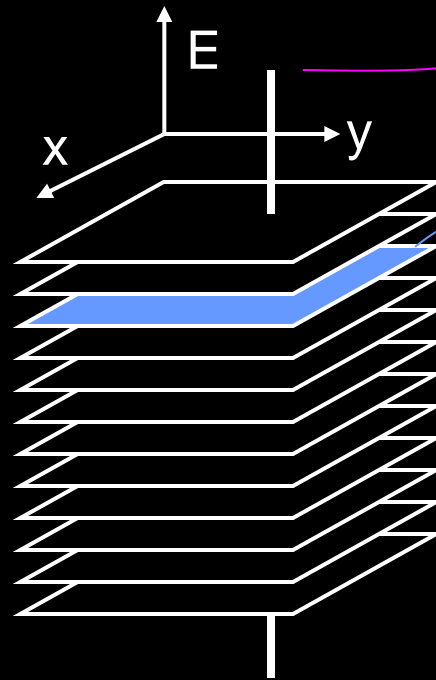


	Z	R
Theory:	$\frac{\bar{N}(E = +eV)}{\bar{N}(E = -eV)} \approx \frac{2n}{1+n}$ <p>Anderson, <i>JPCM</i> (2006)</p>	$\frac{\int_0^{\Omega_c} N(\vec{r}, E) dE}{\int_{-\infty}^0 N(\vec{r}, E) dE} = \frac{2n(\vec{r})}{1-n(\vec{r})}$ <p>Randeria, <i>PRL</i> (2005)</p>
Experiment:	$Z(\vec{r}, V) \equiv \frac{\frac{dI}{dV}(\vec{r}, z, +V)}{\frac{dI}{dV}(\vec{r}, z, -V)}$	$\frac{I(\vec{r}, z, +V)}{I(\vec{r}, z, -V)}$
Advantages:	<p>Maintain energy resolution</p>	<p><u>Divides out the setup condition artifact!</u></p> <p>Integrate over all energies, integrates a small signal, catches a signal at unknown energy.</p>
Disadvantages:	<p><u>Assumes particle-hole symmetry of the signal of interest!</u></p>	<p>Lose energy resolution. What cutoff to use? Theory: $\Omega_c \sim 1$ eV; Expt: $V = 150$ mV</p>
In practice:	QPI	static checkerboards

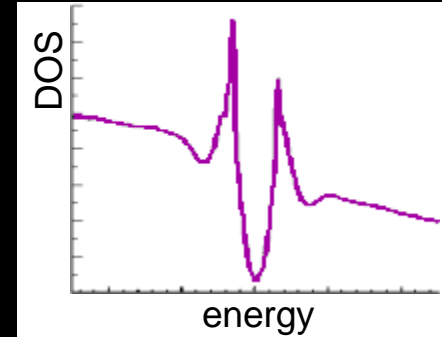
Types of STM Measurements



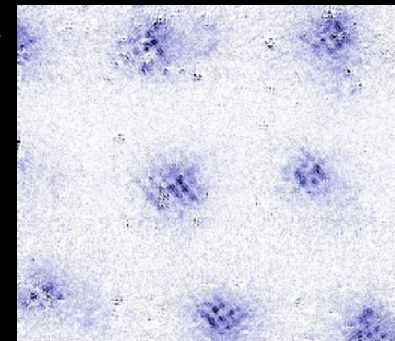
Local Density of States (x, y, E)



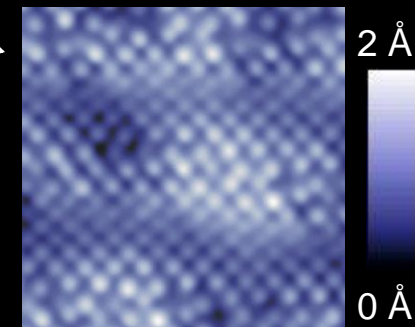
dI/dV Spectrum



dI/dV Map



Topography



Constant current mode:

$$\int \frac{dI}{dV}$$



Advantages

- Filled and empty states
- sub-meV energy resolution
- B-field dependence
- Atomic spatial resolution
- k-information w/ nanoscale resolution (via QPI)

Challenges

- Surface sensitivity
- polarity, termination, reconstruction
- vibration sensitivity

Superconductivity Tunneling Milestones



1960: gap measurement (Pb)

1965: boson energies & coupling (Pb)

1985: charge density wave (TaSe_2)

1989: vortex lattice (NbSe_2)

1997: single atom impurities (Nb)

2002: quasiparticle interference

→ band structure & gap symmetry (BSCCO)

2009: phase-sensitive gap measurement (Na-CCOC)

2010: intra-unit-cell structure (BSCCO)

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1960: Tunneling measurements of Δ



VOLUME 5, NUMBER 4

PHYSICAL REVIEW LETTERS

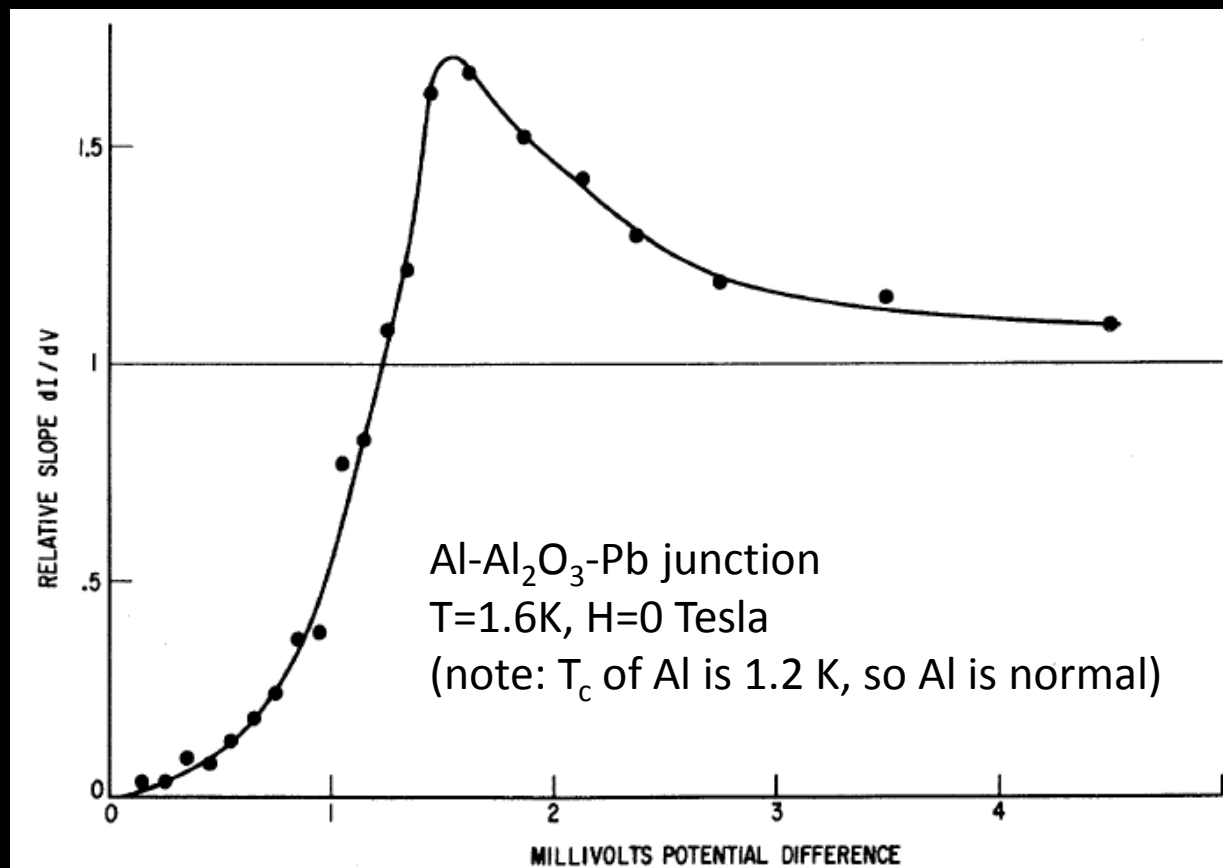
AUGUST 15, 1960

ENERGY GAP IN SUPERCONDUCTORS MEASURED BY ELECTRON TUNNELING

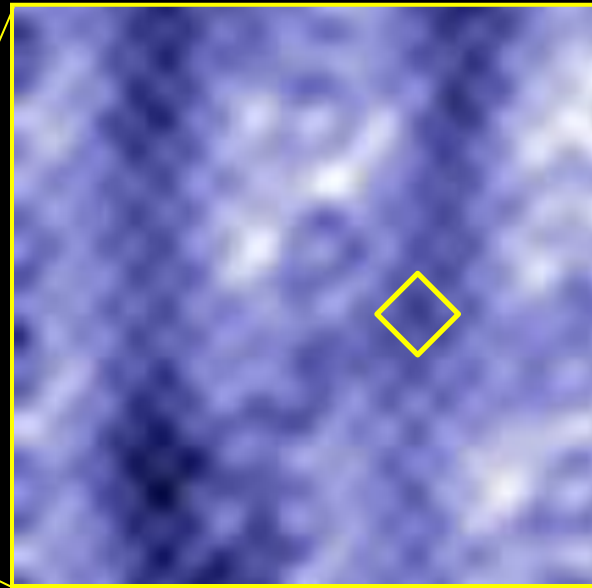
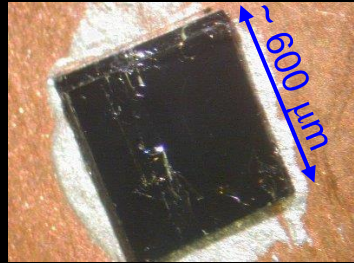
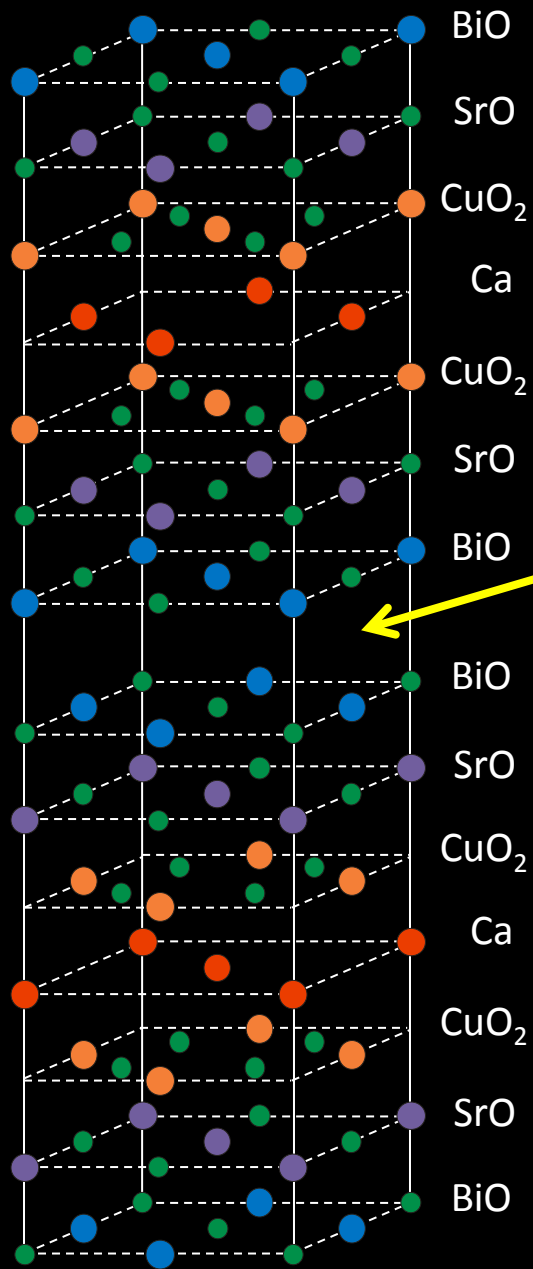
Ivar Giaever

General Electric Research Laboratory, Schenectady, New York

(Received July 5, 1960)

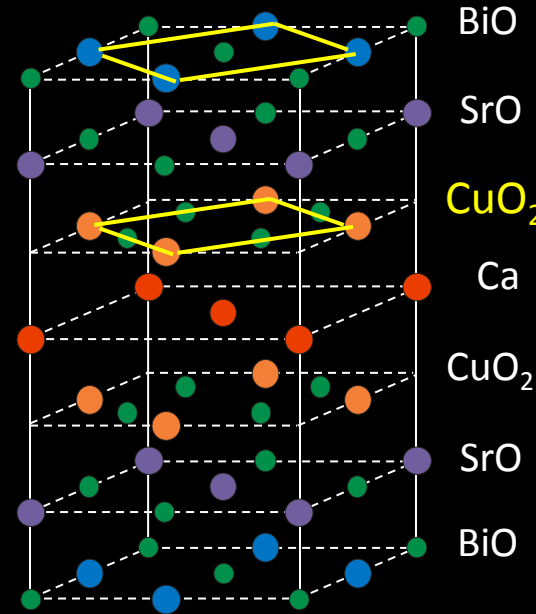


Structure of $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$

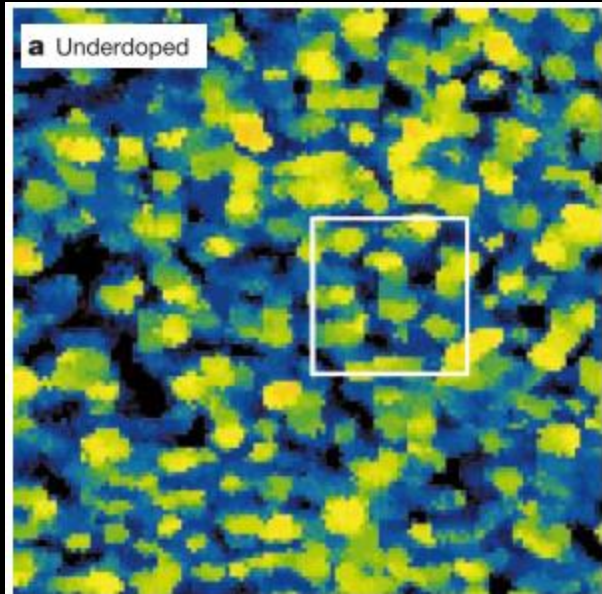


BiO
plaquette

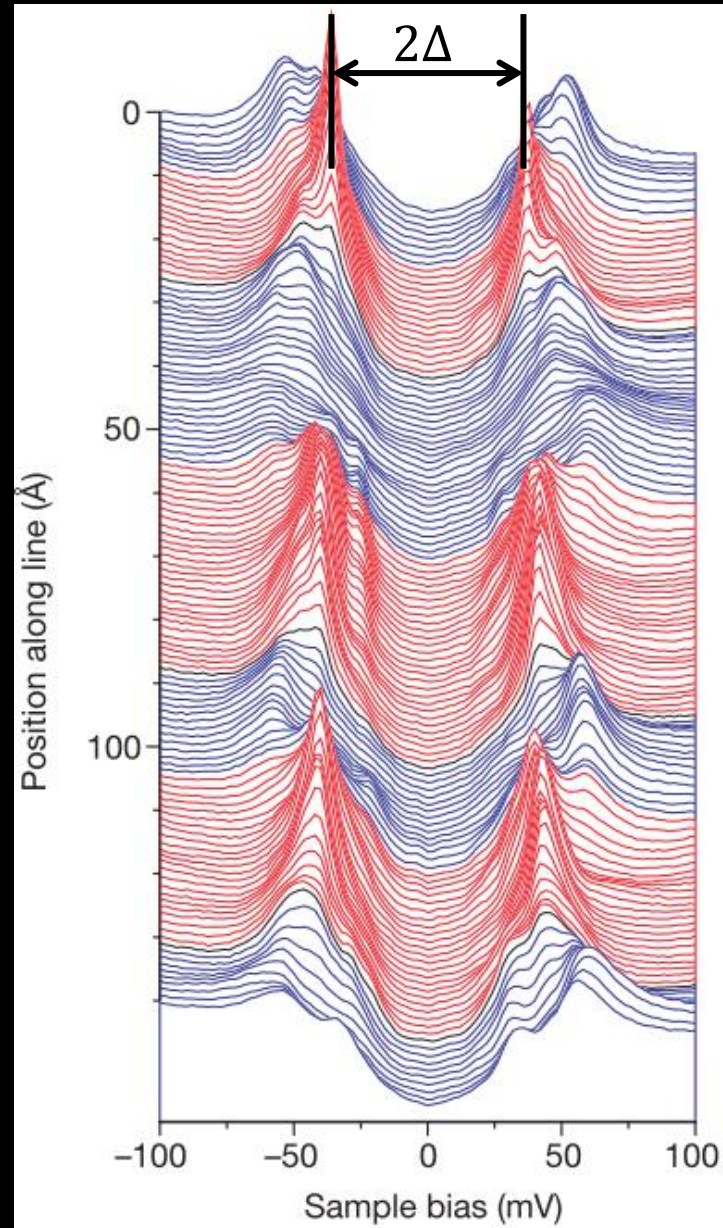
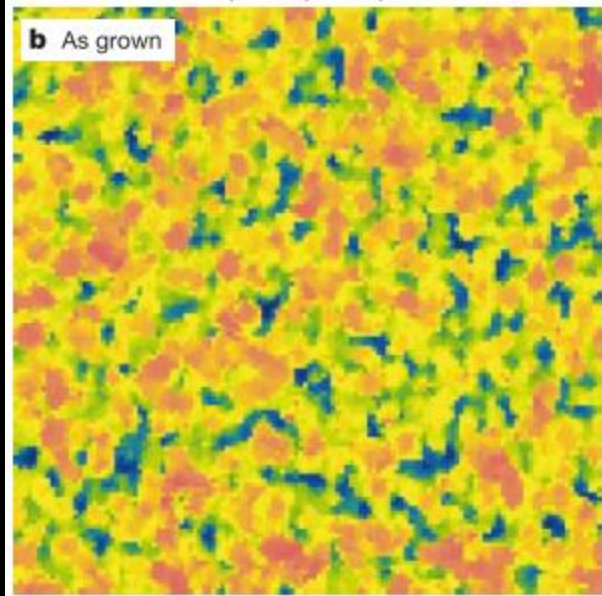
Cleave Here
Reveals
BiO Surface



Δ inhomogeneity in BSCCO

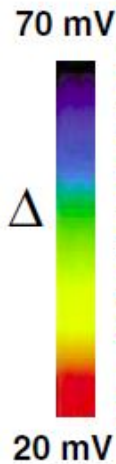
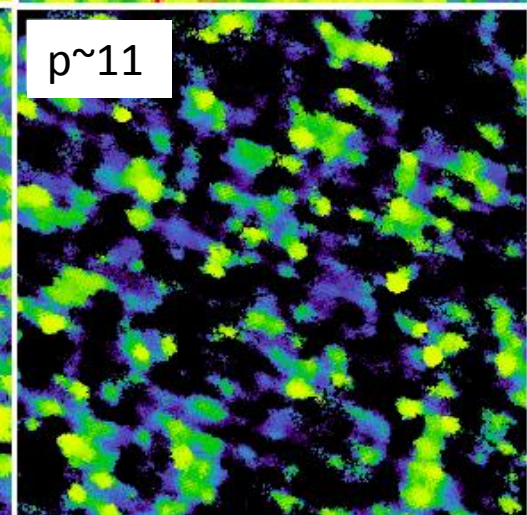
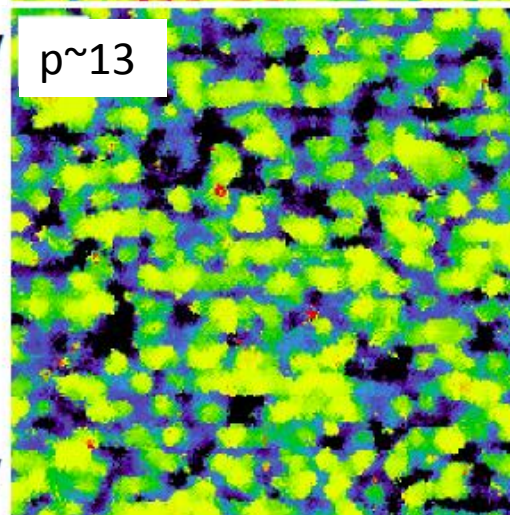
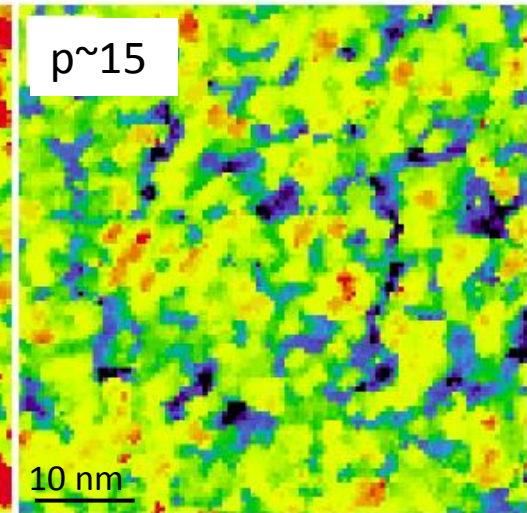
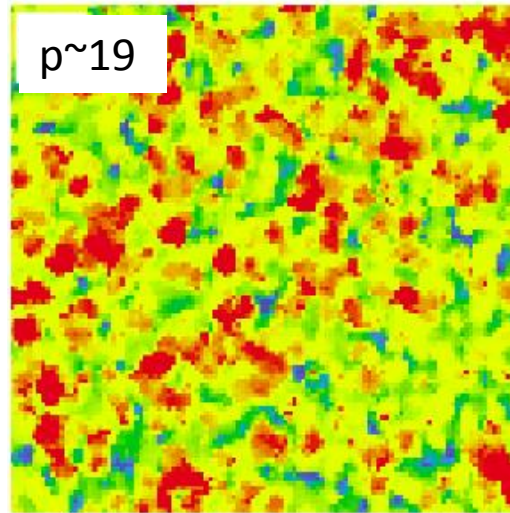
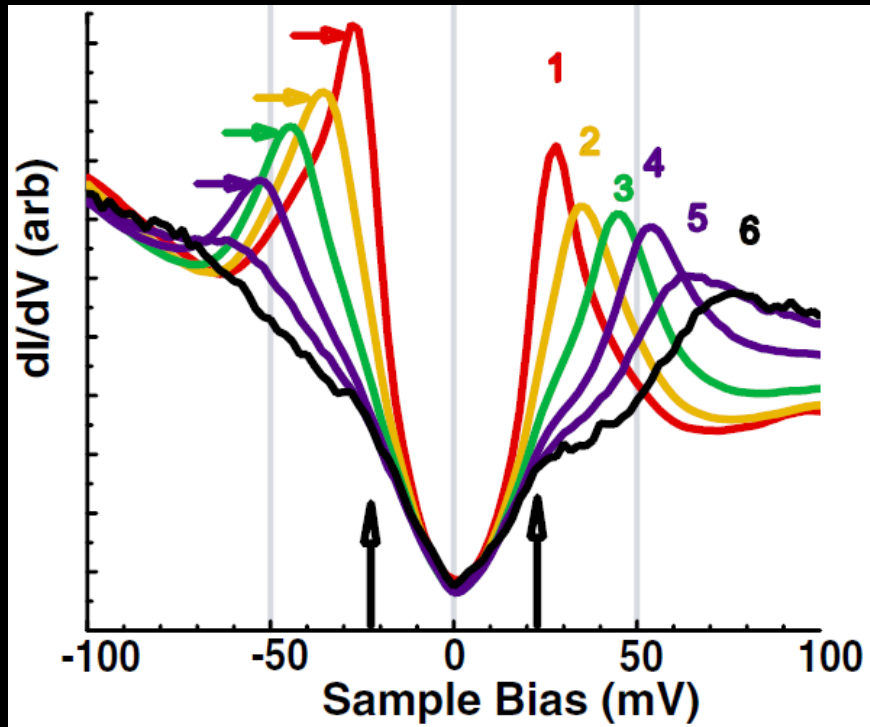


← Δ



Suggests the existence of a local "hidden" variable we could use to control Δ ? (and raise T_c ?)

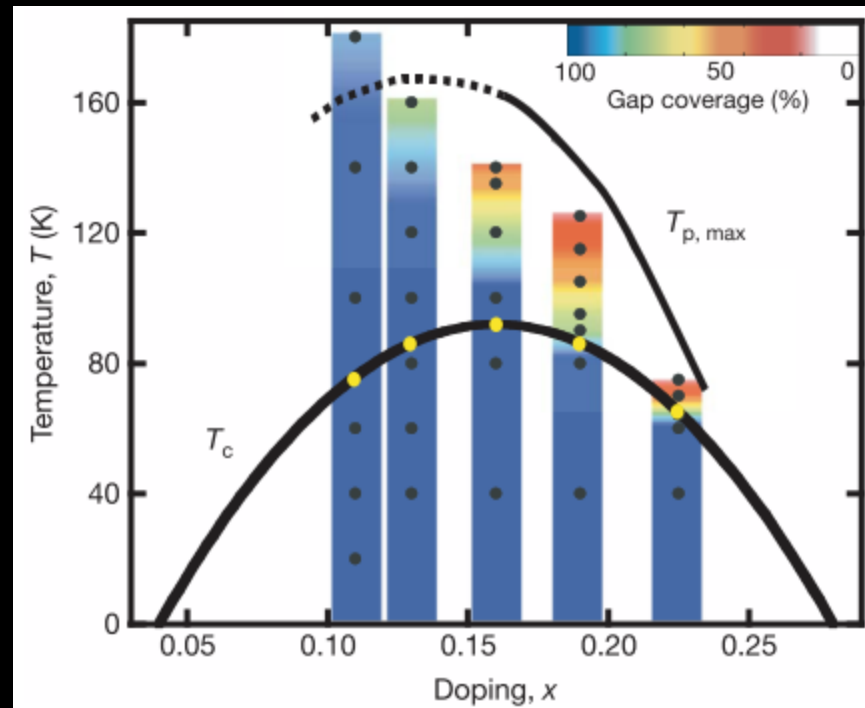
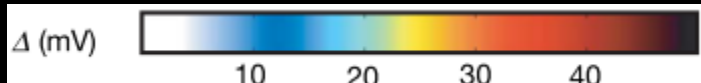
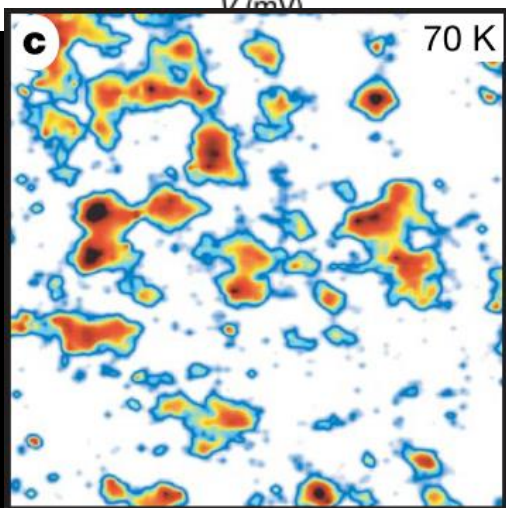
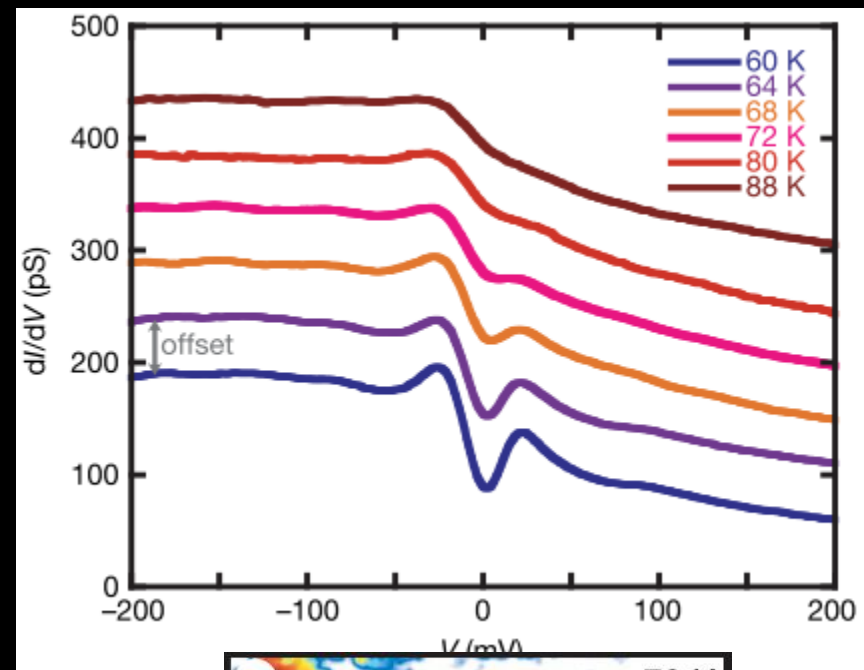
Δ inhomogeneity in BSCCO



Inhomogeneity of $T(\Delta$ closure) in BSCCO



$T_c=65\text{K}$ (overdoped)



Are oxygen dopants causing inhomogeneity?



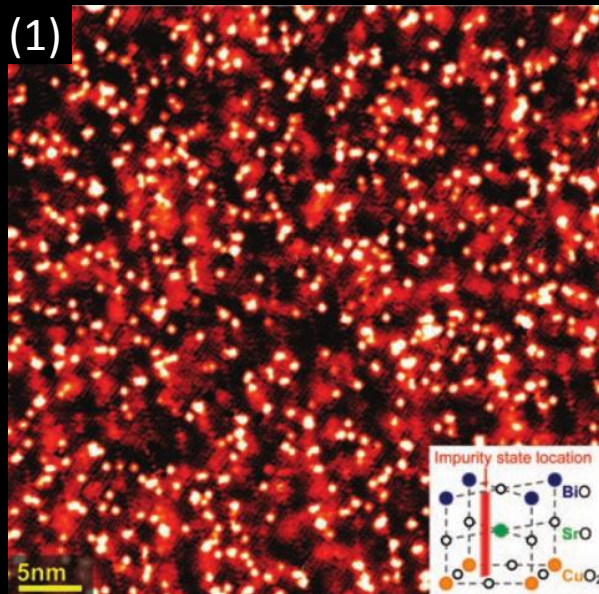
Conclusions about interstitial oxygen:

(1) Observed at -0.96 V in dI/dV

(2) “Strong correlations” exist between these oxygen dopants and “the gap”

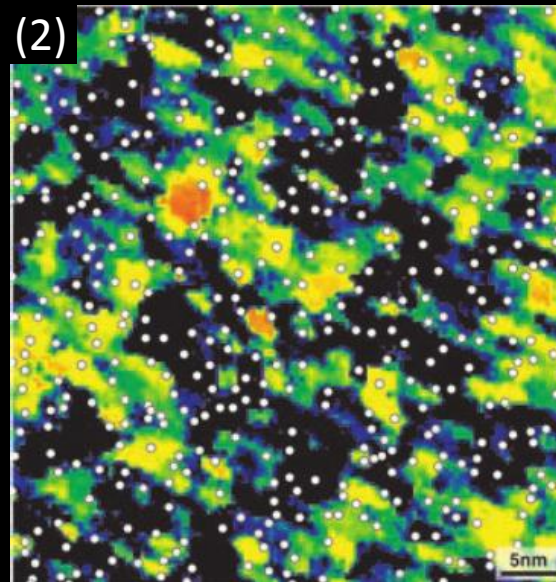
(3) These oxygen dopants are primarily positioned in the minima of the “QPI”

dI/dV at -1 V



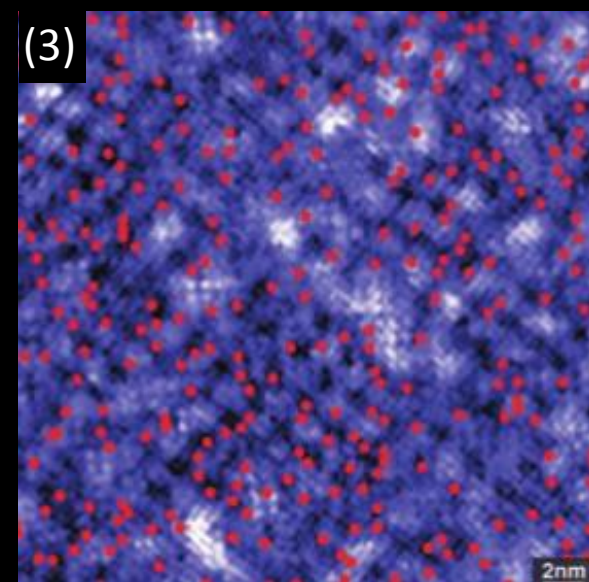
0.4 nS 0.7 nS

gapmap



20 meV 70 meV

dI/dV at -24 mV



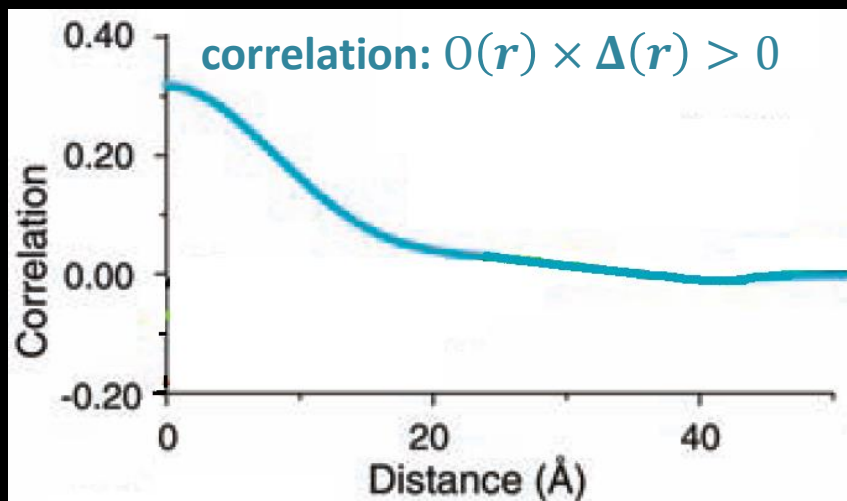
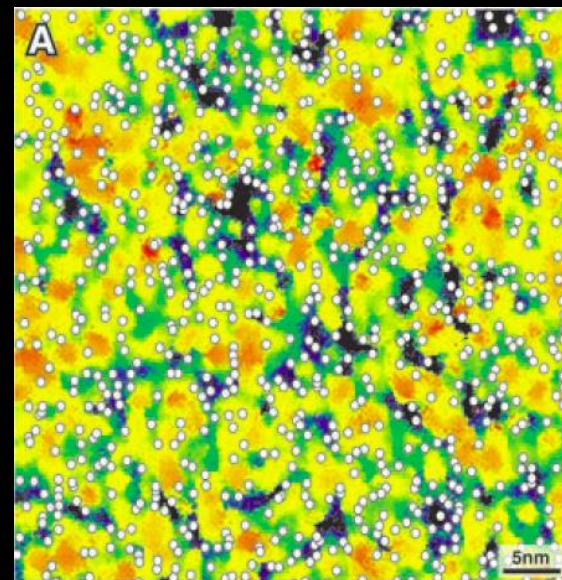
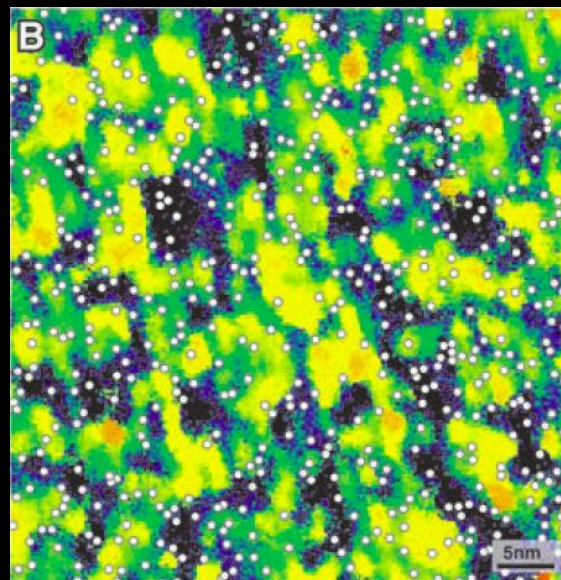
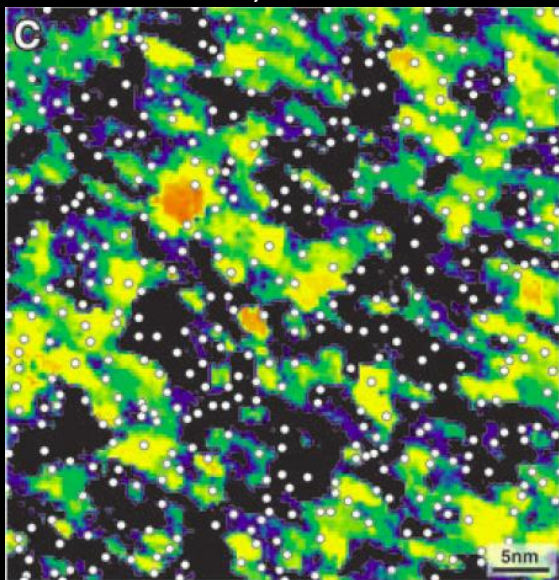
Puzzle: local trend opposes global trend



$\bar{\Delta} = 65$ meV; N=455

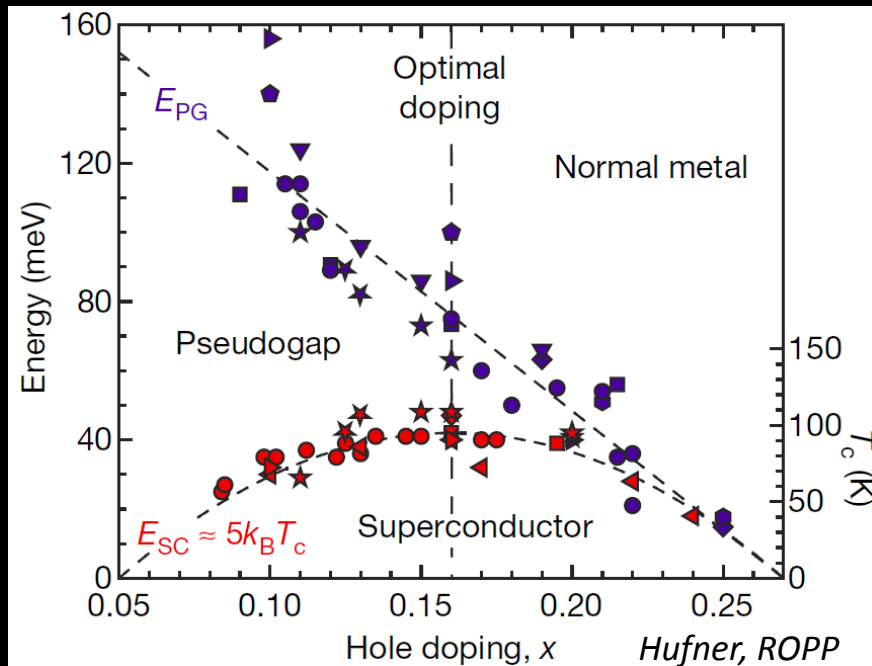
$\bar{\Delta} = 55$ meV; N=580

$\bar{\Delta} = 45$ meV; N=883



McElroy, Science 309, 1048 (2005)

→ Assumption: oxygen dopants **cause** local regions of large Δ

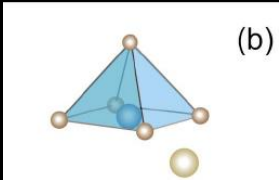


Hufner, ROPP

Zhou prediction: type-A oxygen

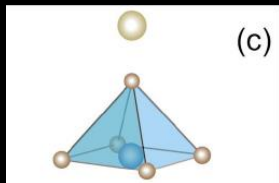


B-site disorder:
(e.g. Pb^{2+} on Bi^{3+} site
or Y^{3+} on Ca^{2+} site)
does not couple to CuO_2



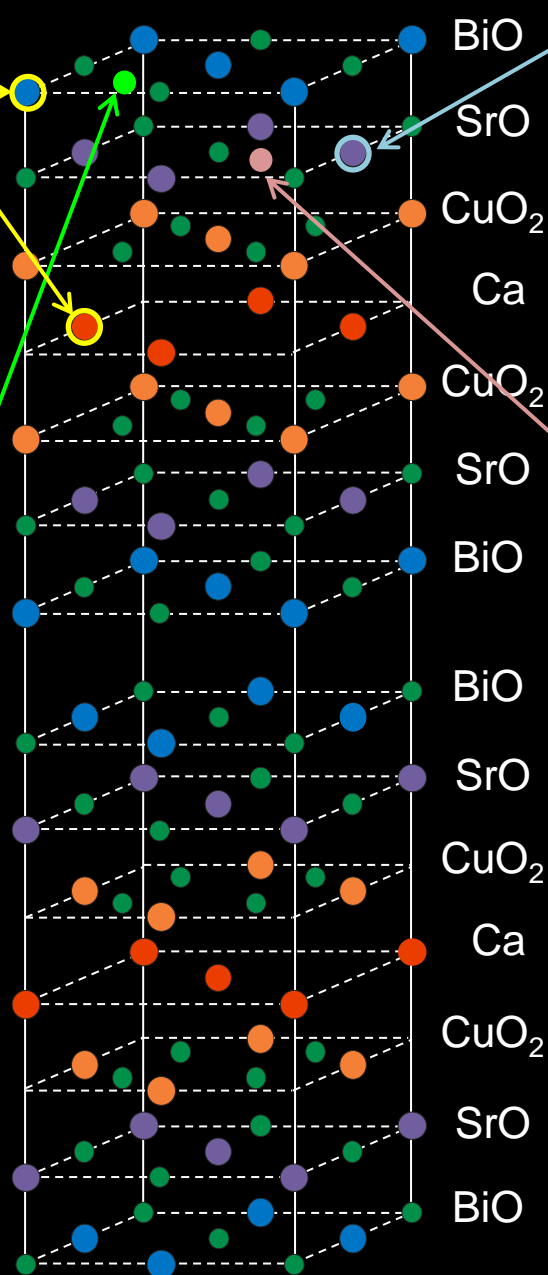
Eisaki, PRB 69, 064512 (2004)

interstitial O in BiO plane
weakly couples to CuO_2
provides charge carriers
but little local effect
→ “type-B oxygen”

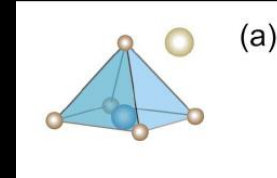


seen at **-0.96V**

McElroy, Science 309, 1048 (2005)

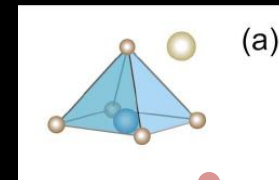


A-site disorder:
(Bi^{3+} on Sr^{2+} site)
strongly couples to apical O



claim: seen at **+1.8V**
Kinoda, PRB 67, 224509 (2003)

interstitial O in SrO plane
strongly couples to CuO_2
provides charge carriers
and disorder
→ “type-A oxygen”



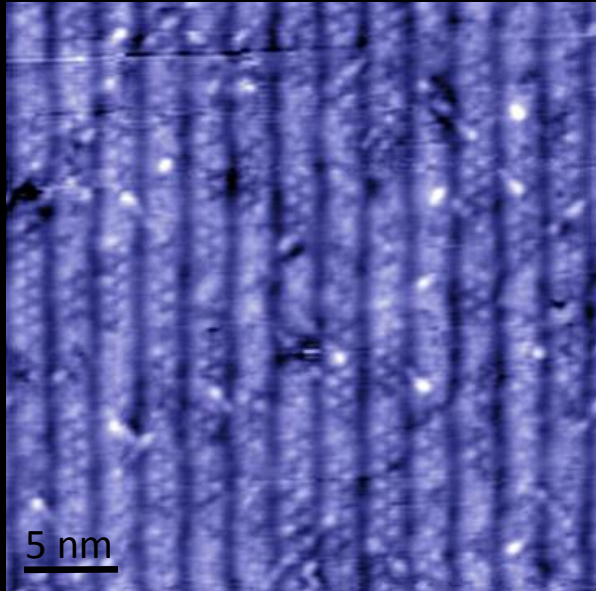
Zhou, PRL 98, 076401 (2007)

expected **<< -1V**

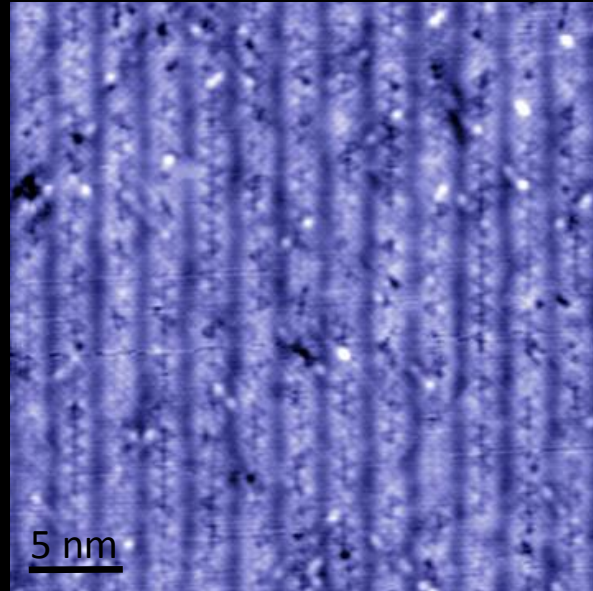
Mapping additional dopants ($T_c=55\text{K}$)



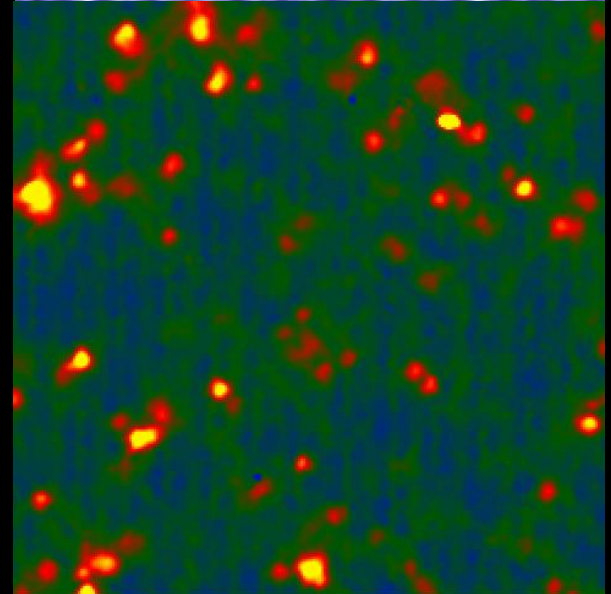
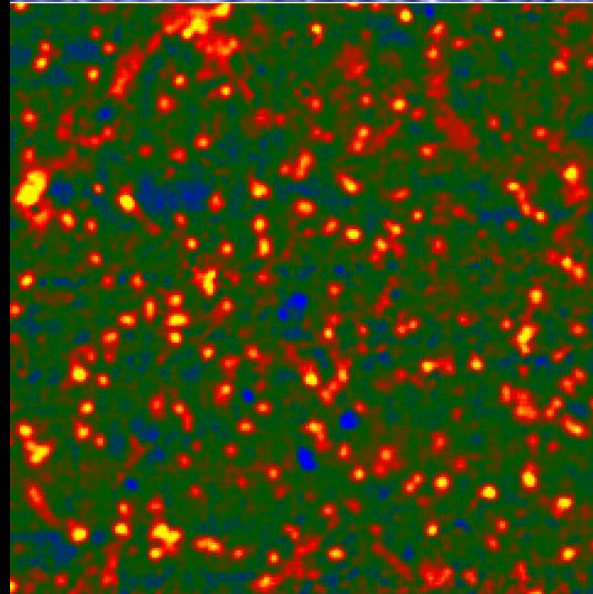
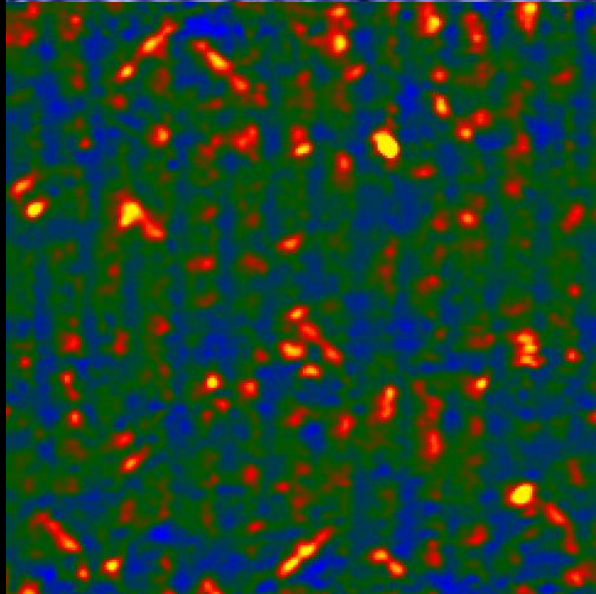
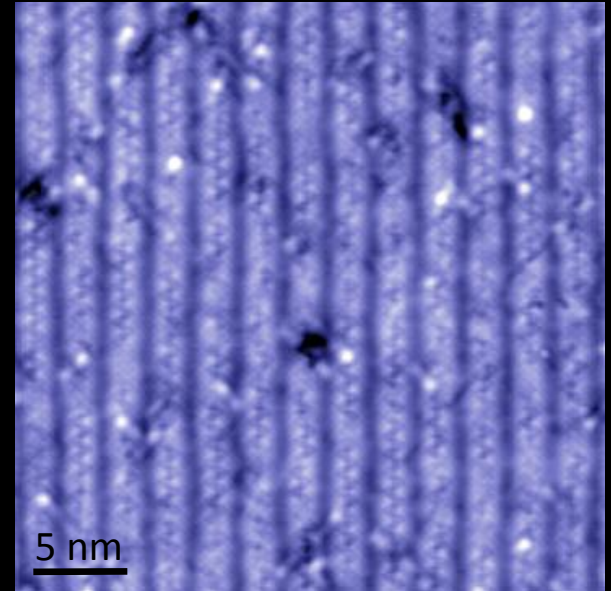
-1.5V, type-A Oxygen



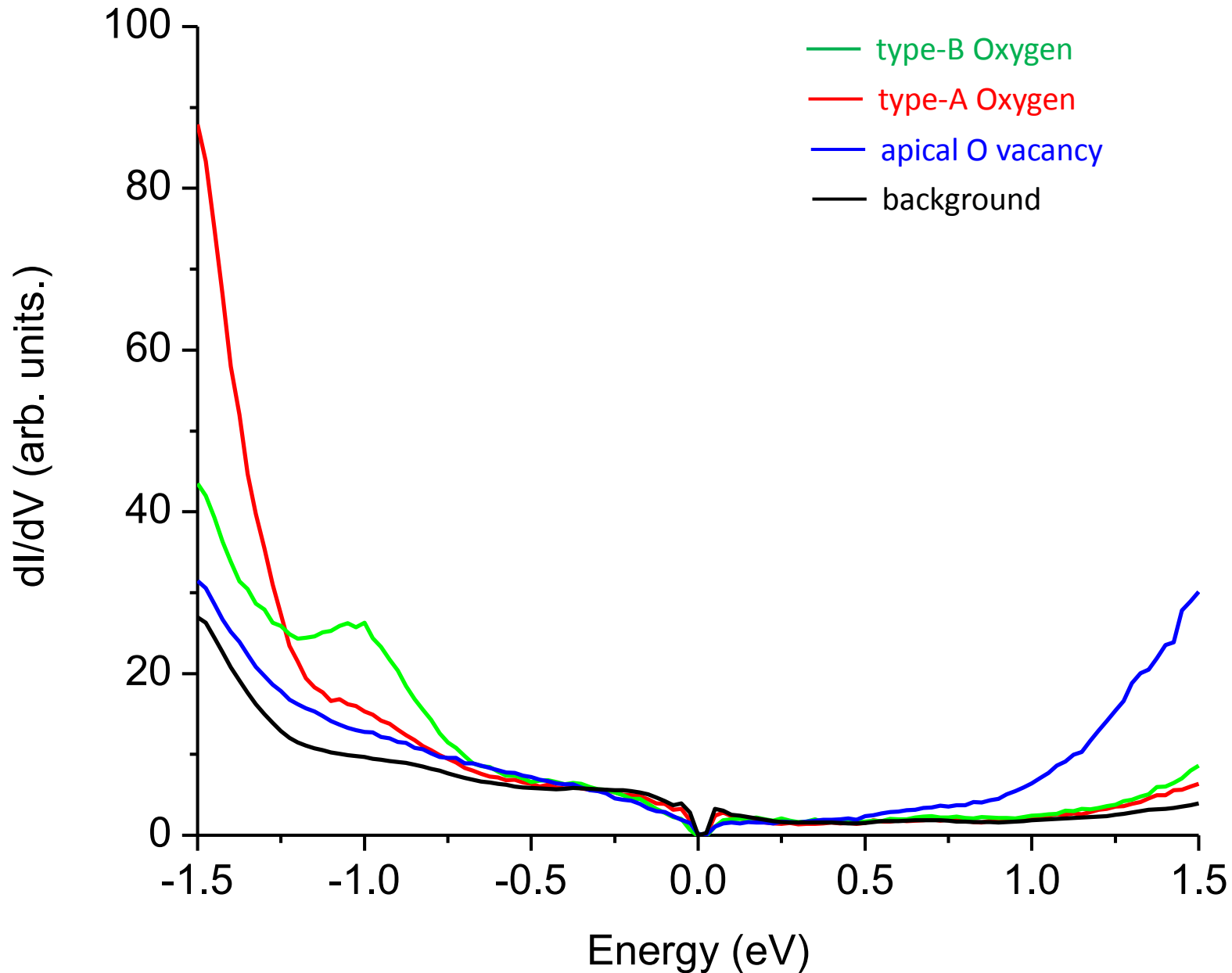
-1V, type-B Oxygen



+1V, unknown ???



Spectral signatures ($T_c=82\text{K}$)

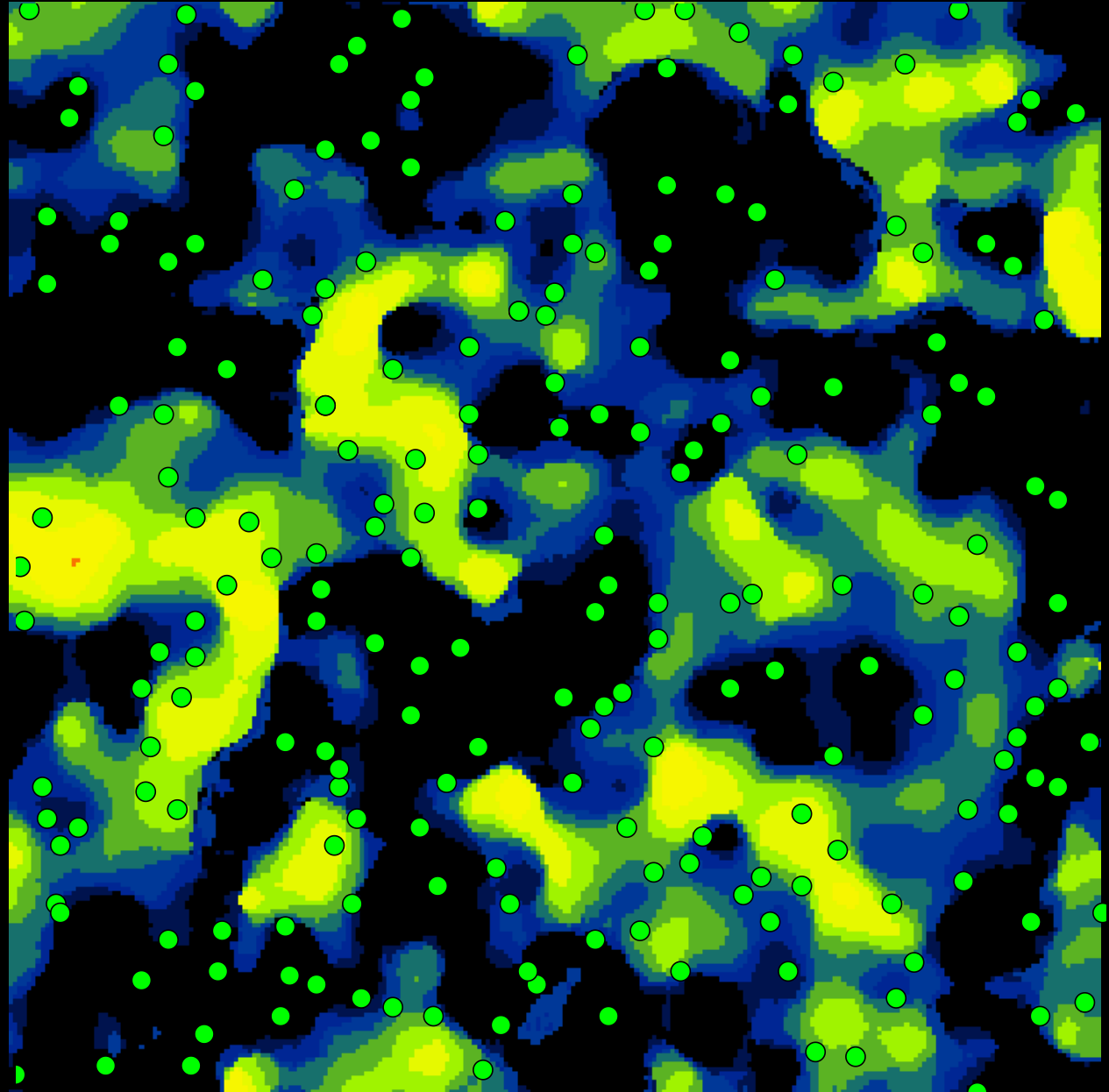
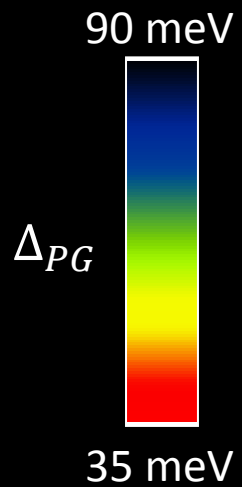


$T_c = 55\text{K}$



● O, type-B

expect $O_B(r) \times \Delta(r) > 0$
(correlation)



29 x 29 nm²

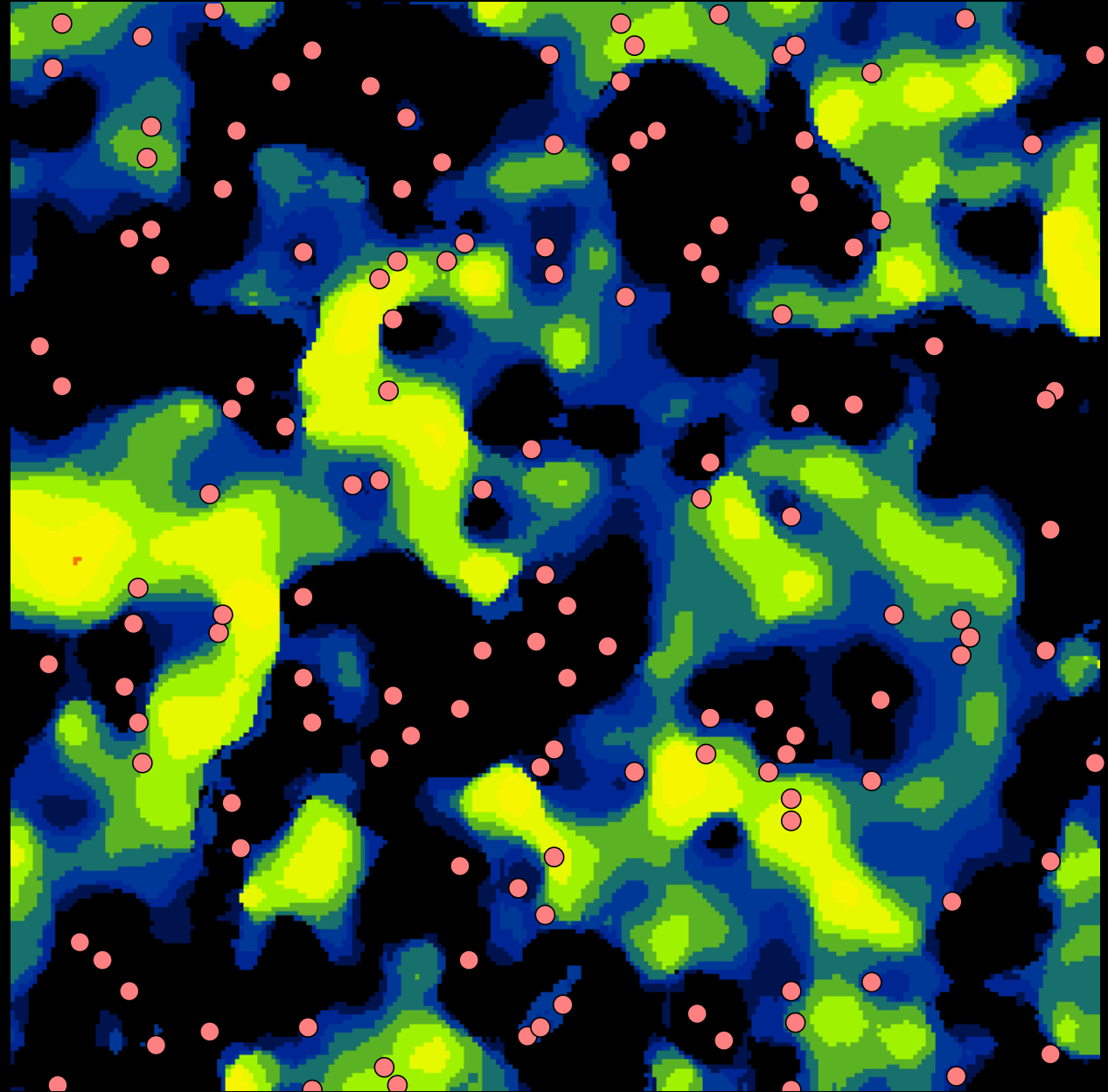
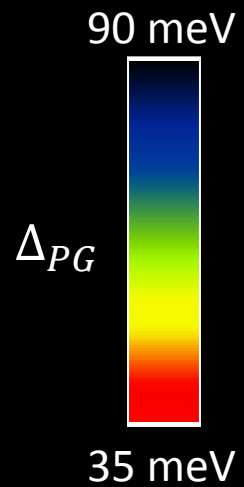
$T_c = 55K$



● O, type-A

expect $O_A(r) \times \Delta(r) < 0$
(causality)

→ NOT OBSERVED

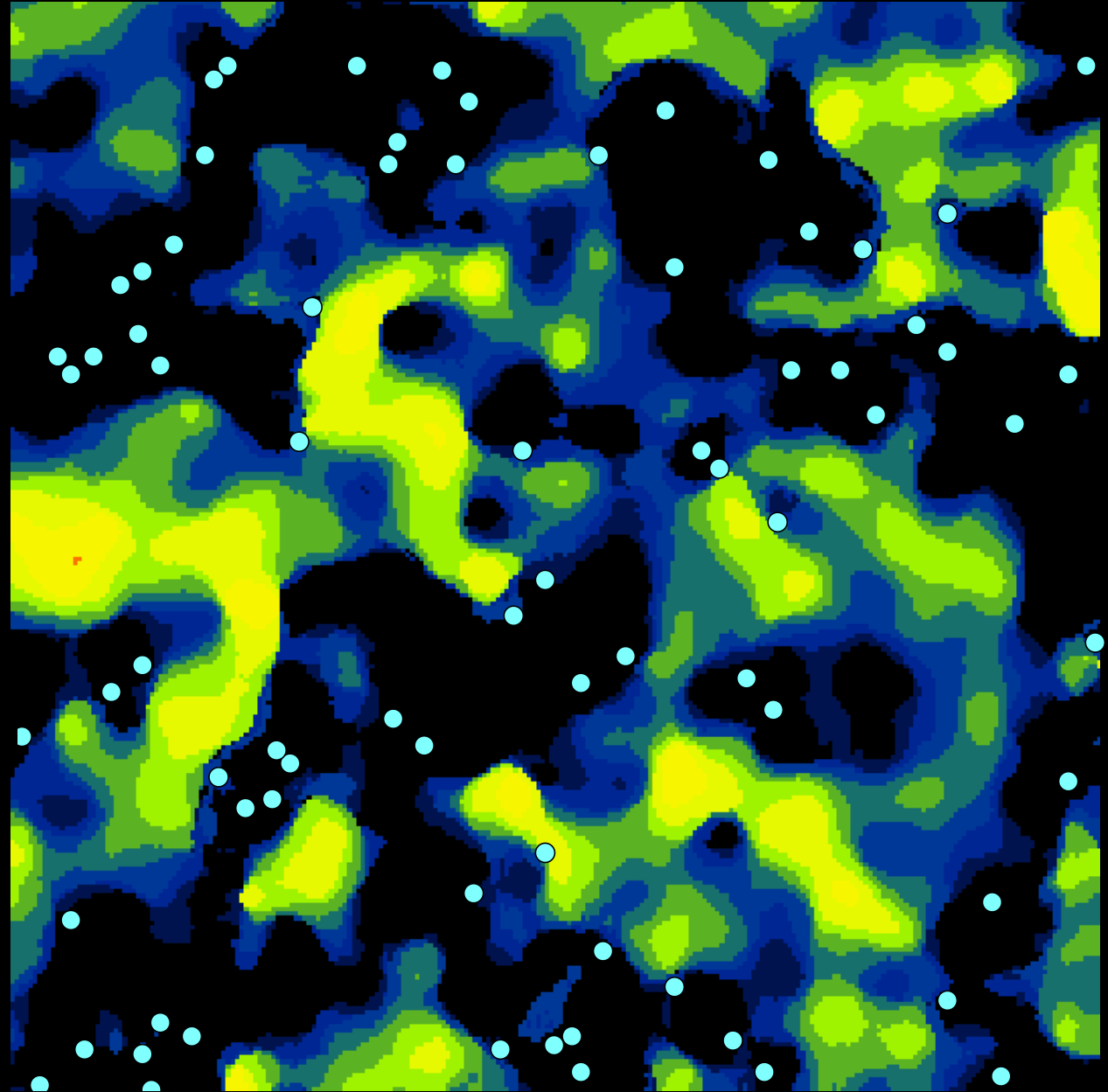
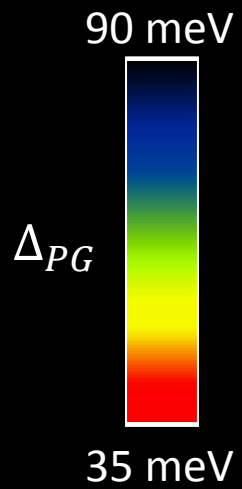


29 x 29 nm²

$T_c = 55\text{K}$

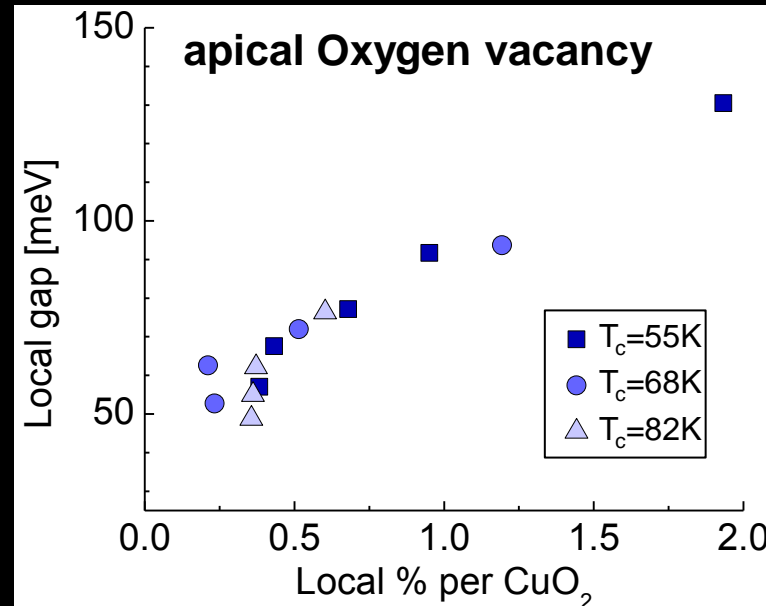
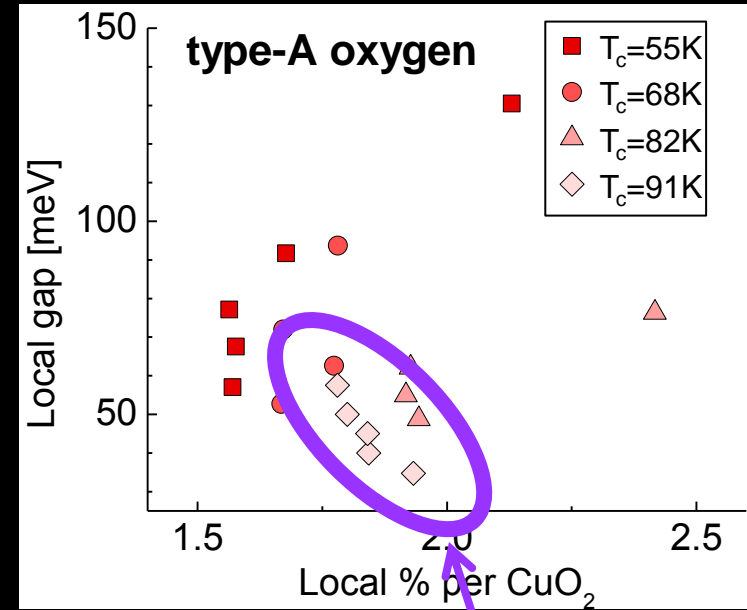
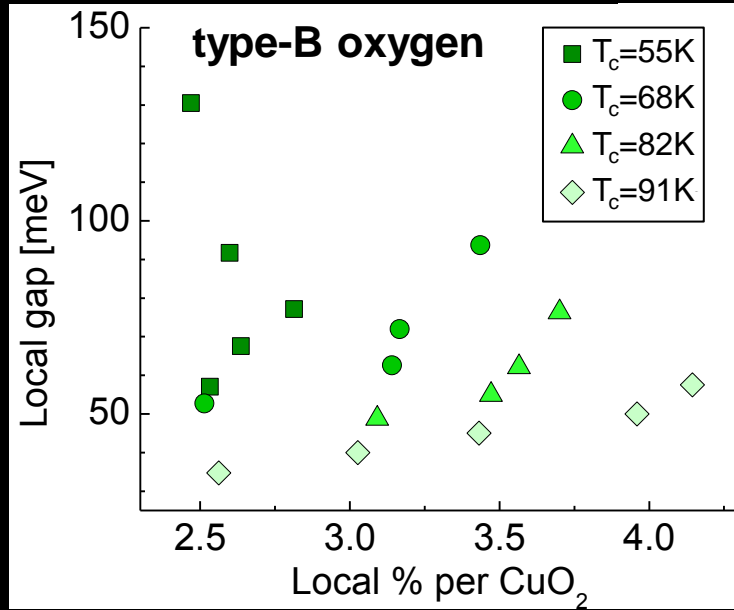


- apical O vacancy



29 x 29 nm²

Resolved! local vs. global dependence

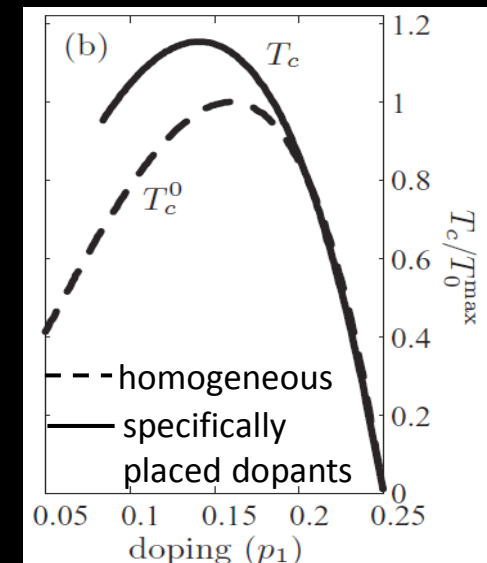
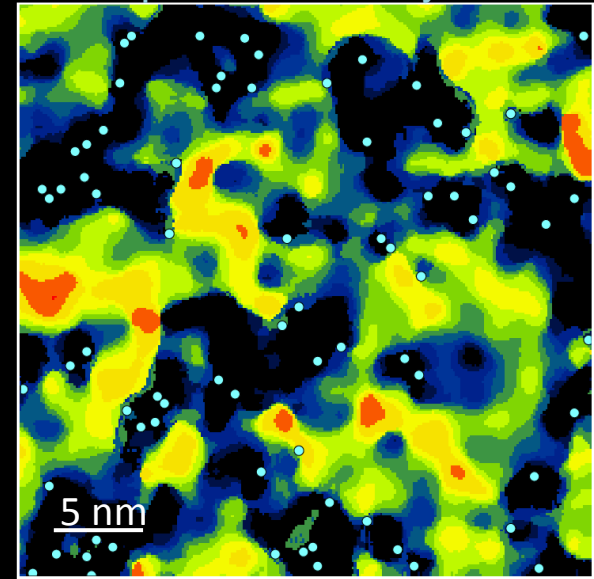


Optimal doping:
no apical O vacancies
→ local charge controlled
by type-A interstitial O

Part I: Conclusions

- Doubled the energy range for local spectroscopy on BSCCO
- Found all oxygen dopants: type-A & B oxygen, apical O vacancies
- apical O vacancies
 - strongly enhance the gap energy
 -
- * type-A oxygens
 - attracted to apical O vacancies in UD
 - control local charge in OPT
- type-B oxygens
 - weakly correlate, secondary effect

• apical O vacancy



Next steps:

- control dopants to raise T_c ??
- fit to find effective charge & radius of dopants
- understand how dopants affect CDW

Superconductivity Tunneling Milestones



1960: gap measurement (Pb)

1965: boson energies & coupling (Pb)

1985: charge density wave (TaSe_2)

1989: vortex lattice (NbSe_2)

1997: single atom impurities (Nb)

2002: quasiparticle interference

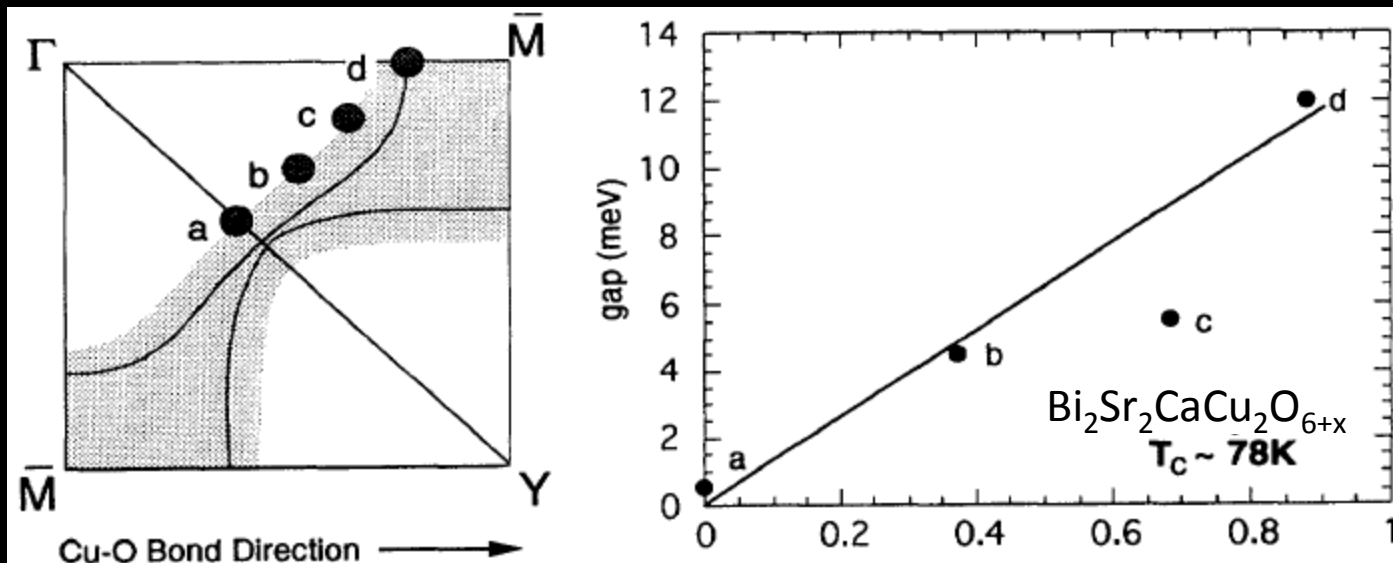
→ band structure & gap symmetry (BSCCO)

2009: phase-sensitive gap measurement (Na-CCOC)

2010: intra-unit-cell structure (BSCCO)

Anomalous Large Gap Anisotropy in the a - b Plane of $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$

Z.-X. Shen,^{(1),(2)} **D. S. Dessau**,^{(1),(2)} B. O. Wells,^{(1),(2),(a)} D. M. King,⁽²⁾ W. E. Spicer,⁽²⁾ A. J. Arko,⁽³⁾
 D. Marshall,⁽²⁾ L. W. Lombardo,⁽¹⁾ A. Kapitulnik,⁽¹⁾ P. Dickinson,⁽¹⁾ S. Doniach,⁽¹⁾ J. DiCarlo,^{(1),(2)}
 A. G. Loeser,^{(1),(2)} and C. H. Park^{(1),(2)}



Questions

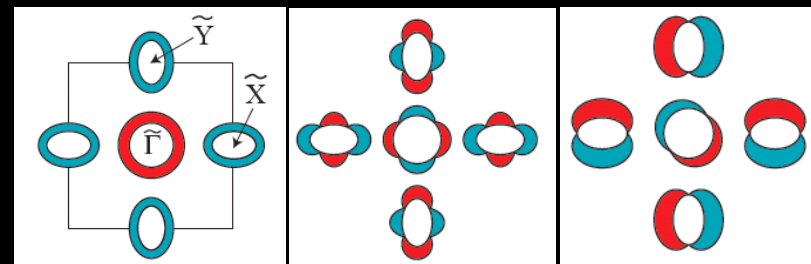
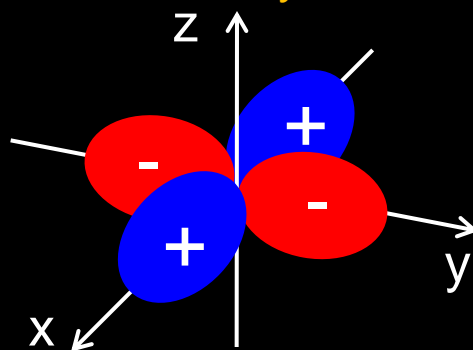
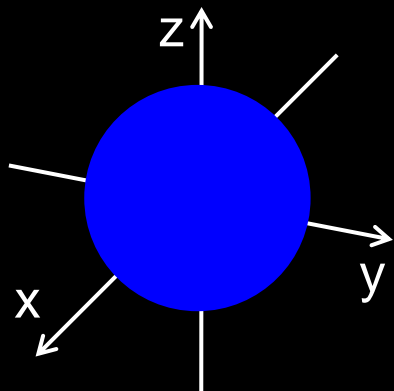


1. What is the pairing symmetry of a superconductor?

Conventional: s-wave

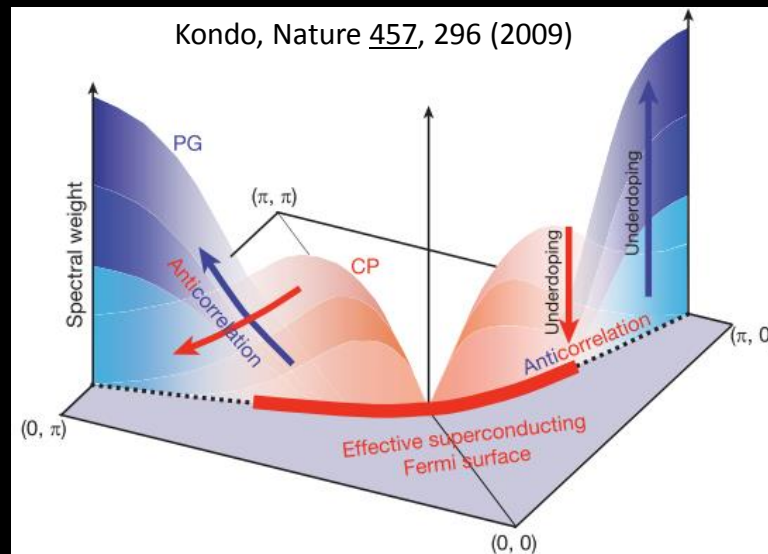
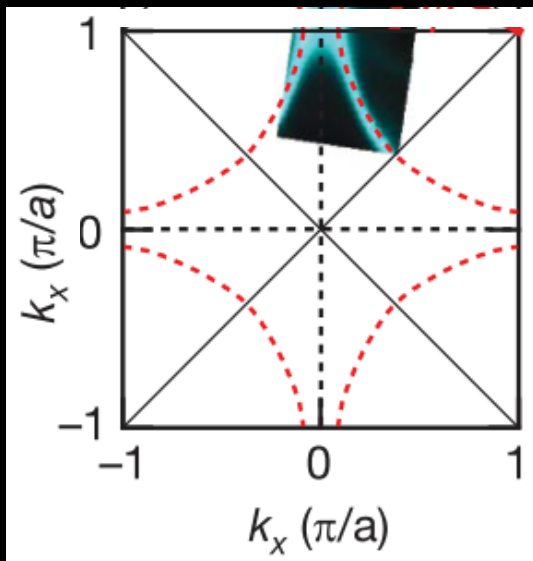
Cuprate: $d_{x^2-y^2}$ wave

Iron: s? d? p?



Hicks, JPSJ 78, 013708 (2009)

2. Where on the Fermi surface does the pairing occur?



How can disorder help us?



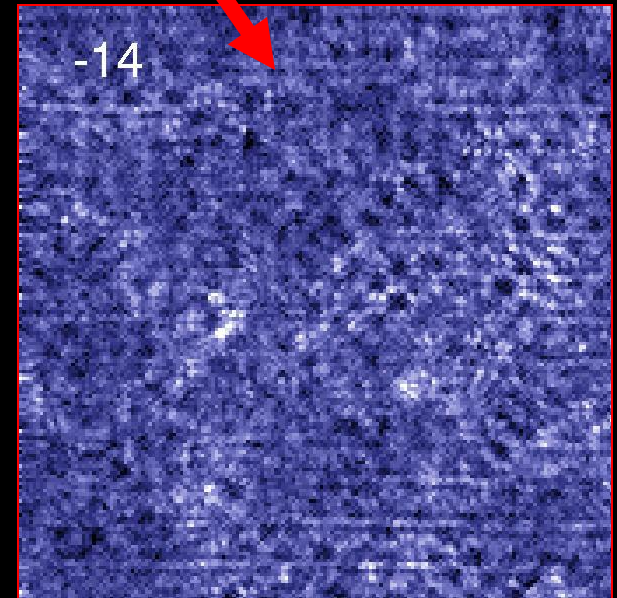
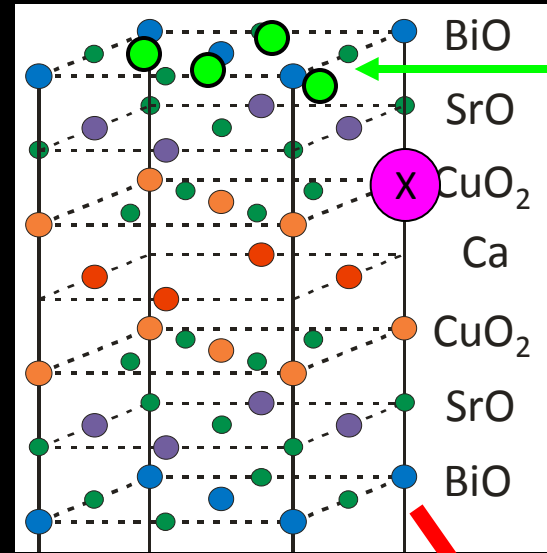
H₂O

ME
(experimentalist)



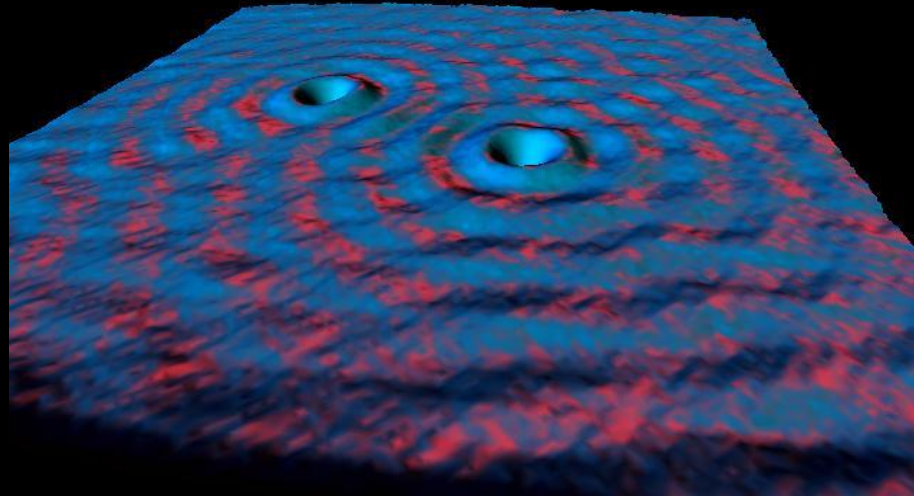
perturbation

interference
patterns



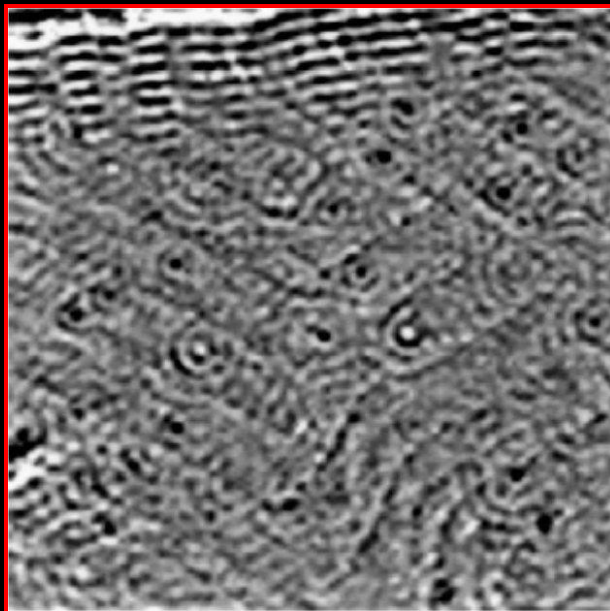
-14

First QPI: metals, real space

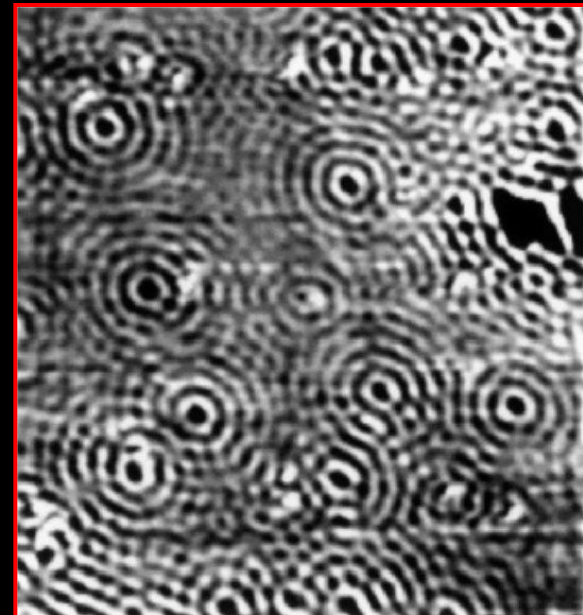


Crommie, Lutz & Eigler, *Nature* 363, 524 (1993)

Au:



Cu:



Peterson, Hofmann, Plummer & Besenbacher, *J. Electron Spectroscopy* 109, 97 (2000)

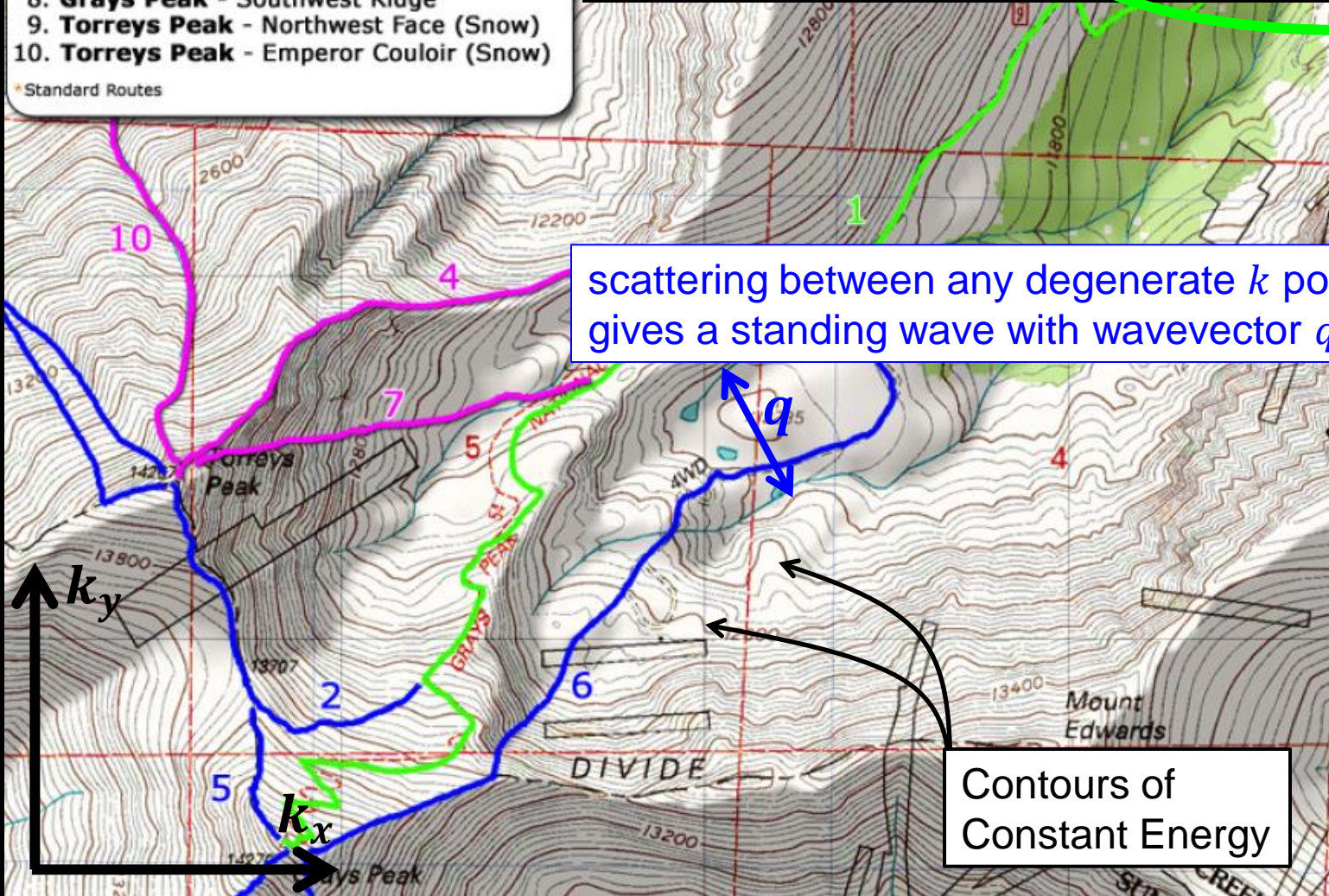
2-dim band structure: topographic map for e^-



- 1. Grays Peak - East Slopes
 - 2. Torreys Peak - South Slopes
 - 3. Grays Peak - South Ridge
 - 4. Torreys Peak - Kelso Ridge
 - 5. **Combination - Grays + Torreys**
 - 6. Grays Peak - Lost Rat Couloir (Snow)
 - 7. Torreys Peak - Dead Dog Couloir (Snow)
 - 8. Grays Peak - Southwest Ridge
 - 9. Torreys Peak - Northwest Face (Snow)
 - 10. Torreys Peak - Emperor Couloir (Snow)
- Standard Routes

Power spectrum of scattering:

$$P(\epsilon, \vec{q}) \propto |V(\vec{q})|^2 n_i(\epsilon_i, \vec{k}_i) n_f(\epsilon_f, \vec{k}_f)$$



scattering between any degenerate k points gives a standing wave with wavevector q

Contours of Constant Energy

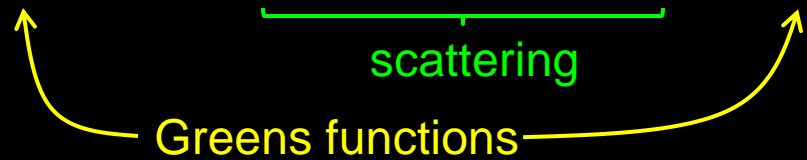
The real theory...



Density of states:

$$n(\mathbf{q}, \omega) = n_0(\mathbf{q}, \omega) - \frac{1}{2\pi i} [A_{11}(\mathbf{q}, \omega) + A_{22}(\mathbf{q}, -\omega) - A_{11}^*(-\mathbf{q}, \omega) - A_{22}^*(-\mathbf{q}, -\omega)]$$

$$A(\mathbf{q}, \omega) = \int \frac{d^2k}{(2\pi)^2} G_0(\mathbf{k} + \mathbf{q}, \omega) \underbrace{T(\mathbf{k} + \mathbf{q}, \mathbf{k}; \omega)}_{\text{scattering}} G_0(\mathbf{k}, \omega)$$



→ There will be cross terms.

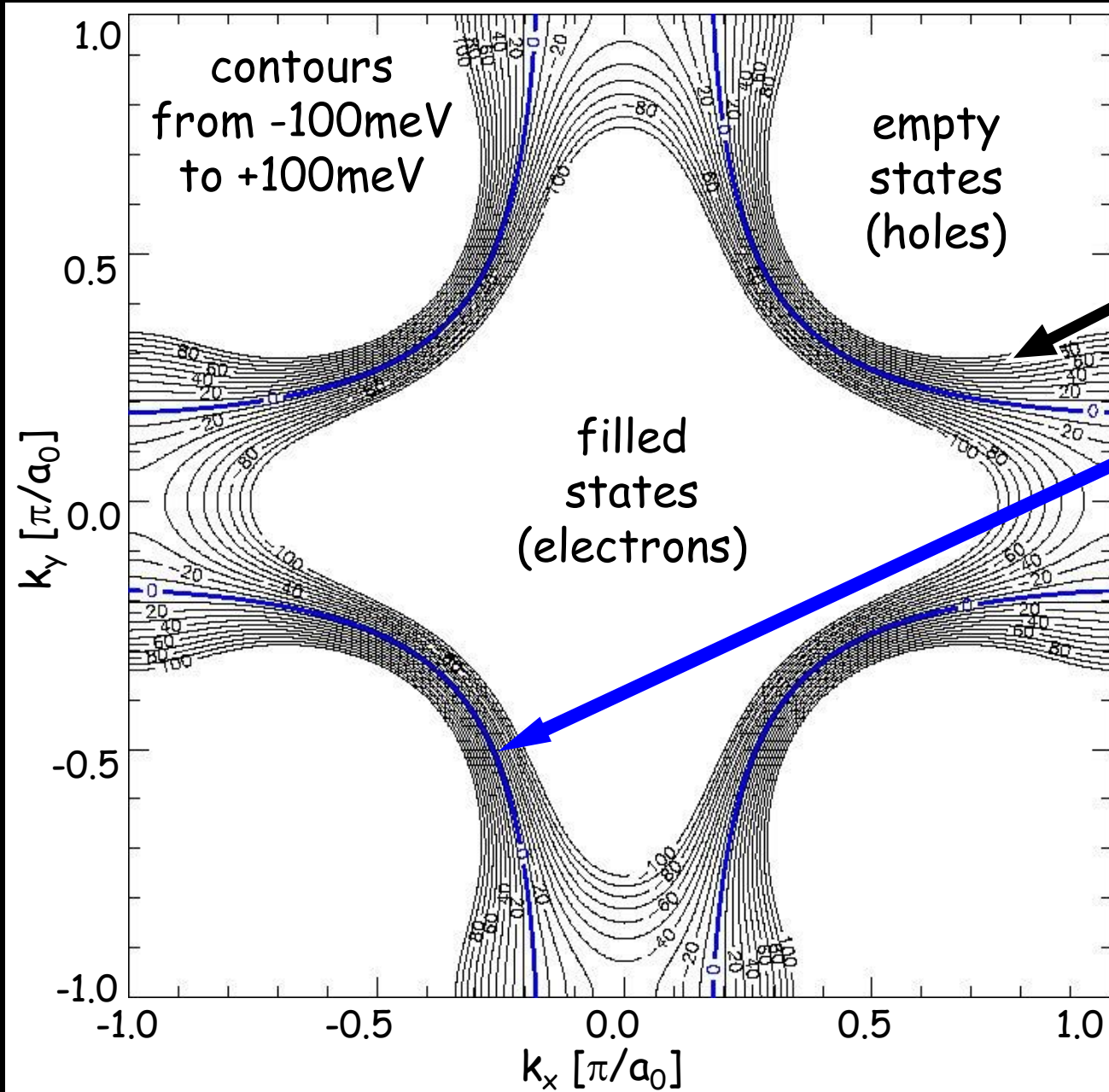
Wang & Lee, PRB 67, 020511 (2003)

But empirically, simple real model is a good approximation to the data:

$$P(\varepsilon, \vec{q}) \propto |V(\vec{q})|^2 n_i(\varepsilon_i, \vec{k}_i) n_f(\varepsilon_f, \vec{k}_f)$$

McElroy, PRL 96, 067005 (2006)

ARPES: Normal State Fermi Surface & Band Structure



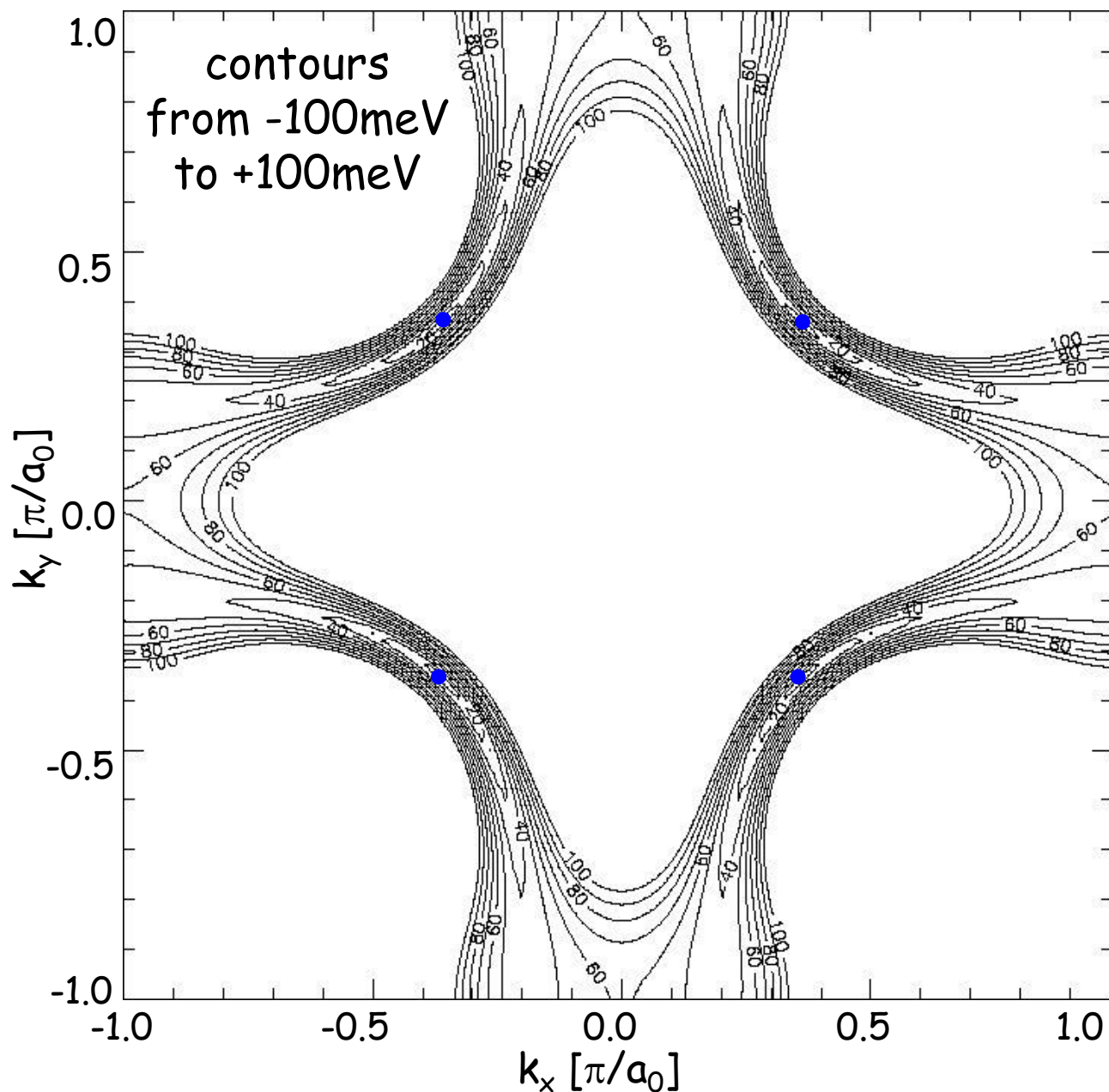
CCE (E): The location in k-space of states with energy E

Fermi Surface

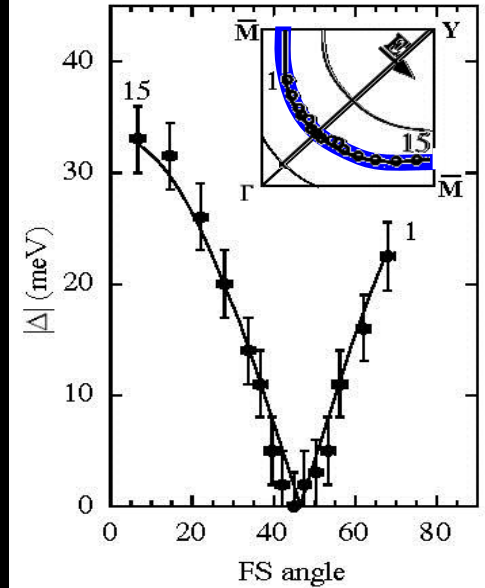
Parameterization:
M. Norman
PRB 52, 615 (1995).

Based on data:
Ding *et al.*,
PRL 74, 2784 (1995).

ARPES: Superconducting anisotropic gap $\Delta(\vec{k})$

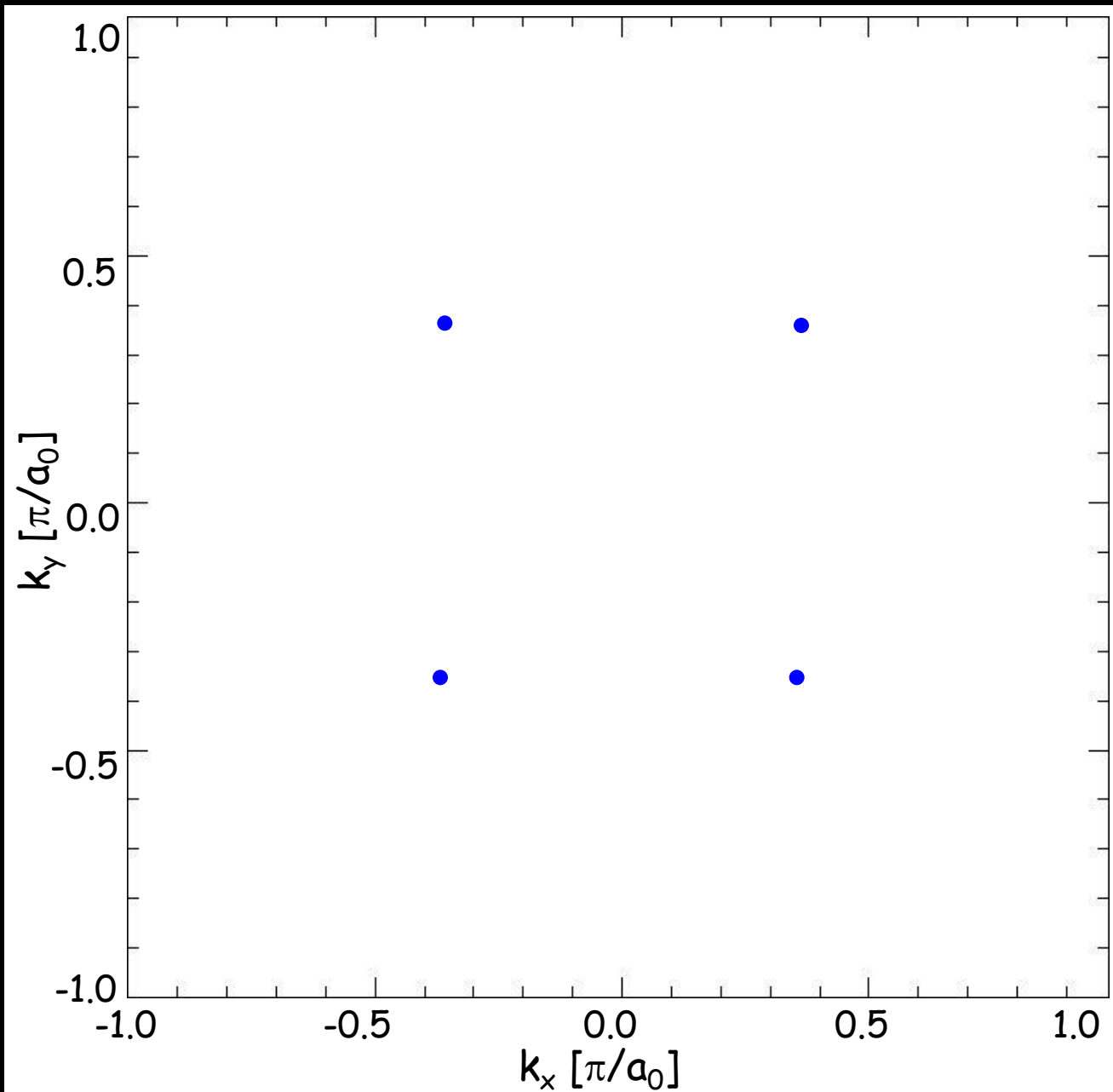


Ding *et al.*, PRL 54, 9678 (1996)

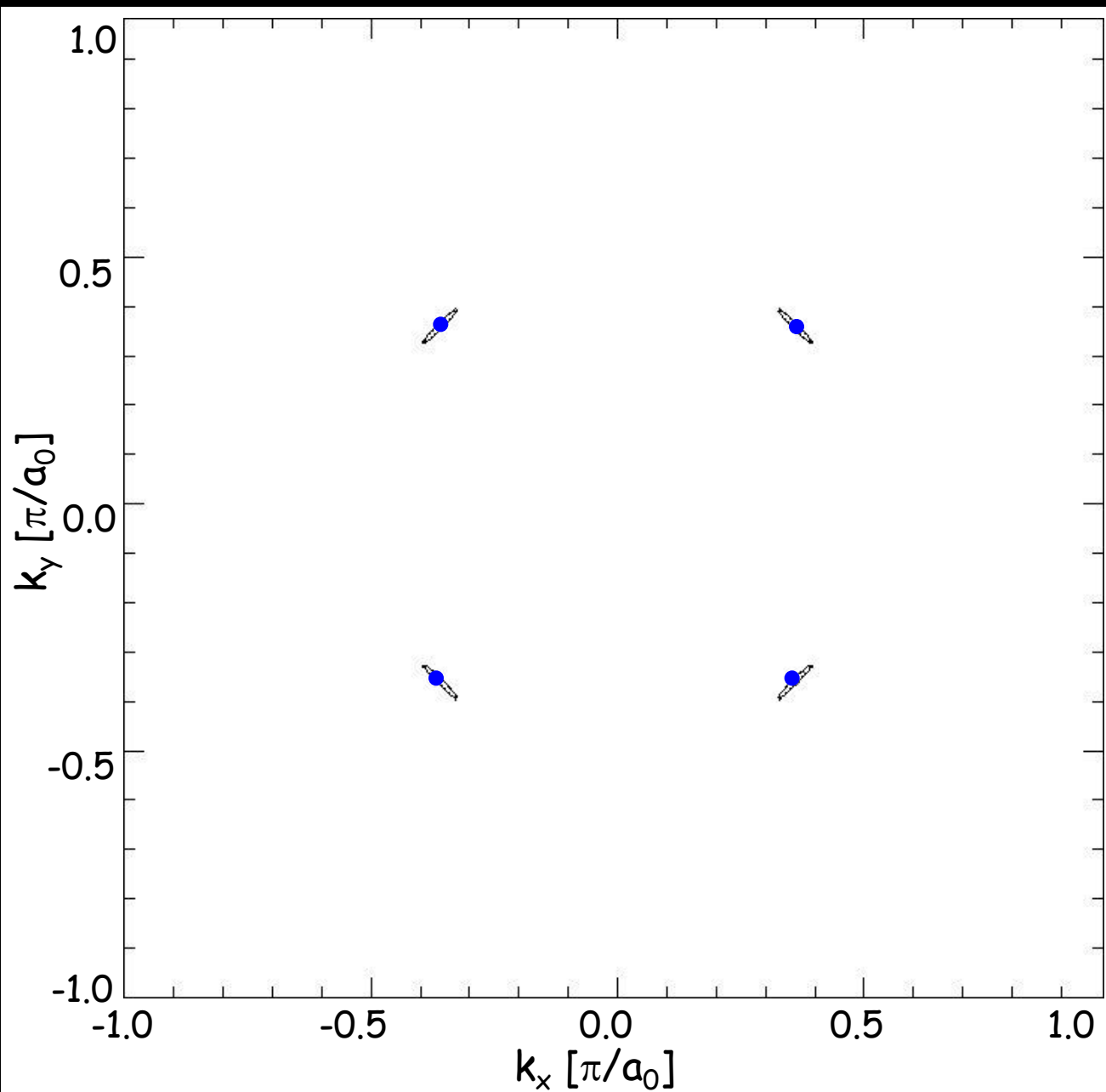


Shen *et al.*, PRL 70 1553 (1993)
Ding *et al.*, PRB 54 9678 (1996)
Mesot *et al.*, PRL 83 840 (1999)

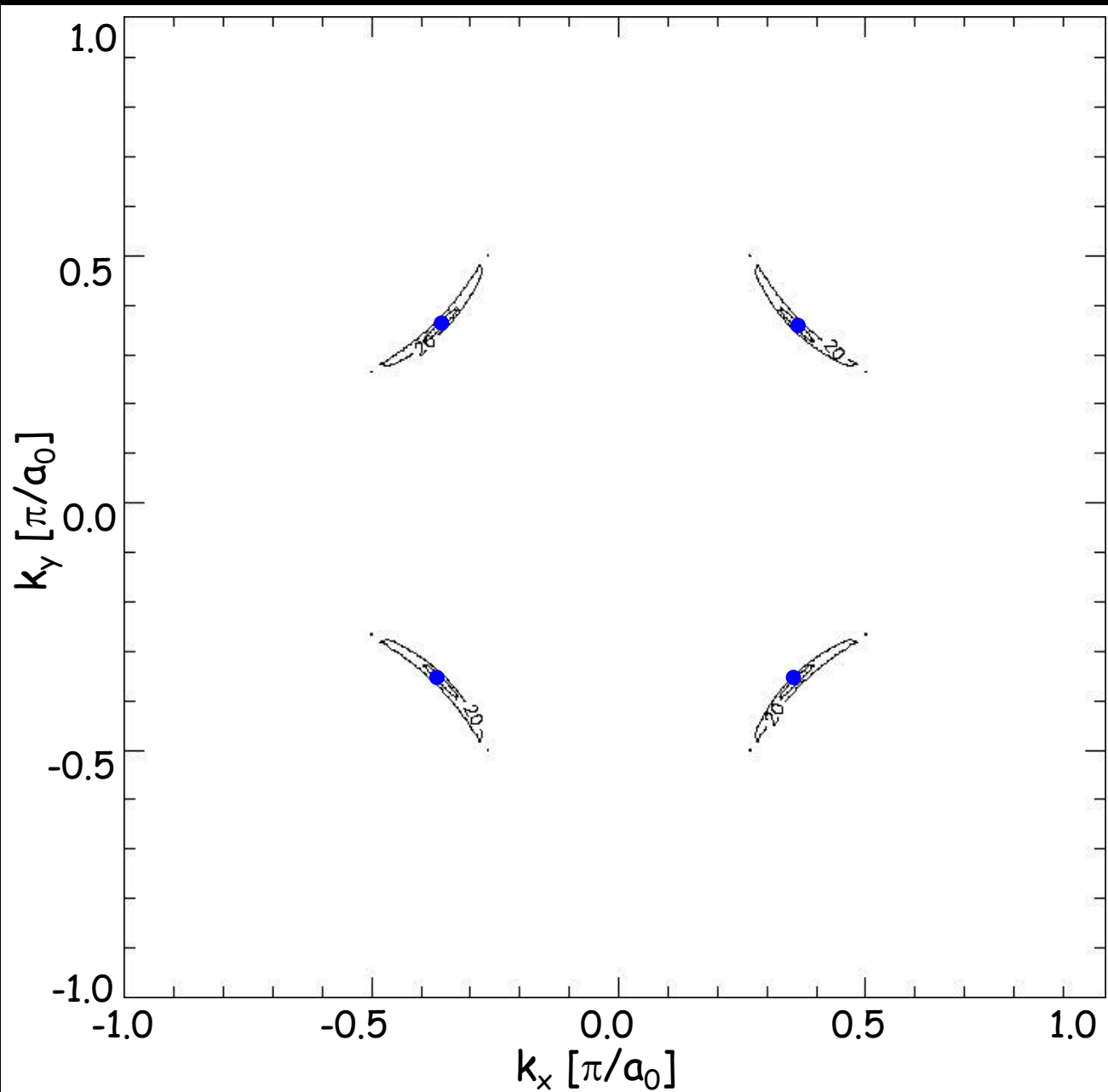
0 meV CCE: the Fermi points



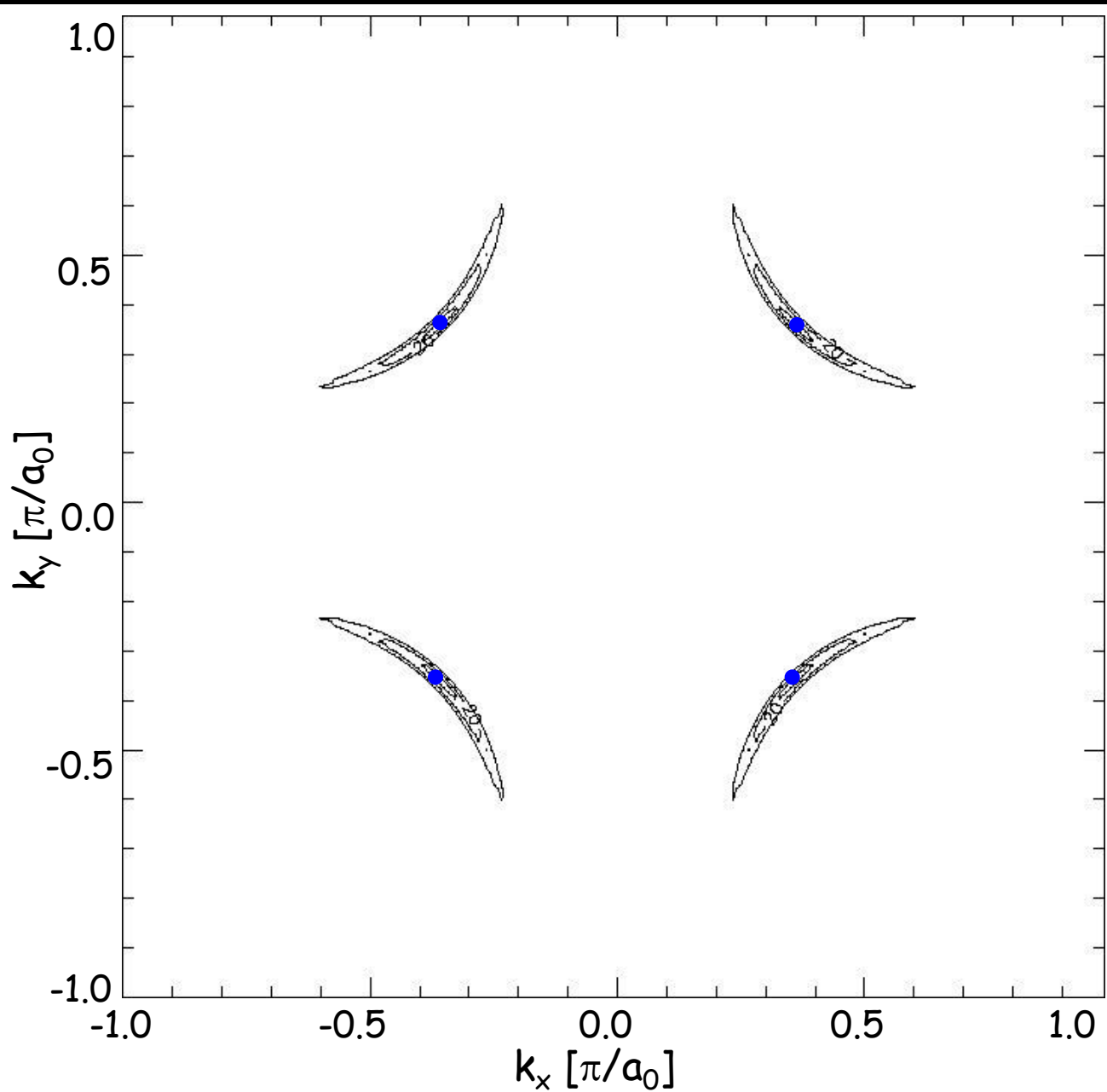
10 meV CCE



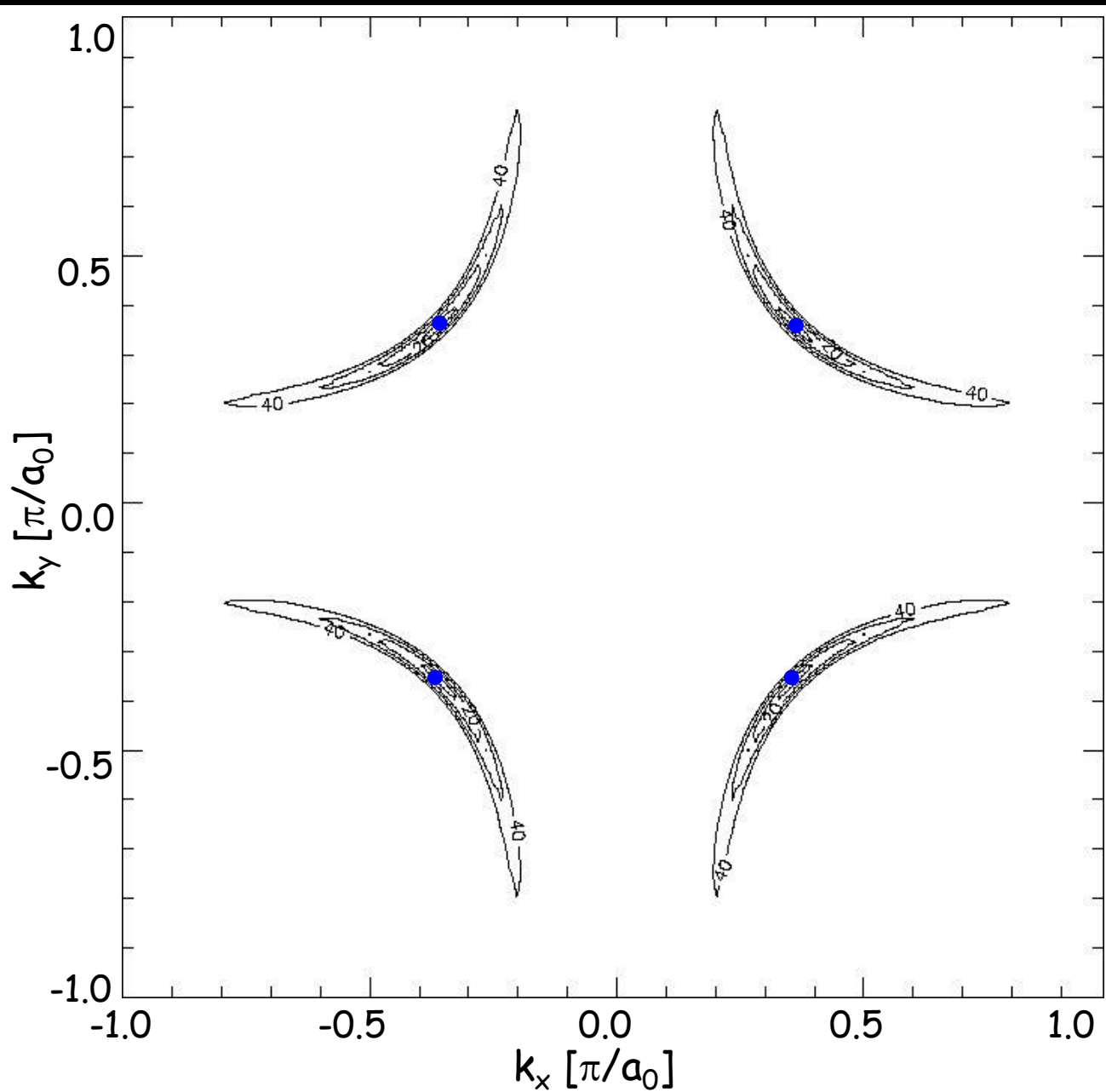
20 meV CCE



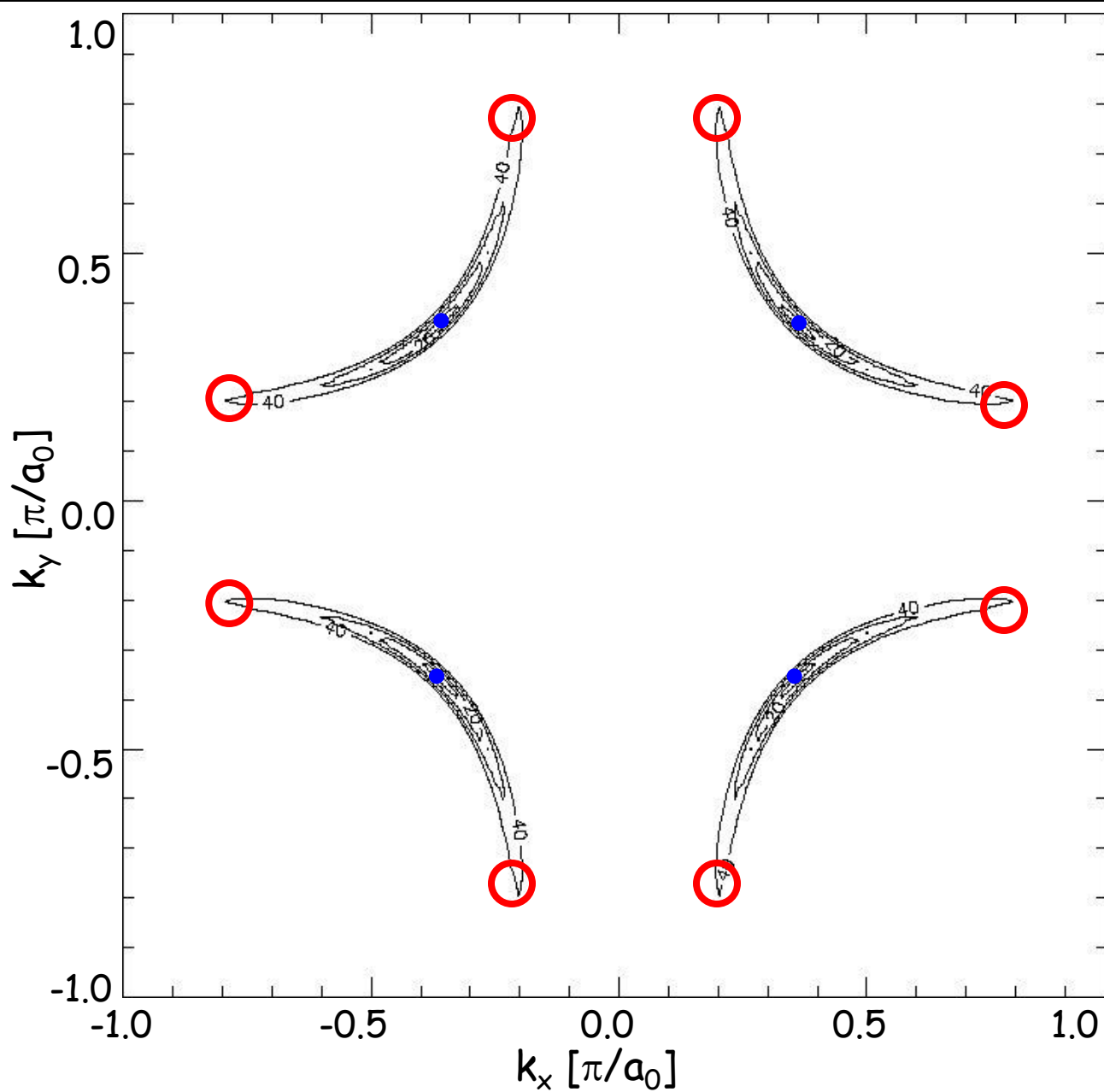
30 meV CCE



40 meV CCE



Octet of regions at ends of 'bananas' have largest $|dk|/dE$



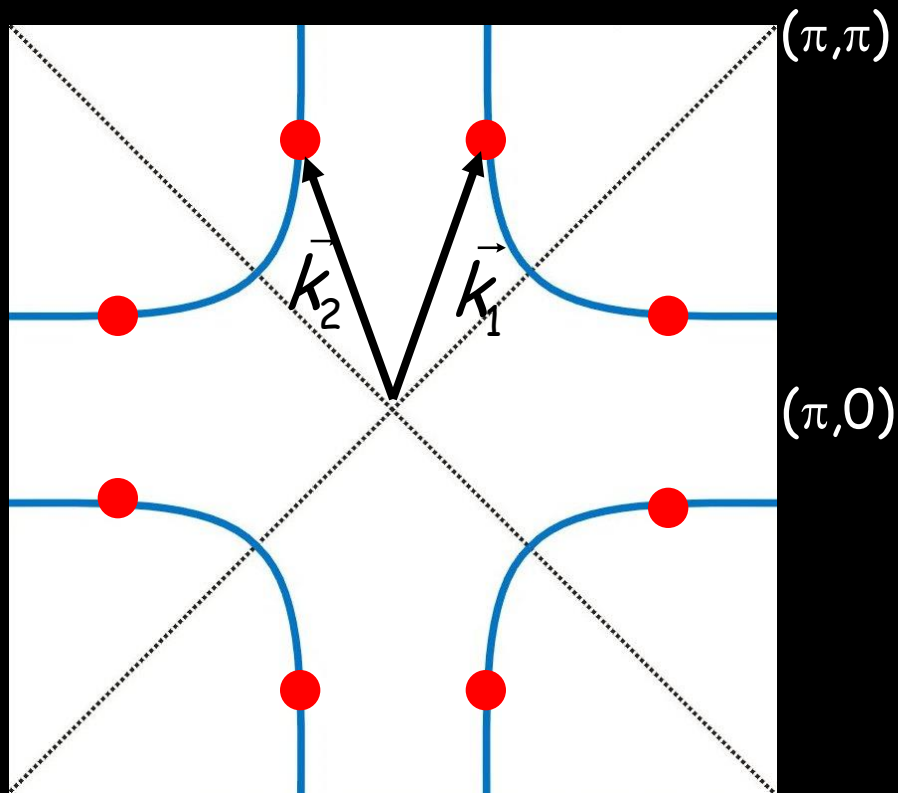
Density of States

$$n(E) = \oint_{E(\vec{k})=E} \frac{1}{|\nabla_{\vec{k}} E(\vec{k})|} dk$$



The octet of k -space locations at the tips of the 'bananas' provide maximum contribution to $n_{i,f}(E)$ and thus dominate elastic scattering processes.

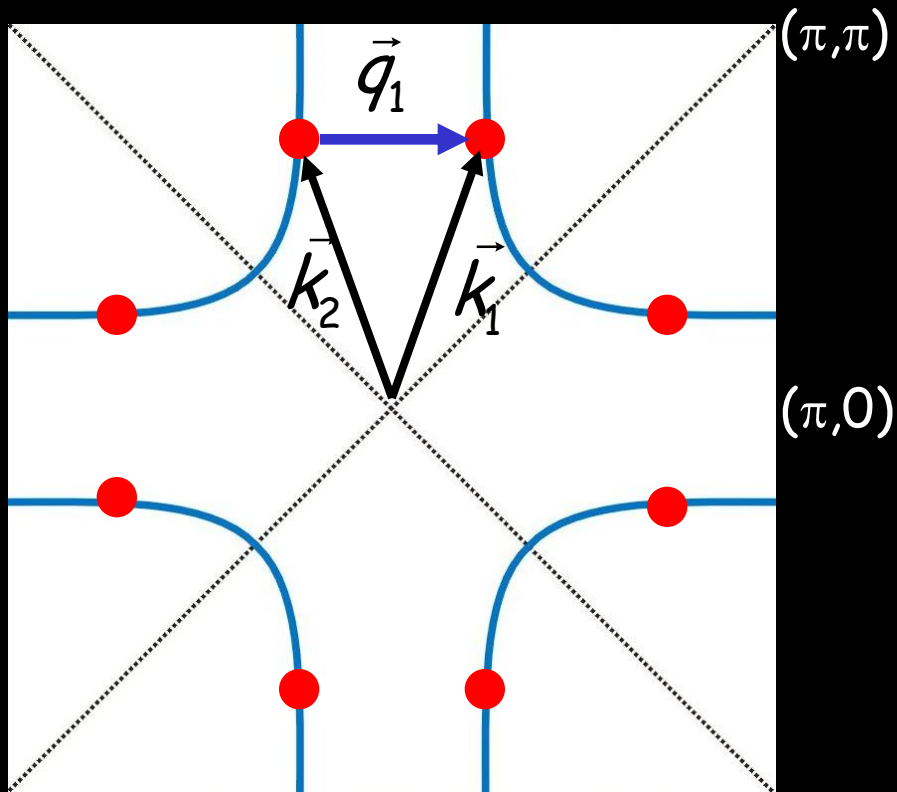
The scattering vectors of QI model



k -space:

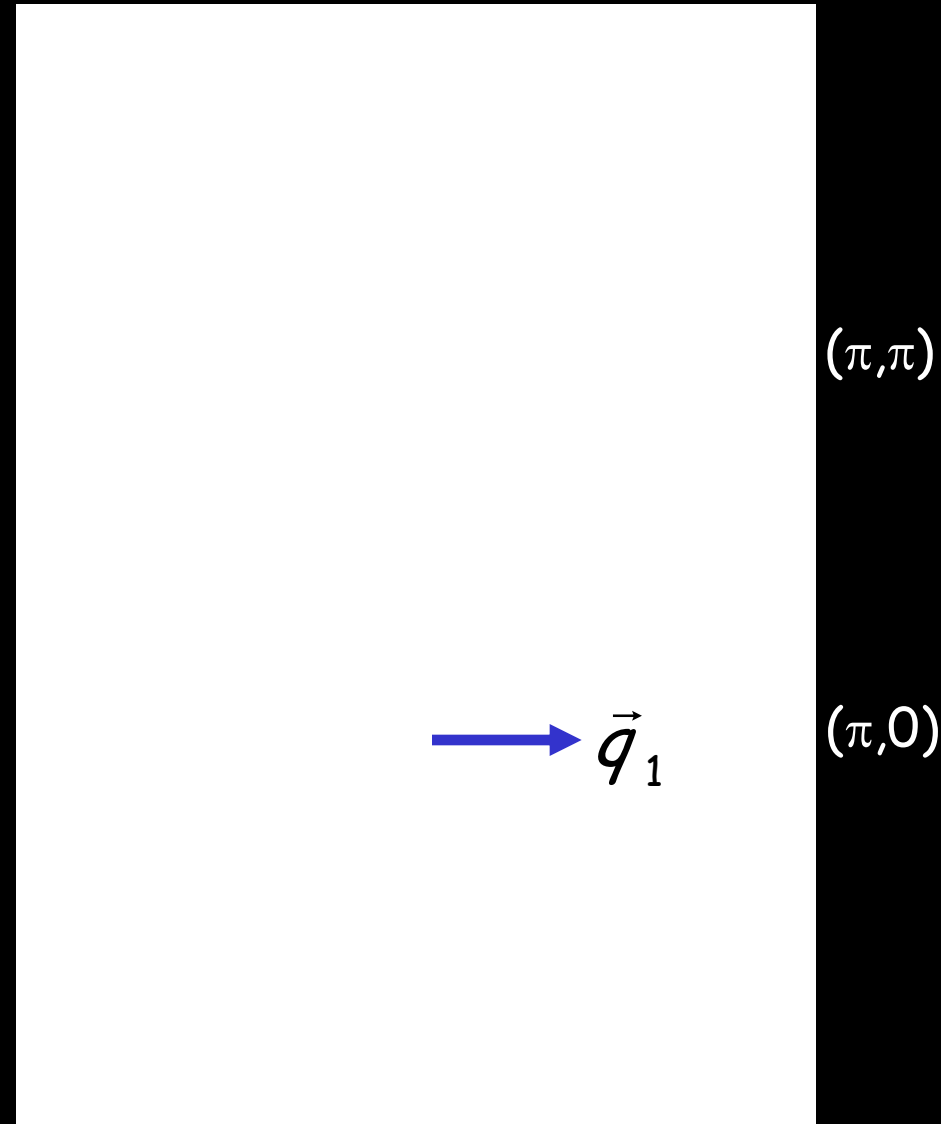
- unperturbed eigenstates
- not directly accessible to STM
- measured by ARPES

The scattering vectors of QI model



k-space:

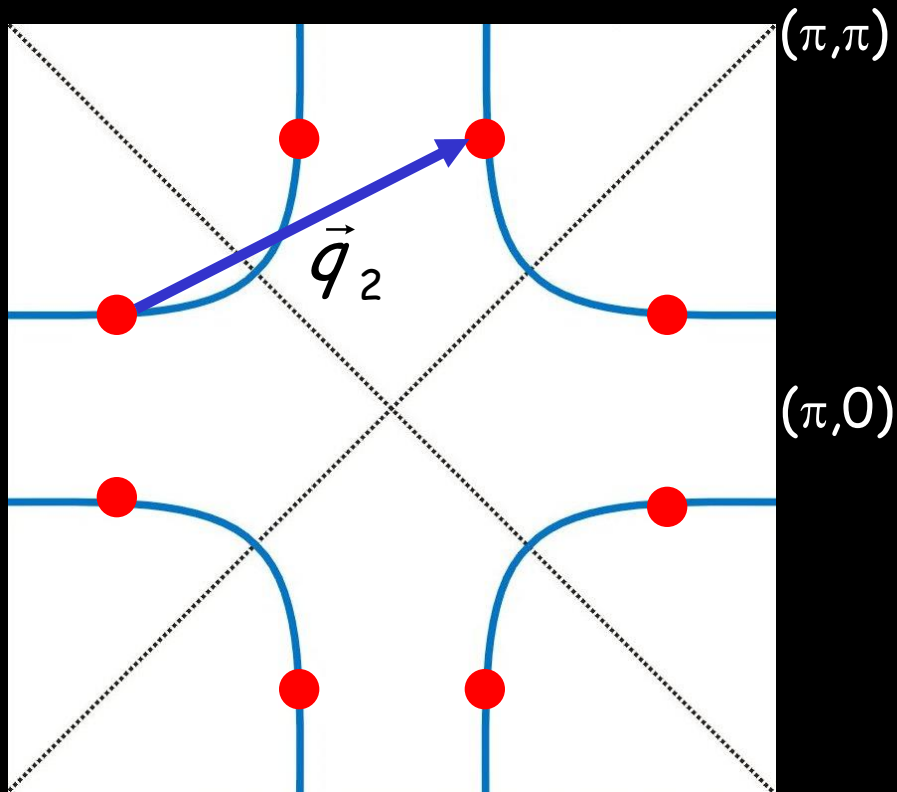
- unperturbed eigenstates
- not directly accessible to STM
- measured by ARPES



q-space:

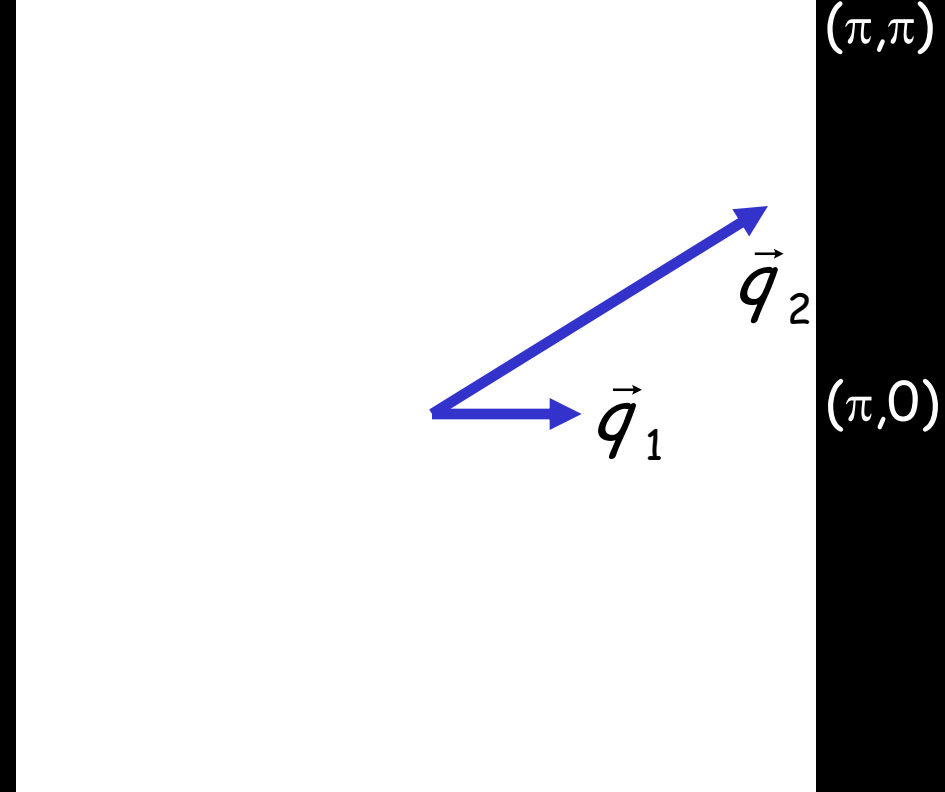
- Scattering \rightarrow standing waves $q = 2\pi/\lambda$
- Measure q from FT of LDOS image

The scattering vectors of QI model



k -space:

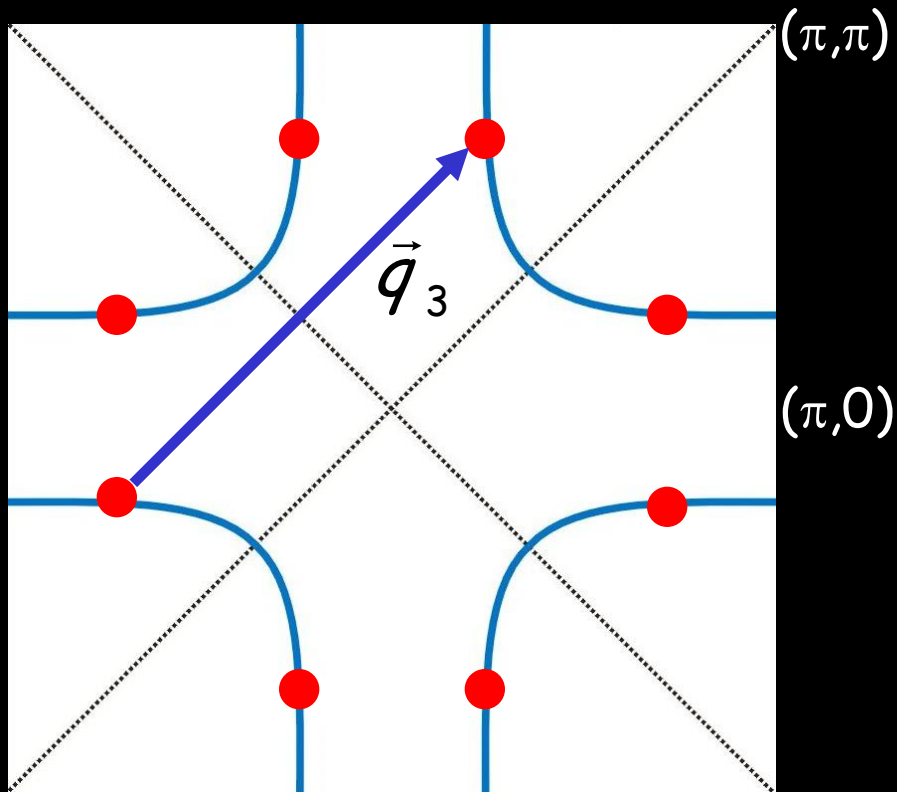
- unperturbed eigenstates
- not directly accessible to STM
- measured by ARPES



q -space:

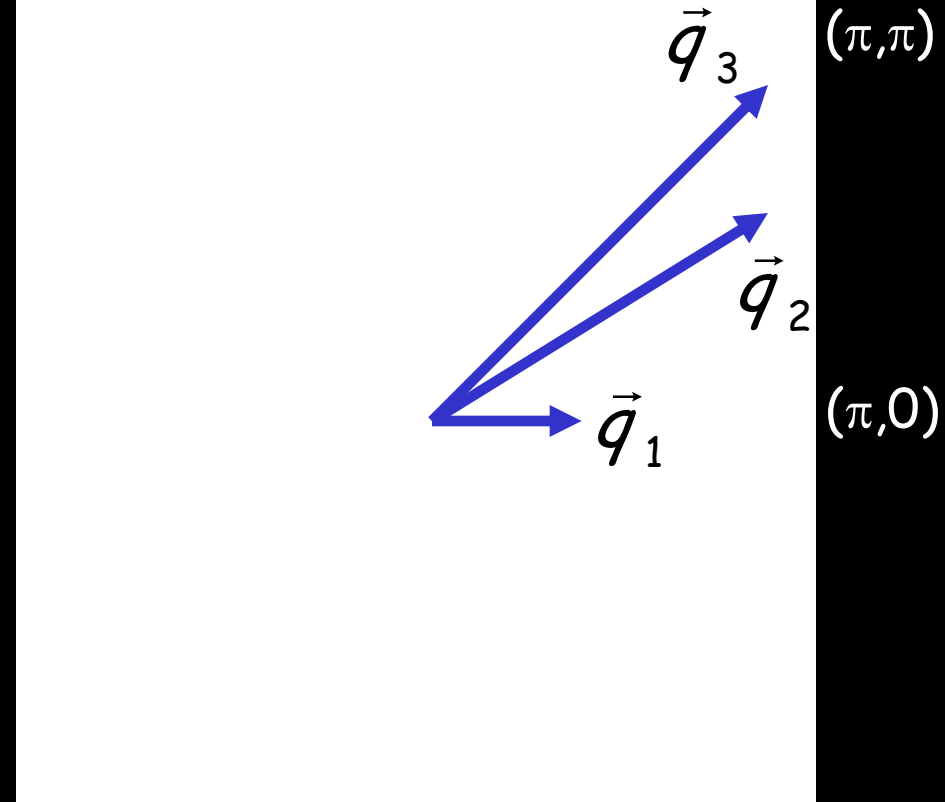
- Scattering \rightarrow standing waves $q = 2\pi/\lambda$
- Measure q from FT of LDOS image

The scattering vectors of QI model



k -space:

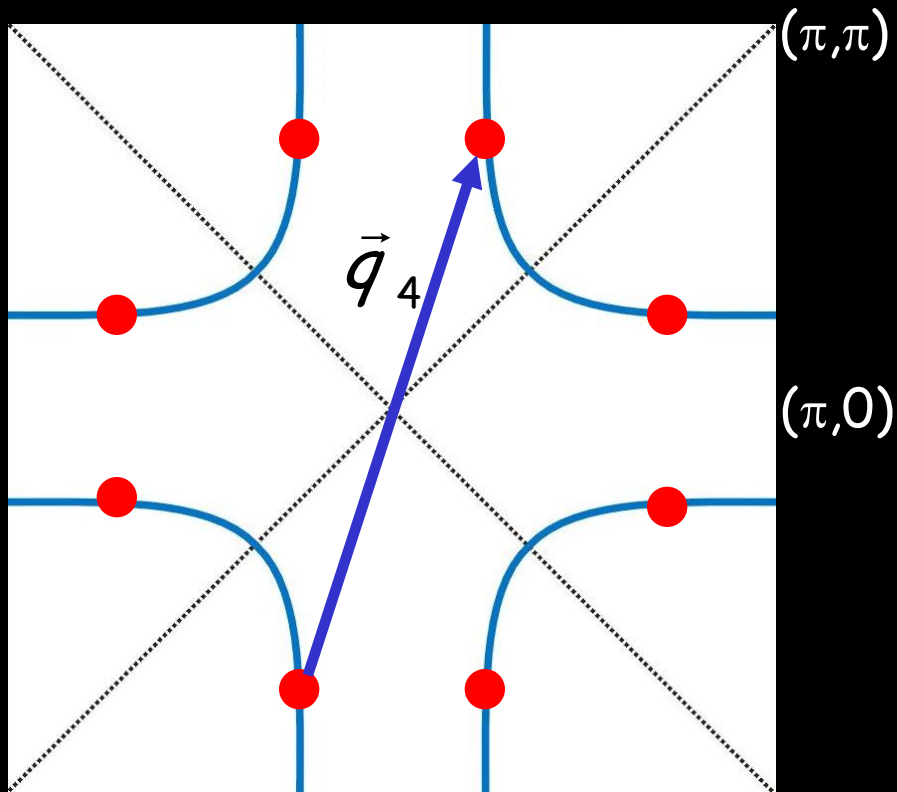
- unperturbed eigenstates
- not directly accessible to STM
- measured by ARPES



q -space:

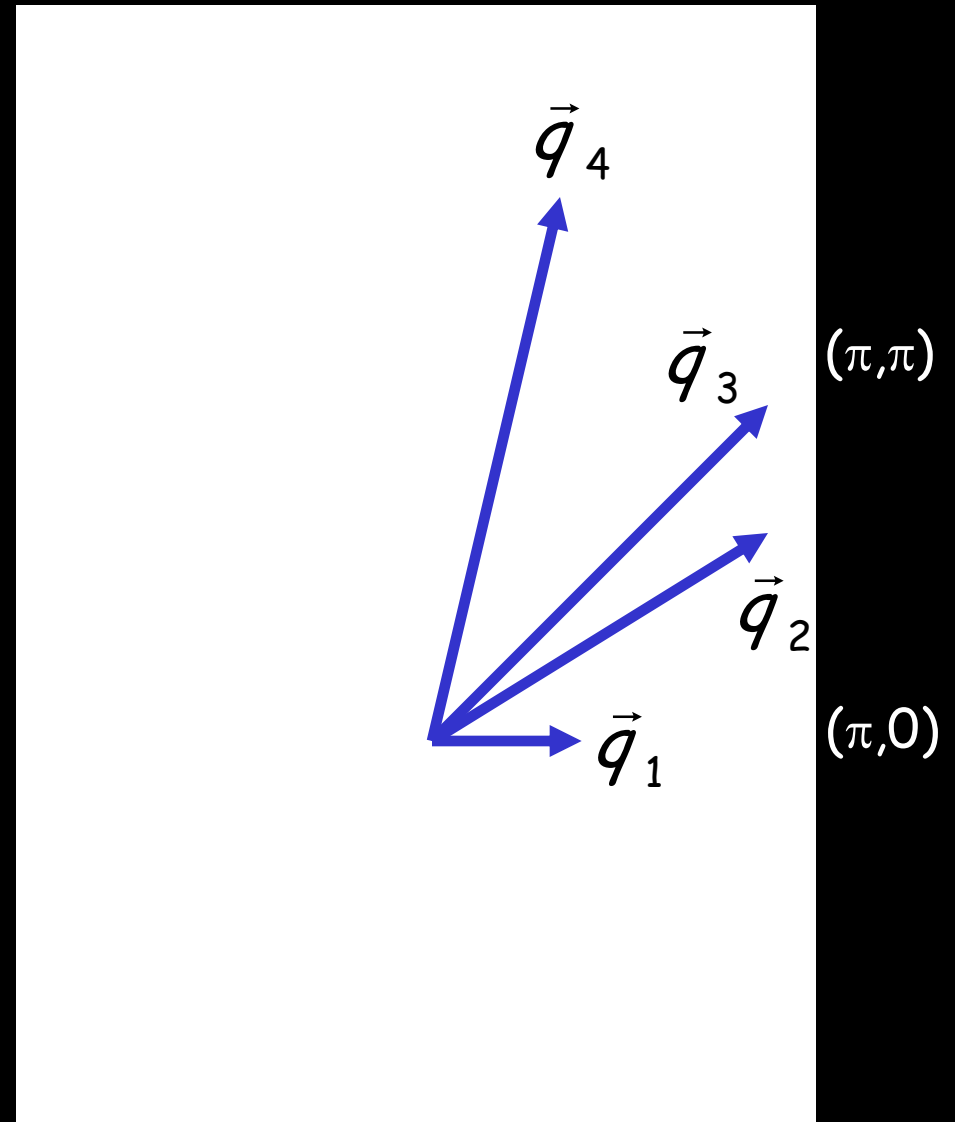
- Scattering \rightarrow standing waves $q = 2\pi/\lambda$
- Measure q from FT of LDOS image

The scattering vectors of QI model



k -space:

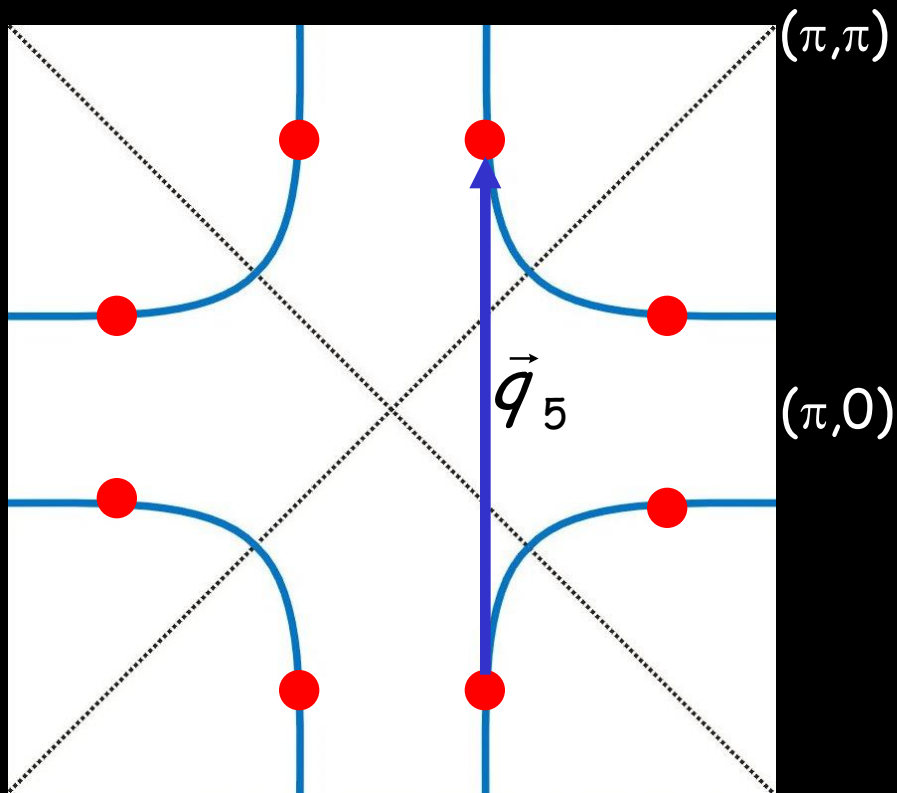
- unperturbed eigenstates
- not directly accessible to STM
- measured by ARPES



q -space:

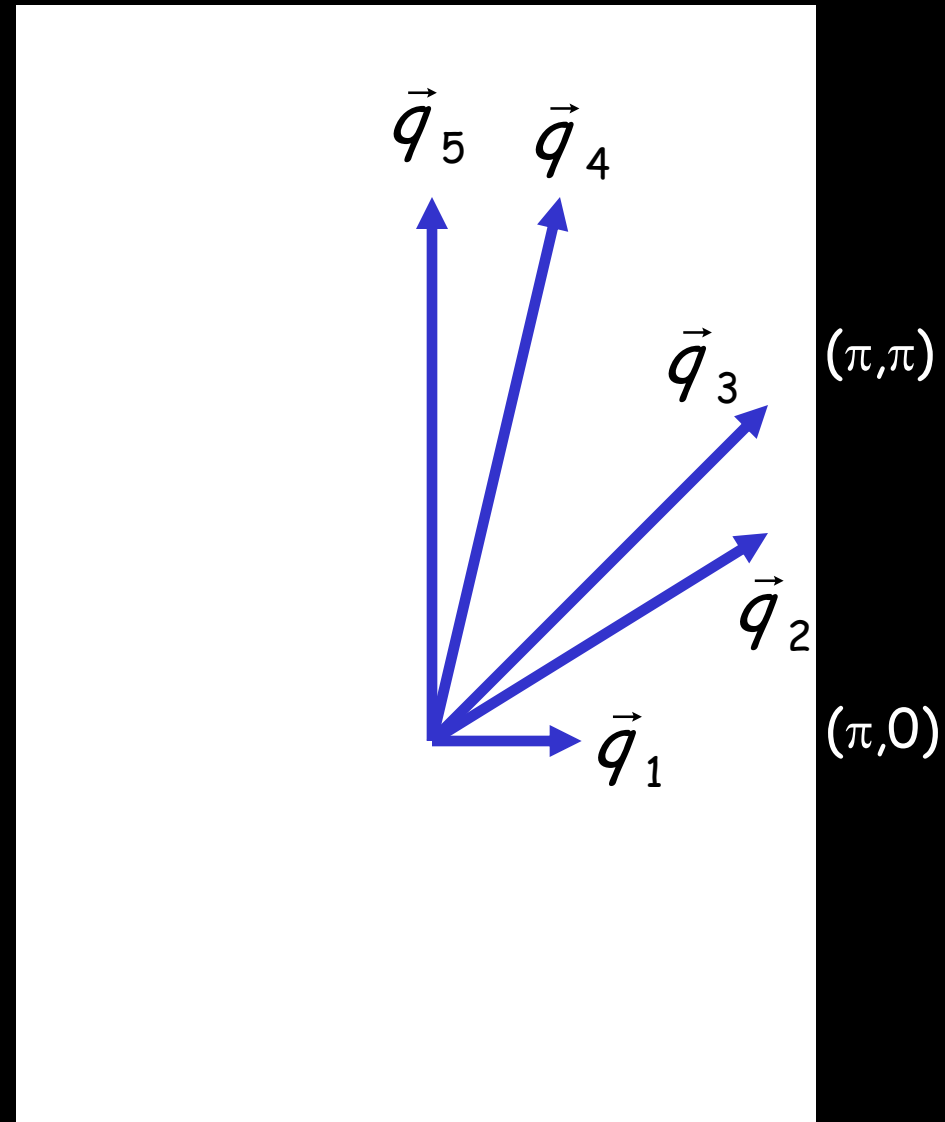
- Scattering \rightarrow standing waves $q = 2\pi/\lambda$
- Measure q from FT of LDOS image

The scattering vectors of QI model



k-space:

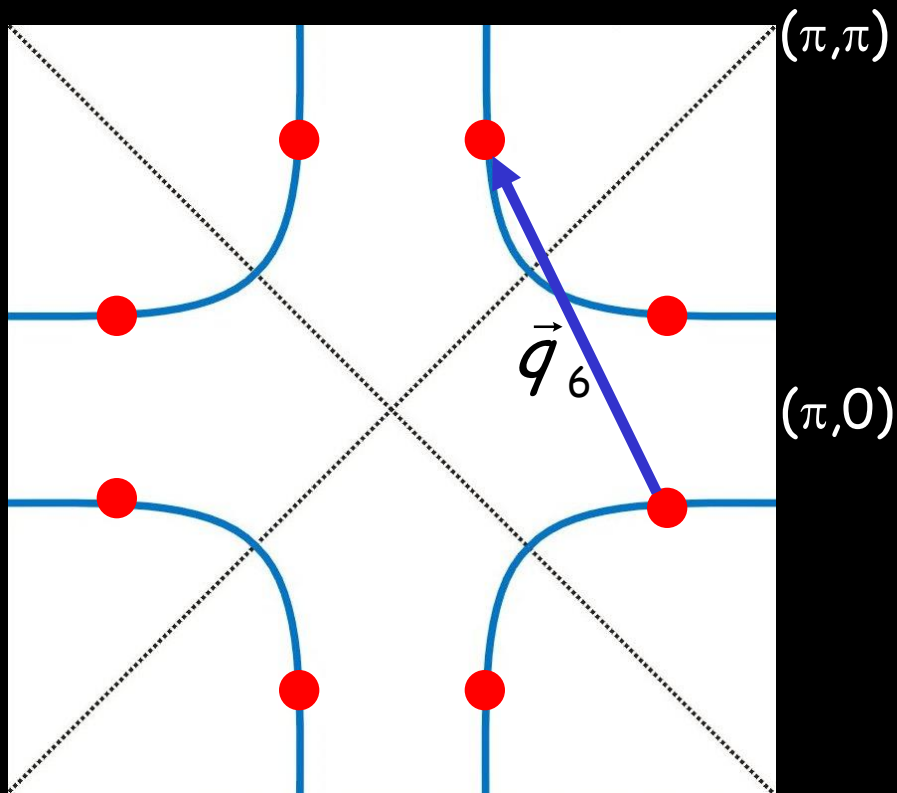
- unperturbed eigenstates
- not directly accessible to STM
- measured by ARPES



q-space:

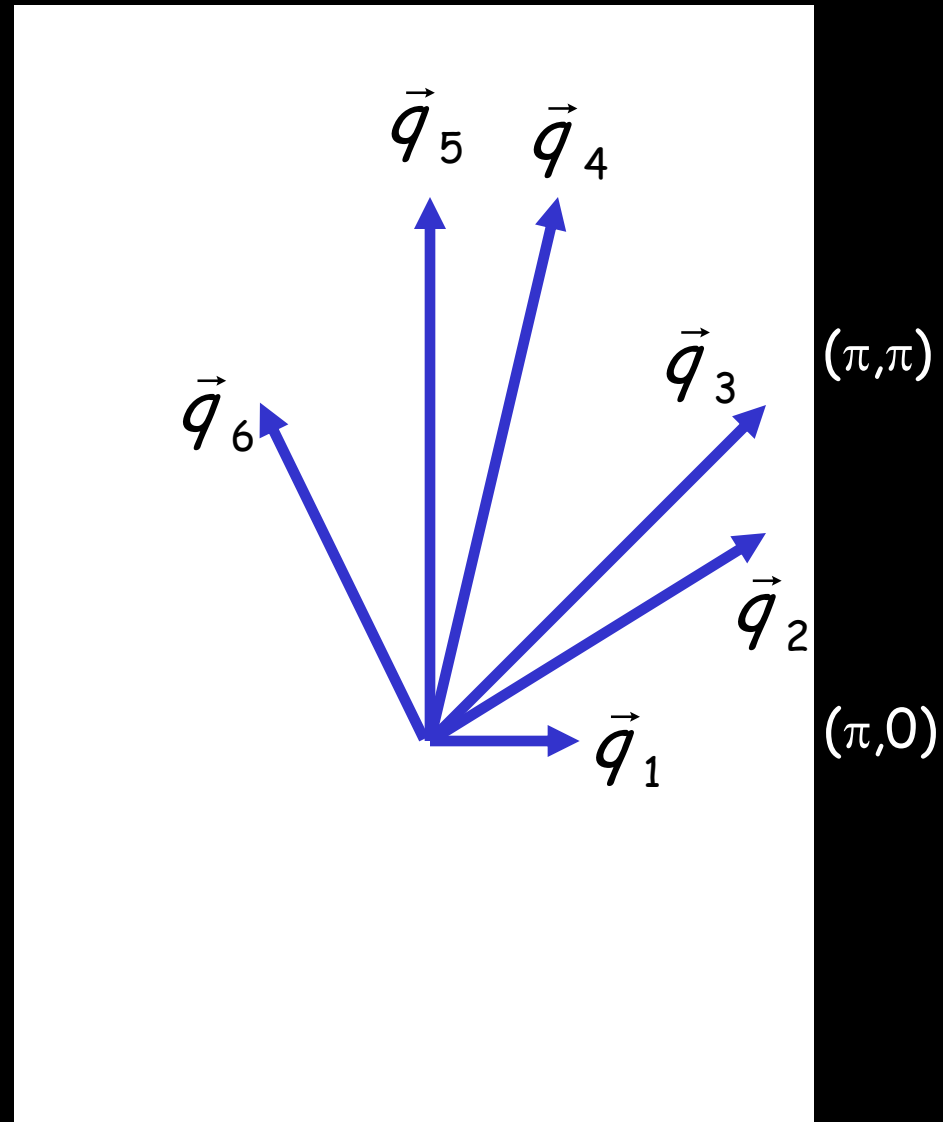
- Scattering \rightarrow standing waves $q = 2\pi/\lambda$
- Measure q from FT of LDOS image

The scattering vectors of QI model



k -space:

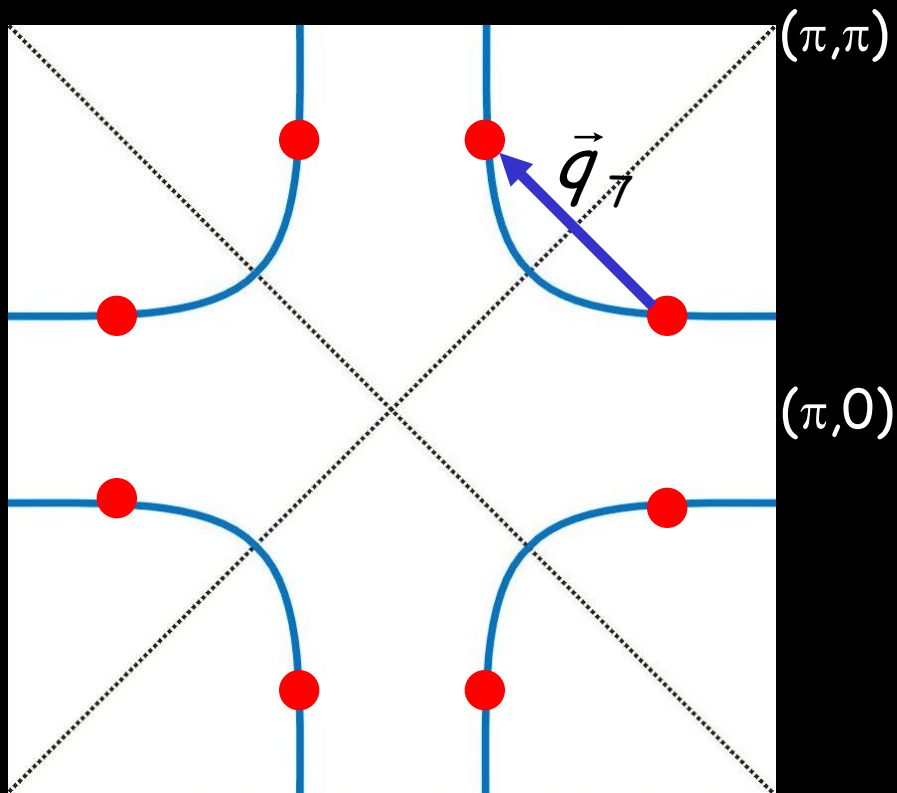
- unperturbed eigenstates
- not directly accessible to STM
- measured by ARPES



q -space:

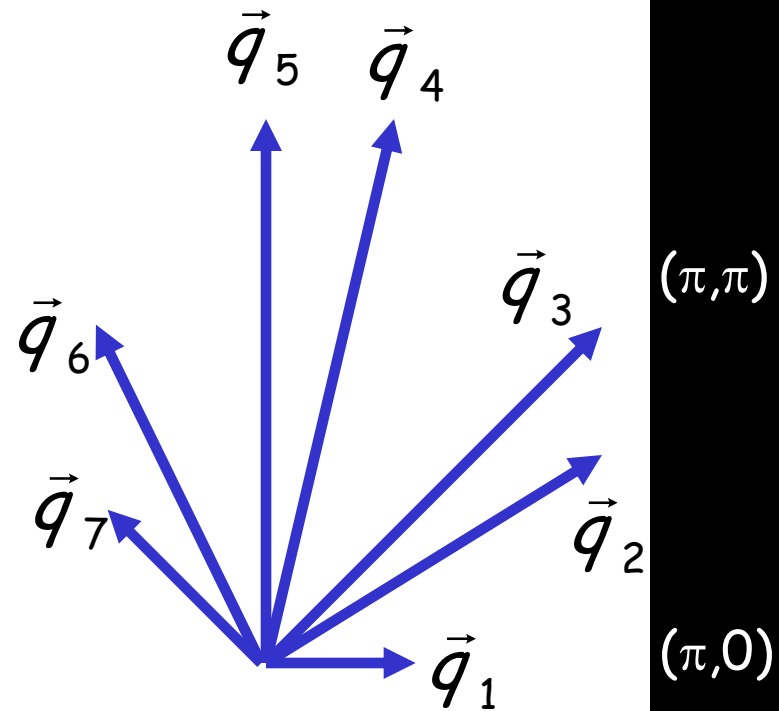
- Scattering \rightarrow standing waves $q = 2\pi/\lambda$
- Measure q from FT of LDOS image

The scattering vectors of QI model



k-space:

- unperturbed eigenstates
- not directly accessible to STM
- measured by ARPES

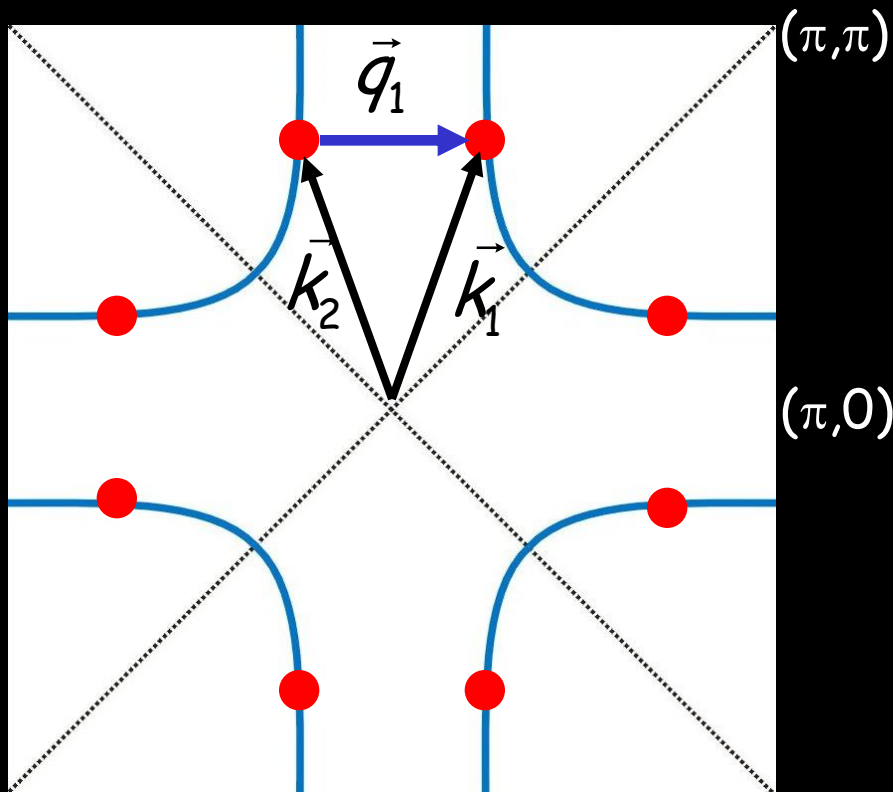


Total sets of q_i (7X8) : 56
 Inequivalent sets of q_i : 32
 Distinguishable via FT-STIS : 16

q-space:

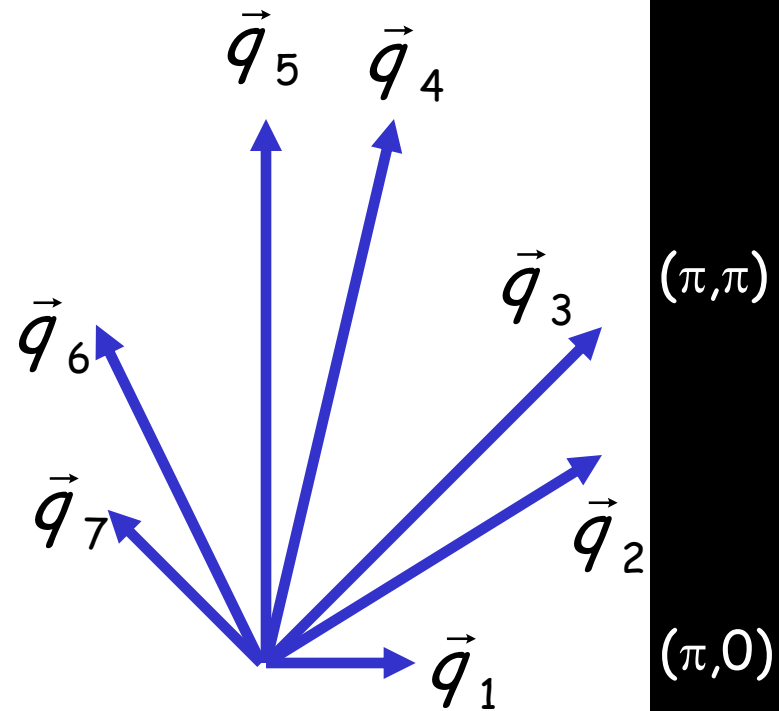
- Scattering \rightarrow standing waves $q = 2\pi/\lambda$
- Measure q from FT of LDOS image

The scattering vectors of QI model



k -space:

- unperturbed eigenstates
- not directly accessible to STM
- measured by ARPES

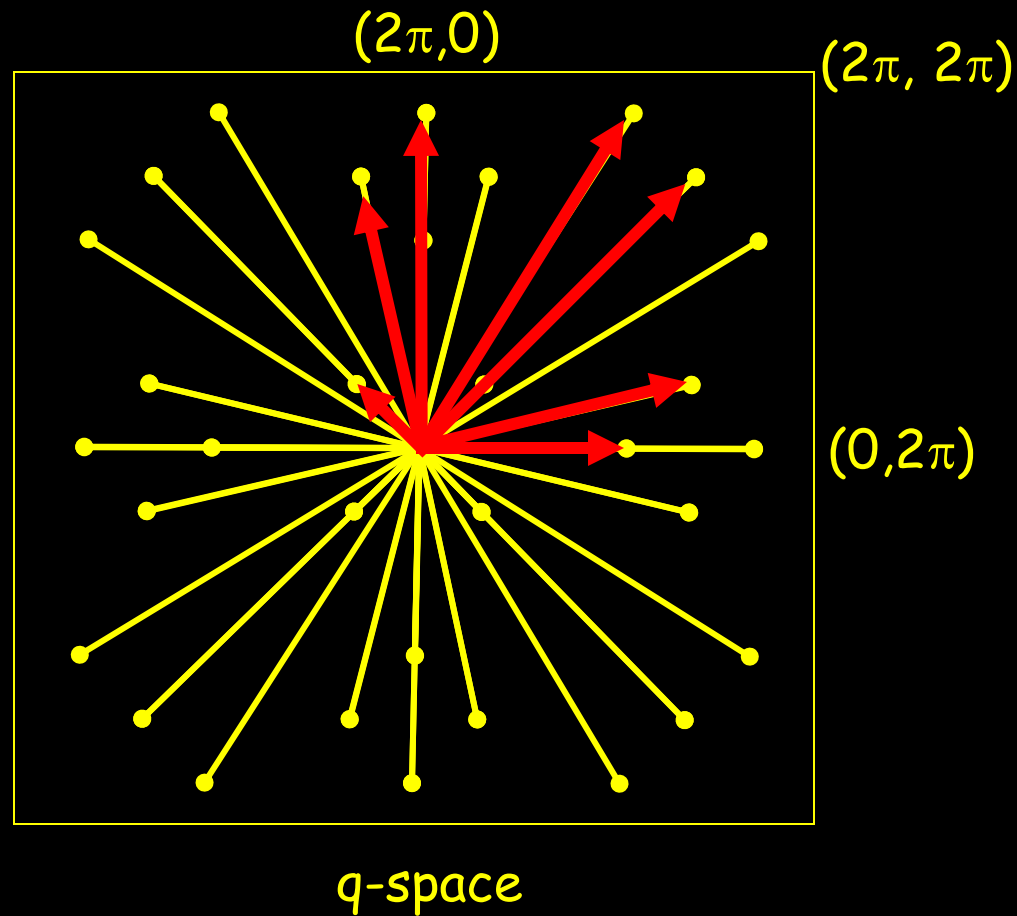


Total sets of q_i (7X8) : 56
 Inequivalent sets of q_i : 32
 Distinguishable via FT-STIS : 16

q -space:

- Scattering \rightarrow standing waves $q = 2\pi/\lambda$
- Measure q from FT of LDOS image

Expected structure of FFT of LDOS(r,E) (for a fixed E)

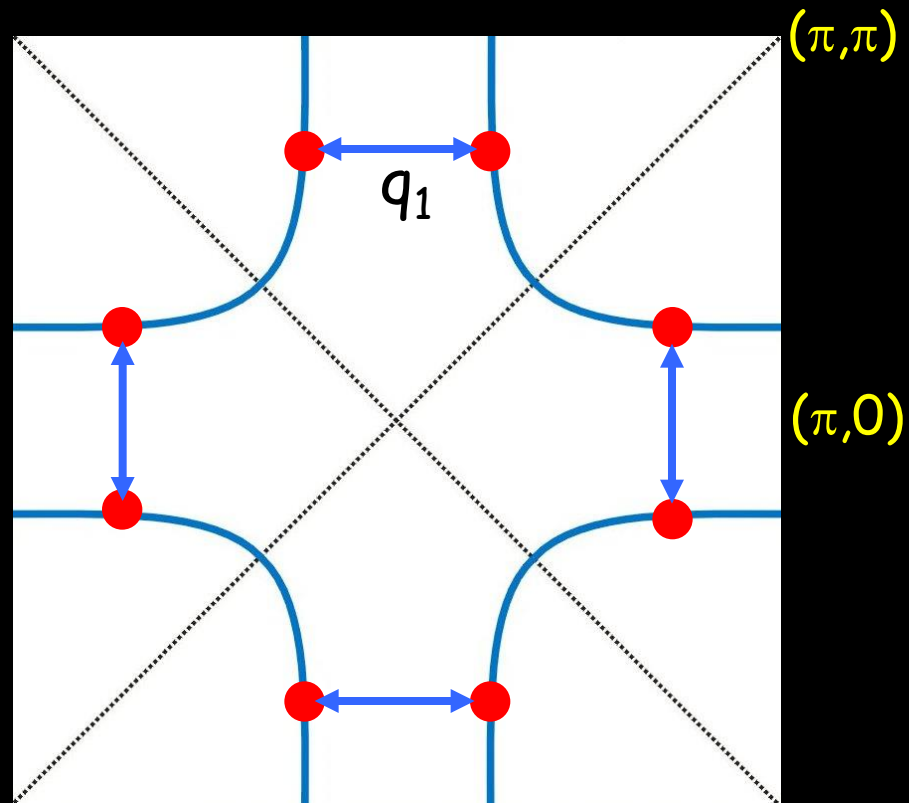


Dispersion:

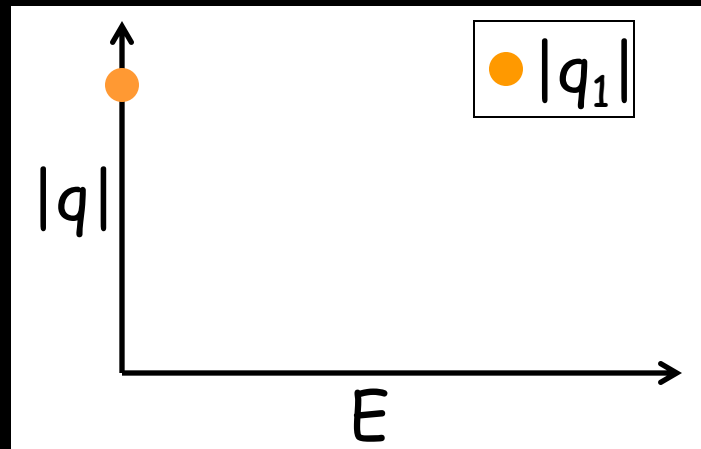
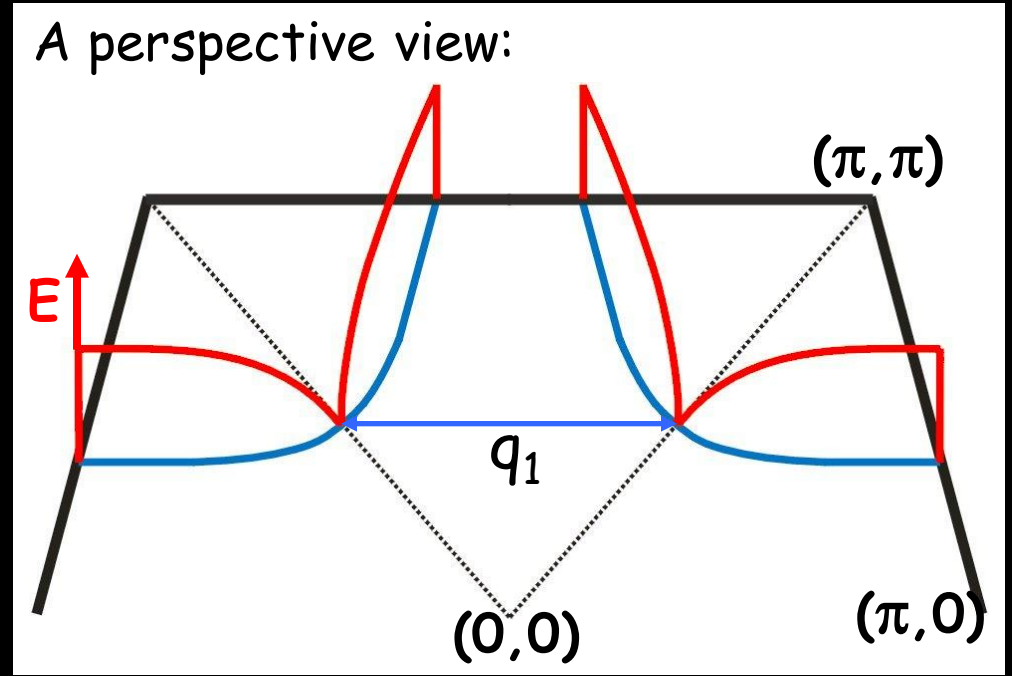
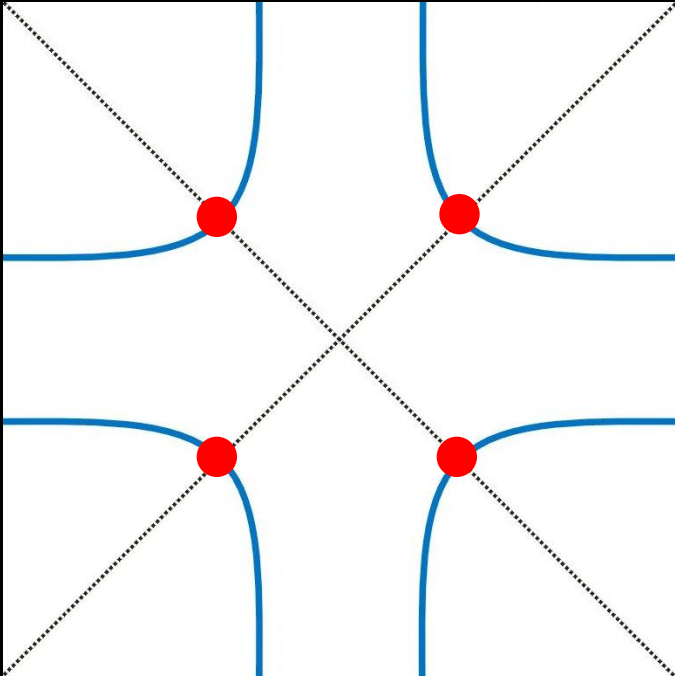
how does each \vec{q}_i vary with E ?

For example, look at the dispersion of:

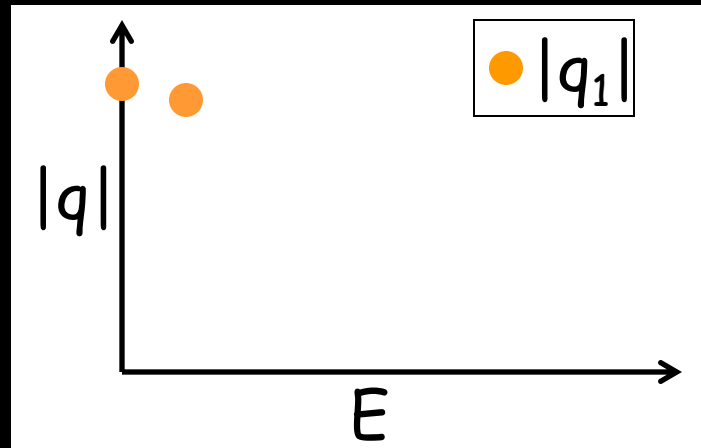
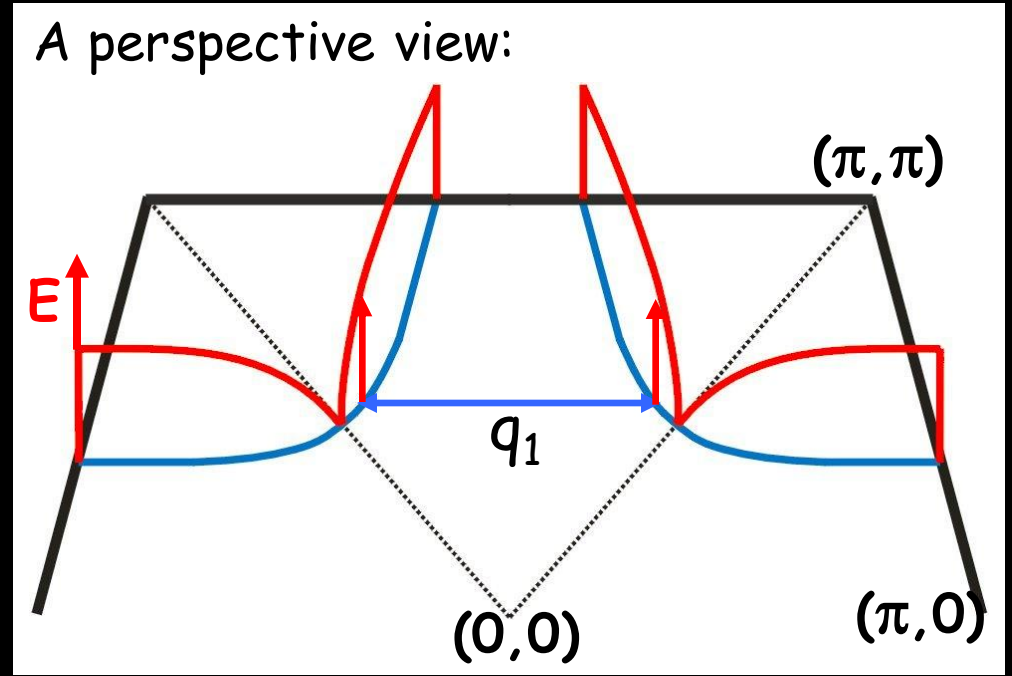
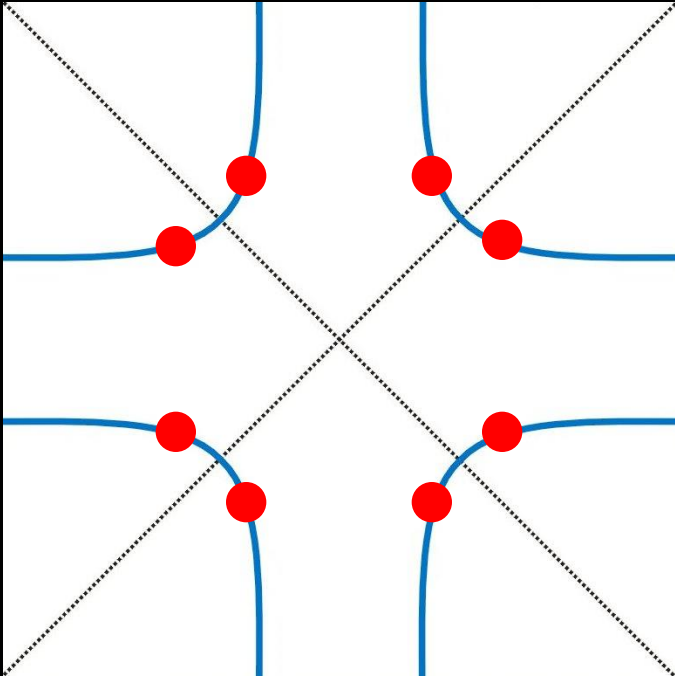
$$\vec{q}_1 \parallel (\pm\pi, 0) \text{ or } (0, \pm\pi)$$



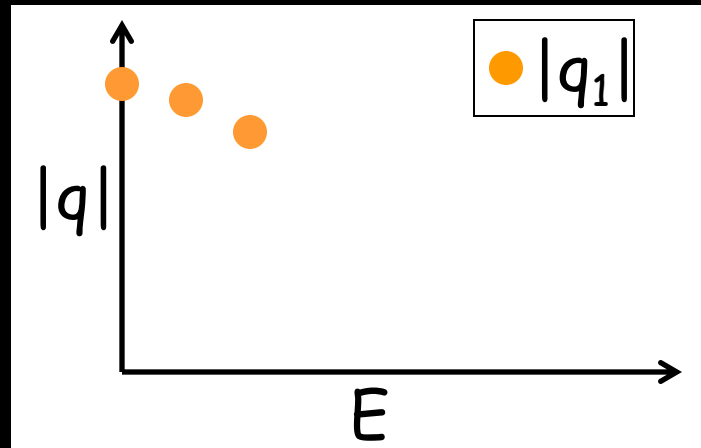
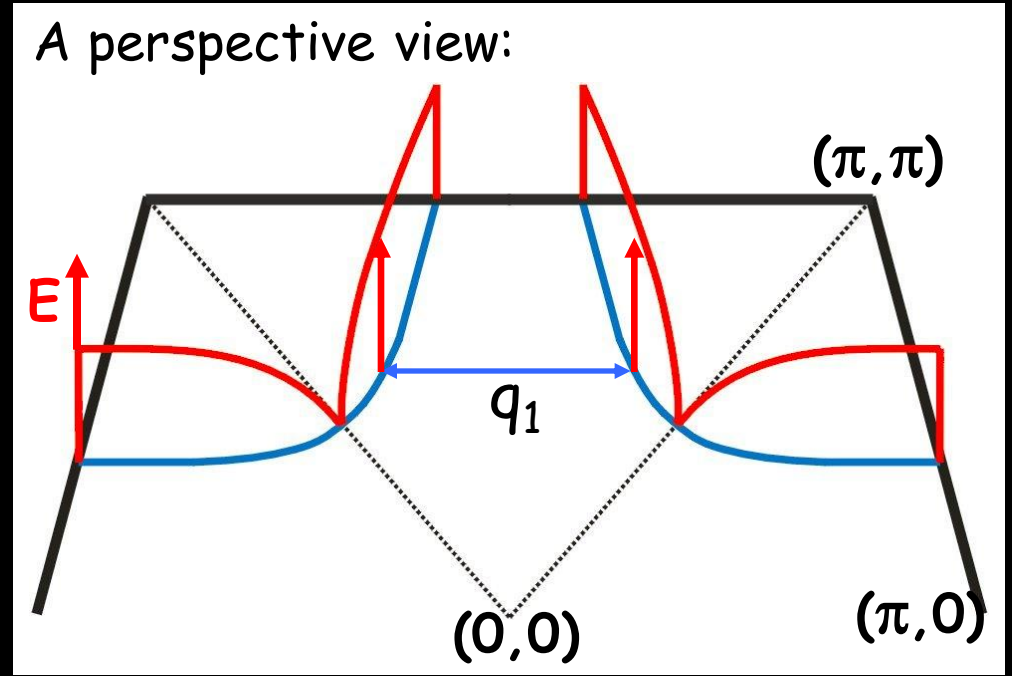
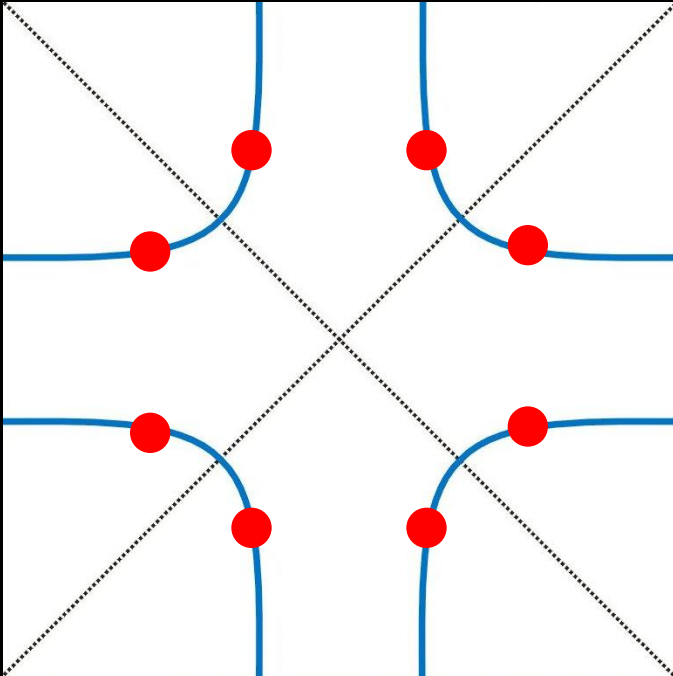
Expected energy dependence of $|\vec{q}_1|$



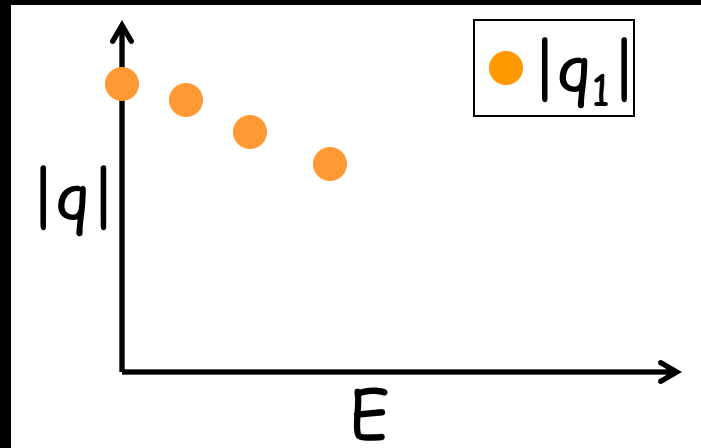
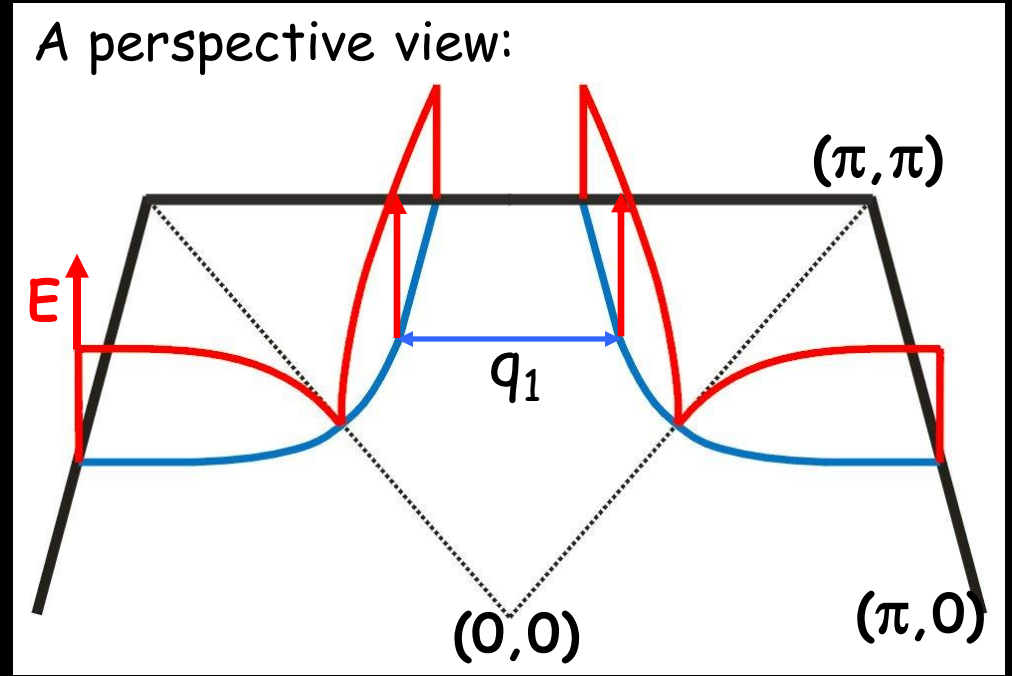
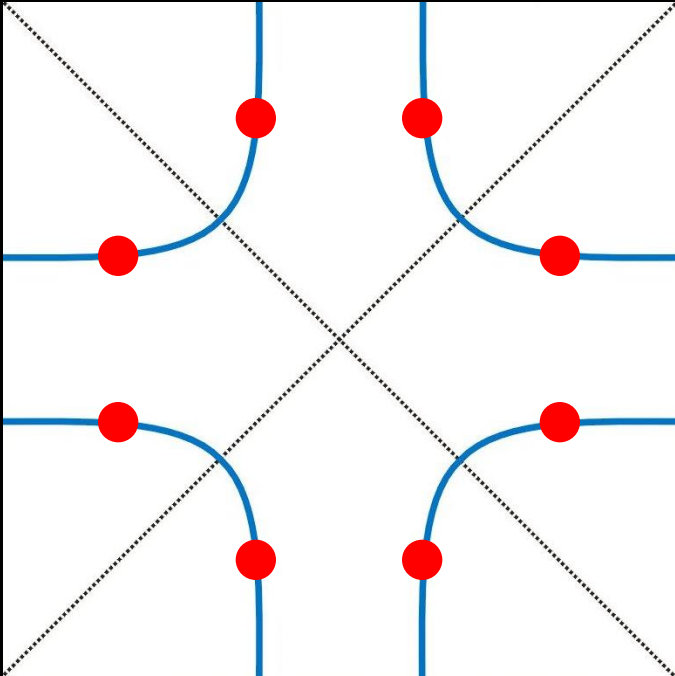
Expected energy dependence of $|\vec{q}_1|$



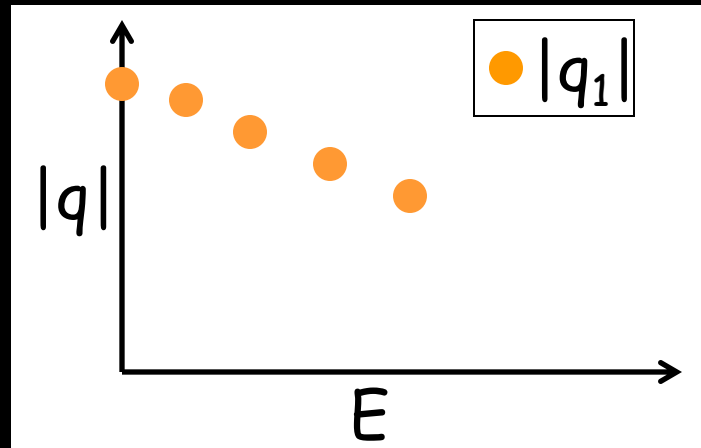
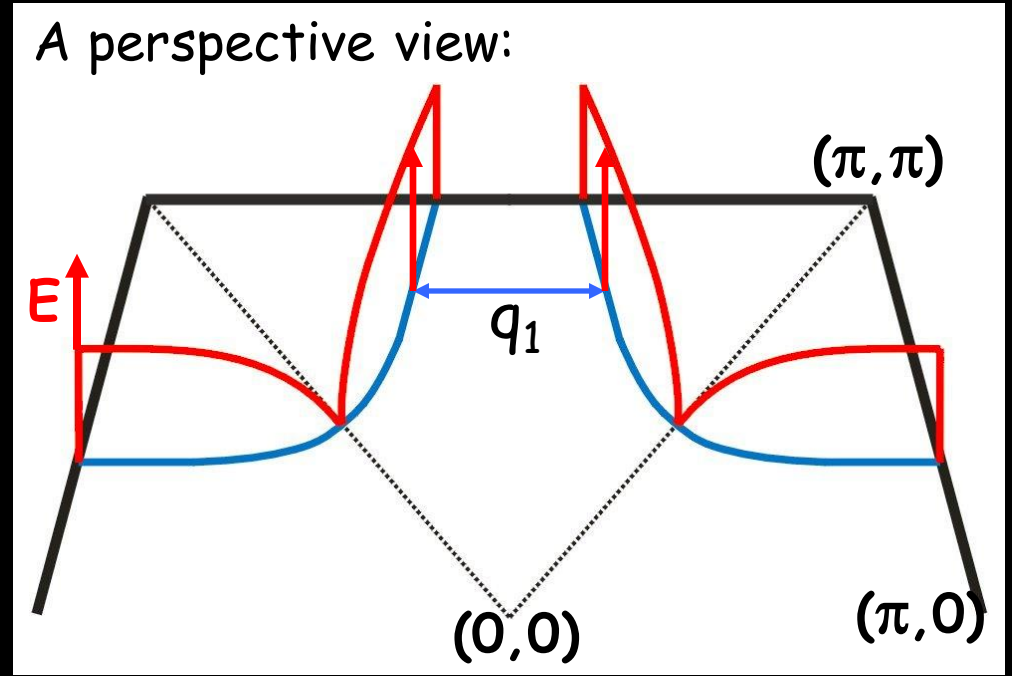
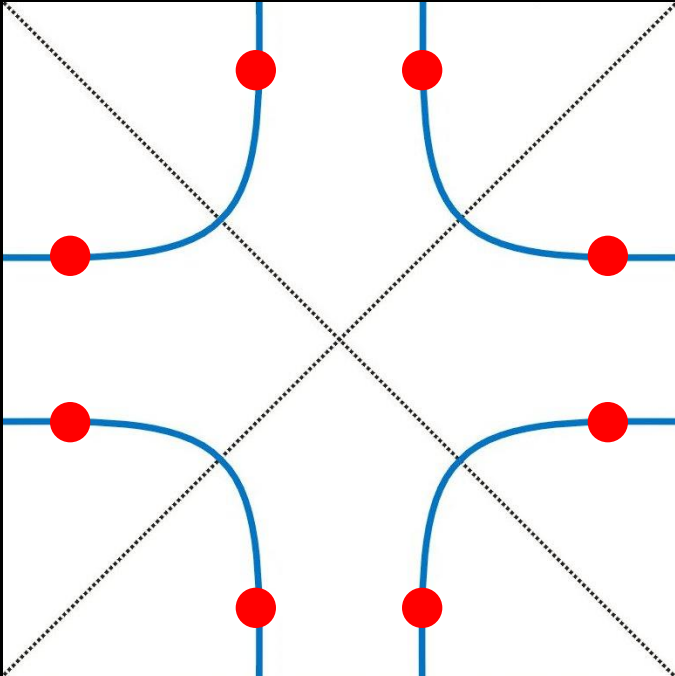
Expected energy dependence of $|\vec{q}_1|$



Expected energy dependence of $|\vec{q}_1|$

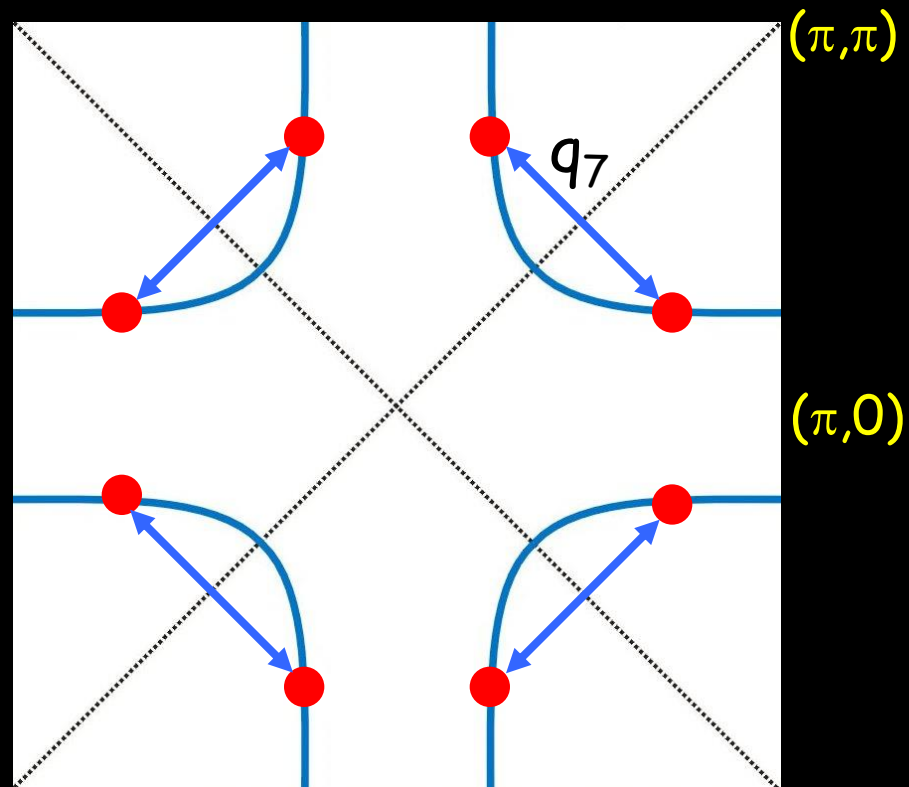


Expected energy dependence of $|\vec{q}_1|$

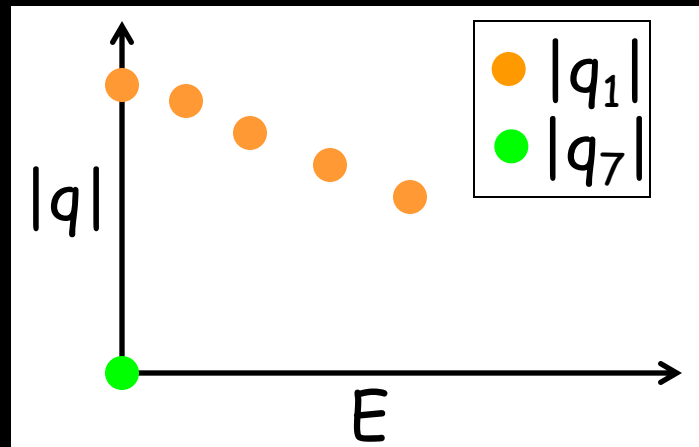
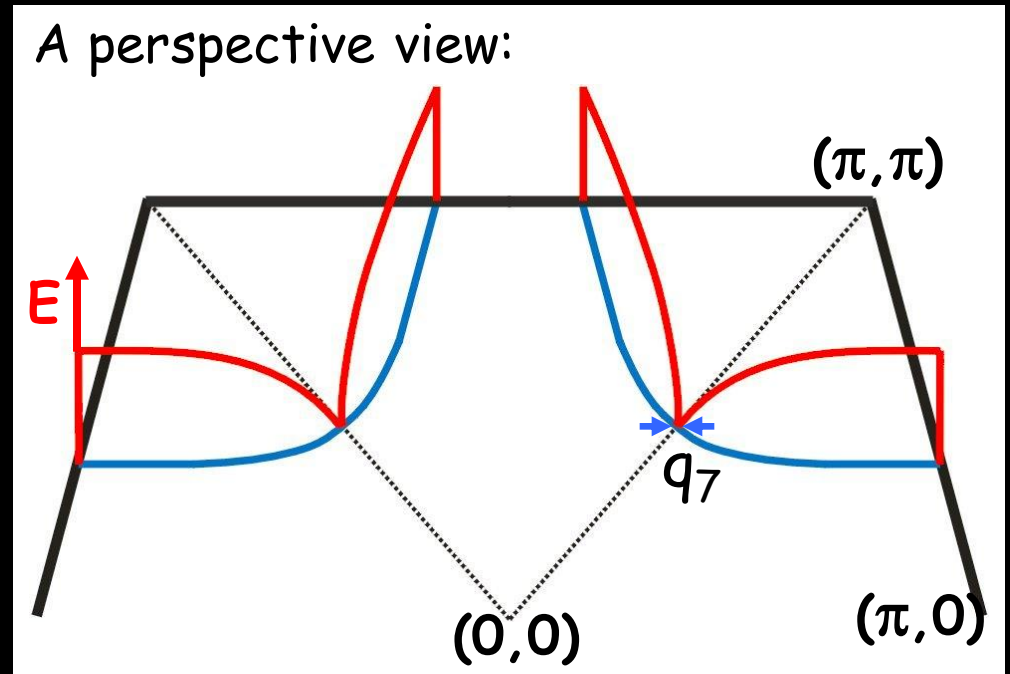
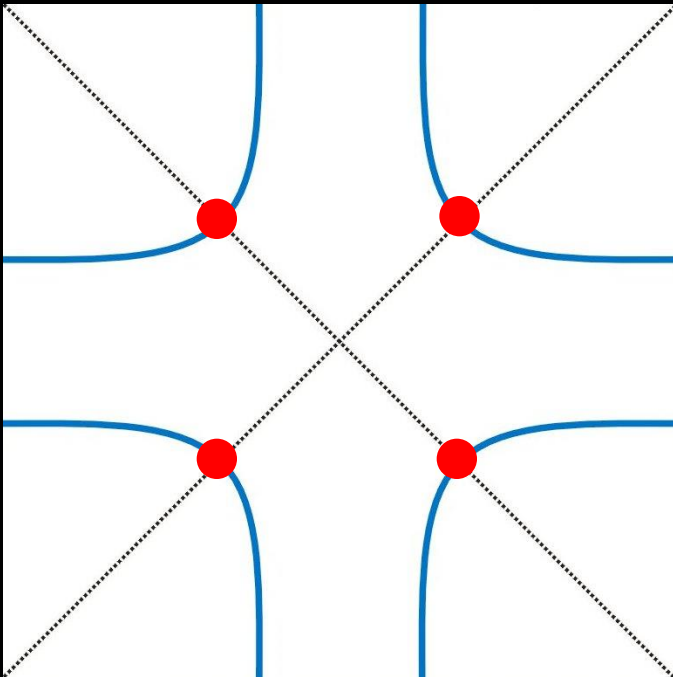


For example, look at the dispersion of:

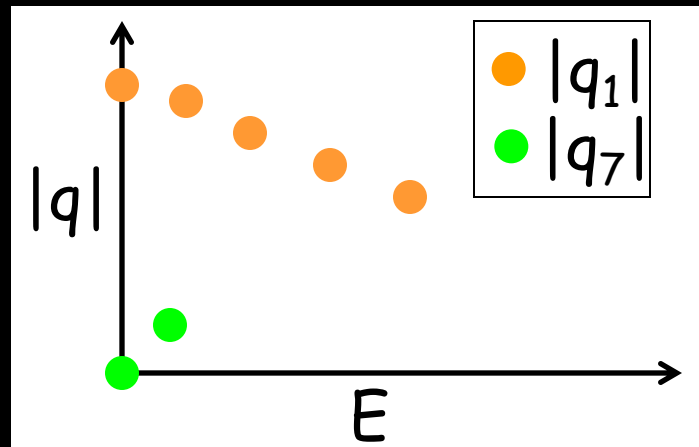
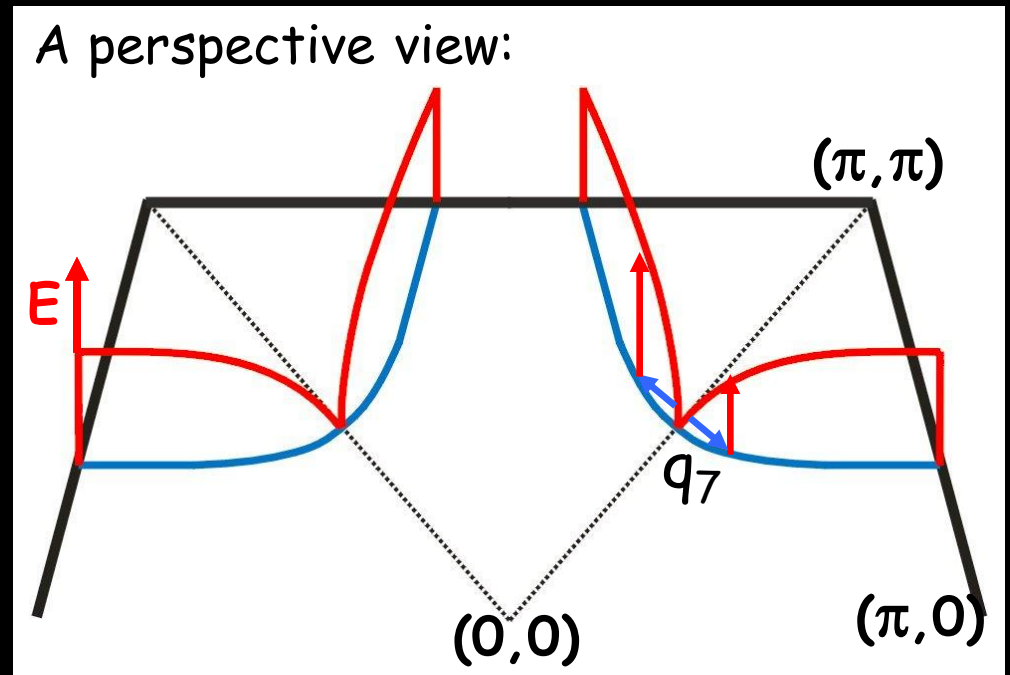
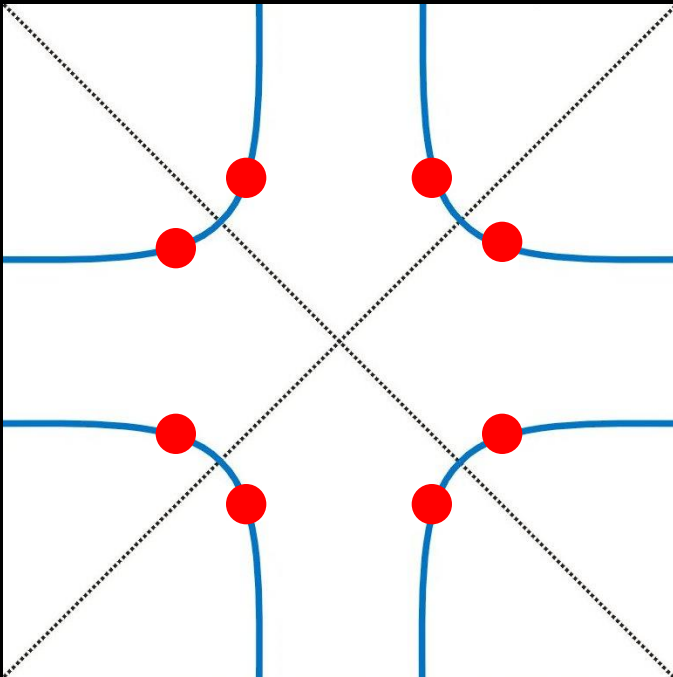
$$\vec{q}_7 \parallel (\pm\pi, \pm\pi)$$



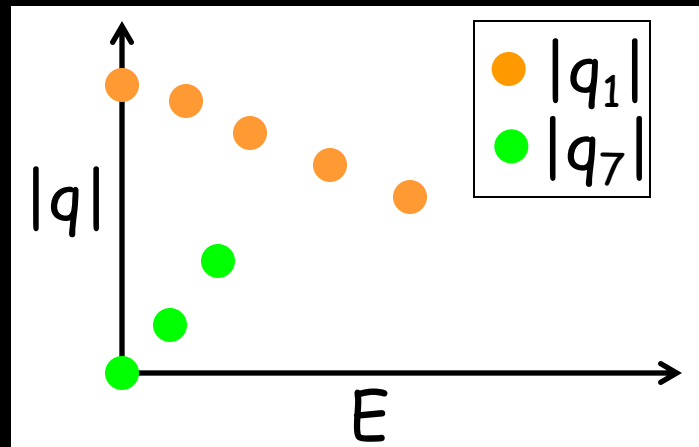
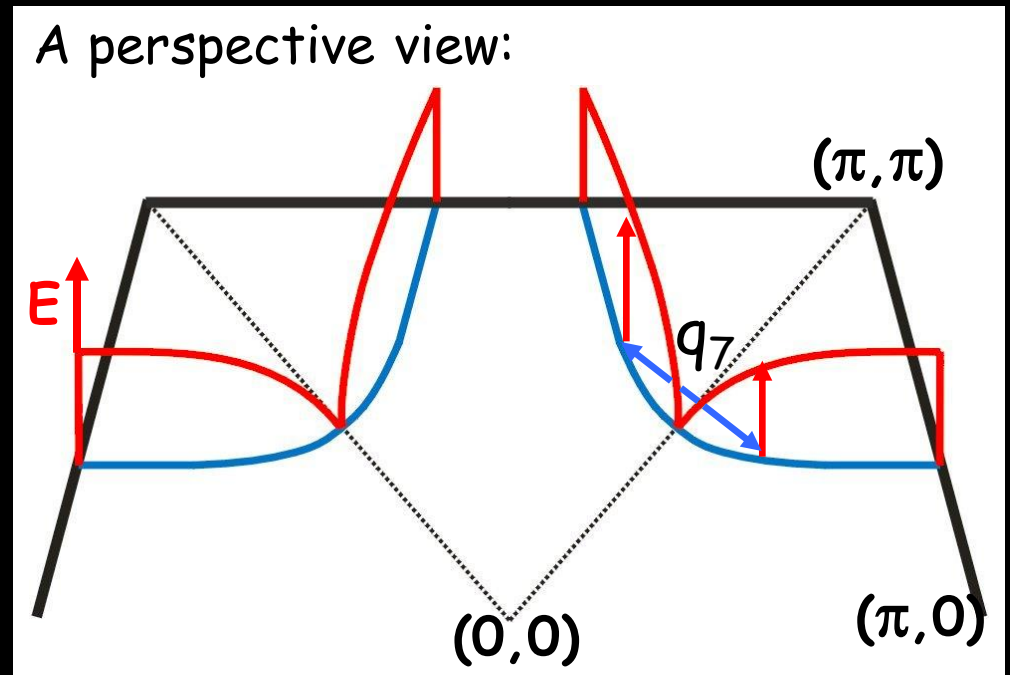
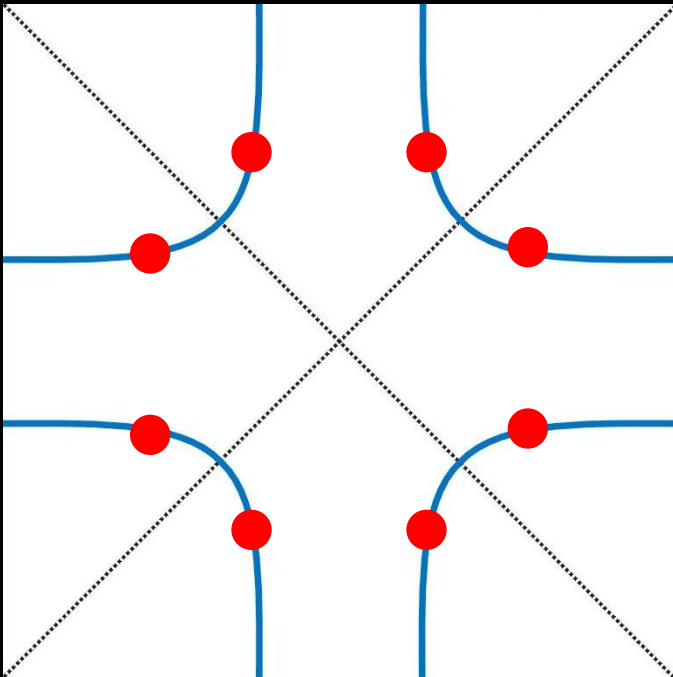
Expected energy dependence of $|\vec{q}_7|$



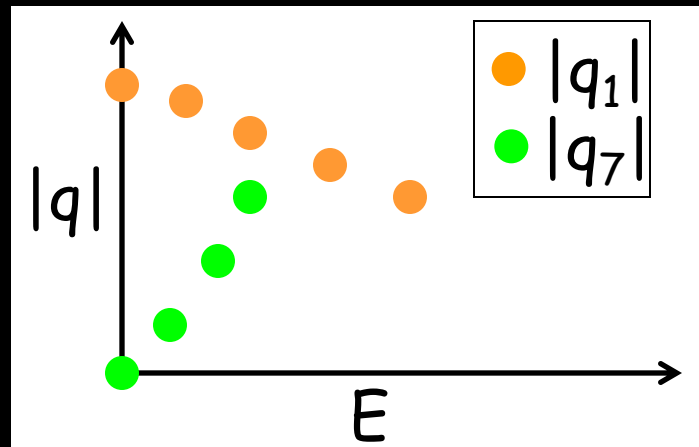
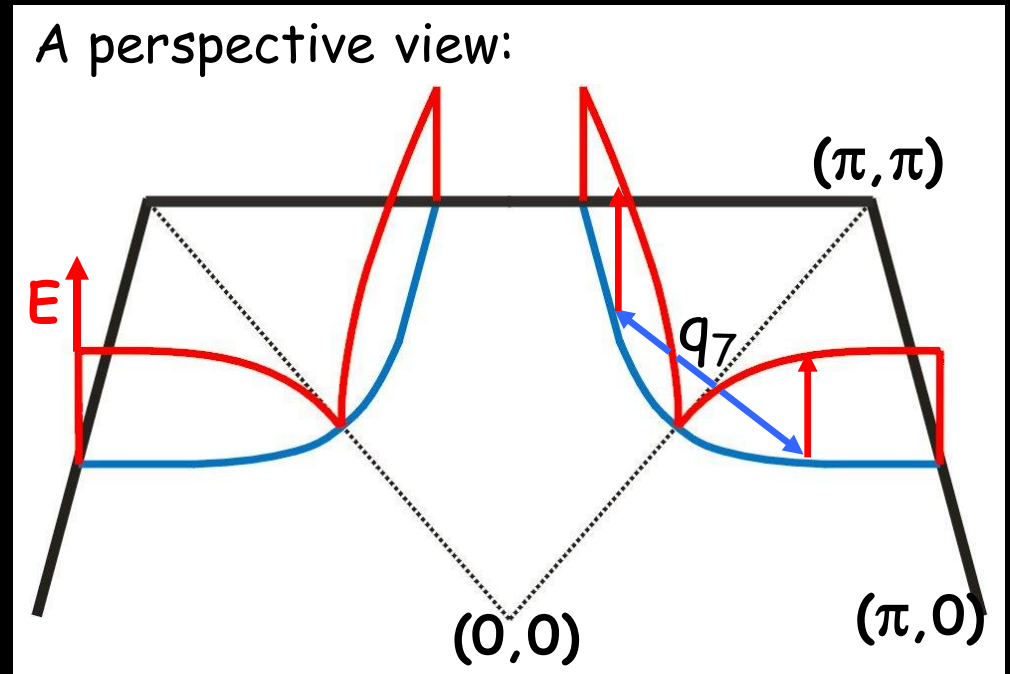
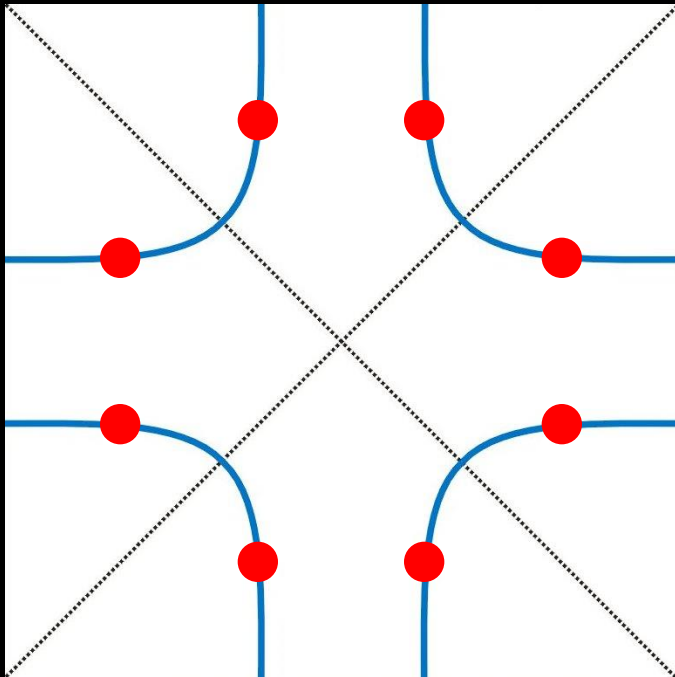
Expected energy dependence of $|\vec{q}_7|$



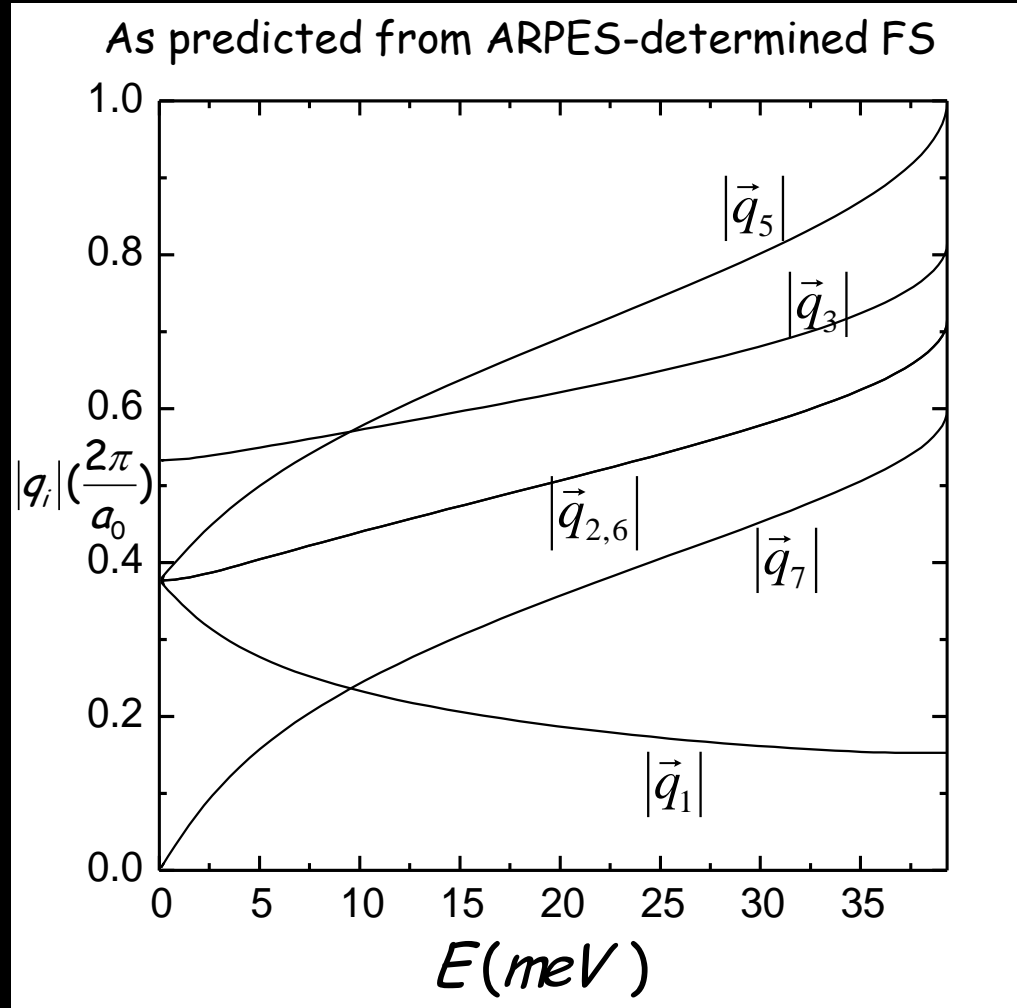
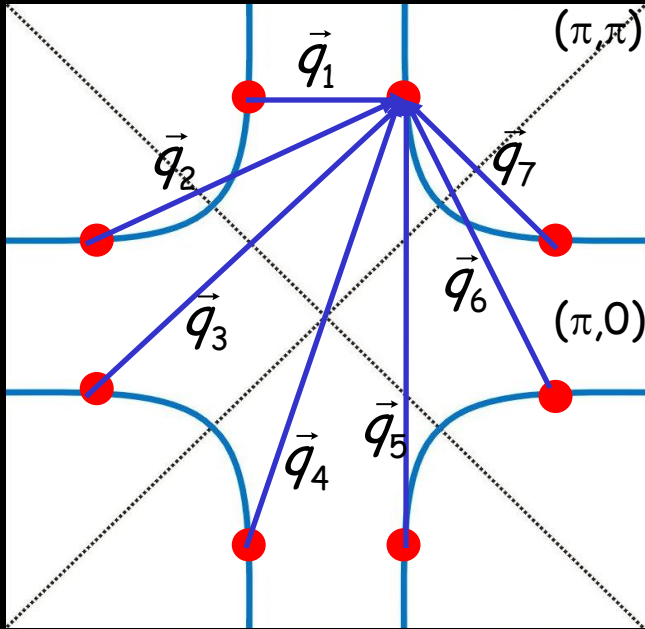
Expected energy dependence of $|\vec{q}_7|$



Expected energy dependence of $|\vec{q}_7|$

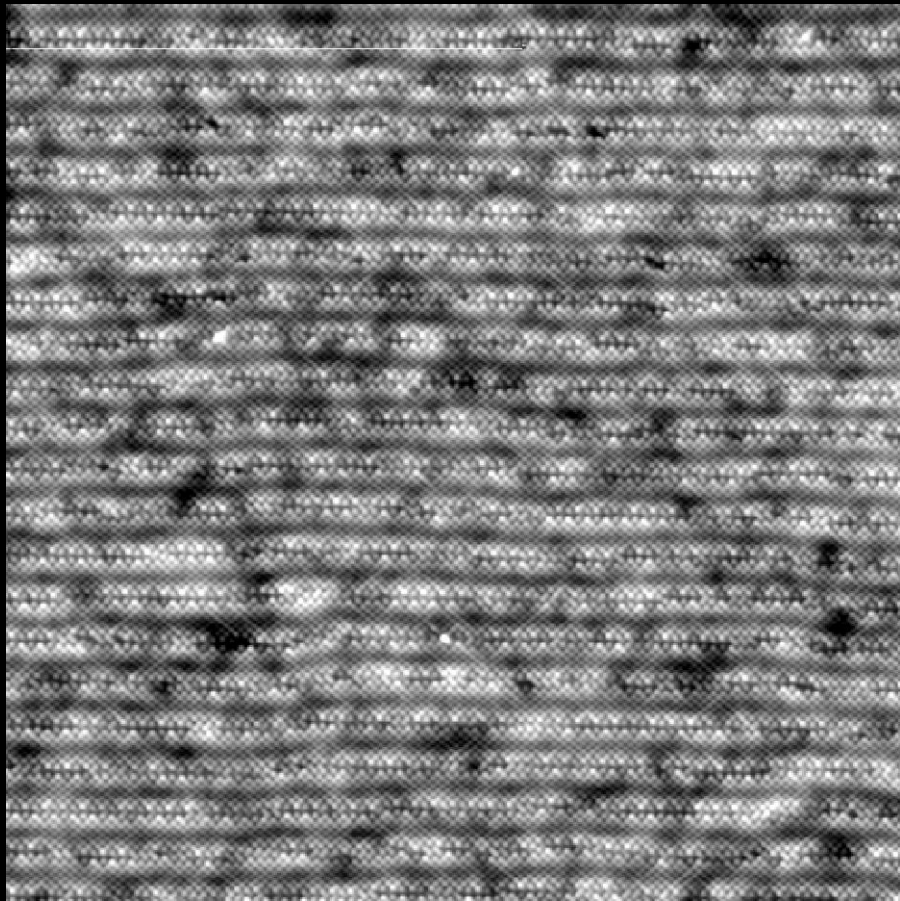


Expected energy dependence of 5 independent q_i 's



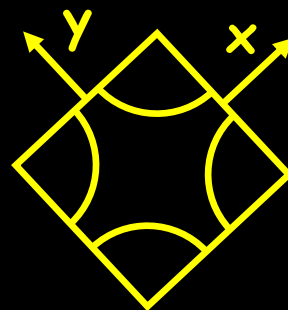
Bi₂Sr₂CaCu₂O_{8+d} Data

topograph



545 Å

Bi-2212
 $T_c = 76$ K
 $\Delta \sim 51$ meV

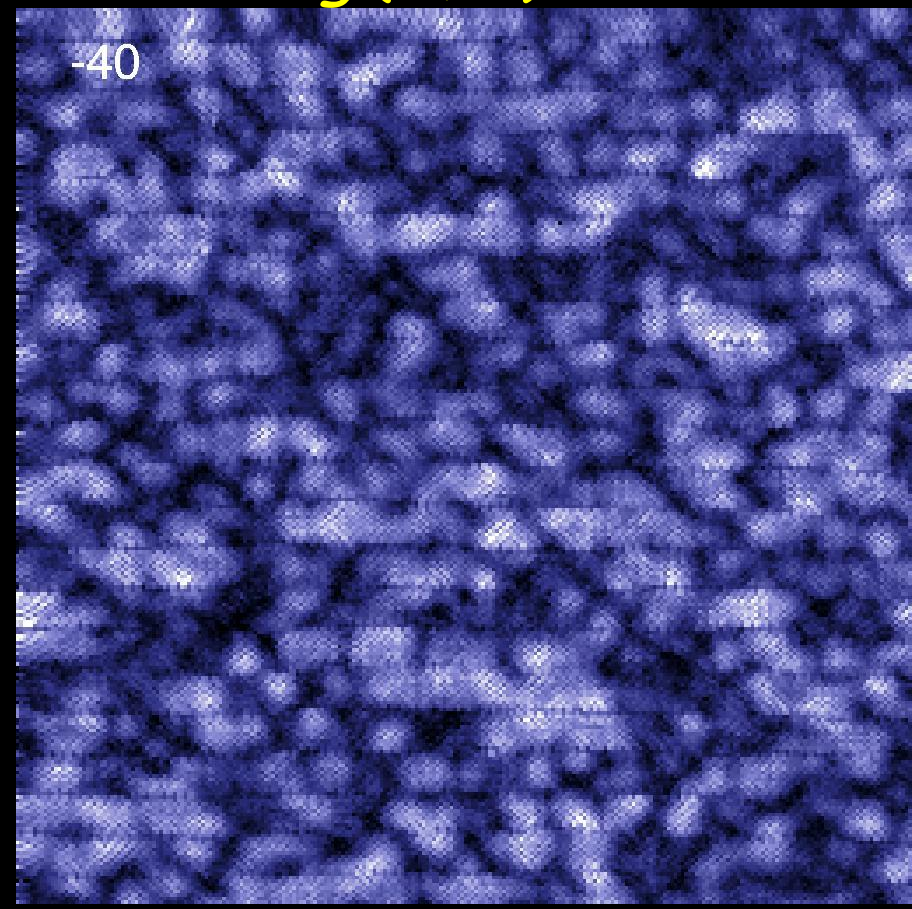


Imaging quasiparticle wavefunctions

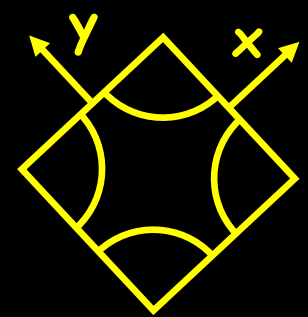
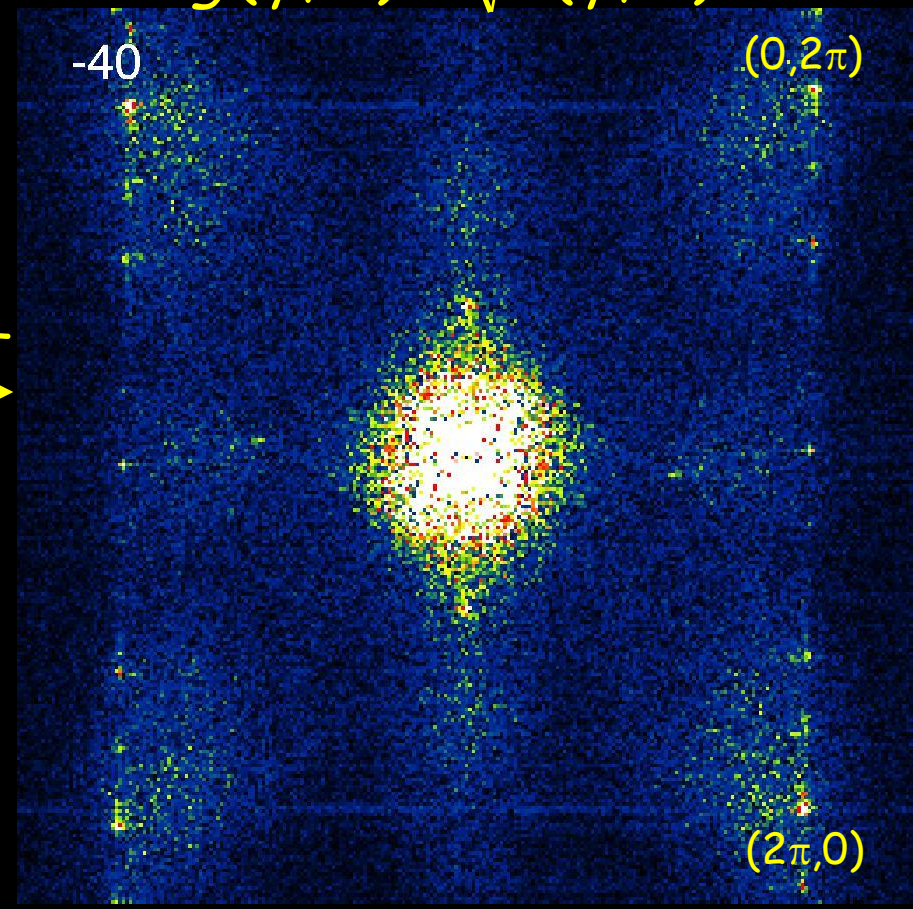
energy
(meV)
↓

$$g(\vec{r}, E)$$

$$g(\vec{q}, E) = \sqrt{P(\vec{q}, E)}$$



FFT
→



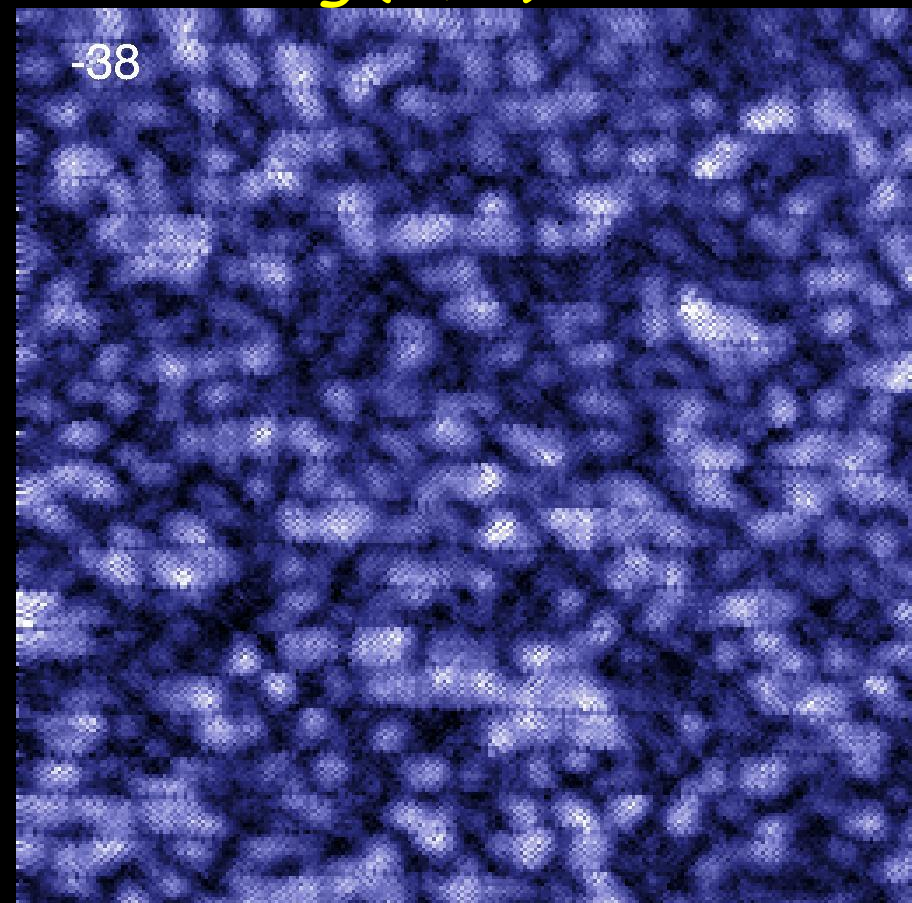
Bi-2212
 $T_c = 76$ K
 $\Delta \sim 51$ meV

Imaging quasiparticle wavefunctions

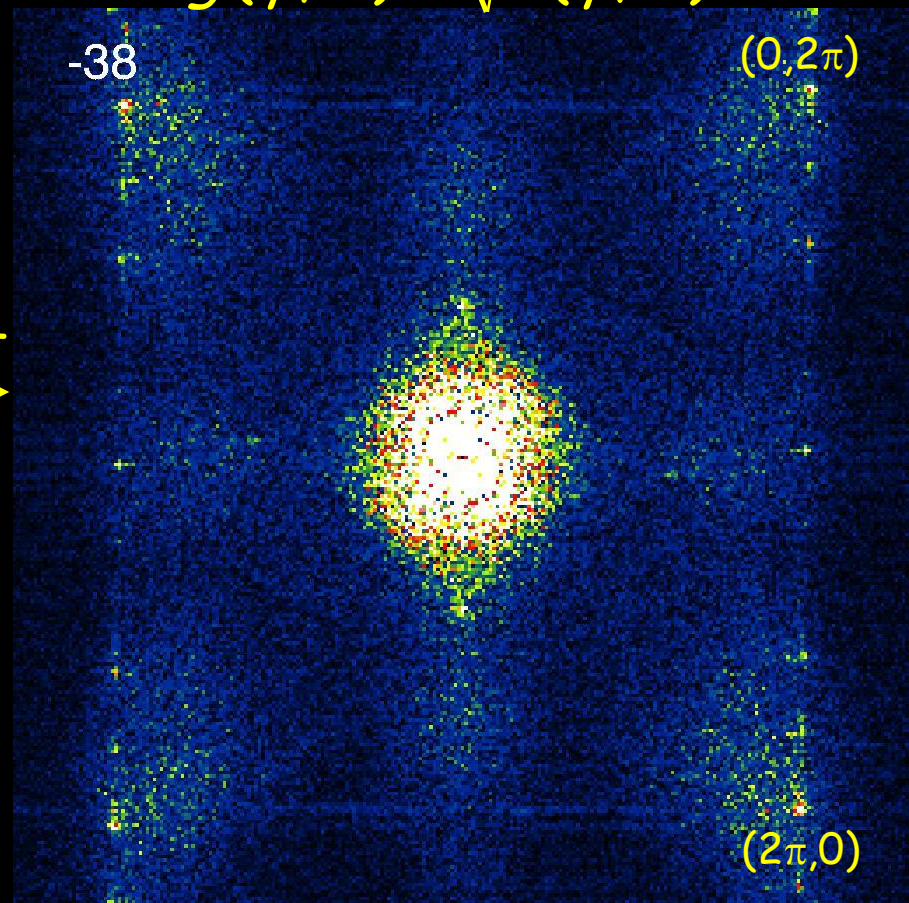
energy
(meV)
↓

$$g(\vec{r}, E)$$

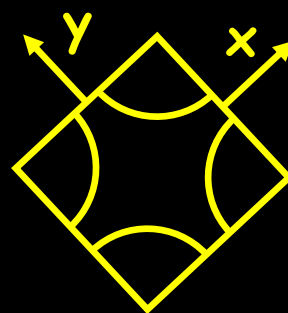
$$g(\vec{q}, E) = \sqrt{P(\vec{q}, E)}$$



FFT
→



Bi-2212
 $T_c = 76$ K
 $\Delta \sim 51$ meV

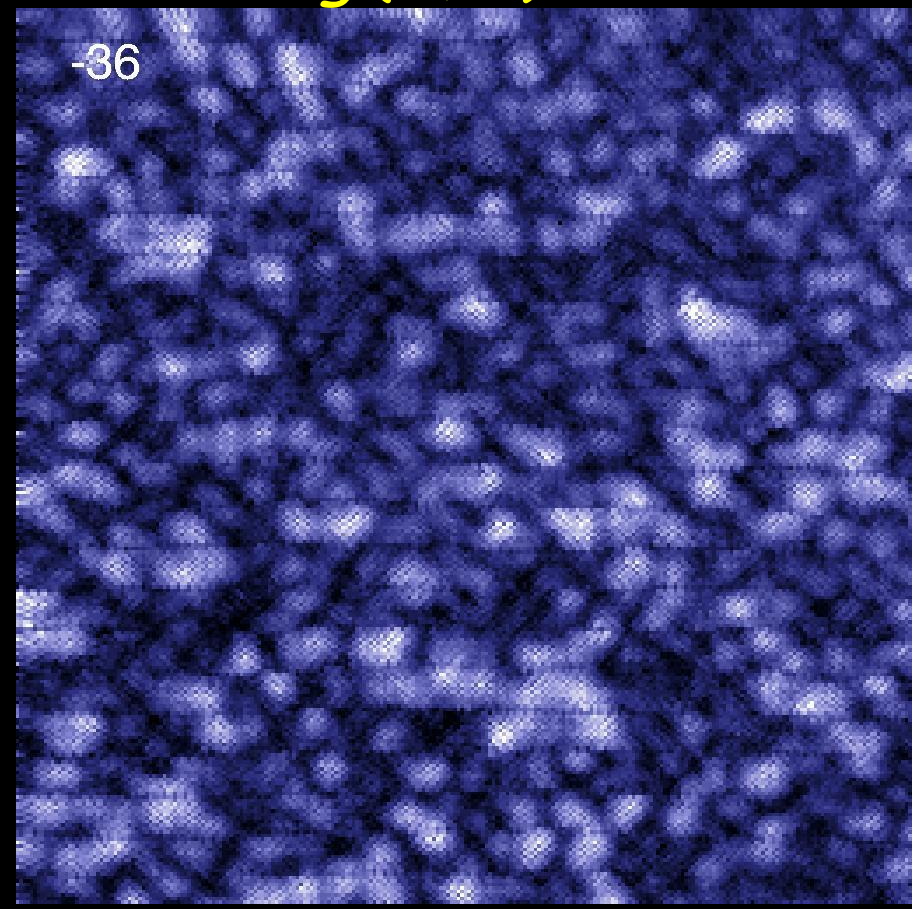


Imaging quasiparticle wavefunctions

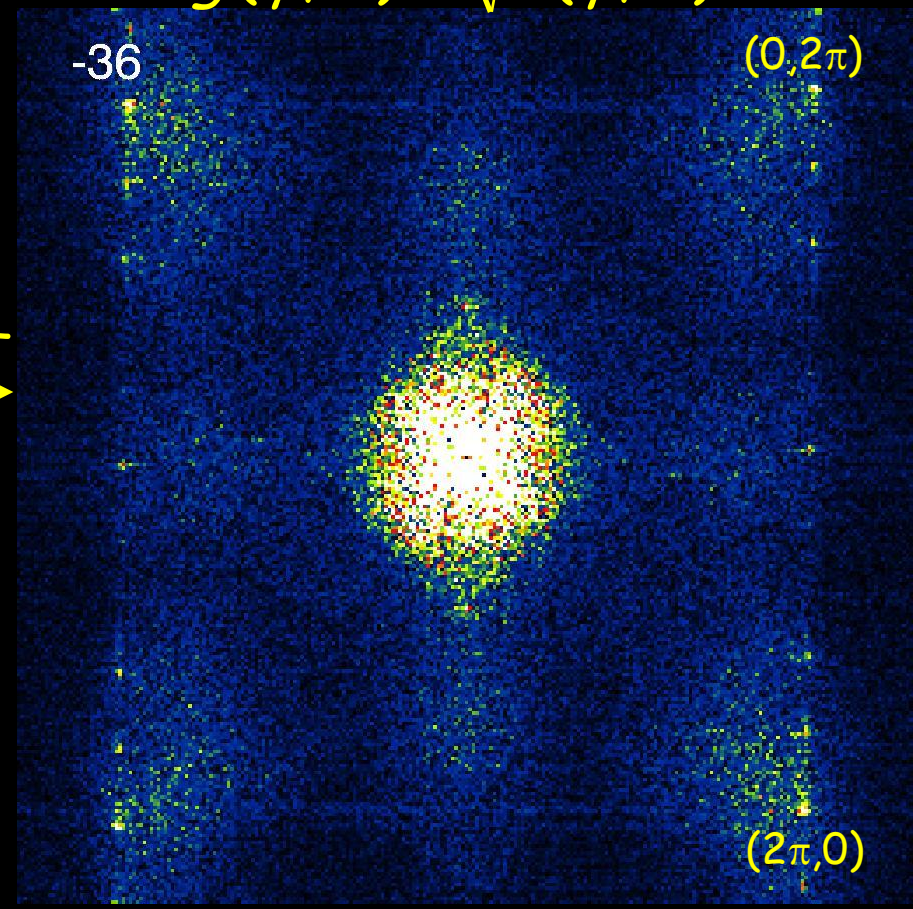
energy
(meV)
↓

$$g(\vec{r}, E)$$

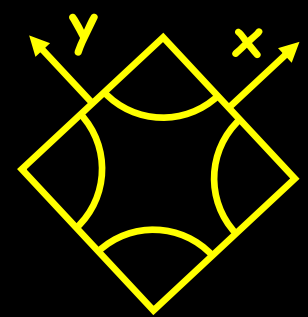
$$g(\vec{q}, E) = \sqrt{P(\vec{q}, E)}$$



FFT
→



Bi-2212
 $T_c = 76$ K
 $\Delta \sim 51$ meV

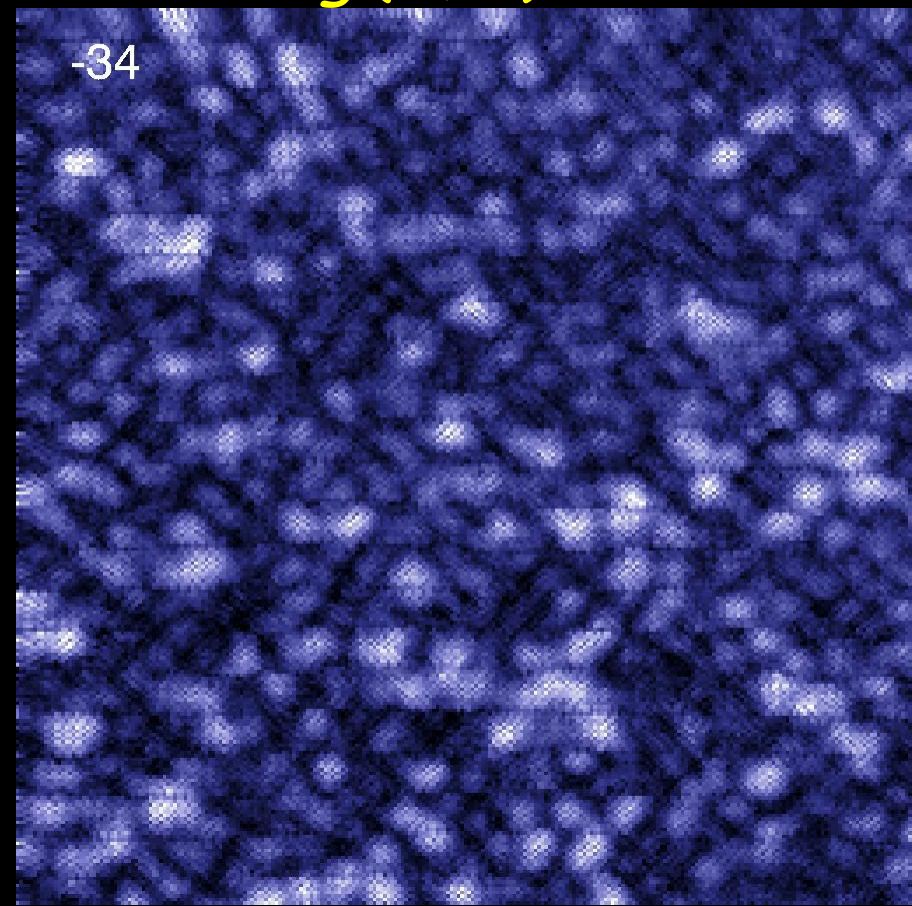


Imaging quasiparticle wavefunctions

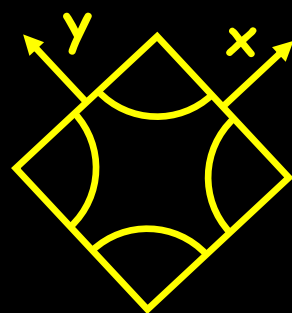
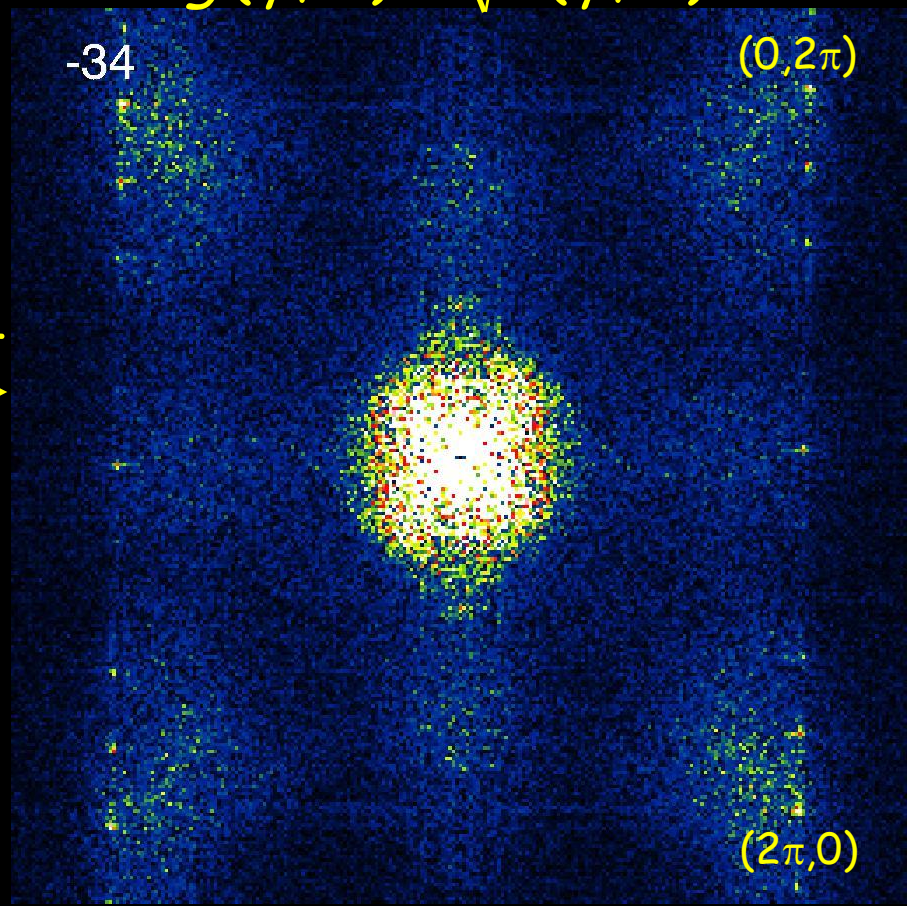
energy
(meV)
↓

$$g(\vec{r}, E)$$

$$g(\vec{q}, E) = \sqrt{P(\vec{q}, E)}$$



FFT
→



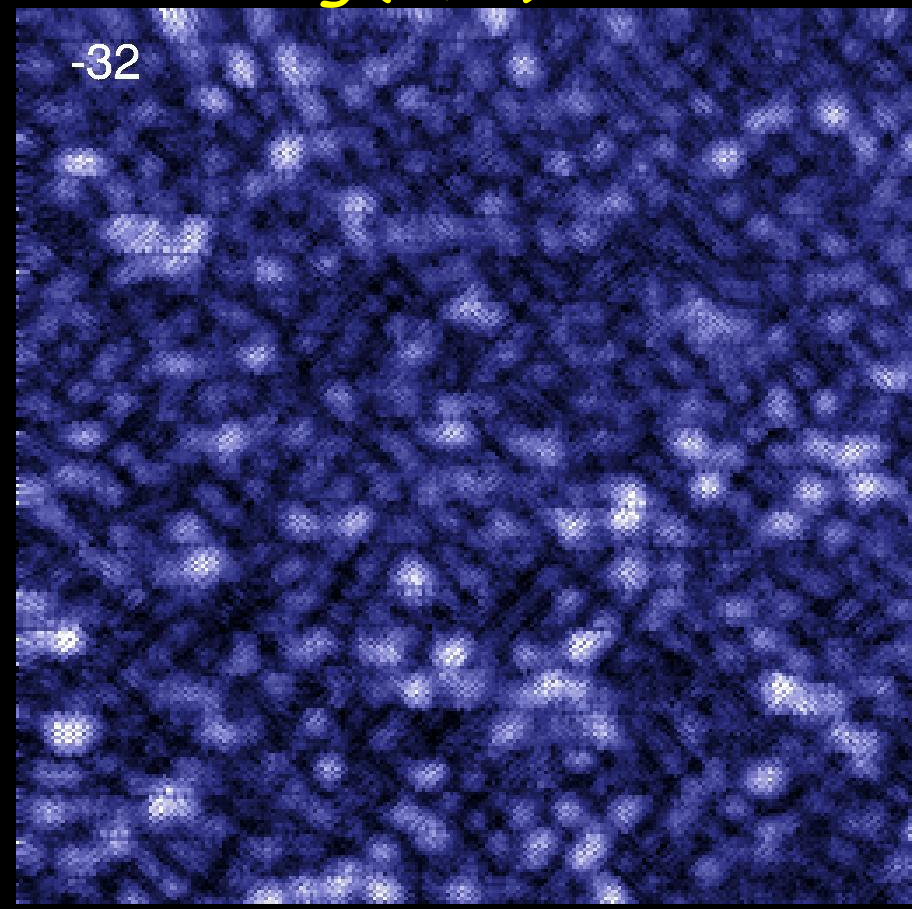
Bi-2212
 $T_c = 76$ K
 $\Delta \sim 51$ meV

Imaging quasiparticle wavefunctions

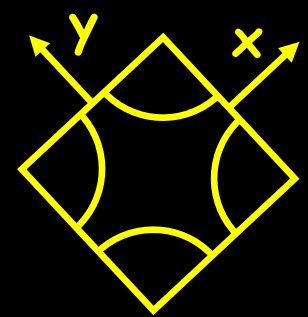
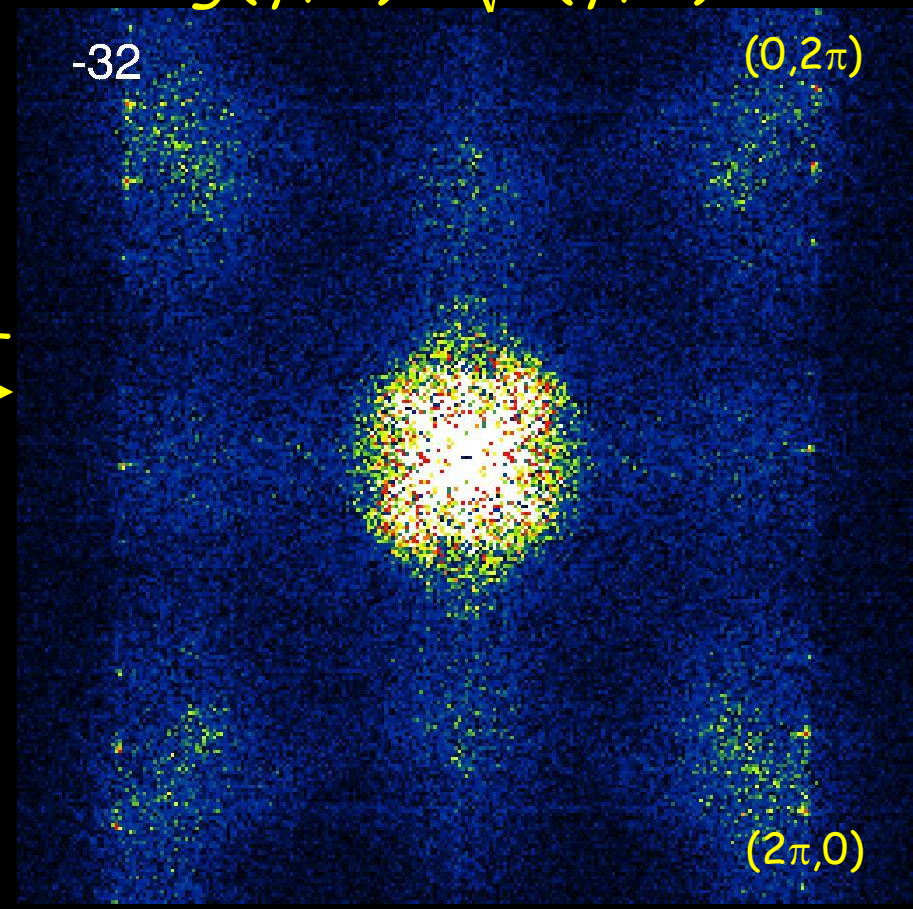
energy
(meV)
↓

$$g(\vec{r}, E)$$

$$g(\vec{q}, E) = \sqrt{P(\vec{q}, E)}$$



FFT
→



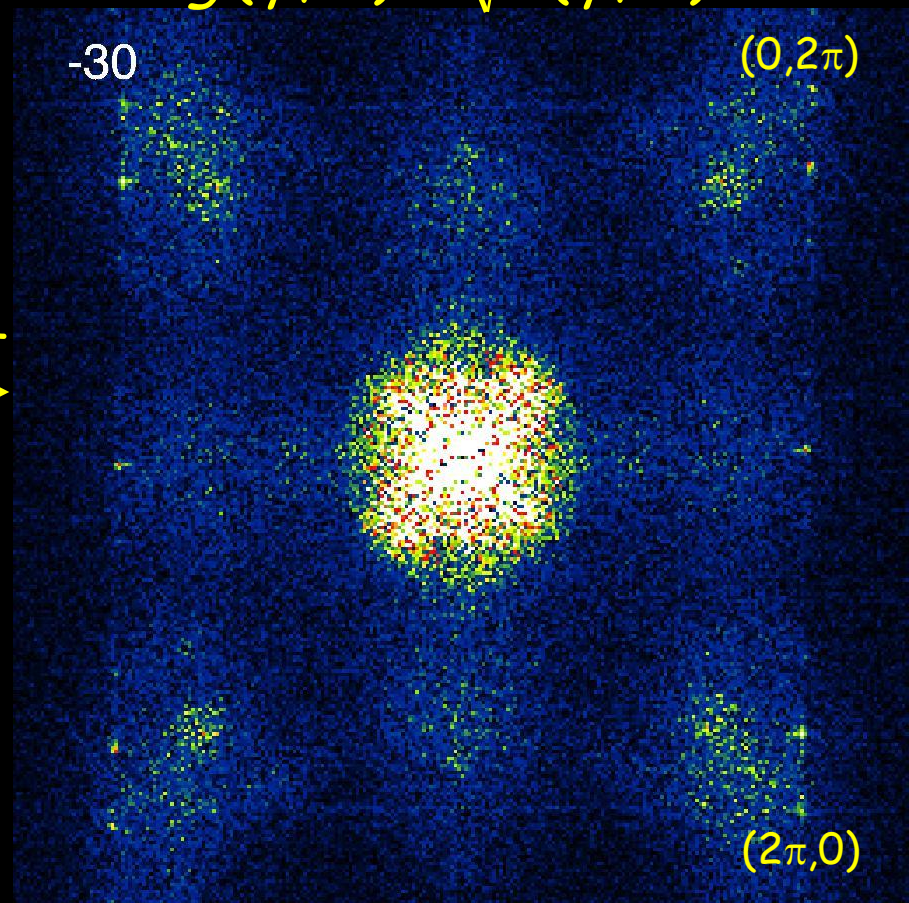
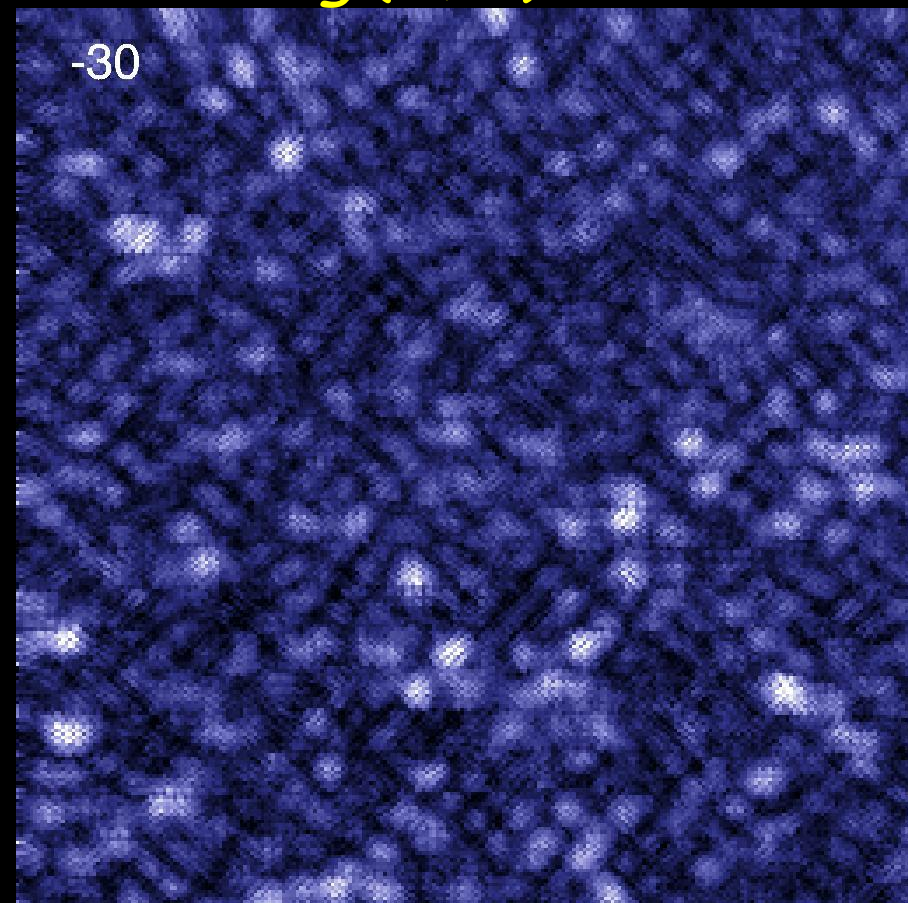
Bi-2212
 $T_c = 76$ K
 $\Delta \sim 51$ meV

Imaging quasiparticle wavefunctions

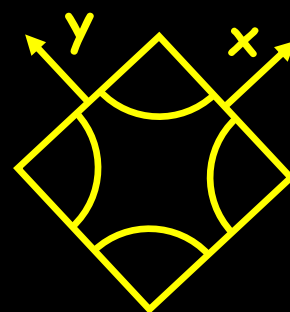
energy
(meV)
↓

$$g(\vec{r}, E)$$

$$g(\vec{q}, E) = \sqrt{P(\vec{q}, E)}$$



Bi-2212
 $T_c = 76$ K
 $\Delta \sim 51$ meV

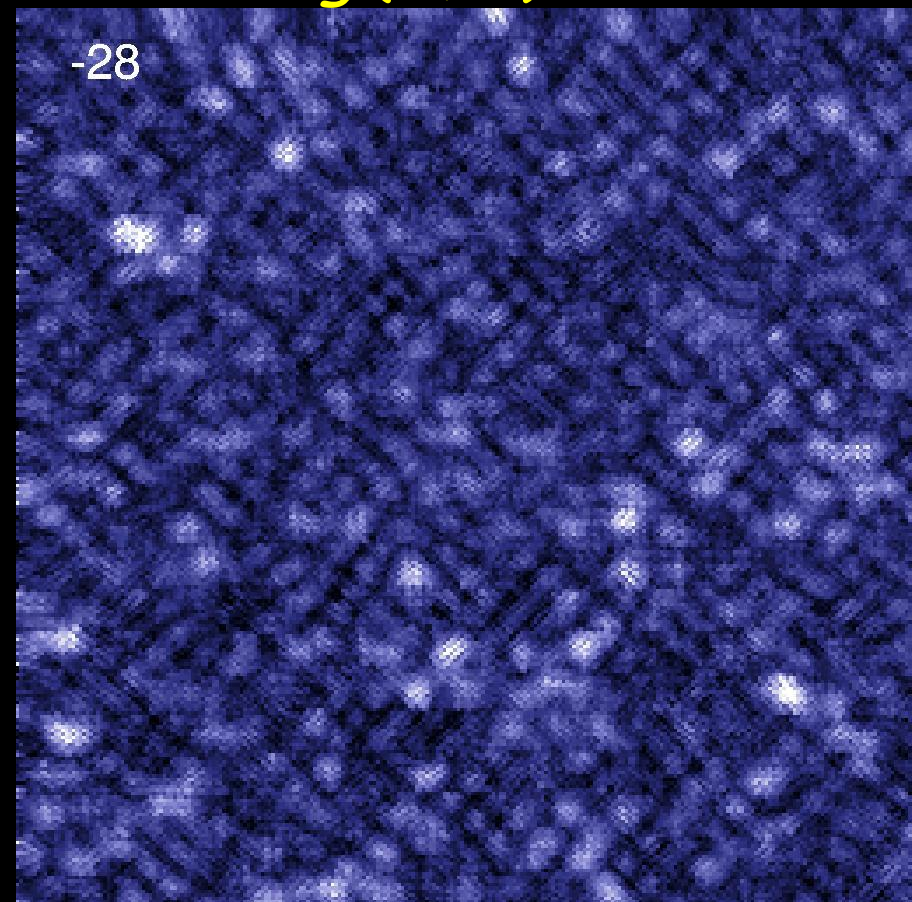


Imaging quasiparticle wavefunctions

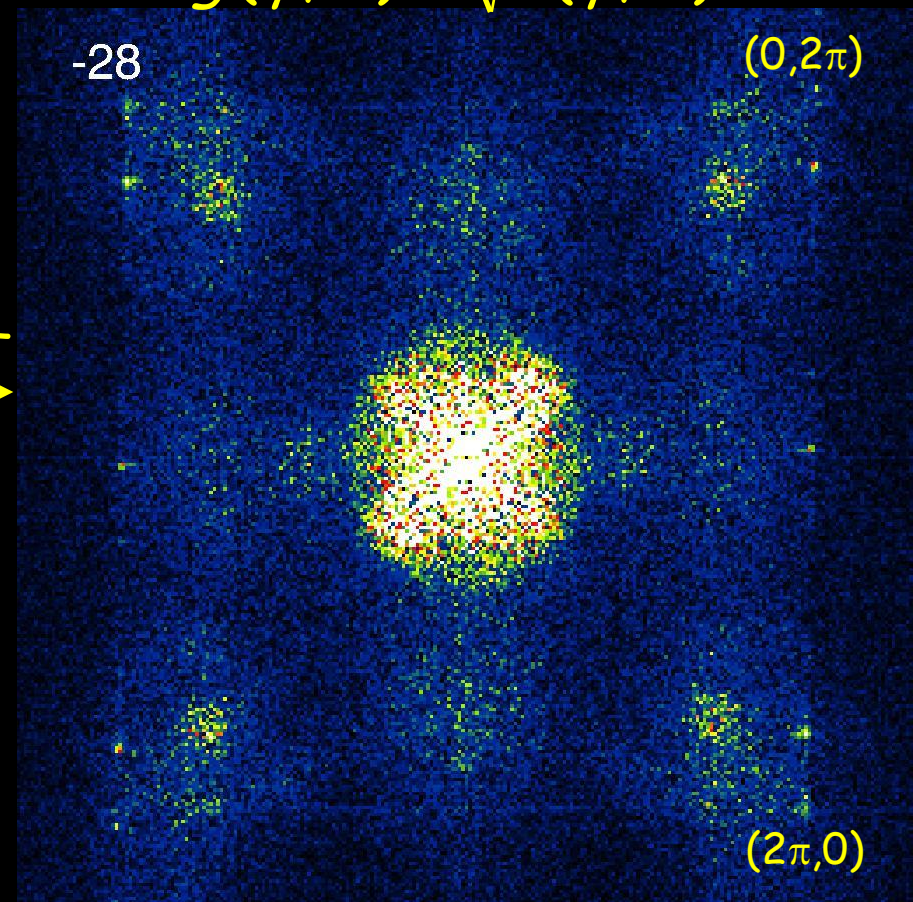
energy
(meV)
↓

$$g(\vec{r}, E)$$

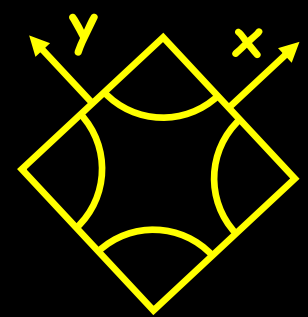
$$g(\vec{q}, E) = \sqrt{P(\vec{q}, E)}$$



FFT
→



Bi-2212
 $T_c = 76$ K
 $\Delta \sim 51$ meV

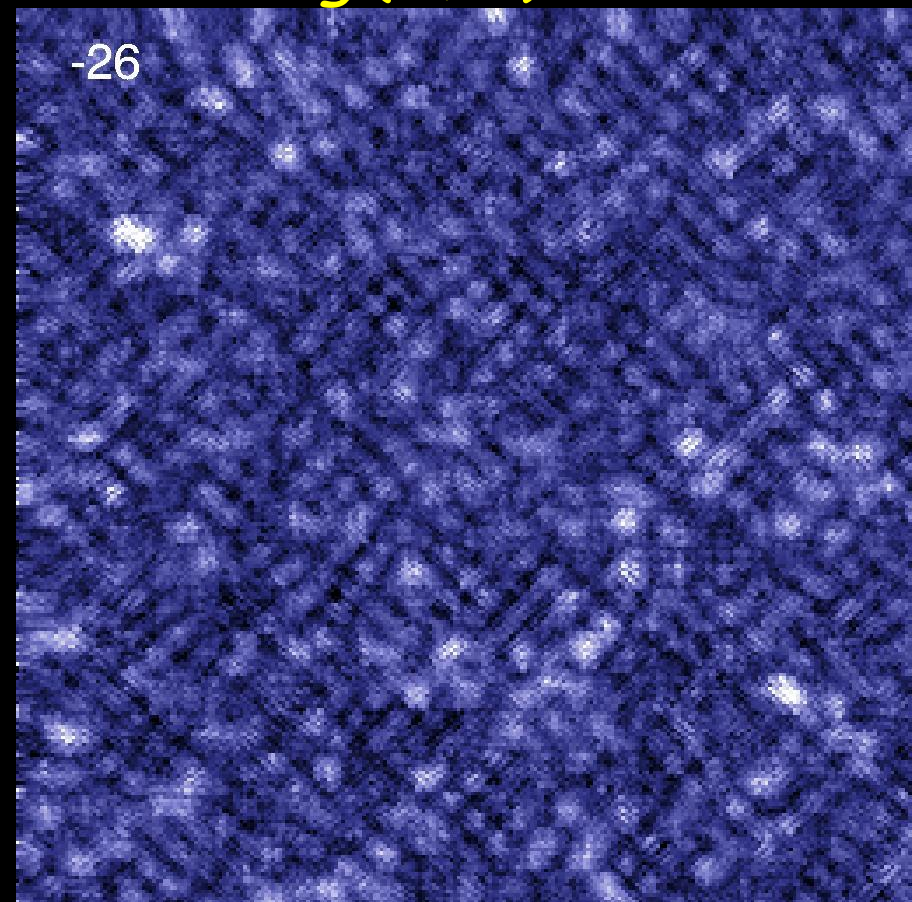


Imaging quasiparticle wavefunctions

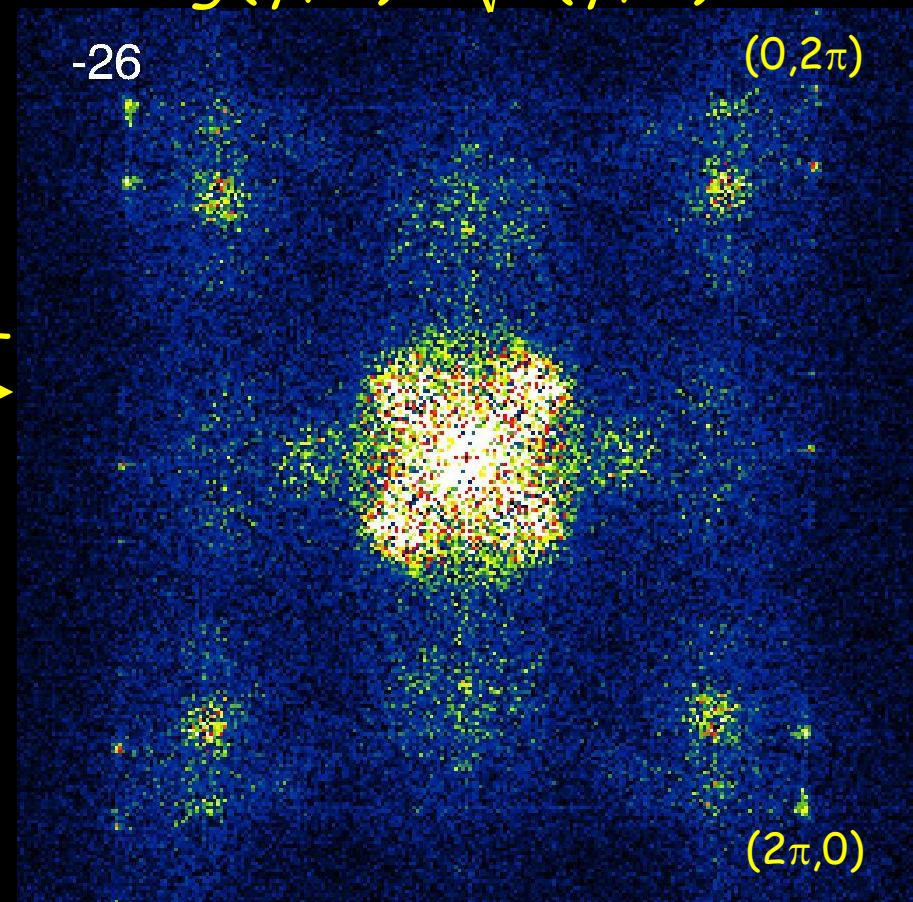
energy
(meV)
↓

$$g(\vec{r}, E)$$

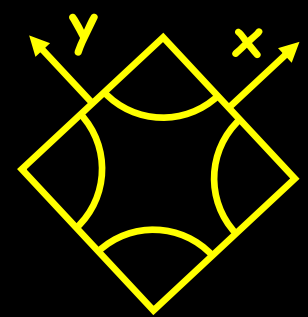
$$g(\vec{q}, E) = \sqrt{P(\vec{q}, E)}$$



FFT
→



Bi-2212
 $T_c = 76$ K
 $\Delta \sim 51$ meV

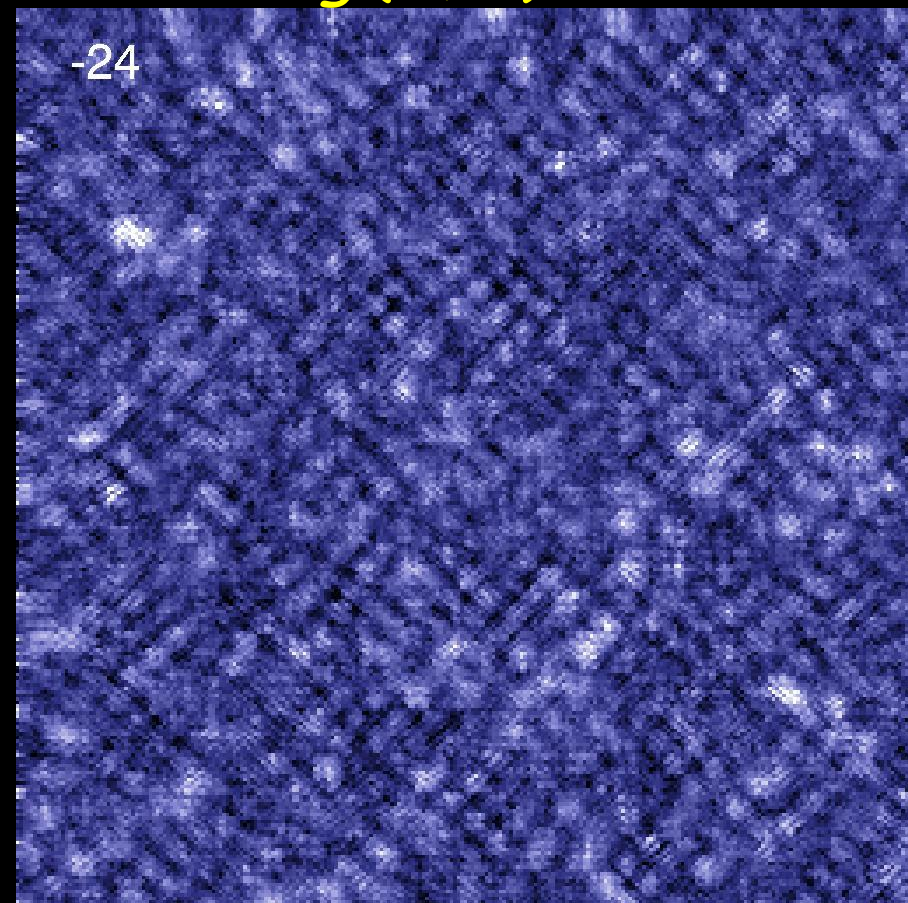


Imaging quasiparticle wavefunctions

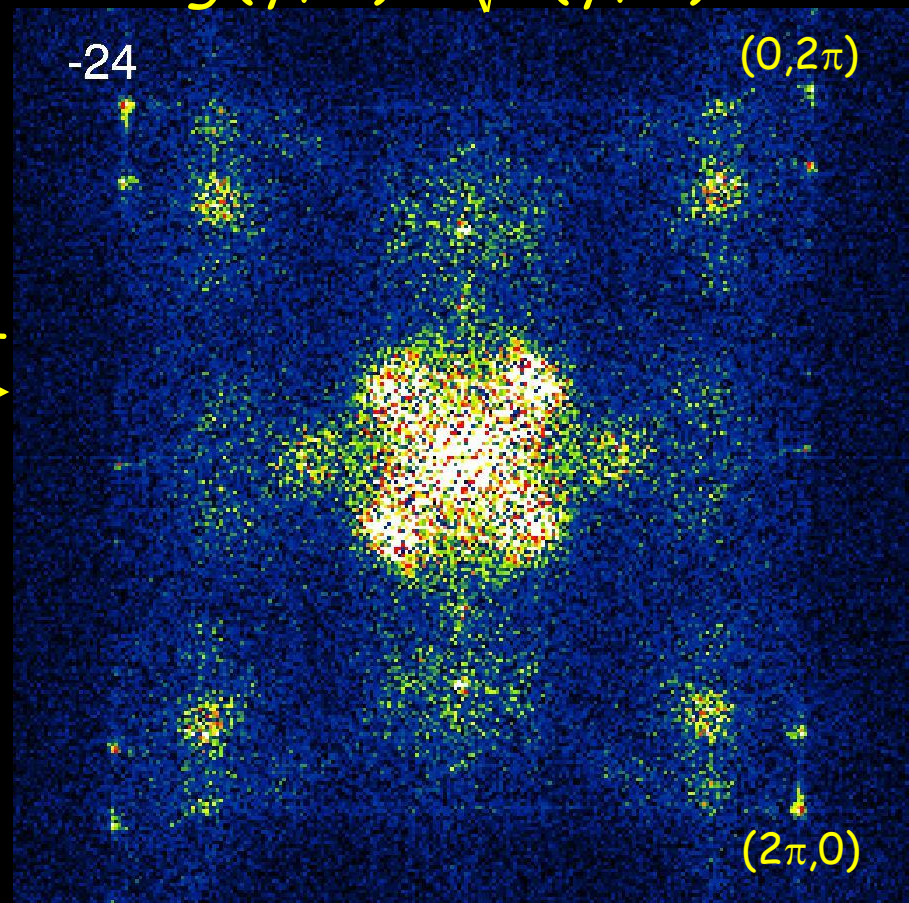
energy
(meV)
↓

$$g(\vec{r}, E)$$

$$g(\vec{q}, E) = \sqrt{P(\vec{q}, E)}$$

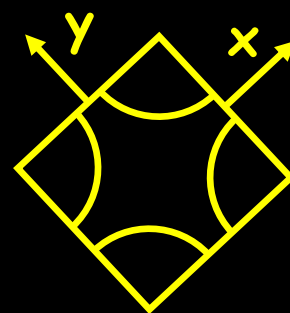


FFT
→



← 545 Å →

Bi-2212
 $T_c = 76$ K
 $\Delta \sim 51$ meV

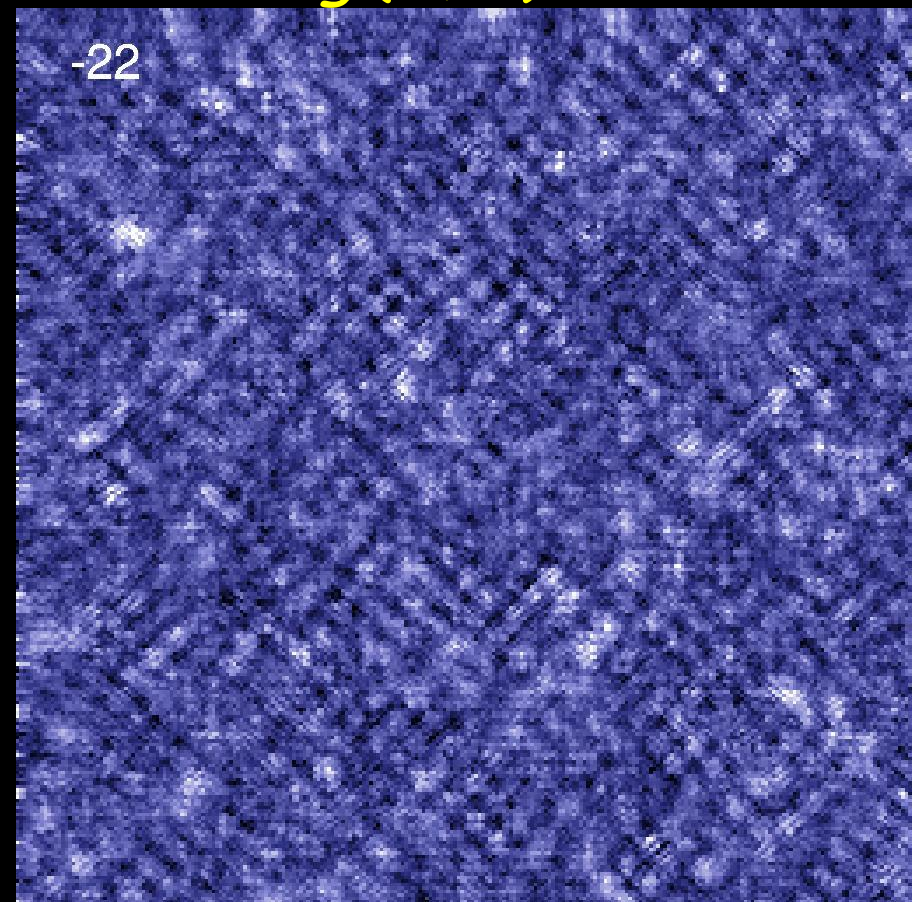


Imaging quasiparticle wavefunctions

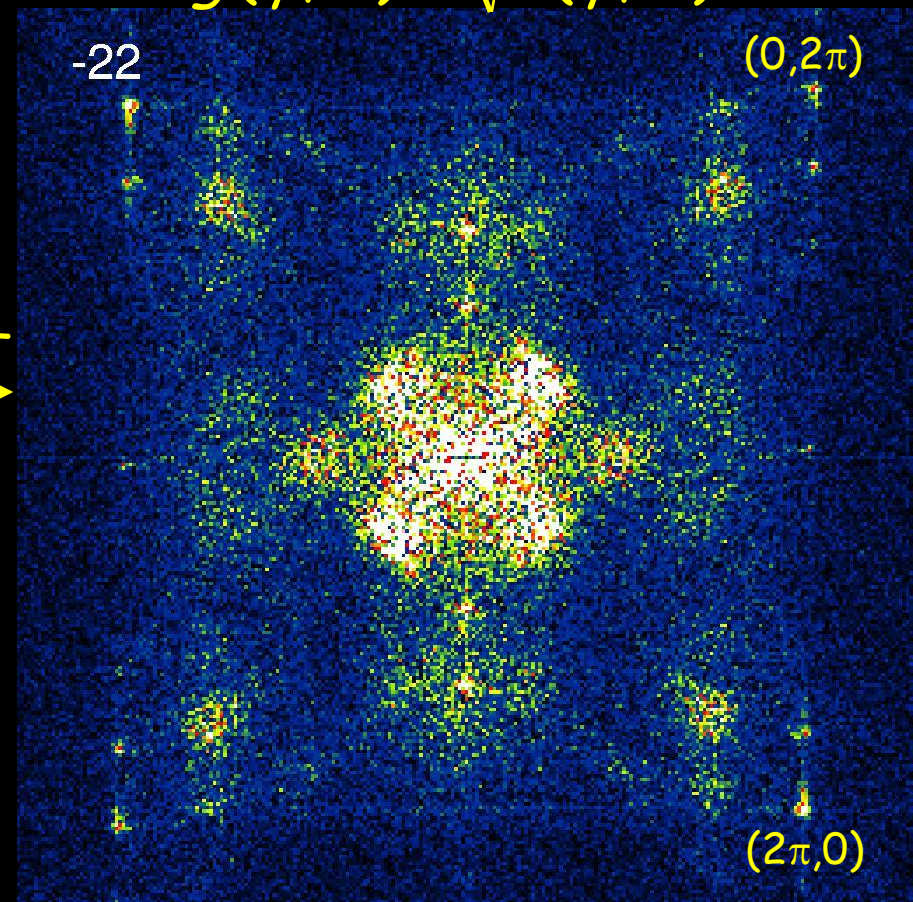
energy
(meV)
↓

$$g(\vec{r}, E)$$

$$g(\vec{q}, E) = \sqrt{P(\vec{q}, E)}$$

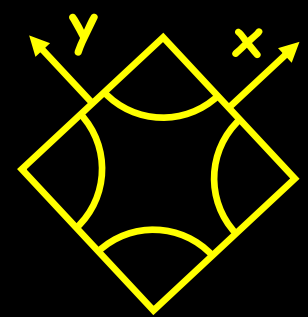


FFT
→



← 545 Å →

Bi-2212
 $T_c = 76$ K
 $\Delta \sim 51$ meV

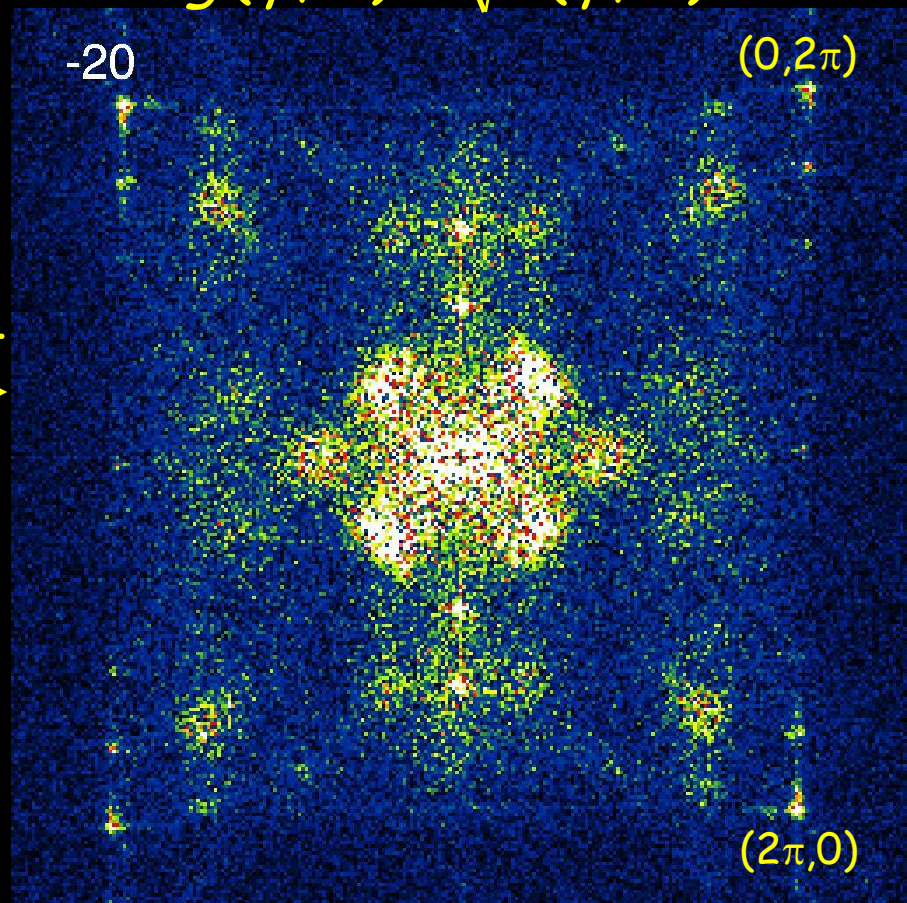
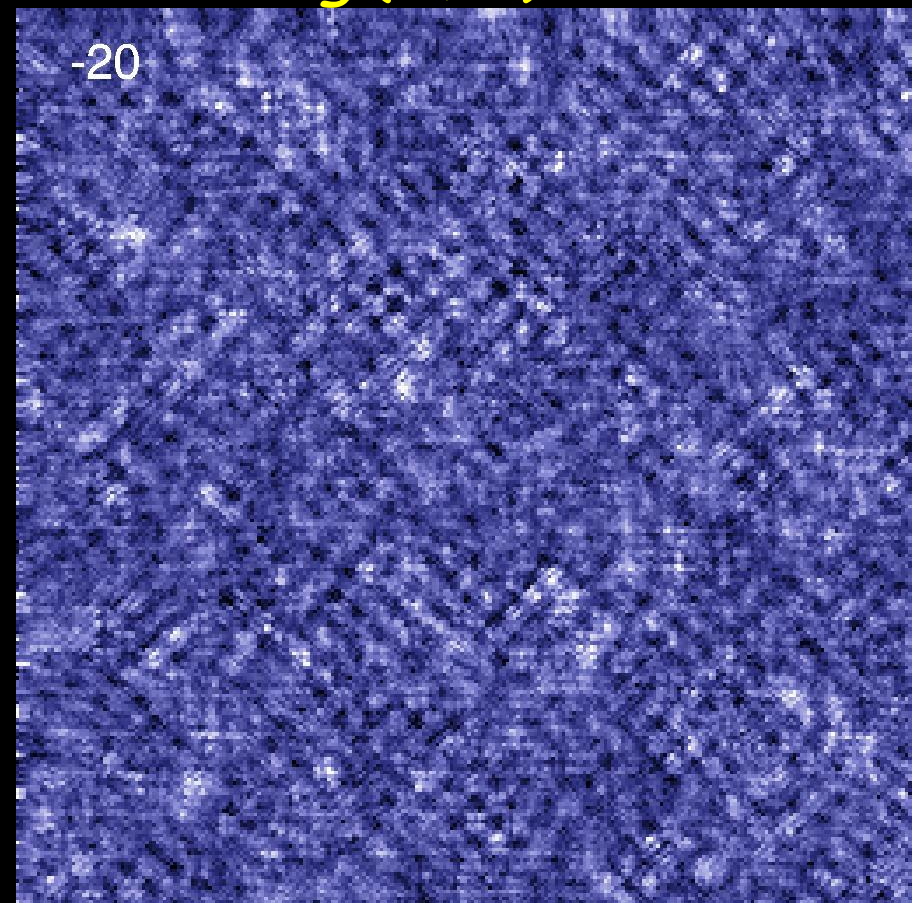


Imaging quasiparticle wavefunctions

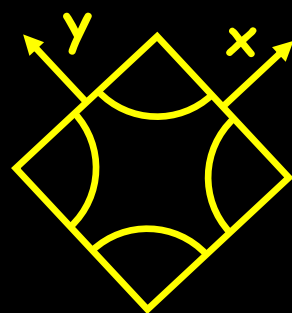
energy
(meV)
↓

$$g(\vec{r}, E)$$

$$g(\vec{q}, E) = \sqrt{P(\vec{q}, E)}$$



← 545 Å →



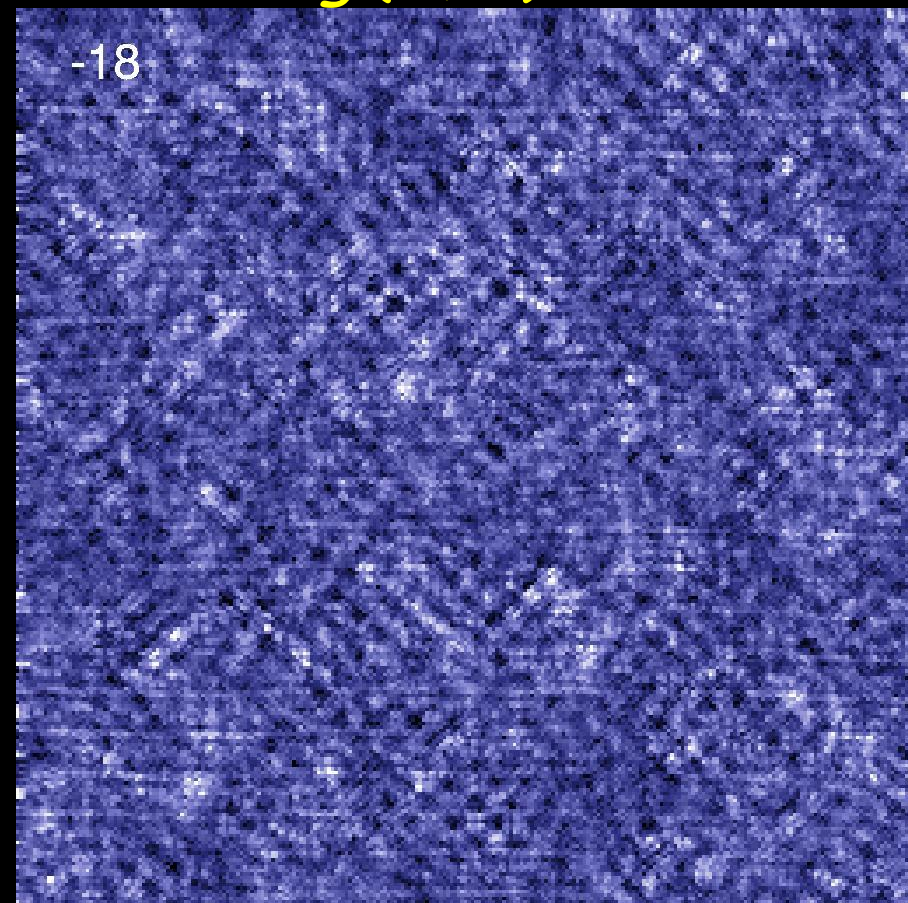
Bi-2212
 $T_c = 76$ K
 $\Delta \sim 51$ meV

Imaging quasiparticle wavefunctions

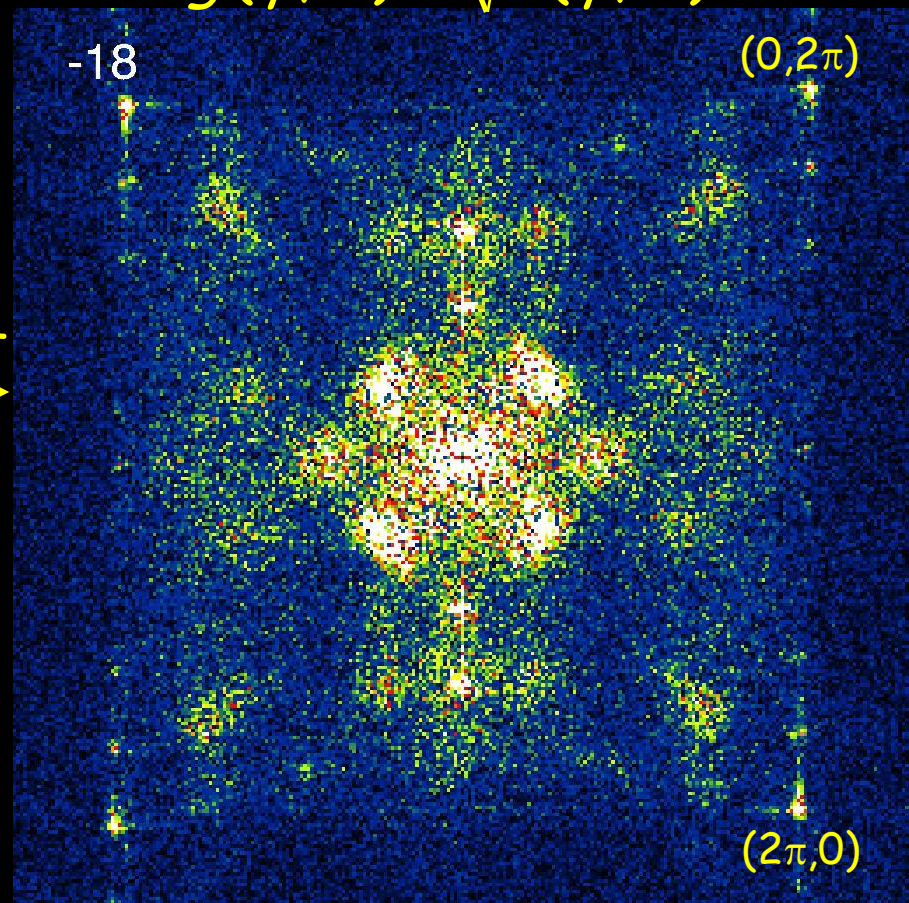
energy
(meV)
↓

$$g(\vec{r}, E)$$

$$g(\vec{q}, E) = \sqrt{P(\vec{q}, E)}$$

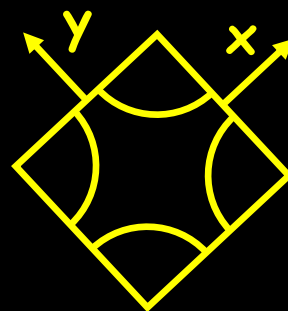


FFT
→



545 Å

Bi-2212
 $T_c = 76$ K
 $\Delta \sim 51$ meV

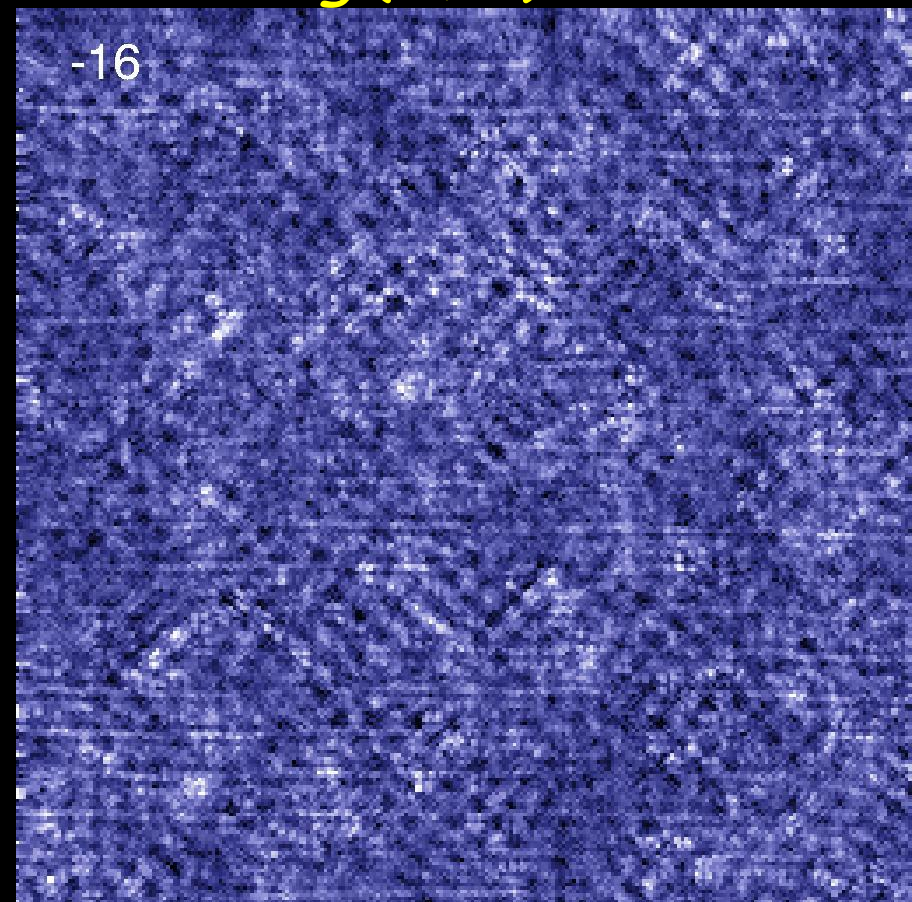


Imaging quasiparticle wavefunctions

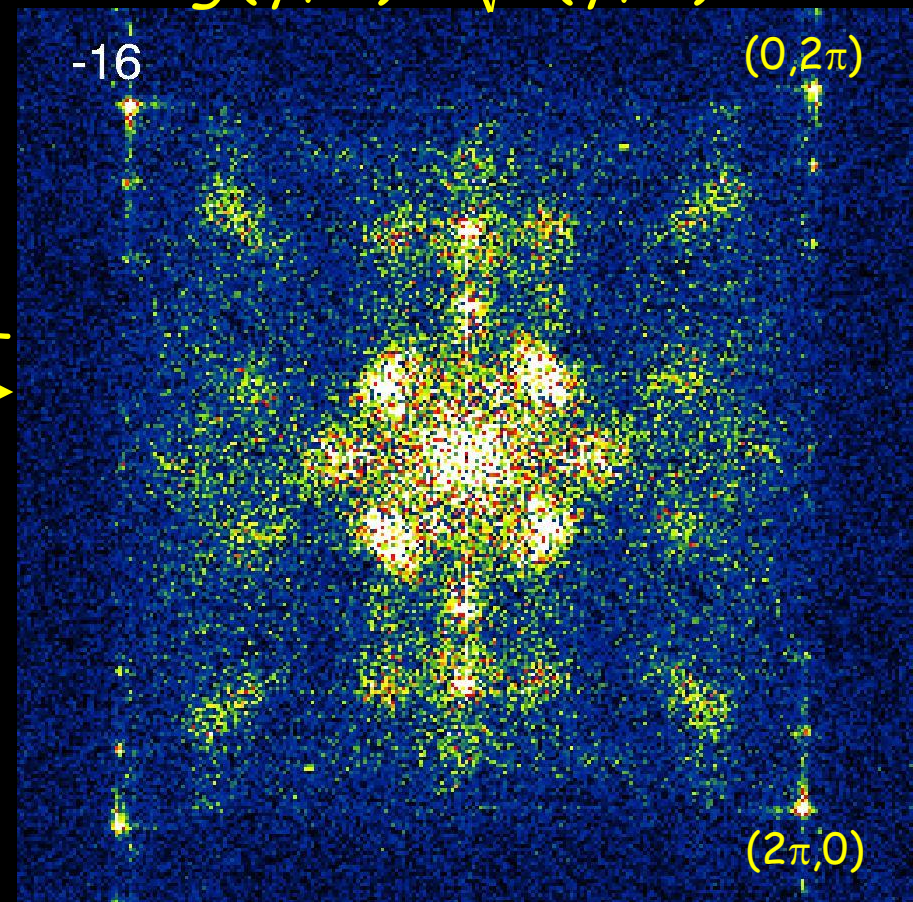
energy
(meV)
↓

$$g(\vec{r}, E)$$

$$g(\vec{q}, E) = \sqrt{P(\vec{q}, E)}$$

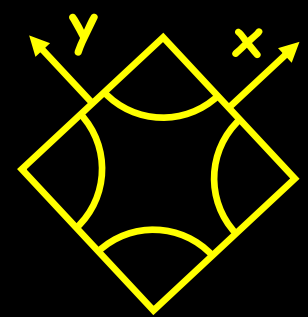


FFT
→



← 545 Å →

Bi-2212
 $T_c = 76$ K
 $\Delta \sim 51$ meV

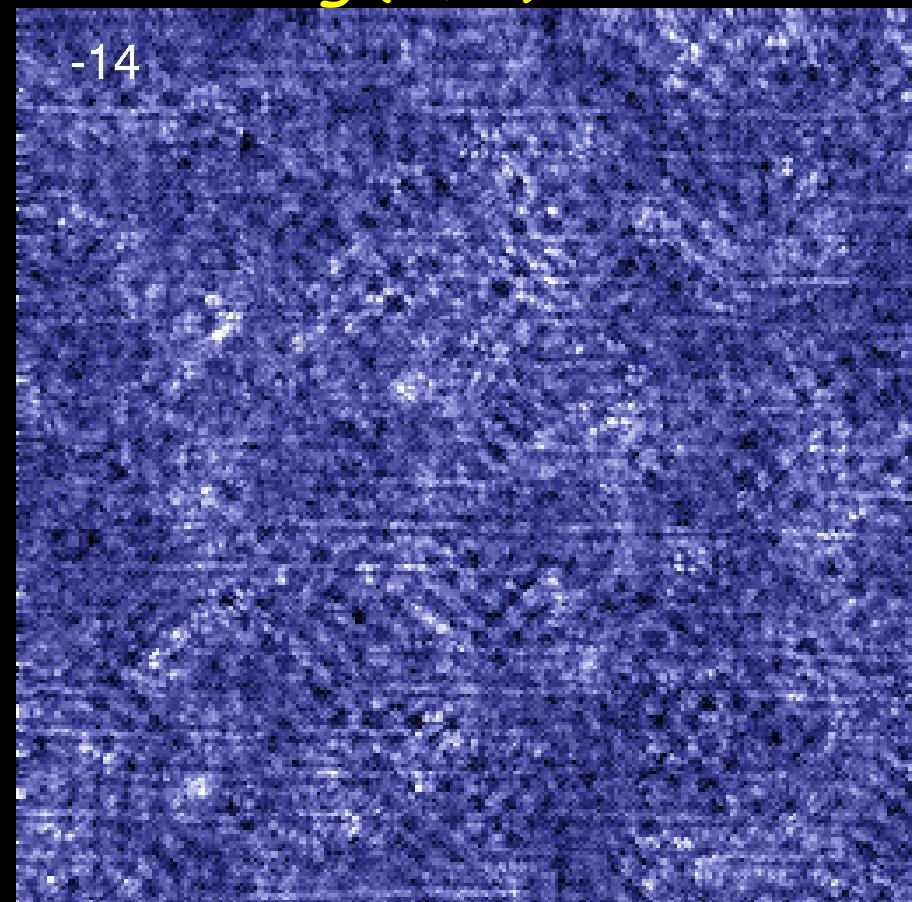


Imaging quasiparticle wavefunctions

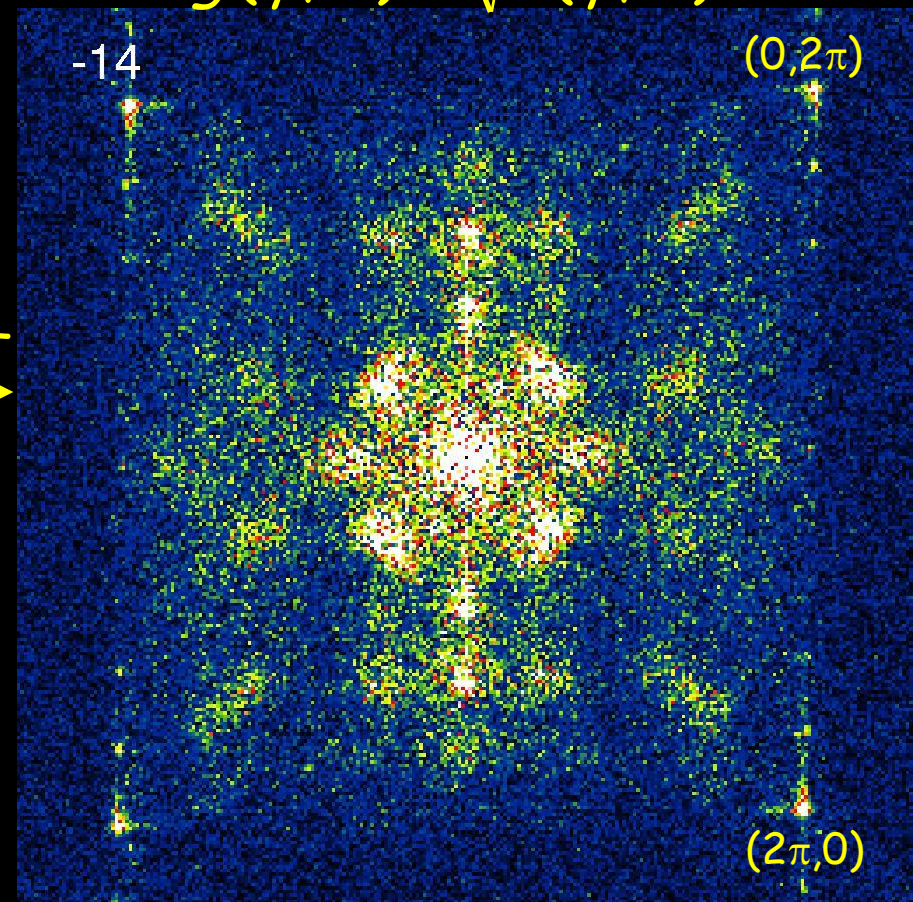
energy
(meV)
↓

$$g(\vec{r}, E)$$

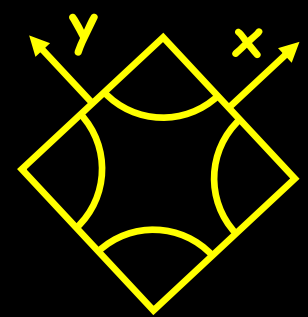
$$g(\vec{q}, E) = \sqrt{P(\vec{q}, E)}$$



FFT →



← 545 Å →



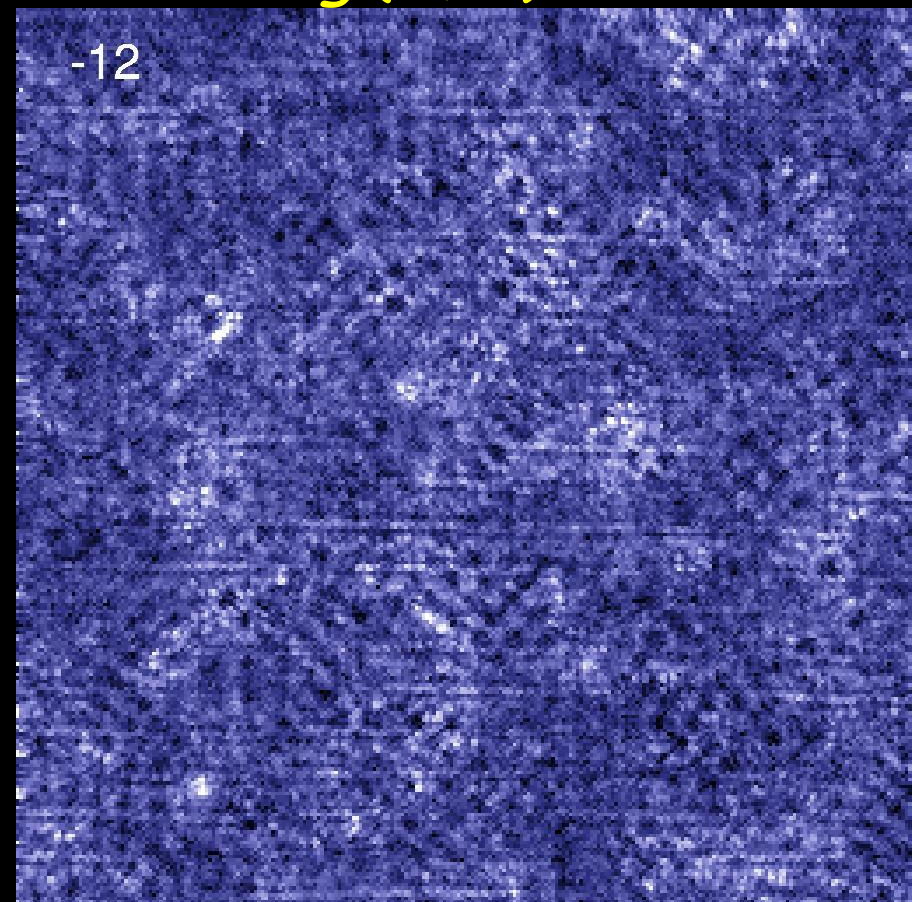
Bi-2212
 $T_c = 76$ K
 $\Delta \sim 51$ meV

Imaging quasiparticle wavefunctions

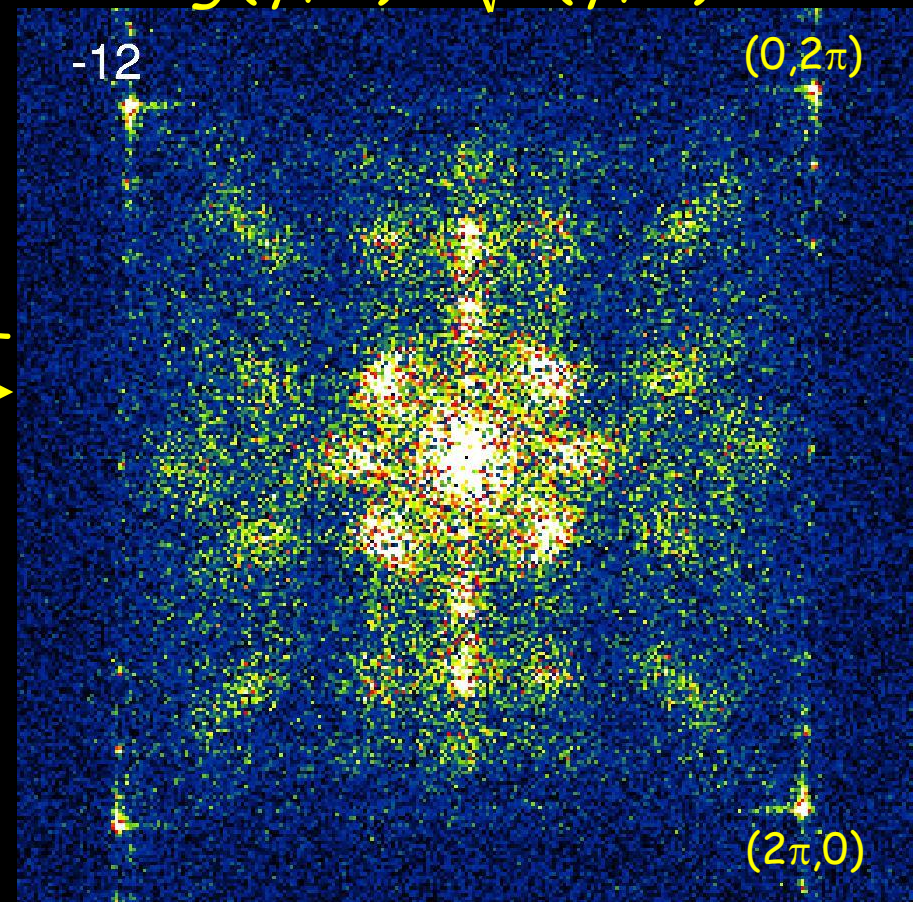
energy
(meV)
↓

$$g(\vec{r}, E)$$

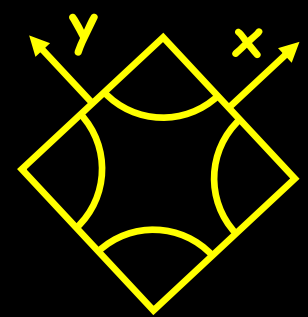
$$g(\vec{q}, E) = \sqrt{P(\vec{q}, E)}$$



FFT
→



Bi-2212
 $T_c = 76$ K
 $\Delta \sim 51$ meV

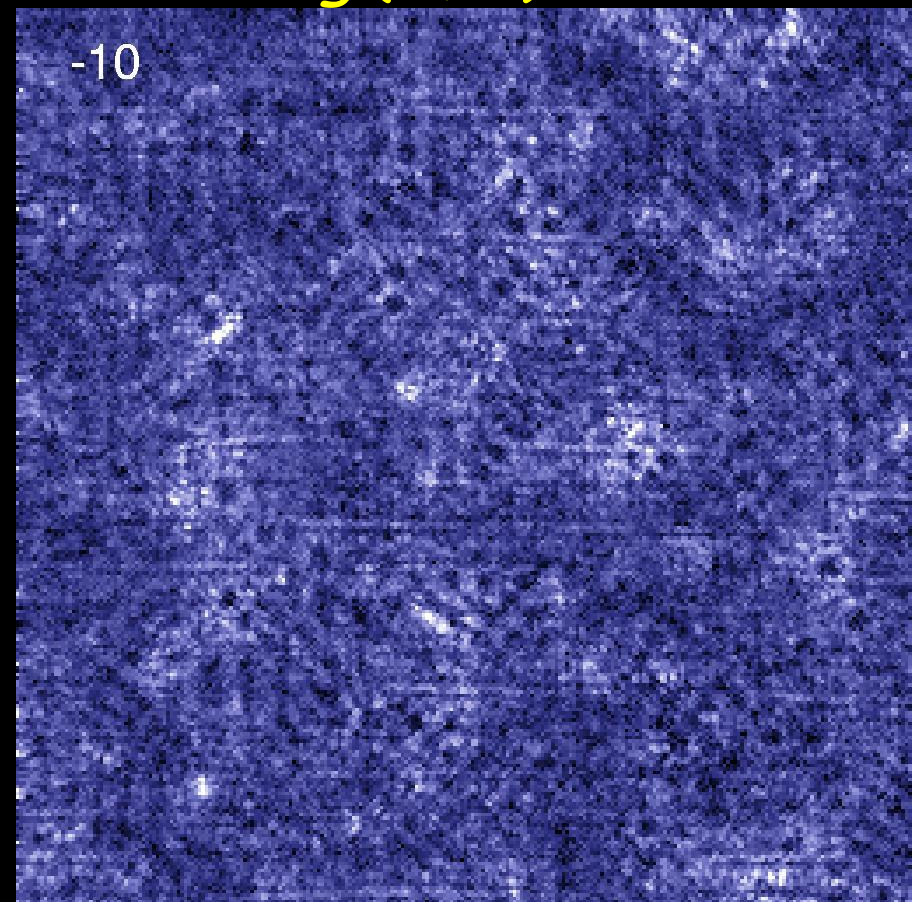


Imaging quasiparticle wavefunctions

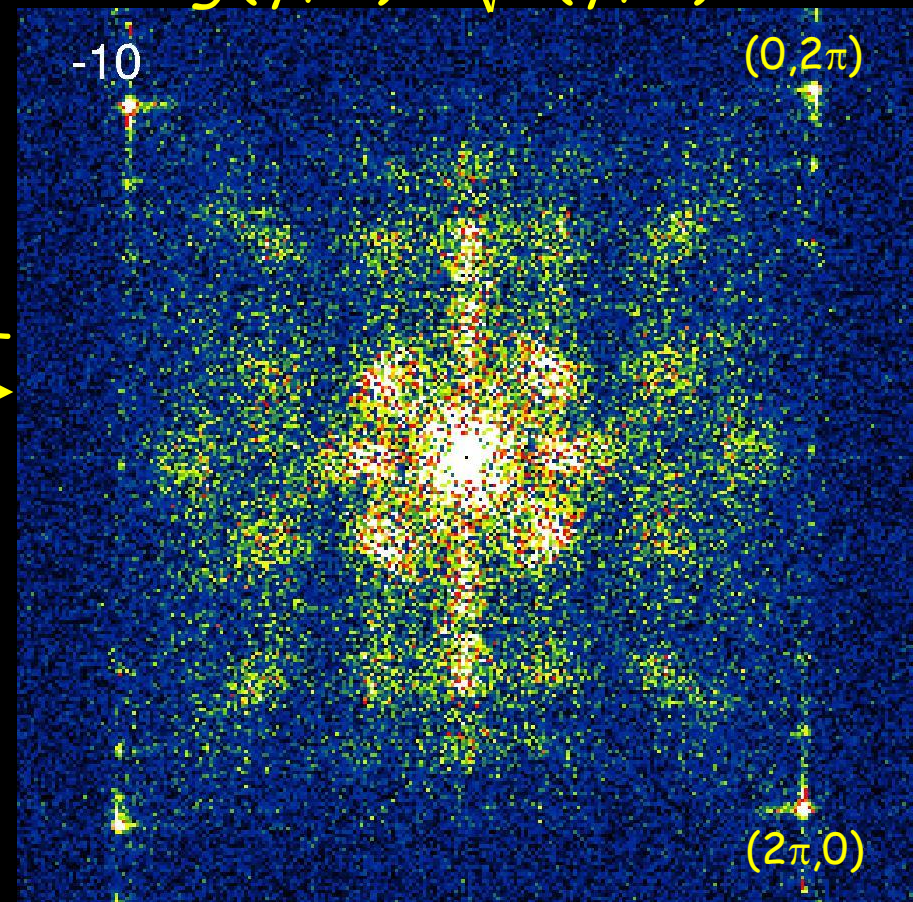
energy
(meV)
↓

$$g(\vec{r}, E)$$

$$g(\vec{q}, E) = \sqrt{P(\vec{q}, E)}$$

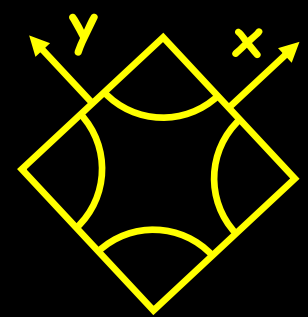


FFT →



← 545 Å →

Bi-2212
 $T_c = 76$ K
 $\Delta \sim 51$ meV

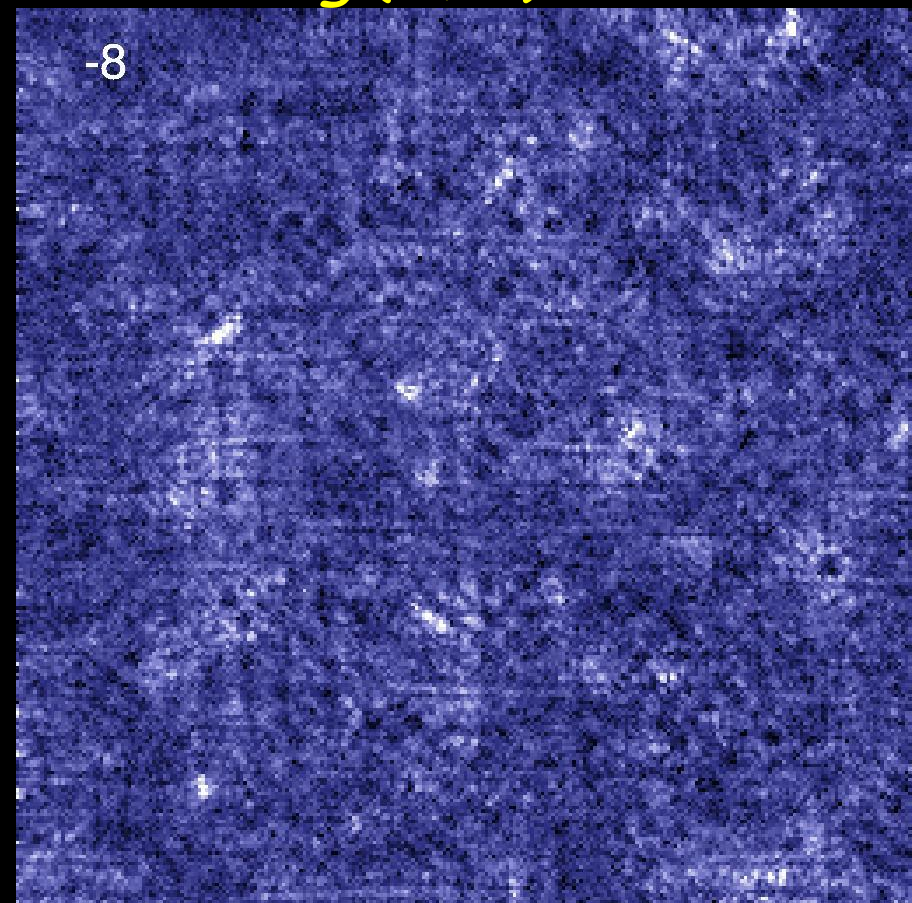


Imaging quasiparticle wavefunctions

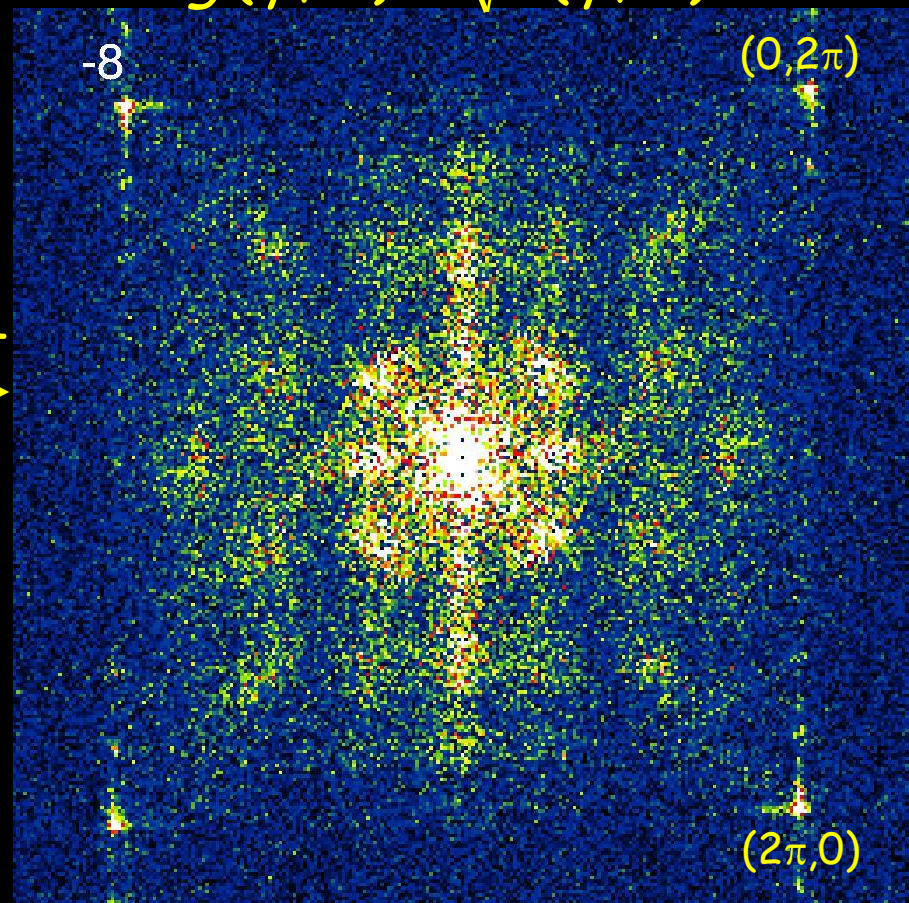
energy
(meV)
↓

$$g(\vec{r}, E)$$

$$g(\vec{q}, E) = \sqrt{P(\vec{q}, E)}$$

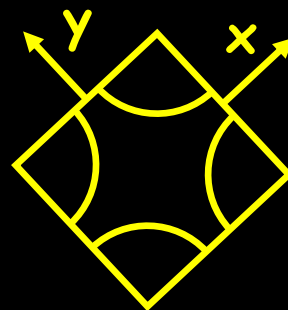


FFT
→



545 Å

Bi-2212
 $T_c = 76$ K
 $\Delta \sim 51$ meV

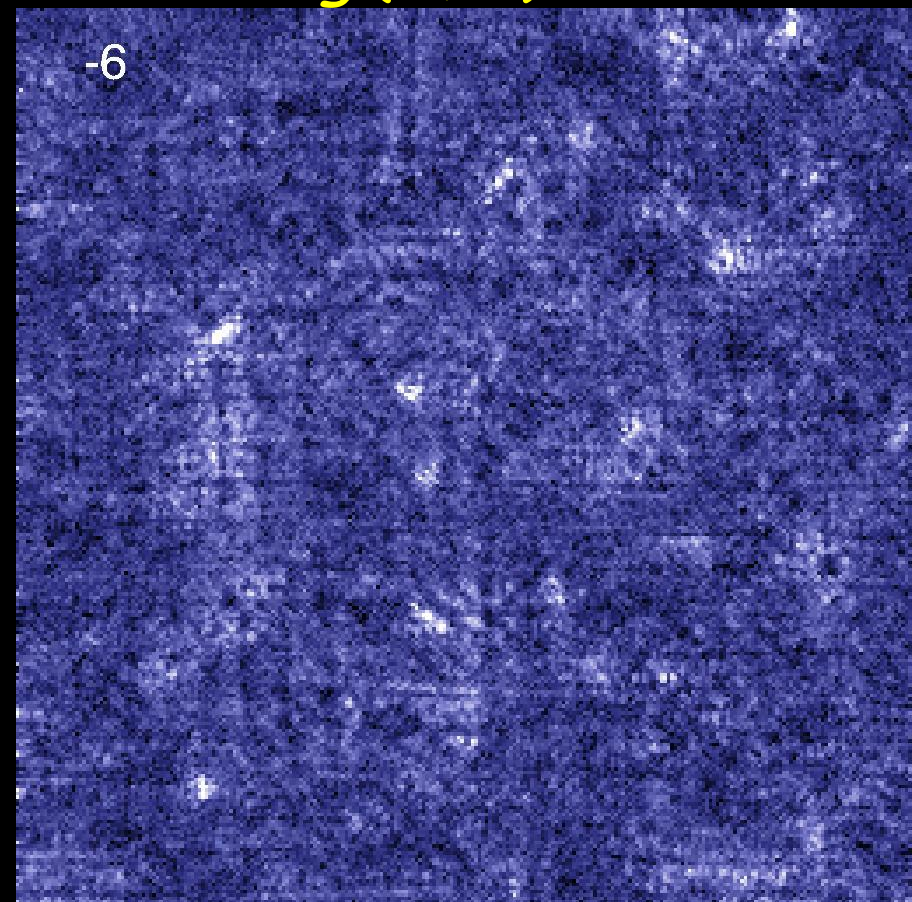


Imaging quasiparticle wavefunctions

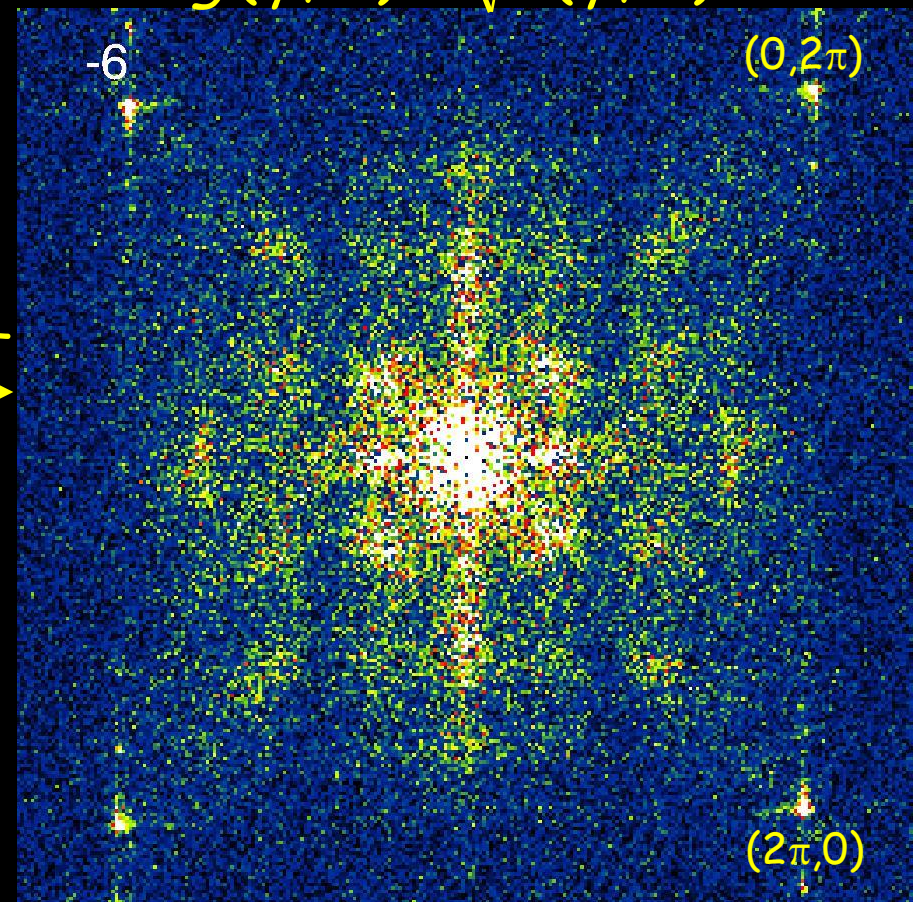
energy
(meV)
↓

$$g(\vec{r}, E)$$

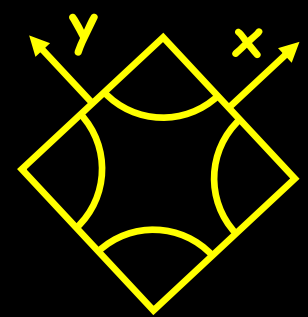
$$g(\vec{q}, E) = \sqrt{P(\vec{q}, E)}$$



FFT
→



← 545 Å →



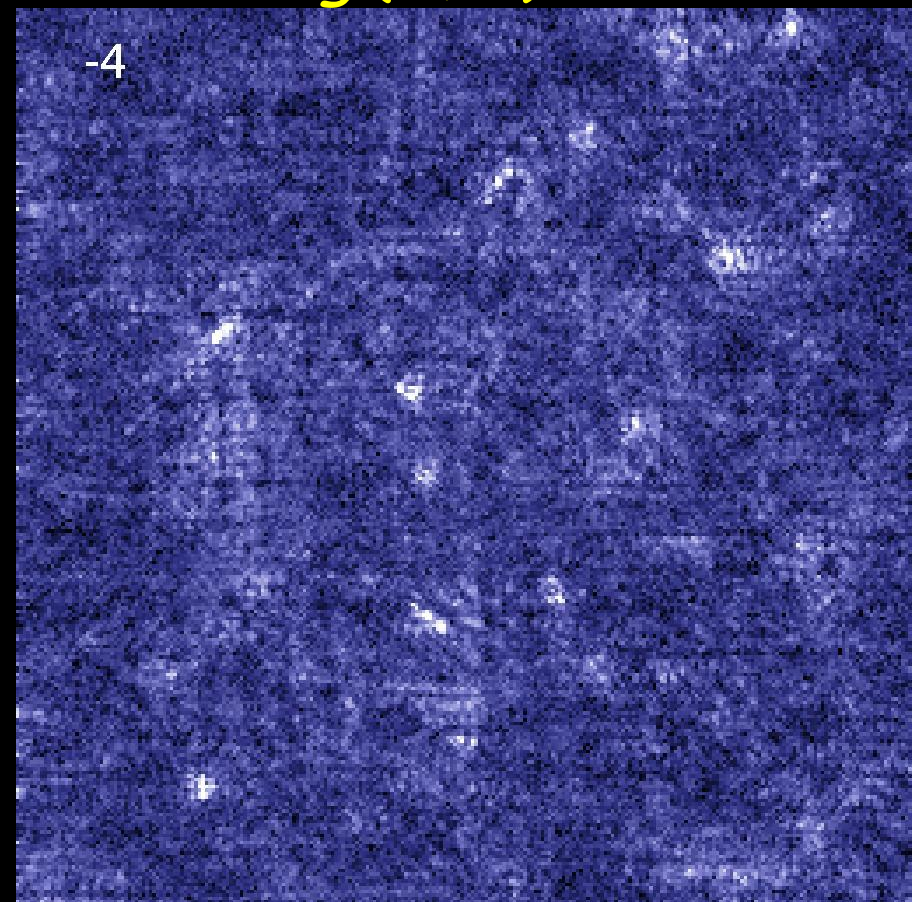
Bi-2212
 $T_c = 76$ K
 $\Delta \sim 51$ meV

Imaging quasiparticle wavefunctions

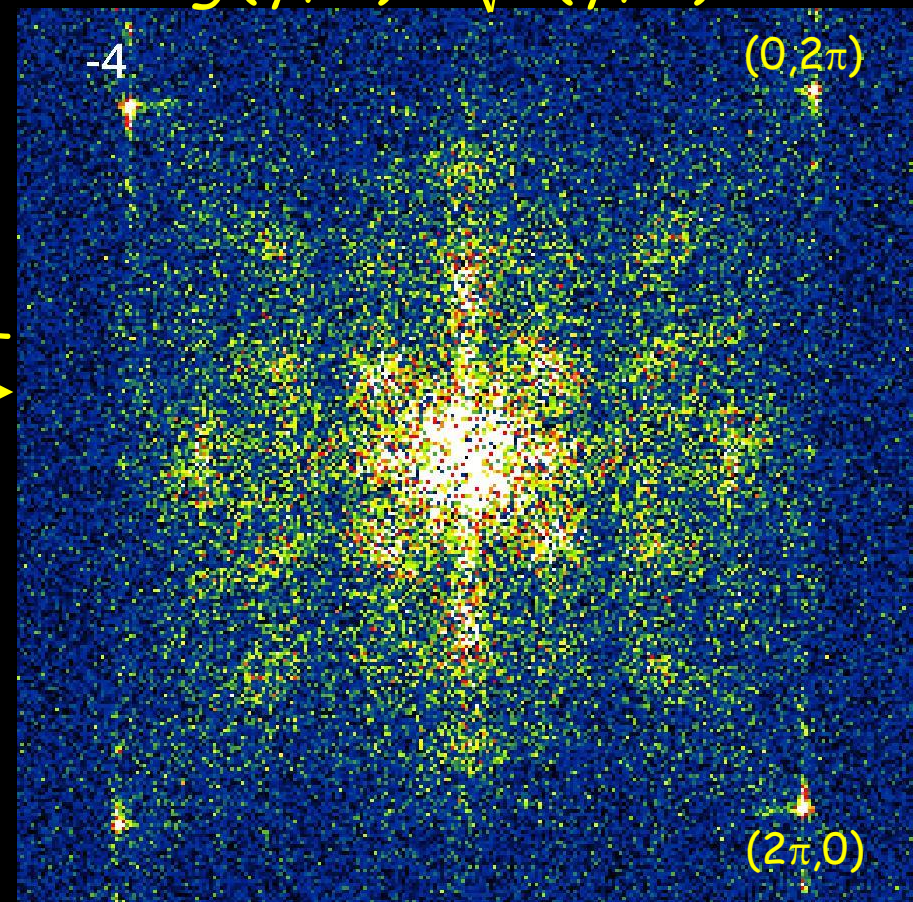
energy
(meV)
↓

$$g(\vec{r}, E)$$

$$g(\vec{q}, E) = \sqrt{P(\vec{q}, E)}$$

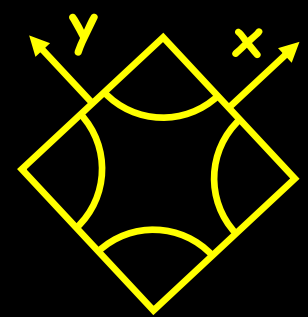


FFT →



← 545 Å →

Bi-2212
 $T_c = 76$ K
 $\Delta \sim 51$ meV

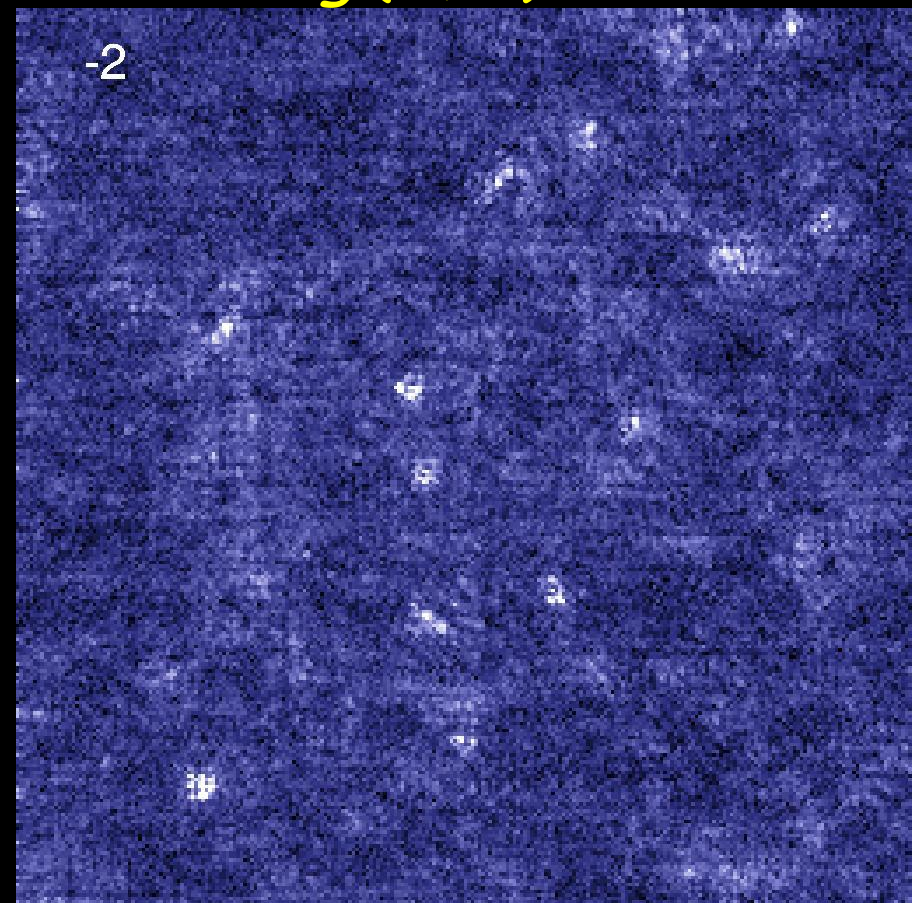


Imaging quasiparticle wavefunctions

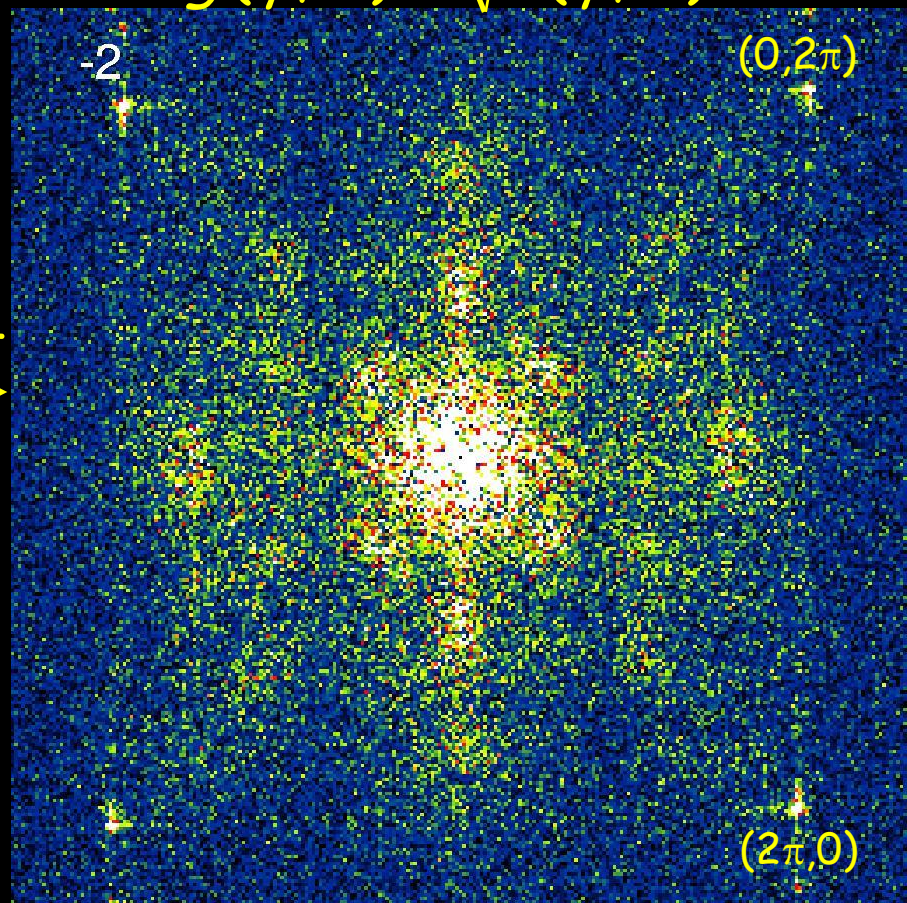
energy
(meV)
↓

$$g(\vec{r}, E)$$

$$g(\vec{q}, E) = \sqrt{P(\vec{q}, E)}$$

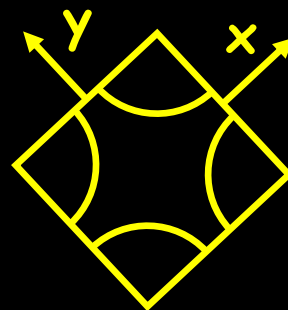


FFT



545 Å

Bi-2212
 $T_c = 76$ K
 $\Delta \sim 51$ meV

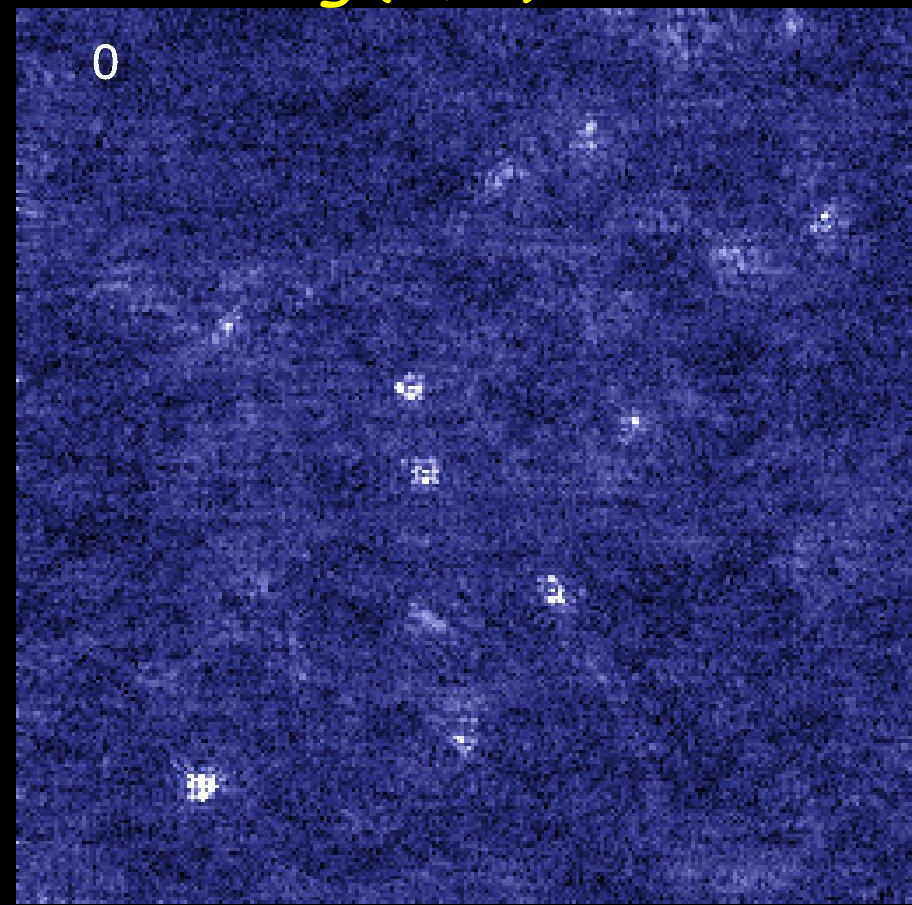


Imaging quasiparticle wavefunctions

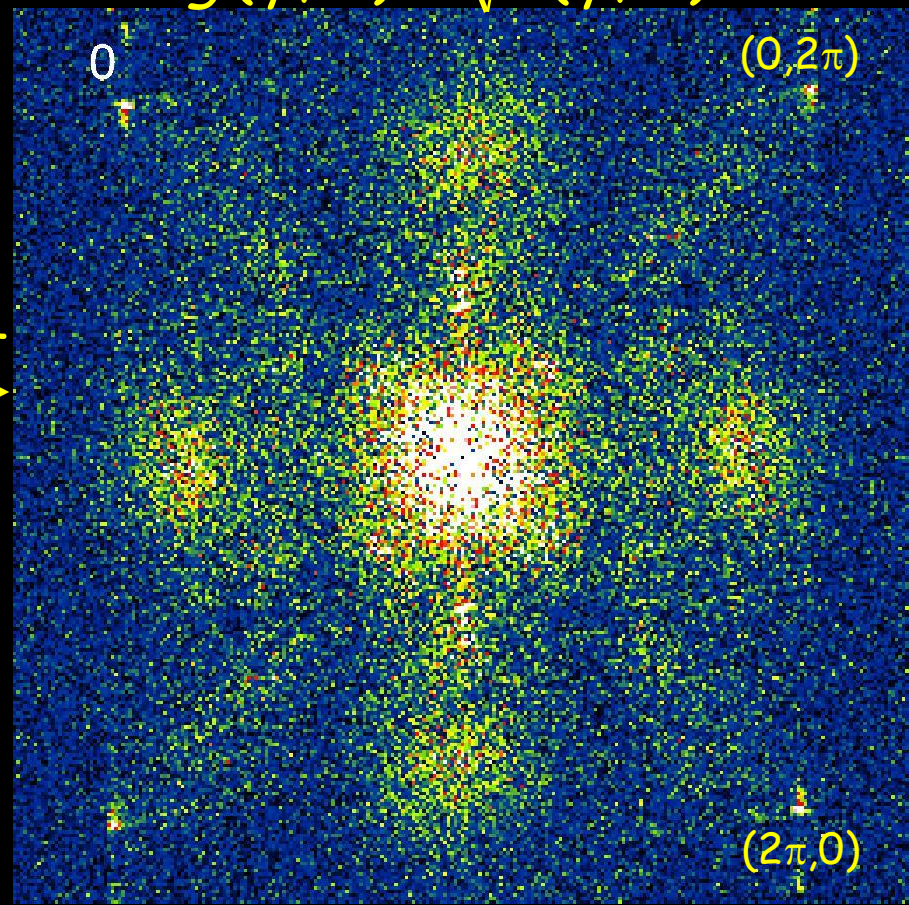
energy
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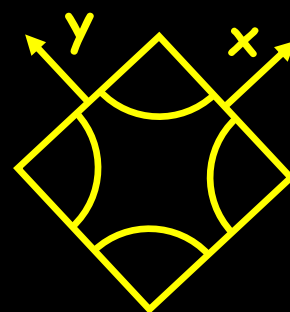


FFT

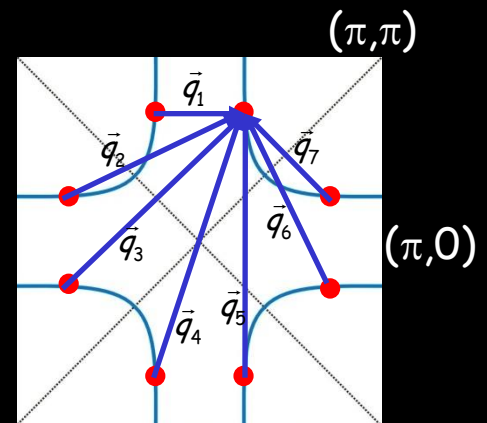
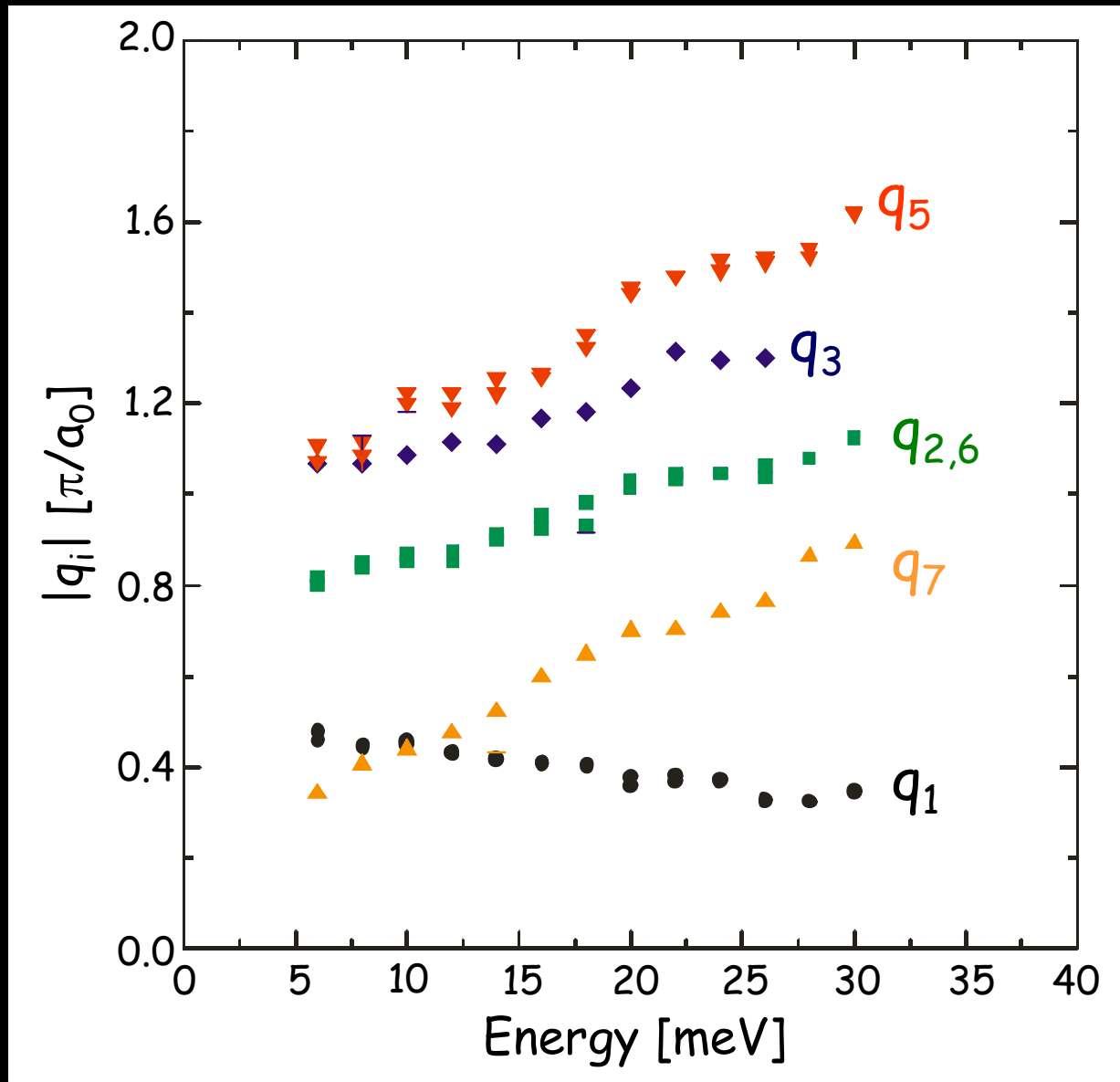


← 545 Å →

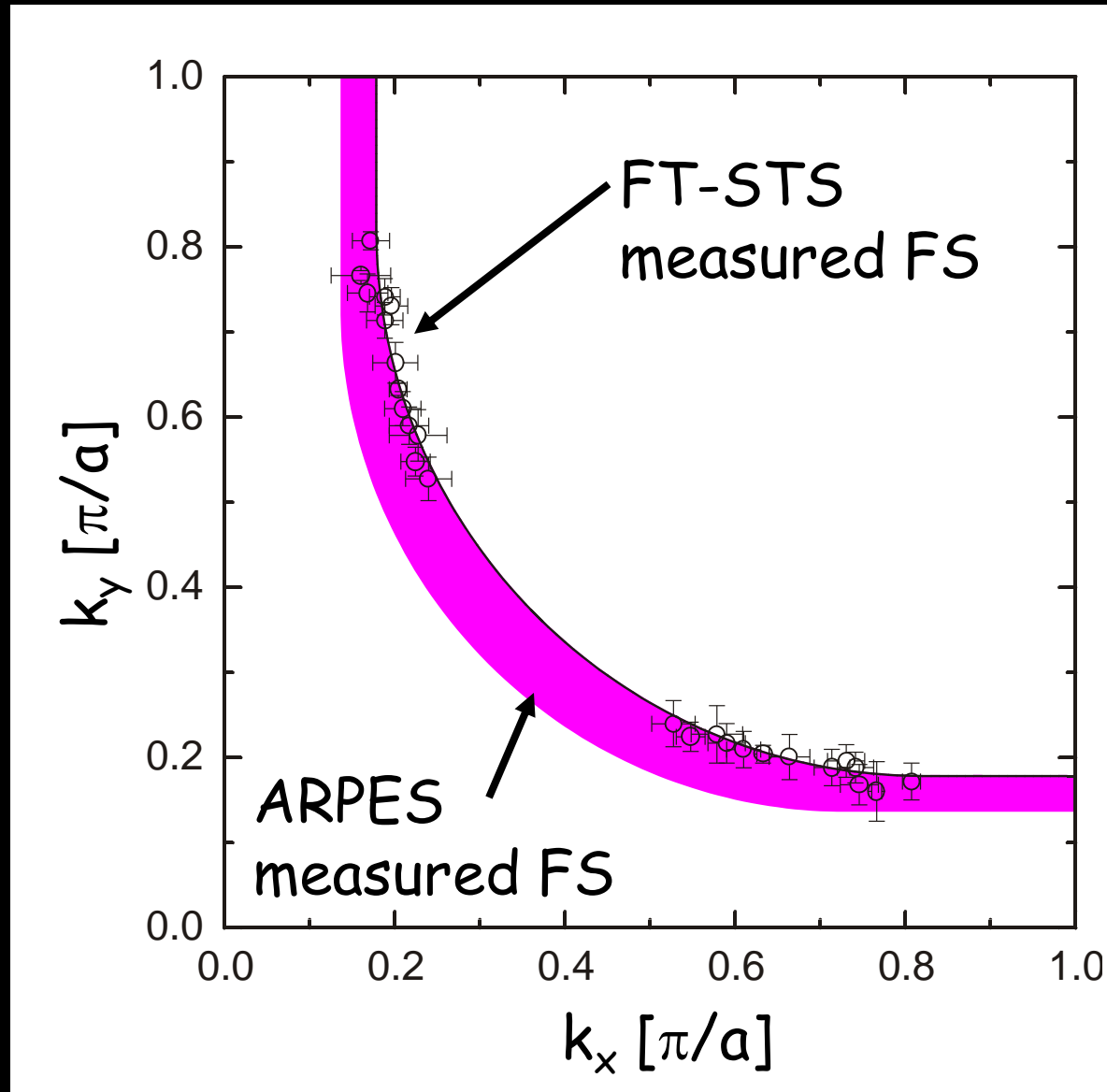
Bi-2212
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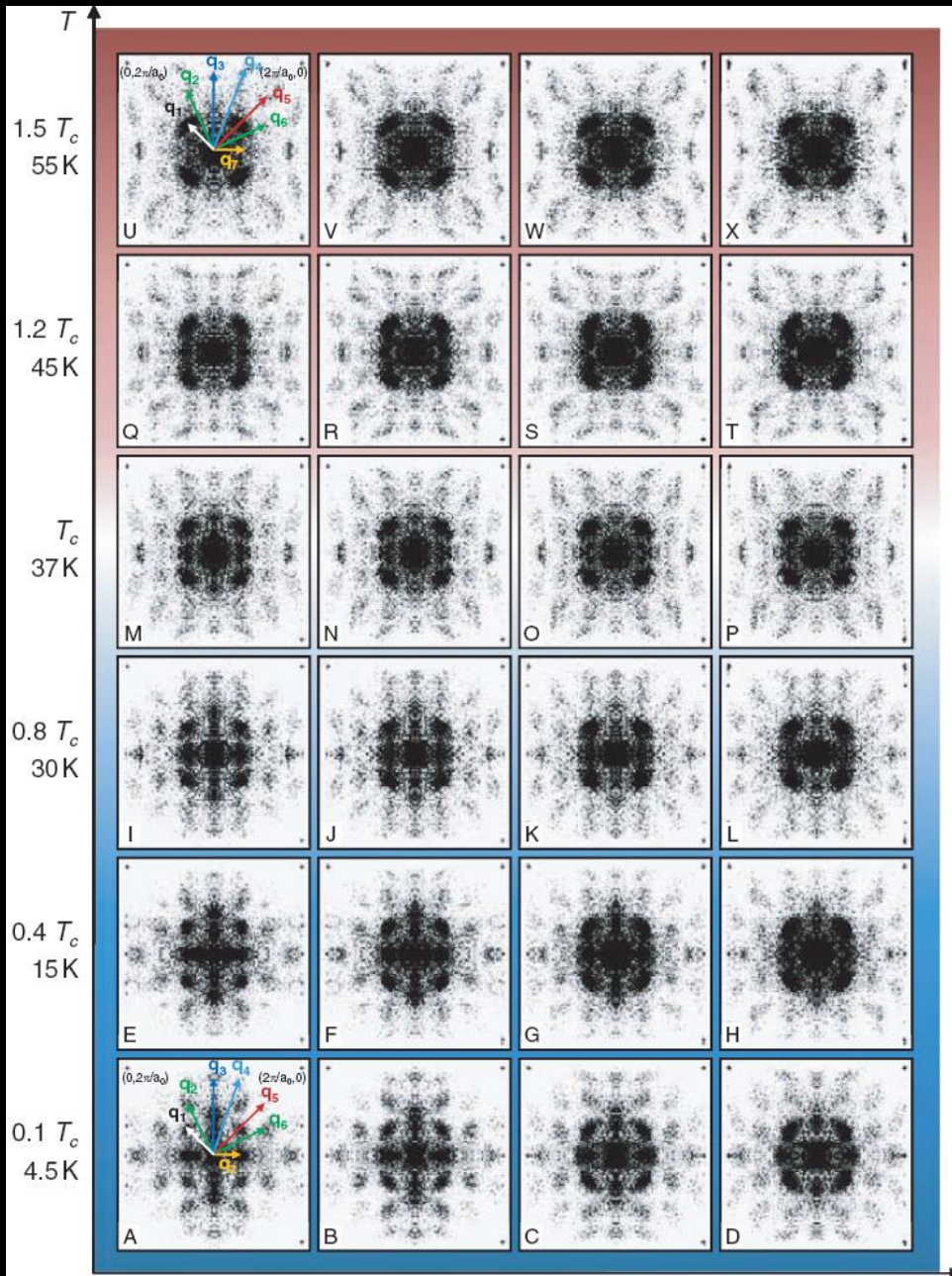
Measuring the dispersion of the $q_i(E)$



ARPES & STM: Fermi surface comparison

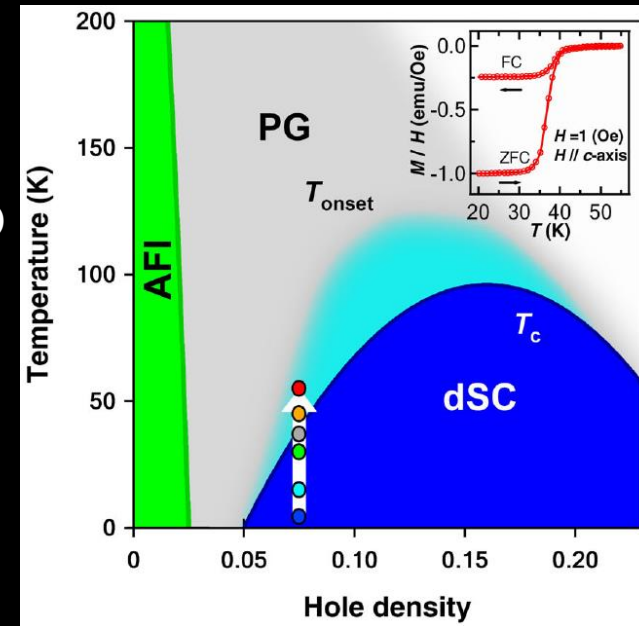


QPI persists to $> 1.5 * T_c$



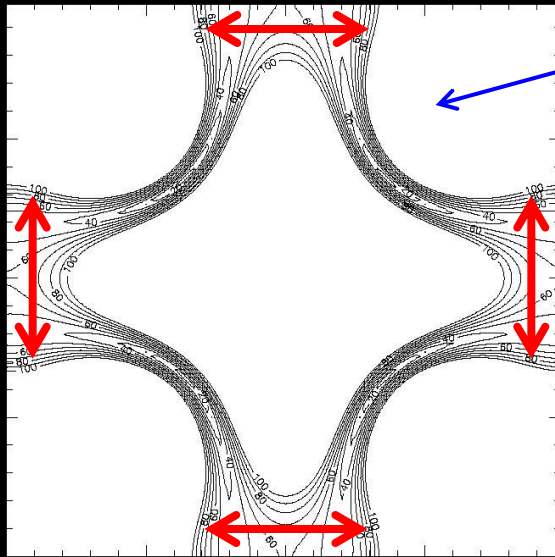
Motivation: QPI is p-h symmetric.
 Claim: no state other than superconductivity is p-h symmetric.
 Therefore, QPI is marker for SC.

Dy-BSCCO
 $T_c \sim 37$ K



Caveat: these are Z maps
 \rightarrow they assume p-h symmetry

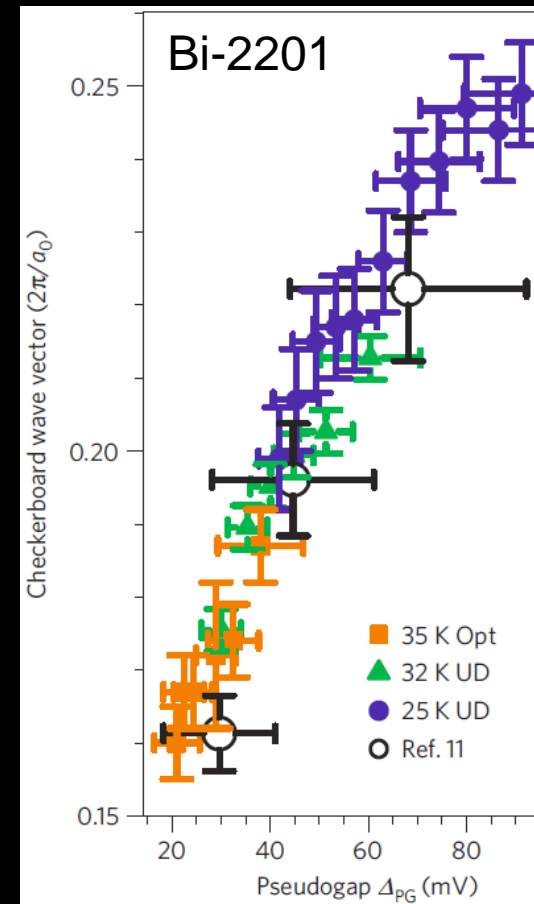
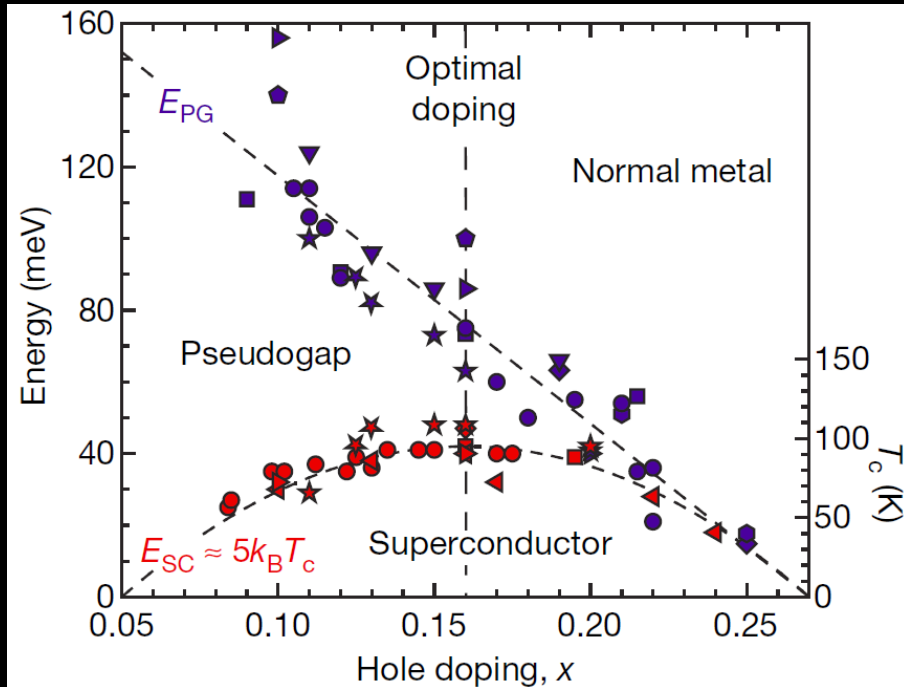
nesting wavelength vs. local *and* global Δ



- hole pocket expands with doping
- nesting wavevector decreases with doping

→ nesting wavevector increases with PG

- pseudogap also decreases with doping



Wise, Hudson, Nat Phys 5, 213 (2009)

Superconductivity Tunneling Milestones



1960: gap measurement (Pb)

1965: boson energies & coupling (Pb)

1985: charge density wave (TaSe_2)

1989: vortex lattice (NbSe_2)

1997: single atom impurities (Nb)

2002: quasiparticle interference

→ band structure & gap symmetry (BSCCO)

2009: phase-sensitive gap measurement (Na-CCOC)

2010: intra-unit-cell structure (BSCCO)

1989: Vortex imaging



Vortex core states
(conventional superconductors):

$$\epsilon_0 \sim \Delta_\infty^2 / E_F$$

Caroli, deGennes, Matricon, *Phys. Lett.* 9, 307 (1964)

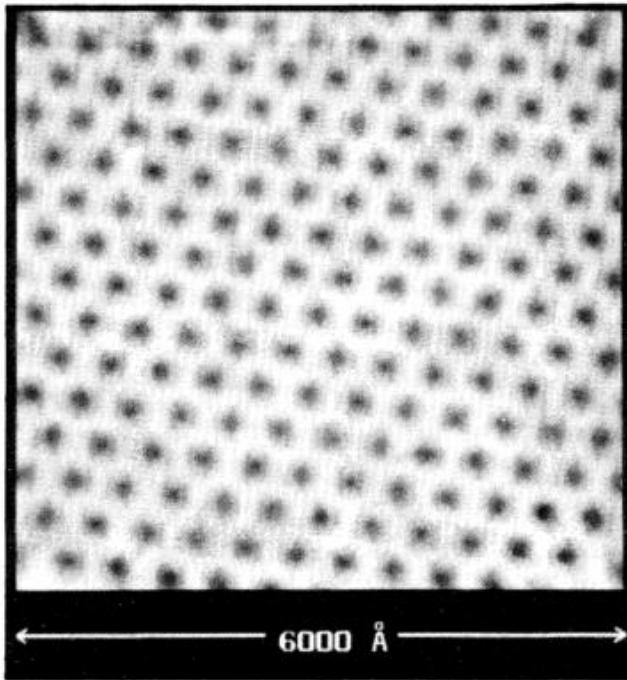


FIG. 2. Abrikosov flux lattice produced by a 1-T magnetic field in NbSe₂ at 1.8 K. The scan range is about 6000 Å. The gray scale corresponds to dI/dV ranging from approximately 1×10^{-8} mho (black) to 1.5×10^{-9} mho (white).

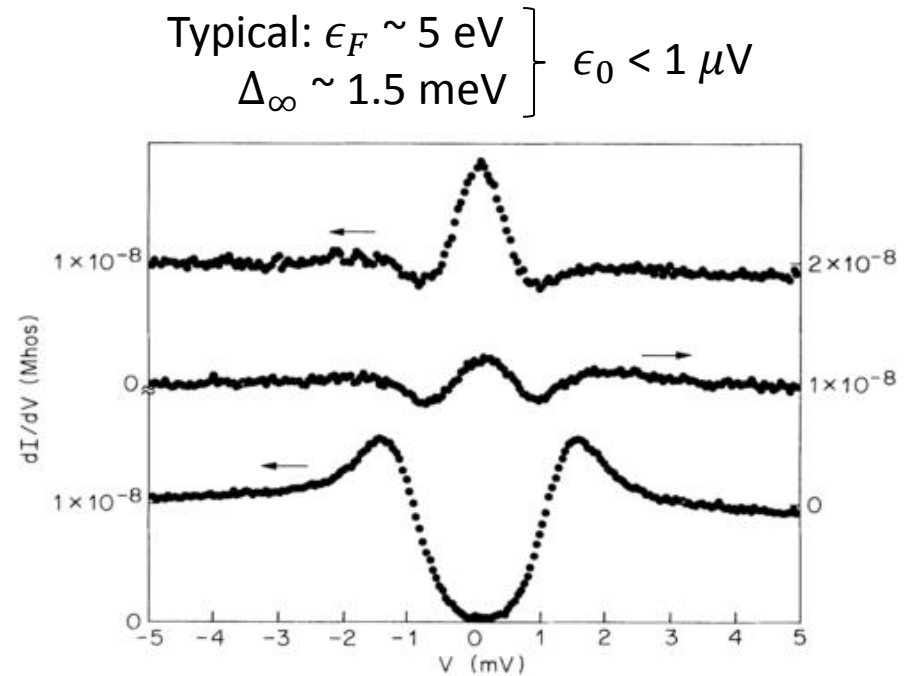
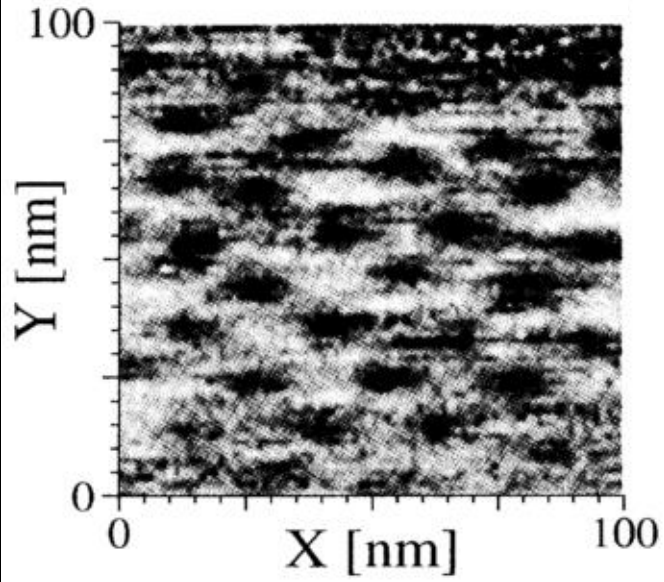


FIG. 3. dI/dV vs V for NbSe₂ at 1.85 K and a 0.02-T field, taken at three positions: on a vortex, about 75 Å from a vortex, and 2000 Å from a vortex. The zero of each successive curve is shifted up by one quarter of the vertical scale.

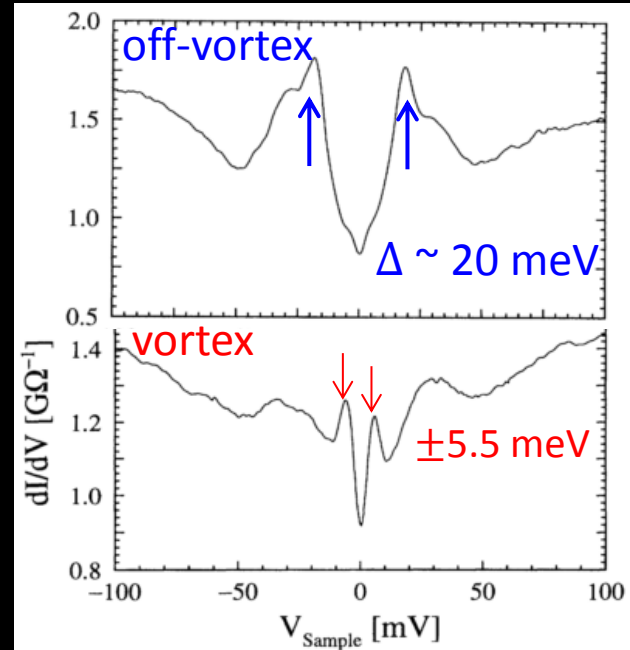
Vortices in cuprates



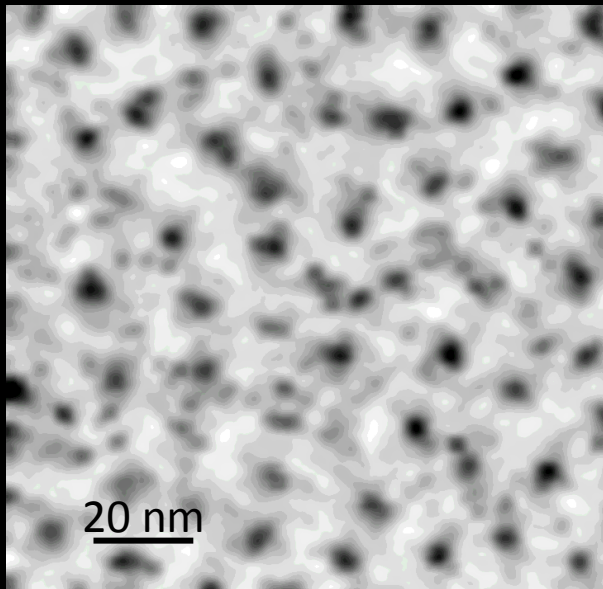
YBCO



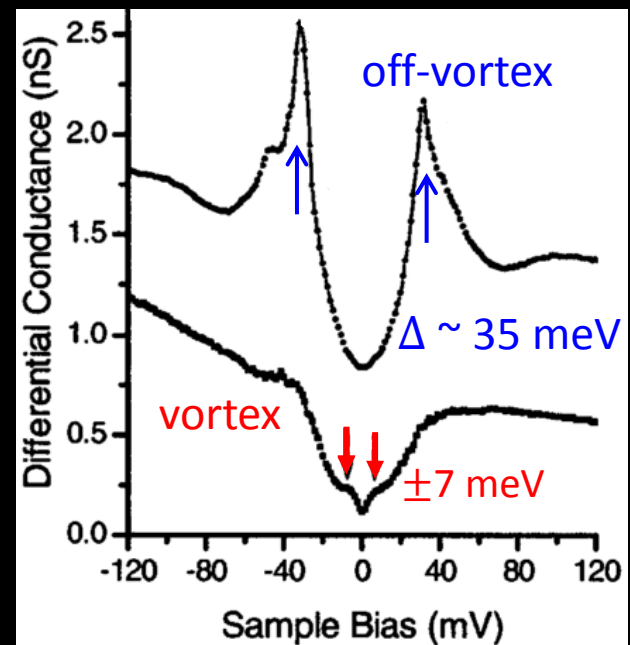
Maggio-Aprile PRL 75, 2754 (1995)



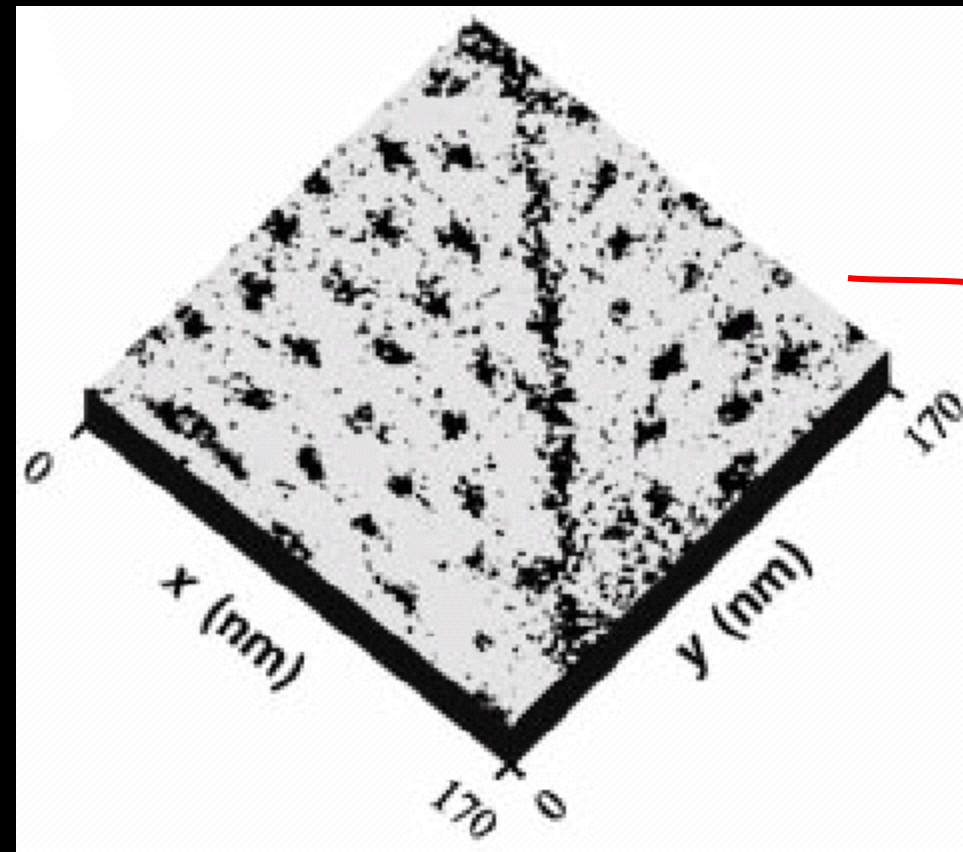
BSCCO



Pan, PRL 85, 1536 (2000)

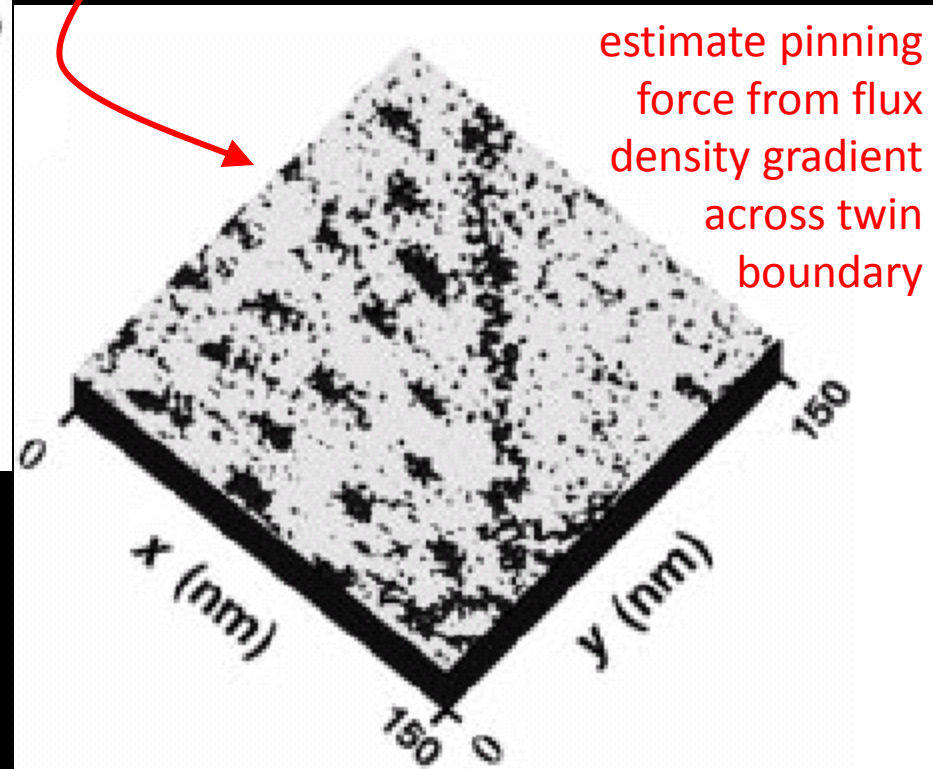


Vortex pinning force measurement



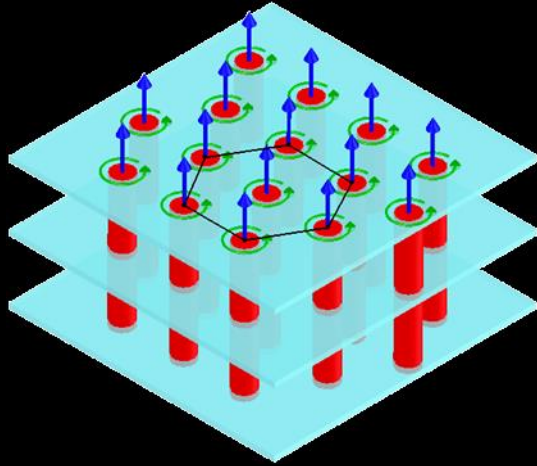
Maggio-Aprile, Nature 390, 487 (1997)

reduce field from
3 Tesla to 1.5 Tesla

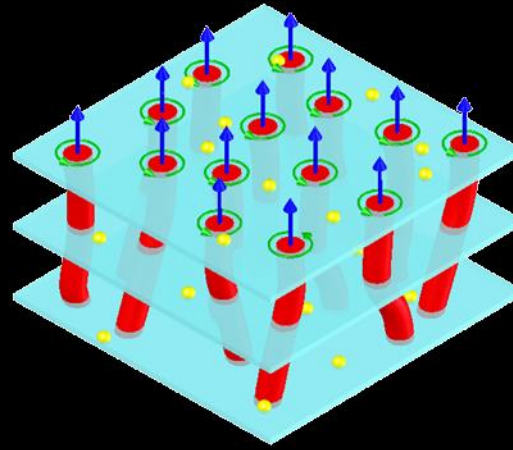


Vortex pinning possibilities

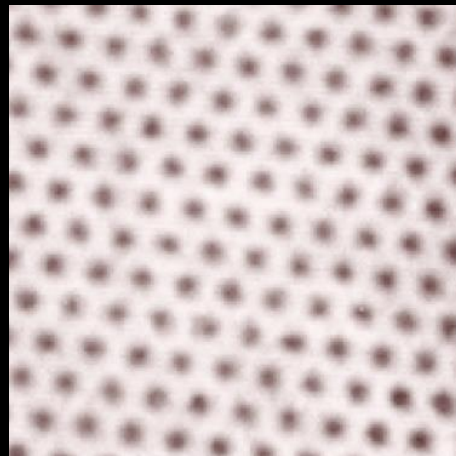
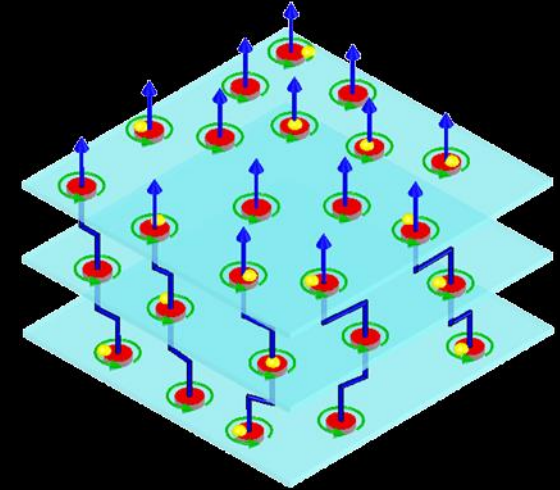
(1) no strong pinners
inter-vortex forces dominate
→ lattice formation



(2) strong pinners exist
low anisotropy
→ vortices bend slightly
to accommodate pinners

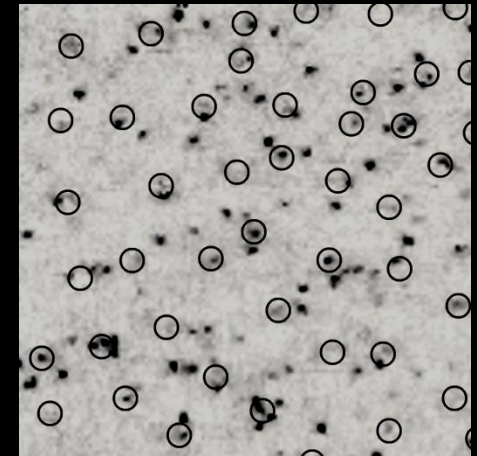


(3) strong pinners exist
high anisotropy
→ vortices pancake
each pancake pins independently



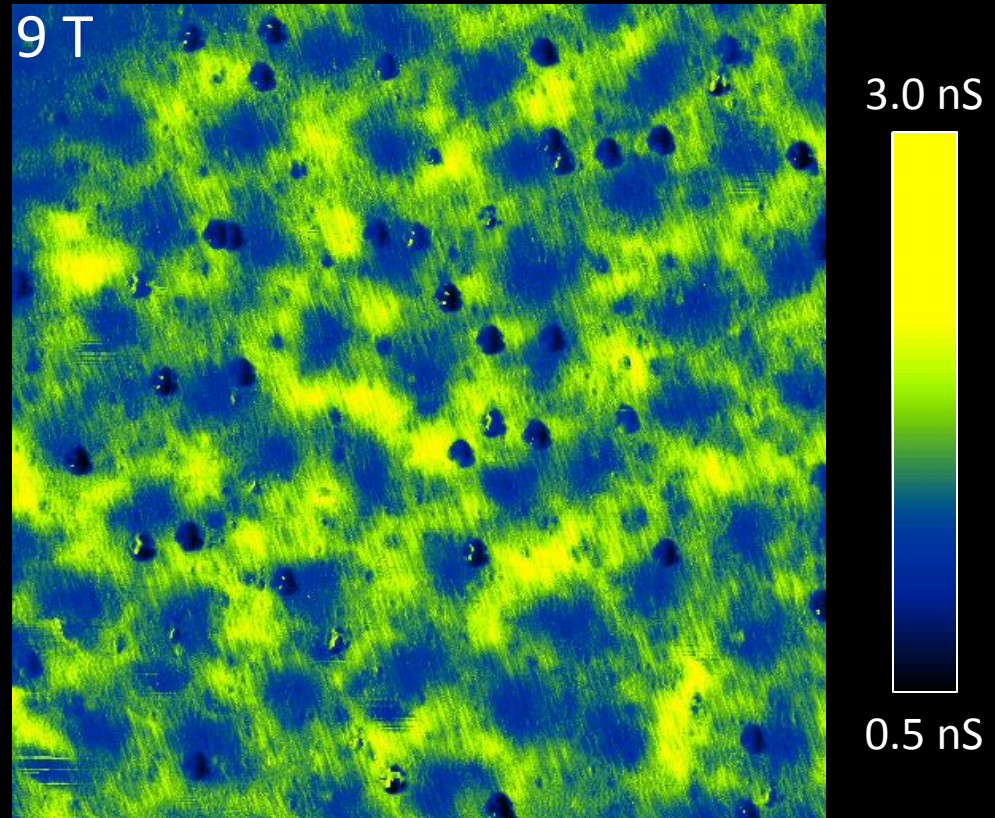
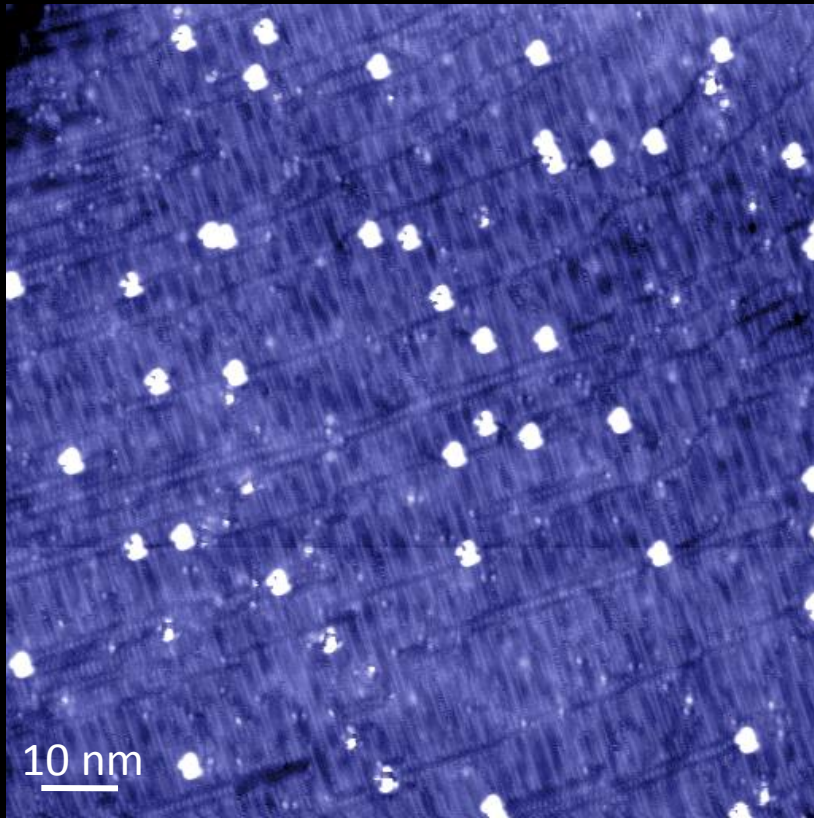
NbSe₂

↓
ideal case
for applications



Bi₂Sr₂CaCu₂O₈

Are Vortices Pinned to Surface Impurities?

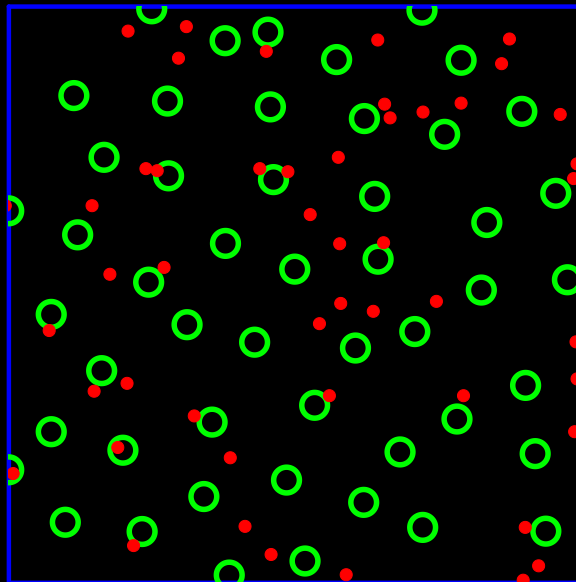
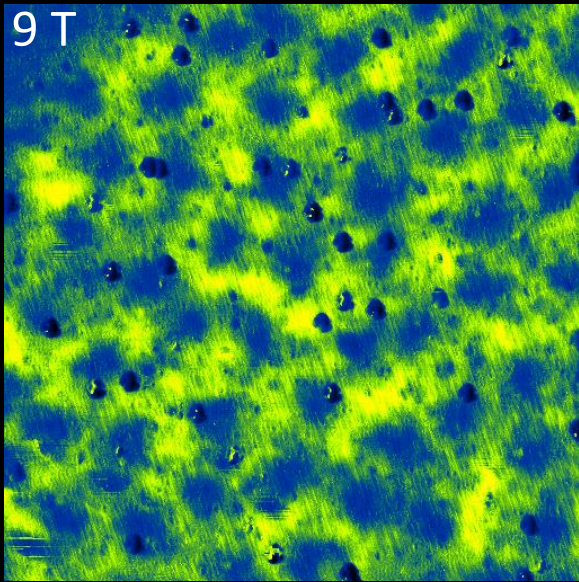


Are Vortices Pinned to Surface Impurities?

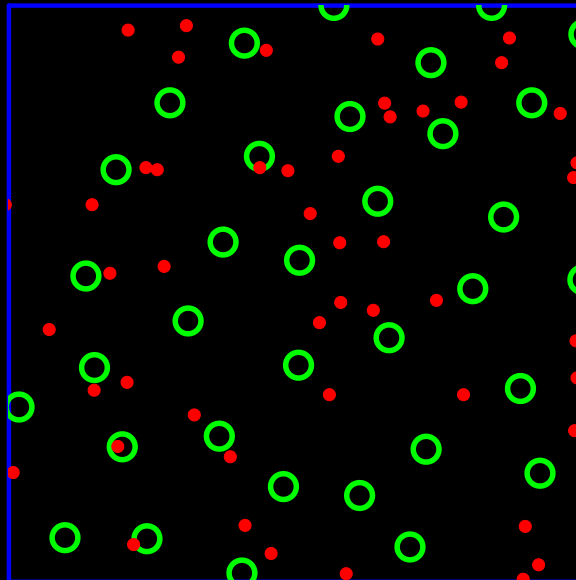
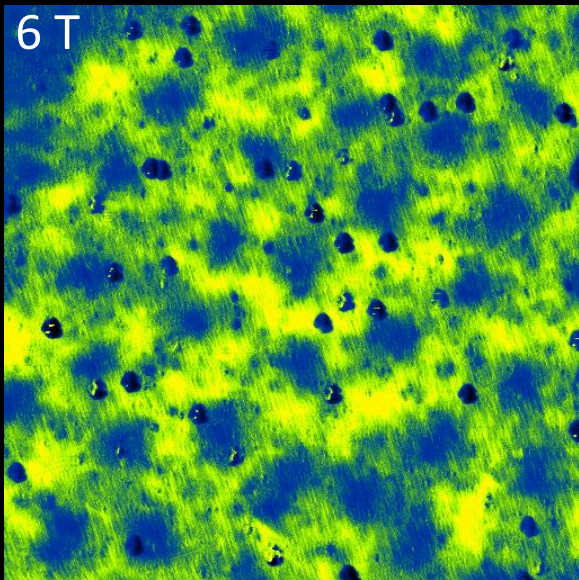


Raw Data

Idealized Data



- vortex, radius $\xi_0 = 2.76$ nm
- impurity

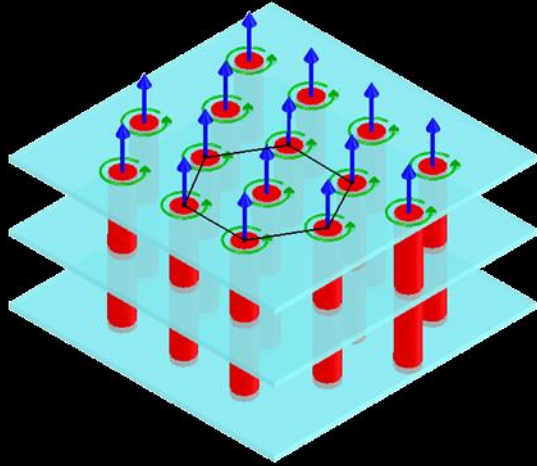


→ Vortices are not pinned to visible surface impurities

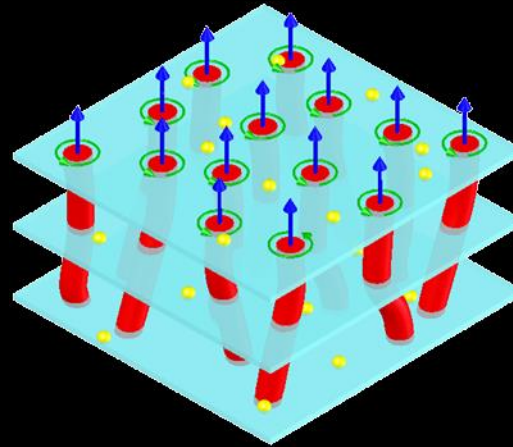
Vortex pinning possibilities



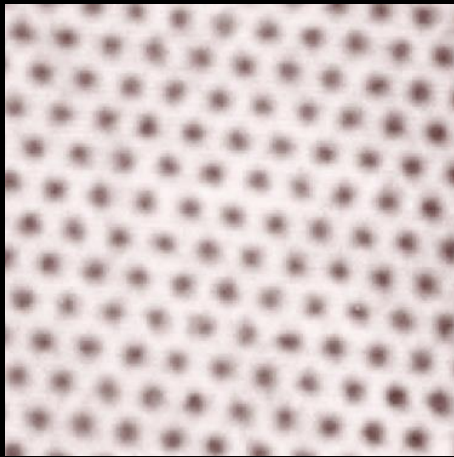
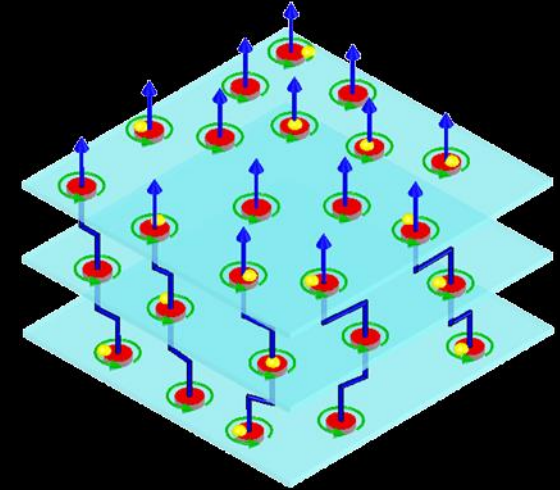
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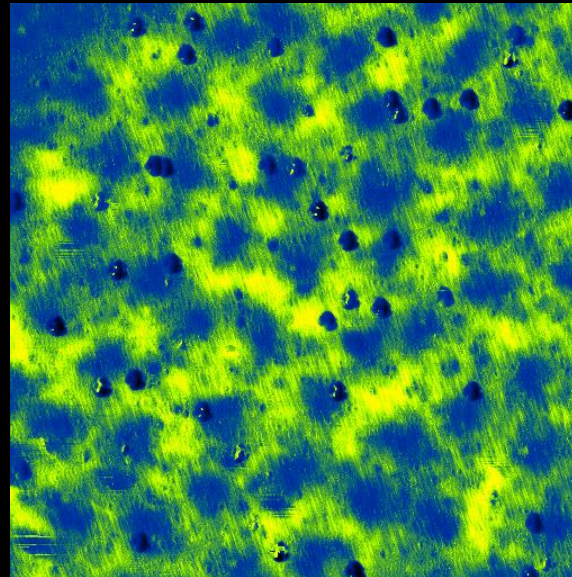
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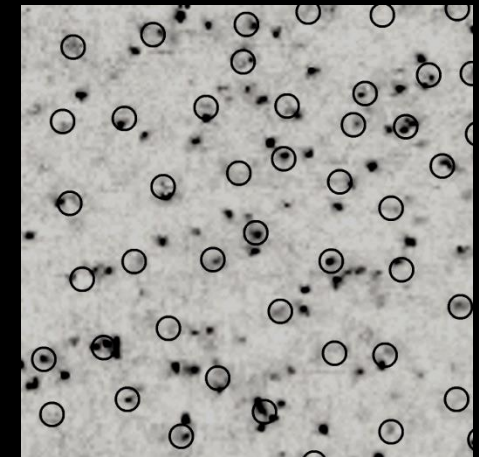
(3) strong pinners exist
high anisotropy
→ vortices pancake
each pancake pins independently



NbSe₂



Ba(Co_xFe_{1-x})₂As₂



Bi₂Sr₂CaCu₂O₈

Next up: vortices as a window to the “normal” state...