



The 17 position knob:

Tuning interactions with rare earths

Paul C. Canfield

Distinguished Professor of Physics

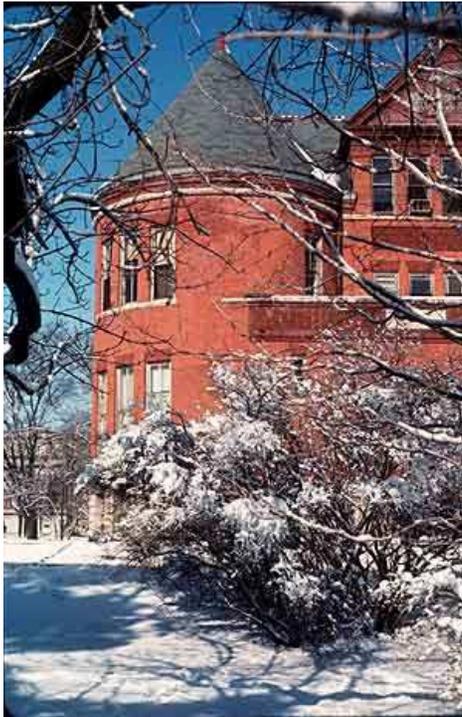
Senior Physicist, Ames Lab

Iowa State University

Boulder 2008 Summer School

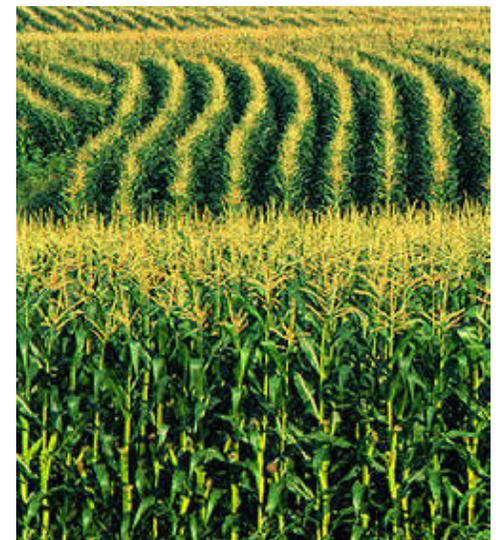
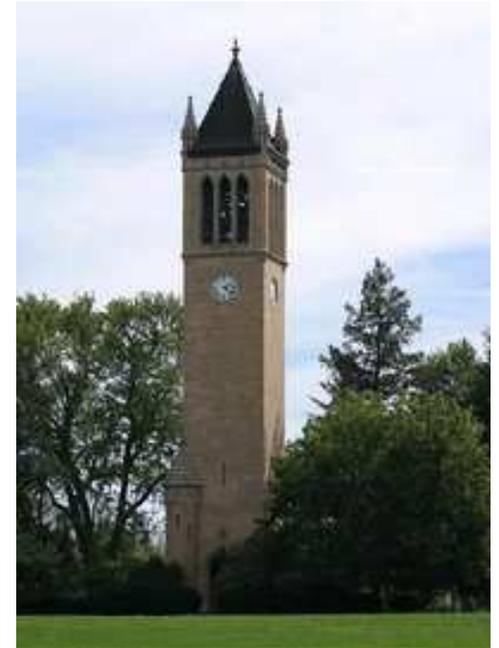


# Iowa State University 150 Years of Land-Grant Education



**~ 25,000 Students**

**Known for Ag. (not Silver),  
Vet., and, in our circles, Physics  
and Chemistry associated with  
Ames Lab.**





# Ames Laboratory



Frank Spedding



Ames Lab was the starting point for the materials used in the Manhattan project. Soon after WWII it became a basic science lab.

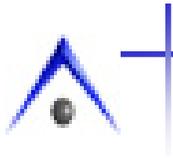
DOE OFFICE OF SCIENCE LABORATORIES



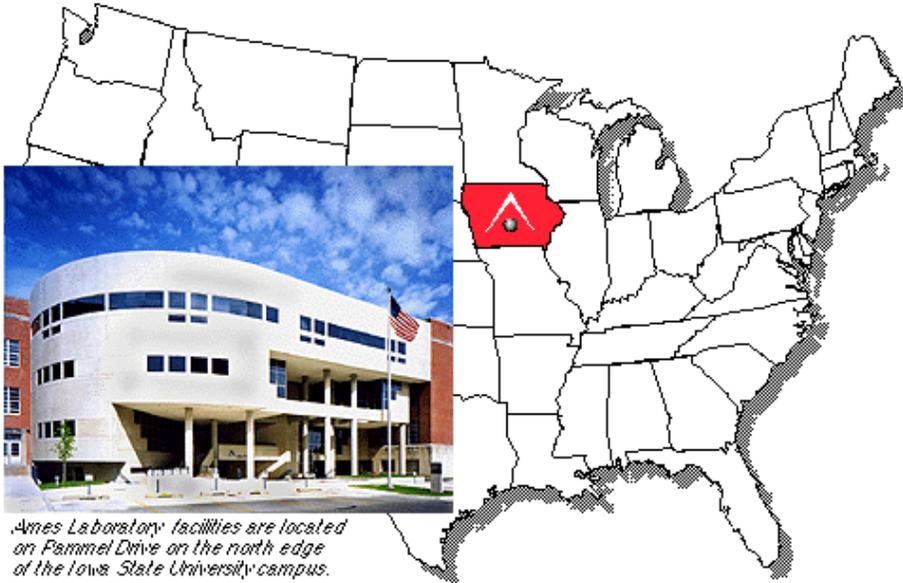
Frank Spedding (right) examines a demonstration column showing the separation of the rare earths with senior chemist Jack Powell (standing) and summer student trainee Tom Erskine. This photo was featured in a 1963 Sunday edition of the *Des Moines Register*

Ames Lab still produces (and sells) the world's highest purity rare earth elements. Please contact Larry Jones or Tom Lograsso about getting quotes or information.





# Ames Laboratory



*Ames Laboratory facilities are located on Fammel Drive on the north edge of the Iowa State University campus.*

Mid-sized DOE Laboratory with ~ 400 employees

## **Now:**

Applied Mathematics and Computational Sciences

Chemical and Biological Sciences

**Condensed Matter Physics**

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Granular and Multiphase Systems

Materials Chemistry

Materials and Engineering Physics

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## **Also:**

Biorenewable Resources Consortium

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**For 60 years Ames Laboratory has been a leader in the physics, chemistry and metallurgy of novel materials.**



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# CANFIELD'S RESEARCH GROUP

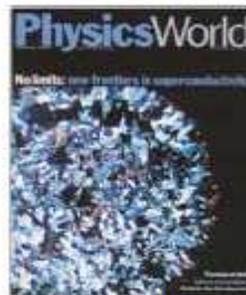
Welcome to our web page, where you may learn about who we are and what we do as part of the [Condensed Matter Physics Group](#) of the [Physics and Astronomy Department](#) at [Iowa State University](#) and [Ames Laboratory](#) (a U. S. Department of Energy (DOE) facility). Our group of faculty, staff, post-docs, graduate and undergraduate students is mostly dedicated to the design, discovery, growth and characterization of novel electronic and magnetic compounds - often in single crystal form - and the study of their interesting physical properties.



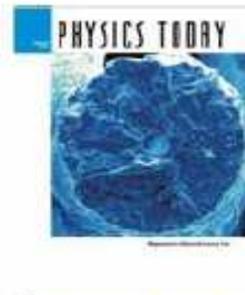
Here are four of our general review articles:



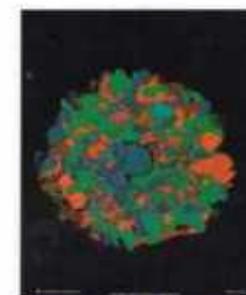
[Physics Today - October 1998](#)  
"New Magnetic Superconductors:  
A Toy Box for Solid-State  
Physicists"



[Physics World - January 2002](#)  
"Magnesium  
Diboride:  
one year on"



[Physics Today - March 2003](#)  
"Magnesium  
Diboride:  
Better Late than  
Never"



[Scientific American - April 2005](#)  
"Low Temperature  
Superconductivity  
Is Warming Up"

If the material I cover is of interest to you explore our home page. We have review articles, lists of activities, papers, people, and even some recipes.

<http://cmpweb.ameslab.gov/personnel/canfield/>





The solid state physicist sees a powerful tuning mechanism.

Atomic number

Symbol

Atomic weight

Metal

Semimetal

Nonmetal

1	2											13	14	15	16	17	18
1 <b>H</b> 1.008																	2 <b>He</b> 4.003
3 <b>Li</b> 6.941	4 <b>Be</b> 9.012											5 <b>B</b> 10.81	6 <b>C</b> 12.01	7 <b>N</b> 14.01	8 <b>O</b> 16.00	9 <b>F</b> 19.00	10 <b>Ne</b> 20.18
11 <b>Na</b> 22.99	12 <b>Mg</b> 24.31											13 <b>Al</b> 26.98	14 <b>Si</b> 28.09	15 <b>P</b> 30.97	16 <b>S</b> 32.07	17 <b>Cl</b> 35.45	18 <b>Ar</b> 39.95
19 <b>K</b> 39.10	20 <b>Ca</b> 40.08	21 <b>Sc</b> 44.96	22 <b>Ti</b> 47.88	23 <b>V</b> 50.94	24 <b>Cr</b> 52.00	25 <b>Mn</b> 54.94	26 <b>Fe</b> 55.85	27 <b>Co</b> 58.93	28 <b>Ni</b> 58.69	29 <b>Cu</b> 63.55	30 <b>Zn</b> 65.39	31 <b>Ga</b> 69.72	32 <b>Ge</b> 72.61	33 <b>As</b> 74.92	34 <b>Se</b> 78.96	35 <b>Br</b> 79.90	36 <b>Kr</b> 83.80
37 <b>Rb</b> 85.47	38 <b>Sr</b> 87.62	39 <b>Y</b> 88.91	40 <b>Zr</b> 91.22	41 <b>Nb</b> 92.91	42 <b>Mo</b> 95.94	43 <b>Tc</b> 98.91	44 <b>Ru</b> 101.1	45 <b>Rh</b> 102.9	46 <b>Pd</b> 106.4	47 <b>Ag</b> 107.9	48 <b>Cd</b> 112.4	49 <b>In</b> 114.8	50 <b>Sn</b> 118.7	51 <b>Sb</b> 121.8	52 <b>Te</b> 127.6	53 <b>I</b> 126.9	54 <b>Xe</b> 131.3
55 <b>Cs</b> 132.9	56 <b>Ba</b> 137.3	71 <b>Lu</b> 175.0	72 <b>Hf</b> 178.5	73 <b>Ta</b> 180.9	74 <b>W</b> 183.8	75 <b>Re</b> 186.2	76 <b>Os</b> 190.2	77 <b>Ir</b> 192.2	78 <b>Pt</b> 195.1	79 <b>Au</b> 197.0	80 <b>Hg</b> 200.6	81 <b>Tl</b> 204.4	82 <b>Pb</b> 207.2	83 <b>Bi</b> 209.0	84 <b>Po</b> 209.0	85 <b>At</b> 210.0	86 <b>Rn</b> 222.0
87 <b>Fr</b> 223.0	88 <b>Ra</b> 226.0	103 <b>Lr</b> 262.1	104 <b>Rf</b> 261.1	105 <b>Db</b> 262.1	106 <b>Sg</b> 263.1	107 <b>Bh</b> 264.1	108 <b>Hs</b> 265.1	109 <b>Mt</b> 268	110 <b>Uun</b> 269	111 <b>Uuu</b> 272	112 <b>Uub</b> 277	113 <b>Uut</b>	114 <b>Uuq</b> 289	115 <b>Uup</b>	116 <b>Uuh</b> 289	117 <b>Uus</b>	118 <b>Uuo</b> 293
		57 <b>La</b> 138.9	58 <b>Ce</b> 140.1	59 <b>Pr</b> 140.9	60 <b>Nd</b> 144.2	61 <b>Pm</b> 146.9	62 <b>Sm</b> 150.4	63 <b>Eu</b> 152.0	64 <b>Gd</b> 157.3	65 <b>Tb</b> 158.9	66 <b>Dy</b> 162.5	67 <b>Ho</b> 164.9	68 <b>Er</b> 167.3	69 <b>Tm</b> 168.9	70 <b>Yb</b> 173.0		
		89 <b>Ac</b> 227.0	90 <b>Th</b> 232.0	91 <b>Pa</b> 231.0	92 <b>U</b> 238.0	93 <b>Np</b> 237.0	94 <b>Pu</b> 244.1	95 <b>Am</b> 243.1	96 <b>Cm</b> 247.1	97 <b>Bk</b> 247.1	98 <b>Cf</b> 251.1	99 <b>Es</b> 252.0	100 <b>Fm</b> 257.1	101 <b>Md</b> 258.1	102 <b>No</b> 259.1		

(c) 1998  
Kromer Paul

The rare earth elements can be chemically similar, but have vastly different magnetic properties. In RXY compounds you can dial in magnetism and tune other physical properties.



So how does a physicist look at (and use) the rare earth elements to get at "the physics" of novel materials?



*The physicist sees a 17 position knob*

For tuning magnetic, electronic and structural properties.

57	58	59	60	61	62	63	64	65	66	67	68	69	70	71
<b>La</b>	<b>Ce</b>	<b>Pr</b>	<b>Nd</b>	<b>Pm</b>	<b>Sm</b>	<b>Eu</b>	<b>Gd</b>	<b>Tb</b>	<b>Dy</b>	<b>Ho</b>	<b>Er</b>	<b>Tm</b>	<b>Yb</b>	<b>Lu</b>
138.9	140.1	140.9	144.2	146.9	150.4	152.0	157.3	158.9	162.5	164.9	167.3	168.9	173.0	175.0

21
<b>Sc</b>
44.96
39
<b>Y</b>
88.91



By using the rare earths, the physicist can tune the:

Size of the unit cell,

Size of the local moment and degree of coupling,

Size and direction of anisotropy,

Amount of entropy that can be removed at low temperatures,

Band filling,

Degree of hybridization.

In terms of temperature and energy scales (another obsession of the physicist), the rare earths can be used to tune:

The magnetic ordering temperature  $T_C$  or  $T_N$       Superconducting  $T_C$

The CEF splitting or  $T_{\Delta_{CEF}}$       Metal-to-insulator  $T_{MI}$

The Kondo temperature  $T_K$       Spinglass freezing  $T_f$

57	58	59	60	61	62	63	64	65	66	67	68	69	70	71
<b>La</b>	<b>Ce</b>	<b>Pr</b>	<b>Nd</b>	<b>Pm</b>	<b>Sm</b>	<b>Eu</b>	<b>Gd</b>	<b>Tb</b>	<b>Dy</b>	<b>Ho</b>	<b>Er</b>	<b>Tm</b>	<b>Yb</b>	<b>Lu</b>
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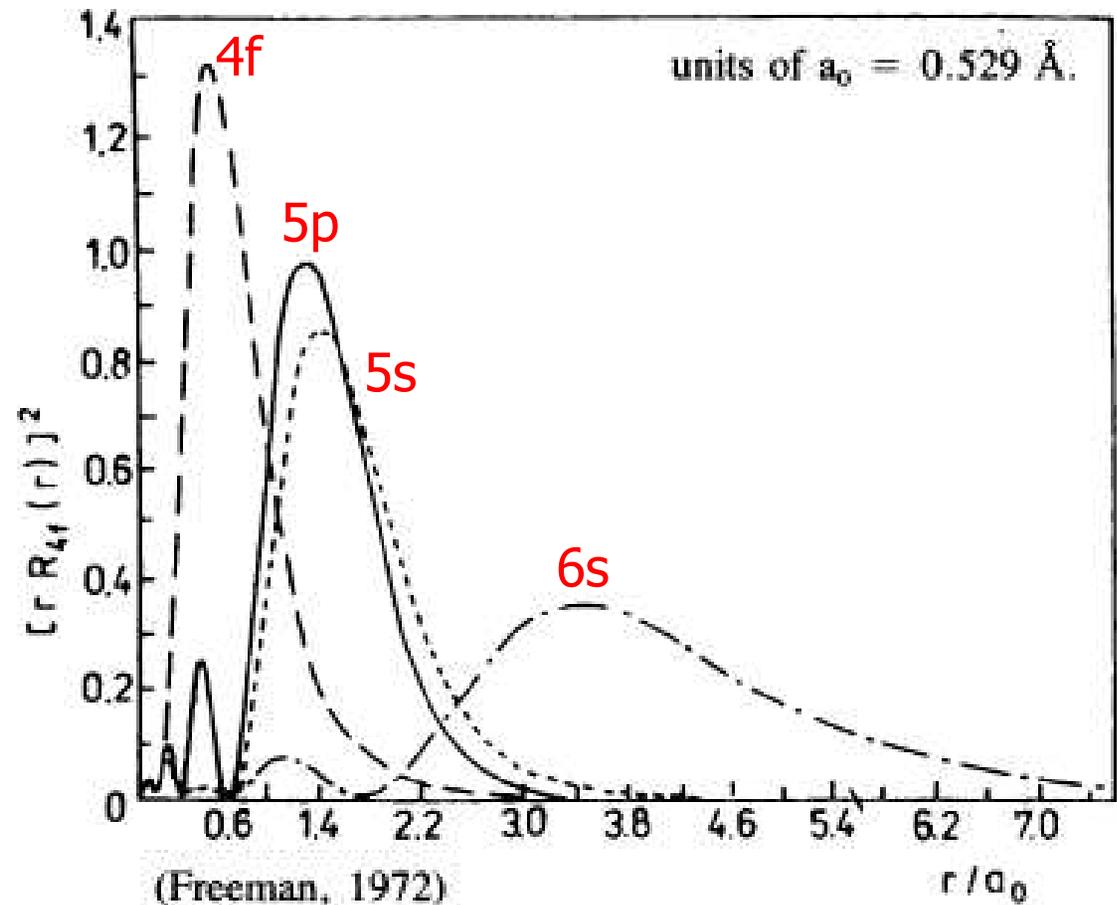
The CEF splitting or  $T_{\Delta_{\text{CEF}}}$

The Kondo temperature  $T_K$



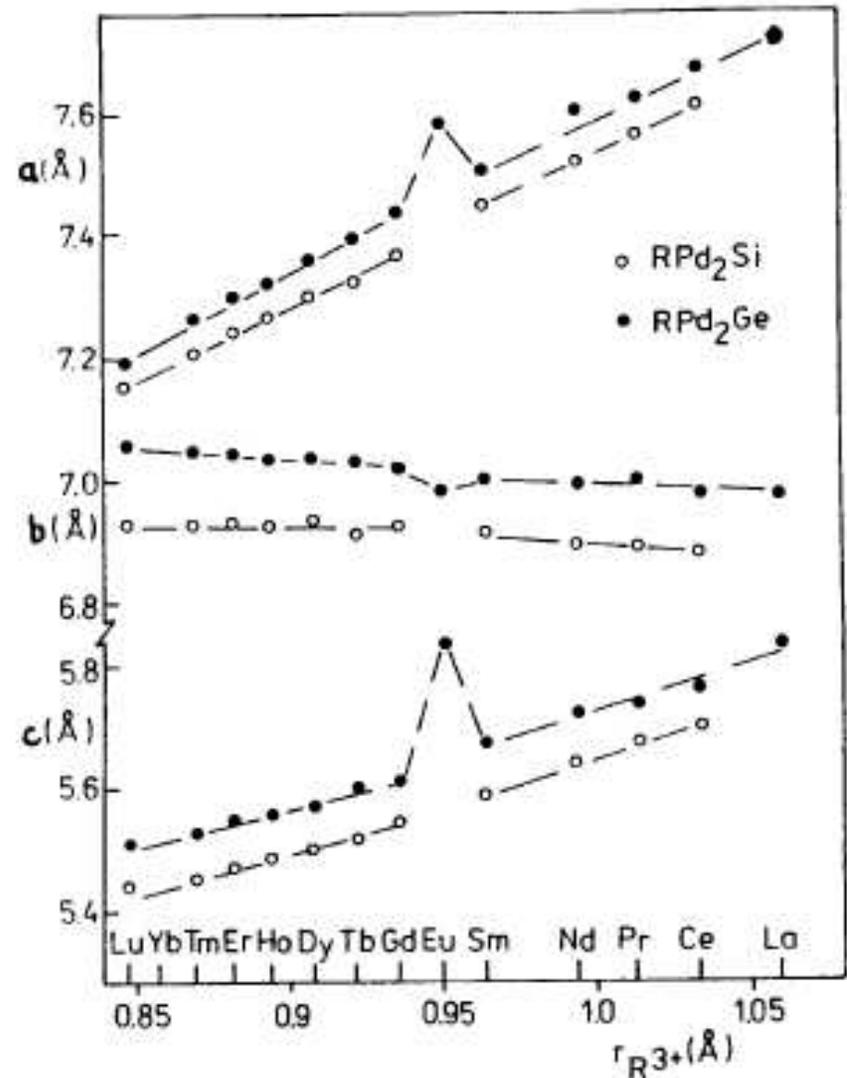
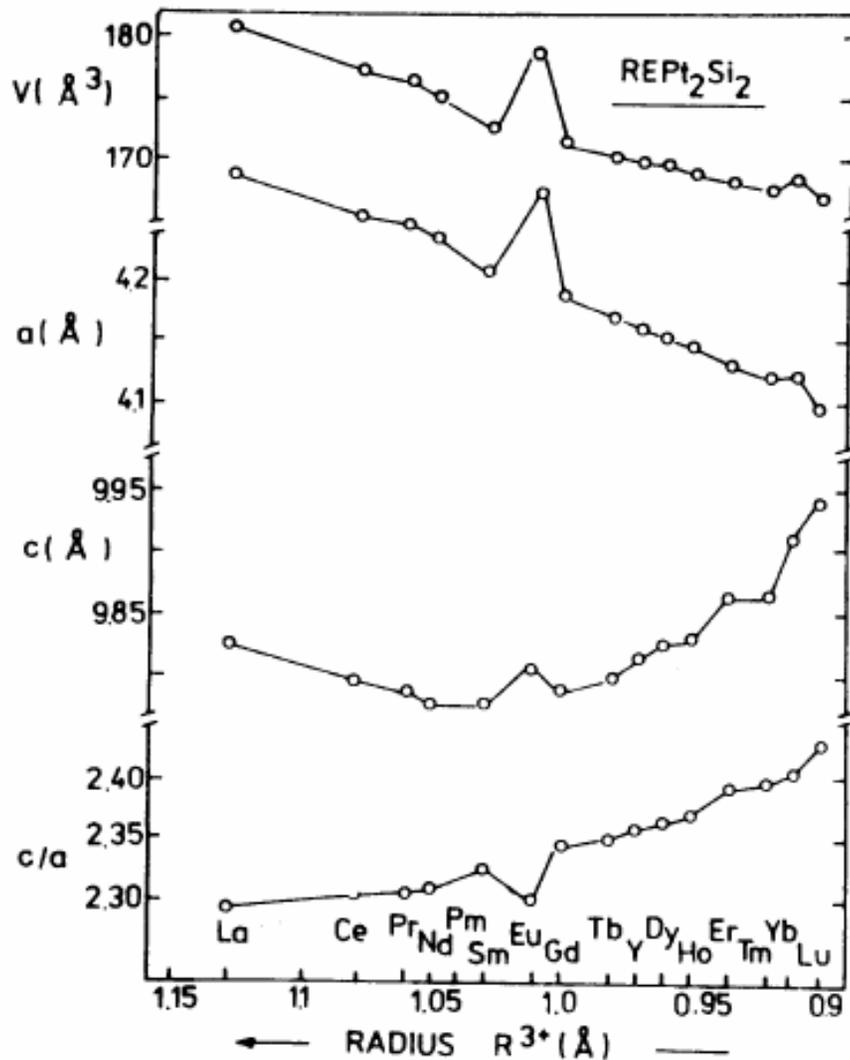
If you can make one member of a RXY series you (usually) can make several. This is due to the fact that the 4f-orbits are shielded by core levels and do not take part in bonding.

There is a structural effect of such substitutions though, *the lanthanide contraction.*



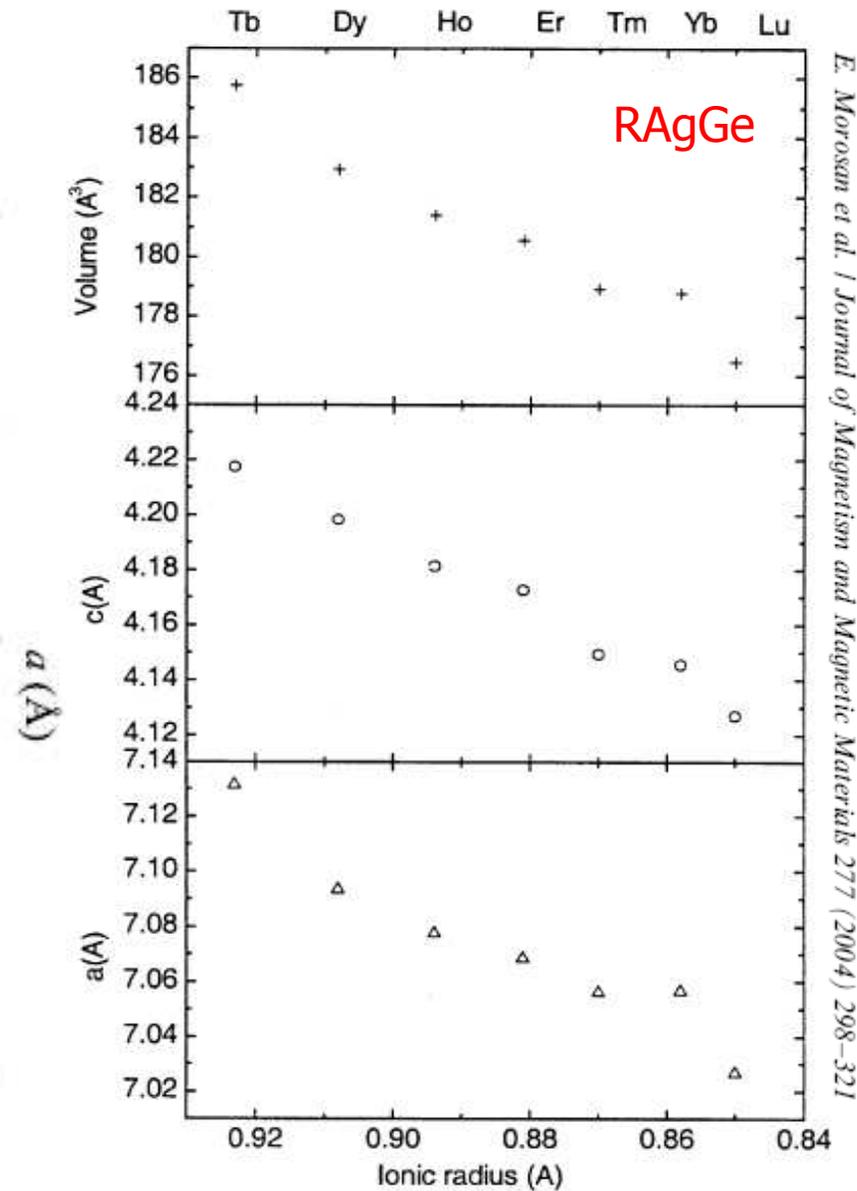
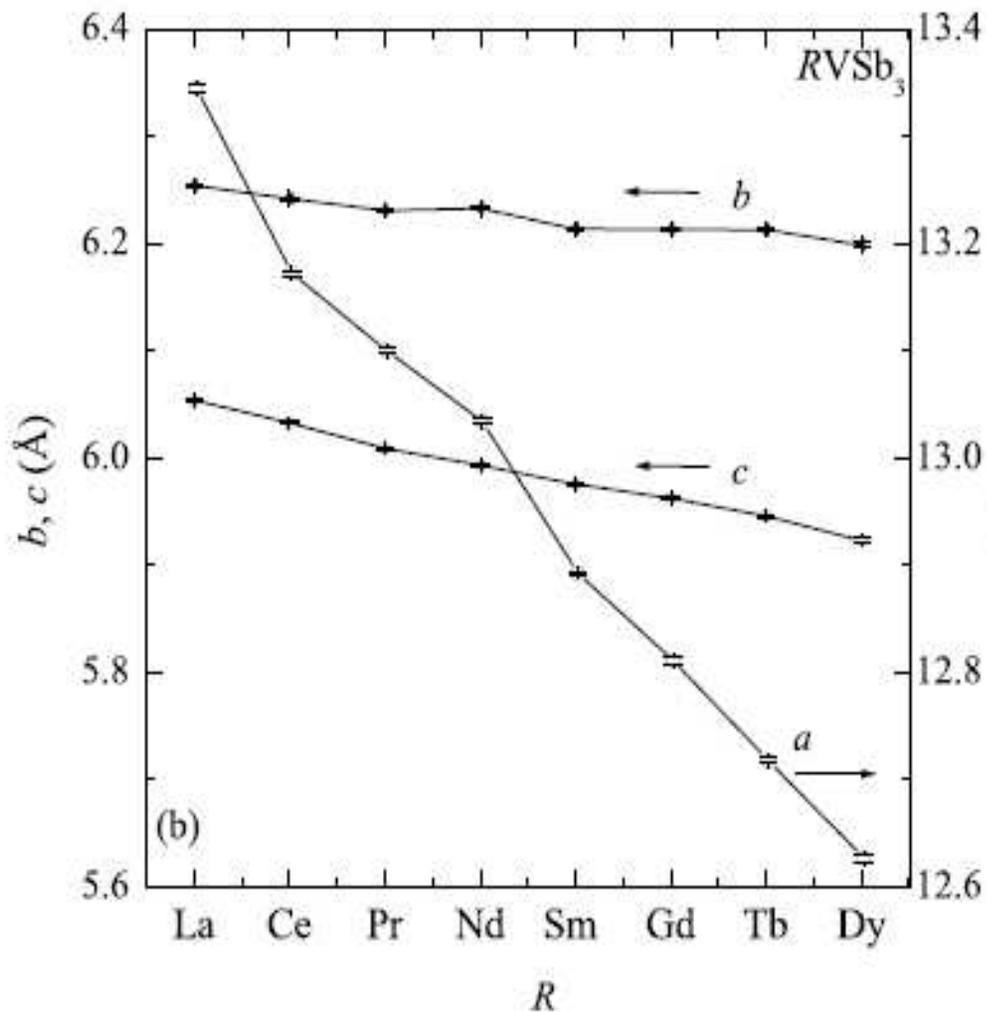


This contraction appears in the volume of the unit cell of isostructural  $R^{3+}XY$  compounds. Note: (1)  $R^{2+}$ ,  $R^{4+}$  deviate; (2)  $a$ ,  $b$ ,  $c$  variation can be different; and (3)  $Y$  usually appears near  $Dy$ .





In many RXY series R does not span the complete rare earth series. This is often associated with the lanthanide contraction bringing the unit cell parameters into / out of ranges of stability.





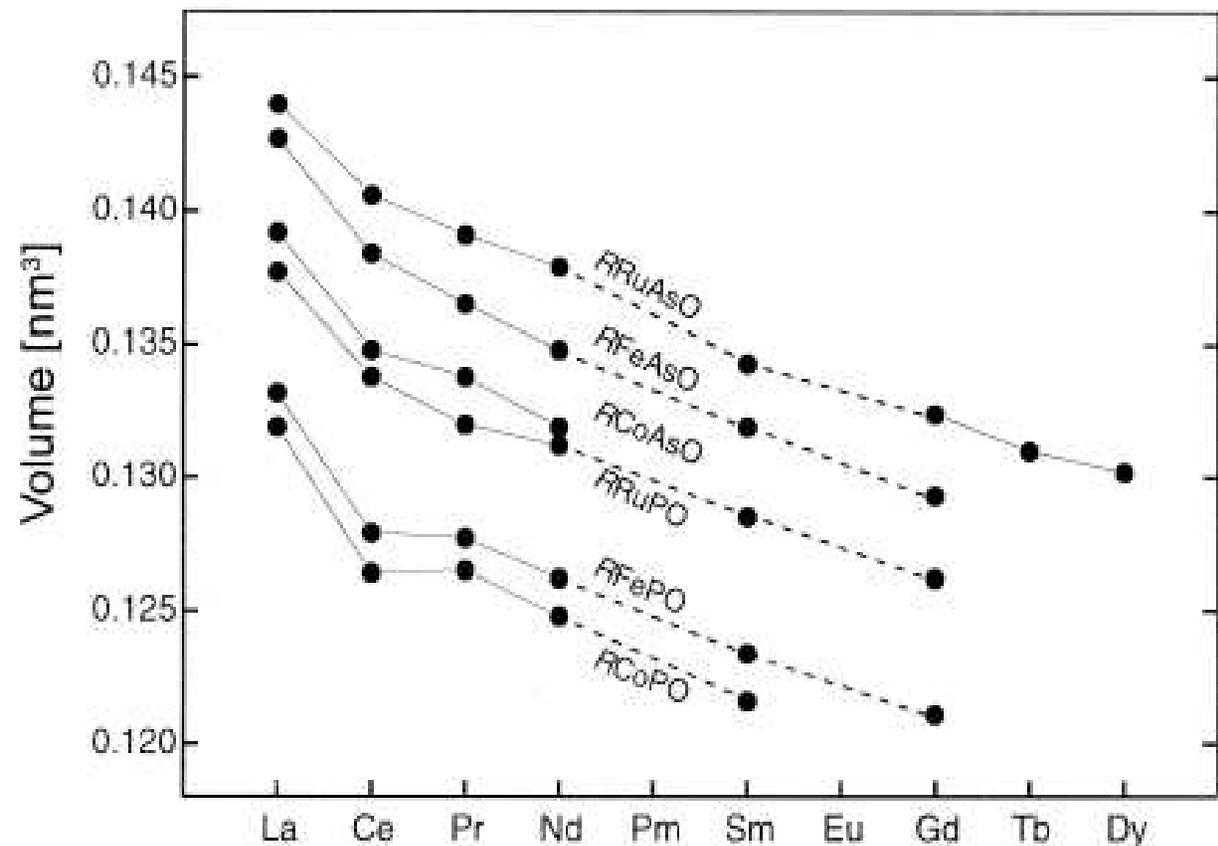
This contraction can often be thought of as a way of approximating either pressure or stress. This is particularly relevant in the current, very hot, topic of superconductivity in the  $R\text{FeAs}(\text{O}_{1-x}\text{F}_x)$  compounds.

(1) For  $x \sim 0.15$  and  $R = \text{La}$  superconductivity was found with  $T_c \sim 30 \text{ K}$

(2) Hydrostatic pressure of  $\sim 2 \text{ GPa}$  (20 kbar) increased  $T_c$  to  $\sim 55 \text{ K}$

Subsequently it has been found that for  $x \sim 0.15$  and  $R = \text{Ce} - \text{Gd}$   $T_c \sim 50 - 55 \text{ K}$

For this series pressure and lanthanide contraction seem to stabilize the same superconducting ground state.





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# Magnetization and susceptibility

The rare earth series really comes into its own when there is a need to tune magnetism. By controlling  $S$ ,  $L$ ,  $J$  we can get a wide variety of magnetic properties:  $\mu_{\text{eff}}$ ,  $\mu_{\text{sat}}$  and coupling.

		$f$ -shell ( $l = 3$ )							$S$	$L =  \sum l_z $	$J$		
$n$	$l_z = 3, 2, 1, 0, -1, -2, -3$												
Ce	1	↓							1/2	3	5/2	} $J =  L - S $	$^2F_{5/2}$
Pr	2	↓	↓						1	5	4		$^3H_4$
Nd	3	↓	↓	↓					3/2	6	9/2		$^4I_{9/2}$
Pm	4	↓	↓	↓	↓				2	6	4		$^5I_4$
Sm	5	↓	↓	↓	↓	↓			5/2	5	5/2		$^6H_{5/2}$
Eu	6	↓	↓	↓	↓	↓	↓		3	3	0		$^7F_0$
Gd	7	↓	↓	↓	↓	↓	↓		7/2	0	7/2		$^8S_{7/2}$
Tb	8	↑↓	↑	↑	↑	↑	↑		3	3	6	} $J = L + S$	$^7F_6$
Dy	9	↑↓	↑↓	↑	↑	↑	↑		5/2	5	15/2		$^6H_{15/2}$
Ho	10	↑↓	↑↓	↑↓	↑	↑	↑		2	6	8		$^5I_8$
Er	11	↑↓	↑↓	↑↓	↑↓	↑	↑		3/2	6	15/2		$^4I_{15/2}$
Tm	12	↑↓	↑↓	↑↓	↑↓	↑↓	↑		1	5	6		$^3H_6$
Yb	13	↑↓	↑↓	↑↓	↑↓	↑↓	↑↓		1/2	3	7/2		$^2F_{7/2}$
Lu	14	↑↓	↑↓	↑↓	↑↓	↑↓	↑↓		0	0	0		$^1S_0$



# Magnetization and susceptibility

**Table 1** Effective magneton numbers  $p$  for trivalent lanthanide group ions  
(Near room temperature)

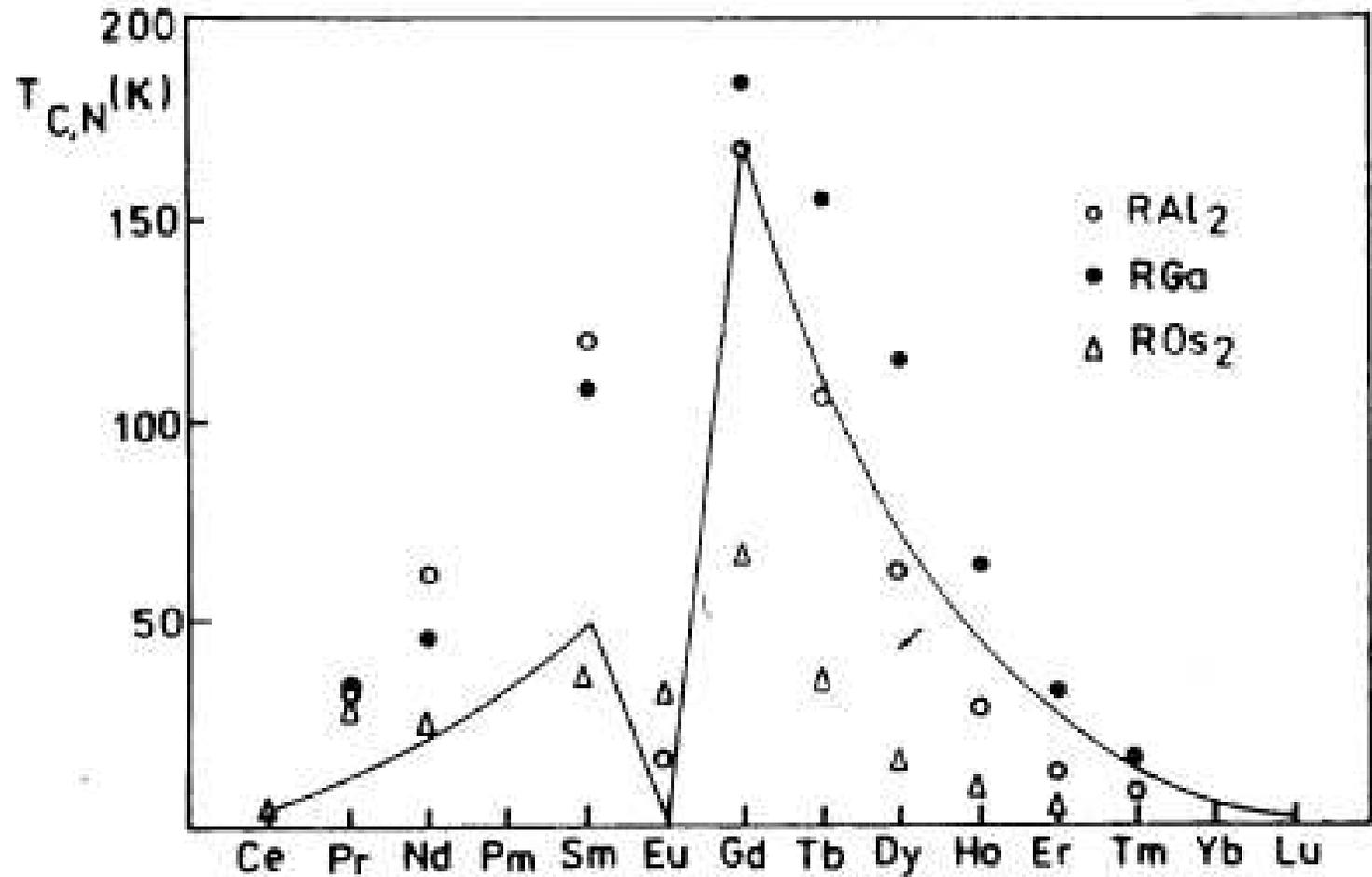
Kittel, Introduction to Solid State physics 4<sup>th</sup> edition

Ion	Configuration	Basic level	$p(\text{calc}) = g[J(J + 1)]^{\frac{1}{2}}$	$p(\text{exp}),$ approximate
Ce <sup>3+</sup>	4f <sup>1</sup> 5s <sup>2</sup> p <sup>6</sup>	<sup>2</sup> F <sub>5/2</sub>	2.54	2.4
Pr <sup>3+</sup>	4f <sup>2</sup> 5s <sup>2</sup> p <sup>6</sup>	<sup>3</sup> H <sub>4</sub>	3.58	3.5
Nd <sup>3+</sup>	4f <sup>3</sup> 5s <sup>2</sup> p <sup>6</sup>	<sup>4</sup> I <sub>9/2</sub>	3.62	3.5
Pm <sup>3+</sup>	4f <sup>4</sup> 5s <sup>2</sup> p <sup>6</sup>	<sup>5</sup> I <sub>4</sub>	2.68	—
Sm <sup>3+</sup>	4f <sup>5</sup> 5s <sup>2</sup> p <sup>6</sup>	<sup>6</sup> H <sub>5/2</sub>	0.84	1.5
Eu <sup>3+</sup>	4f <sup>6</sup> 5s <sup>2</sup> p <sup>6</sup>	<sup>7</sup> F <sub>0</sub>	0	3.4
Gd <sup>3+</sup>	4f <sup>7</sup> 5s <sup>2</sup> p <sup>6</sup>	<sup>8</sup> S <sub>7/2</sub>	7.94	8.0
Tb <sup>3+</sup>	4f <sup>8</sup> 5s <sup>2</sup> p <sup>6</sup>	<sup>7</sup> F <sub>6</sub>	9.72	9.5
Dy <sup>3+</sup>	4f <sup>9</sup> 5s <sup>2</sup> p <sup>6</sup>	<sup>6</sup> H <sub>15/2</sub>	10.63	10.6
Ho <sup>3+</sup>	4f <sup>10</sup> 5s <sup>2</sup> p <sup>6</sup>	<sup>5</sup> I <sub>8</sub>	10.60	10.4
Er <sup>3+</sup>	4f <sup>11</sup> 5s <sup>2</sup> p <sup>6</sup>	<sup>4</sup> I <sub>15/2</sub>	9.59	9.5
Tm <sup>3+</sup>	4f <sup>12</sup> 5s <sup>2</sup> p <sup>6</sup>	<sup>3</sup> H <sub>6</sub>	7.57	7.3
Yb <sup>3+</sup>	4f <sup>13</sup> 5s <sup>2</sup> p <sup>6</sup>	<sup>2</sup> F <sub>7/2</sub>	4.54	4.5



In addition to being able to vary  $S$ ,  $L$ ,  $J$  as well as  $\mu_{\text{eff}}$  and  $\mu_{\text{sat}}$ , by projecting the  $S$ 's interaction onto the total angular momentum,  $J$ , and using mean field theory we find that  $T_N = (\text{Const.}) * (g_J - 1)^2 J(J + 1)$ .

$(g_J - 1)^2 J(J + 1)$  is referred to as the de Gennes factor and is often denoted by  $dG$ .



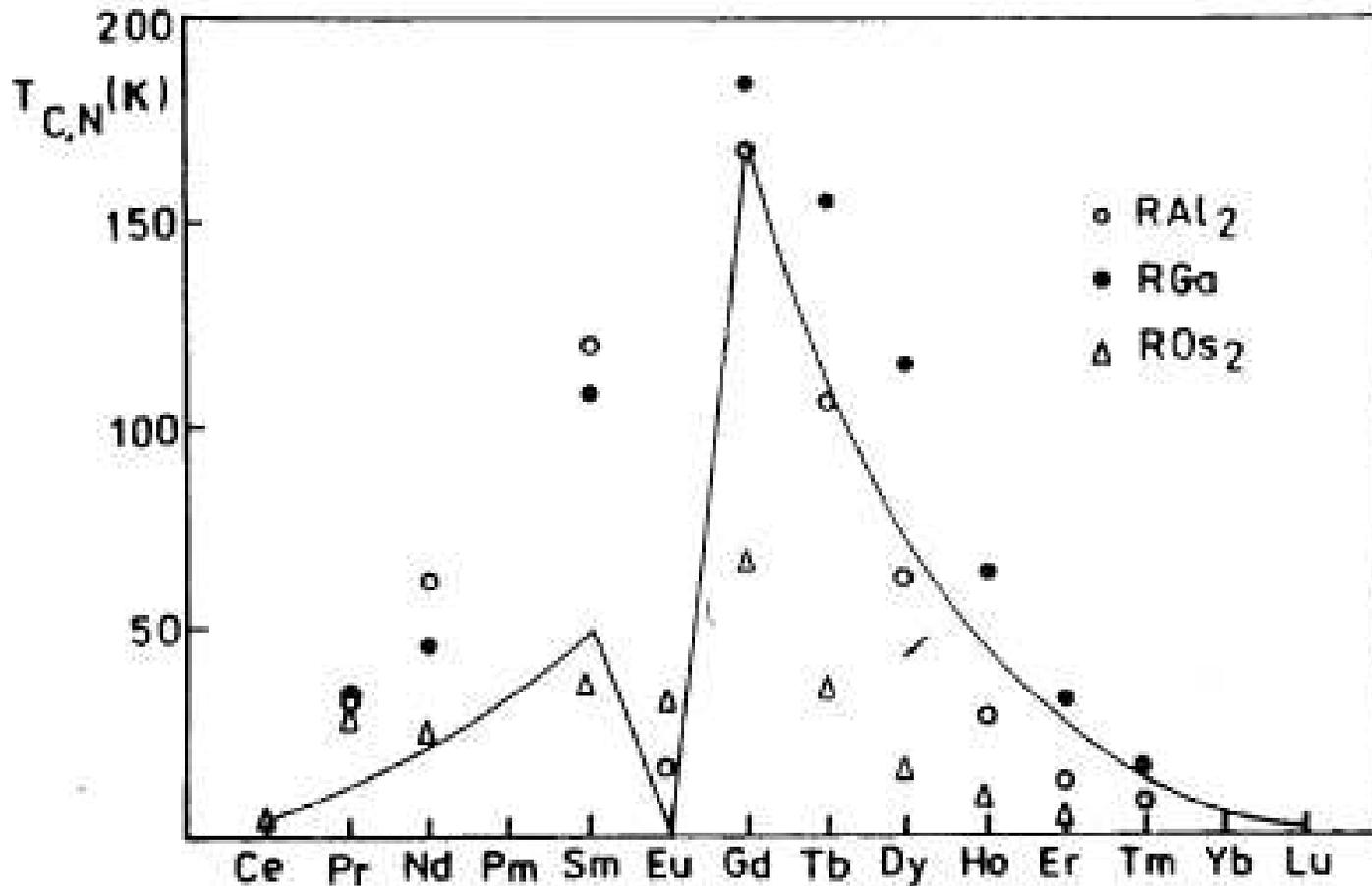
$$T_N = \frac{3\pi n^2}{k_B E_F} J_{\text{Sr}}^2 (g_J - 1)^2 J(J + 1) \sum_{i \neq 0} F(2k_F R_{O_i}) \cos(\vec{k}_O \cdot \vec{R}_{O_i})$$



dG scaling clearly illustrates the difference between the light (La – Eu) and heavy (Gd – Lu) rare earths....

57	58	59	60	61	62	63	64	65	66	67	68	69	70
<b>La</b>	<b>Ce</b>	<b>Pr</b>	<b>Nd</b>	<b>Pm</b>	<b>Sm</b>	<b>Eu</b>	<b>Gd</b>	<b>Tb</b>	<b>Dy</b>	<b>Ho</b>	<b>Er</b>	<b>Tm</b>	<b>Yb</b>
138.9	140.1	140.9	144.2	146.9	150.4	152.0	157.3	158.9	162.5	164.9	167.3	168.9	173.0

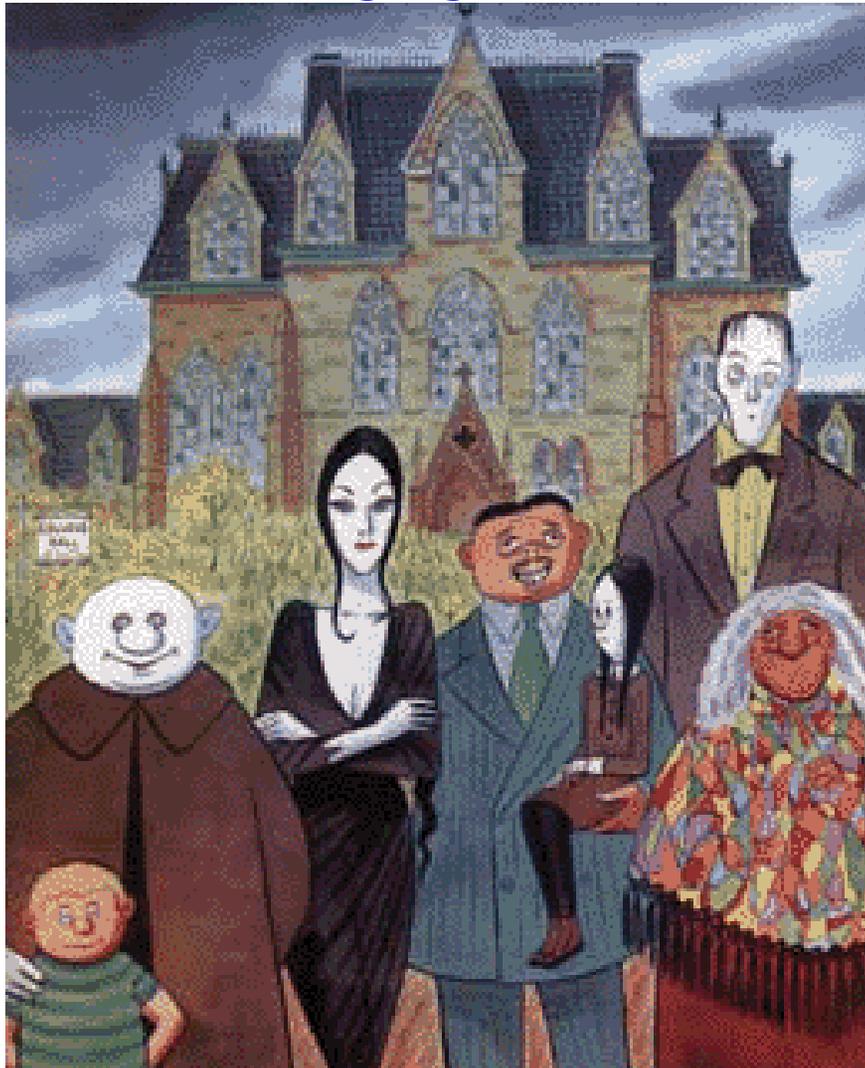
**XXX** **XXX** **3+** **XXX** **XXX** **XXX** **3+** **3+** **3+** **3+** **3+** **3+** **3+** **XXX**  
**hyb** **sng** **OK** **HOT** **Hund** **div** **OK** **OK** **OK** **OK** **OK** **OK** **OK** **hyb**



# The light and heavy rare earths are like two different families

57	58	59	60	61	62	63	64	65	66	67	68	69	70
<b>La</b>	<b>Ce</b>	<b>Pr</b>	<b>Nd</b>	<b>Pm</b>	<b>Sm</b>	<b>Eu</b>	<b>Gd</b>	<b>Tb</b>	<b>Dy</b>	<b>Ho</b>	<b>Er</b>	<b>Tm</b>	<b>Yb</b>
138.9	140.1	140.9	144.2	146.9	150.4	152.0	157.3	158.9	162.5	164.9	167.3	168.9	173.0

Poorly behaved, but interesting, lights



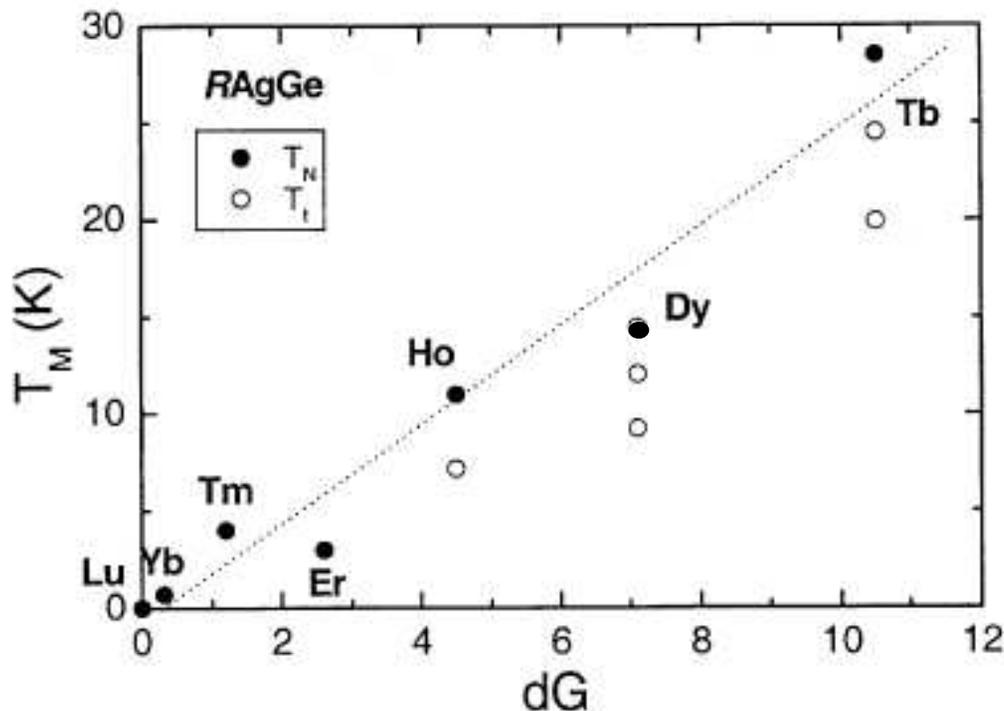
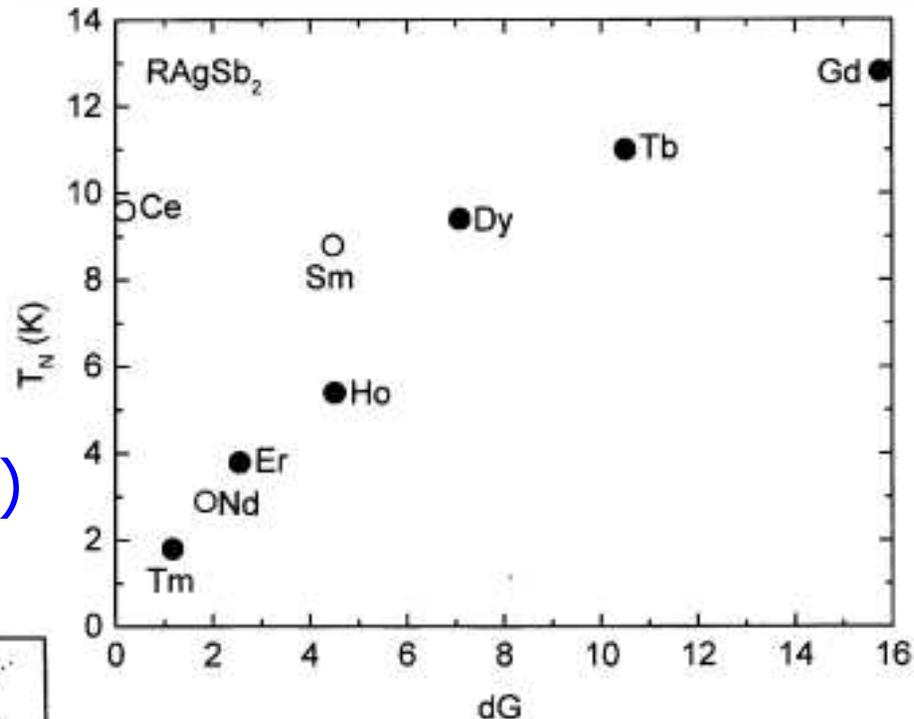
Well behaved heavies that are predicable and useful in many of their properties.




 dG scaling can be used to control / predict ordering temperature, especially for R = heavy members.

For RAgSb<sub>2</sub> R = Nd is on dG line but other lights are off (as usual)

*K.D. Myers et al. / Journal of Magnetism and Magnetic Materials 205 (1999) 27–52*

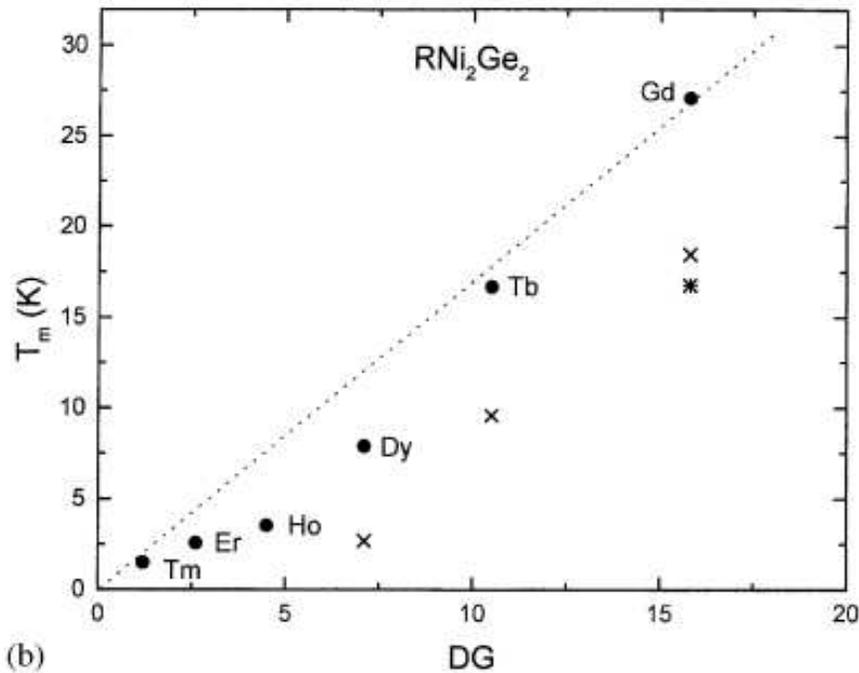


For RAgGe there is fair dG scaling even for lower temperature, order to order, transitions (often incommensurate to commensurate long range order).

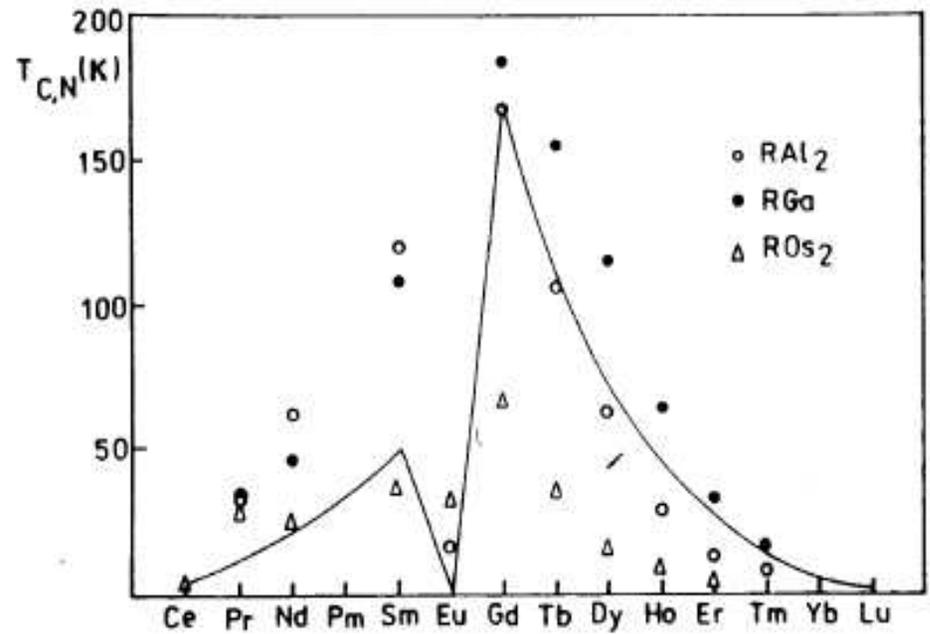
*E. Morosan et al. / Journal of Magnetism and Magnetic Materials 277 (2004) 298–321*



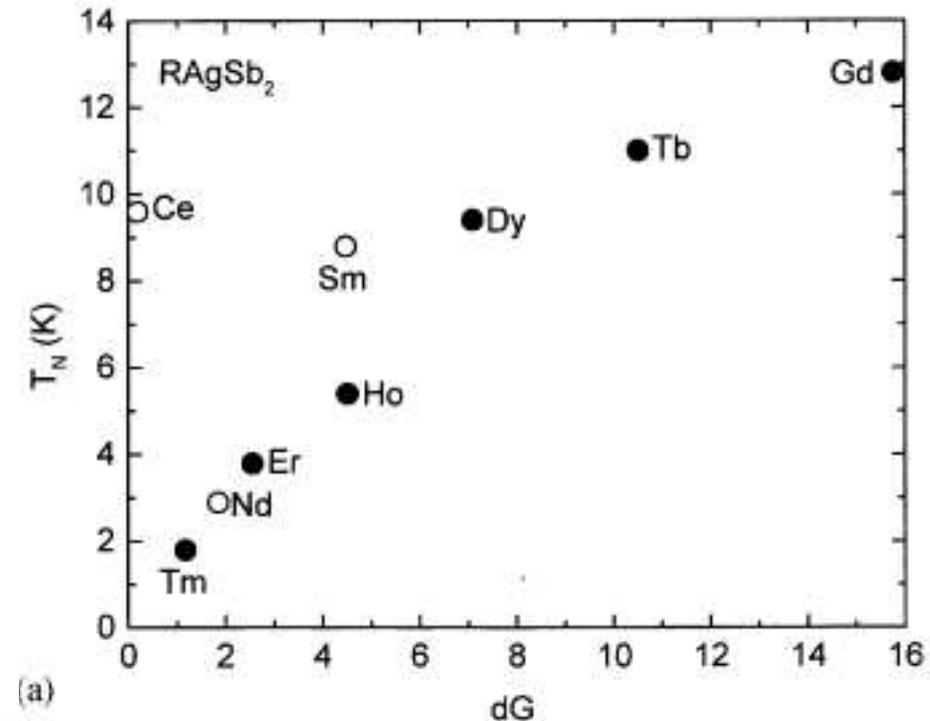
Since dG scaling predicts the R = Gd member of a series will have the highest ordering temperature (and Gd is well behaved), Gd-members of RXY series can be used as litmus tests for strength of ordering....

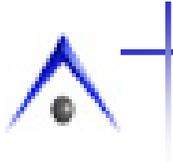


(b)

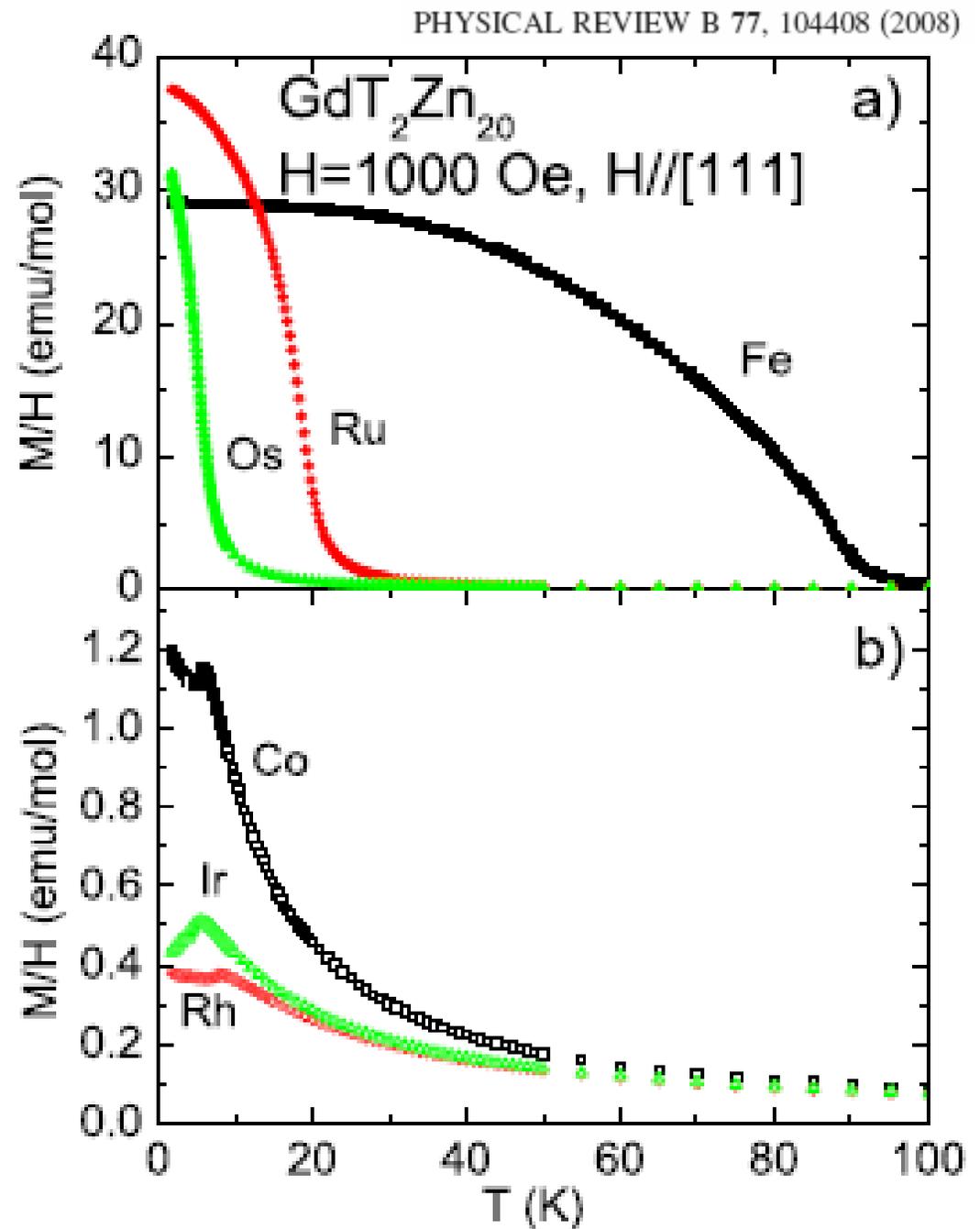


(a)

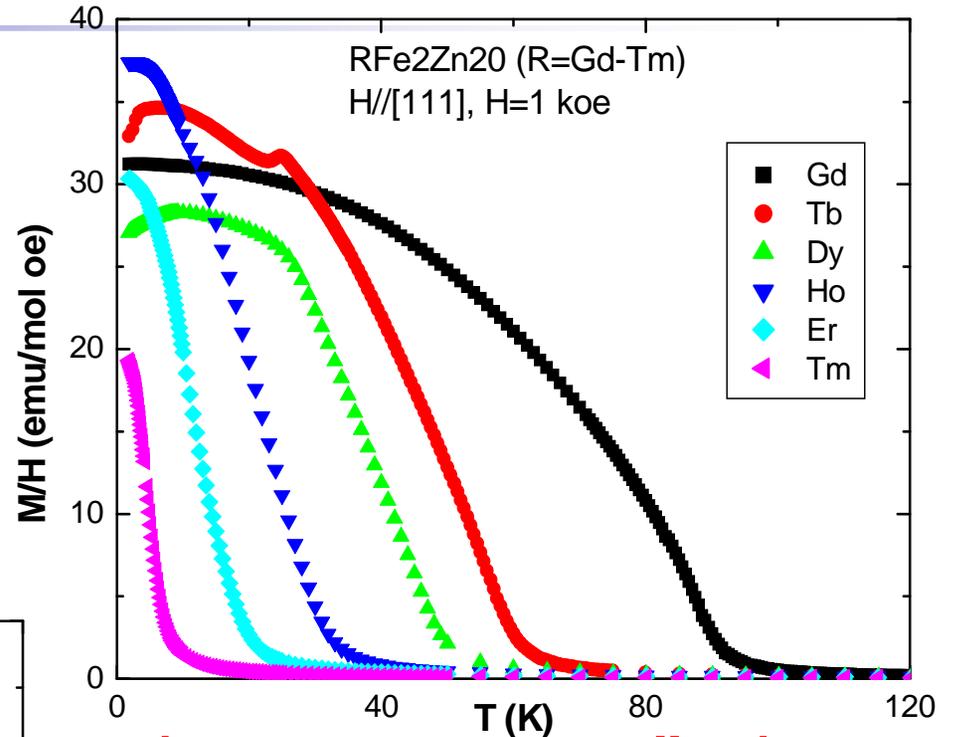
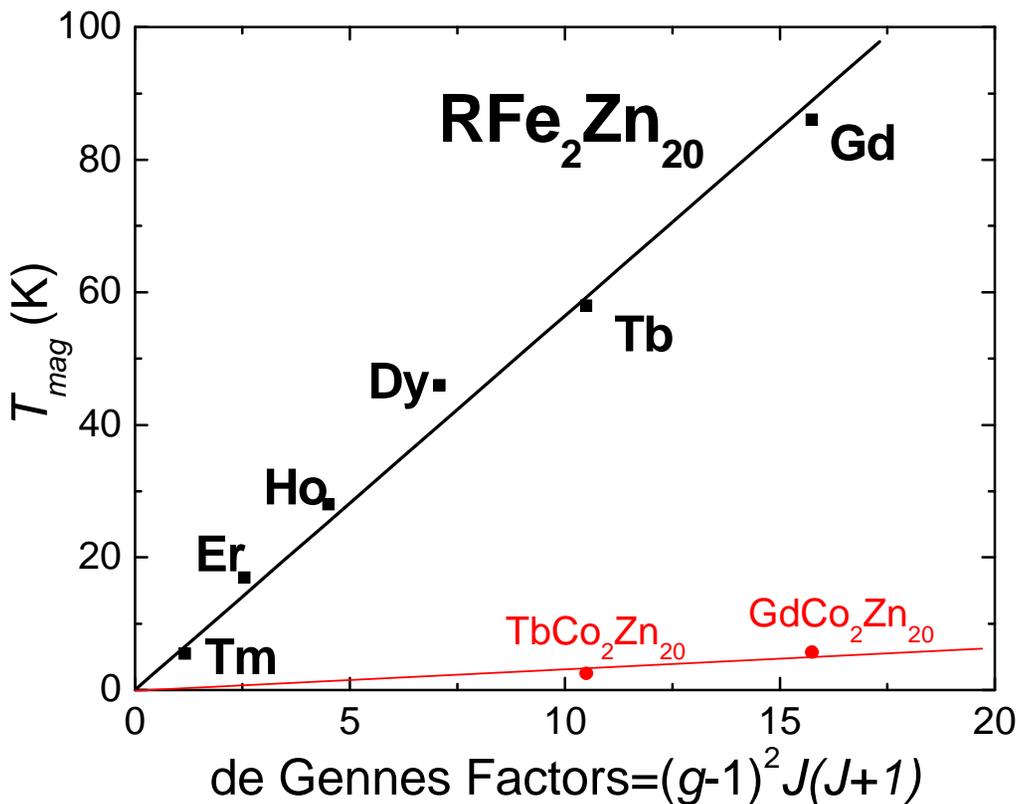




In our recent work on the dilute, rare earth bearing, intermetallic compounds  $RT_2Zn_{20}$  we used the six  $GdT_2Zn_{20}$  compounds to give us a caliper of how strong (and what type) or ordering we could expect from the respective series.



As can be seen, R= Gd is not special: The whole  $RFe_2Zn_{20}$  series has enhanced  $T_C$  values that de Gennes scale well.

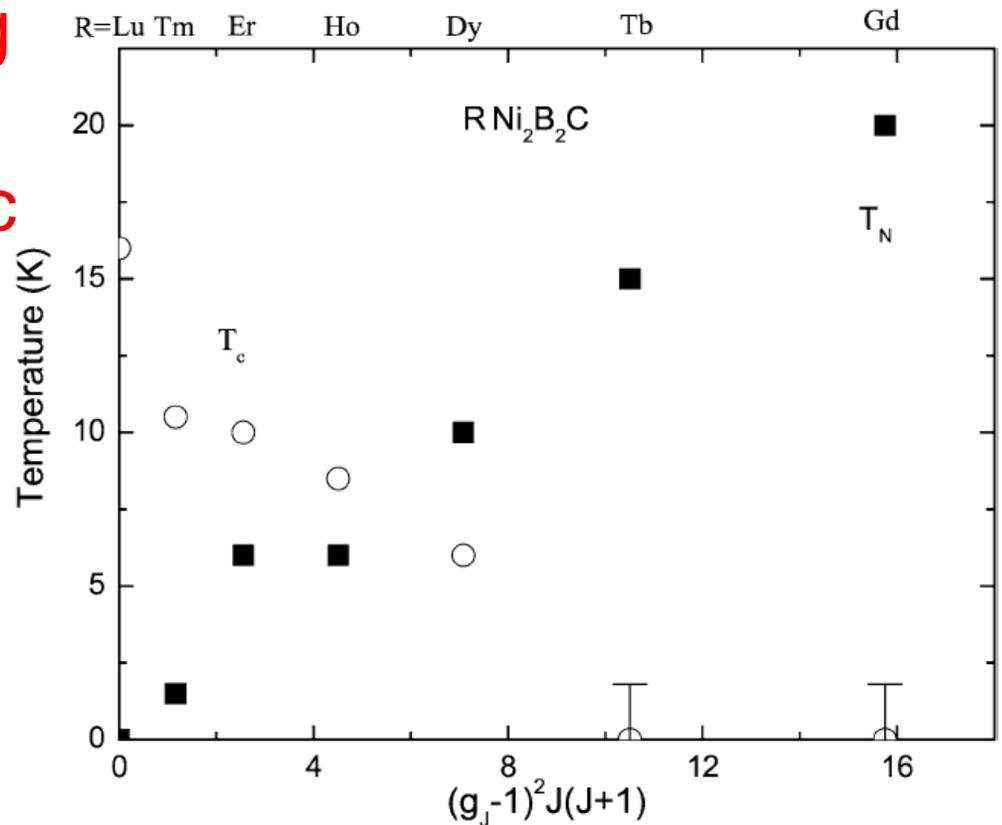


*The question is, "Why does the  $RFe_2Zn_{20}$  series manifest such high ordering temperatures?"*

The answer is Stoner enhancement of the conduction electrons matrix, e.g.  $YFe_2Zn_{20}$  is closer to the Stoner limit than Pd.

Very clear dG scaling of  $T_N$  can be seen in the  $RNi_2B_2C$  family of magnetic superconductors.

In the paramagnetic state, the suppression of  $T_c$  is also proportional to the S-s coupling: the dG factor.



Superconducting for  $R = Dy, Ho, Er, Tm, Lu, Y$  with  $T_c$  values ranging from 17 K – 6 K

Magnetic order for  $R = Gd, Tb, Dy, Ho, Er, Tm$  with  $T_N$  values ranging from 20 K to 1.5 K

More about this tomorrow.





By using the rare earths, the physicist can tune the:

Size of the unit cell,

Size of the local moment and degree of coupling,

Size and direction of anisotropy,

Amount of entropy that can be removed at low temperatures,

Band filling,

Degree of hybridization.

In terms of temperature and energy scales (another obsession of the physicist), the rare earths can be used to tune:

The magnetic ordering temperature  $T_C$  or  $T_N$

The CEF splitting or  $T_{\Delta_{\text{CEF}}}$

The Kondo temperature  $T_K$



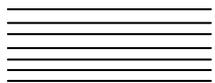
The Hund's rule groundstate multiplet,  $J$ , can be split by the crystal electric field that the rare earth ion finds itself in (associated with the point symmetry of the R ion and the details of its ligands). The CEF splitting determines (i) anisotropy and (ii) entropy, associated with 4f electrons, at a given temperature.

	$n$	$l_z = 3, 2, 1, 0, -1, -2, -3$							$S$	$L =  \sum l_z $	$J$		
Ce	1	↓							1/2	3	5/2	} $J =  L - S $	$^2F_{5/2}$
Pr	2	↓	↓						1	5	4		$^3H_4$
Nd	3	↓	↓	↓					3/2	6	9/2		$^4I_{9/2}$
Pm	4	↓	↓	↓	↓				2	6	4		$^5I_4$
Sm	5	↓	↓	↓	↓	↓			5/2	5	5/2		$^6H_{5/2}$
Eu	6	↓	↓	↓	↓	↓	↓		3	3	0		$^7F_0$
Gd	7	↓	↓	↓	↓	↓	↓	↓	7/2	0	7/2		$^8S_{7/2}$
Tb	8	↑↓	↑	↑	↑	↑	↑	↑	3	3	6	} $J = L + S$	$^7F_6$
Dy	9	↑↓	↑↓	↑	↑	↑	↑	↑	5/2	5	15/2		$^6H_{15/2}$
Ho	10	↑↓	↑↓	↑↓	↑	↑	↑	↑	2	6	8		$^5I_8$
Er	11	↑↓	↑↓	↑↓	↑↓	↑	↑	↑	3/2	6	15/2		$^4I_{15/2}$
Tm	12	↑↓	↑↓	↑↓	↑↓	↑↓	↑	↑	1	5	6		$^3H_6$
Yb	13	↑↓	↑↓	↑↓	↑↓	↑↓	↑↓	↑	1/2	3	7/2		$^2F_{7/2}$
Lu	14	↑↓	↑↓	↑↓	↑↓	↑↓	↑↓	↑↓	0	0	0		$^1S_0$



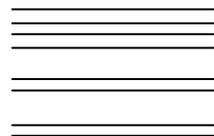
For  $Gd^{3+}$  or  $Eu^{2+}$  ( $L = 0$ ), where there is formally zero CEF splitting, or for very small CEF splitting,  $T_N$  can be well above  $T_{\Delta_{CEF}}$ . In these cases the local moment will be isotropic and full entropy will be removed through ordering.

Gd, zero splitting



OR

small splitting



Antiferromagnetic ordering  
with  $\sim R \ln 8$  entropy removal.  
No CEF anisotropy

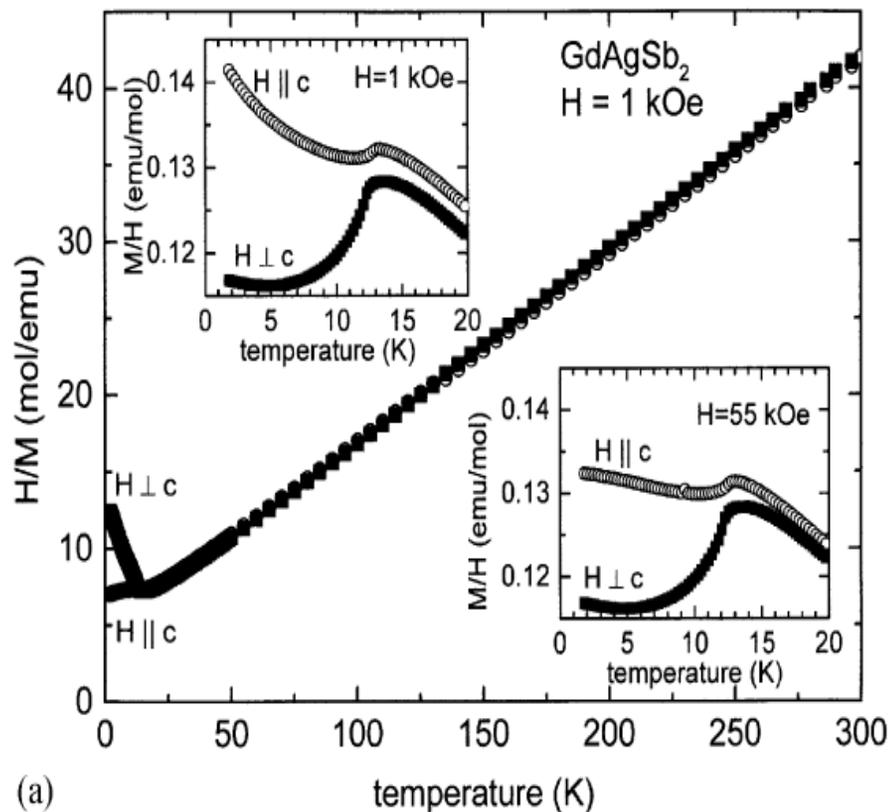
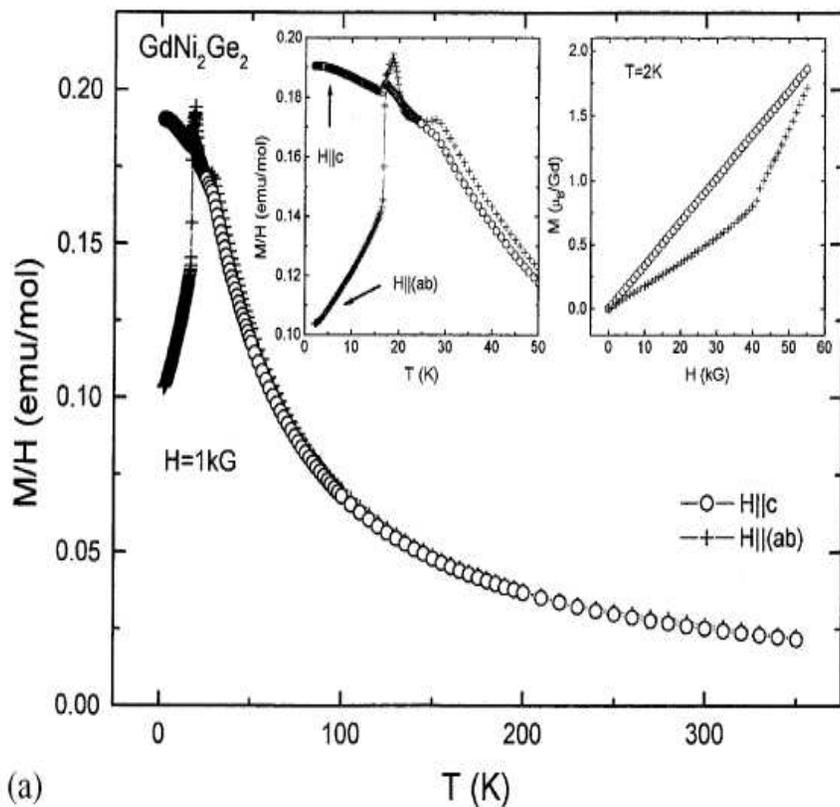
Bandstructure and  
coupling terms....



Gd members of RXY series will be isotropic

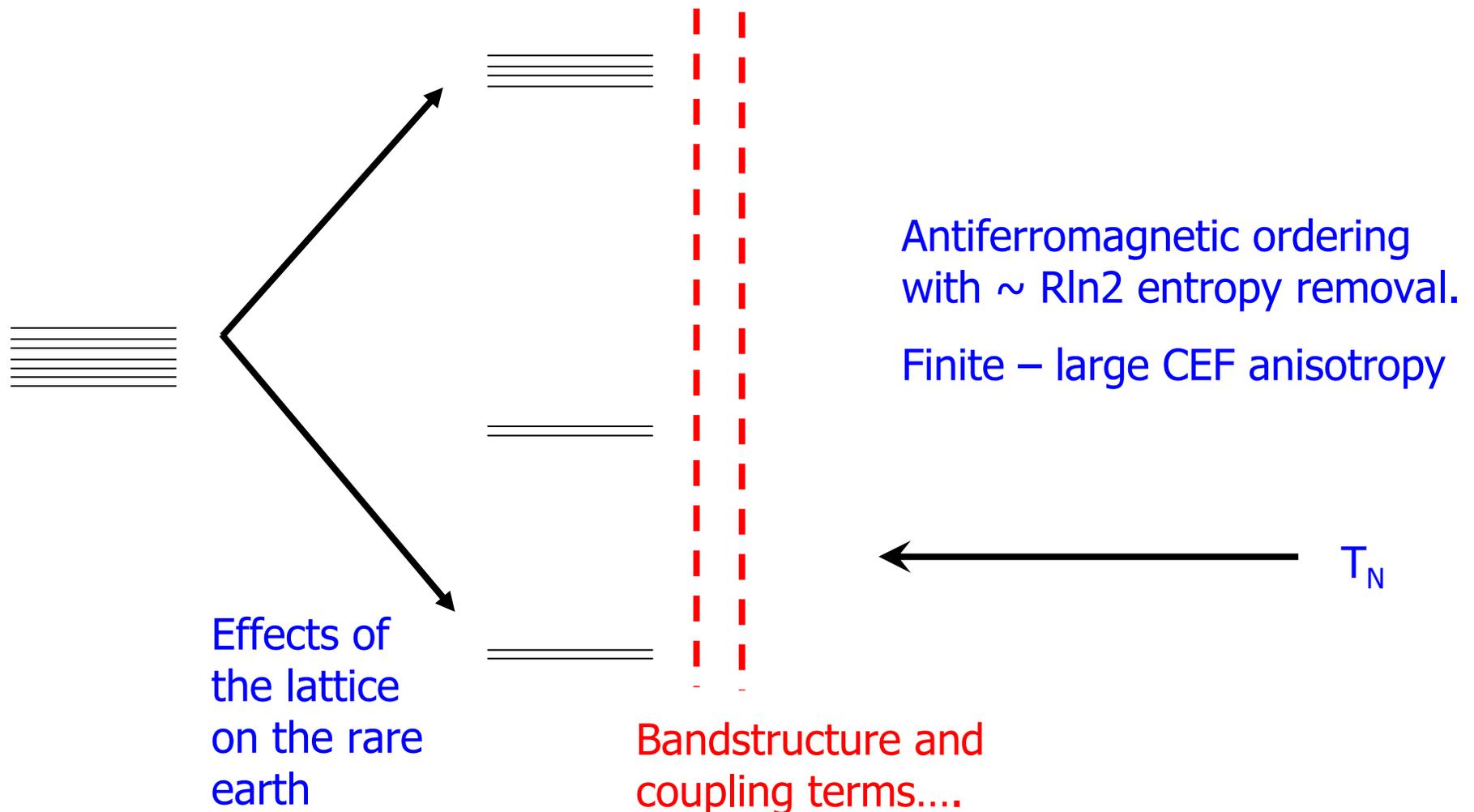
*Gd offers a model Heisenberg moment*

(this is one theoretical limit of treating moments simply)





For rare earths with finite  $J$  and  $L \neq 0$  (i.e. not  $\text{Gd}^{3+}$  or  $\text{Eu}^{2+}$ ) there will be CEF splitting of the Hund's rule ground state multiplet,  $J$ .

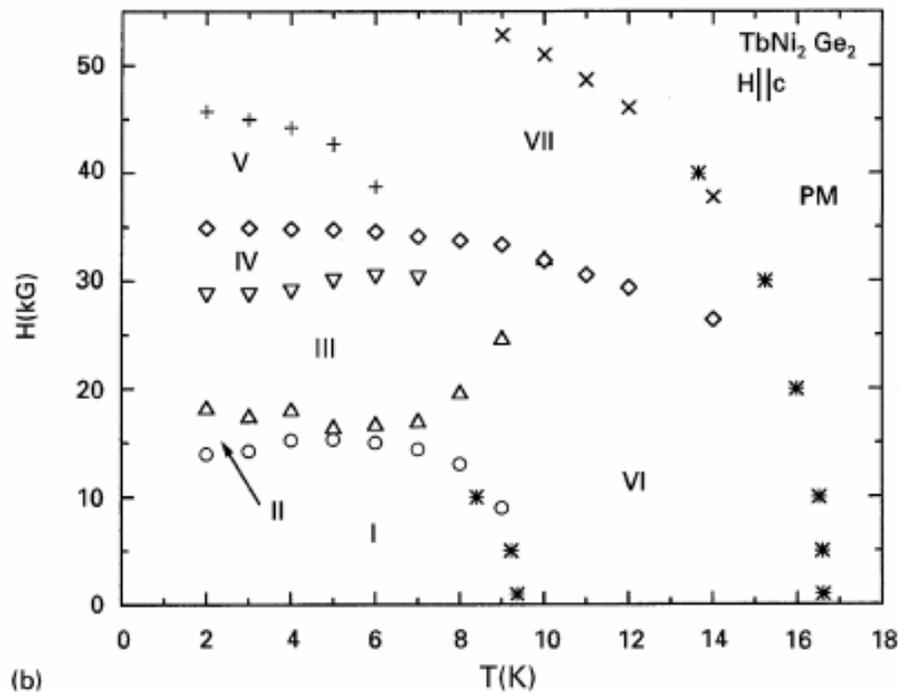
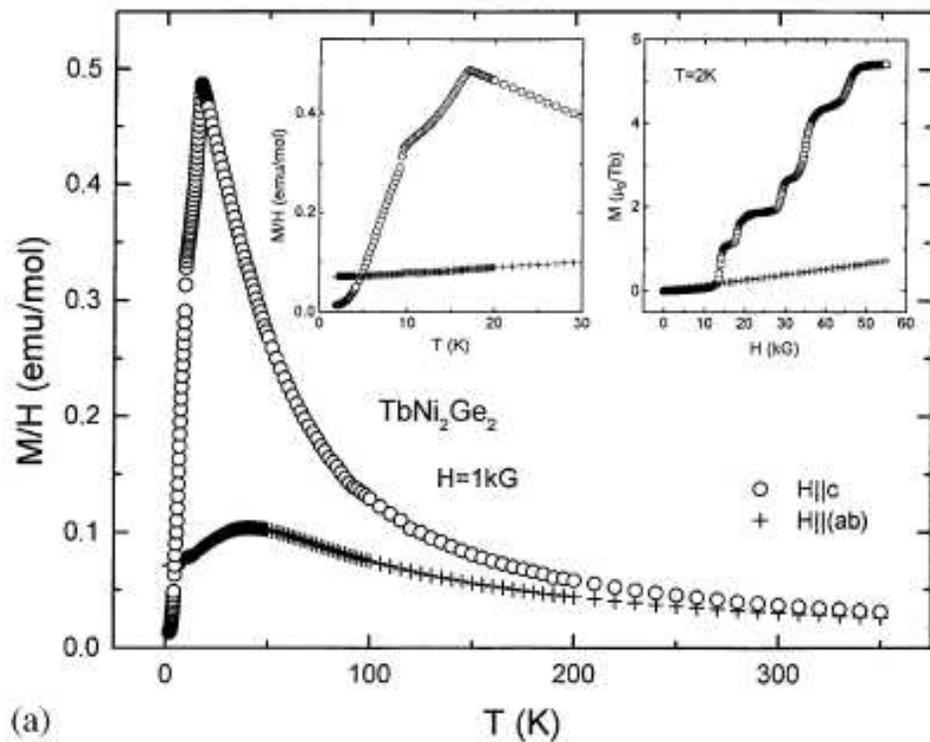


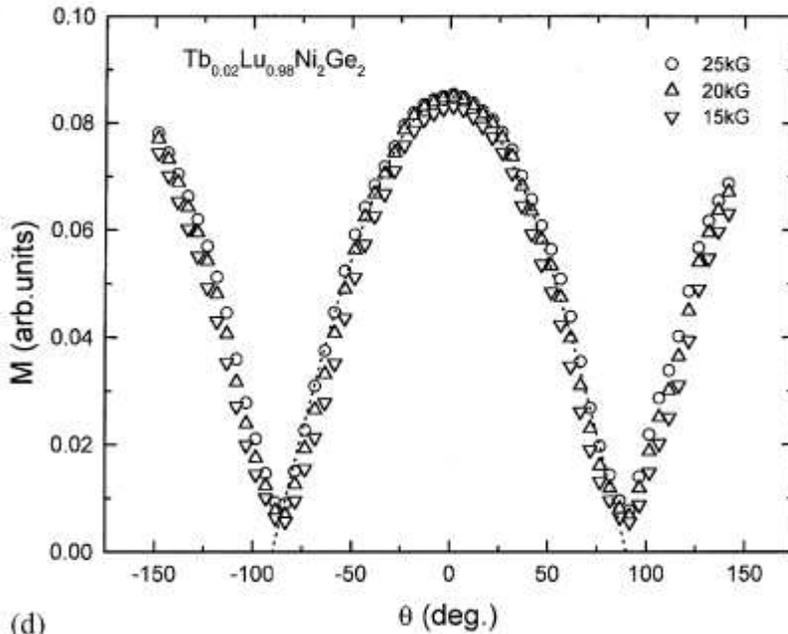


CEF anisotropy can be extreme, giving rise to the possibility of creating systems that approach the theoretical, ideally anisotropic moments.

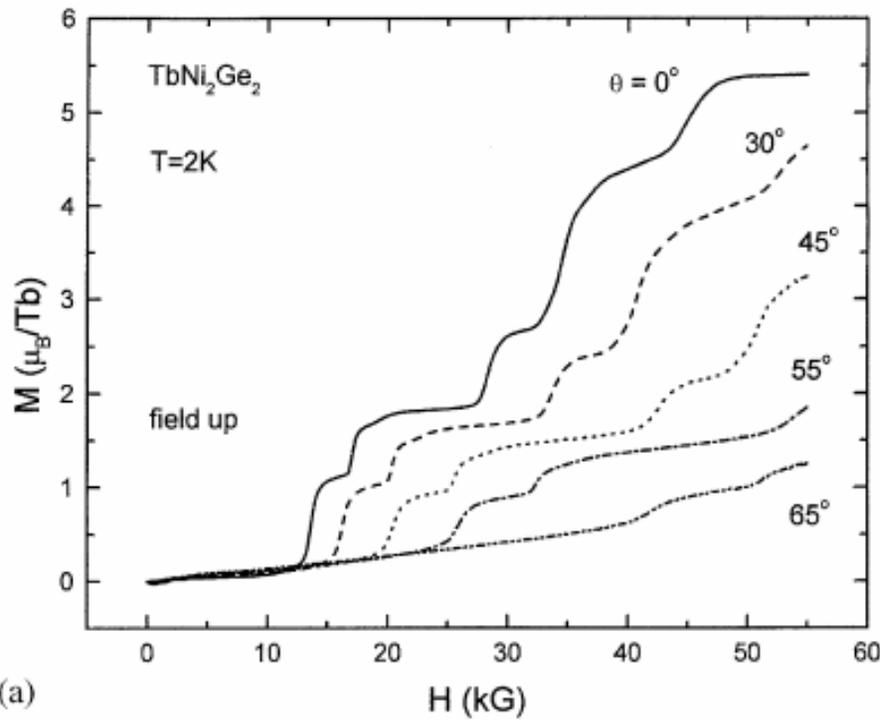
## TbNi<sub>2</sub>Ge<sub>2</sub>

Tetragonal point symmetry of Tb site leads to Ising-like moment at low temperatures, i.e. the local moment only points up or down along the c-axis



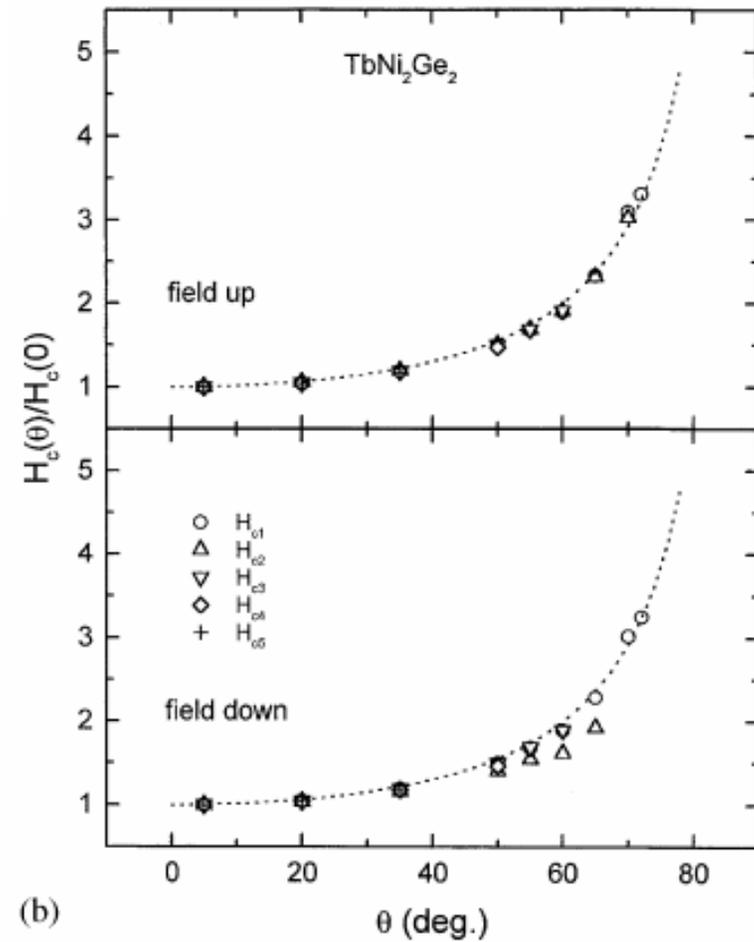


(d)



(a)

The applied magnetic field can be rotated away from the Ising axis and the metamagnetic transitions scale simply as  $1/\cos\theta$ .



(b)



It should be noted that this axial anisotropy is not only of interest to physicists interested in extreme examples of Ising systems.

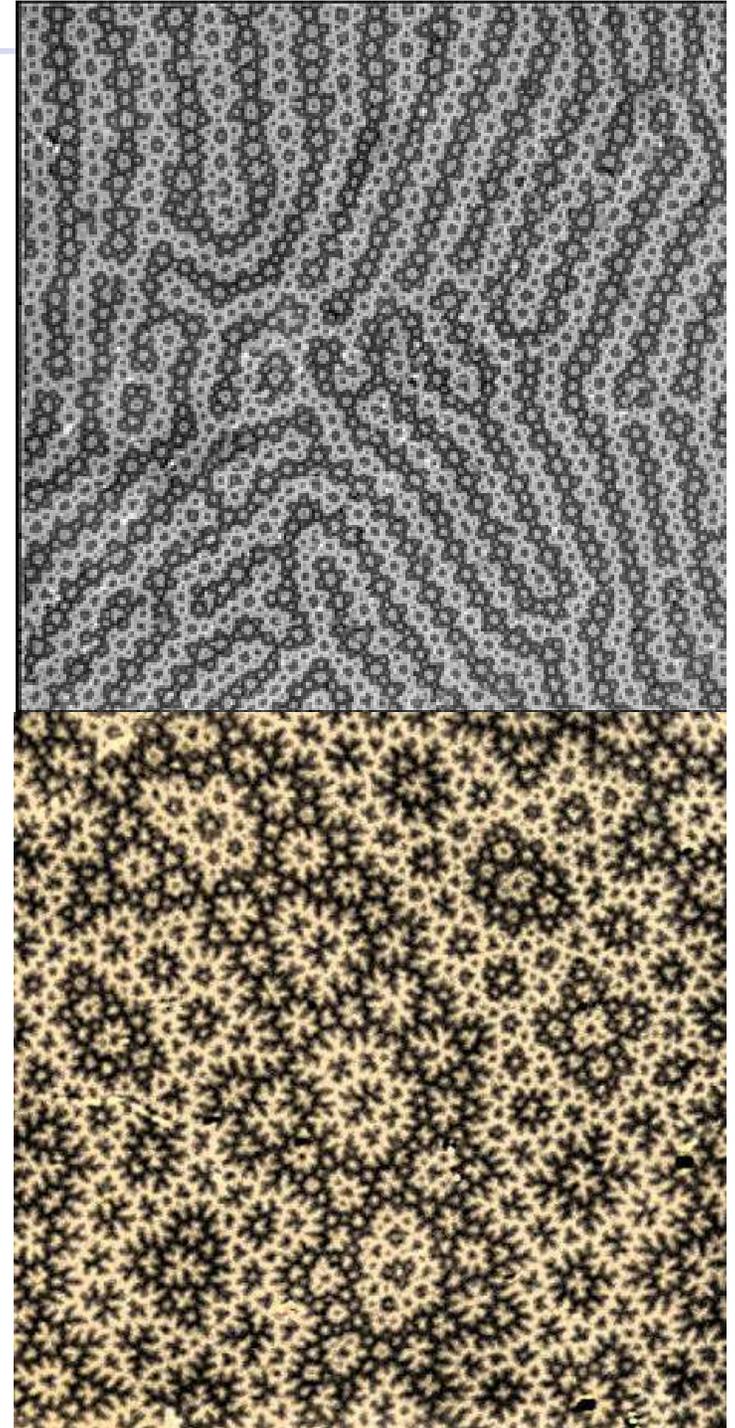
When the rare earth local moment is combined with transition metal (band) magnetism, the local moment can make the whole compound highly anisotropic.

**$\text{Nd}_2\text{Fe}_{14}\text{B}$  is a case in point.**

The well-behaved Nd ion provides an axial (Ising-like) anisotropy to the compound that makes it the industrial ferromagnetic of choice.

It is worth noting that even such an applied material is of current interest to basic research. We have found a fractal-like nature of the magnetic domains in high purity, near zero pinning, single crystals.

A. Kreyssig, R. Prozorov et al., in preparation

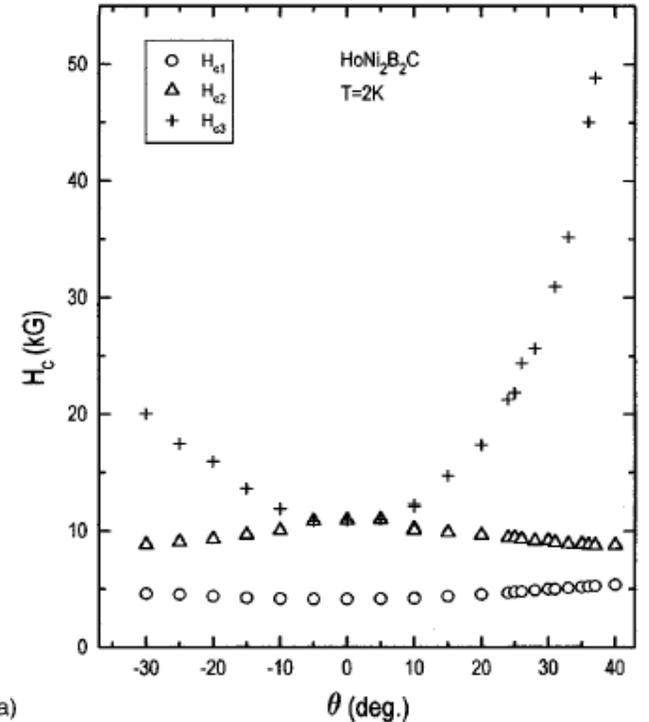




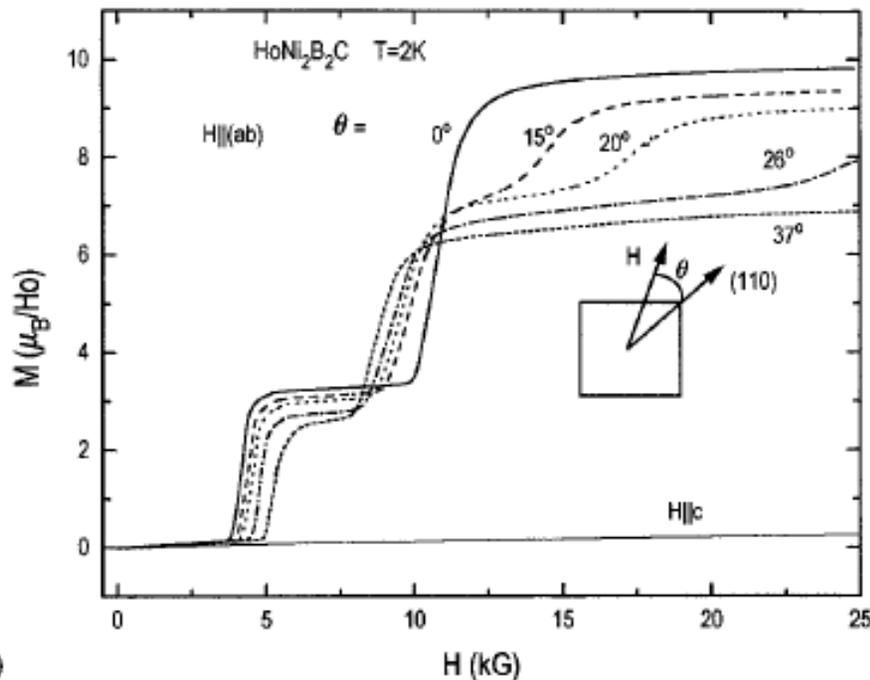
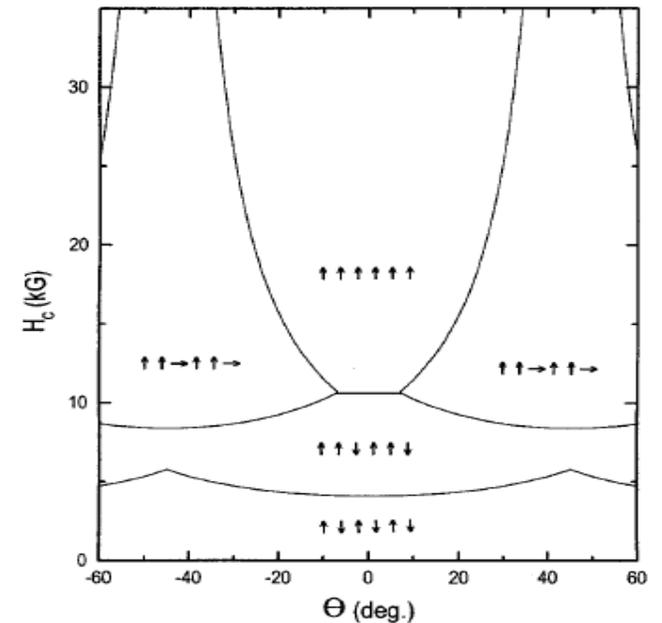
More complex, well defined, anisotropies:

## 4-state clock model in $\text{HoNi}_2\text{B}_2\text{C}$

In the case of  $\text{HoNi}_2\text{B}_2\text{C}$  we were able to determine that the CEF splitting confines the moments to the basal plane along the 110 directions, leading to a 4-state clock model type of system.



(a)

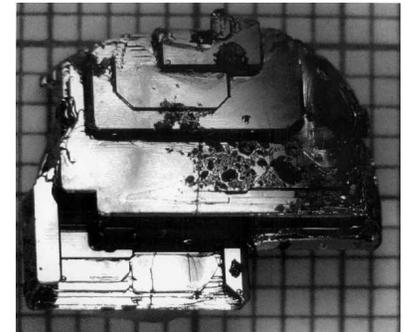


(a)

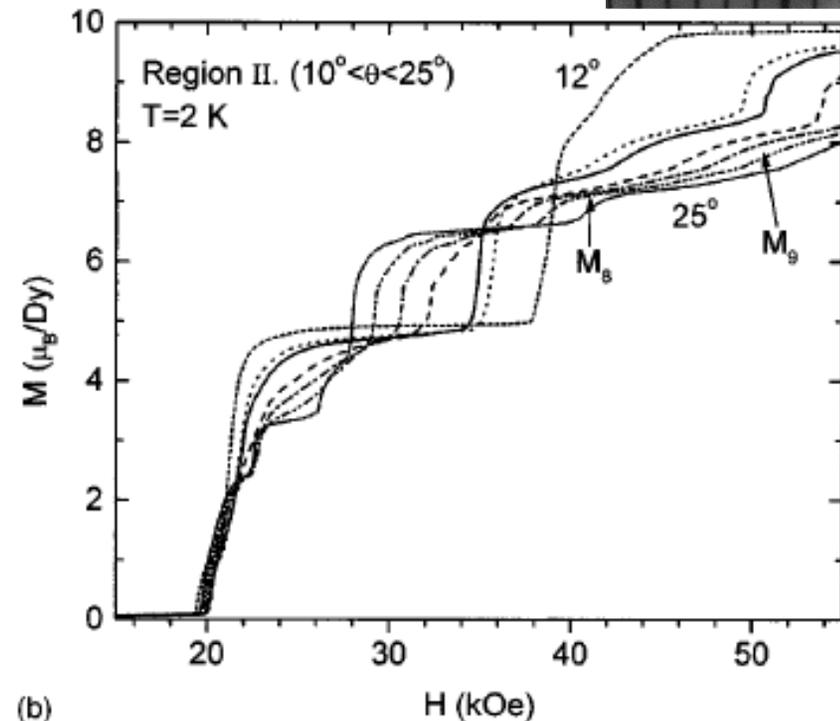
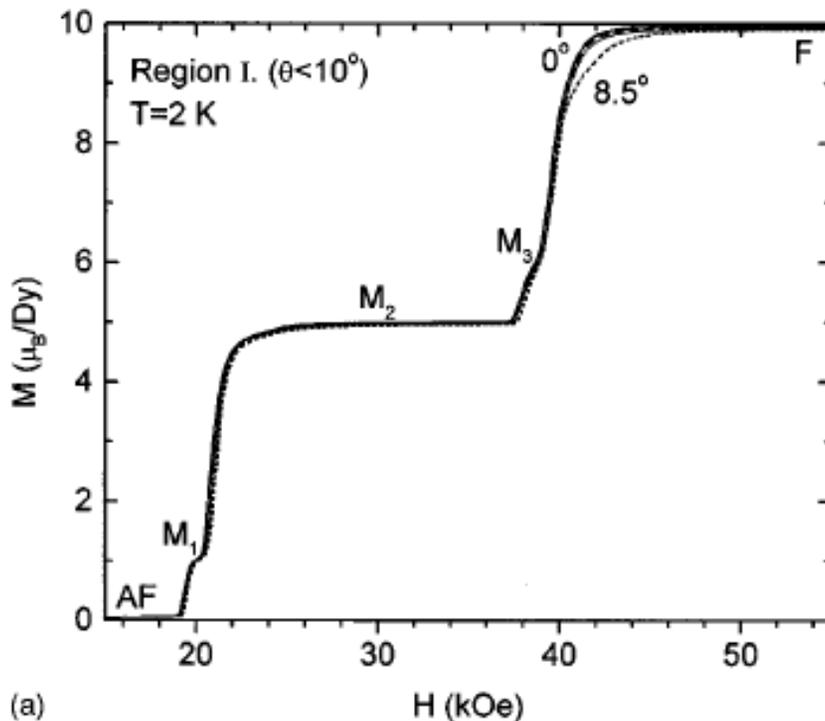


The realization that rare earth anisotropy could give rise to in-plane anisotropy shocked some groups (there was a belief that the moments would have xy isotropy). In order to show that this was a generalizable discovery....

We searched for a different crystal structure class with a single R in a tetragonal point symmetry and found similar physics in



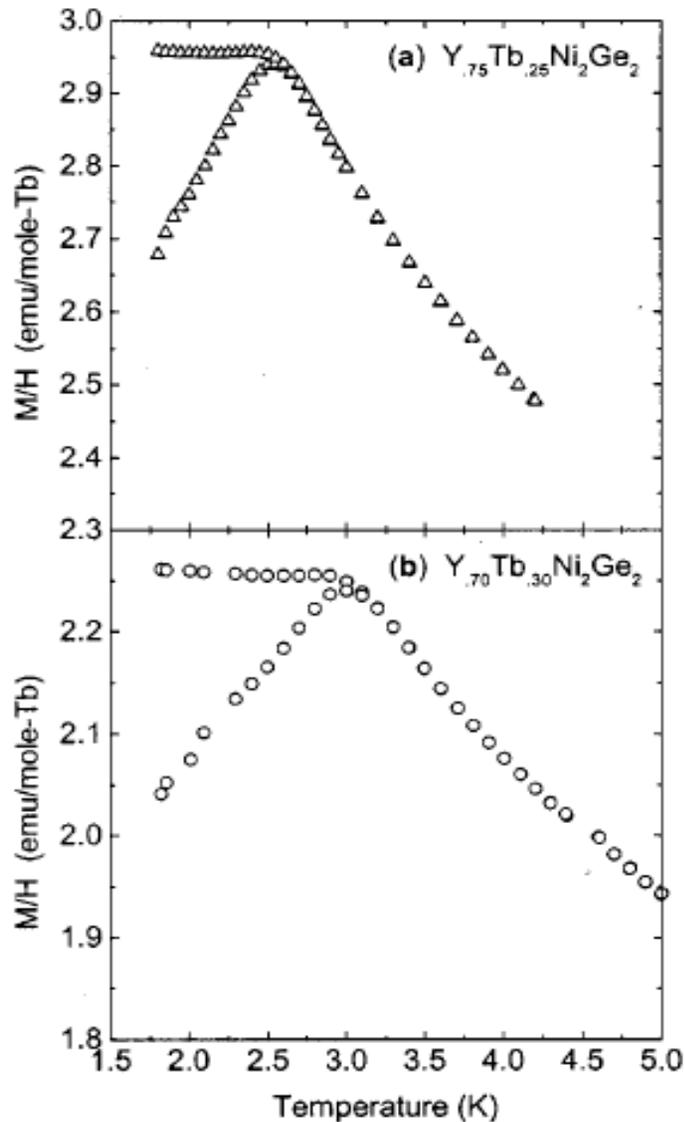
~1 g crystal of LaAgSb<sub>2</sub>





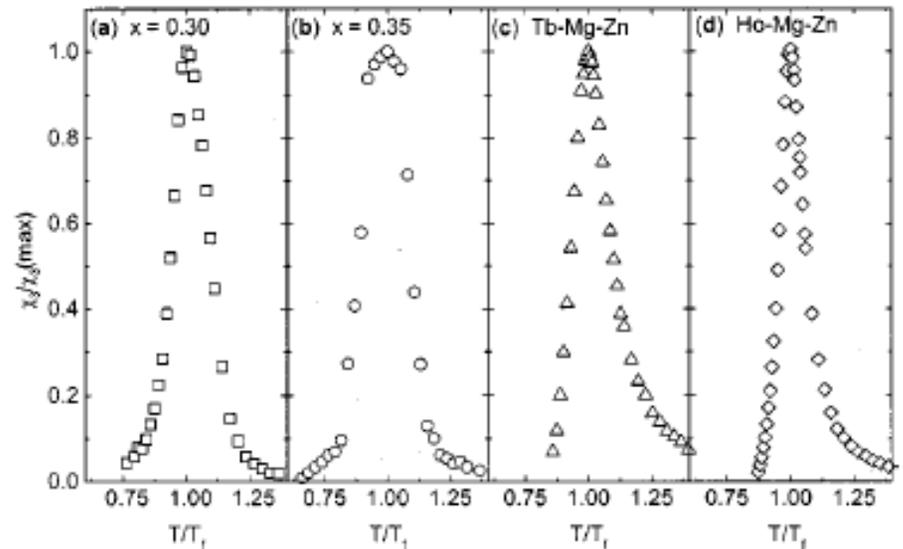
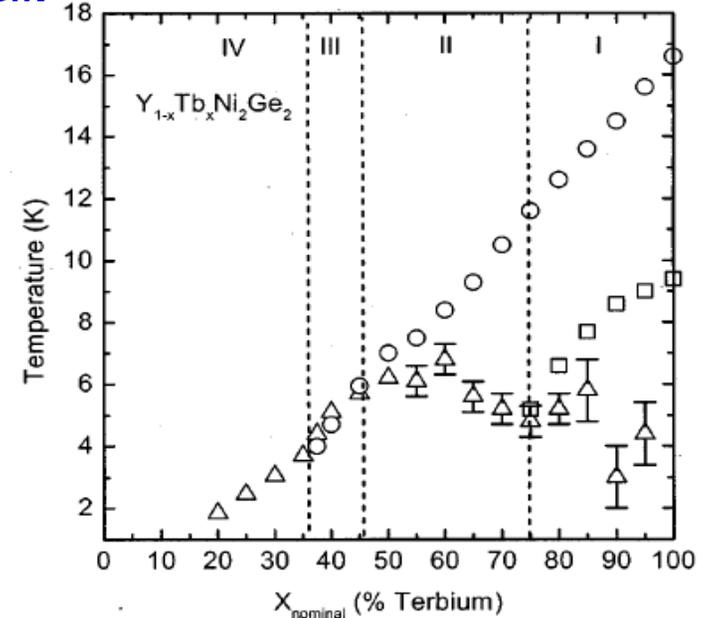


In addition to control of ordered states and field stabilized, meta-magnetic, states, the control over anisotropy that the CEF splitting offers can be used to create and study spinglass states as well.



Spinglasses part I

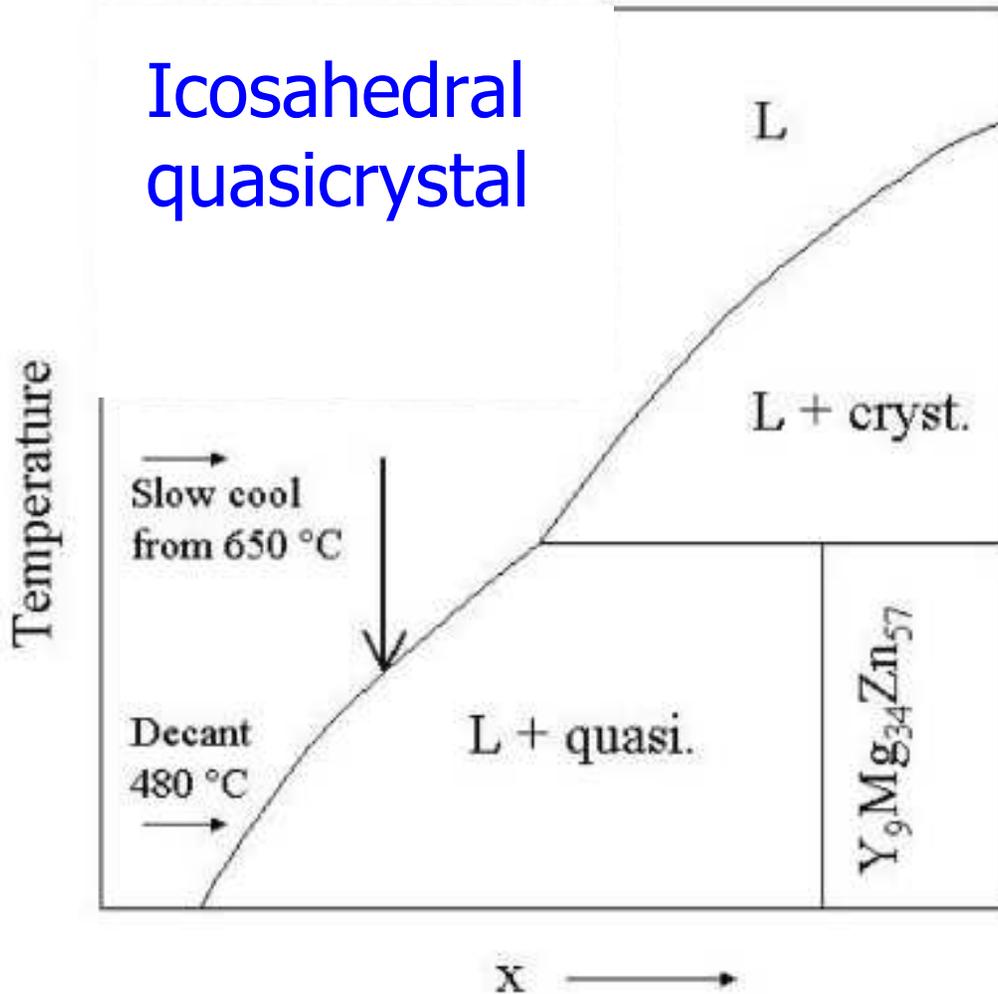
$(Y_{1-x}Tb_x)Ni_2Ge_2$   
Ising spin glass  
system



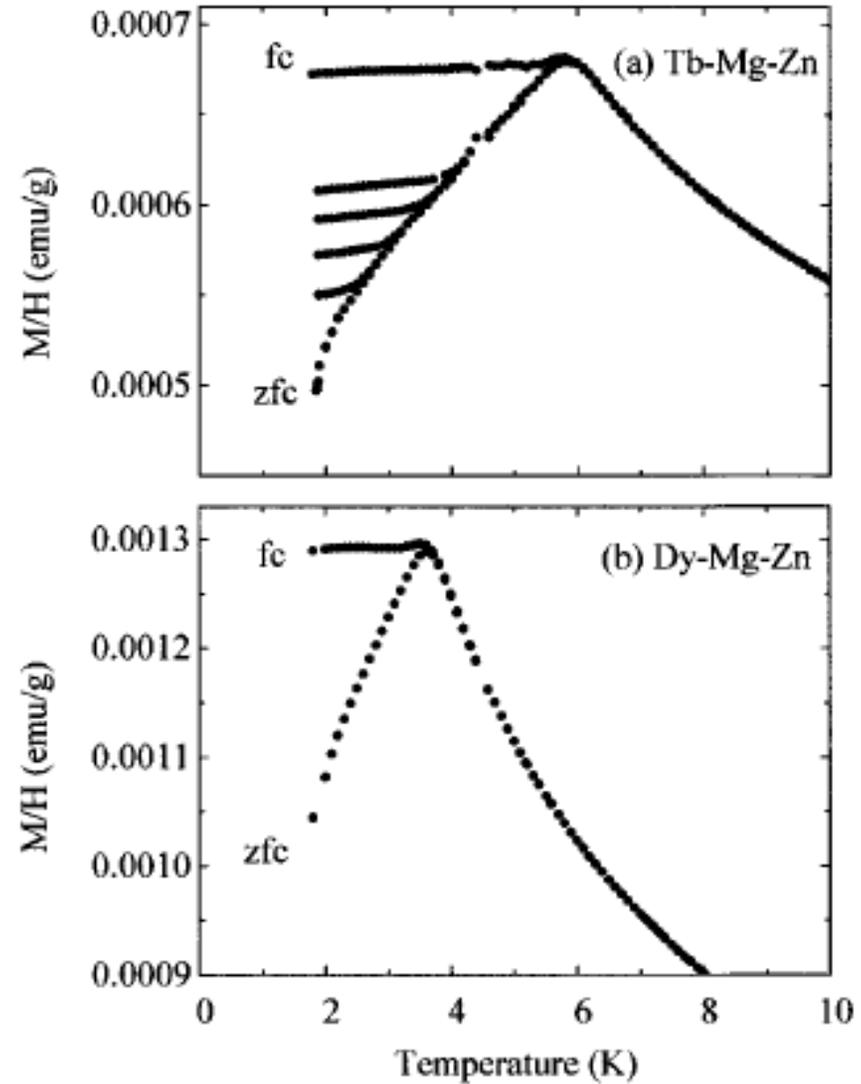
# Spinglass part II: R-Mg-Zn

No long-range order, but instead an ideal spin-glass system

Icosahedral quasicrystal

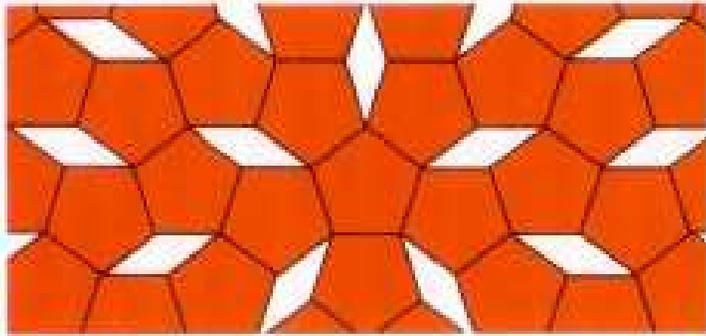


$R_xMg_{60-3x}Zn_{40-2x}$  line



We were able to grow for R = Y, Gd – Er... **MODEL SYSTEM**

Fisher et al., PRB 59 (1999) 308, and Canfield and Fisher, J. Alloys and Comp. 317 (2001) 443



Two-dimensional crystal lattices cannot possess five-fold symmetry points because it is not possible to fill a plane completely with a network of regular pentagons (left).

**M. C. Escher gives a tip of the pen to this in his famous work: reptiles. Whereas you cannot have a tessellation of pentagons, you can form a Platonic solid: the pentagonal dodecahedron. This is what the lizard is rising out of the page and blowing smoke on....**

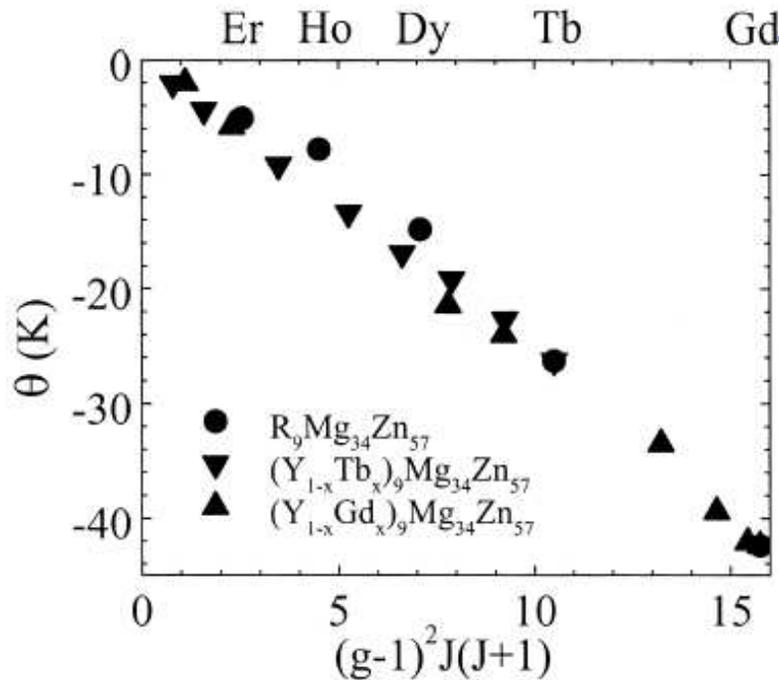
**Keep your eye on the dodecahedron....**





Research Science: Yesterday's impossible is today's commonplace





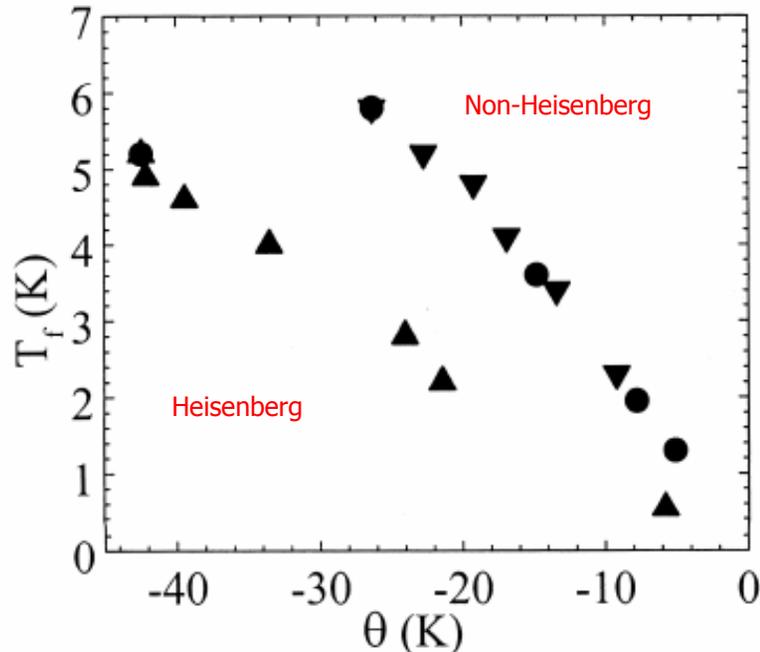
**Model system:** *is there a difference between a Heisenberg and non-Heisenberg spinglass?*

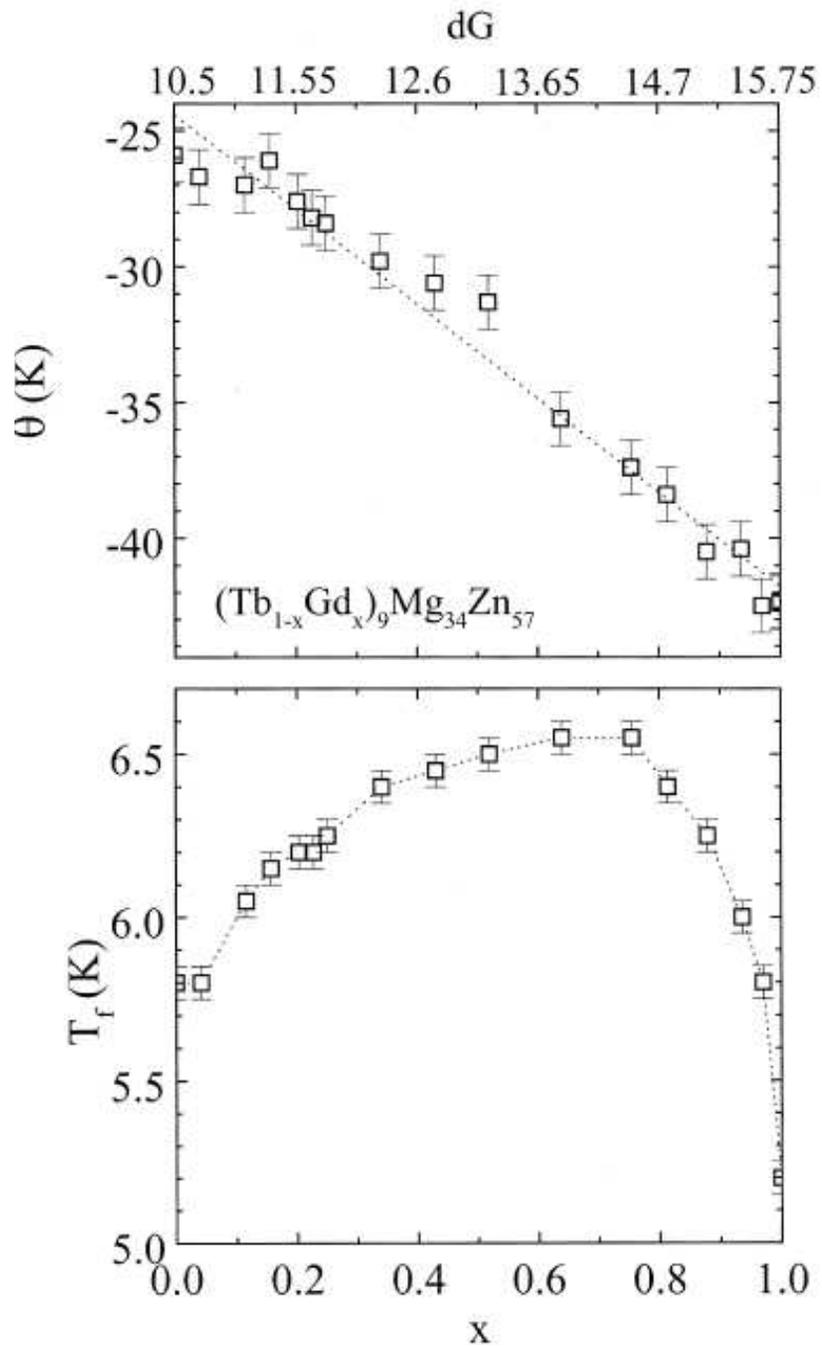
A floor covered with marbles is slippery.

If each marble is non-spherical, then the floor will be less slippery and more inclined to seize up.

A spin glass comprised of spherically symmetric moments (Gd) freezes at a lower temperature than a spin glass comprised of non-spherically symmetric moments (due to crystalline electric field splitting).

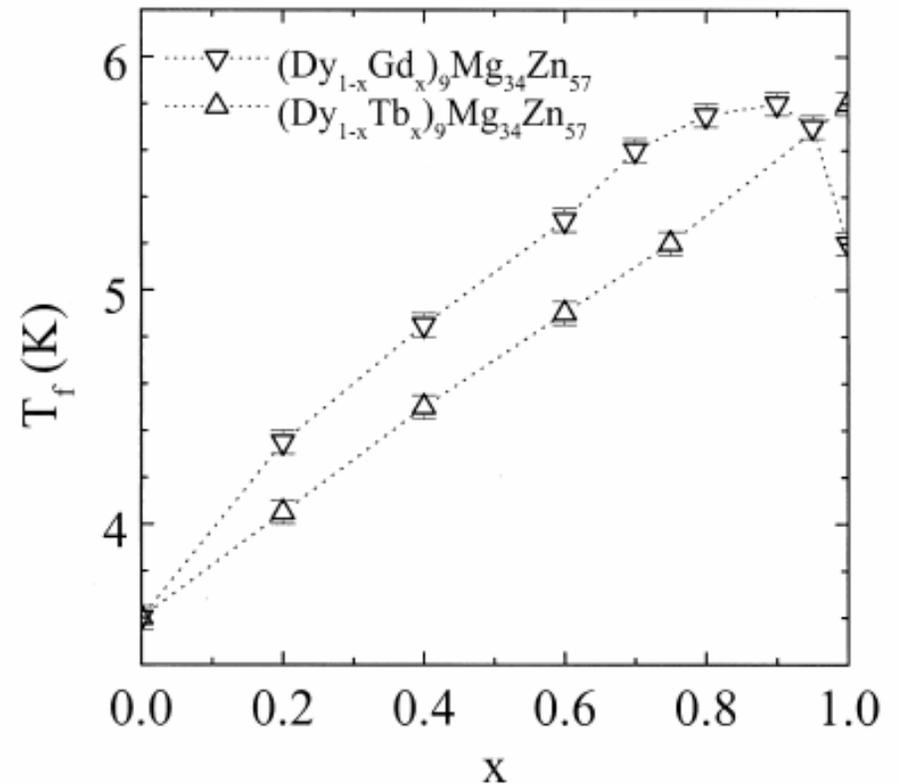
What happens if we titrate spherical moments into non-spherical moments?





As we titrate Gd into either TbMgZn or DyMgZn we see that initially  $T_f$  increases as the interaction strength increases, but beyond  $\sim 80\%$  Gd  $T_f$  drops (beyond  $\sim 80\%$  spheres the floor gets slippery).

This is not a disorder effect, see Dy-Tb series

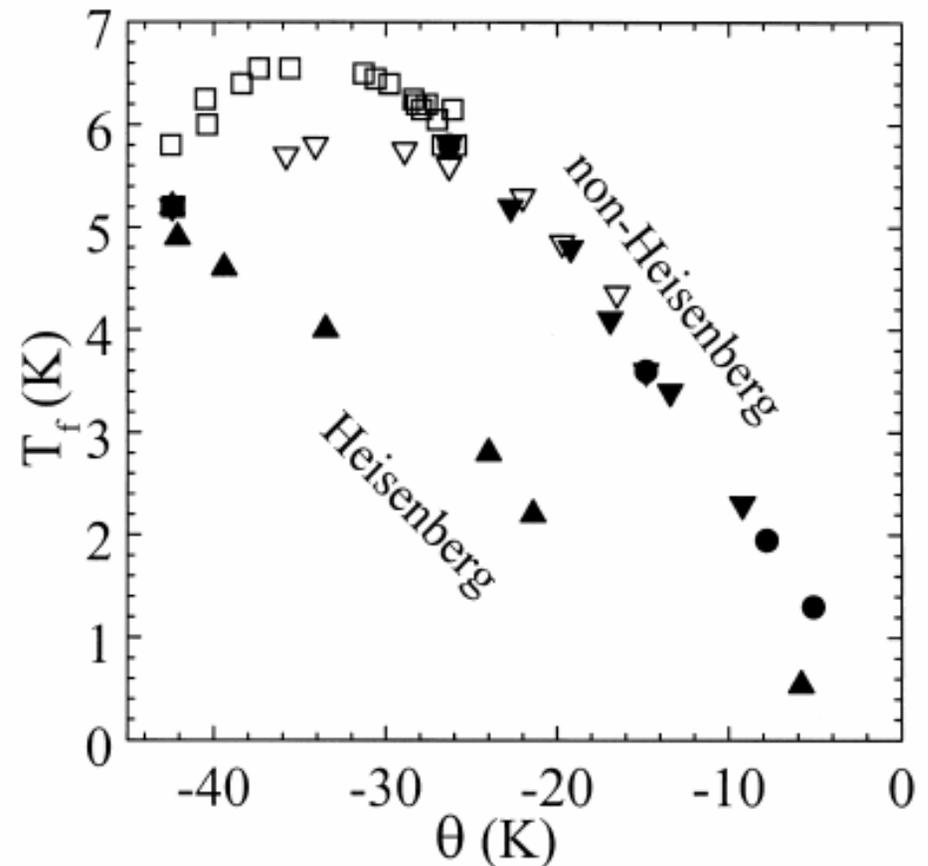




# $R_9Mg_{34}Zn_{57}$ $R = Y, Gd - Er$ Quasicrystals

For RMgZn Icosahedral quasicrystals we went from “want specific material” to “use as a model system” to examine effects of Heisenberg and non-Heisenberg moments on spin glass state manifested in an aperiodic, but highly ordered, system.

For me the RMgZn quasicrystals allowed me to replace the word, “random” with the word “aperiodic” when thinking of the spin-glass state.



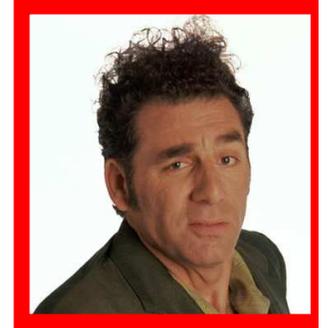


## *A final note on CEF splitting: Kramer's Ions*

There is another systematic variation across the rare earth series, show in color below.

Ce Pr Nd Pm Sm Eu Gd Tb Dy Ho Er Tm Yb

For Kramer's ions (Ce, Nd, Sm, Gd, Dy, Er, Yb) there is a minimum degeneracy of 2 for the  $H = 0$  CEF ground state. This means that there will be a guaranteed local moment at low temperatures and, at least,  $R \ln 2$  worth of entropy that has to be removed at low temperature.

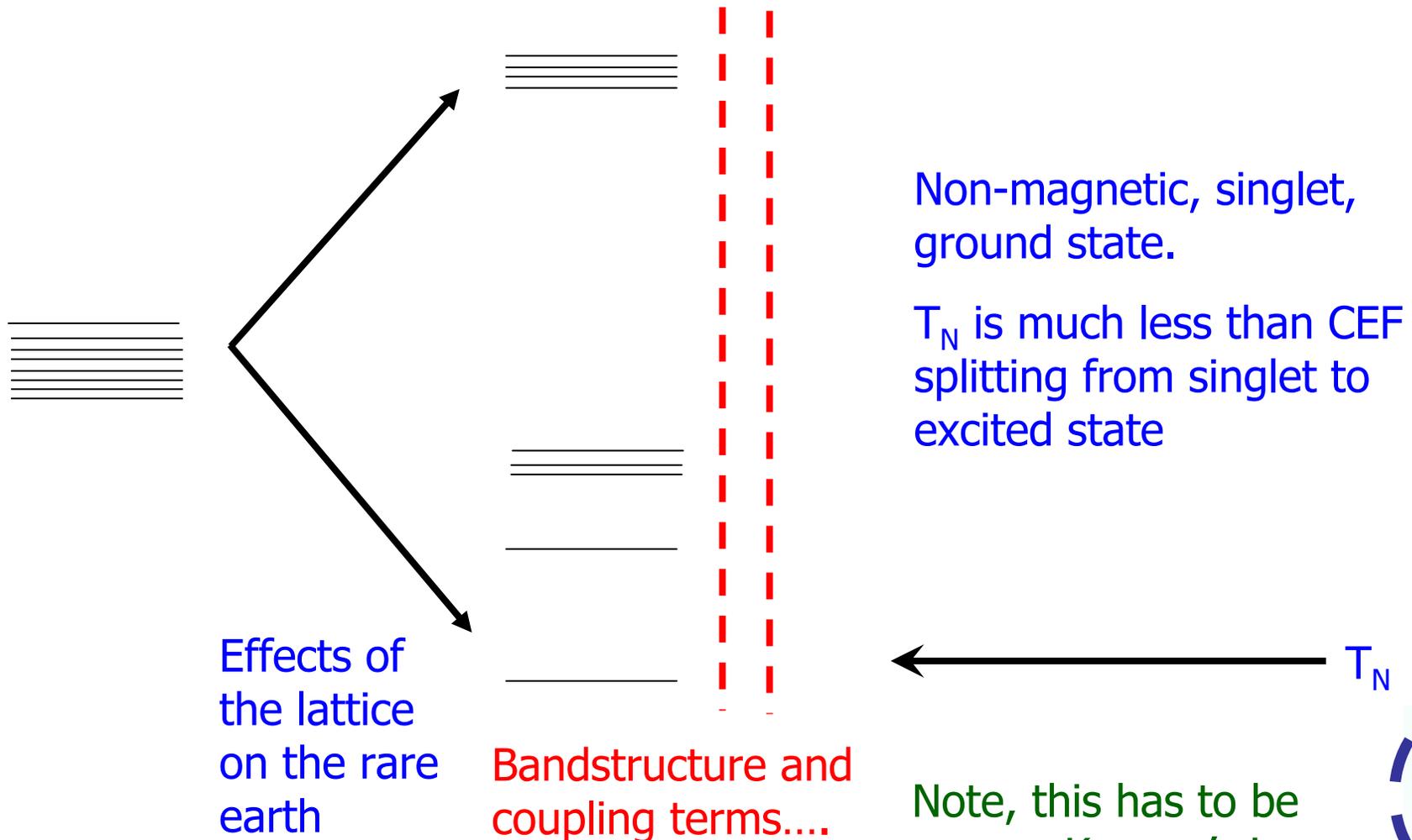


For non-Kramer's ions (Pr, Pm, Eu, Tb, Ho, Tm) there can be CEF singlet ground states. If there is a singlet there no local moment magnetization, since there is no Zeeman splitting and there is  $R \ln 1$  (i.e. zero) entropy to remove.....



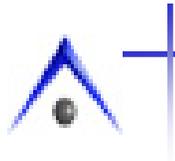


When the CEF split ground state is a singlet, the compound loses its local moment nature and instead manifests a van Vleck paramagnetism associated with the splitting to the first excited state.



Note, this has to be an non-Kramer's ion

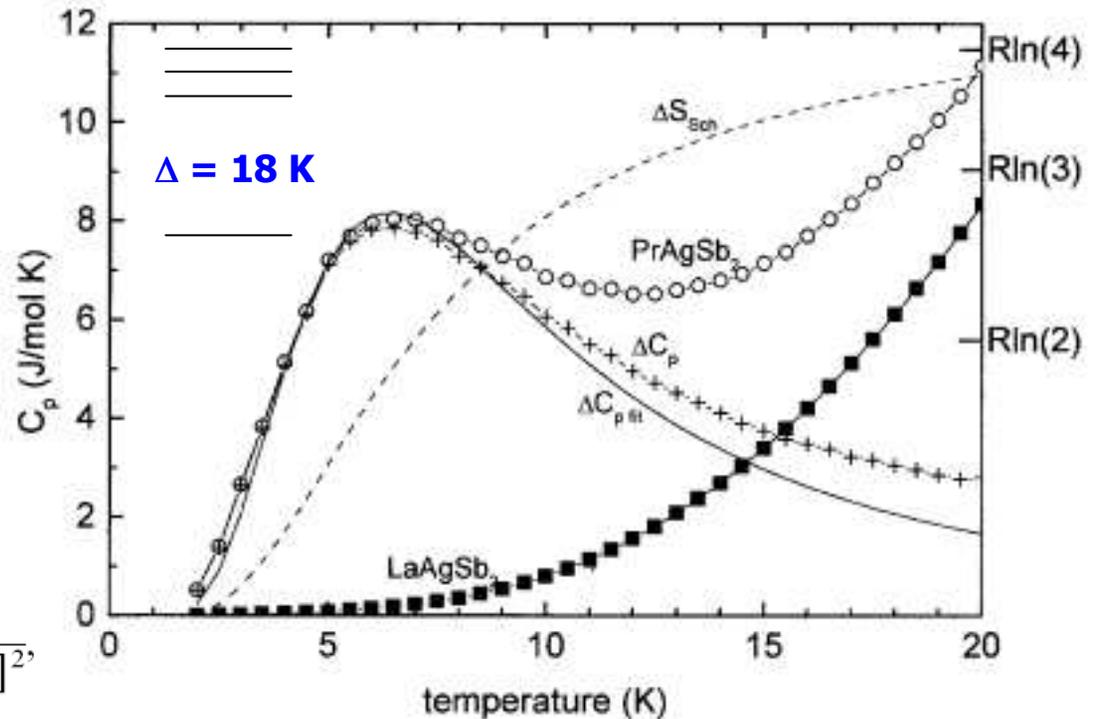
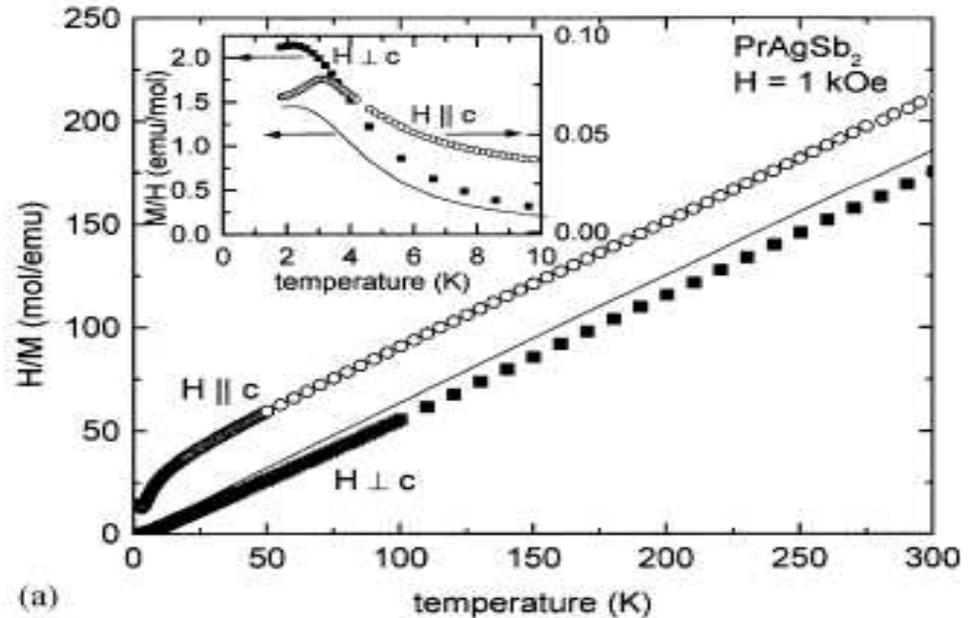




An experimental manifestation of this is  $\text{PrAgSb}_2$ , which instead of ordering at low temperatures, drops into a non-magnetic state associated with a singlet CEF split groundstate.

This can be seen in the  $C_p$  as a Schottky anomaly. This is clearly shown at the right in  $\text{PrAgSb}_2$ . This is modeled as a two level system.

$$C_{\text{Sch}} = R \left( \frac{\Delta}{T} \right)^2 \frac{g_0}{g_1} \frac{\exp(\Delta/T)}{[1 + (g_0/g_1) \exp(\Delta/T)]^2}$$





By using the rare earths, the physicist can tune the:

Size of the unit cell,

Size of the local moment and degree of coupling,

Size and direction of anisotropy,

Amount of entropy that can be removed at low temperatures,

Band filling,

Degree of hybridization.

In terms of temperature and energy scales (another obsession of the physicist), the rare earths can be used to tune:

The magnetic ordering temperature  $T_C$  or  $T_N$

The CEF splitting or  $T_{\Delta_{\text{CEF}}}$

The Kondo temperature  $T_K$

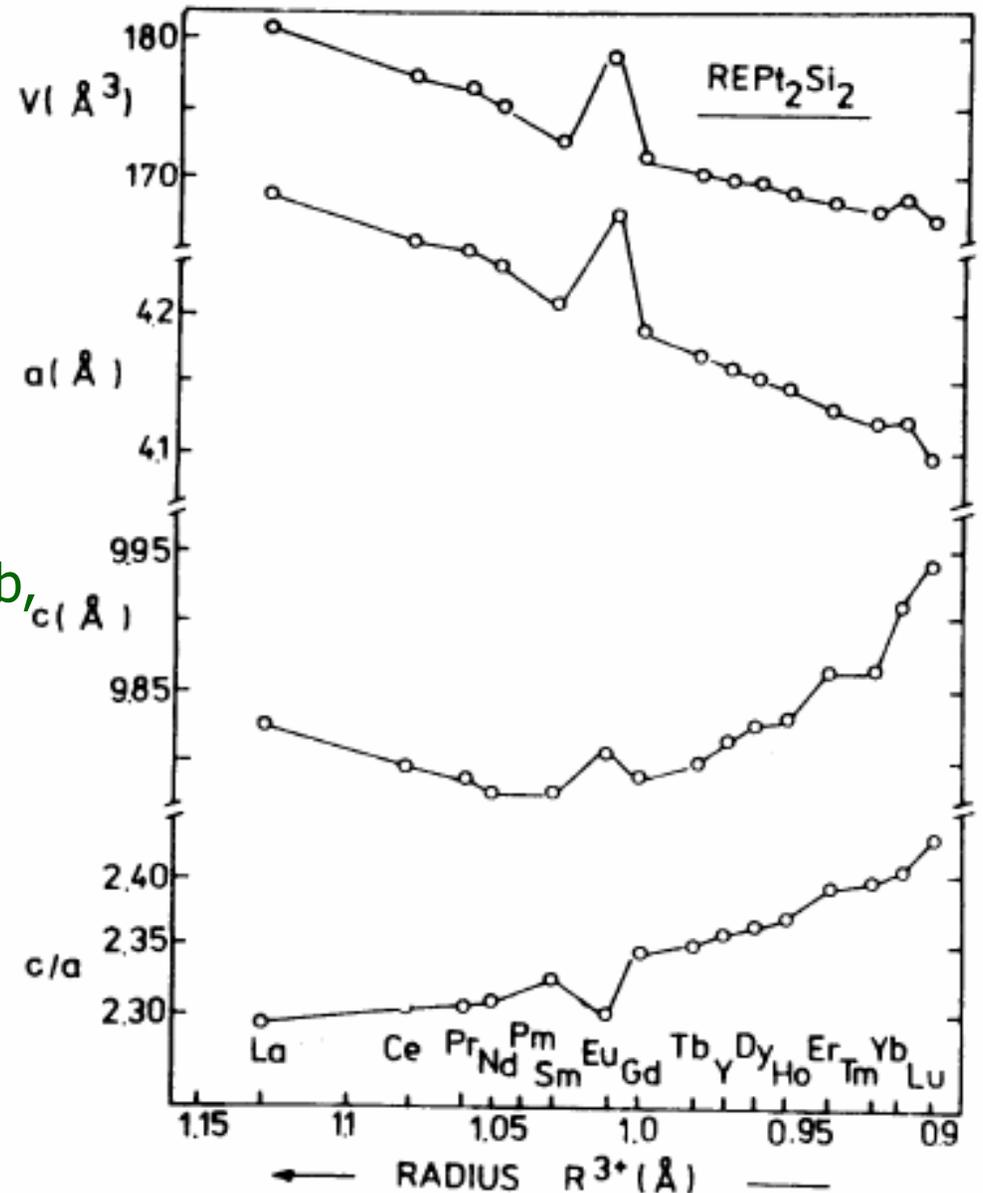


In the most extreme cases  $\text{Ce}^{4+}$ ,  $\text{Eu}^{2+}$  and  $\text{Yb}^{2+}$  can be stabilized.

The empty ( $\text{Ce}^{4+}$ ) and fully filled ( $\text{Yb}^{2+}$ ) as well as exactly  $\frac{1}{2}$  filled ( $\text{Eu}^{2+}$ ) 4f-shell can be more stable, leading to these deviations from the standard  $\text{R}^{3+}$  state.

This leads to non-magnetic Ce and Yb,

and Eu goes from non-magnetic to being the same as  $\text{Gd}^{3+}$ , but with different band filling.

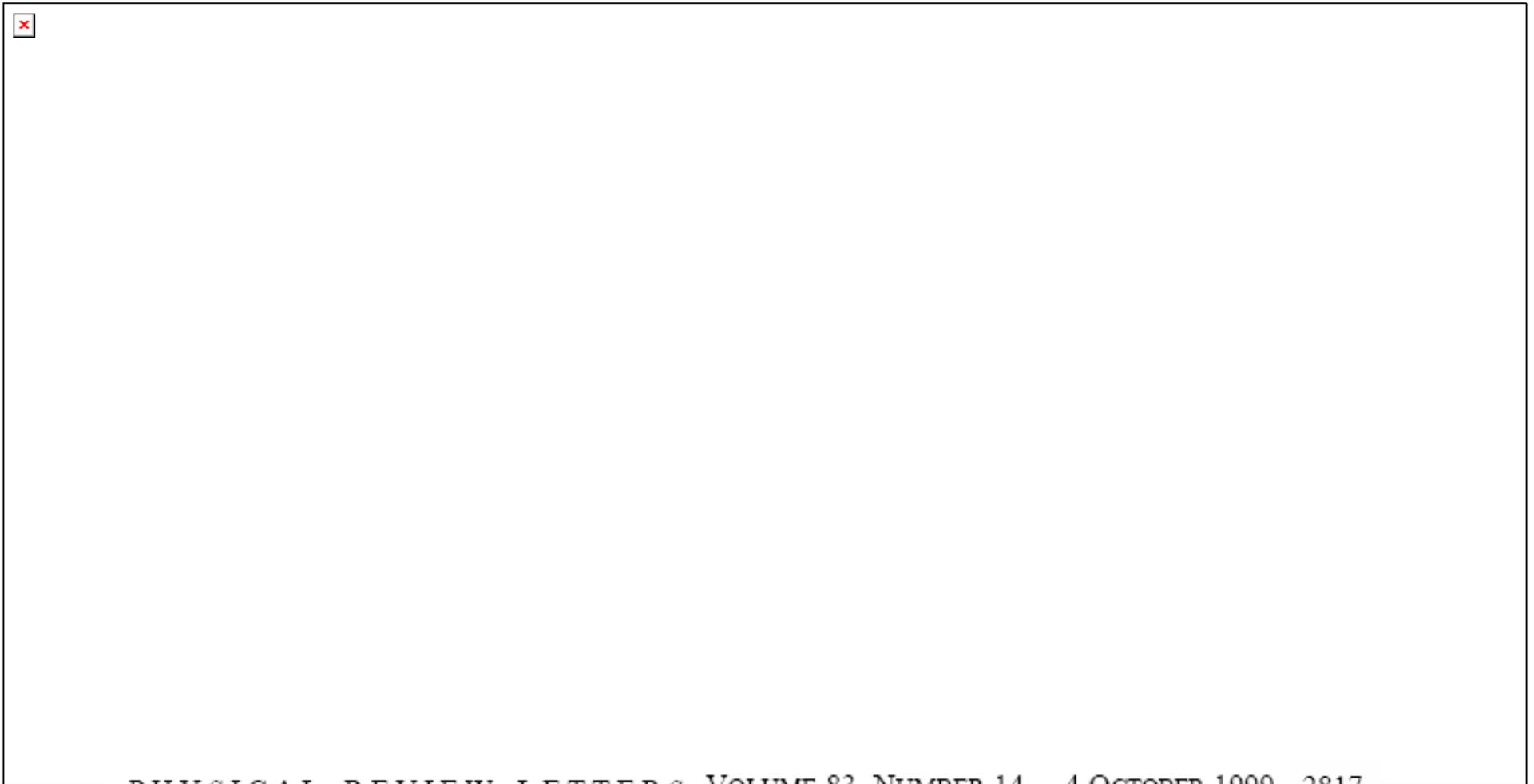


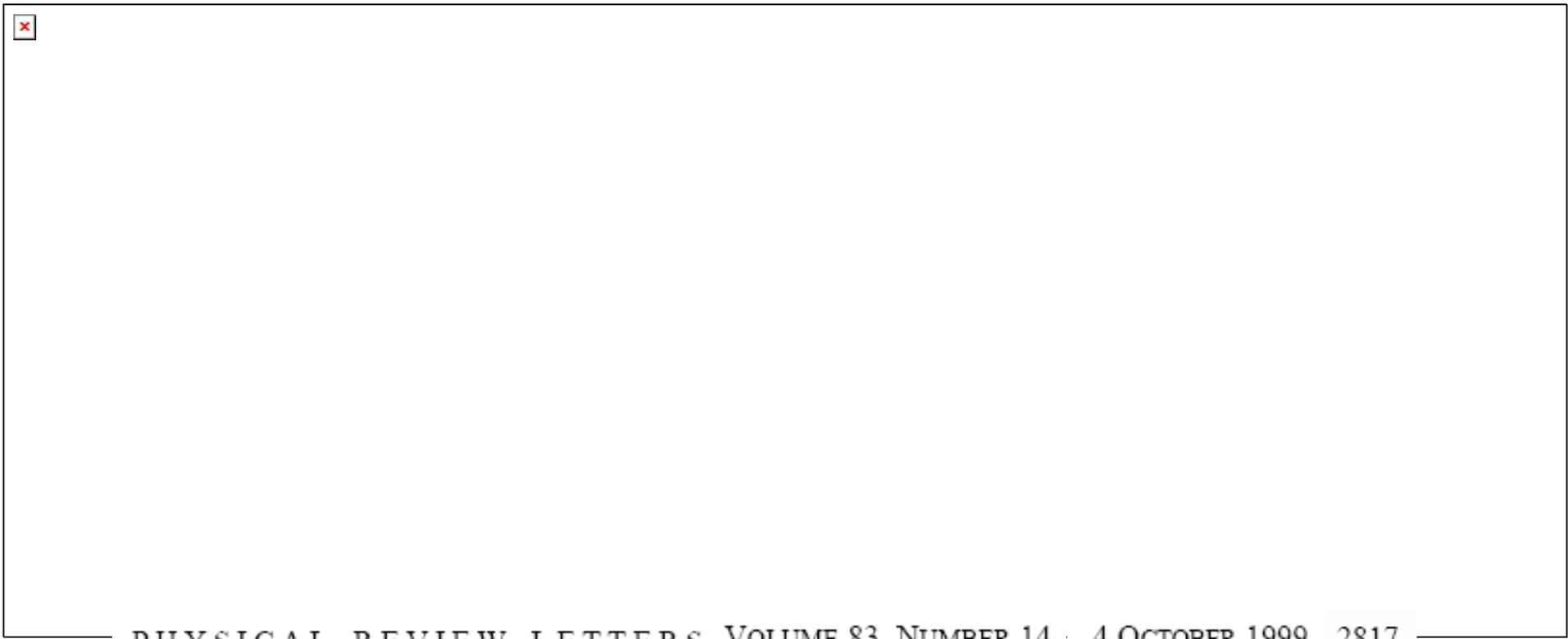
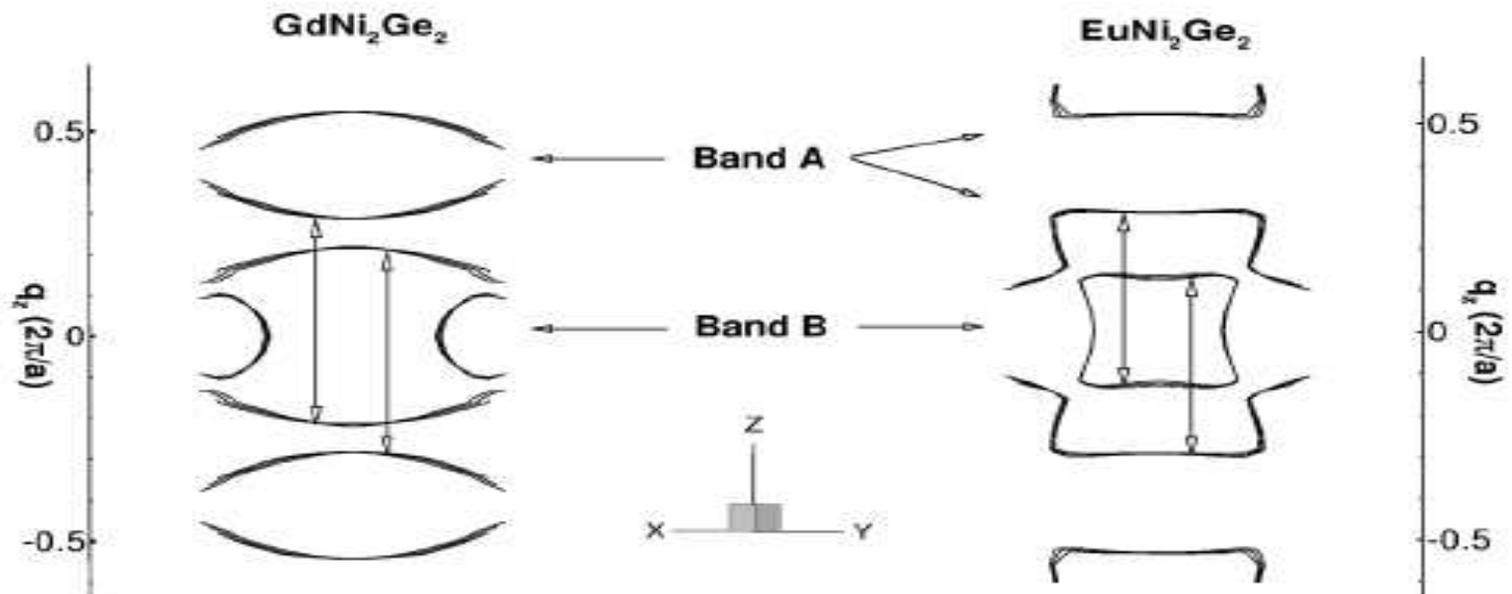
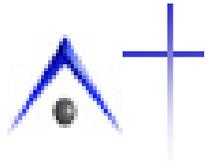


The effects of band filling on magnetism can be probed with  $\text{Gd}^{3+}$  and  $\text{Eu}^{2+}$  isostructural materials

$$q = (0 \ 0 \ 0.793 - 0.805)$$

$$q = (0 \ 0 \ 1)$$

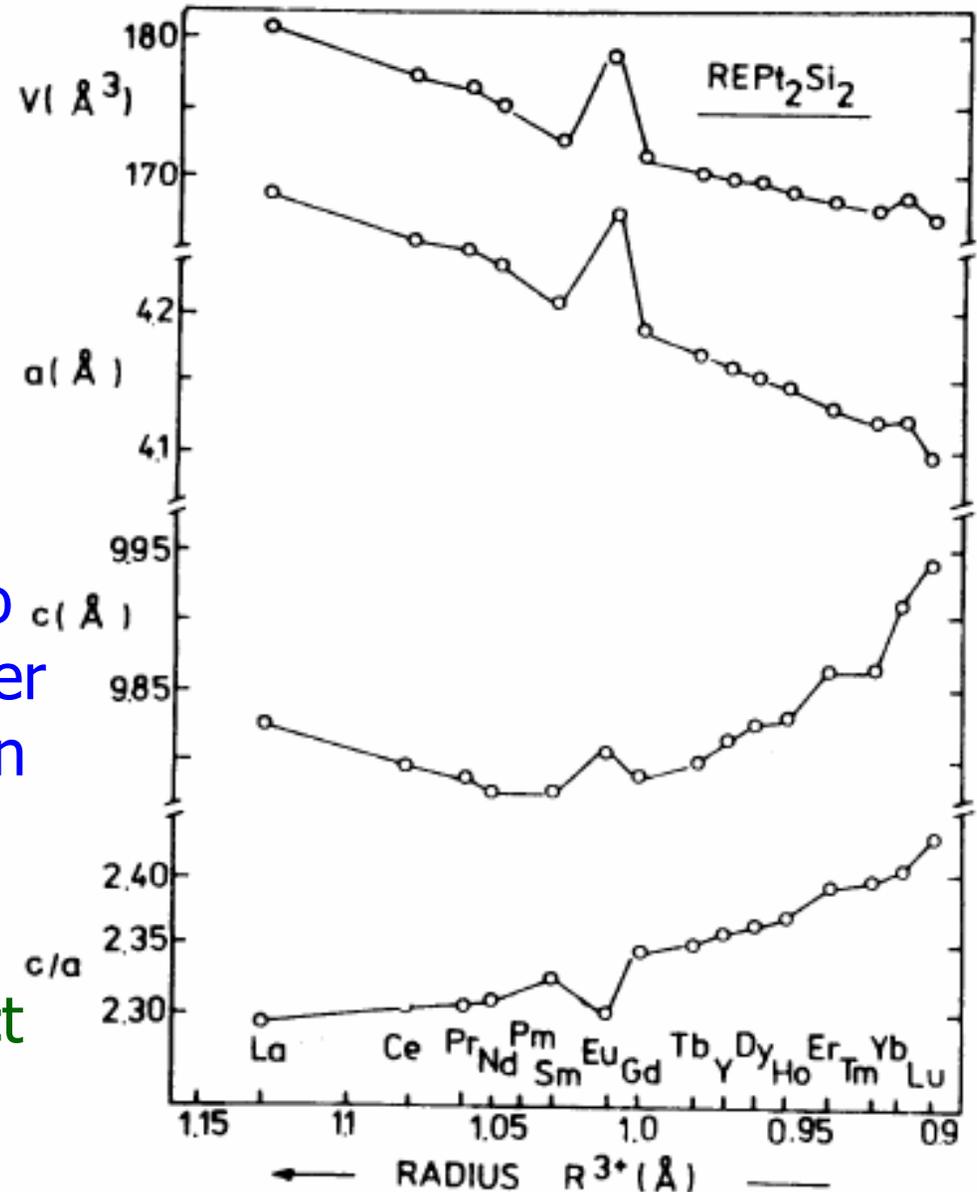





 In only the most extreme cases  $\text{Ce}^{4+}$ ,  $\text{Eu}^{2+}$  and  $\text{Yb}^{2+}$  can be stabilized.

But even when, Ce and Yb appear to be essentially  $3^+$  at room temperature, at low temperature, below a characteristic temperature,  $T_K$ , they can hybridize with the conduction band. This leads to a loss of local moment character and strongly correlated electron effects.

This more subtle interaction is at the heart of the Kondo effect and heavy fermions.





## Hybridization, heavy fermions, and entropy

Ce Pr Nd Pm Sm Eu Gd Tb Dy Ho Er Tm Yb

For Kramer's ions (Ce, Nd, Sm, Gd, Dy, Er, Yb) there is a minimum degeneracy of 2 for the  $H = 0$  CEF ground state. This means that there will be at least  $R\ln 2$  worth of entropy that has to be removed by (i) magnetic ordering or **(ii) some other, more exotic, mechanism.**



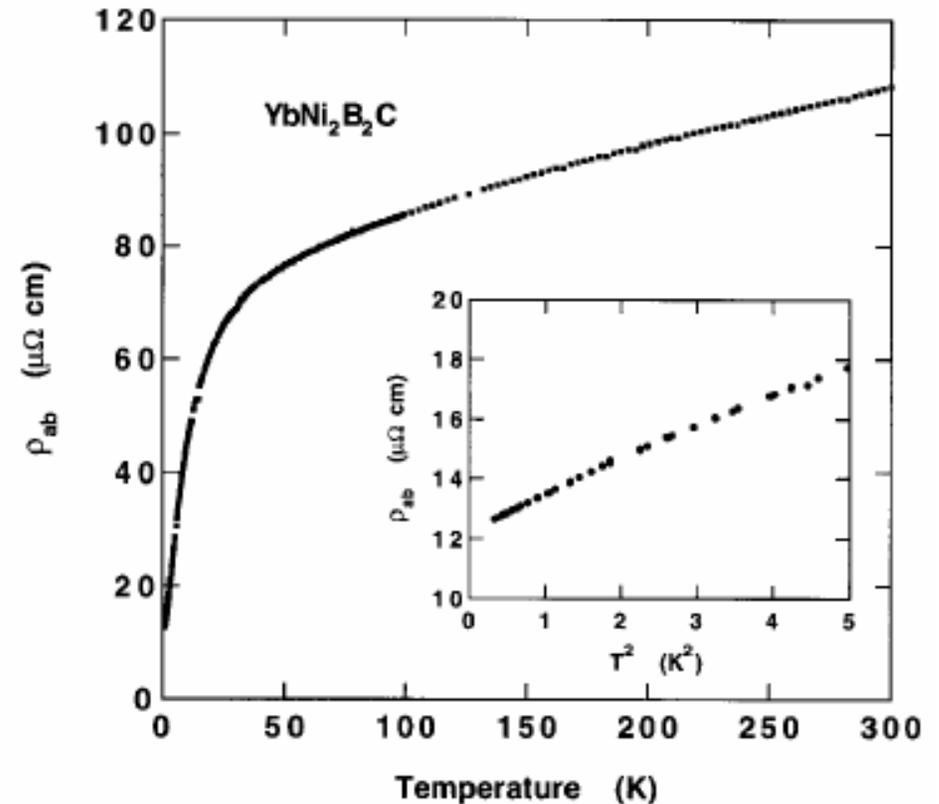
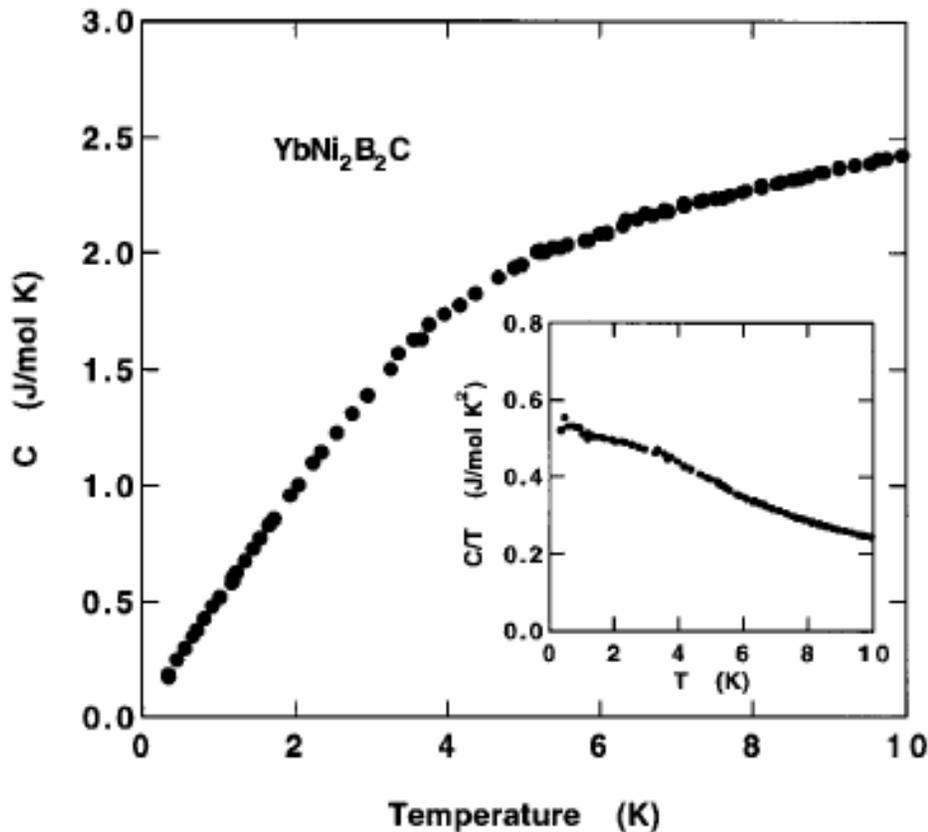
One such mechanism for  $R = \text{Ce, Sm, Yb}$  is to allow hybridization between the 4f electrons and the conduction electrons below a characteristic  $T_K$ . This leads to Kondo lattices...heavy fermions.

$\gamma T_K \sim R\ln 2$  for a CEF doublet groundstate

*$\gamma$  is proportional to the electron mass. Large  $\gamma$  implies large  $m$ ,  $\therefore$  heavy fermion.*

Whereas this ground state has been extensively studied in Ce-based compounds, until recently there has been a dearth of Yb-based examples.

# YbNi<sub>2</sub>B<sub>2</sub>C – The rare, model Yb-based heavy fermion



$$\gamma = 530 \text{ mJ/mol K}^2$$

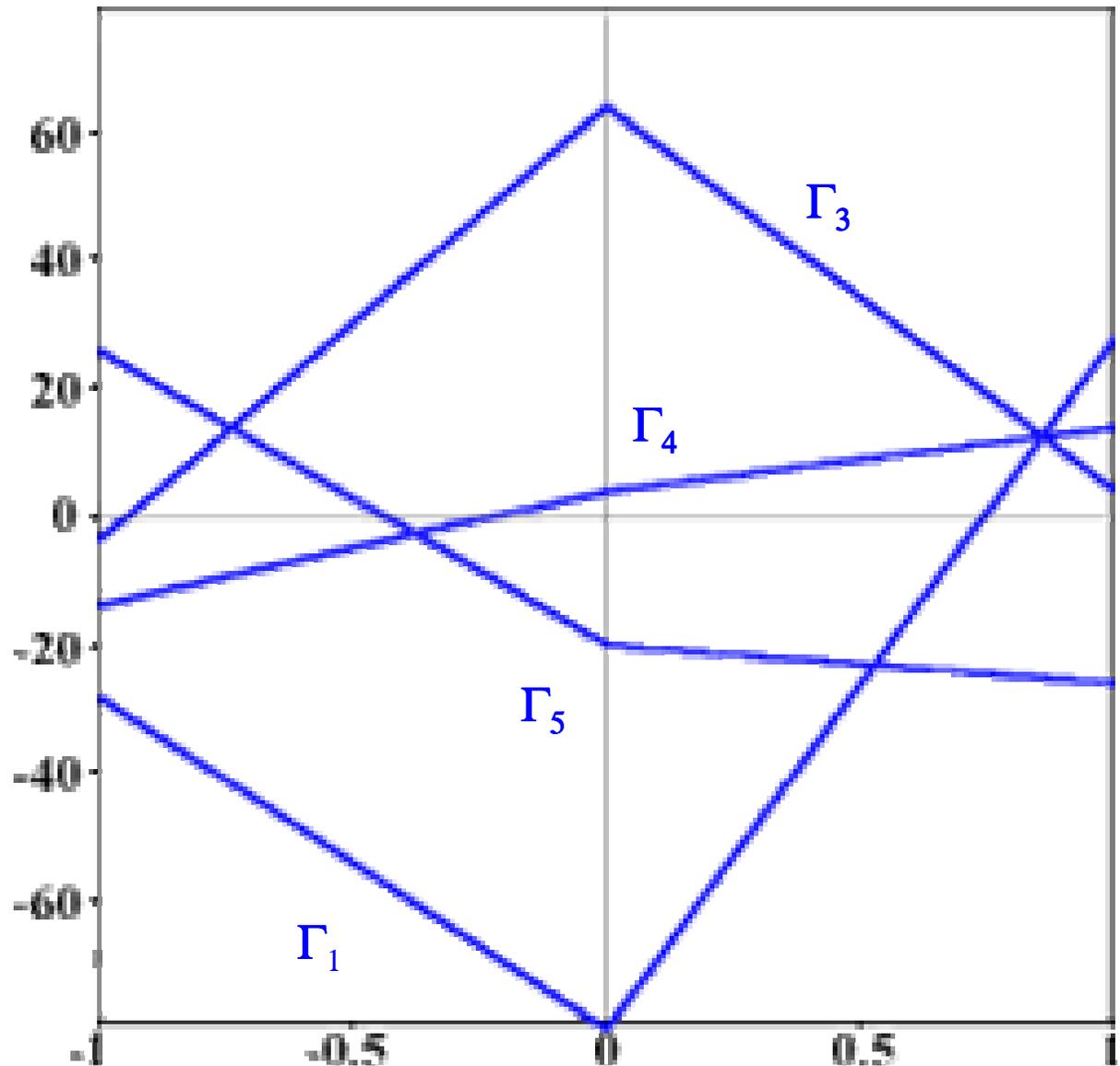
$$T_N, T_C \ll T_K \ll T_{\Delta\text{CEF}}$$

$$0.03 \text{ K} \ll 10 \text{ K} \ll 100 \text{ K}$$

This separation of energy scales makes YbNi<sub>2</sub>B<sub>2</sub>C a model heavy fermion system!

**What about non-Kramers ions: Can entropy be preserved in Pr-based samples to low enough temperatures to allow for hybridization? i.e. can a Pr-based sample go heavy?**

**Cubic point symmetry can help preserve entropy of this non-Kramer's ion. (The  $\Gamma_3$  state is a non-magnetic doublet and can, sometimes, be the ground state)**



**Lea, Leask, Wolf splitting for  $\text{Pr}^{3+}$**

K. R. Lea, M. J. M. Leask, and W. P. Wolf, J. Phys. Chem. Solids 23, 1381 (1962).



Make a list of cubic compounds with a single RE in cubic point symmetry, refine list, make compounds, hunt physics.

466

Structure Type Index

**cF12**

AcH<sub>3</sub> (A)  
Al<sub>2</sub>Au (B)  
AlNi<sub>3</sub>Si<sub>2</sub> (B)  
Al<sub>2</sub>Pt (A) (B)  
As<sub>2</sub>GeLi<sub>3</sub>  
As<sub>2</sub>Li<sub>3</sub>Ti  
AsNaZn  
AsRh<sub>2</sub> (A)  
AuGa<sub>2</sub>  
AuIn<sub>2</sub> (A)  
BiO<sub>2</sub> (B)  
CaF<sub>2</sub>  
CdLiSb  
ClO<sub>2</sub>  
CoMnSb  
Cu<sub>2</sub>Se (B)  
ErH<sub>2</sub> (A)  
Fe<sub>3</sub>Ni<sub>2</sub>Si<sub>10</sub> (B)  
GdH<sub>4</sub>Y (A) (B)  
GeMg<sub>2</sub>  
H<sub>2</sub>La (B) (A)  
H<sub>2</sub>Nb  
H<sub>2</sub>Np (B) (A)  
H<sub>2</sub>Sc  
H<sub>4</sub>TaV (B)  
H<sub>4</sub>TiV (B)  
H<sub>2</sub>Y (A)  
HfO<sub>2</sub>  
IrMnSb  
K<sub>2</sub>S  
LiMgN  
Li<sub>2</sub>O  
Li<sub>2</sub>P<sub>3</sub>Ti  
Li<sub>2</sub>S  
Mg<sub>2</sub>Pb  
Mg<sub>2</sub>Si (A)  
Mg<sub>2</sub>Sn  
Na<sub>2</sub>S  
NiSi<sub>2</sub> (A)  
O<sub>2</sub>Pb  
O<sub>2</sub>Pu  
O<sub>2</sub>Tb (A)  
O<sub>2</sub>U  
PRh<sub>2</sub>  
Rh<sub>2</sub>Se

AgAsZn  
Al<sub>7</sub>Cu<sub>4</sub>Li  
Al<sub>2</sub>Pd (A)  
AmH<sub>2</sub> (B)  
As<sub>2</sub>Li<sub>7</sub>Mn  
As<sub>4</sub>Li<sub>7</sub>V  
As<sub>2</sub>P<sub>3</sub>Rh<sub>10</sub> (B)  
As<sub>2</sub>CdIn<sub>2</sub>Sn (B)  
Au<sub>17</sub>Ge<sub>30</sub>Pd<sub>3</sub> (B)  
BBi<sub>2</sub> (A)  
BkH<sub>2</sub>  
CdLi<sub>2</sub>MgP<sub>2</sub> (B)  
CeH<sub>2</sub> (B) (A)  
CmH<sub>2</sub> (A)  
CoNiSi<sub>4</sub> (B)  
DyH<sub>2</sub> (A)  
ErH<sub>20</sub>Y<sub>3</sub> (A) (B)  
G<sub>2</sub>Pt  
Gd<sub>2</sub>O<sub>3</sub>  
H<sub>2</sub>Hf  
H<sub>2</sub>Lu (A)  
H<sub>4</sub>NbV (B)  
H<sub>2</sub>Pr (B)  
H<sub>2</sub>Sm (B)  
H<sub>2</sub>Tb  
H<sub>2</sub>Tm (A)  
H<sub>2</sub>Yb (A)  
Hc<sub>2</sub>O<sub>3</sub>  
Ir<sub>2</sub>P  
K<sub>2</sub>Se  
LiMgP  
Li<sub>2</sub>P<sub>2</sub>Si  
Li<sub>7</sub>P<sub>4</sub>V  
Li<sub>2</sub>Se (B)  
Mg<sub>2</sub>Sb<sub>2</sub>Si<sub>2</sub> (B)  
Mg<sub>7</sub>Si<sub>2</sub>Sn (B)  
MnPtSn  
Na<sub>2</sub>Se  
NpO<sub>2</sub> (A)  
O<sub>2</sub>Po  
ORb<sub>2</sub> (A)  
O<sub>2</sub>Tb<sub>2</sub>  
O<sub>2</sub>U  
PtSi<sub>2</sub>

Structure Type  
CaF<sub>2</sub>  
Space Group  
Fm $\bar{3}$ m  
No.  
225

AgCuTe  
AlIrMn  
Al<sub>12</sub>Pd<sub>4</sub>Si<sub>3</sub> (B)  
AmO<sub>2</sub>  
As<sub>2</sub>Li<sub>2</sub>Si  
AsLiZn  
As<sub>4</sub>PRh<sub>10</sub> (B)  
AuCdSn  
Au<sub>10</sub>Ge<sub>48</sub>Pd (B)  
Be<sub>2</sub>C  
BkO<sub>2</sub>  
CdLi<sub>2</sub>P<sub>2</sub>Zn (B)  
CeO<sub>2</sub> (B)  
CmO<sub>2</sub> (B)  
CoSi<sub>2</sub>  
Dy<sub>2</sub>O<sub>3</sub>  
Er<sub>2</sub>O<sub>3</sub>  
GdH<sub>2</sub> (A)  
GeLi<sub>3</sub>P<sub>3</sub>  
H<sub>2</sub>Ho  
H<sub>2</sub>Mg<sub>2</sub>Ni (F)  
H<sub>2</sub>Nd (B) (A)  
H<sub>2</sub>Pu (B)  
H<sub>2</sub>Ta  
H<sub>2</sub>Ti (A) (B)  
H<sub>2</sub>V (A) (B)  
H<sub>2</sub>Zr (A) (B)  
In<sub>2</sub>Pt  
K<sub>2</sub>O  
K<sub>2</sub>Te  
Li<sub>7</sub>MnP<sub>4</sub>  
Li<sub>2</sub>P<sub>2</sub>Sn  
LiPZn  
Li<sub>2</sub>Te  
Mg<sub>2</sub>Sb<sub>2</sub>Sn (B)  
Mg<sub>7</sub>Si<sub>2</sub>Sn (B)  
N<sub>2</sub>U (A)  
Na<sub>2</sub>Te (A)  
O<sub>2</sub>Pa  
O<sub>2</sub>Pr (B)  
O<sub>2</sub>Sm<sub>2</sub> (A)  
O<sub>2</sub>Th  
O<sub>2</sub>Zr (A)  
Rb<sub>2</sub>S

Structure Type  
BiF<sub>3</sub>  
Space Group  
Fm $\bar{3}$ m  
No.  
225

AgAuCd<sub>2</sub>  
Ag<sub>2</sub>CdMg (B)  
Ag<sub>2</sub>CeIn  
Ag<sub>12</sub>GeMg<sub>2</sub> (B)

AgAuZn<sub>2</sub> (B)  
Ag<sub>2</sub>CeIn (B)  
Ag<sub>2</sub>DyIn  
Ag<sub>2</sub>GdIn

AgCdMg<sub>2</sub> (B)  
Ag<sub>2</sub>InMg<sub>4</sub> (B)  
Ag<sub>2</sub>InPr  
Ag<sub>2</sub>InTb  
Ag<sub>2</sub>LaMg (B)  
Ag<sub>2</sub>LiSn  
AgMg<sub>2</sub>Sm (B)  
AlAu<sub>2</sub>Hf  
AlAu<sub>2</sub>Ti  
AlCo<sub>2</sub>Fe  
AlCo<sub>2</sub>Nb  
AlCo<sub>2</sub>V  
AlCrFe<sub>2</sub>  
AlCo<sub>2</sub>Mn  
AlCo<sub>2</sub>Sc  
AlFe<sub>2</sub>

Ag<sub>2</sub>Holn  
Ag<sub>2</sub>In<sub>2</sub>Mn<sub>2</sub>Pd<sub>2</sub> (B)  
Ag<sub>2</sub>InSc  
Ag<sub>2</sub>InTm  
AgLi<sub>2</sub>Mg  
AgMg<sub>2</sub>Nd (B)  
AgMg<sub>2</sub>Tb<sub>2</sub> (B)  
AlAu<sub>2</sub>Mn  
AlBiPd<sub>2</sub> (A)  
AlCo<sub>2</sub>Hf  
AlCo<sub>2</sub>Ta  
AlCo<sub>2</sub>Zr (B)  
AlCrNi<sub>2</sub>  
Al<sub>2</sub>Co<sub>4</sub>Mn<sub>2</sub>Pd<sub>4</sub> (B)  
AlCu<sub>2</sub>Ti  
AlFeMn (B)  
AlFeNi  
AlFe<sub>2</sub>V (B)  
AlHfP<sub>2</sub>  
AlMnPd<sub>2</sub>  
AlMnV  
AlNi<sub>2</sub>Ta  
AlNi<sub>2</sub>Zr  
As<sub>2</sub>Bi<sub>2</sub>Pd<sub>12</sub> (A)

Ag<sub>2</sub>InLa  
Ag<sub>2</sub>InNd  
Ag<sub>2</sub>InSm  
Ag<sub>2</sub>InY  
AgLi<sub>2</sub>Sn (A)  
AgMg<sub>2</sub>Pr (B)  
Ag<sub>2</sub>MgZn (B)  
AlAu<sub>2</sub>Sc  
AlCo<sub>2</sub>Cr  
AlCo<sub>2</sub>Mn  
AlCo<sub>2</sub>Ti (B)  
AlCrCu<sub>2</sub>  
AlCu<sub>2</sub>Hf  
Al<sub>17</sub>Cu<sub>40</sub>Mn<sub>20</sub>Sn<sub>2</sub> (B)  
AlCo<sub>2</sub>Zr  
AlFe<sub>2</sub>Mn  
AlFe<sub>2</sub>Si (B)  
AlHfNi<sub>2</sub>  
AlIr<sub>2</sub>Mn  
AlMnPt<sub>2</sub>  
AlNbNi<sub>2</sub>  
AlNi<sub>2</sub>Ti (A) (B)  
AlPd<sub>2</sub>Sc  
As<sub>2</sub>InPd<sub>12</sub> (A)

**cF16**

Structure Type  
DiF<sub>2</sub>  
Space Group  
Fm $\bar{3}$ m  
No.  
225

Au<sub>2</sub>InY  
AuLi<sub>2</sub>  
Au<sub>2</sub>SnU  
BeNi<sub>2</sub>Si  
BiGePd<sub>4</sub> (A)  
BiLi<sub>2</sub>Mg  
BiPd<sub>2</sub>Y  
Ca<sub>3</sub>Ti  
CdGeLi<sub>2</sub> (A)  
CdLi<sub>2</sub>Sn (A)  
CeCuMg<sub>2</sub> (B)  
CeMg<sub>2</sub>  
Co<sub>10</sub>CrMn<sub>4</sub>Si<sub>2</sub>  
CoFe<sub>2</sub>Ga  
Co<sub>2</sub>FeGe  
Co<sub>2</sub>FeSi (B)  
CoGa<sub>2</sub>Mn (B)  
Co<sub>2</sub>GaTa  
Co<sub>2</sub>GeLi  
Co<sub>2</sub>GeTi  
CoMnNiSn (B)  
CoMnSb

AgCdMg<sub>2</sub> (B)  
Ag<sub>2</sub>InMg<sub>4</sub> (B)  
Ag<sub>2</sub>InPr  
Ag<sub>2</sub>InTb  
Ag<sub>2</sub>LaMg (B)  
Ag<sub>2</sub>LiSn

**cF16**

Ag<sub>2</sub>ABc  
AgCd<sub>2</sub>Ce  
Ag<sub>2</sub>CeIn  
Ag<sub>2</sub>ErIn

One of many pages from Pearson's Handbook of crystallographic data....



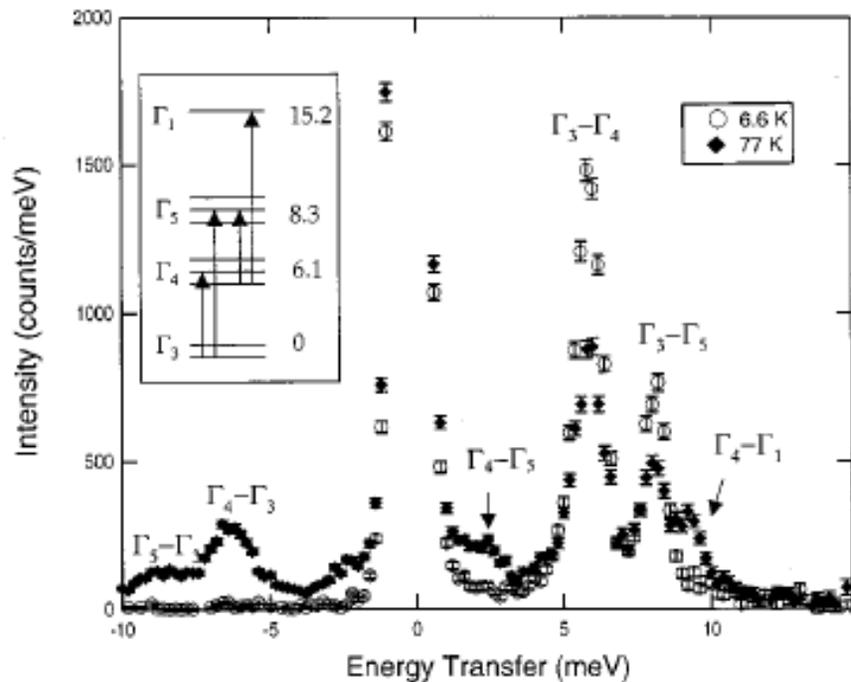
# PrAg<sub>2</sub>In matched the cascade of requirements:

Cubic unit cell

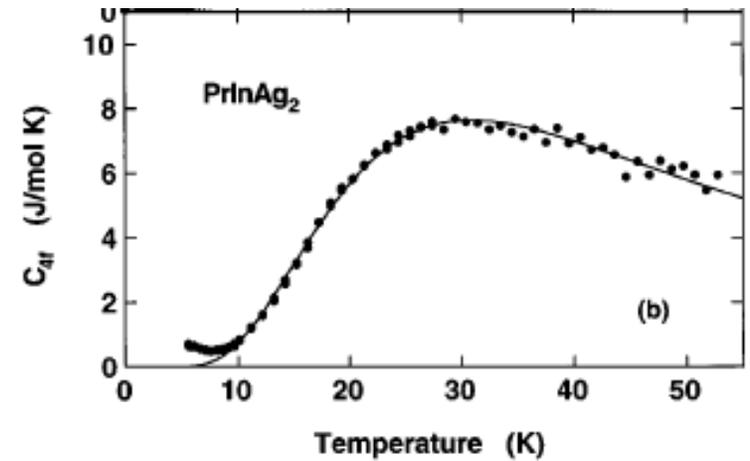
Cubic point symmetry for Pr

$\Gamma_3$  CEF groundstate

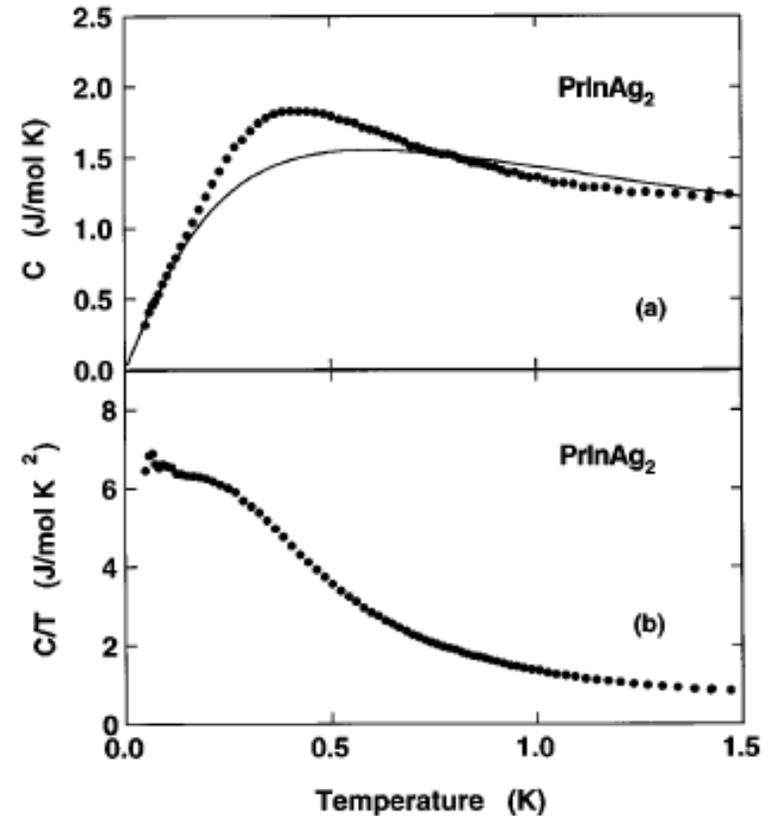
Large  $C/T$  for  $T < 300$  mK



Kelly et al., PRB 61 (2000) 1831



Yatskar et al., PRL 77 (1996) 3637





## **PrAg<sub>2</sub>In**

**Can entropy be preserved in Pr-based samples to low enough temperatures to allow for hybridization?**

**Yes, if done carefully....cubic unit cell, cubic point symmetry.**

**Can a Pr-based sample go heavy?**

**Yes, but it is fundamentally different physics since the heavy fermion ground state is evolving from a non-magnetic CEF level. My pet theory is dynamic screening of Jahn-Teller distortion as mechanism for entropy transfer....**

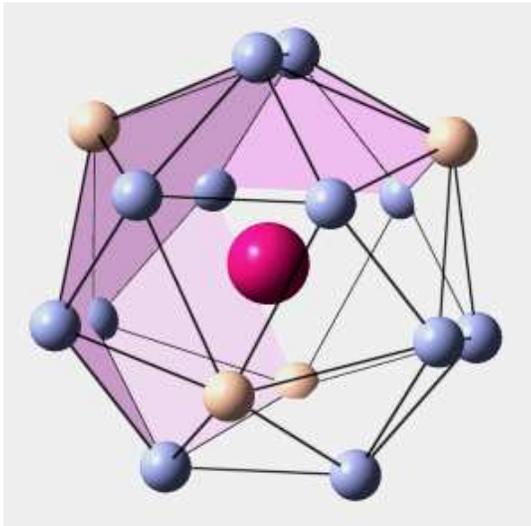
**PrAg<sub>2</sub>In opened the area of Pr-based heavy fermion research and generalized the idea of preservation of entropy as a route to heavy fermion ground states. This system inspired several searches for other examples.**



# Recently this dearth of Yb-based heavy fermions has been ameliorated

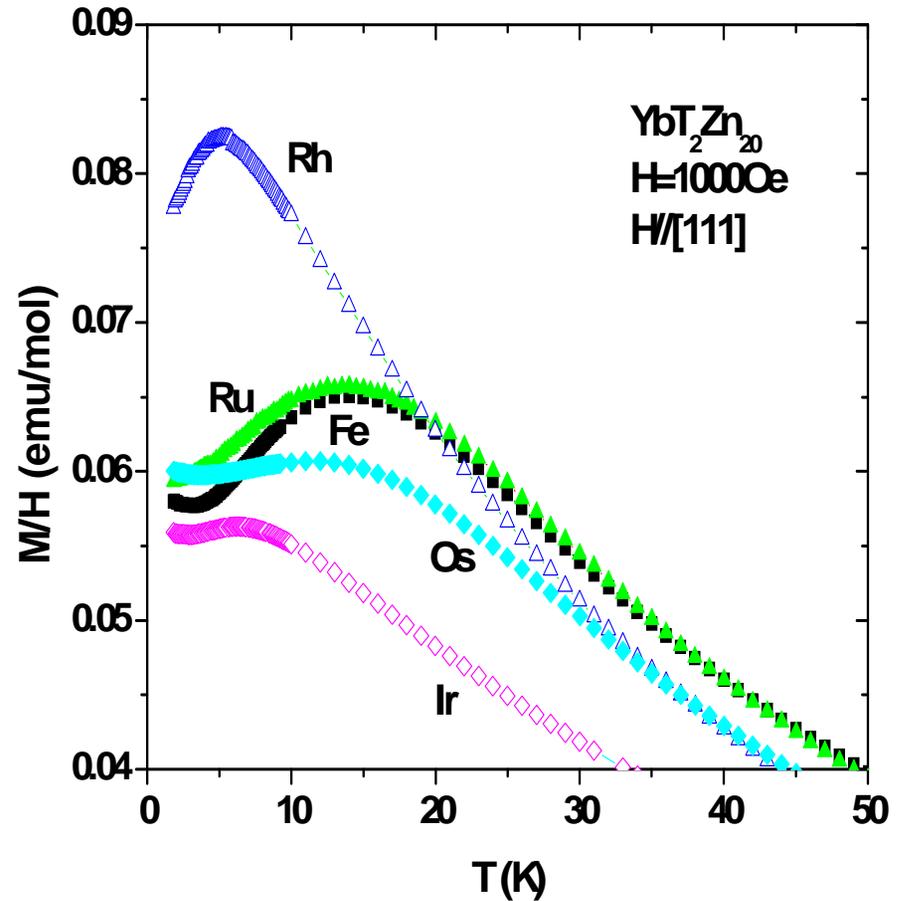
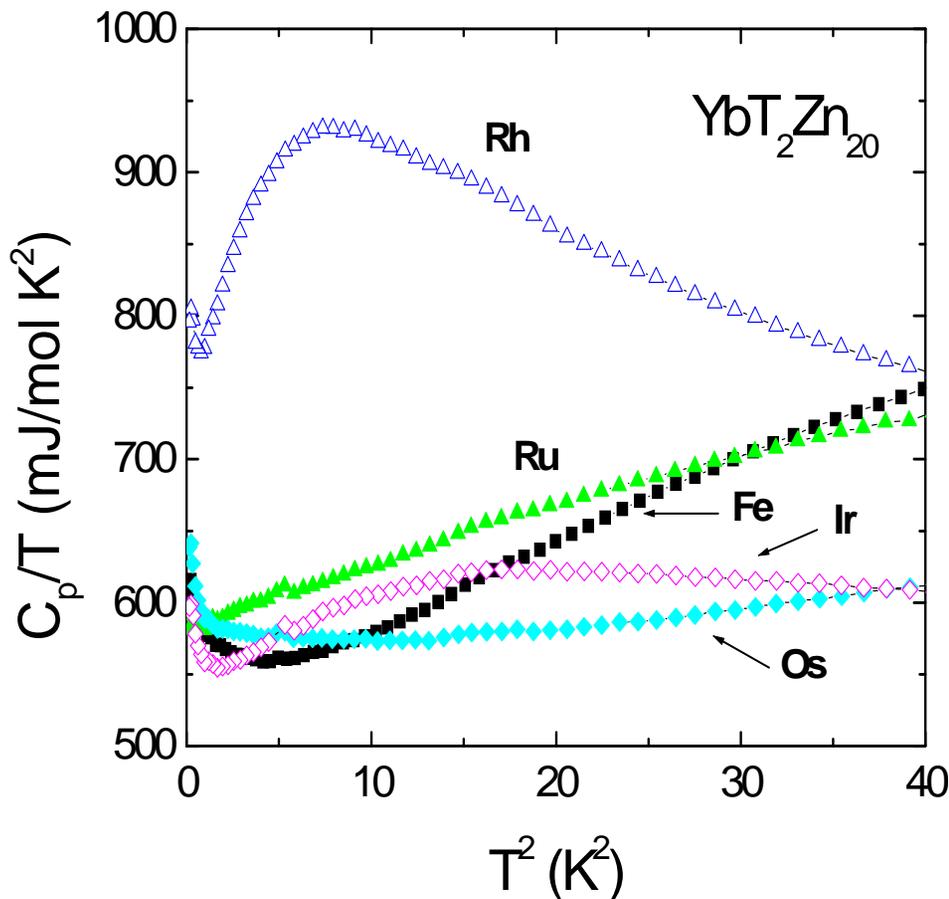


- Hybridizing members of the  $\text{RT}_2\text{Zn}_{20}$  series are examples of ordered Kondo lattices that are approaching a single ion impurity concentration level.
- For  $T = \text{Fe, Co, Ru, Rh, Os, Ir}$  we have discovered **SIX NEW** Yb-based heavy fermion compounds. (*Formally, doubling the number of such compounds!*)



With very similar R coordination, this half dozen new systems allows for comparison of the thermodynamic and transport properties between very closely related heavy fermion compounds.

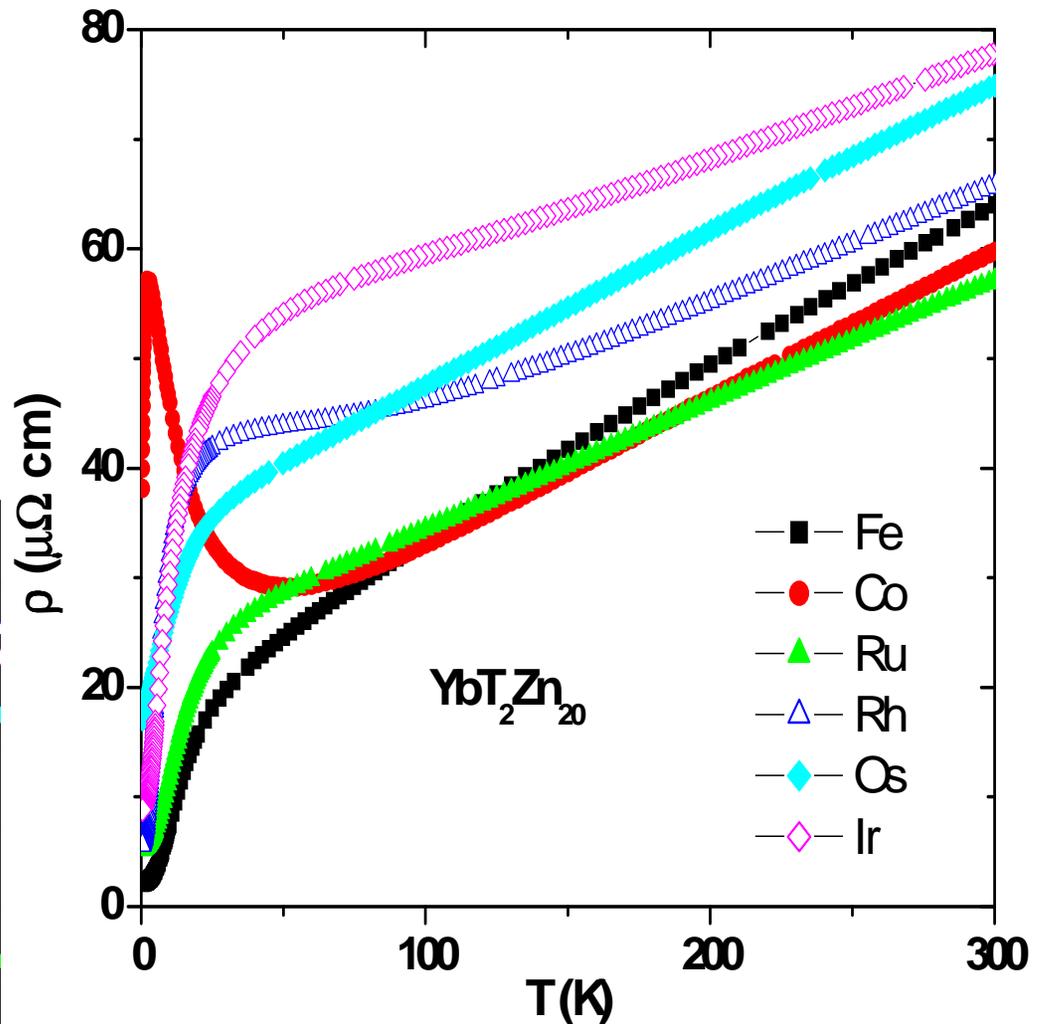
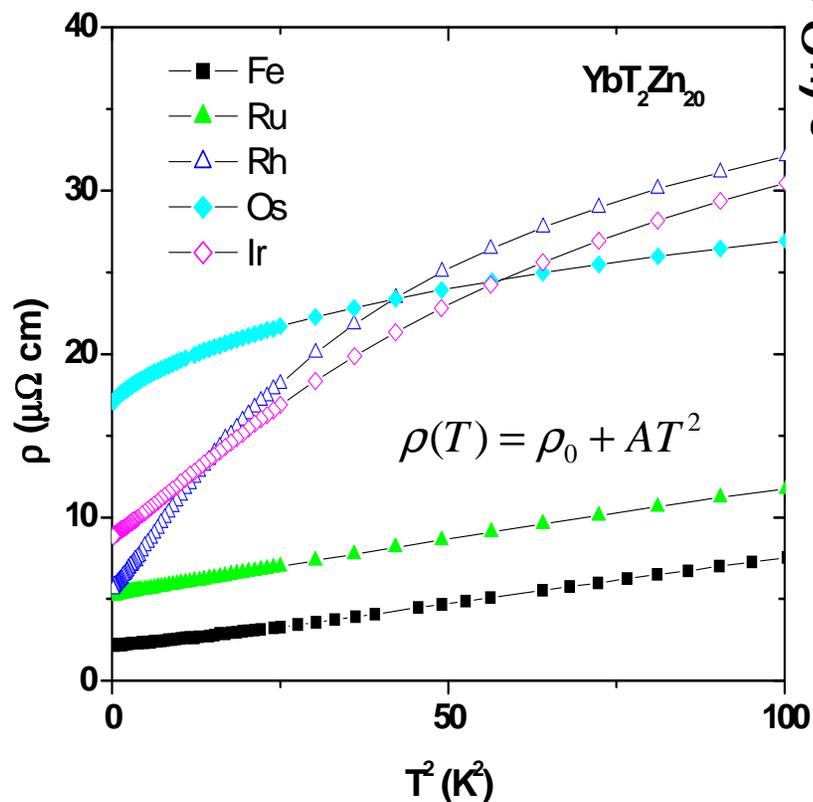
For T = Fe, Ru, Rh, Os & Ir, clear loss of local moment behavior at low T



The compounds appear to be an example of a Yb-based heavy fermion with large  $\gamma$ .



T-dependent resistivity of these 6 compounds manifest classic heavy fermion features; 5 *very* similar and  $\text{YbCo}_2\text{Zn}_{20}$  related.

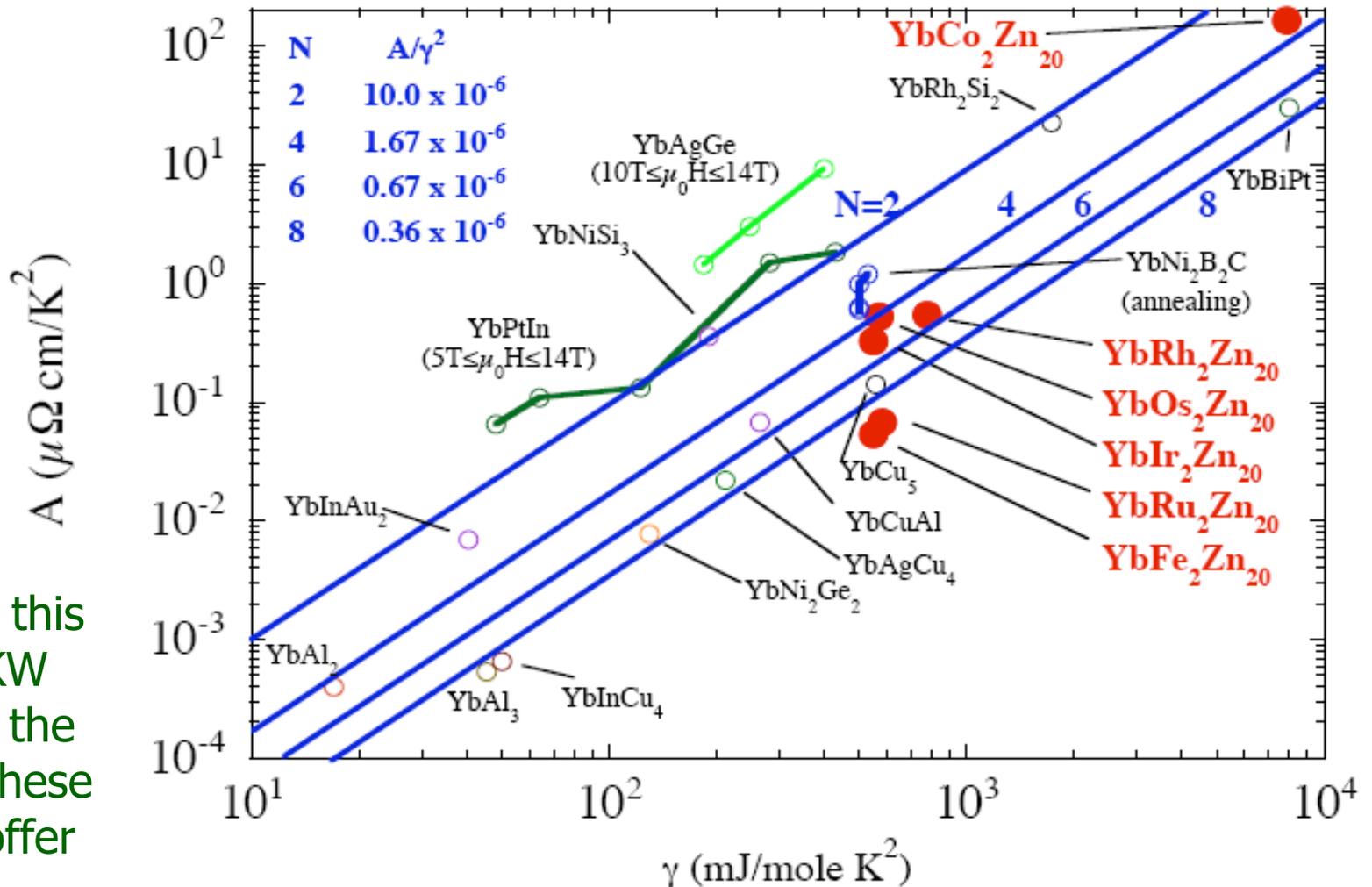


These 5 compounds show clear  $T^2$  dependencies at low T.

We can plot the data for our six new  $\text{YbT}_2\text{Zn}_{20}$  heavy fermions on a Kadowaki-Woods plot with some other Yb-based systems. We see that for  $T = \text{Fe, Ru, Rh, Os, Ir}$  there is a vertical spread that implies a significant difference in the Yb ion degeneracy for  $T \sim T_K$ . E.g. for  $T = \text{Fe, Ru}$  have higher  $T_K / T_{\Delta\text{CEF}}$  ratios.

Can we correlate this with other data we have collected?

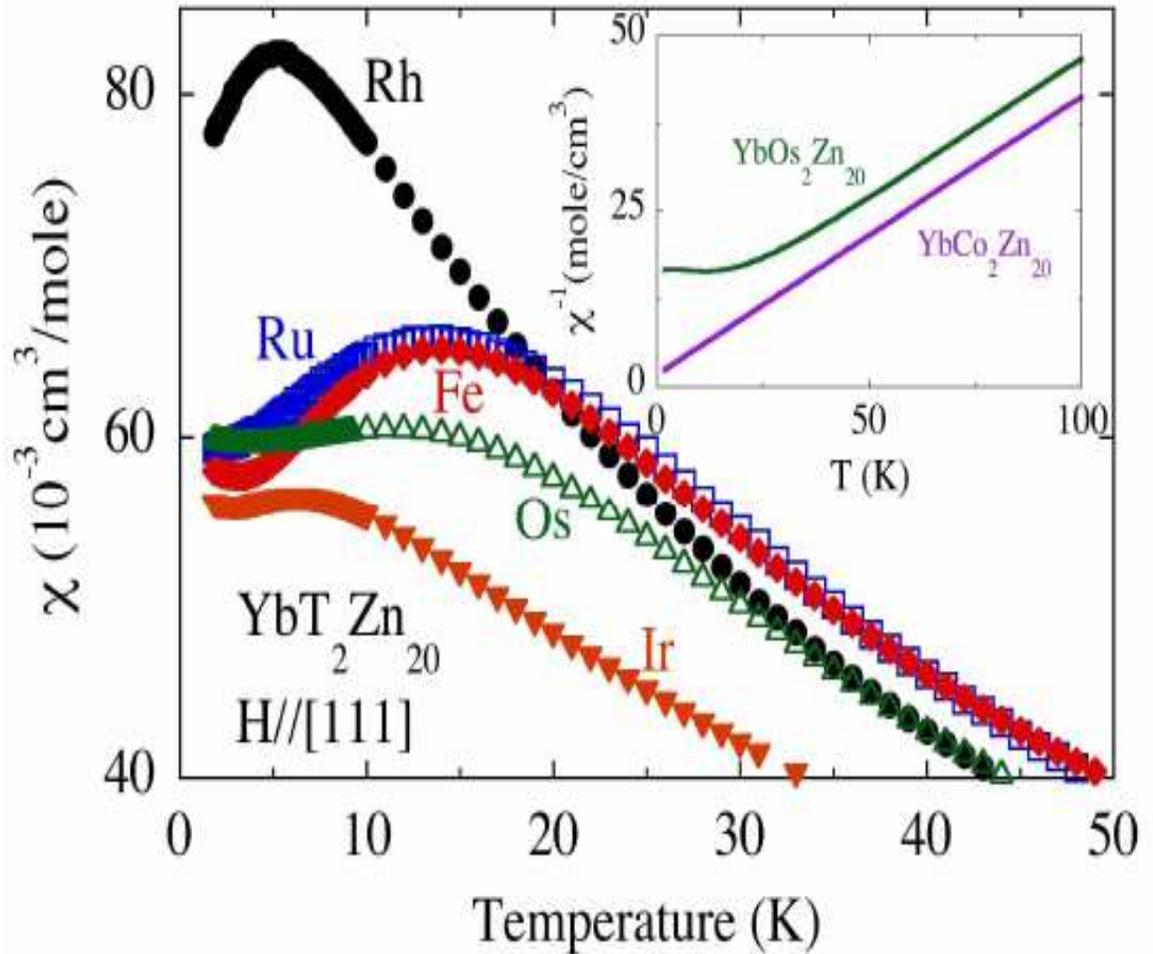
Can we gain some faith in this generalized KW plot by using the systematics these compounds offer us?





*At a qualitative level:*

--The temperature of  $\chi_{\max}$  can be used as a caliper of the Kondo temperature. For  $T = \text{Ru}$  and  $\text{Fe}$   $\chi_{\max}$  occurs near 14 K and for  $T = \text{Ir}$  and  $\text{Rh}$   $\chi_{\max}$  occurs near 6 K. ( $T = \text{Os}$  is intermediate.)

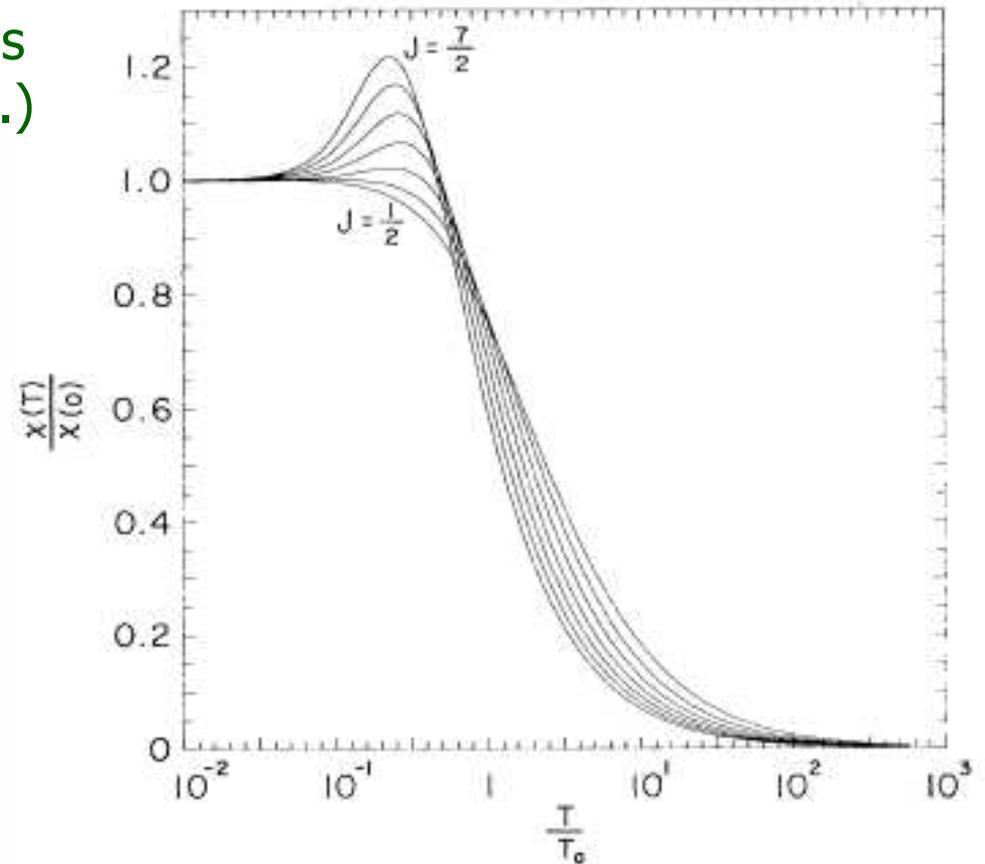
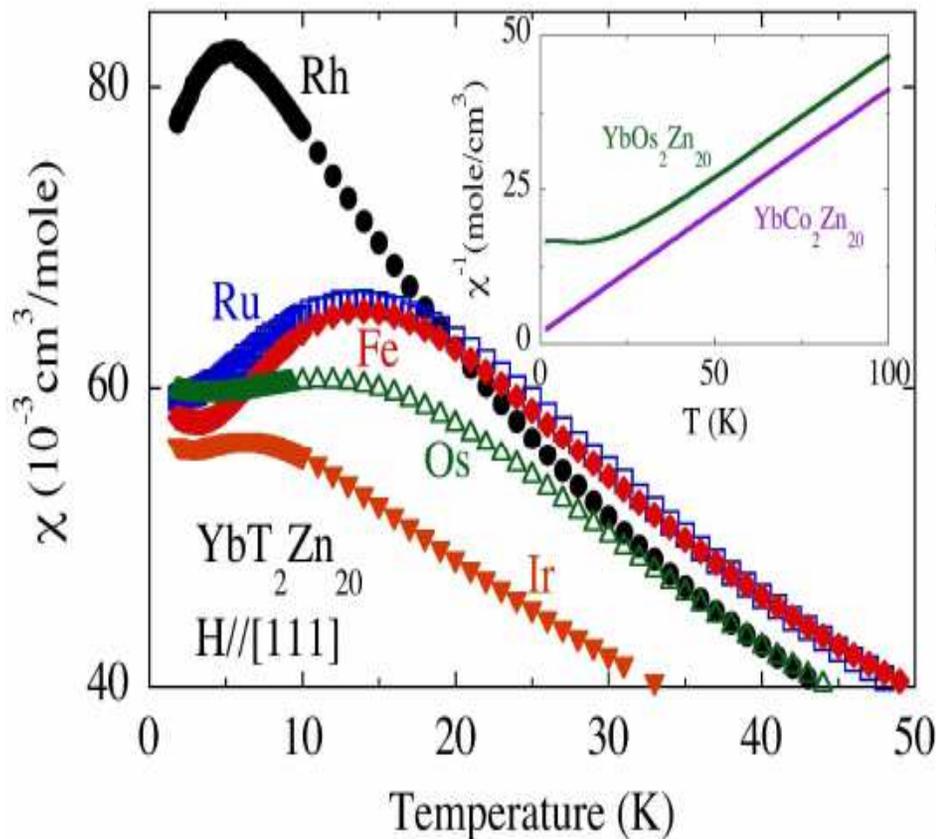


--If we assume that  $T_{\Delta\text{CEF}}$  does not vary significantly (for the R site the nearest neighbors and next nearest neighbors are all Zn), then the  $T_K / T_{\Delta\text{CEF}}$  ratio (and therefore the degeneracy) is higher for  $T = \text{Fe}$  and  $\text{Ru}$  than it is for  $T = \text{Ir}, \text{Rh}$ .



Slightly more quantitatively, if we use Rajan's analysis of the Coqblin Schrieffer model, we can estimate the degeneracy by evaluating  $\chi_{\max} / \chi(T \sim 0 \text{ K})$ .

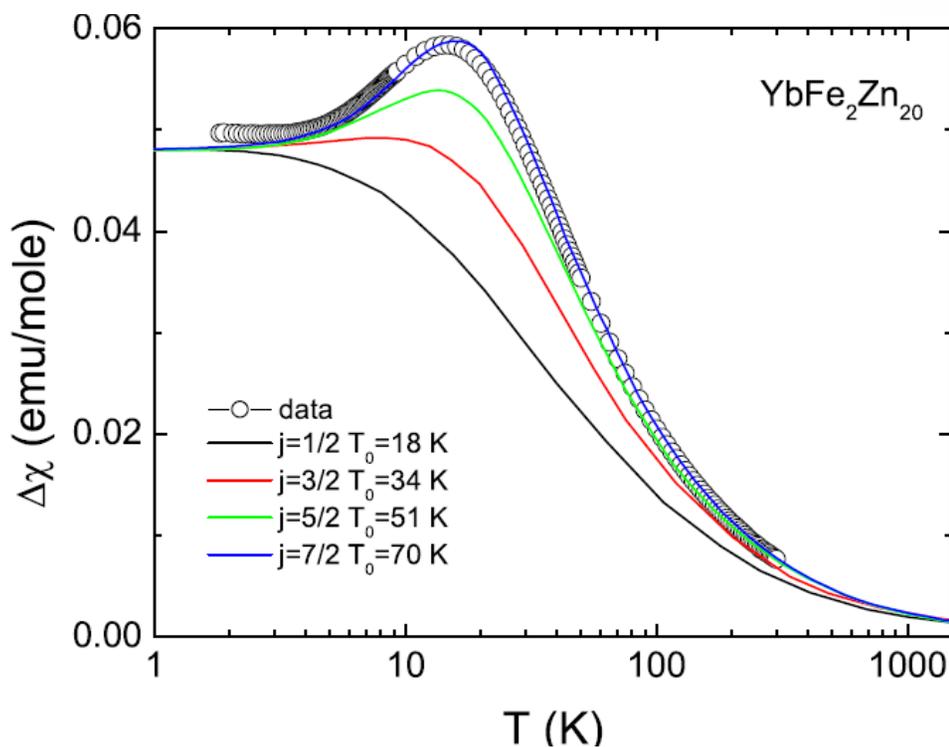
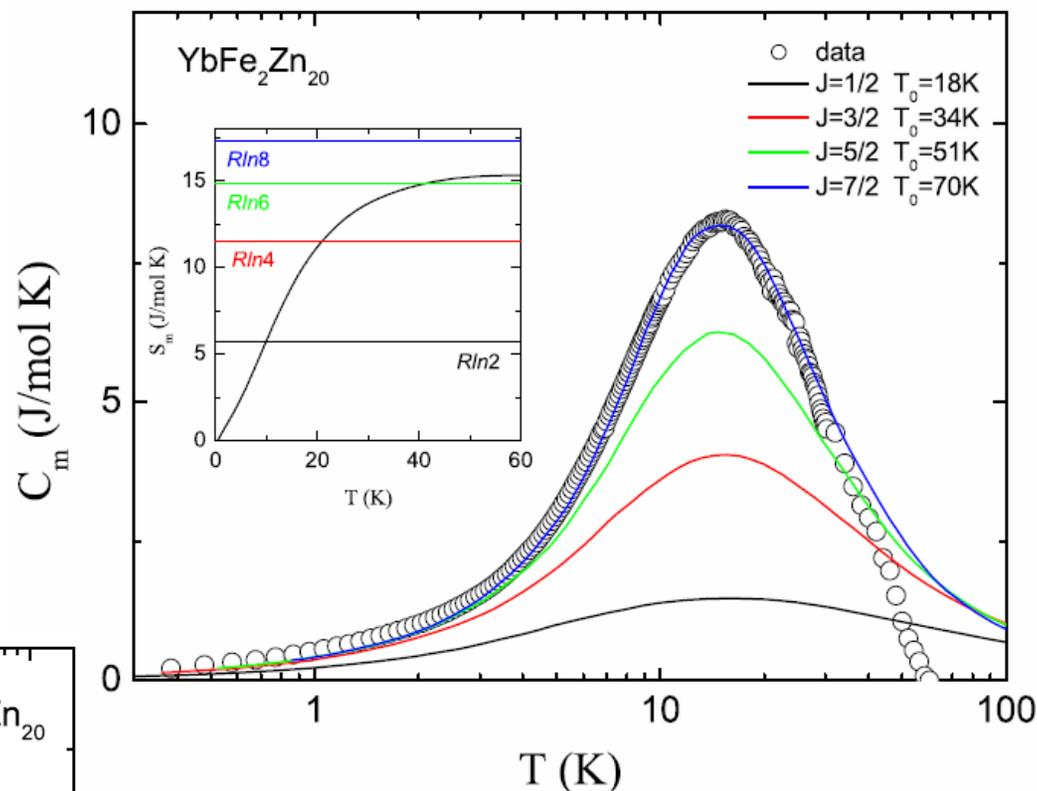
From this analysis we find that  $T = \text{Fe}$  and  $\text{Ru}$  have  $J \sim 5/2$  and  $T = \text{Ir}$  and  $\text{Os}$  have  $J \sim 3/2$ . ( $T = \text{Rh}$  is intermediate.)



PHYSICAL REVIEW LETTERS  
V. T. Rajan VOLUME 51, NUMBER 4 308 25 JULY 1983  
Magnetic Susceptibility and Specific Heat of the Coqblin-Schrieffer Model



We can pursue this even further (and much more formally) by fitting both the  $C_p$  and  $\chi$  data to the Coqblin Schrieffer model.

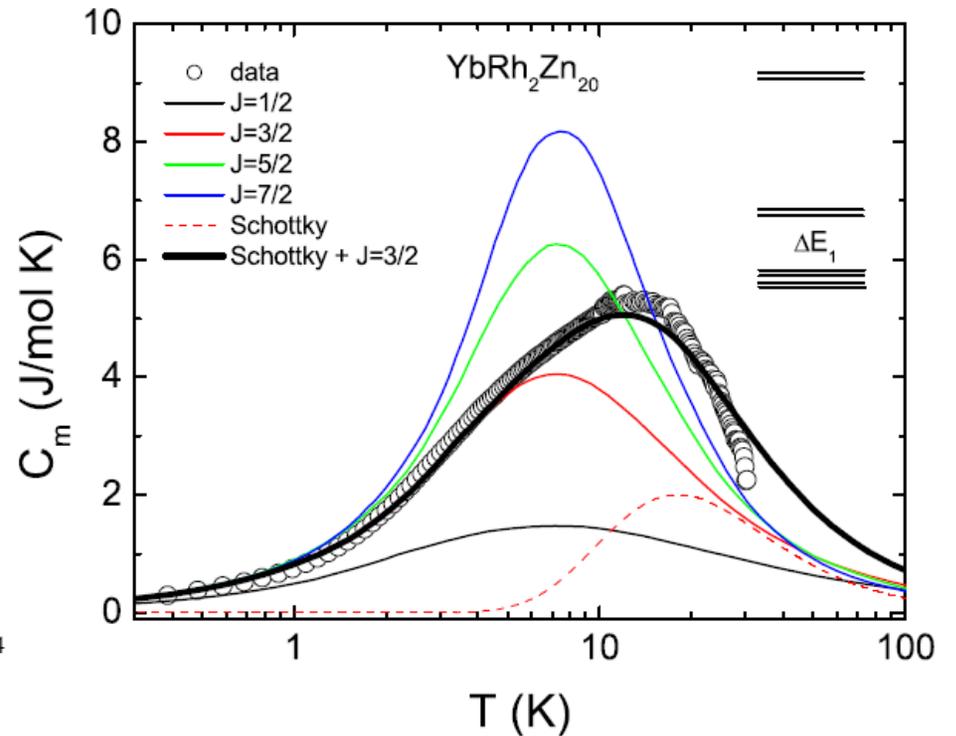
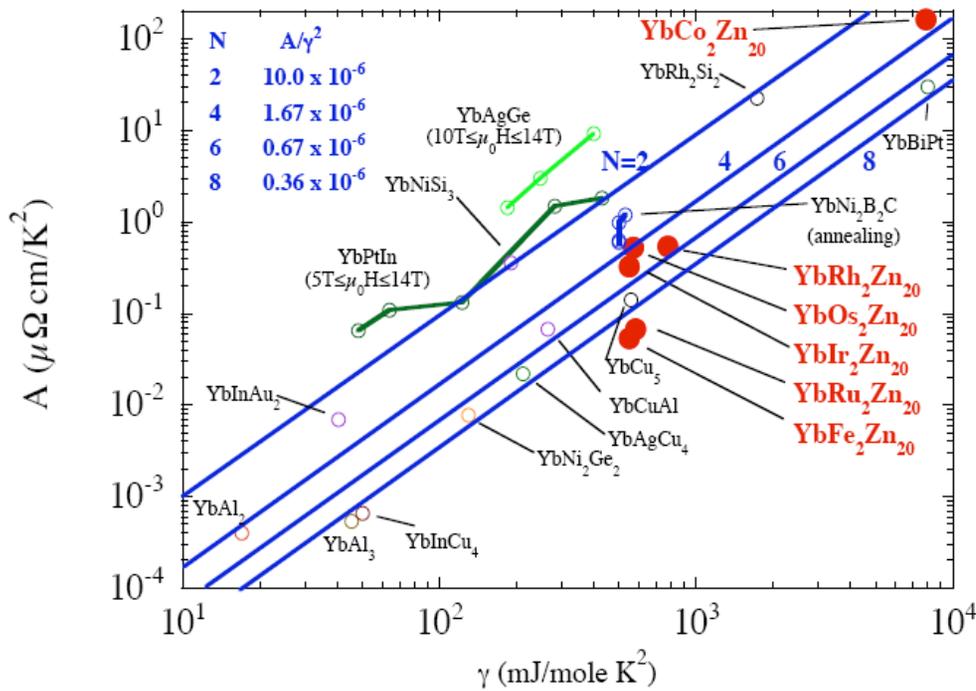
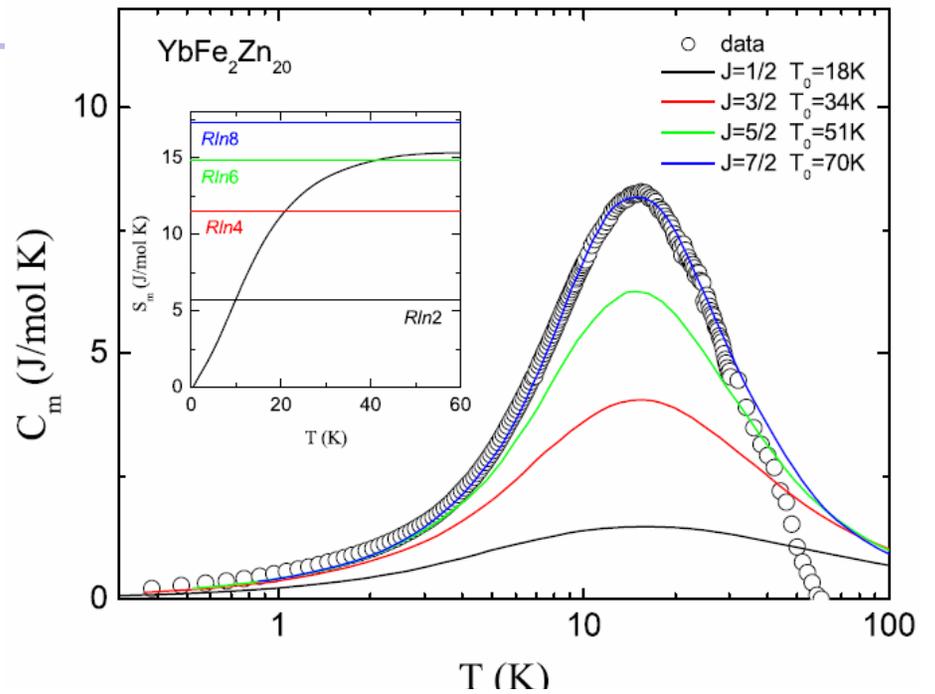


As can be seen, the degeneracy value of  $N = 8$  ( $J = 7/2$ ) from the K-W analysis (as well as the more informal analysis of  $\chi$ ) is clearly supported by both these data sets.



$\text{YbFe}_2\text{Zn}_{20}$  is a high degeneracy,  $N = 8$ , Kondo lattice.

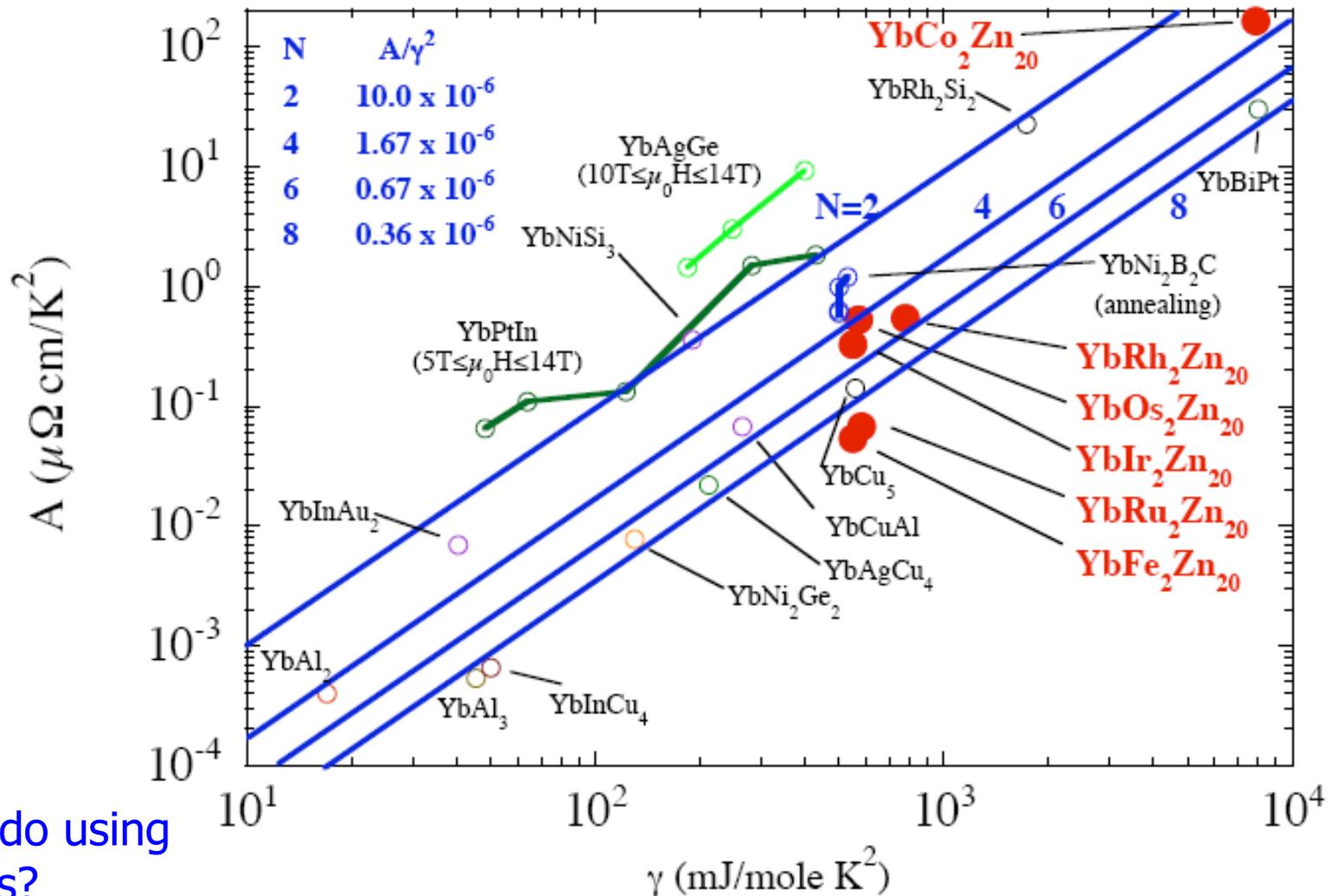
On the other extreme  $\text{YbRh}_2\text{Zn}_{20}$   $C_p(T)$  data has to be fit with  $N = 4$  plus CEF Schottky anomaly.





Both qualitative and quantitative analysis support the conclusion we reach from the Kadawaki-Woods analysis:  $\text{YbFe}_2\text{Zn}_{20}$  and  $\text{YbRu}_2\text{Zn}_{20}$  both have higher Yb ion degeneracies at  $T_K$ .

The question of whether this is associated with the properties of  $\text{LuFe}_2\text{Zn}_{20}$  and  $\text{LuRu}_2\text{Zn}_{20}$  (Stoner-like) remains open.



What can we do using these N values?



# Evaluation of $T_K$ ....This can be *easy* or **hard**.

From simple transfer of entropy arguments we get  $\gamma T_K = R \ln(N)$

$$T_0 = \frac{\log(N)}{\gamma_{\text{imp}}}$$

More erudite and detailed analysis gives:

$$\gamma_{\text{imp}} = \frac{\pi^2 \omega_N}{3 T_K} \frac{N-1}{N}$$

$$\omega_N = \frac{e^{C+1-3/(2N)}}{2\pi\Gamma(1+1/N)}$$

J W Rasul and A C Hewson  
J. Phys. C: Solid State Phys., 17 (1984) 2555-2573.

When I compared the easy with the profound, I was delighted to find that for physical values of  $N$  (8 or less), the easy, physically intuitive, approach is within 6% of the rather complex, formal one. !!!!

$$\kappa(N) \equiv \frac{T_K}{T_0} = \frac{\pi^2 \omega_N}{3} \frac{N-1}{N \log(N)}$$

$N$	$\kappa(N)$
2	0.97466
3	1.04484
4	1.03992
5	1.01667
6	0.98974
7	0.96344
8	0.93901
9	0.91670
10	0.89643

Thanks to J. Schmalian for checking my work on this.



We can then use our  $\gamma$  and  $N$  values to extract  $T_K$

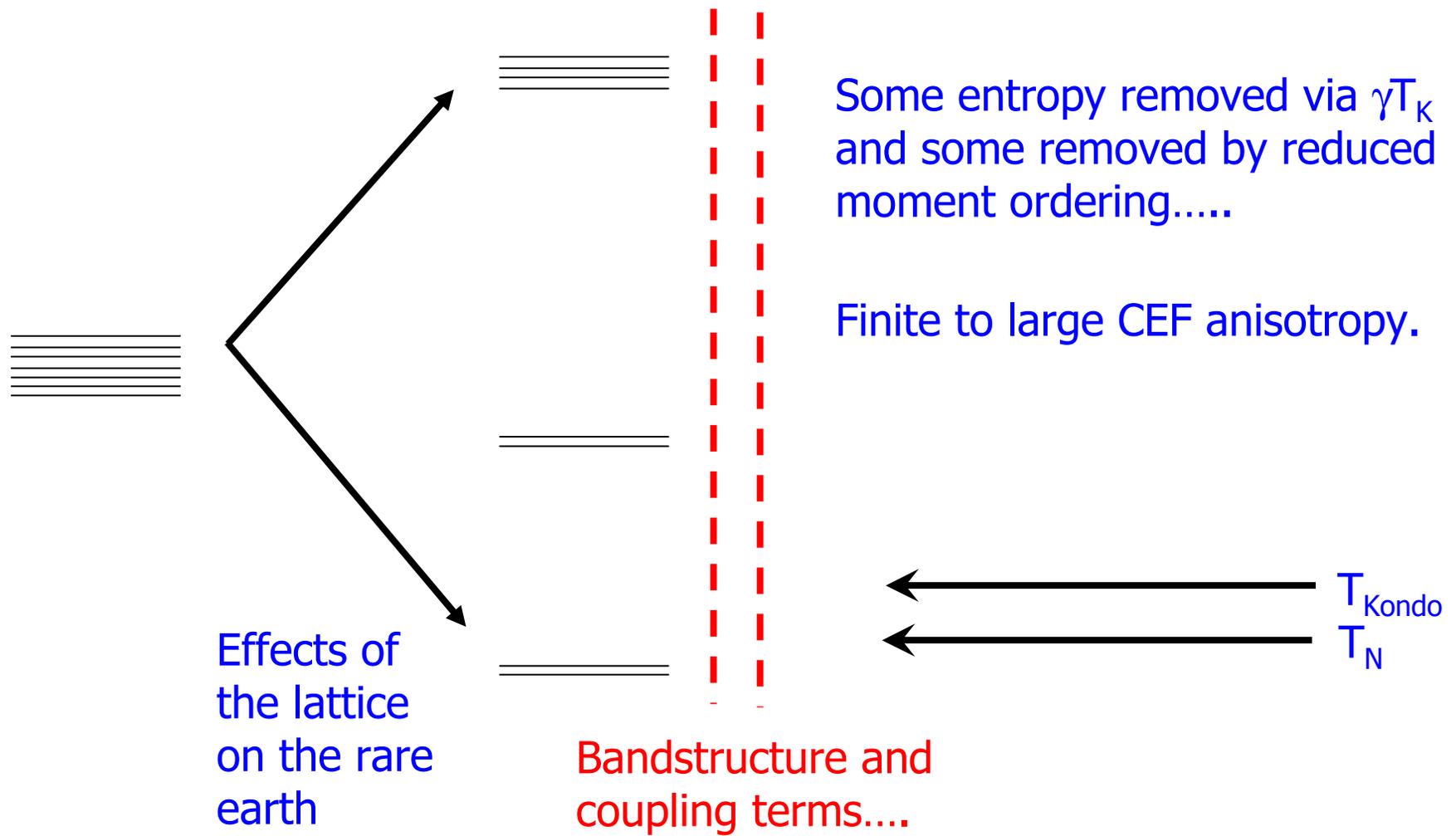
TABLE I: Summary of structural, thermodynamic and transport data on  $\text{YbT}_2\text{Zn}_{20}$  compounds  
( $T = \text{Fe, Co, Ru, Rh, Os, Ir}$ )

T	$a$ $\text{\AA}$	$\Theta$ K	$\mu_{eff}$ $\mu_B$	$\chi_0$ $\frac{10^{-3}\text{cm}^3}{\text{mole}}$	$\chi_{max}$ $\frac{10^{-3}\text{cm}^3}{\text{mole}}$	$T_{\chi_{max}}$ K	$\rho_0$ $\mu\Omega \text{ cm}$	$A$ $\frac{\mu\Omega \text{ cm}}{\text{K}^2}$	RRR	$\gamma$ $\frac{\text{mJ}}{\text{mol K}^2}$	WR	KWR $\frac{\mu\Omega \text{ cm mole}^2 \text{ K}^2}{\text{mJ}^2}$	$N$	$T_K$ K
Fe	14.062	-22.6	4.5	58.0	65.1	14.0	2.1	$5.4 \cdot 10^{-2}$ ( $T \leq 11 \text{ K}$ )	31.2	520	1.2	$2.0 \cdot 10^{-7}$	8	33
Co	14.005	-4.3	4.3	415.1			21	165 ( $T \leq 0.2 \text{ K}$ )	2.8	7900		$27 \cdot 10^{-7}$	4	1.5
Ru	14.193	-15.5	4.5	58.9	65.4	13.5	5.3	$6.8 \cdot 10^{-2}$ ( $T \leq 11 \text{ K}$ )	10.9	580	1.1	$2.0 \cdot 10^{-7}$	8	30
Rh	14.150	-15.9	4.4	77.7	82.4	5.3	5.6	$54 \cdot 10^{-2}$ ( $T \leq 6 \text{ K}$ )	11.8	740	1.3	$10.1 \cdot 10^{-7}$	4	16
Os	14.205	-19.18	4.5	60.0	60.7	11.5	17	$53 \cdot 10^{-2}$ ( $T \leq 1 \text{ K}$ )	4.4	580	1.1	$15 \cdot 10^{-7}$	4	20
Ir	14.165	-23.8	4.4	55.9	56.3	6.5	8.8	$33 \cdot 10^{-2}$ ( $T \leq 5 \text{ K}$ )	8.9	540	1.2	$11 \cdot 10^{-7}$	4	21

$T_K$  is indeed higher for  $T = \text{Fe}$  and  $\text{Ru}$  compounds.  
This confirms our qualitative analysis of  $\chi(T)$  data.



If the Kondo temperature and the magnetic ordering temperature can be brought a bit closer together (playing with the energy scales), then the system can be tuned from the local moment side to the correlated electron (heavy fermion) side.

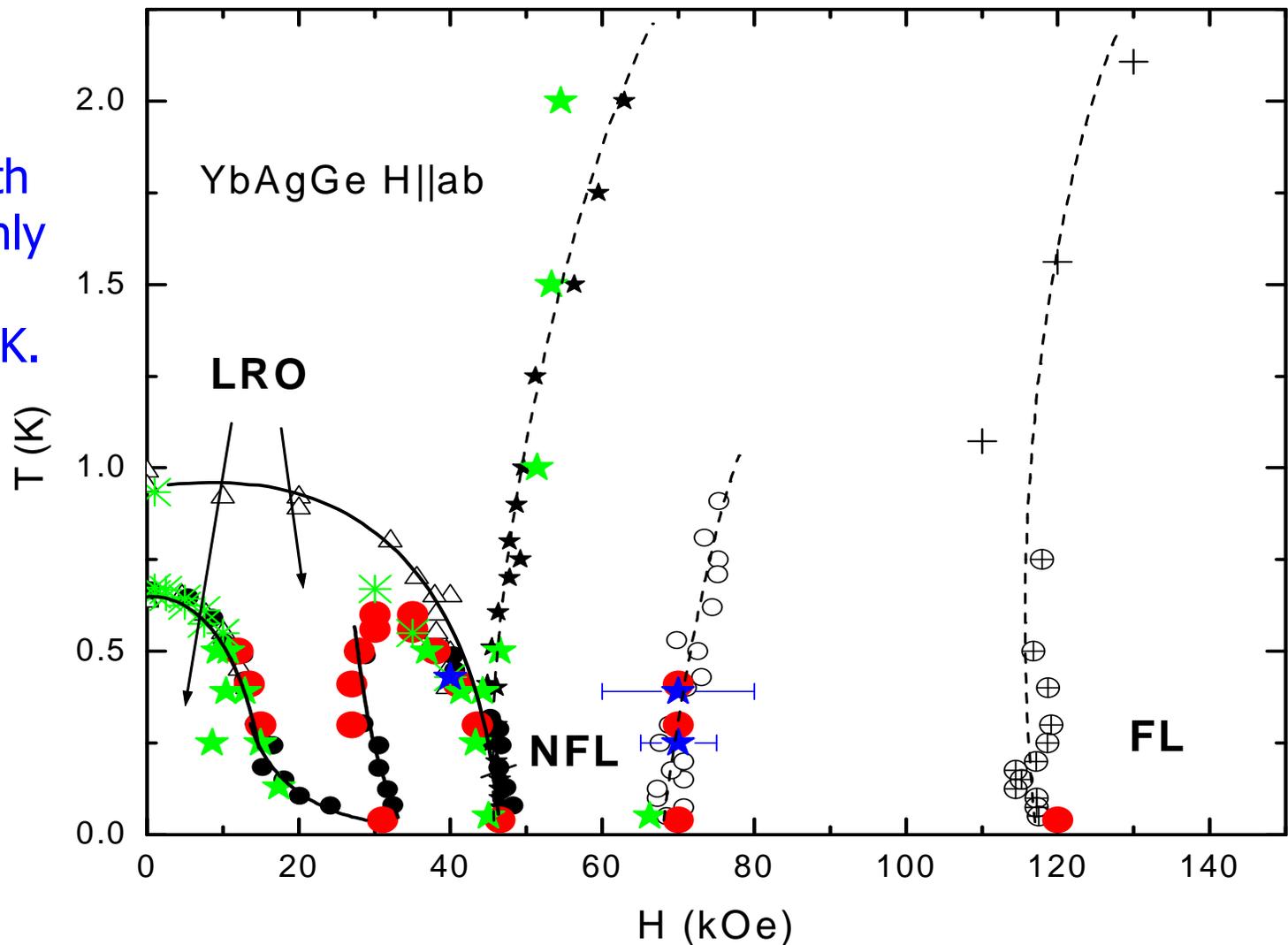




For example, in YbAgGe the system can be tuned to a quantum critical point by application of modest magnetic fields....A physicists playground.

In zero field, the system orders with reduced, and highly anisotropic, moment below 1 K.

Application of H suppresses LRO and the evolution to a correlated Fermi liquid state can be studied.





With quantum criticality we can fine tune rare earth systems from the local moment behavior we know and love into strongly, or moderately, correlated electron states that bear similarity of d-shell metals.

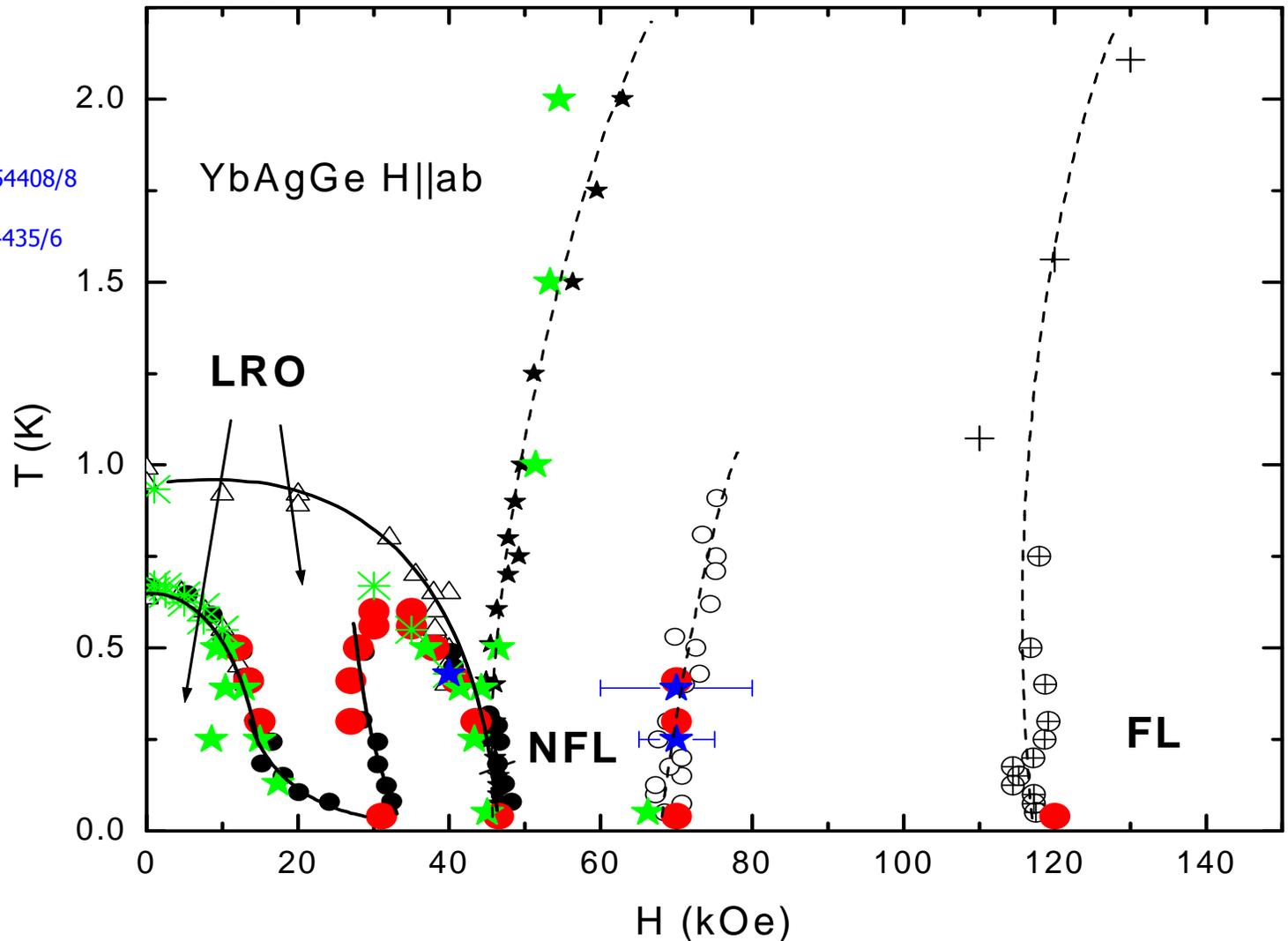
JMMM (2004), 277(3), 298-321

PRB (2004), 69(1), 014415/1-8

PRB (2005), 71(5), 054408/1-054408/8

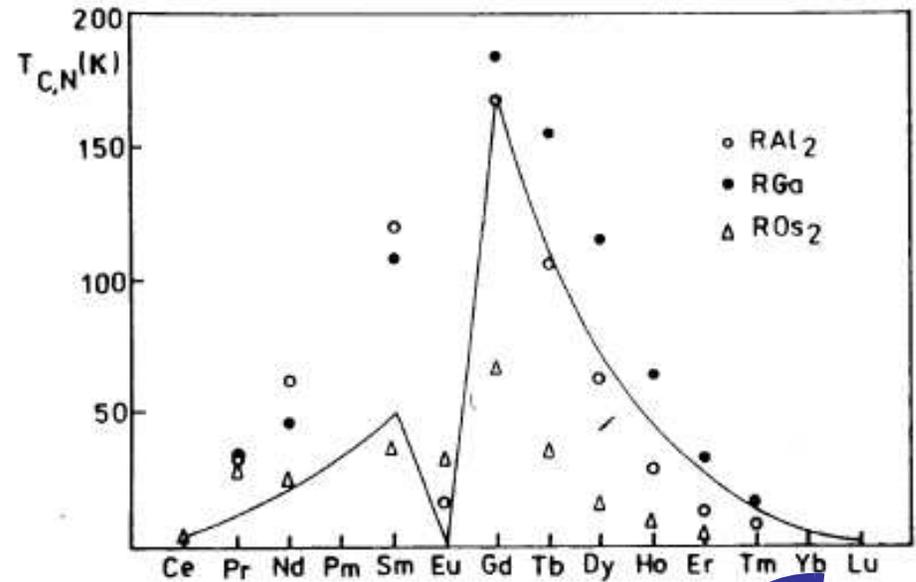
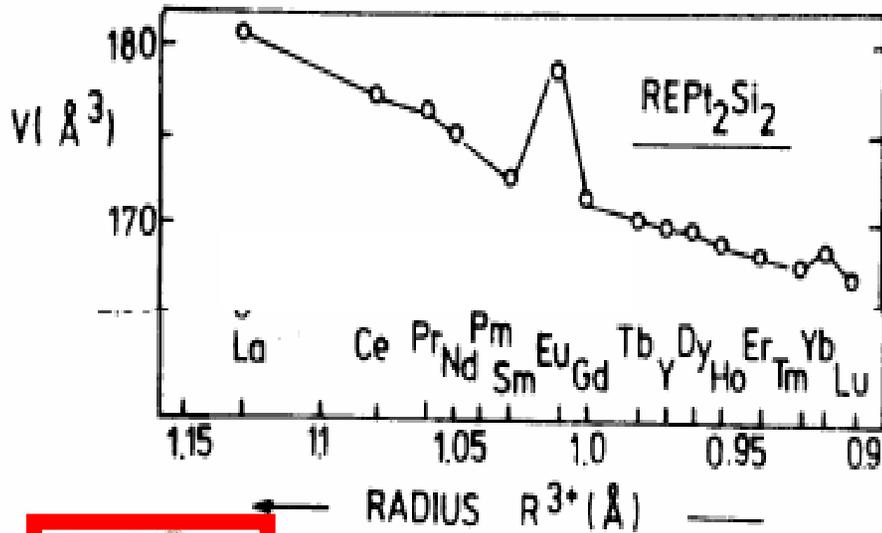
PRB (2006), 73(9), 094435/1-094435/6

If we think of decreasing field, we can study the birth of local moment behavior.





The purpose of this talk was to review how the rare earths can be viewed, and used by the physicist



Ce Pr Nd Pm Sm Eu Gd Tb Dy Ho Er Tm Yb



57	58	59	60	61	62	63	64	65	66	67	68	69	70
<b>La</b>	<b>Ce</b>	<b>Pr</b>	<b>Nd</b>	<b>Pm</b>	<b>Sm</b>	<b>Eu</b>	<b>Gd</b>	<b>Tb</b>	<b>Dy</b>	<b>Ho</b>	<b>Er</b>	<b>Tm</b>	<b>Yb</b>
138.9	140.1	140.9	144.2	146.9	150.4	152.0	157.3	158.9	162.5	164.9	167.3	168.9	173.0

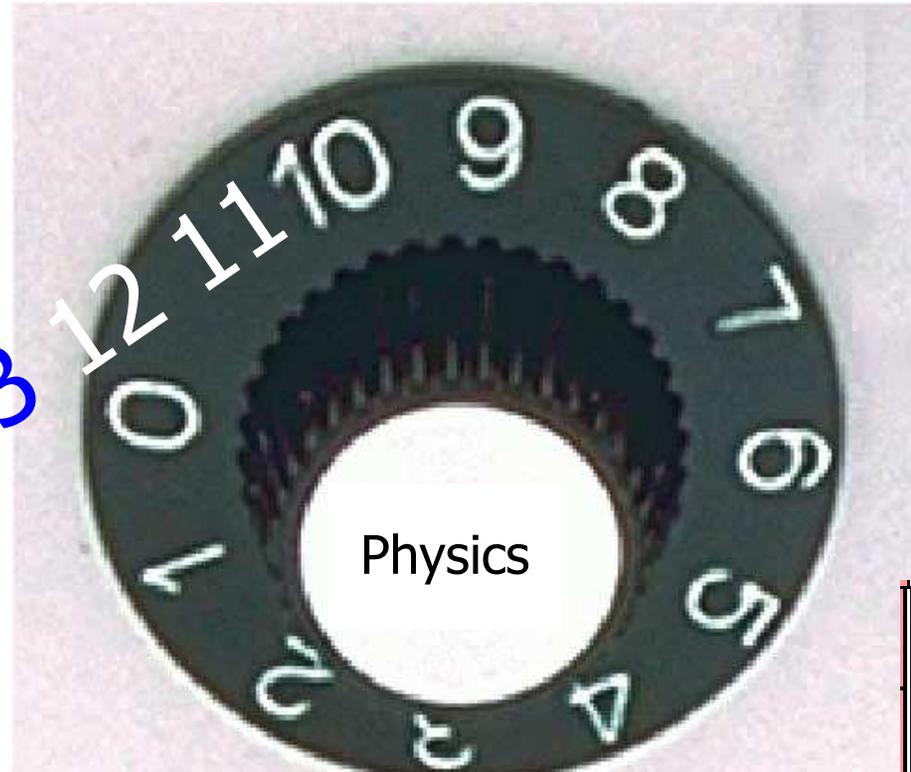
**XXX** **XXX** **3+** **XXX** **XXX** **XXX** **3+** **3+** **3+** **3+** **3+** **3+** **3+** **XXX**  
**hyb** **sng** **OK** **HOT** **Hund** **div** **OK** **OK** **OK** **OK** **OK** **OK** **OK** **hyb**



## *The physicist sees a 17 position knob*

- That can be used to dial in magnetism
- That can be used to control unit cell volume
- That can be used to influence anisotropy
- That can be used to effect entropy
- That can allow varying degrees of hybridization

It is this control and variety that draws the physicist to the rare earth series and compounds.



17 16 15 14 13

57	58	59	60	61	62	63	64	65	66	67	68	69	70	71
<b>La</b>	<b>Ce</b>	<b>Pr</b>	<b>Nd</b>	<b>Pm</b>	<b>Sm</b>	<b>Eu</b>	<b>Gd</b>	<b>Tb</b>	<b>Dy</b>	<b>Ho</b>	<b>Er</b>	<b>Tm</b>	<b>Yb</b>	<b>Lu</b>
138.9	140.1	140.9	144.2	146.9	150.4	152.0	157.3	158.9	162.5	164.9	167.3	168.9	173.0	175.0

21
<b>Sc</b>
44.96
39
<b>Y</b>
88.91



## Acknowledgements

Orson Welles once said that making films was like being a small child with a very expensive paint box. In a similar manner searching for new materials and growing single crystals of a wide variety of compounds requires an adequate and flexible materials budget. We gratefully acknowledge the US Department of Energy, Office of Basic Energy Sciences. Their unflagging support has made all of this research possible.

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*That's All Folks*