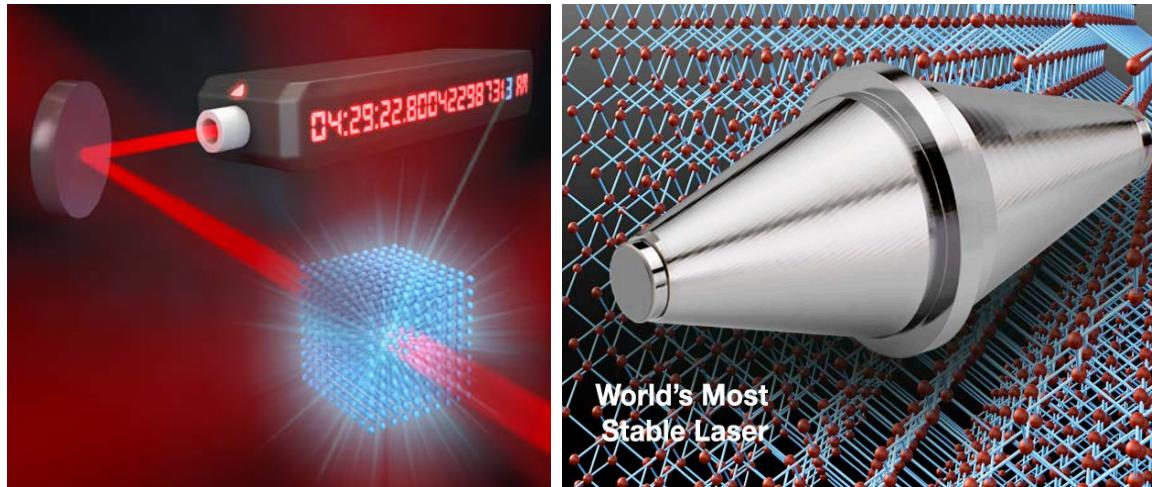


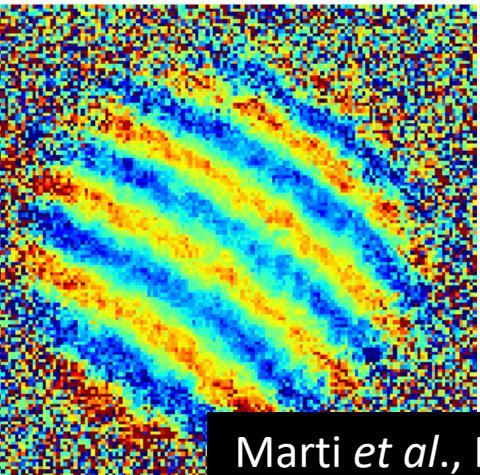
# Measurement at the quantum frontier

J. Ye

Boulder Summer School, July 24, 2018

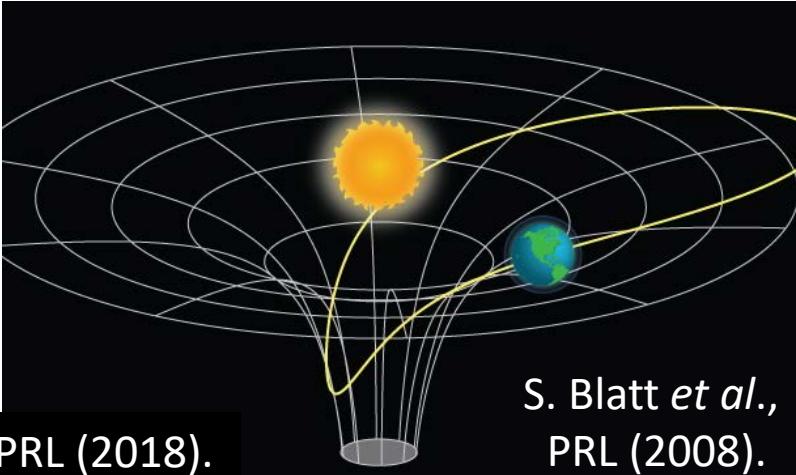


Quantum sensing



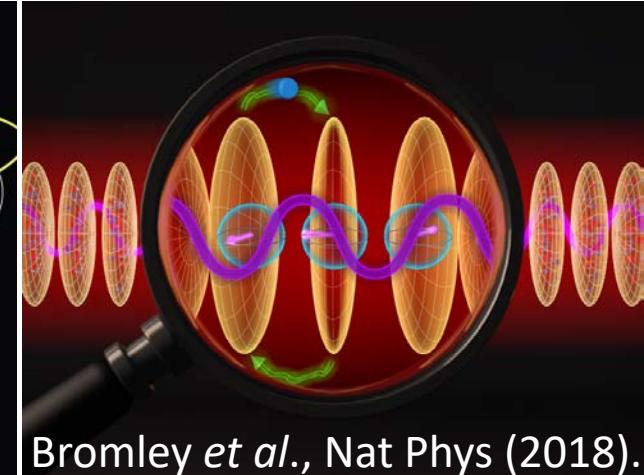
Marti *et al.*, PRL (2018).

Table-top search for new physics



S. Blatt *et al.*,  
PRL (2008).

Many-body dynamics



Bromley *et al.*, Nat Phys (2018).

# Lecture outlines

## Lecture I

- Simple atomic physics
- Basic quantum physics
- Basic laser science

→ The ingredients for control & measurement of quantum coherence

## Lecture II

- Atomic interactions
- Spin Hamiltonians
- Emergence of complexity from simple ingredients

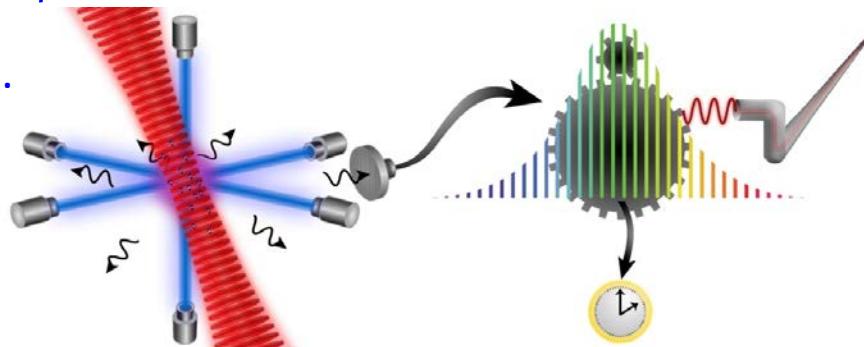
→ A new frontier: quantum metrology & many-body physics

# Atomic/Molecular Ultracold Matter

Precise control of quantum systems

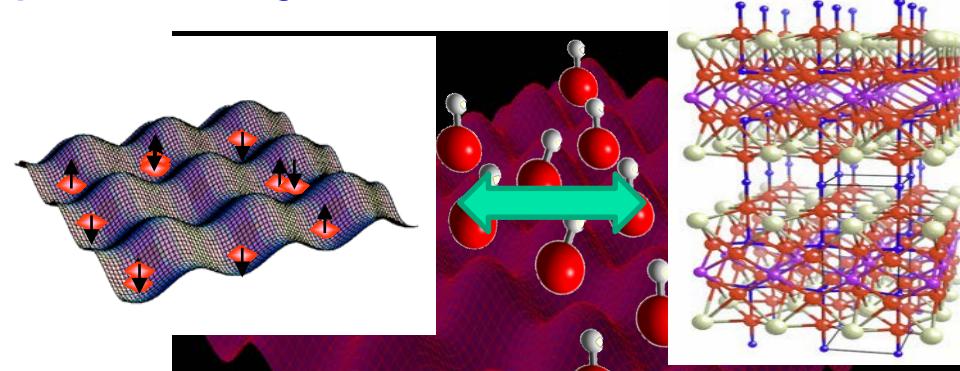
- Clocks, quantum information, sensors

Bloom *et al.*, Nature **506**, 71 (2014).



Understanding complexities  
& strong correlations

- Superconductivity & Superfluidity
- Quantum magnetism
- Quantum chemistry



Universality & scaling

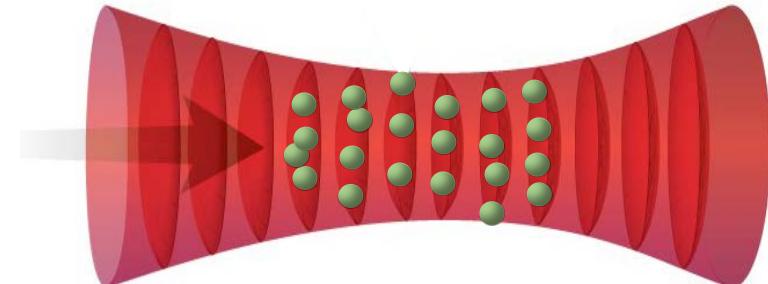
- Contact vs. long-range
- Drive vs. interaction

Atoms  $\leftrightarrow$  Electrons  
Optical lattice  $\leftrightarrow$  Ionic Crystal

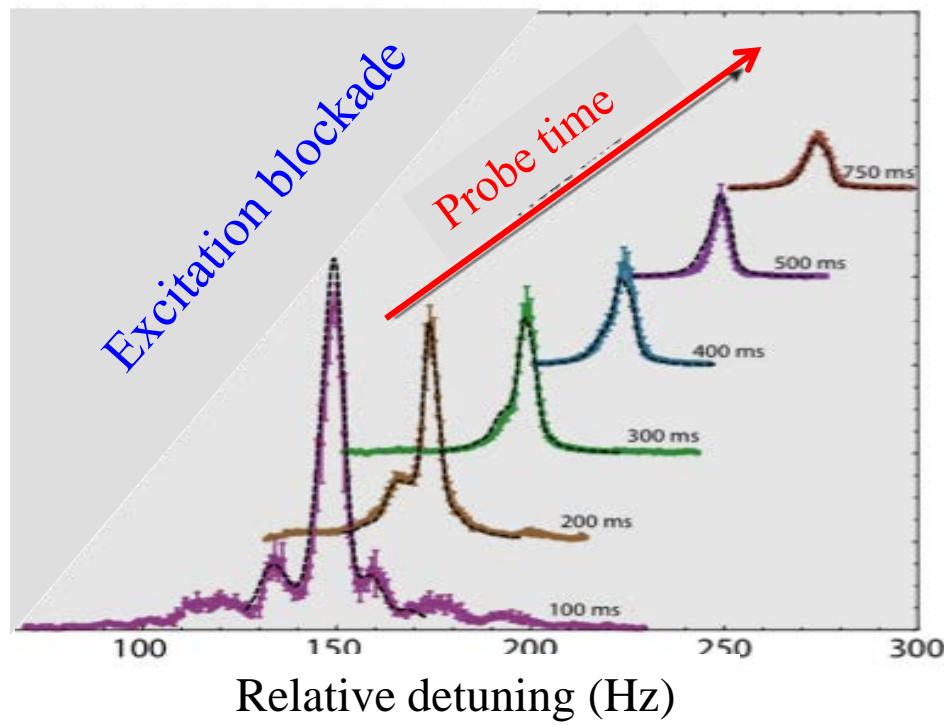
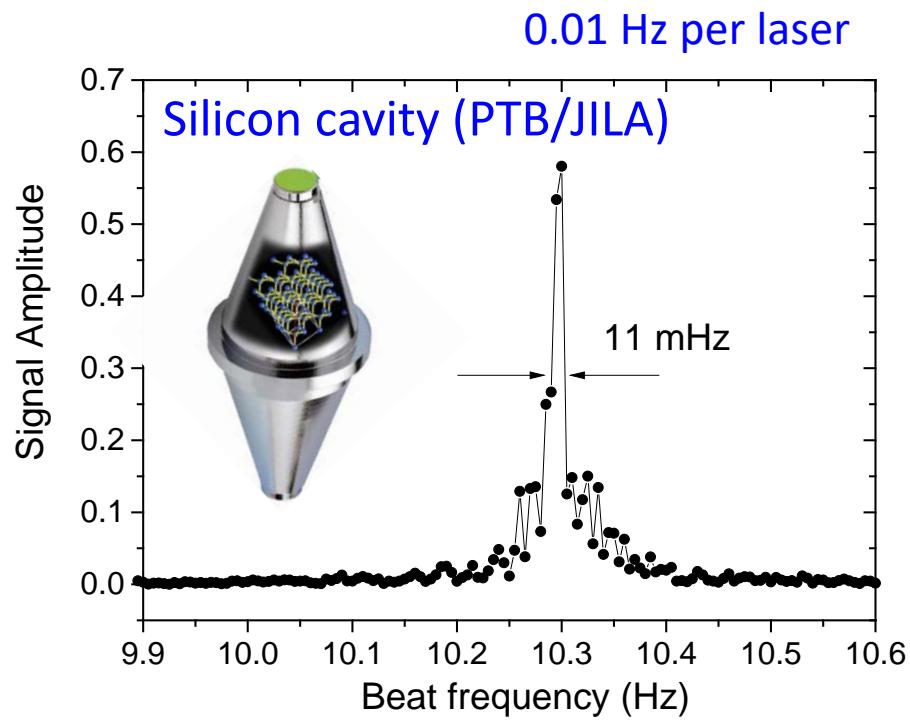
# Precision metrology meets many-body physics

Martin *et al.*, Science 341, 632 (2013).

A new generation of stable lasers



1D Lattice

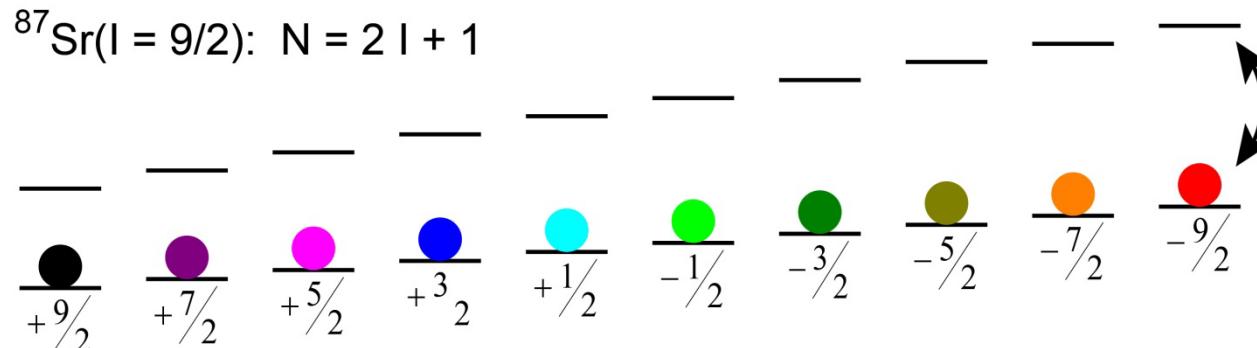


# 3 degrees of freedom: electronic, nuclear, spatial

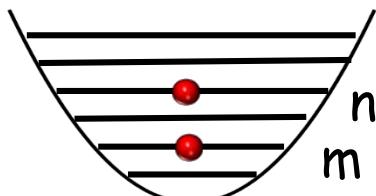
$^{87}\text{Sr} (I = 9/2): N = 2I + 1$

$|e\rangle \uparrow^3P_0$

$|g\rangle \downarrow^1S_0$



hyperfine coupling  
 $I \cdot J = 0$ .



nuclear

$\otimes$

electronic

$\otimes$

motional



$|n m\rangle + |m n\rangle$

Spatially Symmetric



$|n m\rangle - |m n\rangle$

Spatially Anti-Symmetric

$$\left( \begin{array}{c} |\bullet\bullet\bullet\rangle \\ |\bullet\bullet\bullet\rangle \\ |\bullet\bullet\bullet\rangle + |\bullet\bullet\bullet\rangle \\ |\bullet\bullet\bullet\rangle - |\bullet\bullet\bullet\rangle \end{array} \right) \otimes$$

OR

$$\left( \begin{array}{c} |\uparrow\uparrow\rangle \\ |\downarrow\downarrow\rangle \\ |\uparrow\downarrow\rangle + |\downarrow\uparrow\rangle \\ |\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle \end{array} \right) \otimes$$

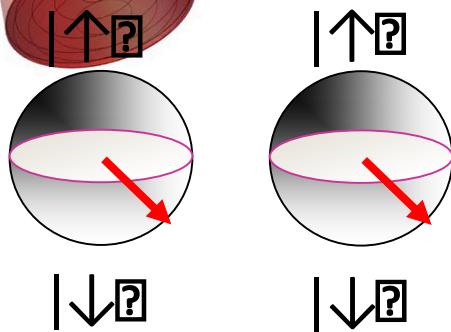
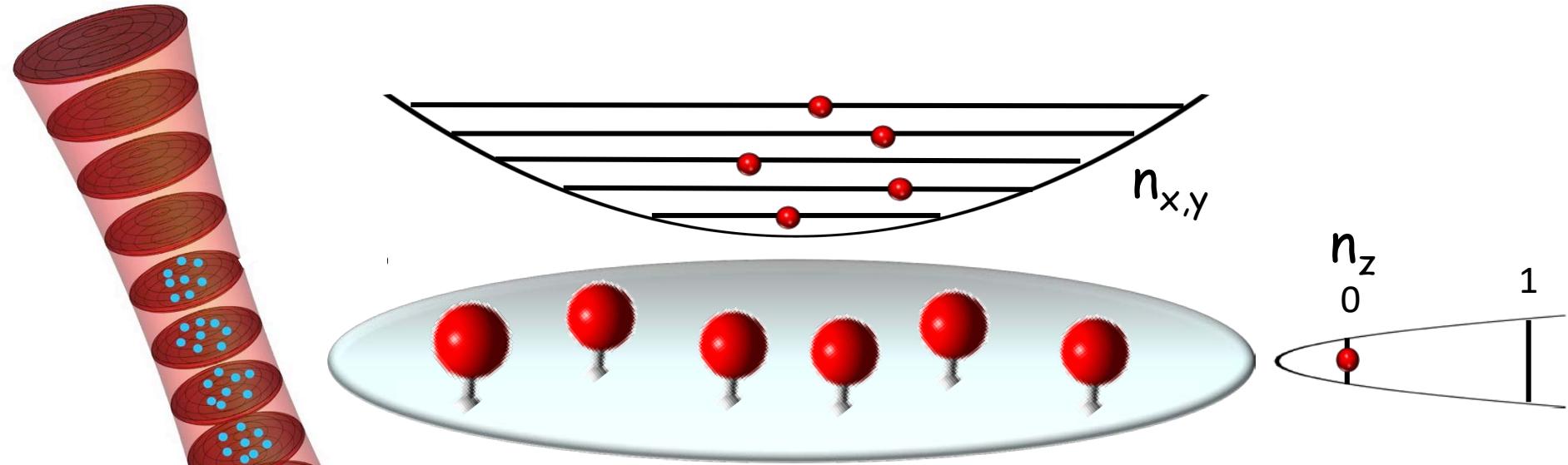
OR

$$\left( \begin{array}{c} |n m\rangle + |m n\rangle \\ |n m\rangle - |m n\rangle \end{array} \right)$$

OR

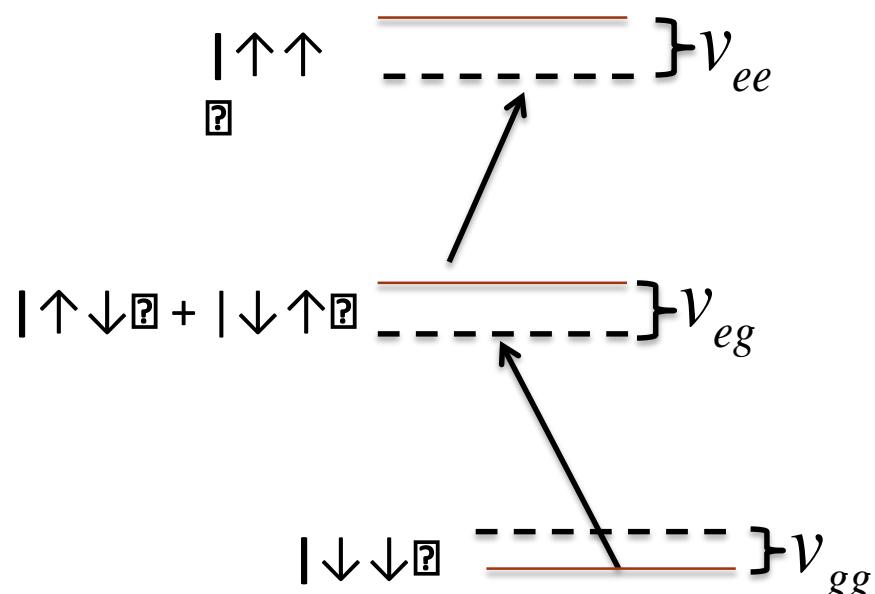
= “—”

# Interactions between Fermions



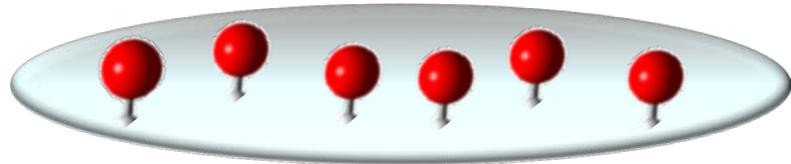
$$|\uparrow\downarrow\Psi\rangle + |\downarrow\uparrow\Psi\rangle \otimes \begin{matrix} |n_1 n_2\Psi\rangle - |n_2 \\ n_1\Psi\rangle \end{matrix}$$

*p - wave interaction*



# 1D lattice clock: spin model

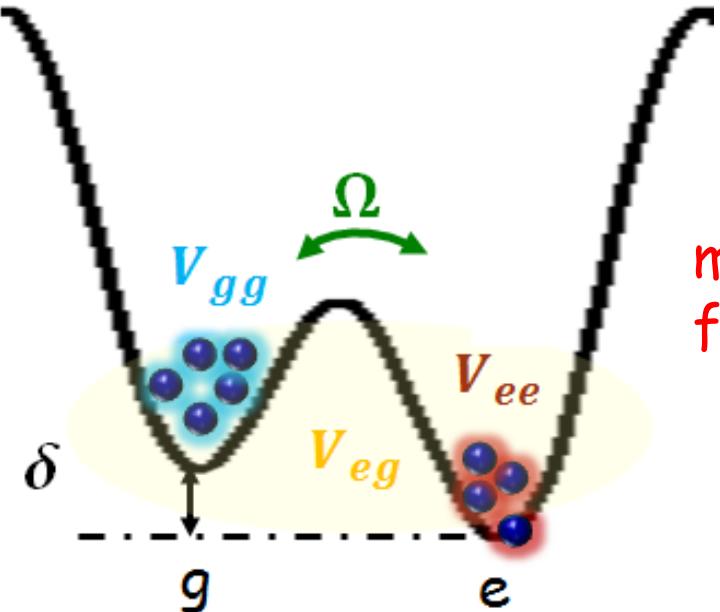
Collective-spin  $S = N/2$



$$\hat{H}/\hbar = -\delta S^z - \Omega S^x + \chi (S^z)^2 + C(N-1) S^z$$

$$C = \frac{\nu_{ee} - \nu_{gg}}{2}$$

$$\chi = \frac{\nu_{ee} + \nu_{gg} - 2\nu_{eg}}{2}$$



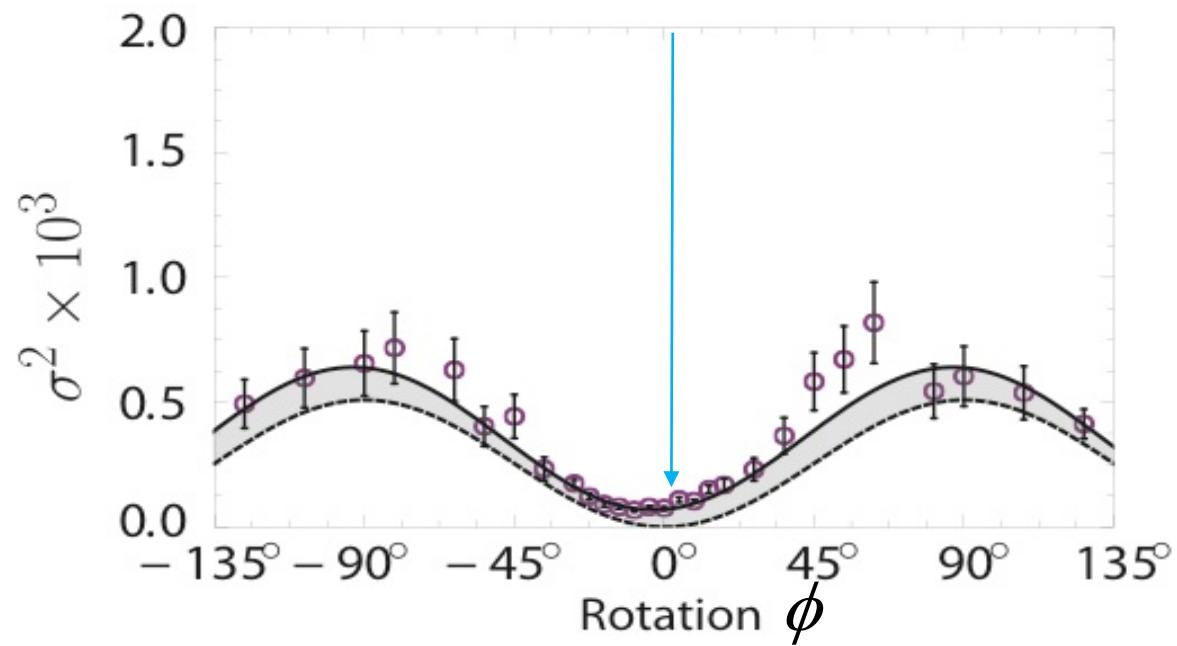
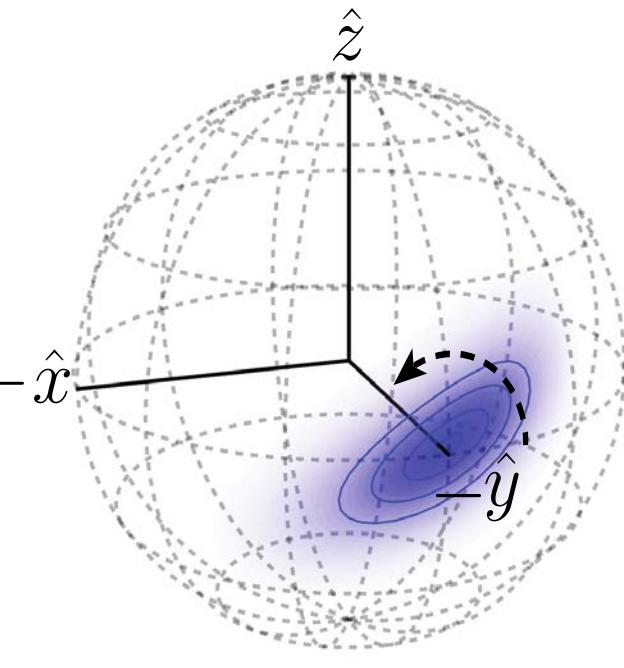
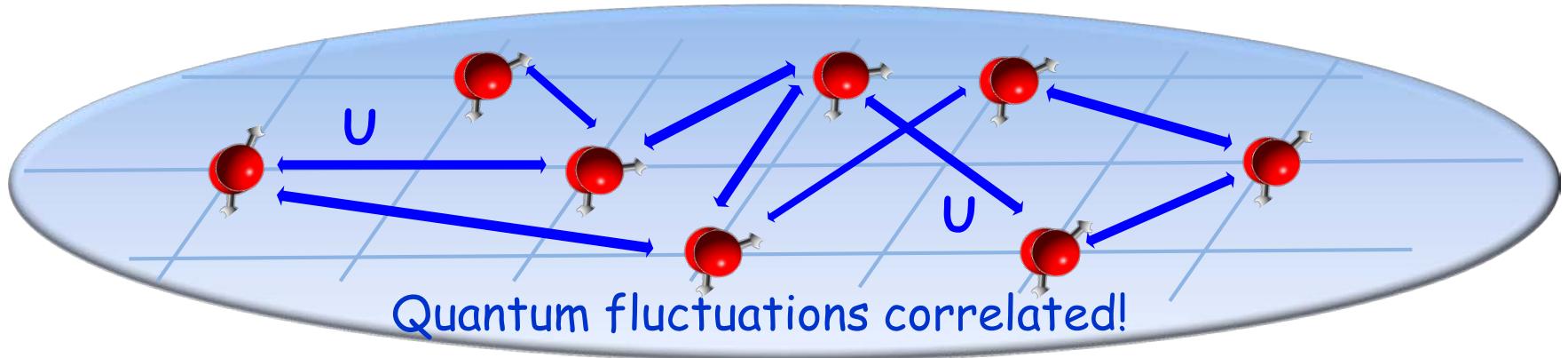
mapping interacting  
fermions to bosons

Two-component BEC:  
Sorensen, Moller, Cirac, Zoller, Lewenstein, ...

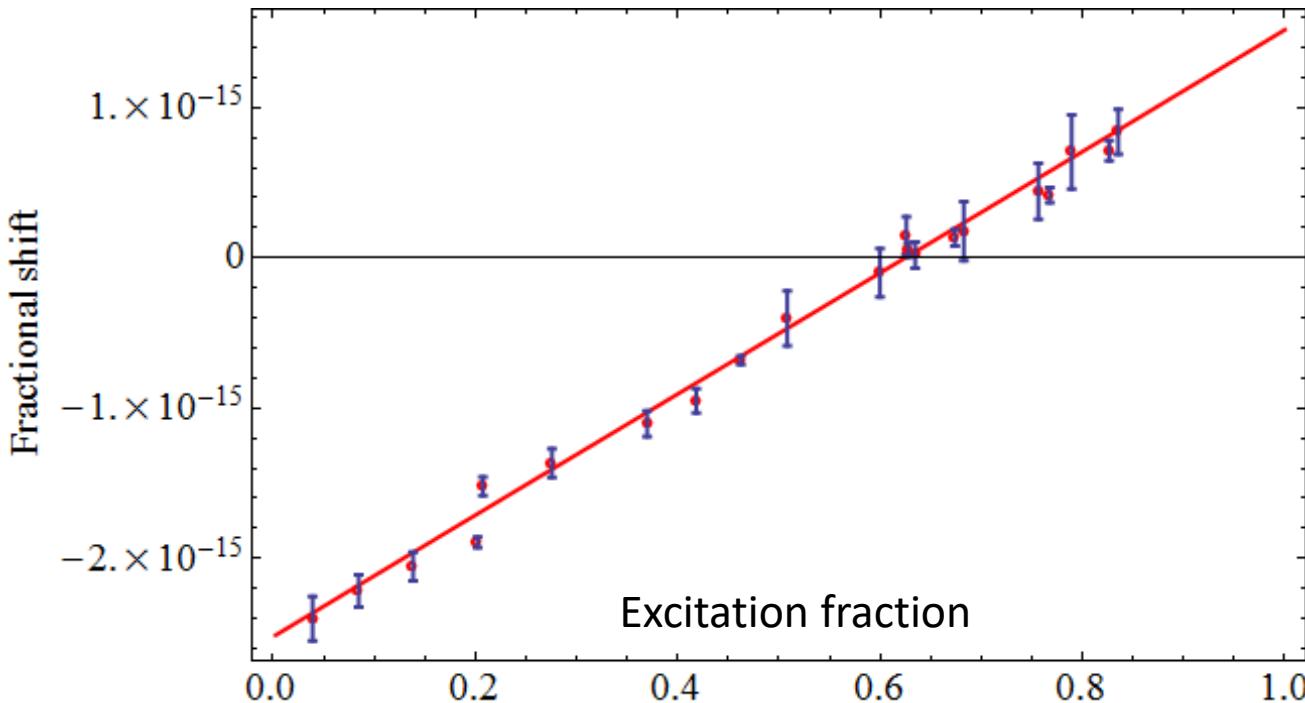
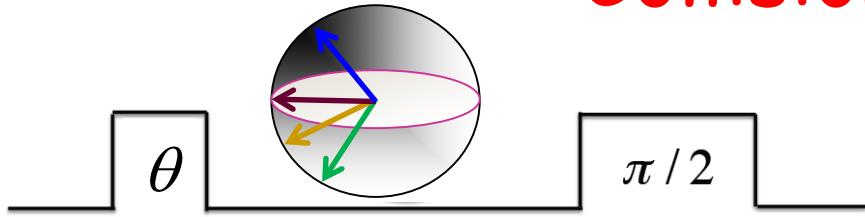
# Clock probes many-body spin dynamics

Martin et al., Science **341**, 632 (2013).

$$\hat{H}/\hbar = \chi (S^z)^2 + C(N - 1) S^z$$



# Collisional frequency shift



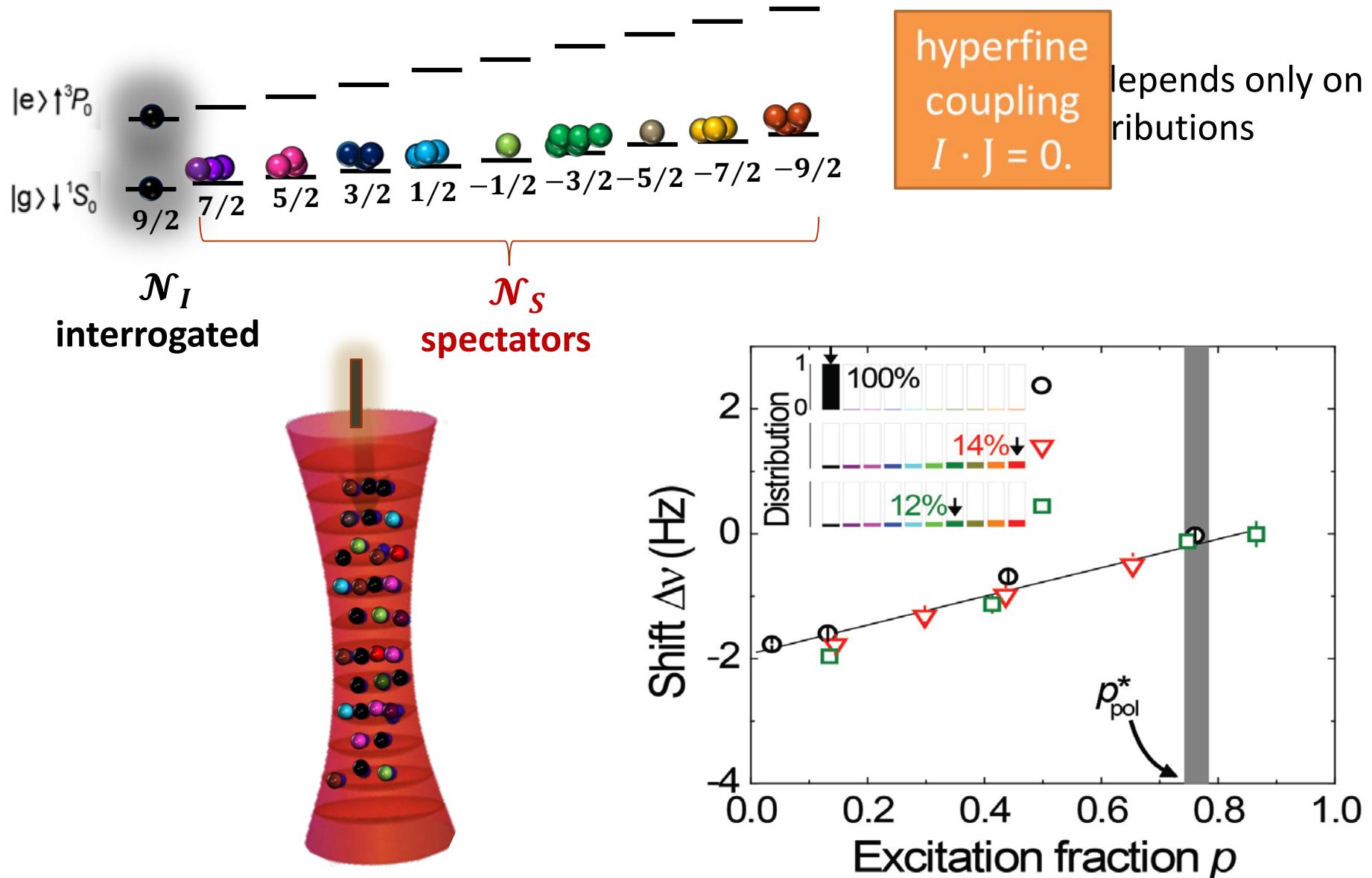
$$\frac{V_{ee} - V_{gg}}{V_{eg} - V_{gg}} = 0.4$$

Collisional shift has a linear dependence on  $S_z = \cos(\theta)$ .

$$\Delta v = H / S_z \sim \frac{V_{ee} - V_{gg}}{2} + C \cos(\theta) \left[ \frac{2V_{eg} - V_{ee} - V_{gg}}{2} \right] \chi$$

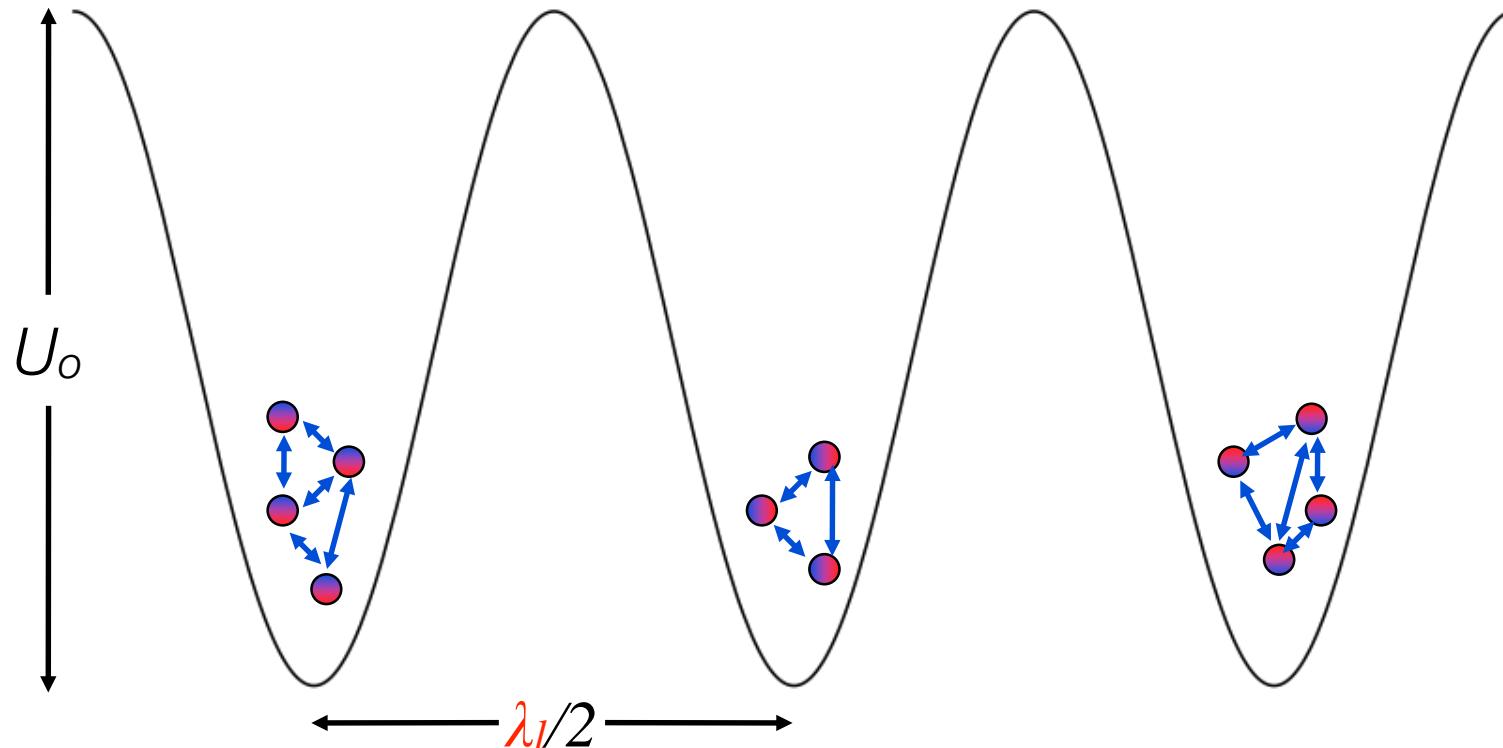
# Density shifts & SU( $N$ ) symmetry

Zhang et al., Science 345, 1467 (2014). Fallani (2014); Fölling (2014)



# So far, interactions in a single pancake

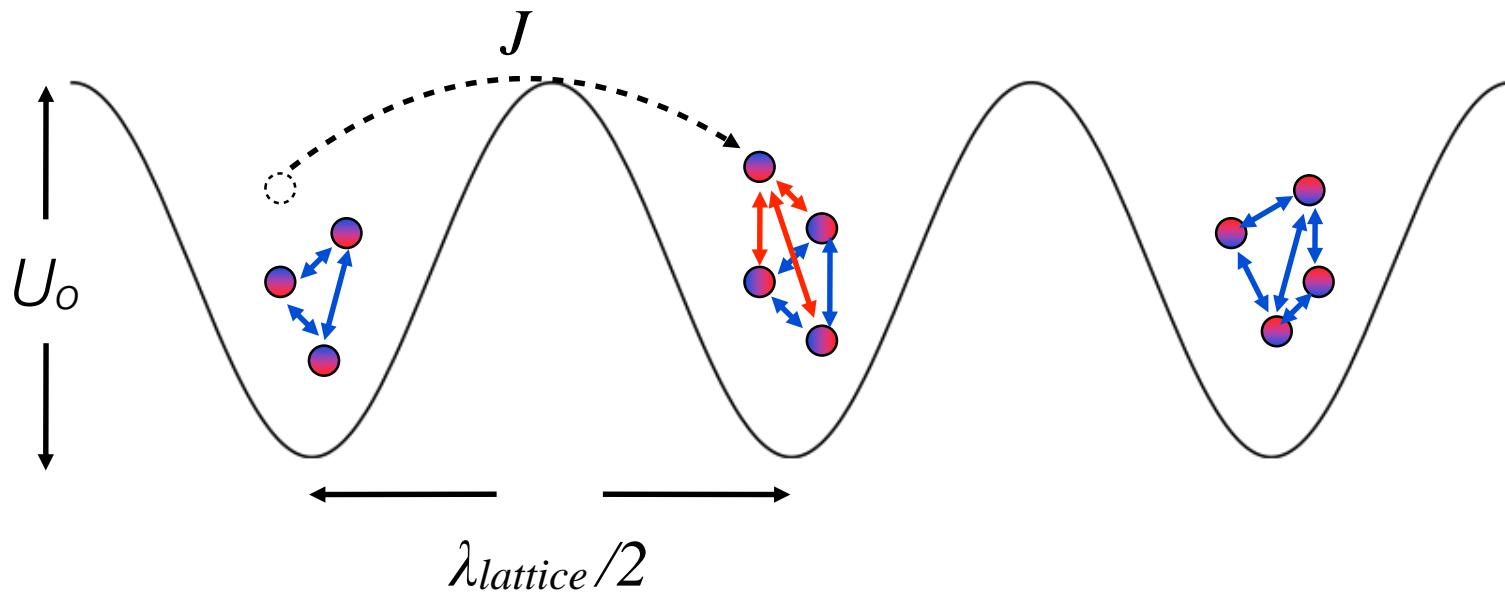
- Identical fermions,  $p$ -wave dominates
- Multiple nuclear spins,  $s$ - and  $p$ -waves under  $SU(N)$



$U_0 \gg E_R$  : Tunneling negligible

# A new regime for interactions

... when tunneling is allowed.



# Quantum simulation wishlist

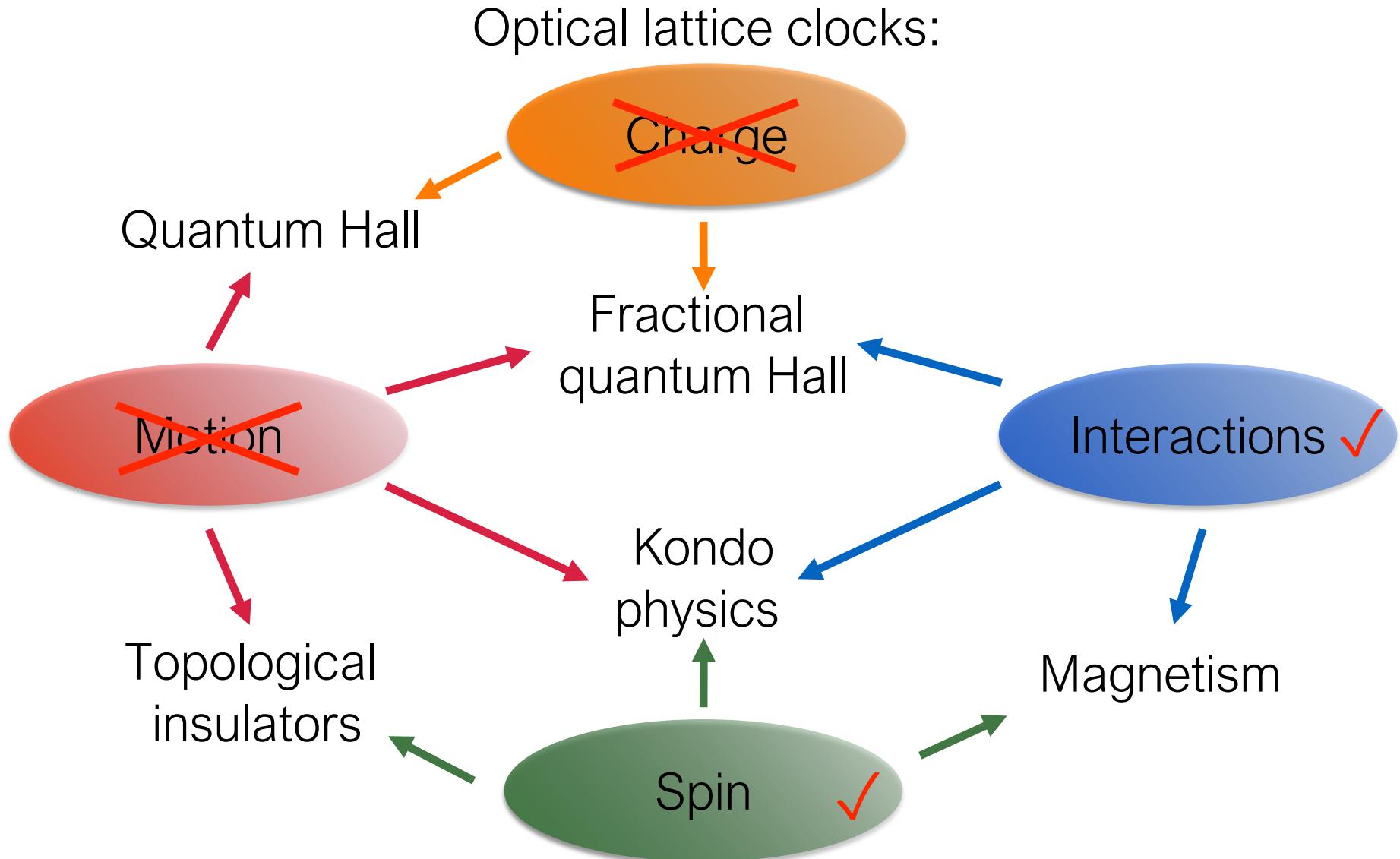
Charge

Motion

Interactions

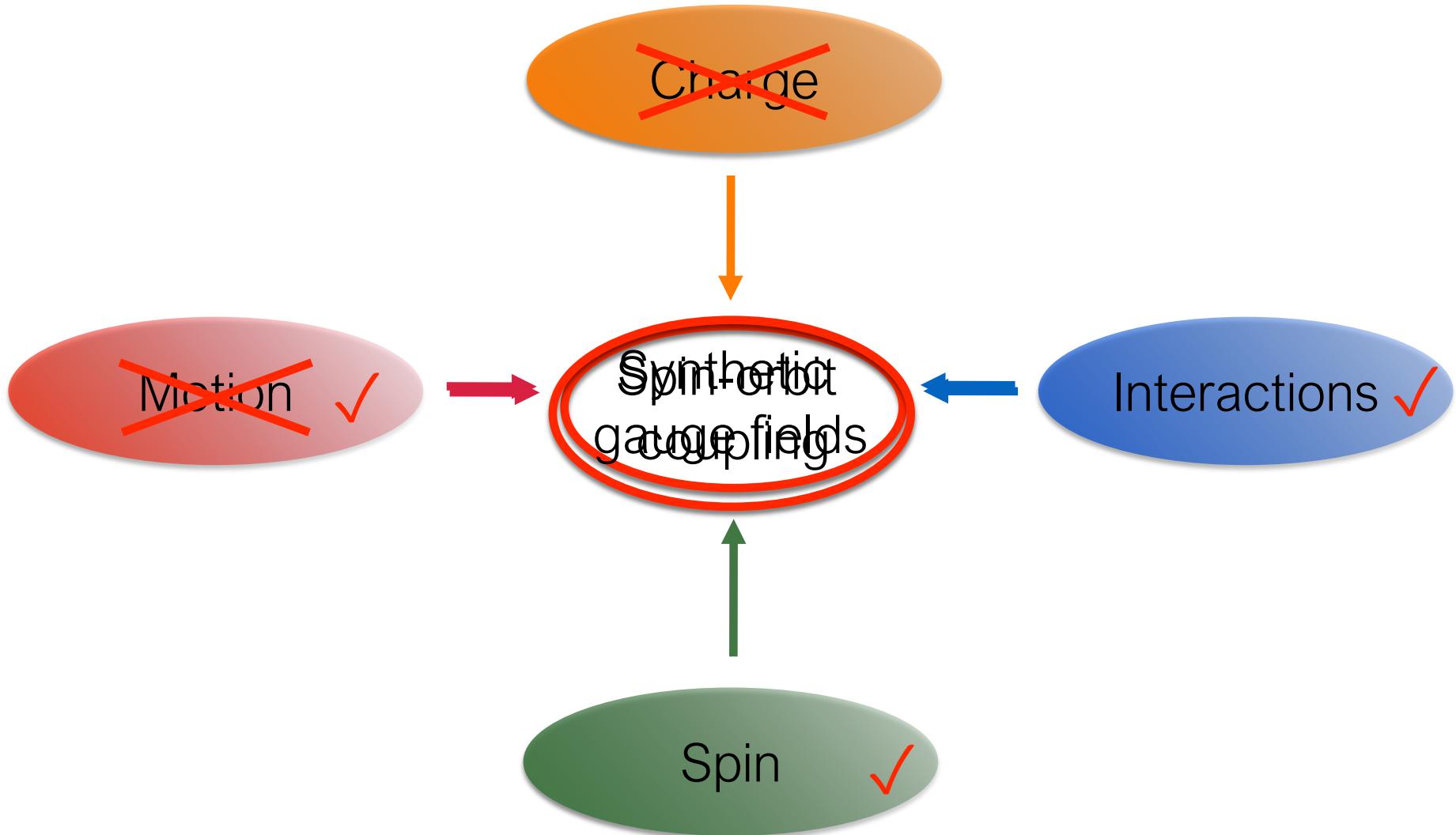
Spin

# Quantum simulation wishlist



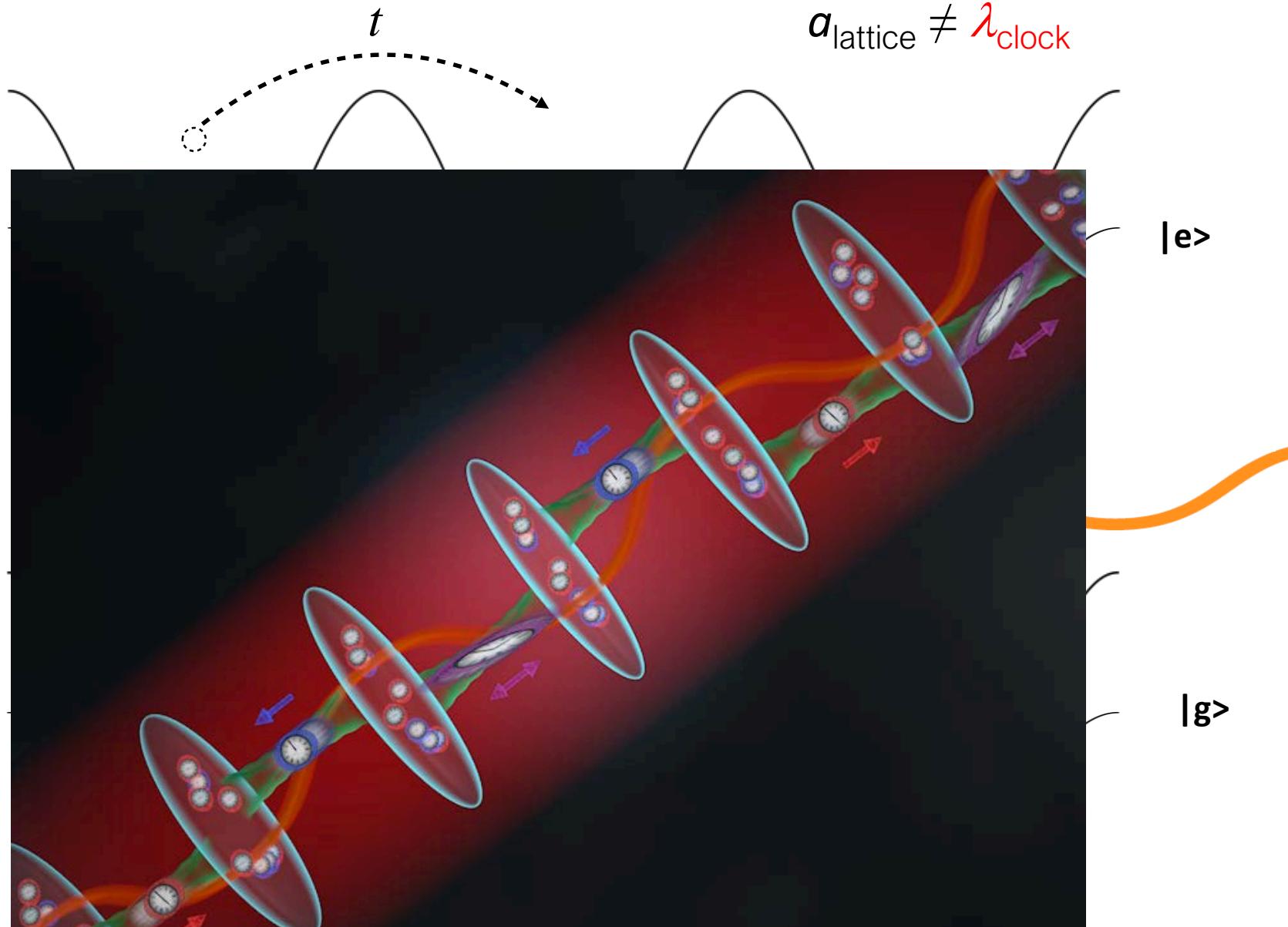
# Quantum simulation wishlist

Optical lattice clocks:

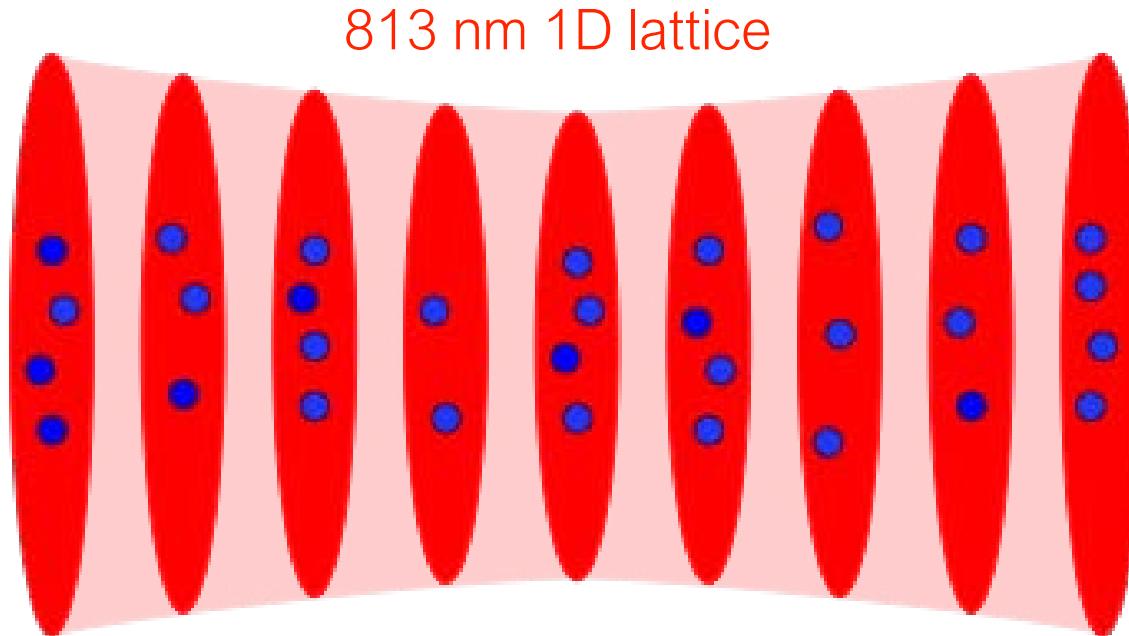


# Spin-orbit coupled fermion interactions

Kolkowitz *et al.*, Nature **542**, 66 (2017); Bromley *et al.*, Nature Phys. (2018).



# Synthetic magnetic field in the clock



1

2

3

4

5

6

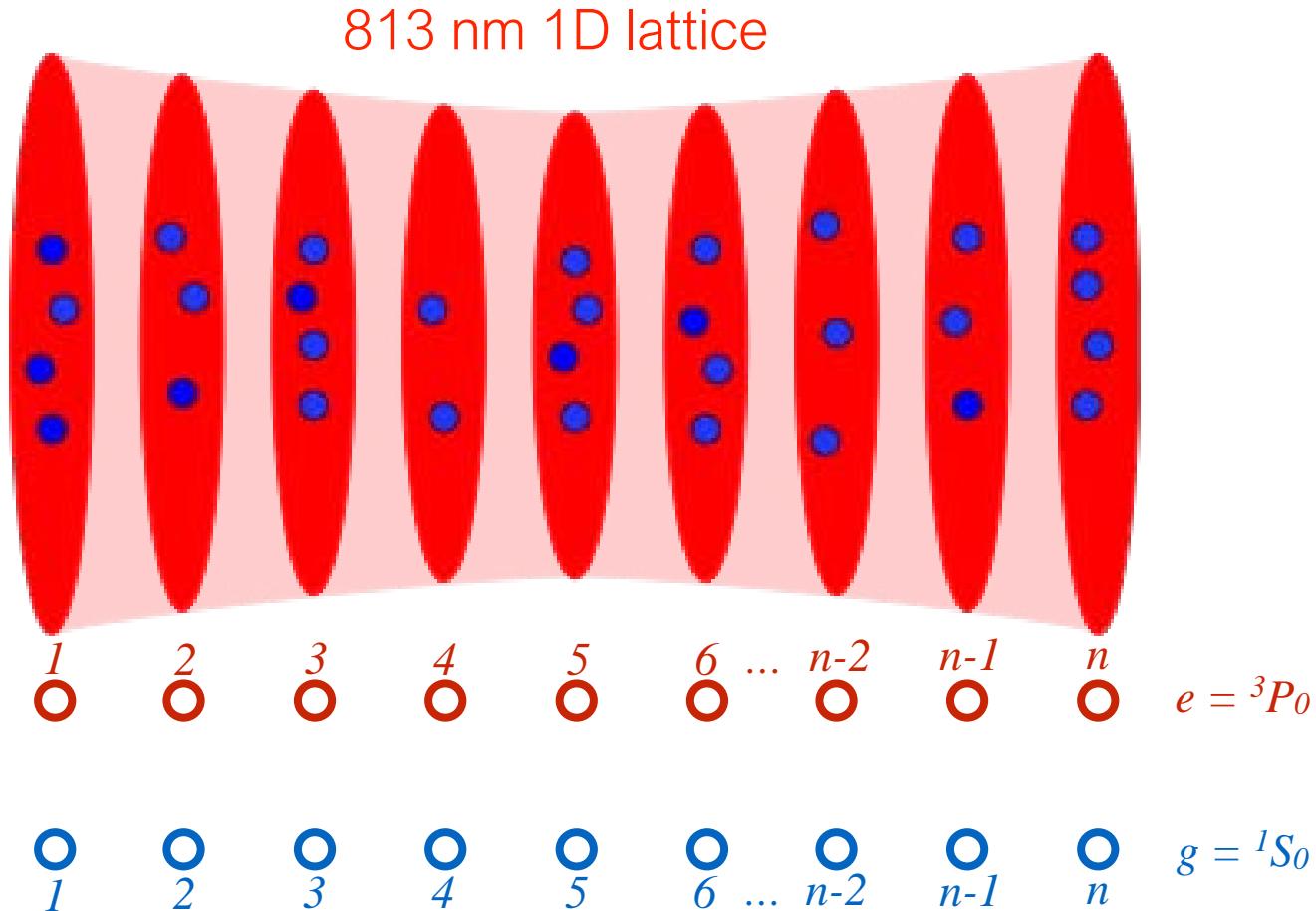
...

n-2

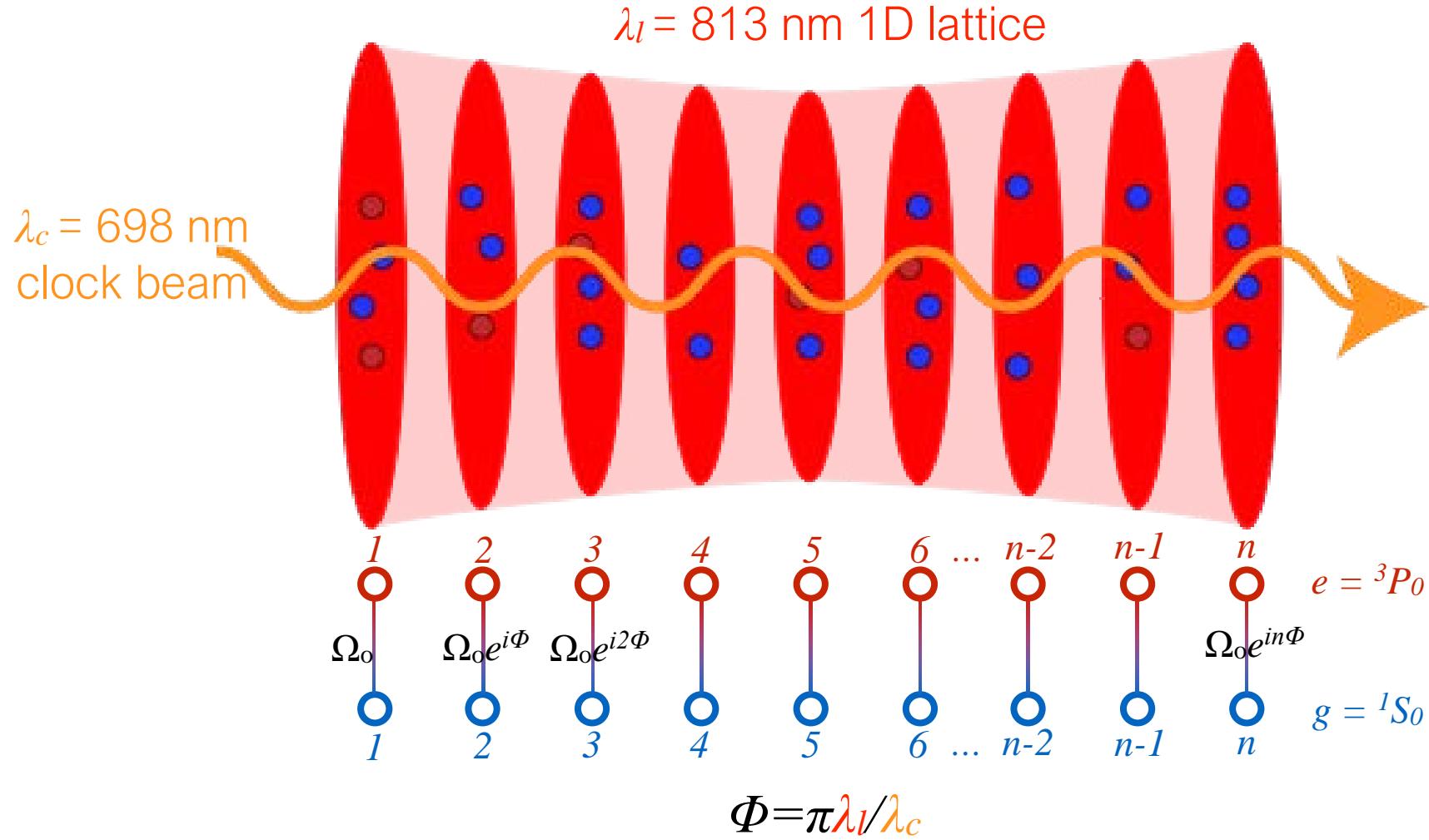
n-1

n

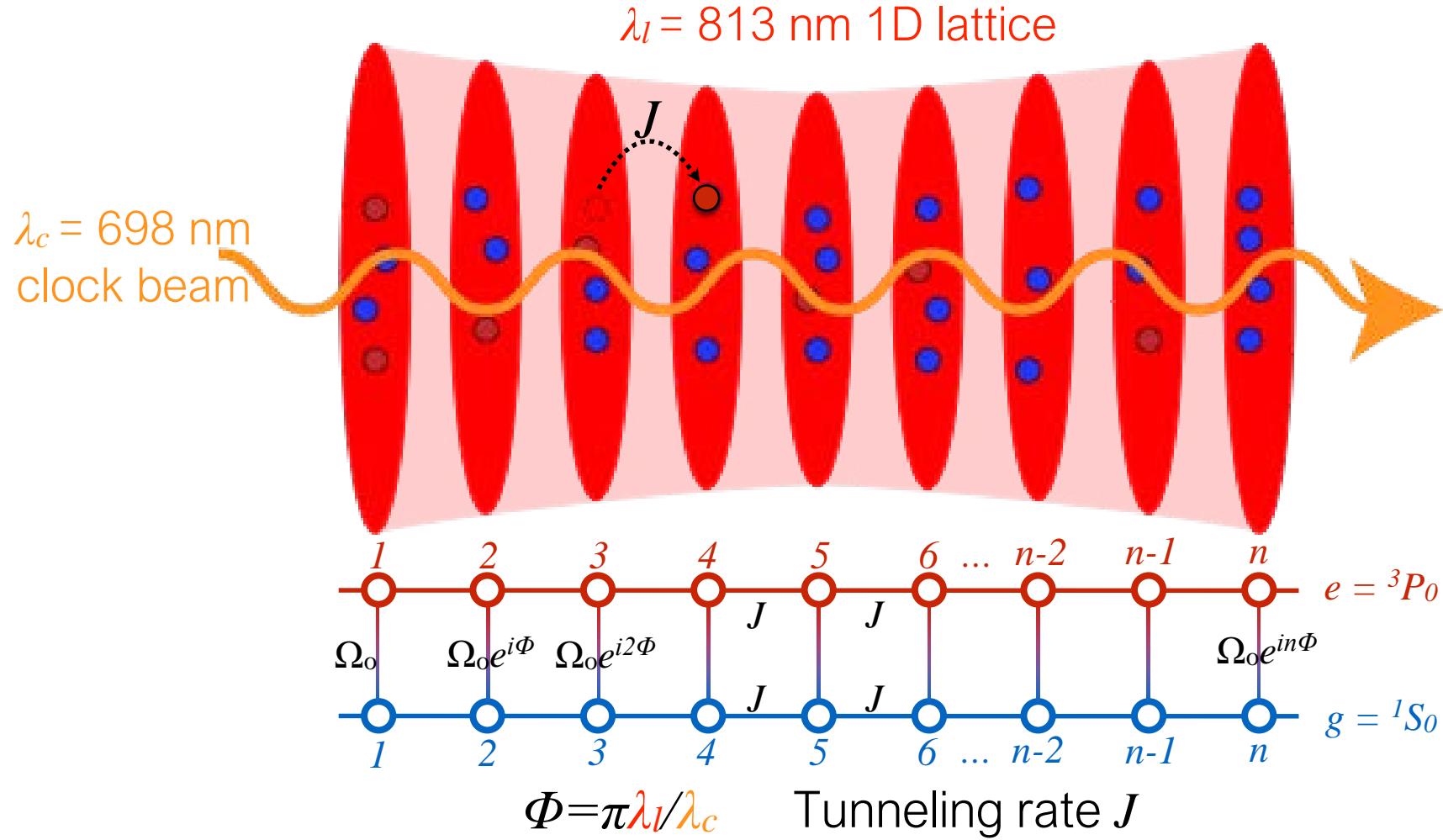
# Synthetic magnetic field in the clock



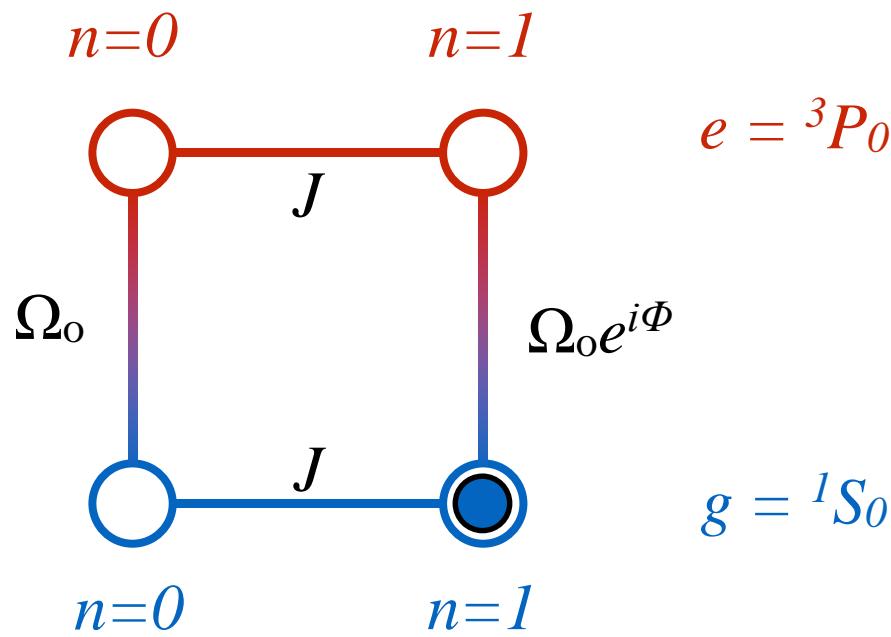
# Synthetic magnetic field in the clock



# Synthetic magnetic field in the clock

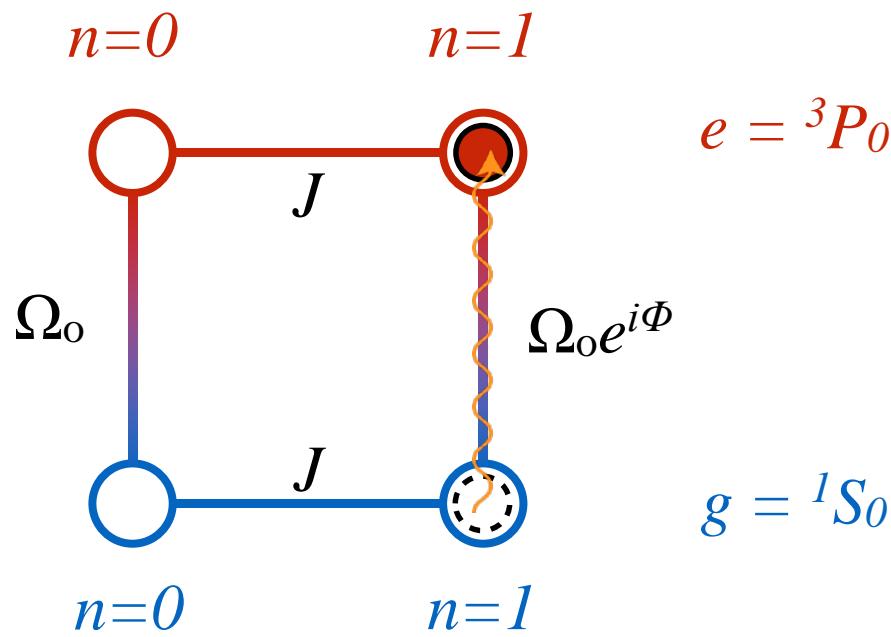


# Synthetic magnetic field in the clock



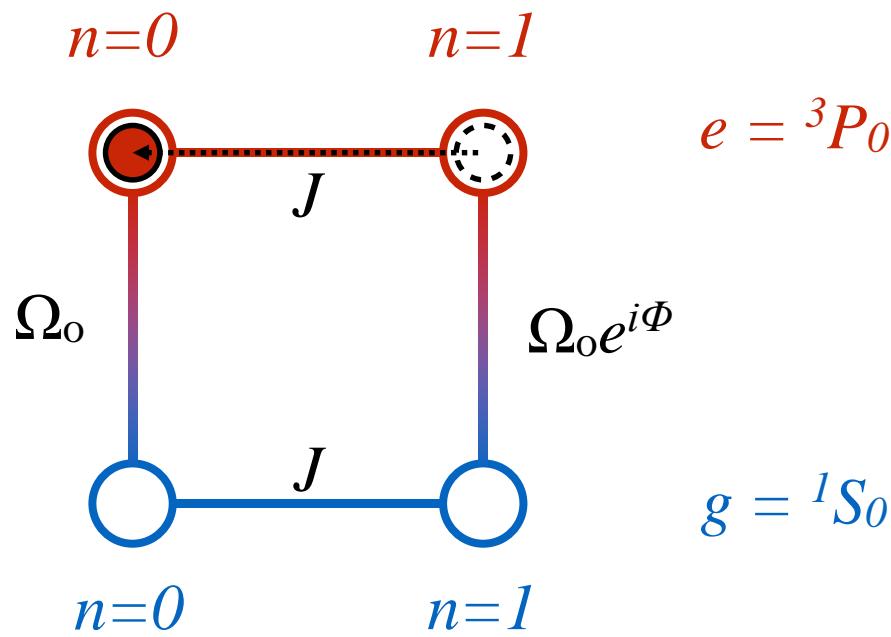
$$\psi_o = |1, g\rangle$$

# Synthetic magnetic field in the clock



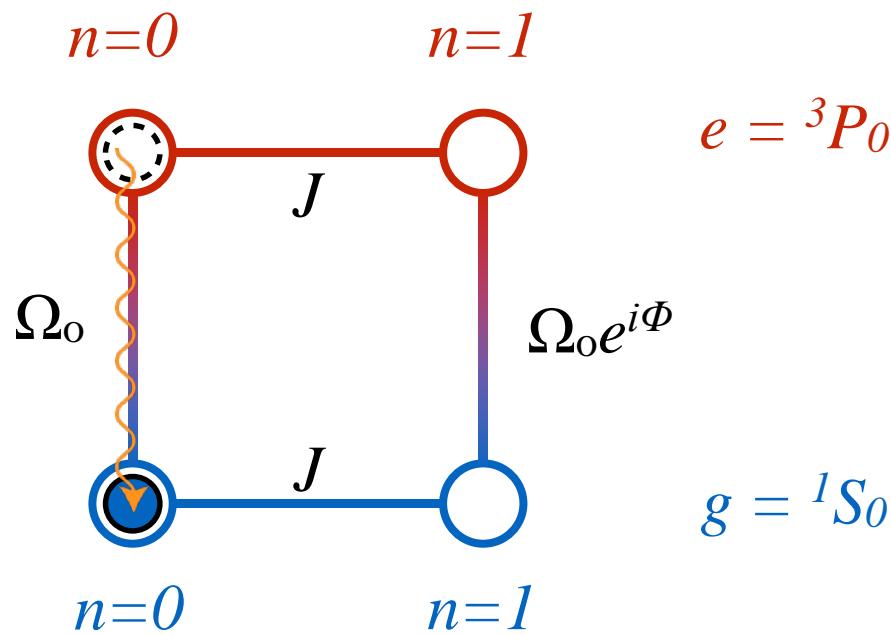
$$\psi_1 = e^{i\phi} |1, e\rangle$$

# Synthetic magnetic field in the clock



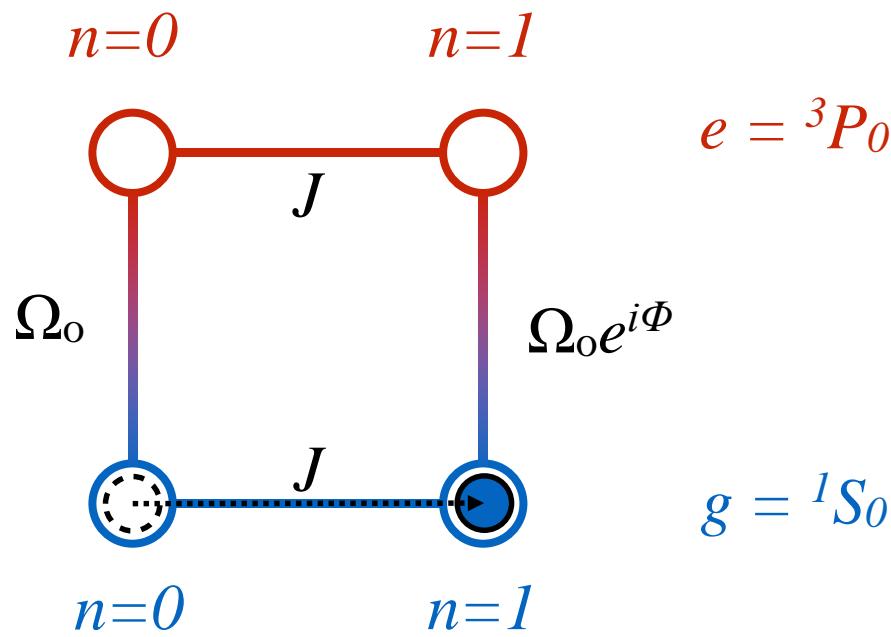
$$\psi_2 = e^{i\phi} |0, e\rangle$$

# Synthetic magnetic field in the clock



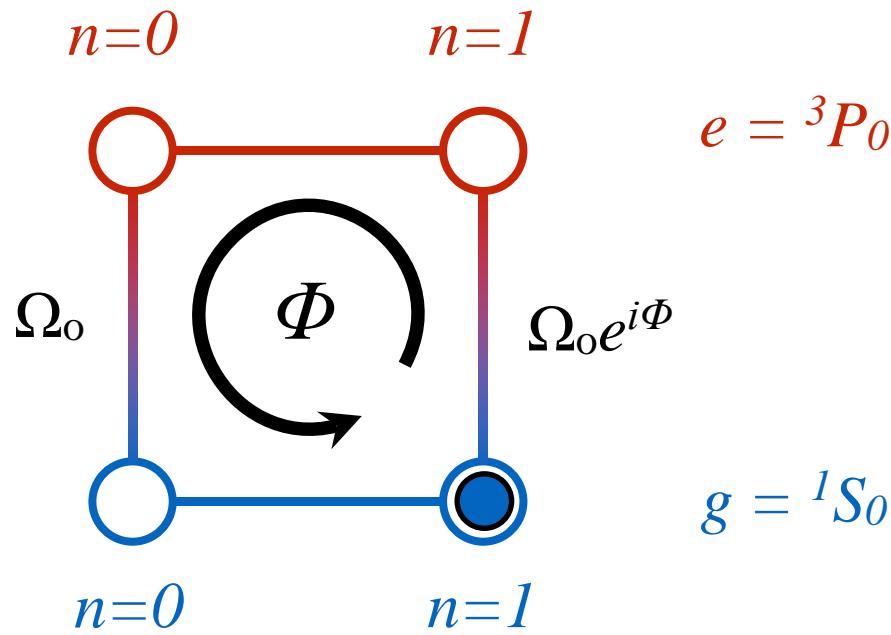
$$\psi_3 = e^{i\phi} |0,g\rangle$$

# Synthetic magnetic field in the clock



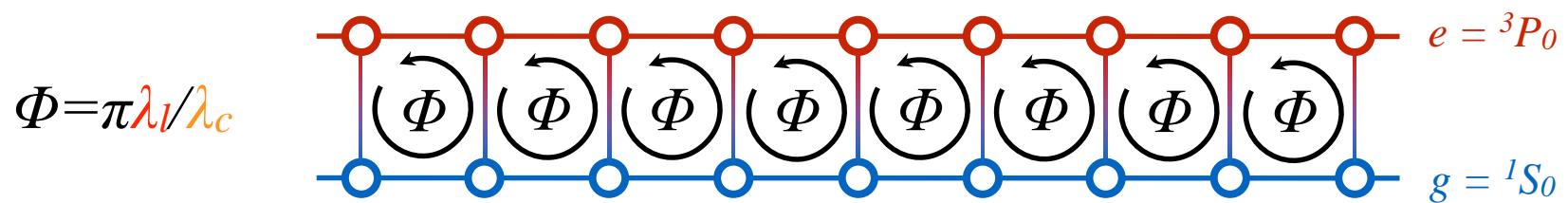
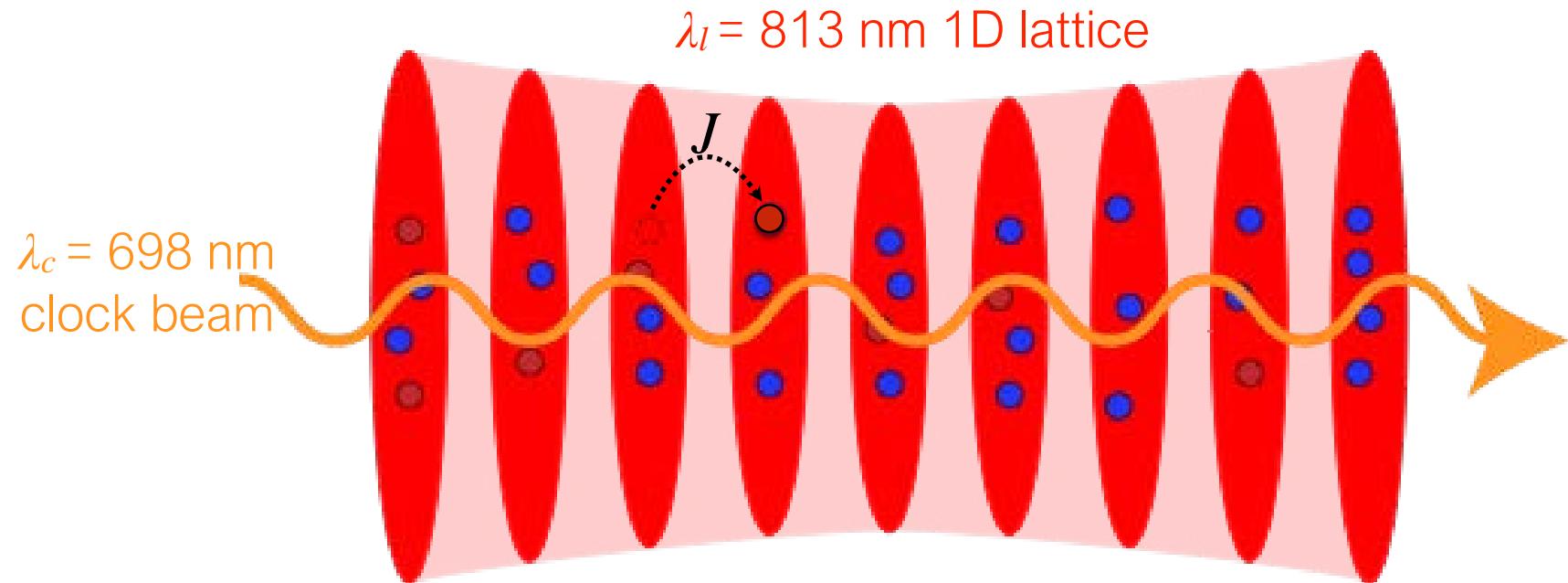
$$\psi_f = e^{i\phi} |1, g\rangle$$

# Synthetic magnetic field in the clock

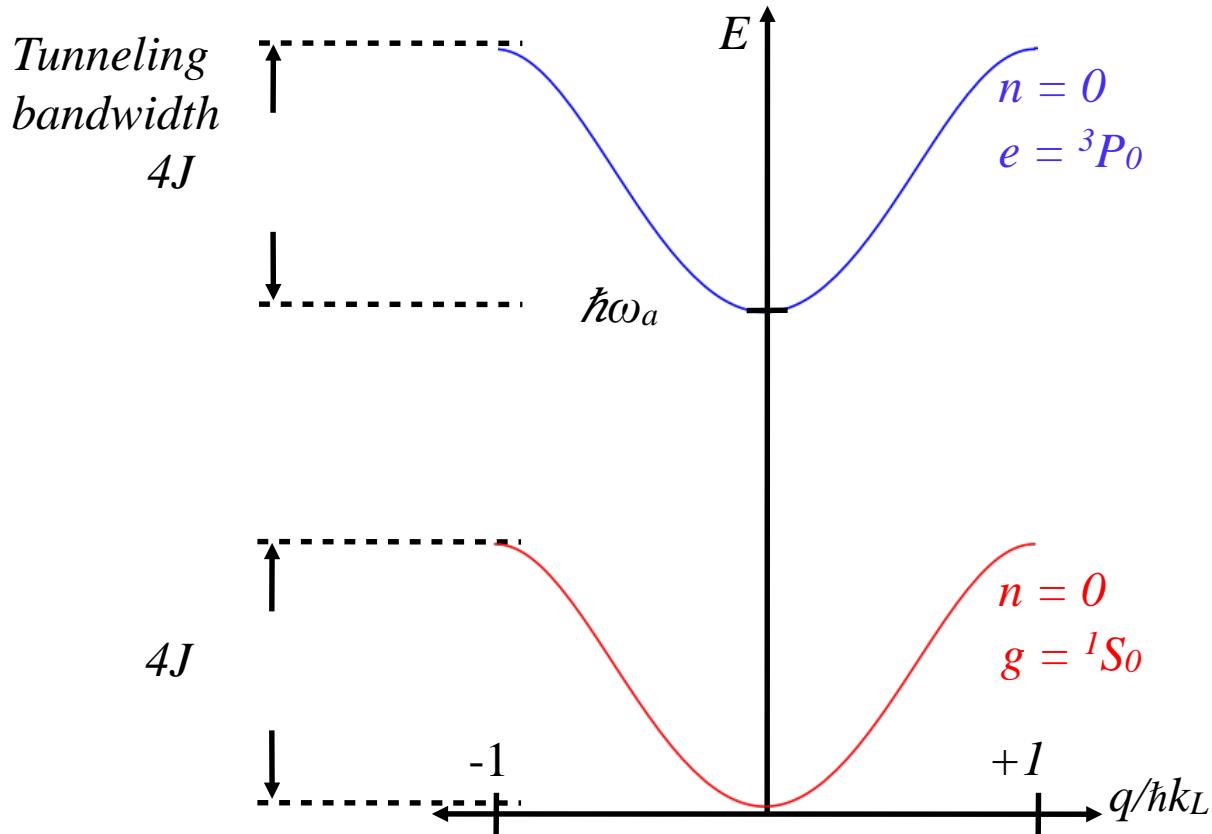


$$\psi_f = e^{i\phi} \psi_o$$

# Synthetic magnetic field in the clock

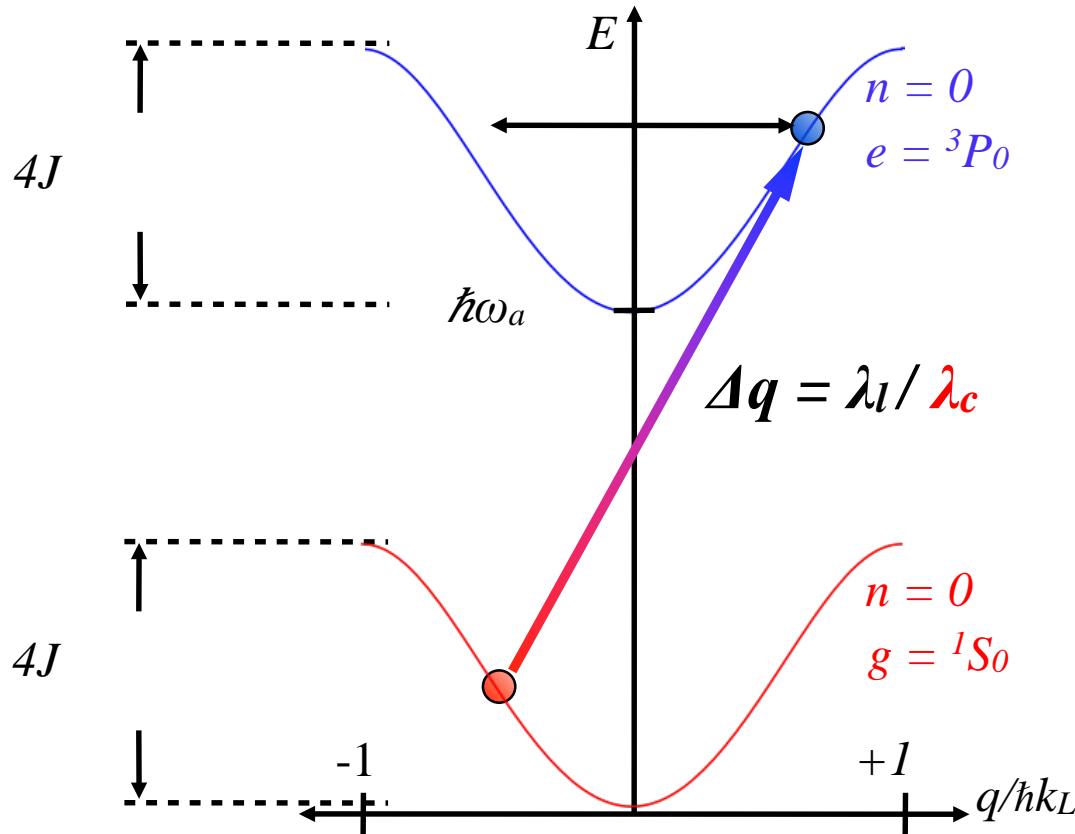


# Spin-orbit coupling



# Spin-orbit coupling

Kolkowitz *et al.*, Nature **542**, 66 (2017).

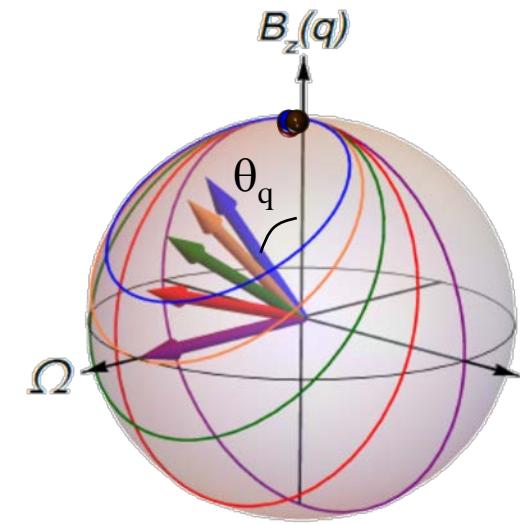
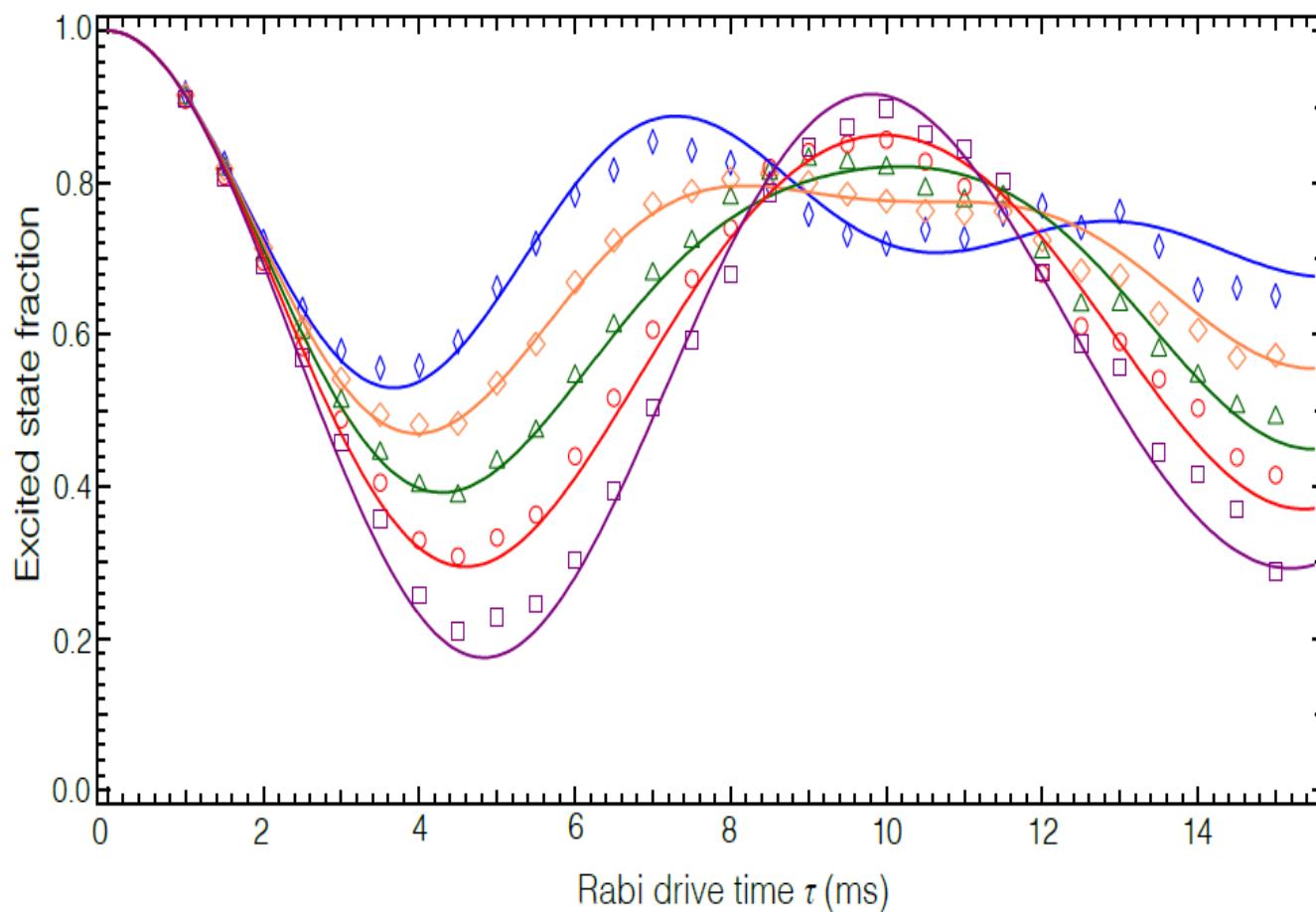


# Spin-orbit coupling

Kolkowitz *et al.*, Nature 542, 66 (2017).

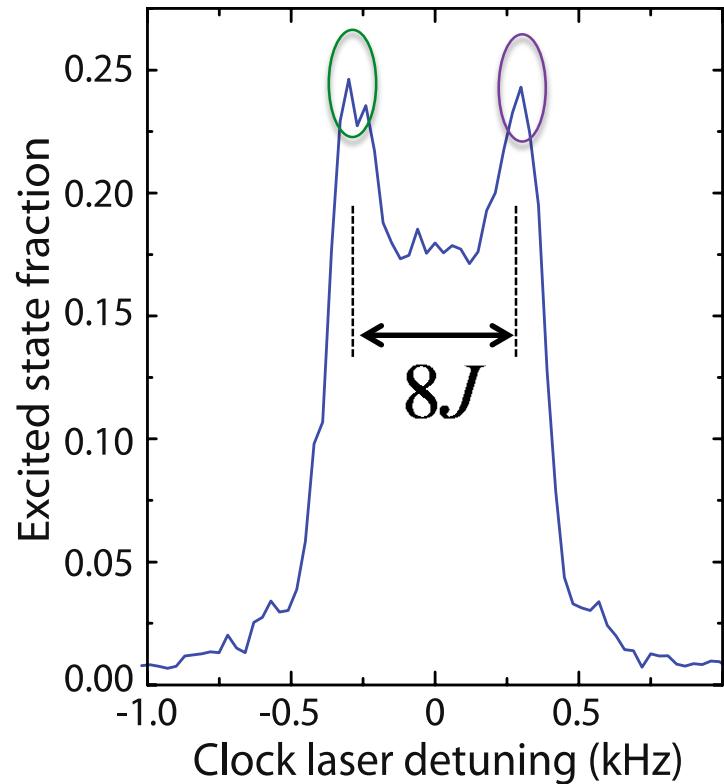
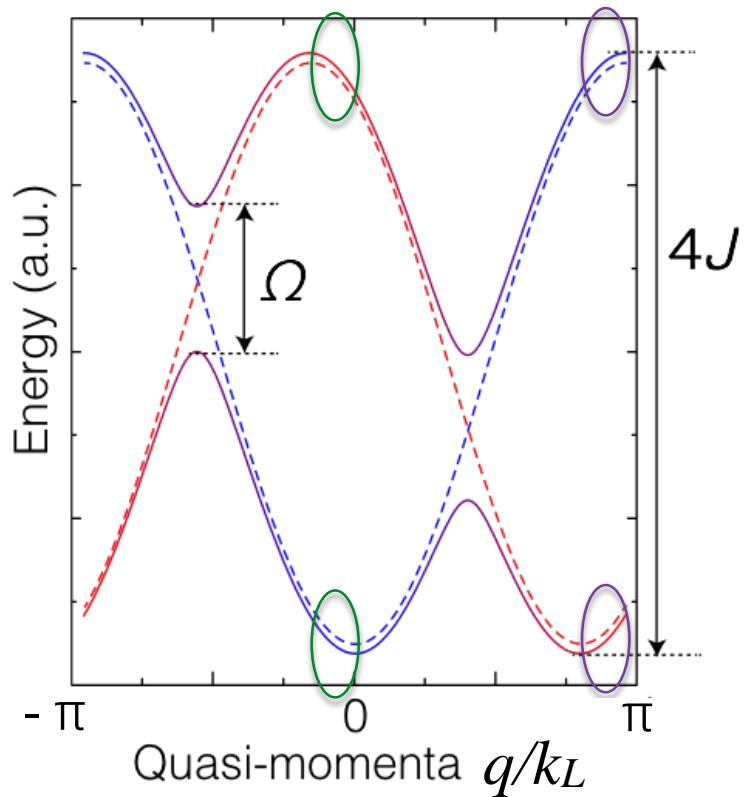
$$H_q = -\Omega S^x - (\Delta E(q) + \delta) S^z = \vec{B}_{eff}(q, \delta) \cdot \hat{S}$$

$$\Delta E(q) = -J [\cos(\pi q/k_L + \Phi) - \cos(\pi q/k_L)]$$



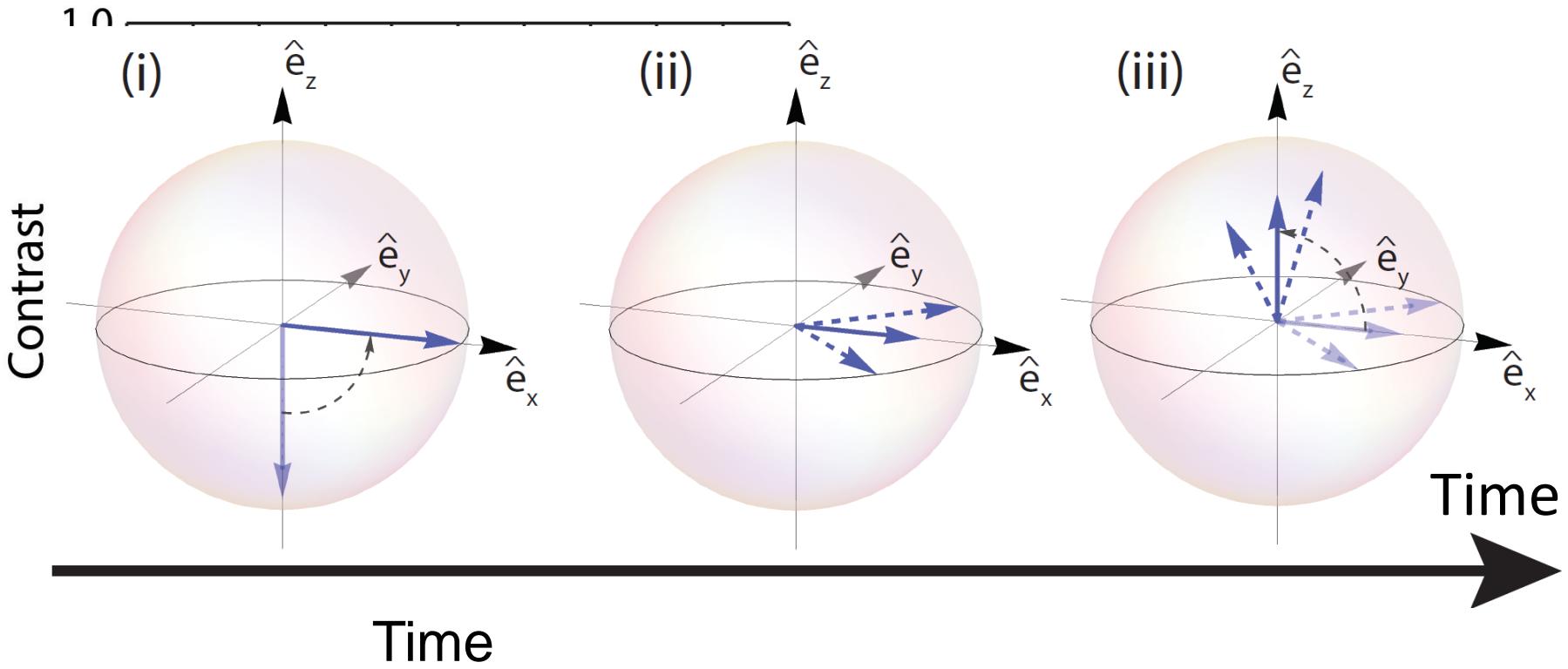
Spin-motion locking:  $\vec{B}(q_i) \cdot \vec{s}_i$

# Spin-orbit coupled band structure



Density of states diverge at  $dE/dk = 0$  :  
van Hove singularities

# Interacting fermions under SOC



$$\begin{aligned}\hat{H}/\hbar = & \quad \vec{B}(q_i) \cdot \vec{s}_i \\ & + \chi (S^z)^2 + C(N-1) S^z \\ & + \xi \vec{S} \cdot \vec{S}\end{aligned}$$

# 3D Fermi Insulator Clock

Scaling up the Sr quantum clock:

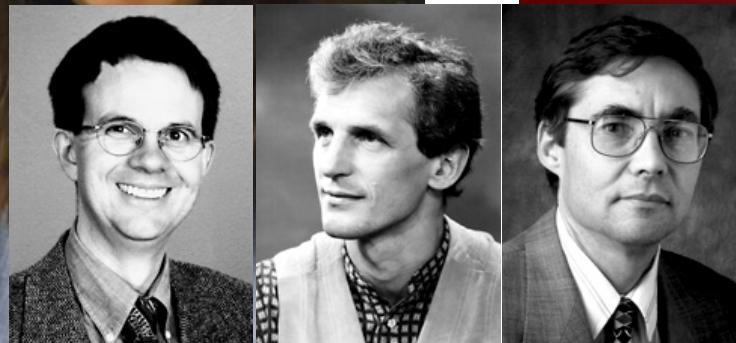
1 million atoms  
( $100 \times 100 \times 100$  cells)

Coherence 160 s

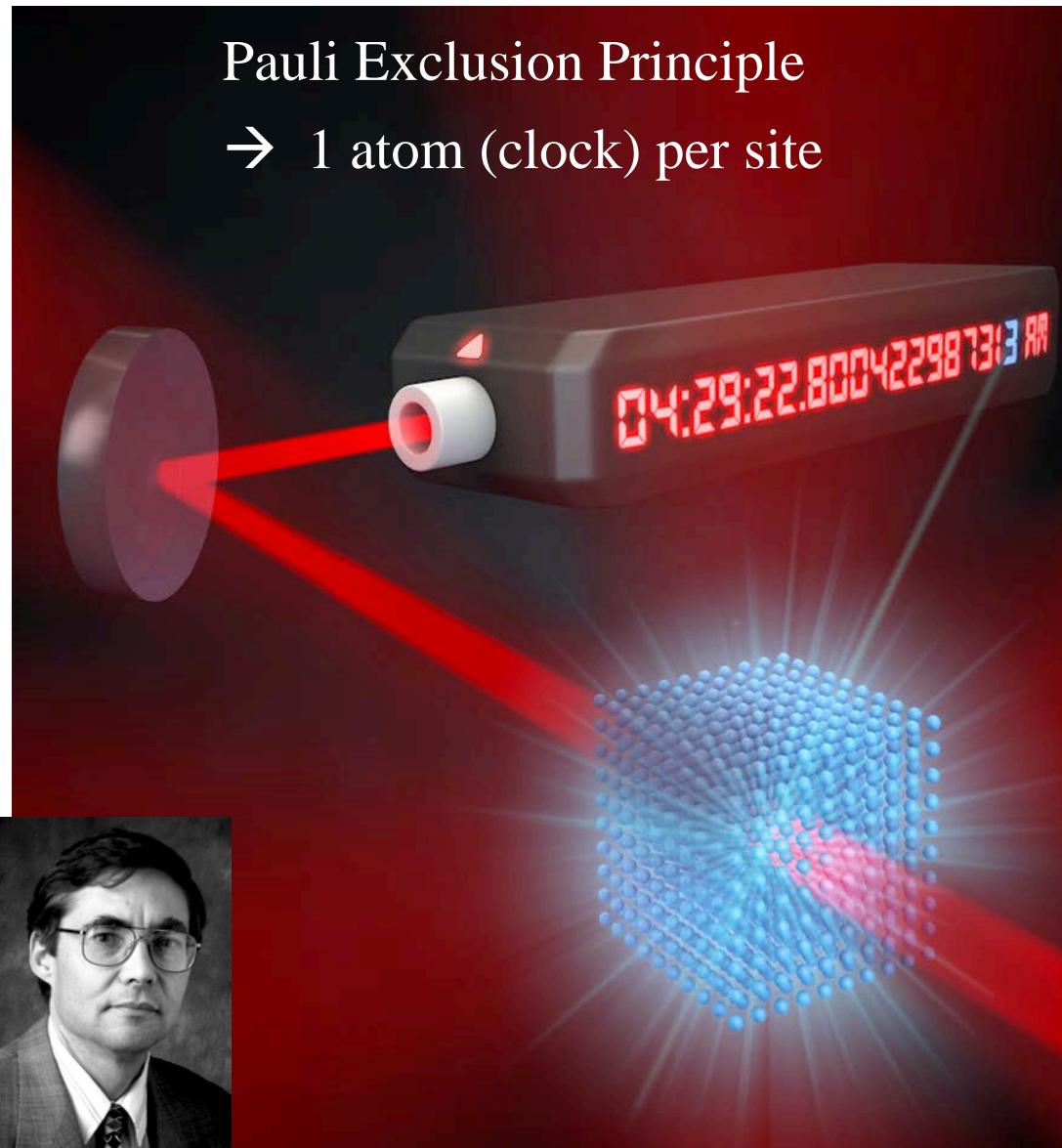
Precision  $3 \times 10^{-20} \text{ Hz}^{-1/2}$



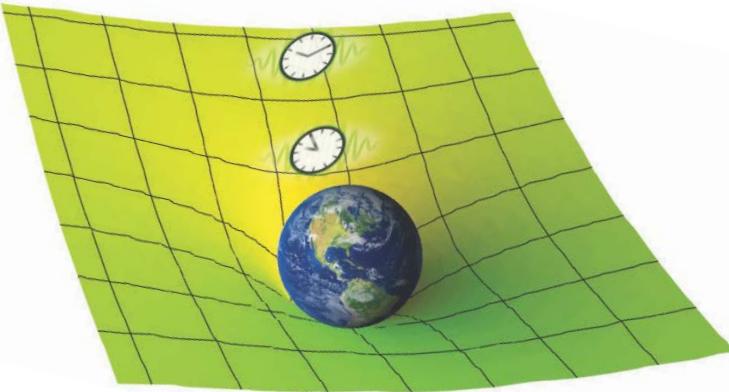
**Deborah Jin**  
(1968 – 2016)



Pauli Exclusion Principle  
→ 1 atom (clock) per site

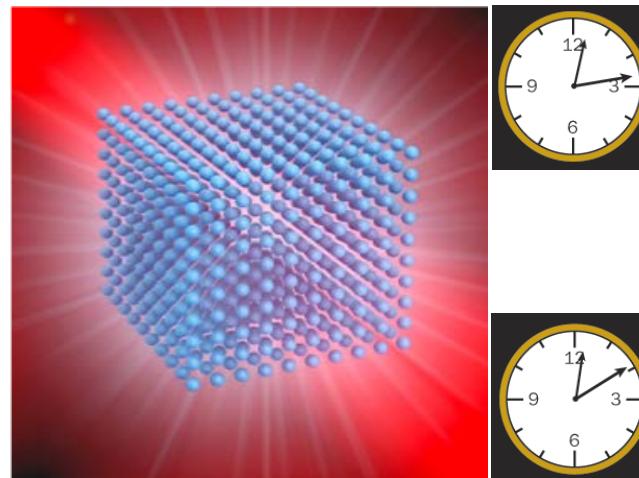


# Gravitational potential & gravity at once ?



Extreme spatial resolution & precision

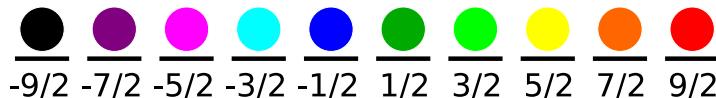
Jean Dalibard's grand challenge,  
Kastler Symposium 12/1/2016



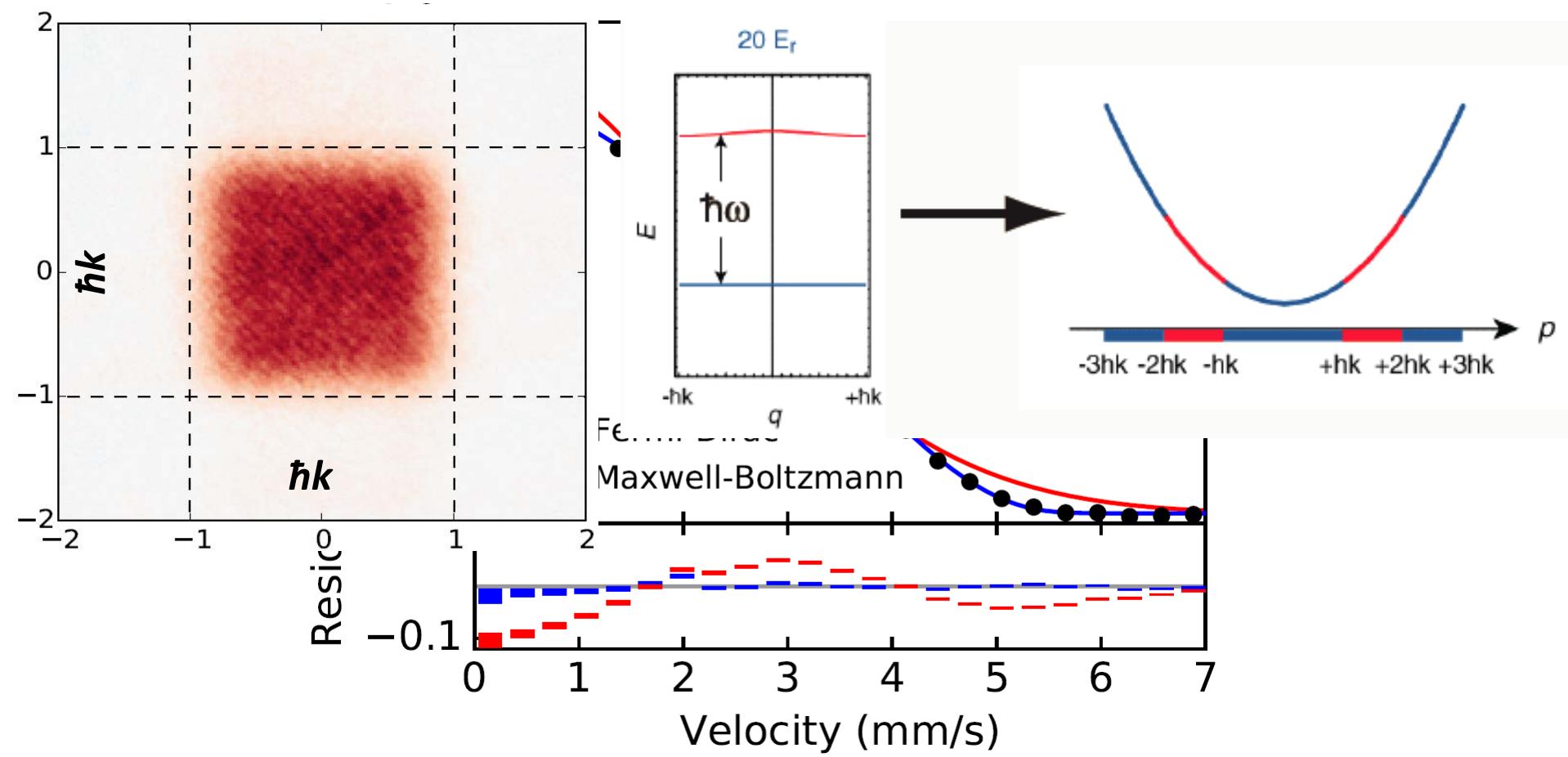
# Deeply Fermi degenerate

63,000  $^{87}\text{Sr}$  atoms (6,300 per nuclear spin state); 8.1 nK

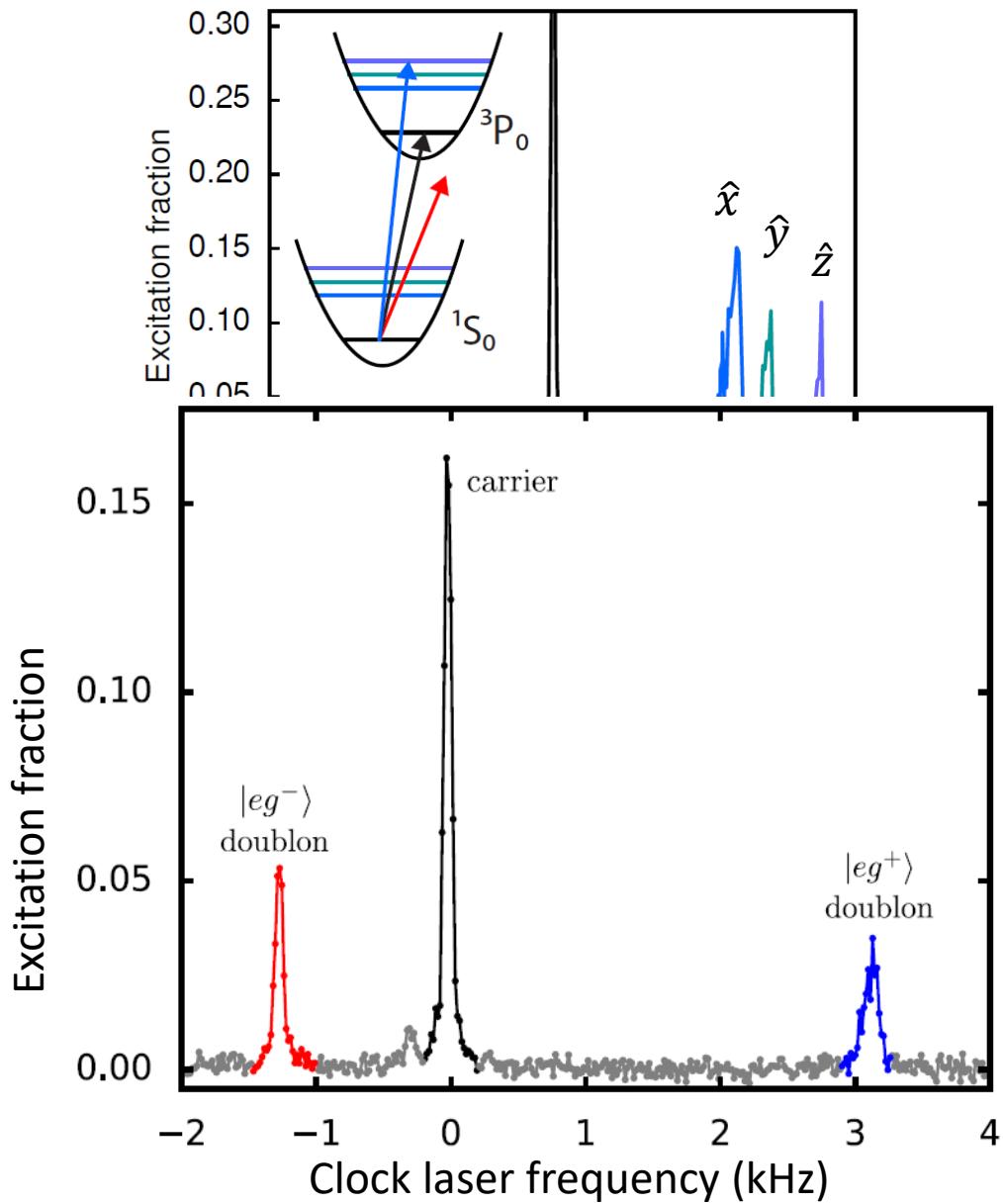
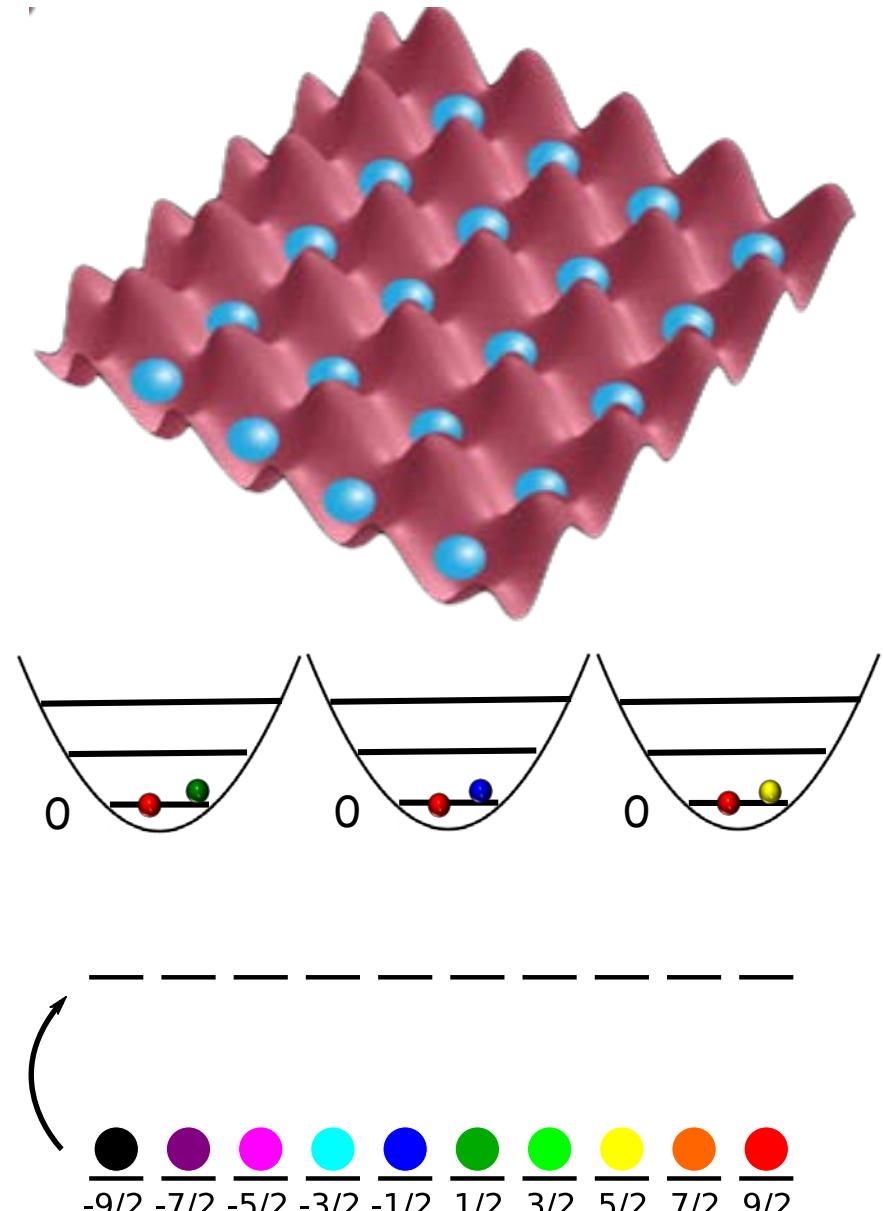
$$T/T_F = 0.05$$



$SU(N) \rightarrow$  same scattering length for all spin states

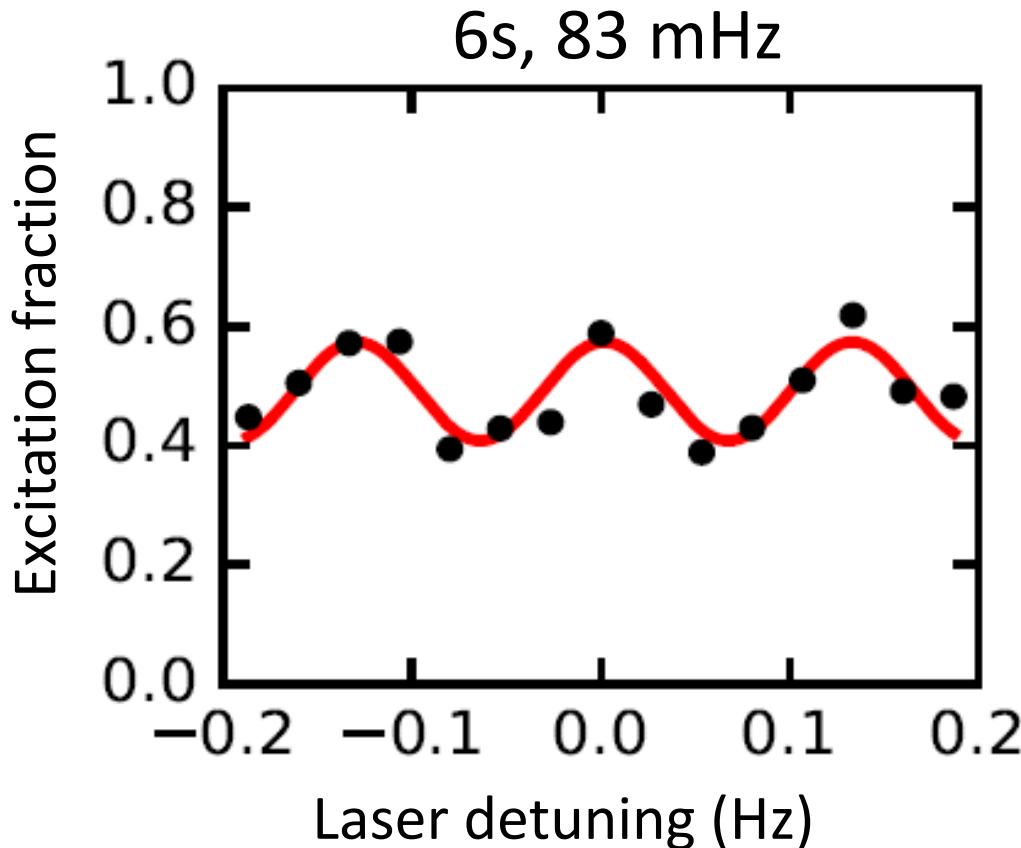


# A Fermi Gas Mott Insulator Clock



# Long atom-light coherence

S. Campbell *et al.*, Science **358**, 90 (2017).

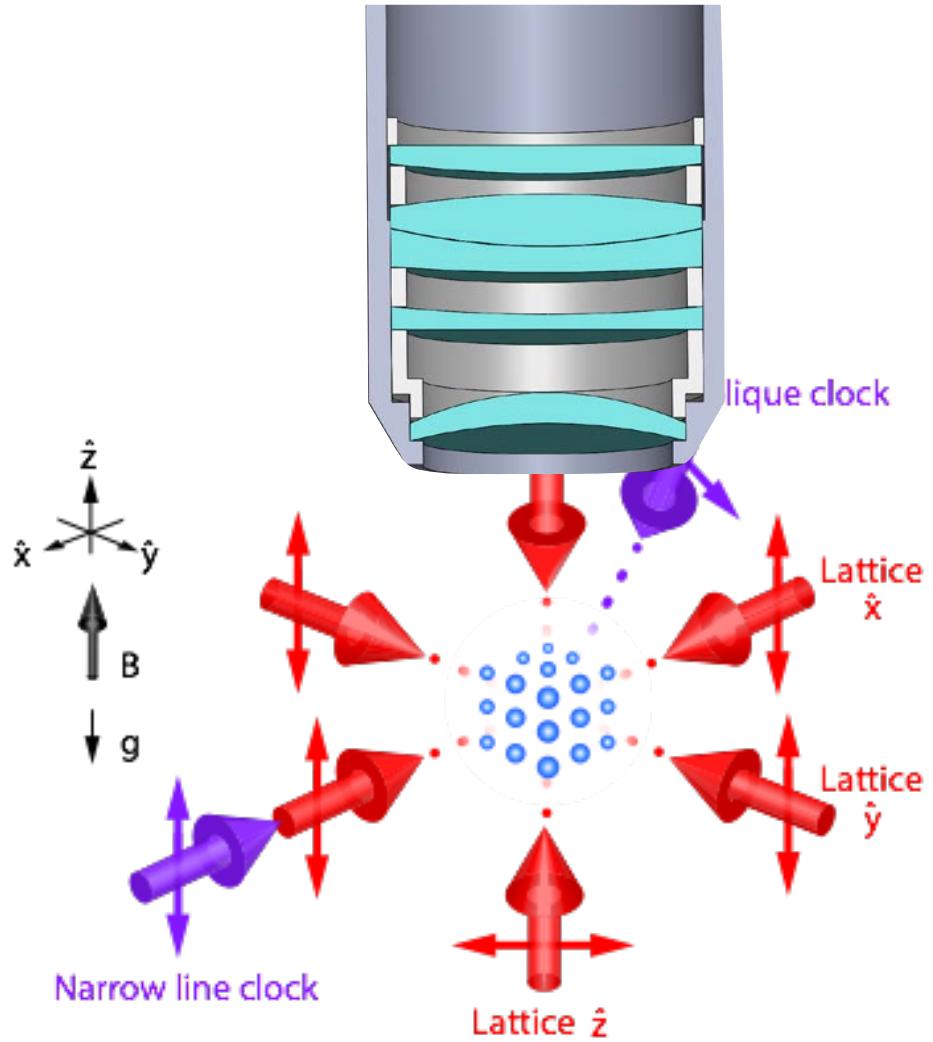
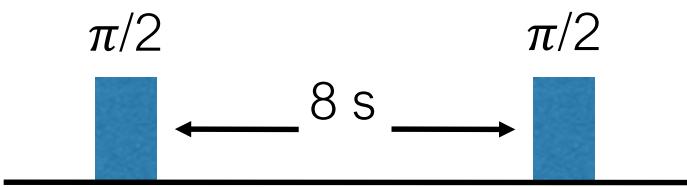


Atom-Light coherence: 10 s

Quality factor:  $8 \times 10^{15}$

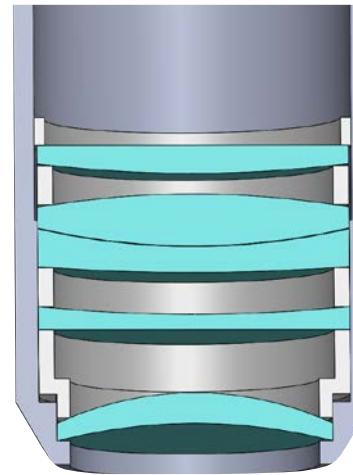
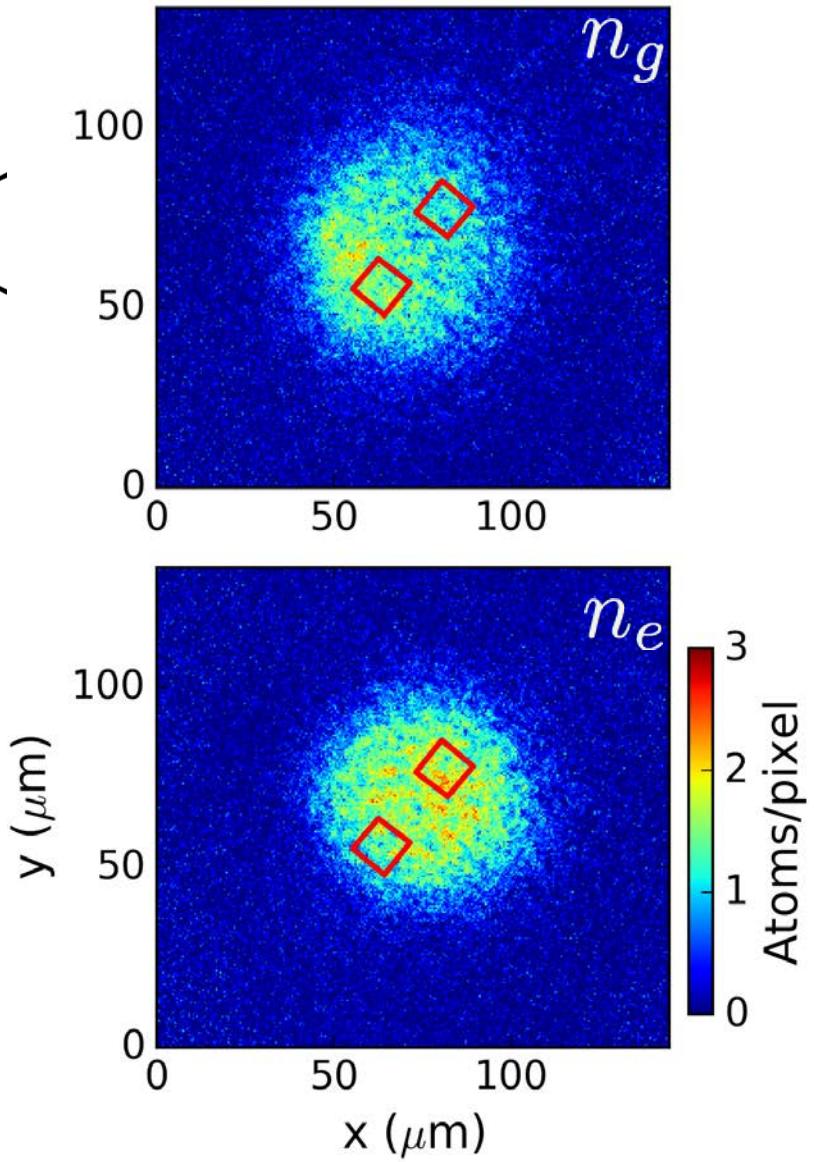
# Spatial + Spectral resolution

Marti *et al.*, Phys Rev Lett **120**, 103201 (2018).

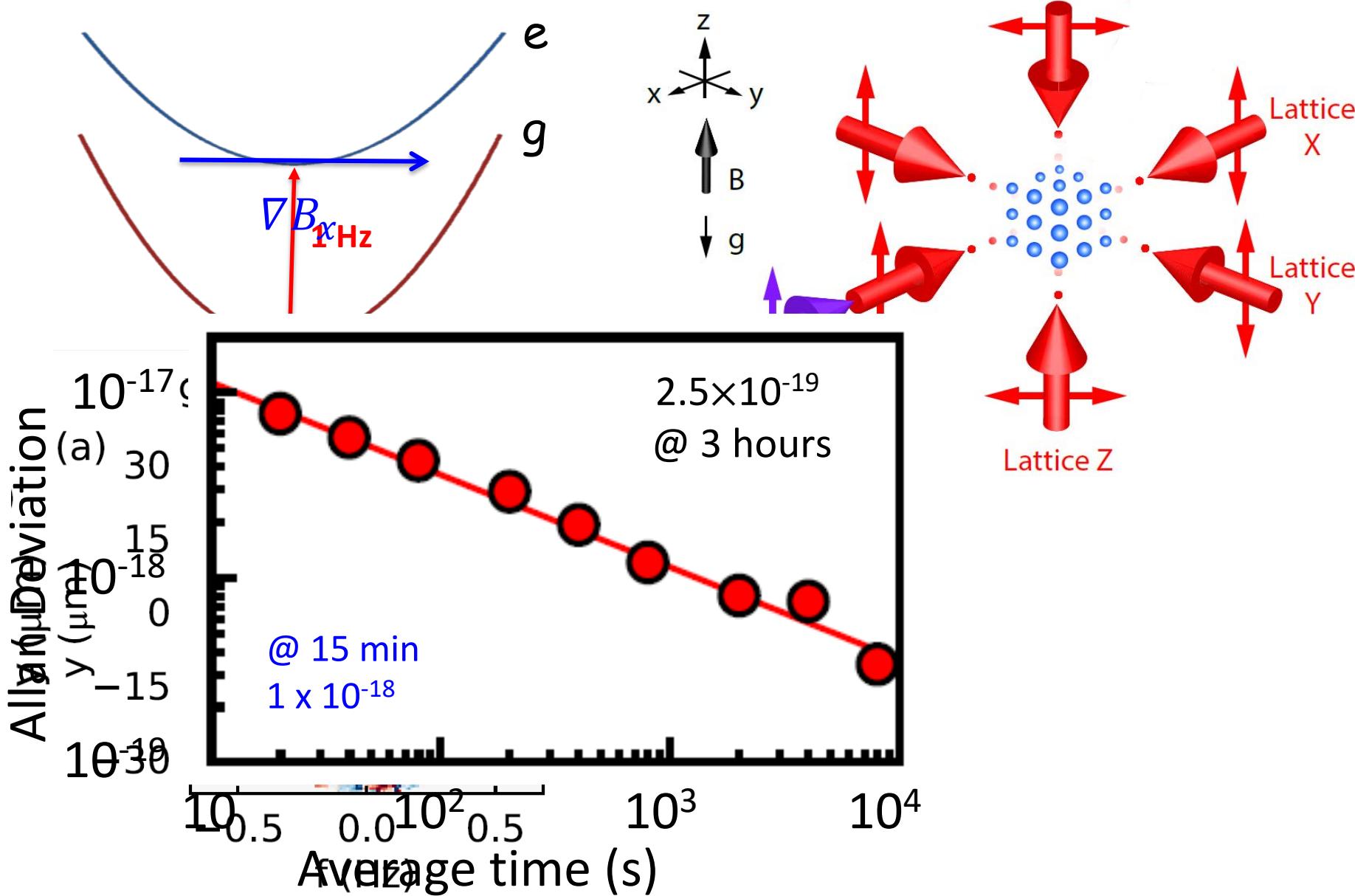


# Spatial + Spectral resolution

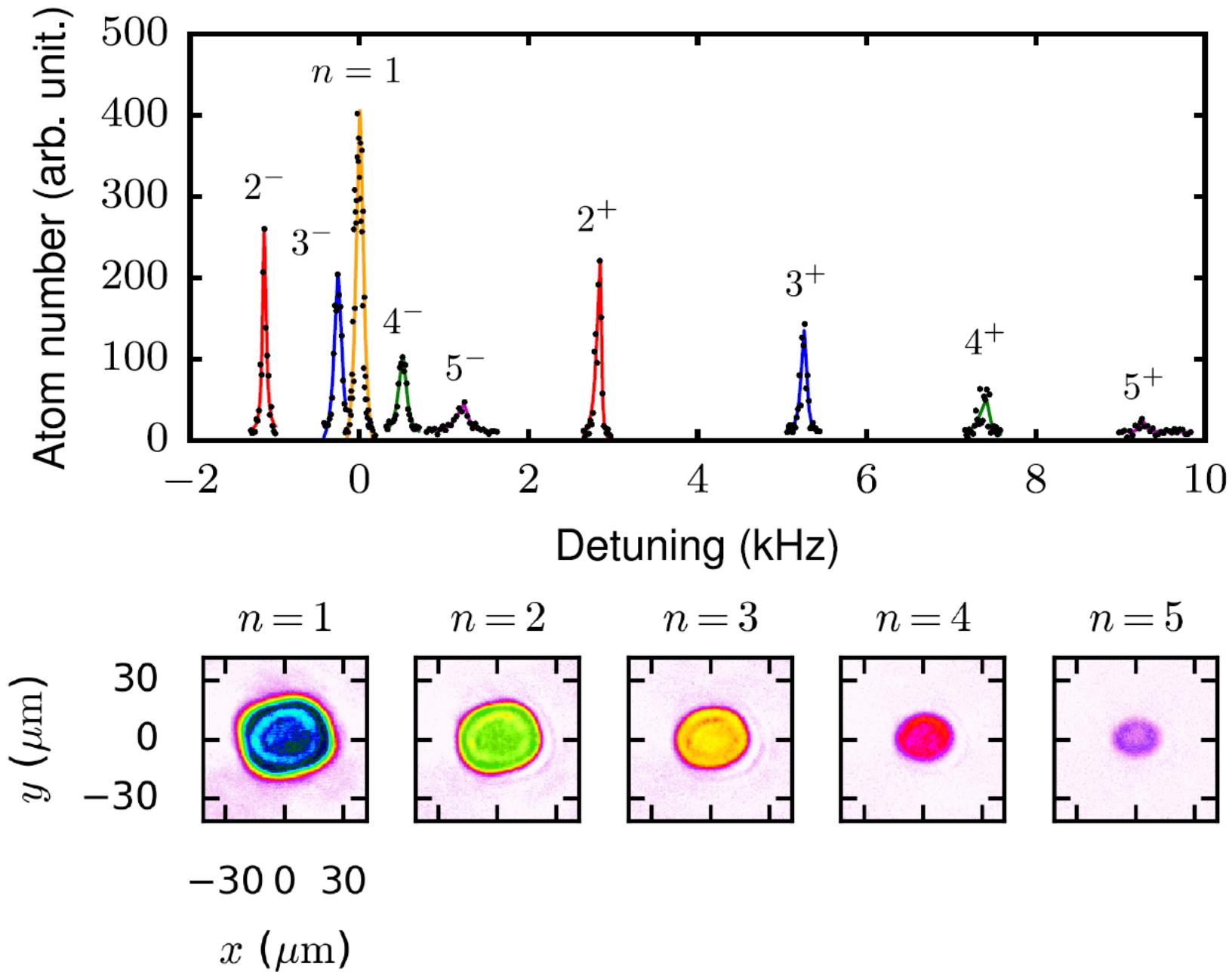
Marti *et al.*, Phys Rev Lett **120**, 103201 (2018).



# Snap shots of optical phase evolutions



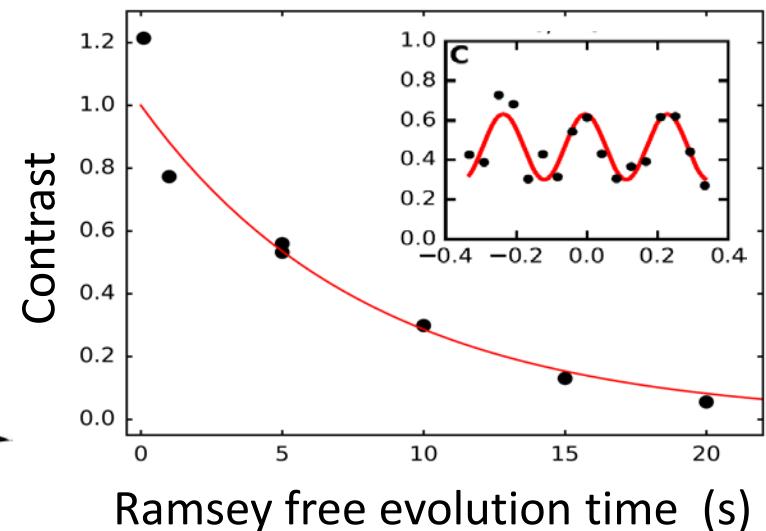
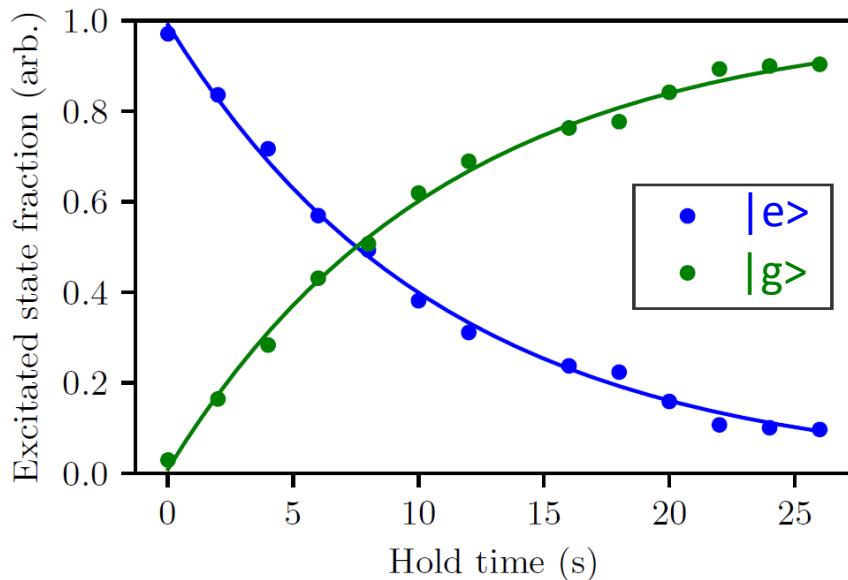
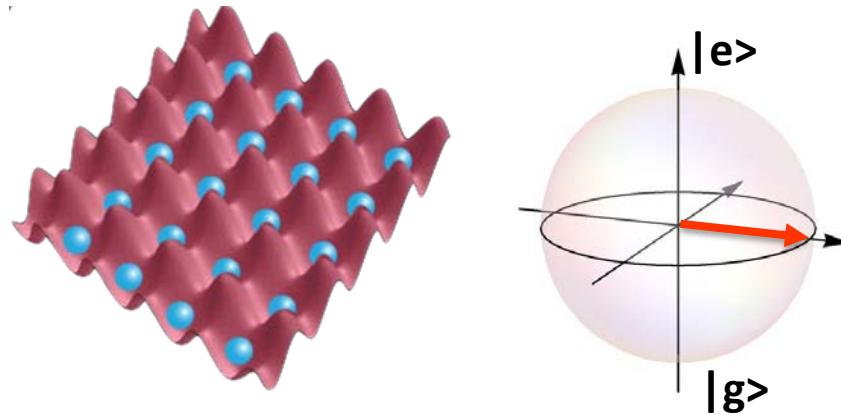
# Emergence of multi-atom interactions



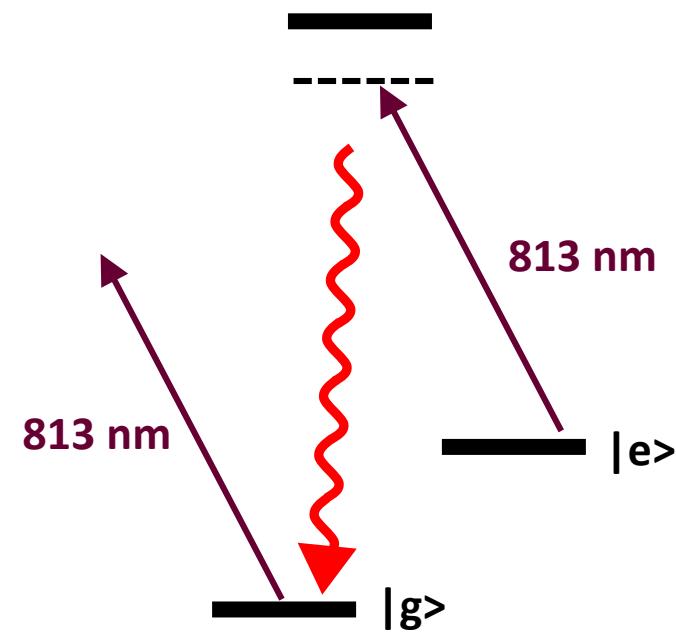
# So, let's go for the 160 s coherence time ?

We must reduce the lattice intensity !

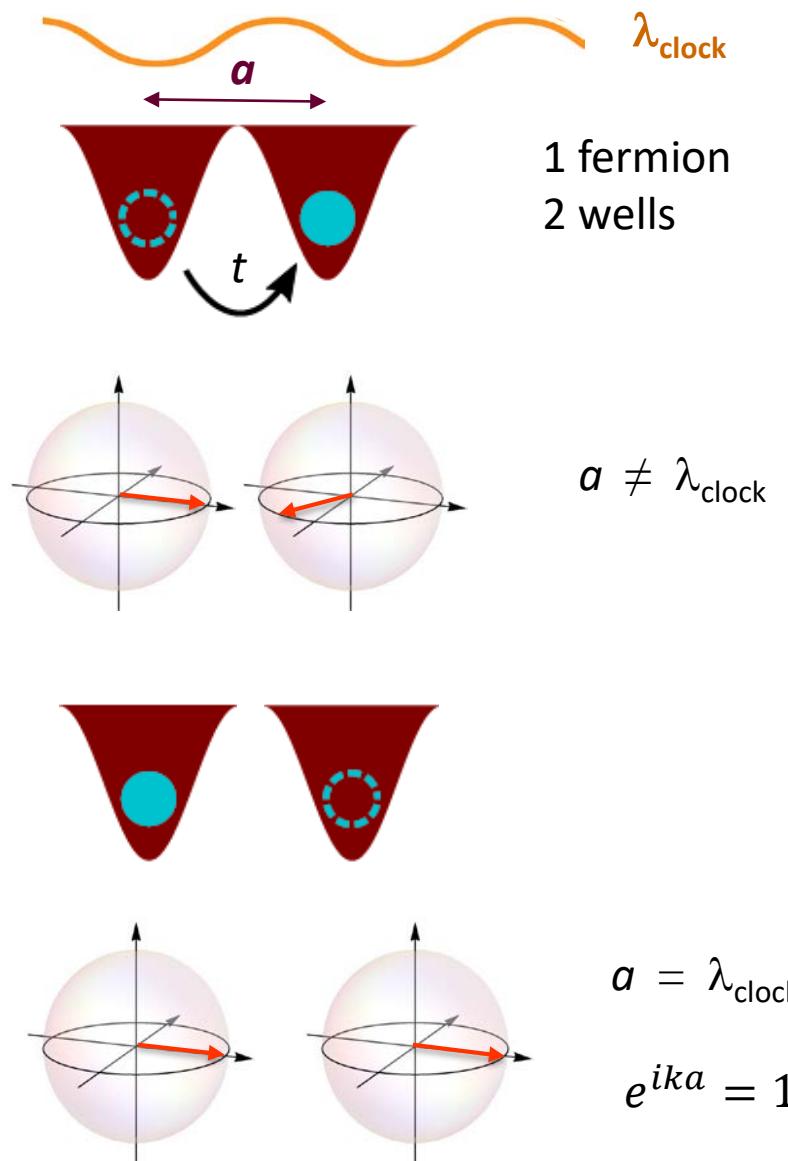
For  $|g\rangle$  atoms, lattice lifetime is  $>100$  s



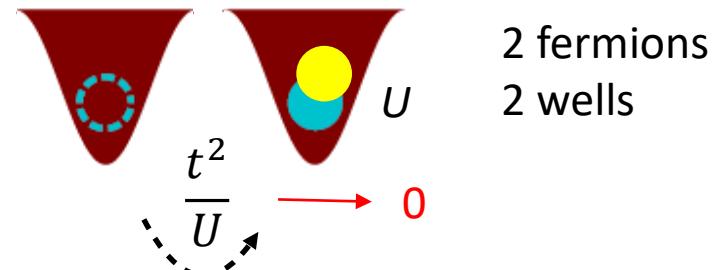
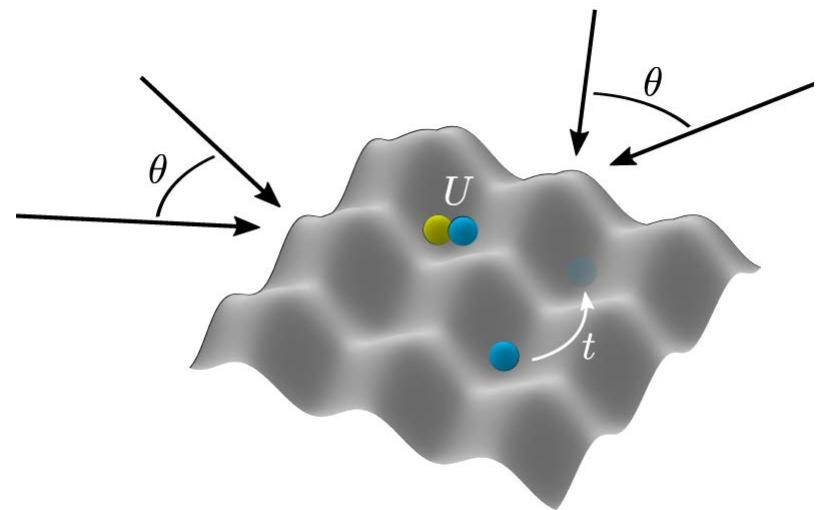
Ramsey free evolution time (s)



# A Fermi band/Mott insulator clock



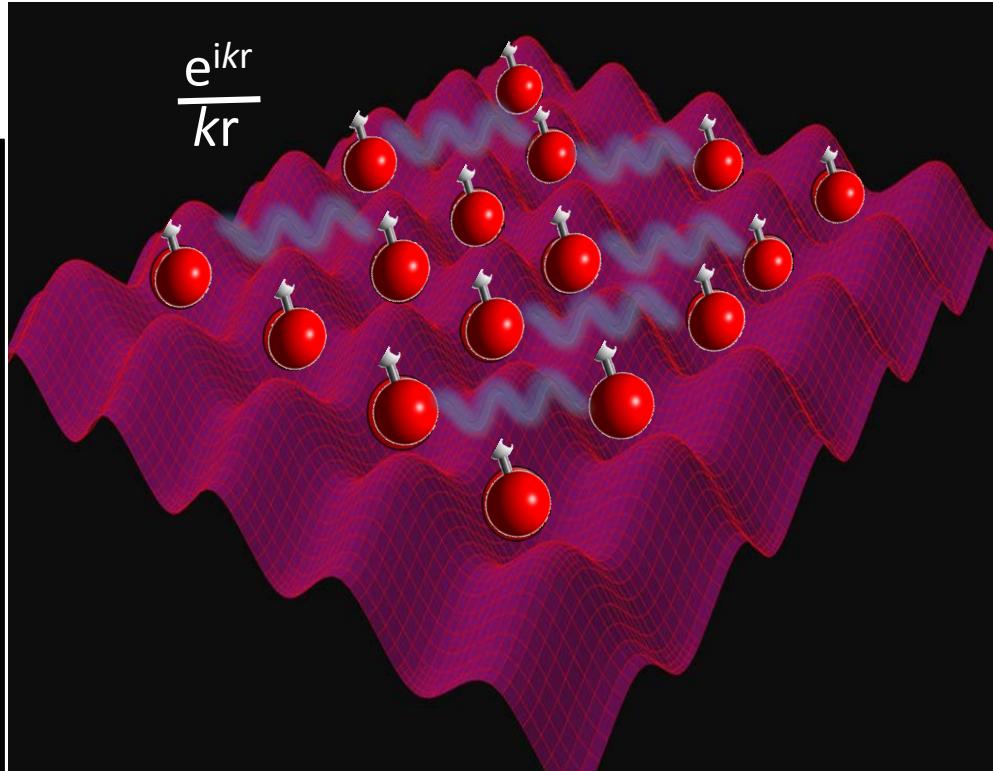
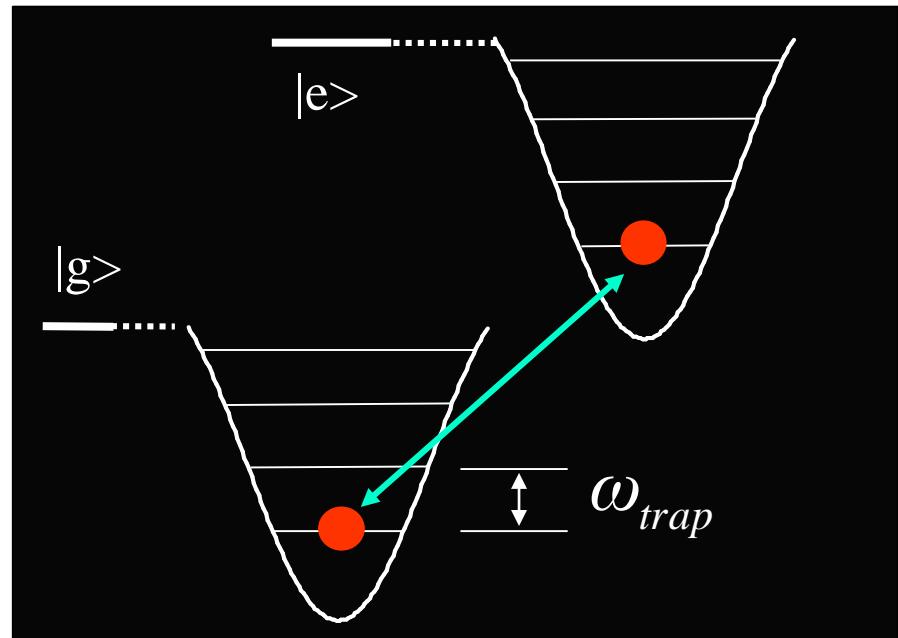
Lattice spacing =  $813 \text{ nm} / 2\sin(\theta/2)$



# Sr clock: the next systematic uncertainty - collective dipoles

Chang, Ye, Lukin, Phys. Rev. A **69**, 023810 (2004).

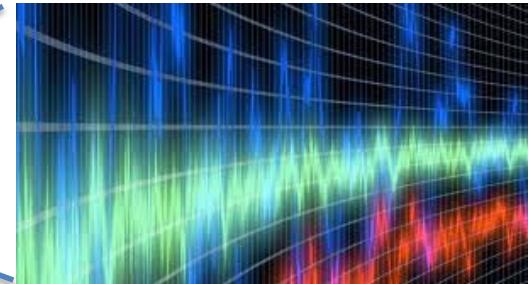
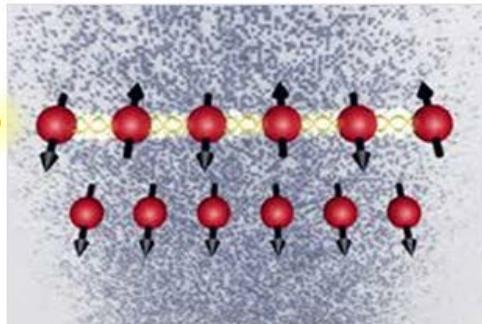
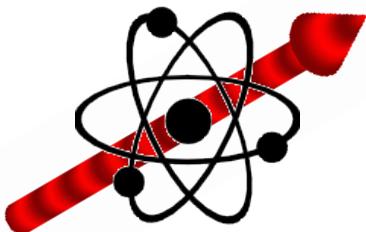
$\leq 1 \text{ mHz}$  effect for a unity filled lattice  
( $10^{-19}$ )



- Collective dipolar couplings ( ${}^1\text{S}_0 - {}^3\text{P}_1$ : Bromley *et al.*, Nature Comm., 2016)
- Real part: clock shift; Imaginary part: line broadening, super-radiance

# Quantum Measurement Frontier

Optical atomic clock



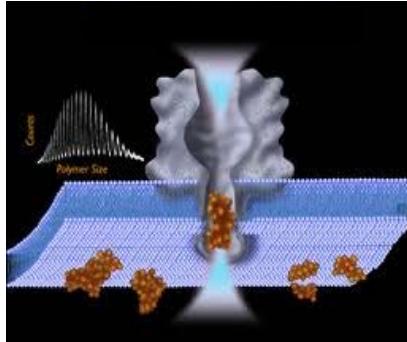
Advanced materials



Room-Temp.  
superconductor



Loss-less electric grid



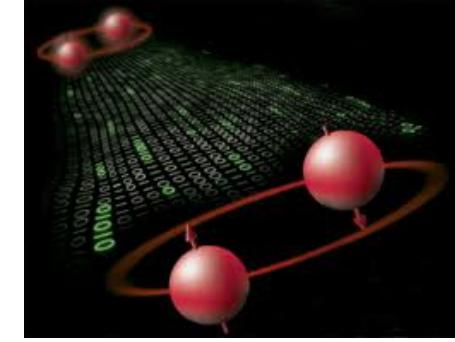
Protein folding



Drug design



Entangled-states



Quantum Simulators

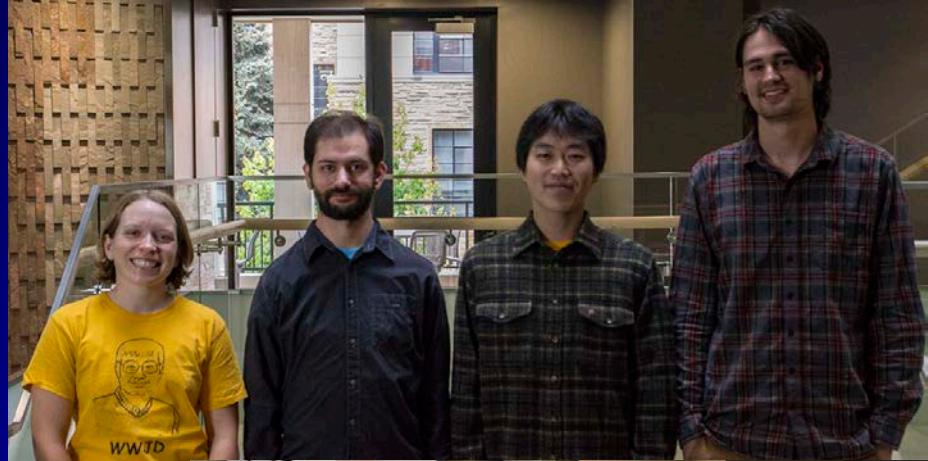
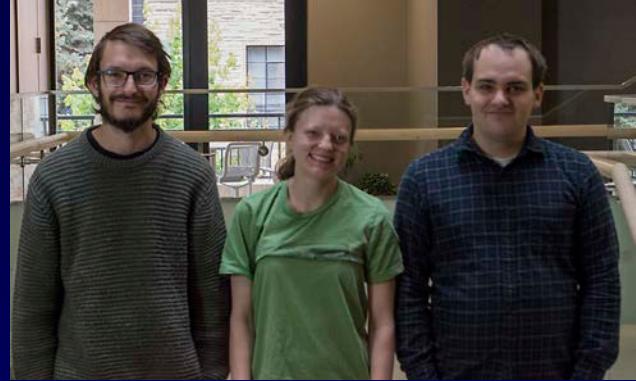
Quantum Cryptography

# Sr optical clock - advancing state-of-the-art

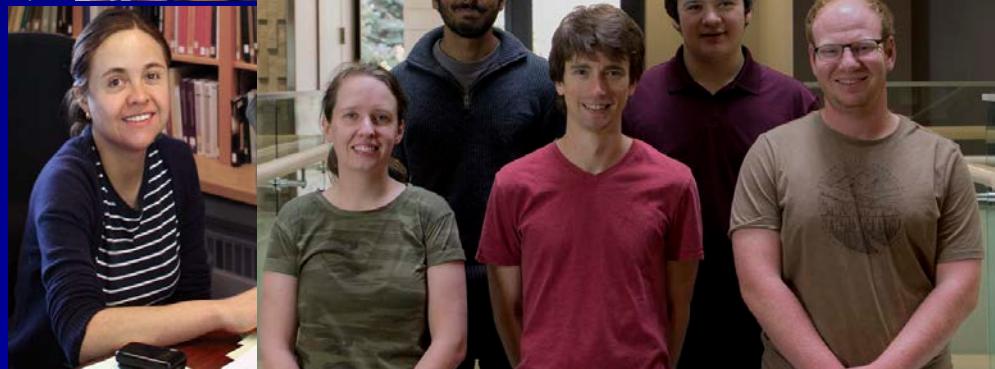
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