Quantum simulation (and information processing) with Rydberg atoms



Outline

- Lecture 1: Programmable Rydberg arrays introduction to the platform
- Lecture 2: Quantum simulation experiments with programmable Rydberg arrays
- Lecture 3: Quantum information processing with programmable Rydberg arrays

Programmable quantum platform: modes of operation



Analog

Engineer the system Hamiltonian such that the desired phase is the ground state in accessible range of parameters







Implement quantum circuit to generate the desired entangled state



Programmable quantum platform: modes of operation



Engineer the system Hamiltonian such that the desired phase is the ground state in accessible range of parameters





analog + digital



Implement quantum circuit to

generate the desired entangled state

Programmable quantum platform: modes of operation



Engineer the system Hamiltonian such that the desired phase is the ground state in accessible range of parameters











Analog quantum dynamics: an example





Analog quantum dynamics: an example



Analog quantum dynamics: an example



Quantum simulation with Rydberg atom arrays

Many-body phases

"Conventional" phases (symmetry breaking)

Topological phases

Quantum phase transitions and criticality

(2+1)D Ising QPT

Quantum dynamics

Quantum many-body scars

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nearest neighbors?

S. Ebadi et al., Nature 595, 227–232 (2021)

quasi-adiabatic preparation in different points of the phase diagram

how do we characterize the state we prepare?



Numerical phase diagram





 $G^{(2)}(k,l) = \langle n_k n_l \rangle - \langle n_k \rangle \langle n_l \rangle$ averaged over all pairs separated by (k, l)



quasi-adiabatic preparation in different points of the phase diagram

 $\langle \rangle$

kx (π)

Peak at

(π, π)

how do we characterize the state we prepare?





canonical AF order parameter:

staggered magnetization

Fourier transform of single-shot measurement outcomes $\mathcal{F}(\mathbf{k}) = |\sum_{i} \exp(i\mathbf{k} \cdot \mathbf{x}_{i}/a) n_{i}/N|$

we construct order parameters for all observed phases using $\mathcal{F}(\mathbf{k})$ averaged over all exp repetitions



S. Ebadi et al., Nature 595, 227-232 (2021)

quasi-adiabatic preparation in different points of the phase diagram

how do we characterize the state we prepare?



S. Ebadi et al., Nature 595, 227-232 (2021)

Ordered phases: Square and triangular lattice

Related experiment from Antoine Browaeys' group



Detailed characterization of the AF phase



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Quantum phase transition: (2+1)D Ising

Quantum phase transition into the checkerboard phase



Slower sweep rate s

- = more adiabatic
- = larger correlation length $\boldsymbol{\xi}$



S. Ebadi et al., Nature 595, 227-232 (2021)

Quantum phase transition: (2+1)D Ising

Universality

Quantum phase transitions fall into universality classes characterized by critical exponents that determine universal behaviour of the system near the quantum critical point

Transition into checkerboard phase predicted to be in the (2+1)D quantum Ising universality class



Quantum phase transition: (2+1)D Ising Universal scaling



Study the dynamical build-up of correlations associated with the quantum Kibble–Zurek mechanism

> predicts a universal scaling between the control parameter Δ and the correlation length ξ (both rescaled with the sweep rate *s*):

$$\widetilde{\xi} = \xi (s/s_0)^{\mu} \qquad \qquad \mu = v/(1+zv) \\ \widetilde{\delta} = (\Delta - \Delta_c)(s/s_0)^{\kappa} \qquad \qquad \kappa = -1/(1+zv)$$

Hold z = 1 constant and find experimental value of v that gives universal collapse

First observation of (2+1)D Ising quantum phase transition

S. Ebadi et al., Nature 595, 227-232 (2021)

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Topological phases: SSH model for hard-core bosons

More recent works with XY Hamiltonian: G. Bornet et al, arXiv (2023) V. Liu et al, Nature (2023)

Many-body symmetry-protected topological phase in quasi-1D atom array

asymmetric interaction Α four-fold ground state Topological configuration 13 190° sub-chain. degeneracy due to edge states ∧ B $8 \mu m$ 10 chain B θ_m $12 \mu m$ Test robustness of SPT phase: sub Α Trivial configuration В Single particle Many body В \mathbf{B} $\left(\frac{a^2}{R_{ii}^3}(3\cos^2\theta_{ij}-1)\right)$ $8 \mu m$ 0.5 $60P_{1/2}$ $60P_{1/2}$ Occupancy $12 \mu \mathrm{m}$ $-0 - b_i^{\dagger} |0\rangle$ θ_m $-\mathbf{Q} b_i^{\dagger} |0\rangle$ $|0\rangle$ -Ò--0- $|0\rangle$ dipolar exchange $60S_{1/2}$ $60S_{1/2}$ interaction Probe $\Delta_{uw}/(2\pi)$ (MHz) Probe $\Delta_{\mu w}/(2\pi)$ (MHz) Dipolar flip-flop interaction between hard-core bosons bosonic Su-Schrieffer-Heeger (SSH) model 2 Rydberg states coupled by MW hopping along the chain

De Léséleuc et al., Science 365, 775-780 (2019)

spin 1/2 particles with AF interactions on a frustrated lattice







resonating valence bond (RVB) state

P. Anderson, Materials Research Bulletin 8 (1973)

Analogue dimer models in Rydberg atom arrays:

blockade





R. Samajdar, W. W. Ho, H. Pichler, M. Lukin, S. Sachdev, "Quantum phases of Rydberg atoms on a kagome lattice", PNAS (2021)

R. Verresen, M. Lukin and A. Vishwanath,

"Prediction of Toric Code Topological Order from Rydberg Blockade", PRX (2021)



quantum spin liquid state: superposition of all dimer coverings

$$|\psi_{QSL}\rangle = |\psi_{QSL}\rangle + |\psi_{$$

R. Verresen, M. Lukin and A. Vishwanath, Phys Rev. X 11, 031005 (2021) G. Semeghini et al., Science 374, 1242 (2021)

P. Anderson, Materials Research Bulletin 8 (1973)



quantum spin liquid state: superposition of all dimer coverings



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Topological phases: Quantum spin liquid

quasi-adiabatic state preparation



$$\mathcal{H} = \frac{1}{2}\Omega(t)\sum_{i}\sigma_{x}^{(i)} - \sum_{i}\Delta(t)n_{i} + \sum_{i < j}V_{ij}n_{i}n_{j}$$

G. Semeghini et al., Science 374, 1242 (2021)

Topological phases: Quantum spin liquid

quasi-adiabatic state preparation





•

$$\mathcal{H} = \frac{1}{2}\Omega(t)\sum_{i}\sigma_{x}^{(i)} - \sum_{i}\Delta(t)n_{i} + \sum_{i< j}V_{ij}n_{i}n_{j}$$

 $\langle Z \rangle = (-1)^{\# \text{ enclosed vertices}}$

Topological phases: Quantum spin liquid



diagonal string operator Z:

$$\langle Z \rangle = -1$$



parity of dimers along a string



diagonal string operator Z:





parity of dimers along a string



fluorescence imaging: atoms in $|r\rangle$ are identified as losses \rightarrow marked as dimers



off-diagonal string operator X:



→ coherence between dimer coverings





R. Verresen, M. Lukin and A. Vishwanath, Phys Rev. X 11, 031005 (2021)

G. Semeghini et al., Science 374, 1242 (2021)

off-diagonal string operator X:



coherence between dimer coverings

$$: \left\{ \begin{array}{c} \bigtriangleup \leftrightarrow (-1) \bigtriangleup \\ \swarrow \leftarrow \rightarrow \bigtriangleup \end{array} \right\}$$

basis rotation to measure X:



off-diagonal string operator X:

 \leftrightarrow (-1)



coherence between dimer coverings

basis rotation to measure X:





Order parameters?



closed loops vs open strings

closed loops: detect non-trivial topological correlations

open strings: distinguish QSL from nearby phases

FM string order parameters:





K. Fredenhagen and M. Marcu, Comm. Math. Phys. 92 (1983)



R. Verresen, M. Lukin and A. Vishwanath, Phys Rev. X 11, 031005 (2021) G. Semeghini et al., Science 374, 1242 (2021)

K. Fredenhagen and M. Marcu, Comm. Math. Phys. 92 (1983)

Understanding experimental observations

- quantum dynamics of a 219-atom system: not possible to simulate classically
- ground state properties:

DMRG on a cylinder with periodic boundary conditions show that long-range interactions destabilize spin liquids!

 quasi-adiabatic state preparation: time-dependent DMRG simulations on a small system state with SL properties; qualitative agreement with experiment



R. Verresen, M. Lukin and A. Vishwanath, Phys Rev. X 11, 031005 (2021) G. Semeghini et al., Science 374, 1242 (2021)

long-range interactions result in





Understanding experimental observations



non-trivial topology: array with a hole

Topological qubit?

topological protection

dimer states separate into two distinct topological sectors:



See related work form Google group: Science 374 (2021) and arXiv:2210.10255

G. Semeghini et al., Science 374, 1242 (2021)

logical

operators



detect measuring syndromes on Z plaquettes detect measuring syndromes on X plaquettes

Enhancing detection of topological order

Idea: local error correction + coarse graining (RG flow)







Hastings, Levin, Wen (2005)

Enhancing detection of topological order

Post-processing of experimental data



What's next?

Topological qubit encoding and manipulation
 study of Abelian anyons



- Engineering alternating m- and e- boundaries
 - non-Abelian anyons at the intersections
 collaboration with S. Choi and B. Kang at MIT,
 H. Pichler in Innsbruck



More topological phases with Rydberg atom arrays

A. Kitaev, Ann Phys-New York 321, 2 (2006) M. Kalinowski, N. Maskara, M. Lukin, arXiv:2211.00017 (2022)

Non-Abelian topological phases?

Kitaev honeycomb model



More topological phases with Rydberg atom arrays

A. Kitaev, Ann Phys-New York 321, 2 (2006)

M. Kalinowski, N. Maskara, M. Lukin, arXiv:2211.00017 (2022)

Non-Abelian topological phases?

Kitaev honeycomb model



$$U(\tau) = e^{-iH_X\tau} e^{-iH_Y\tau} e^{-iH_Z\tau} = e^{-iH_F[\tau]\tau} \longrightarrow H_F[\tau] = H_0 + \frac{1}{2}\tau[H_X, H_Y] + \frac{1}{2}\tau[H_X, H_Z + \frac{1}{2}\tau[H_Y, H_Z]) + O(\tau^2)$$

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Strongly interacting many-body systems

Can entangled dynamics be controlled?

Experiment: 1D arrays of Rydberg atoms

• Persistent oscillations, not relaxing to thermal values after quench



Further studies in 2D geometries (Bluvstein et al, Science 2021):



Extensive theoretical efforts to understand this nonthermalizing behavior ———> Connection to quantum many-body scars

Heller PRL (1984), Fendley PRB (2004), Lesanovsky PRA (2012), Turner Nat Phys (2018), Lin PRL (2019), Iadecola PRB (2019), Khemani PRB (2019), Sala PRX (2020), Surace PRX (2020), Mukherjee PRB (2020), Michailidis PRX (2020), ...

New tools to probe many-body systems \longrightarrow Modular and hybrid analog-digital quantum circuits



Modular and hybrid analog-digital quantum circuits

Measure Renyi entanglement entropy by effectively interfering two copies of a many-body system

$Purity Tr[\rho_A^2] = Tr[S_A \rho \otimes \rho]$ Renyi Entropy S₂ = $-\ln(Tr[\rho_A^2])$

Key idea:

To measure expectation value of SWAP operator, measure occurrences of singlet: Can be done with a Bell measurement!

Inspired by Islam, Kaufman, ... Greiner experiments

$$\frac{|01\rangle - |10\rangle}{\sqrt{2}} = |\Psi^-\rangle$$

D. Bluvstein, et al, Nature 604, 451-456 (2022)

Modular and hybrid analog-digital quantum circuits



Measure Renyi entanglement entropy by effectively interfering two copies of a many-body system

Thermalizing state vs Non-thermalizing scar state

D. Bluvstein, et al, Nature 604, 451-456 (2022)

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