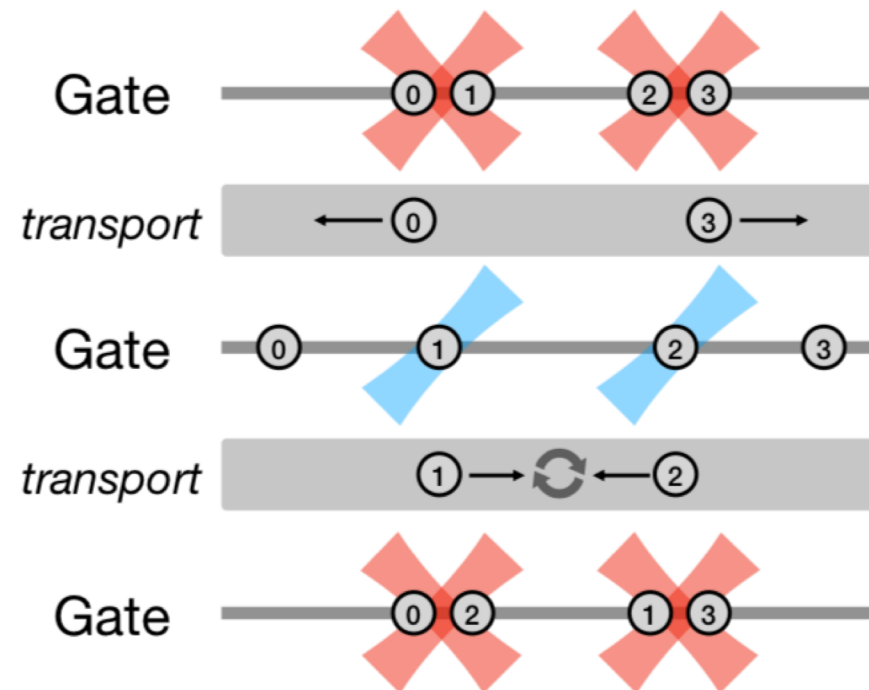
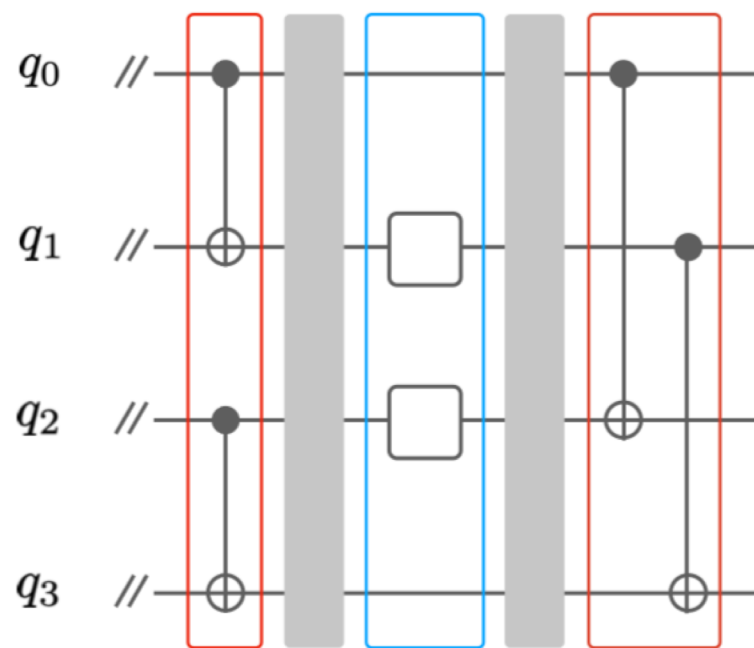


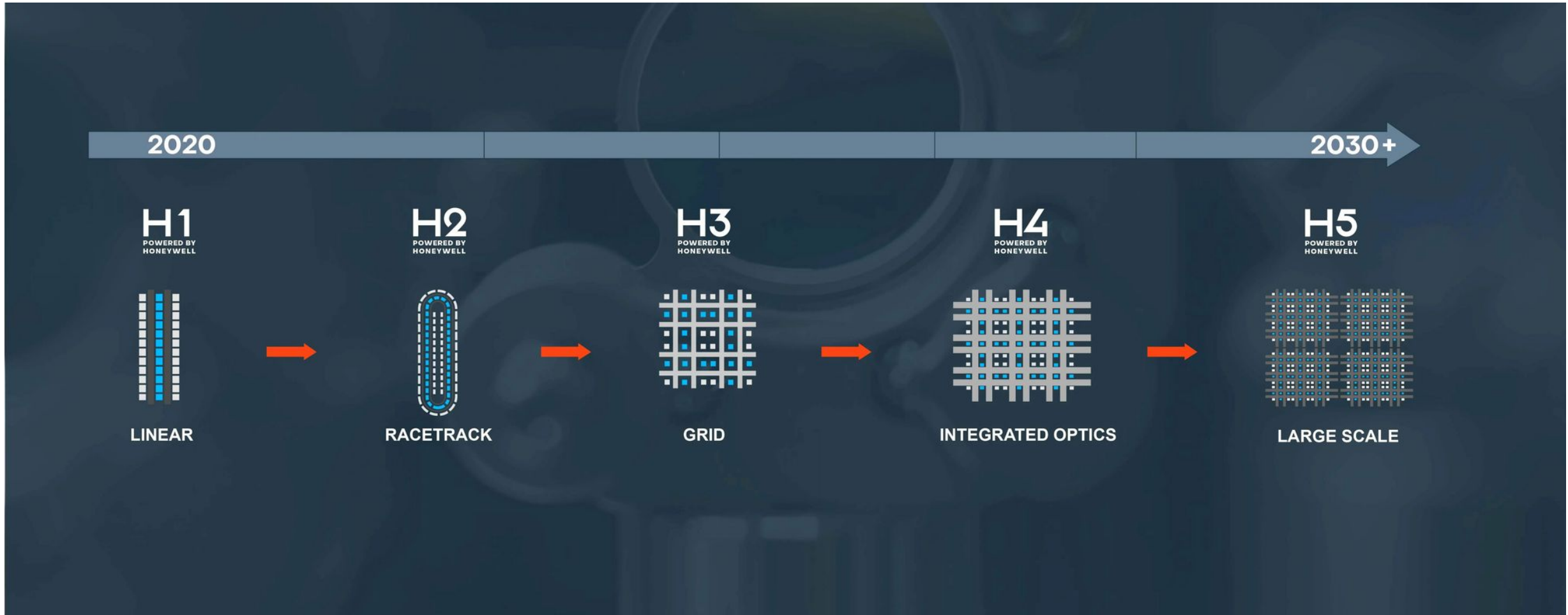
# Trapped Ion Architectures

# QCCD

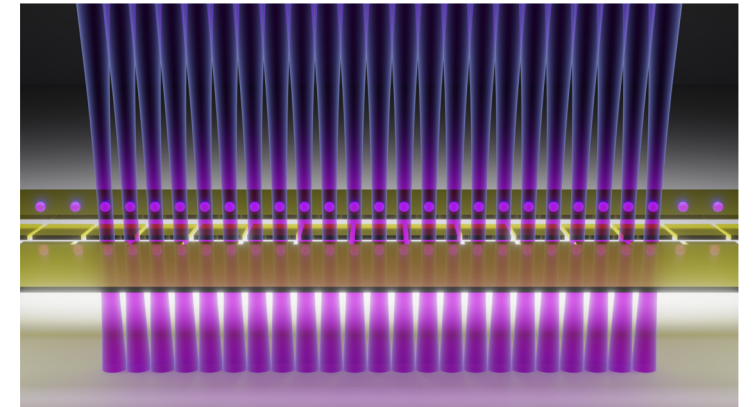
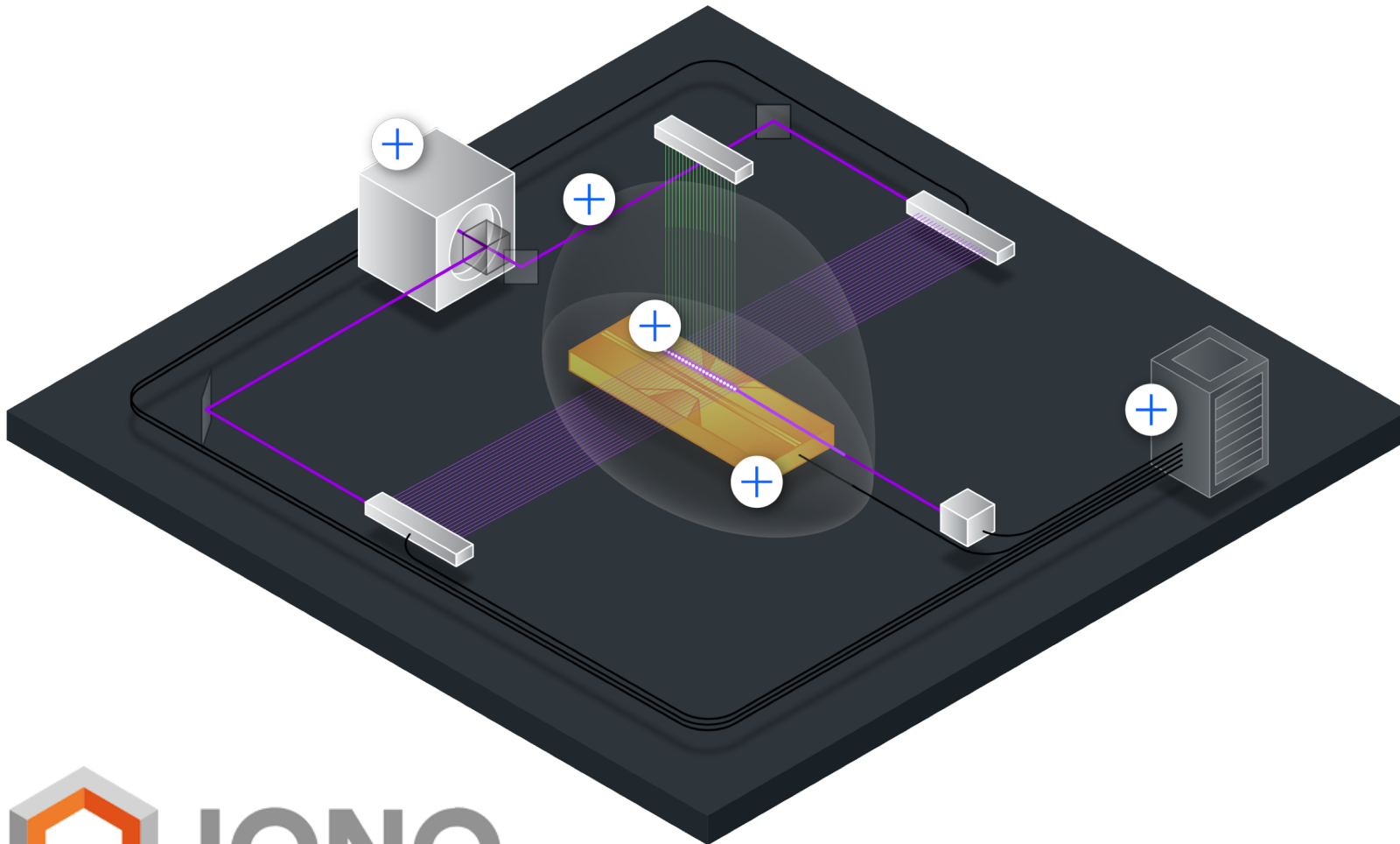
(c)



# QCCD



# Long Chain

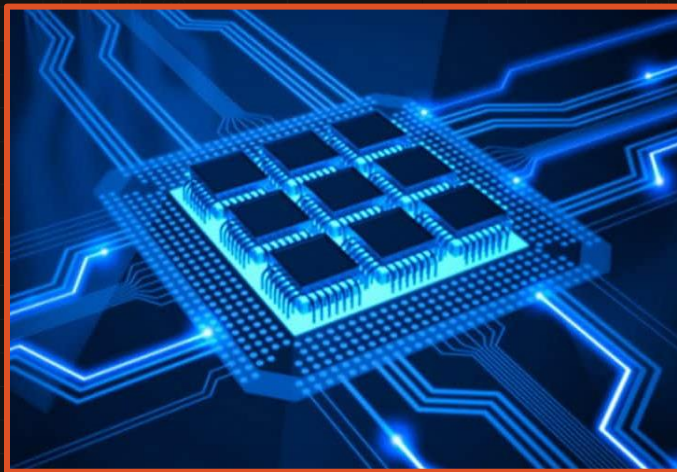


# Photonic Interconnects

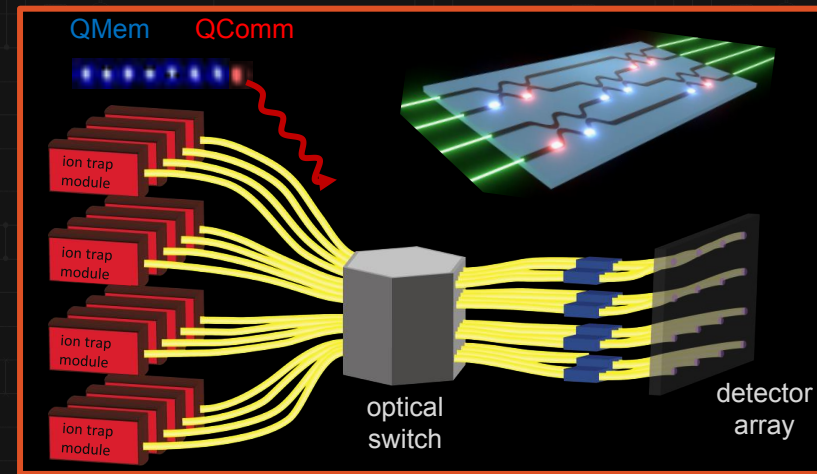


## Quantum Computer Scaling >1000 qubits

**Plan:** Multicore quantum processing



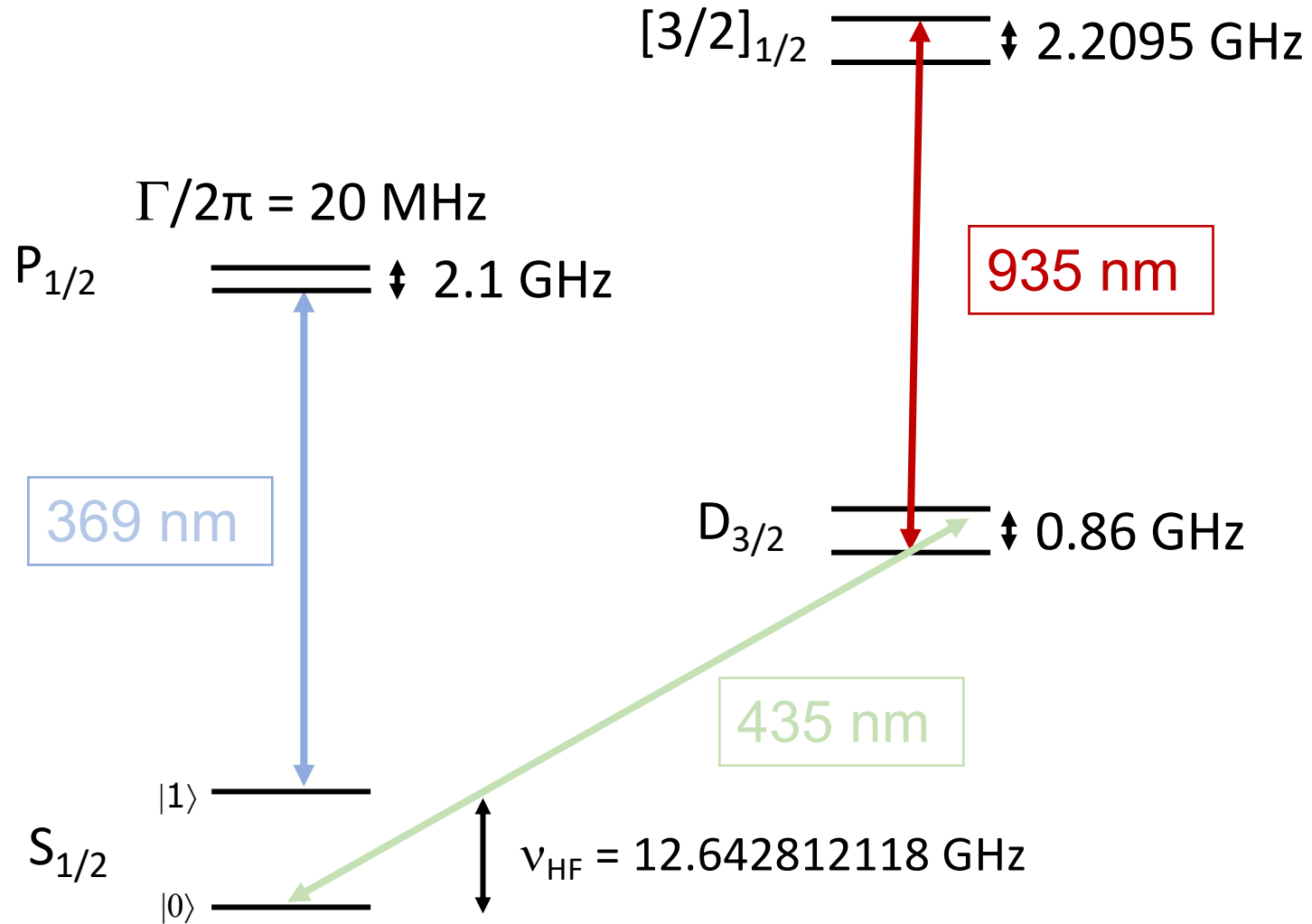
**Technology:** Integrated photonics and switches, SNSPD detector array



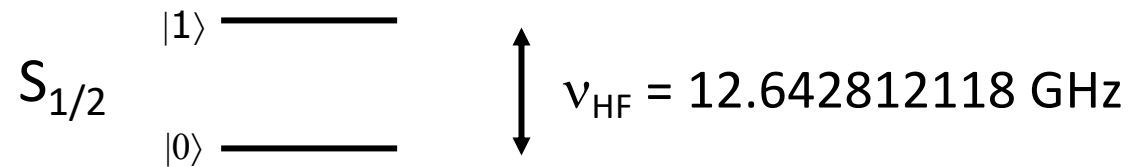
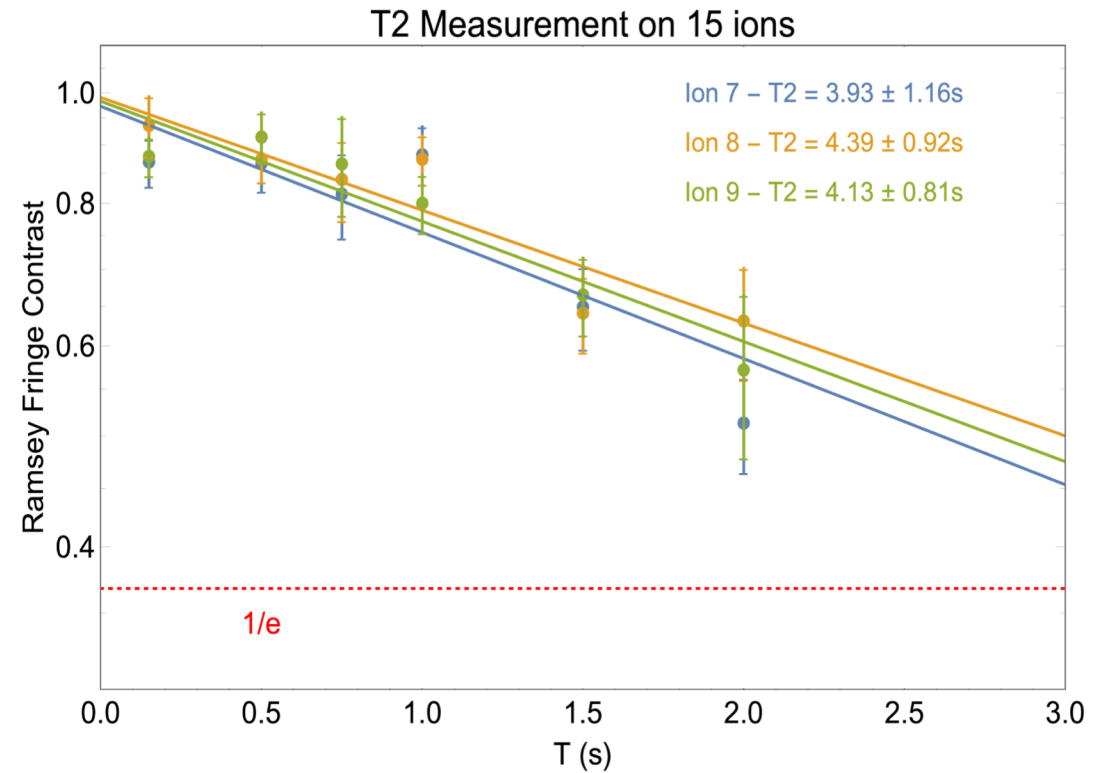
Systems at Duke

# Atomic Ion Qubit

$^{171}\text{Yb}^+$

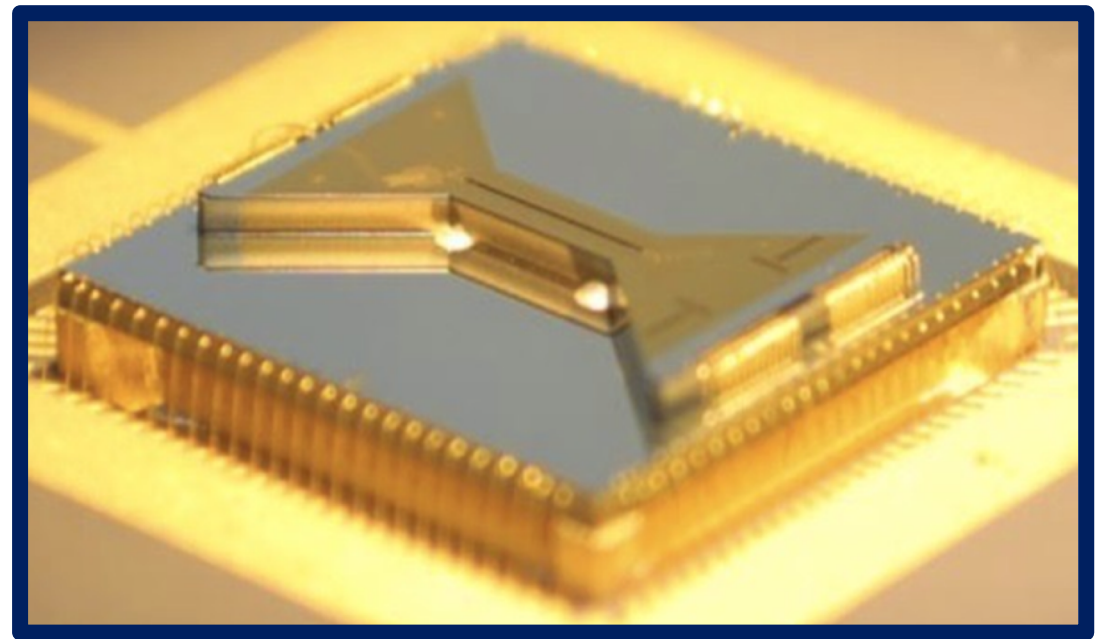
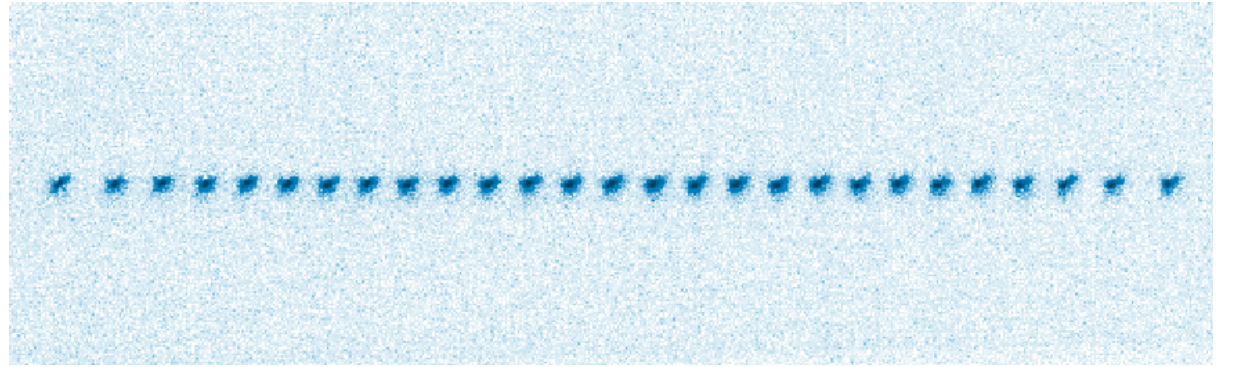


# Atomic Ion Qubit



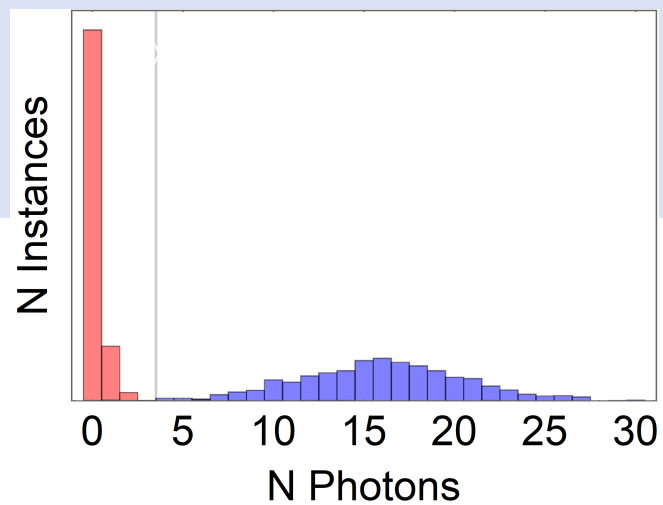


# Single Long Chain

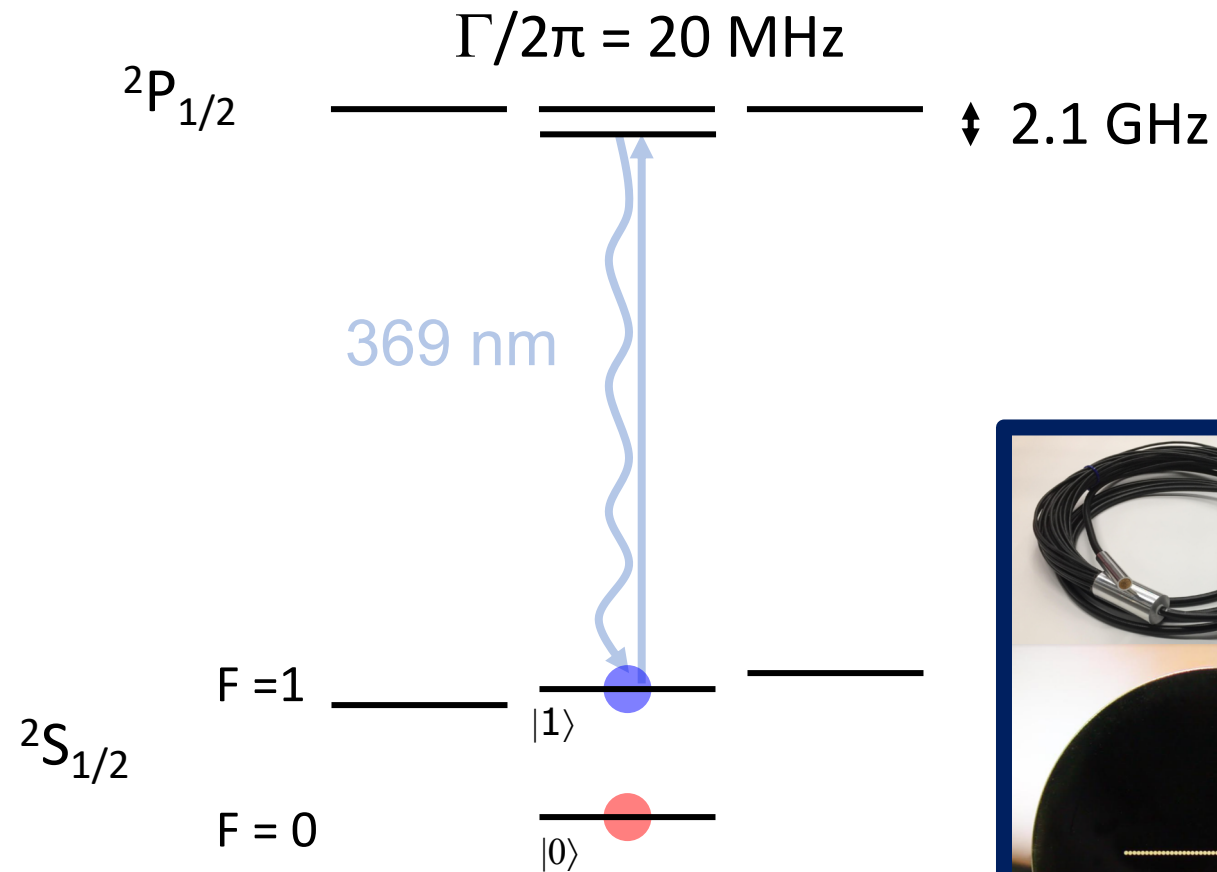


Sandia National Laboratories HOA

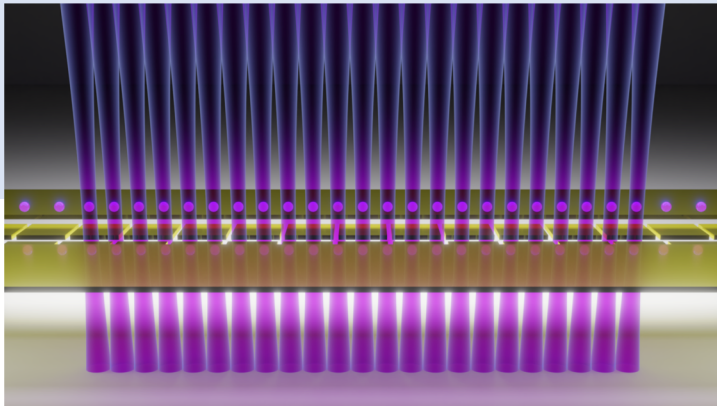
# Laser cooling and detection



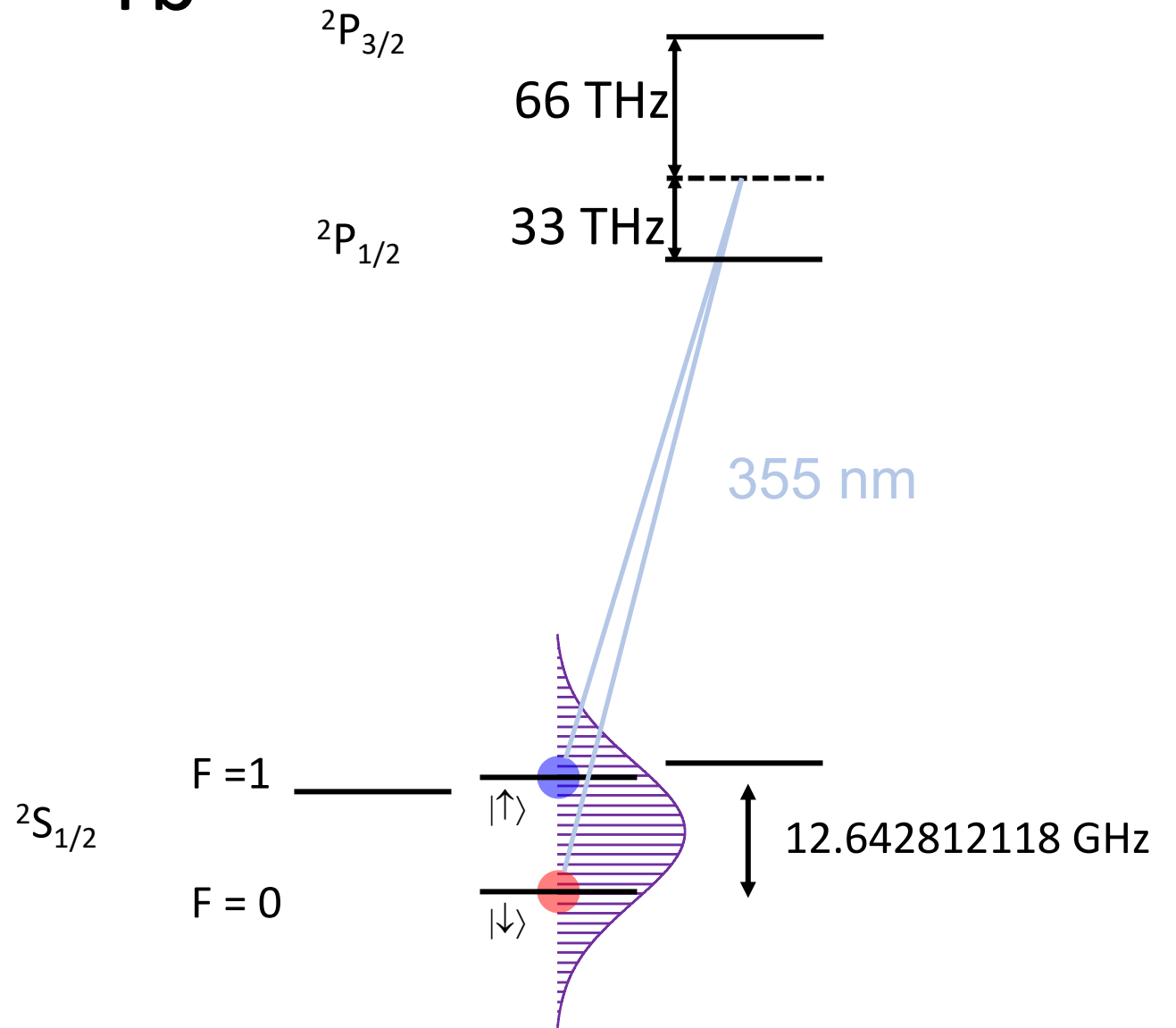
$^{171}\text{Yb}^+$



# Laser qubit operations

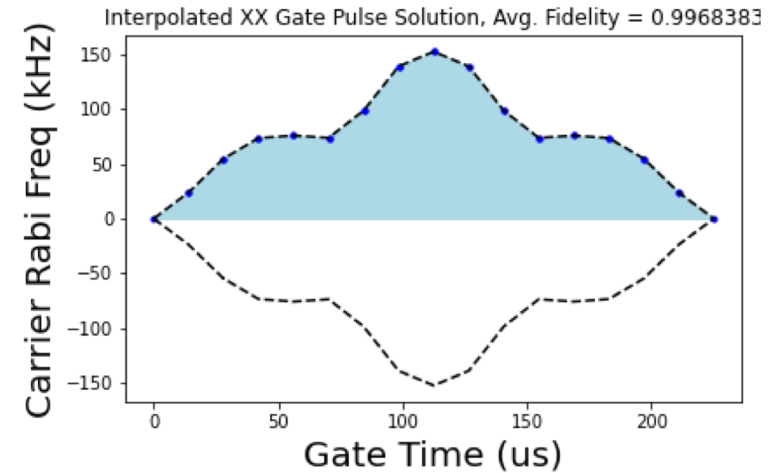
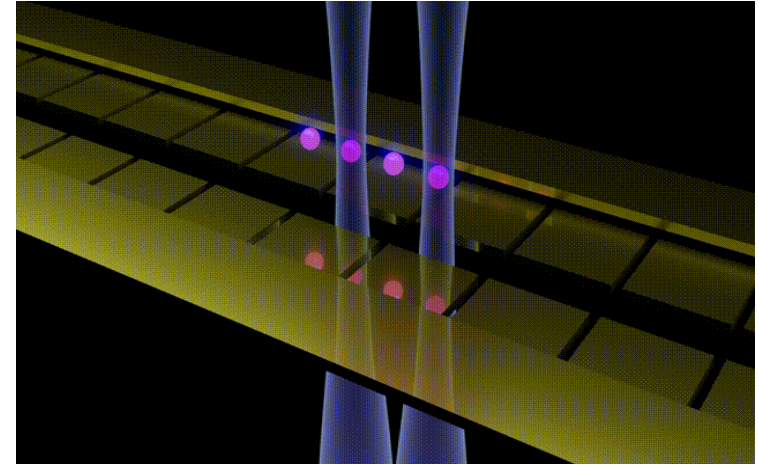
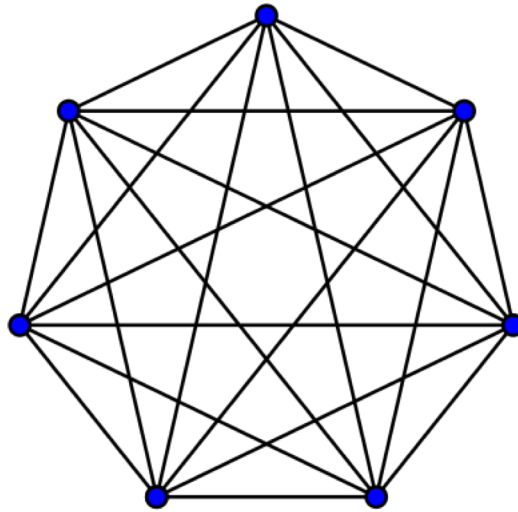


$^{171}\text{Yb}^+$



# Coupled through motion

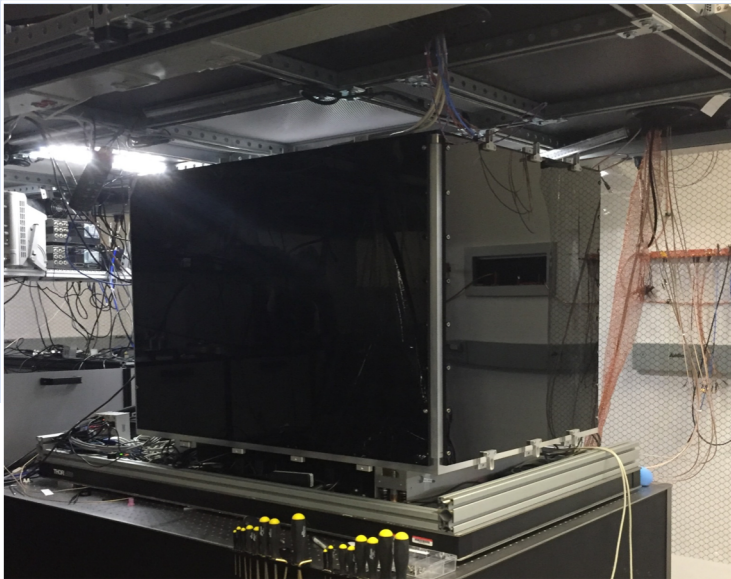
- High connectivity
- Engineered motional modes
- Optimized gate pulses



Native Ion Trap Operation: “Ising” gate

$$XX[\varphi] = e^{-i\sigma_x^{(1)}\sigma_x^{(2)}\varphi}$$

# Blue System Snapshot



Metric	Typical Performance
# qubits	13
Connectivity	All-to-all
2-qubit gate fidelity	98.5-99.3% (Parity fringe)
1-qubit gate fidelity	>99.96% (RB)
SPAM	<0.5%

## Blue System

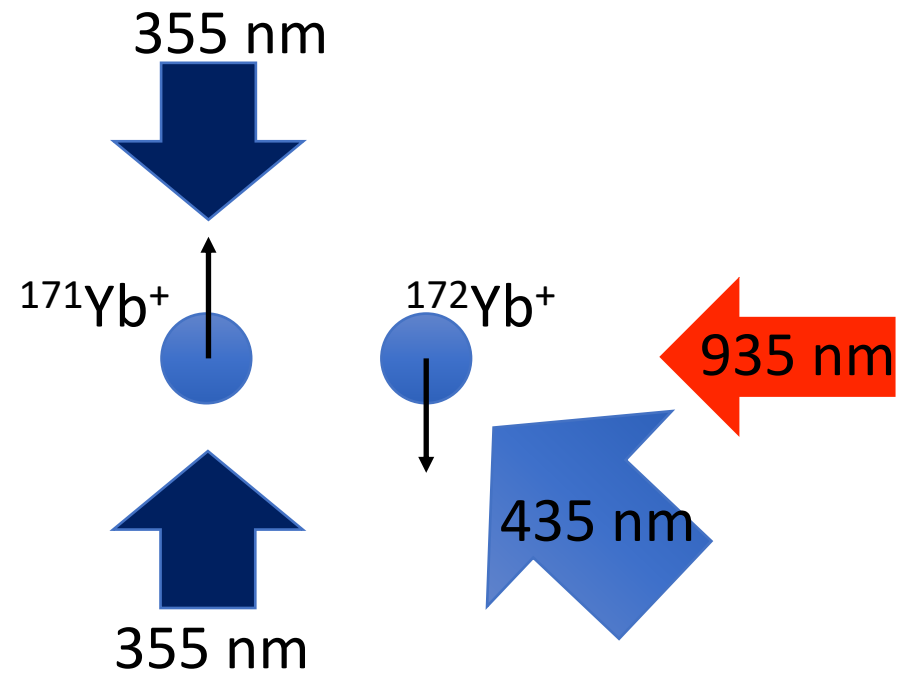
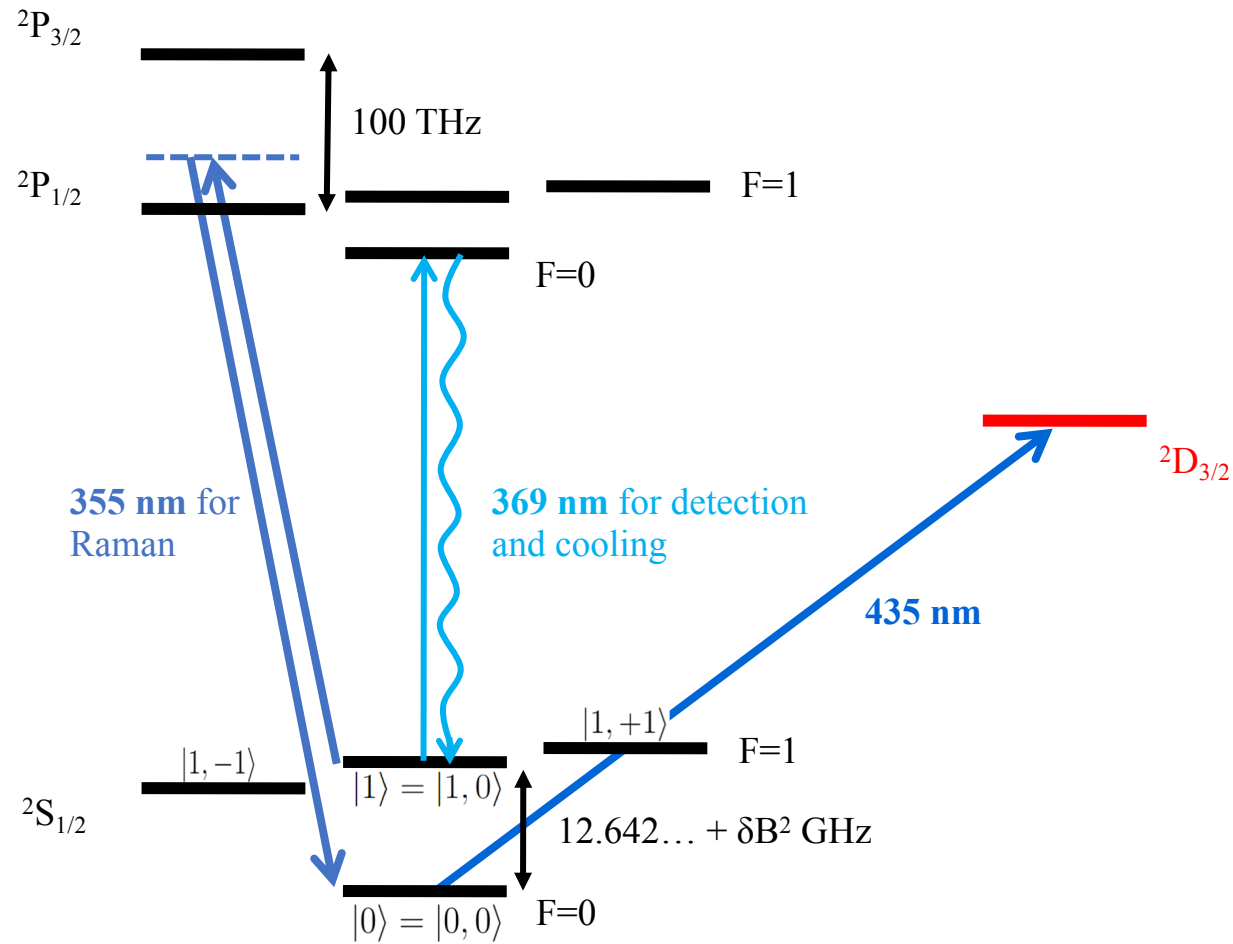


Chris Monroe

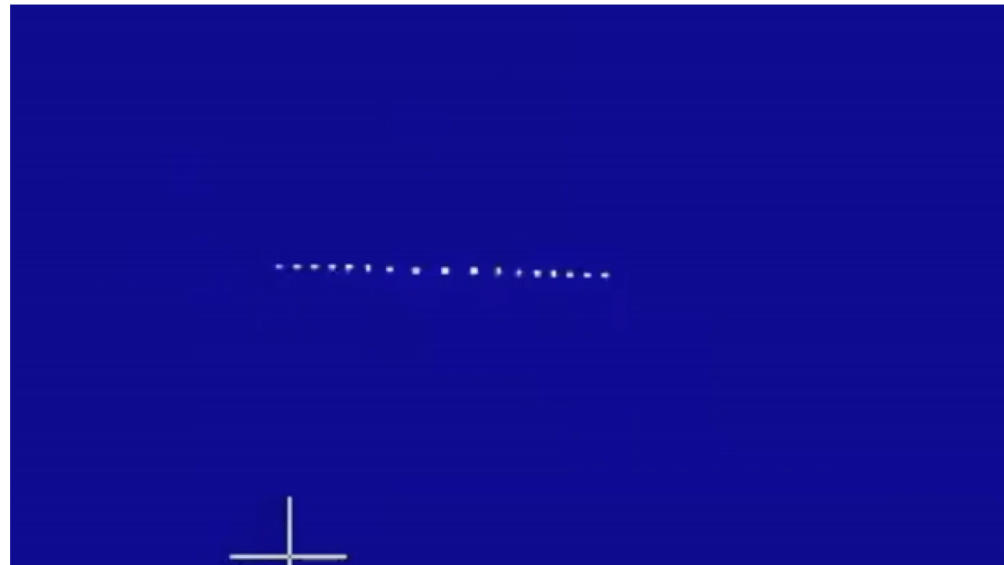
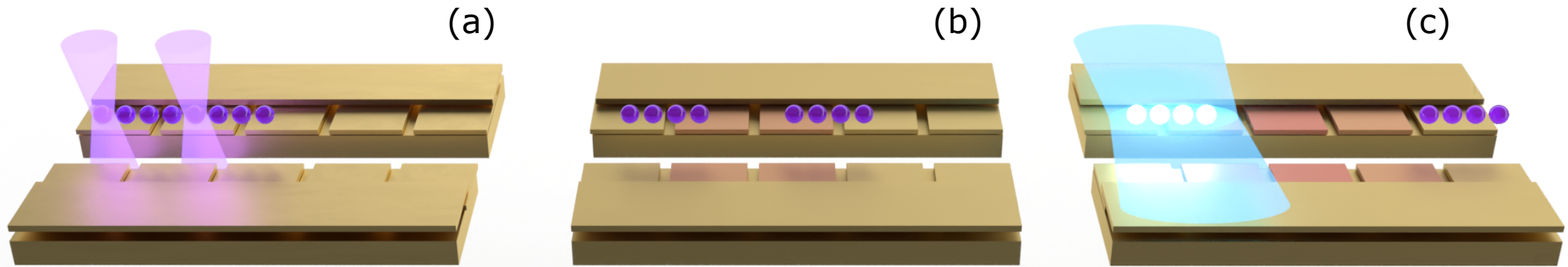


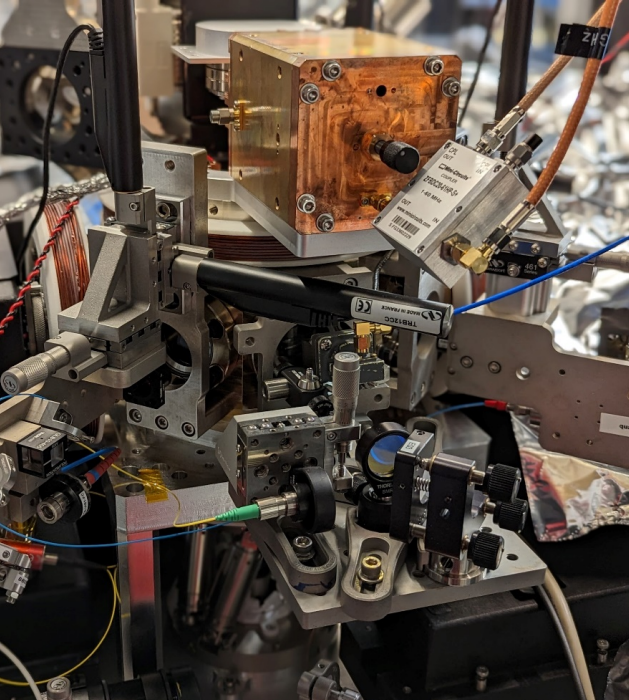
Marko Cetina

# $^{172}\text{Yb}$ Sympathetic Cooling



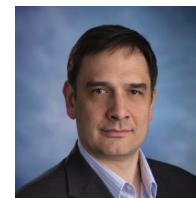
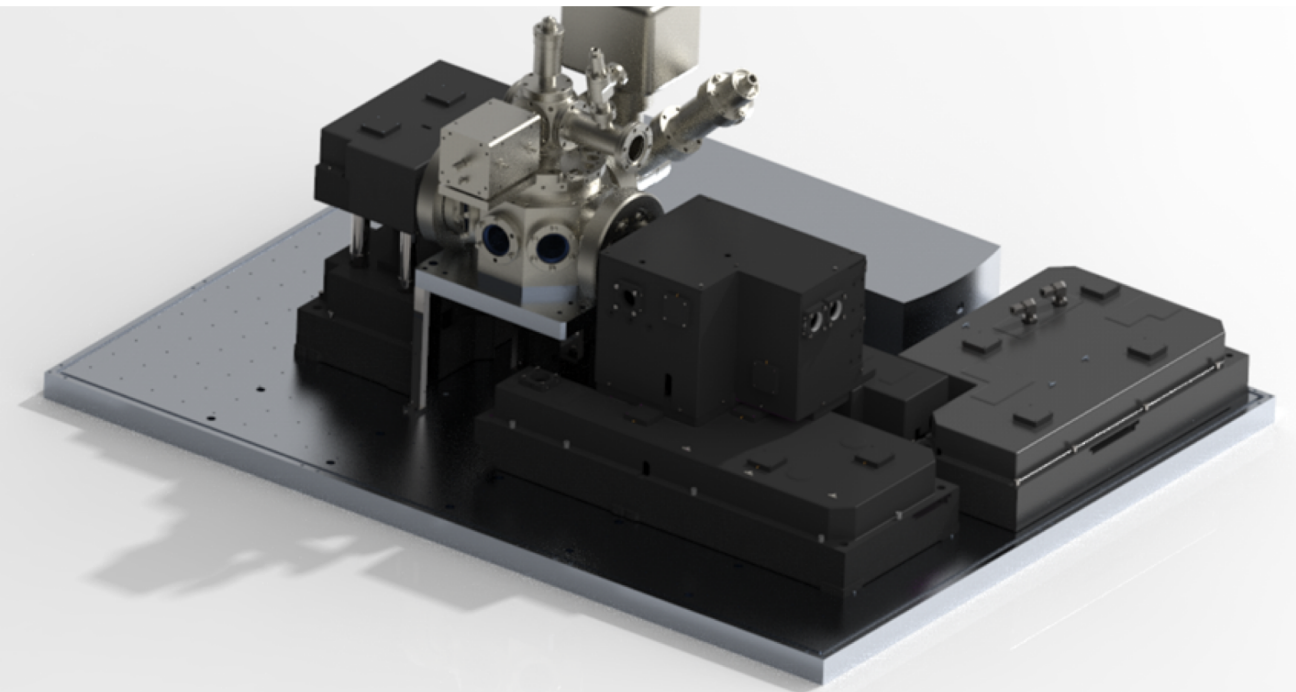
# Mid-circuit measurement via shuttling





# New Gold System

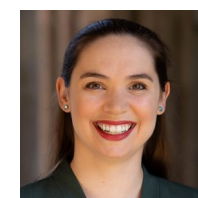
- Individual Addressing
- Fully-connected long chain
- Up to 32 qubits
- Improved stability and control



Alexander Kozhanov



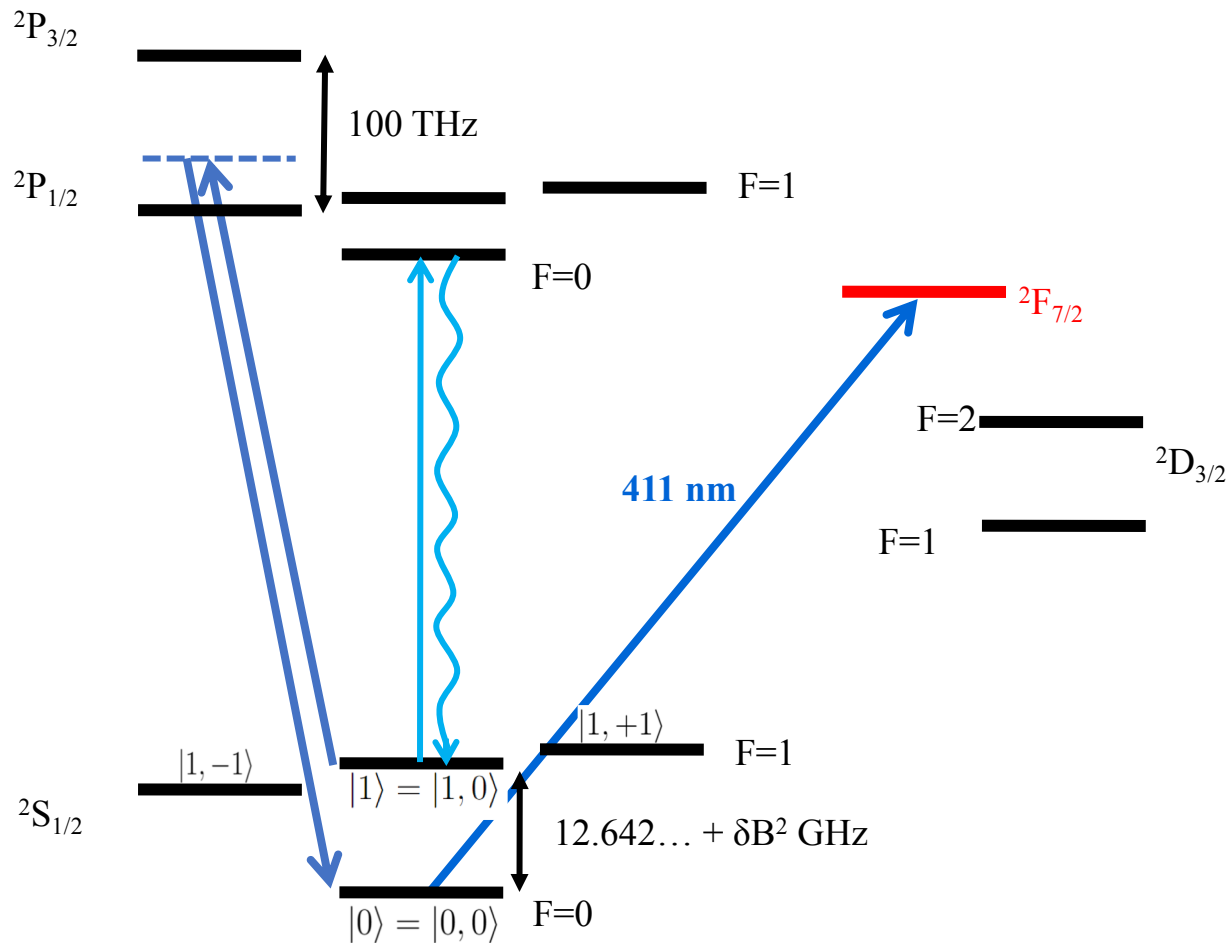
Chris Monroe



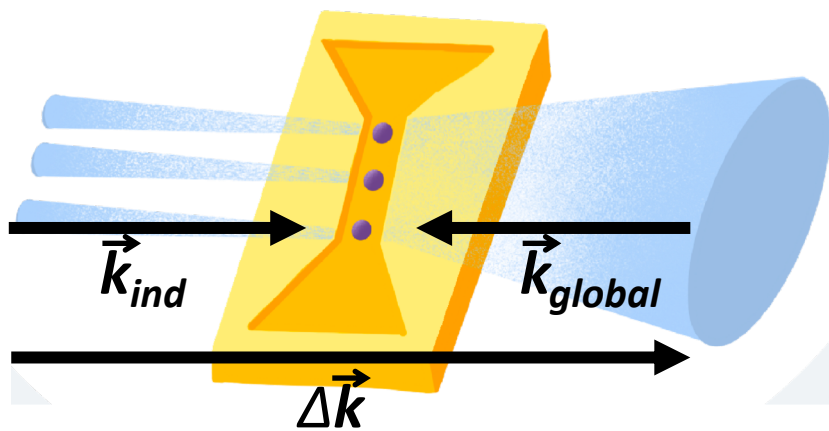
Crystal Noel



# $^{171}\text{Yb}$ Shelving



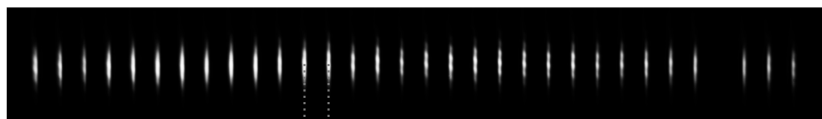
- Hide information during readout
- Reduce shuttling needed
- Possible F-state qubit operation



Raman  
system

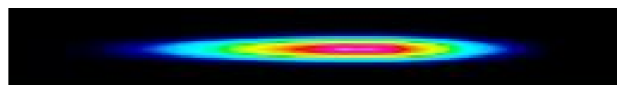


**L3HARRIS**™

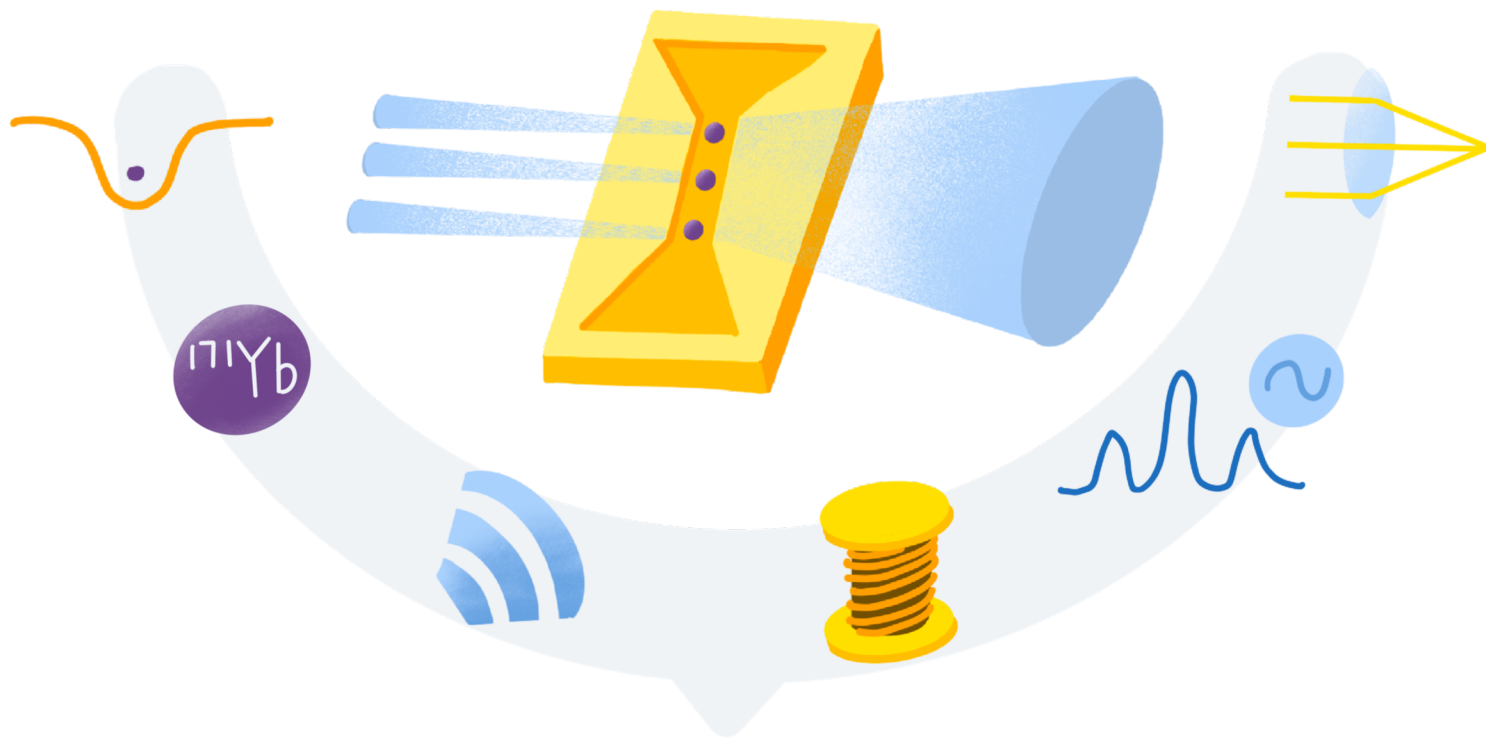


4.5  $\mu\text{m}$

Individual Raman Beams



Global Raman Beam

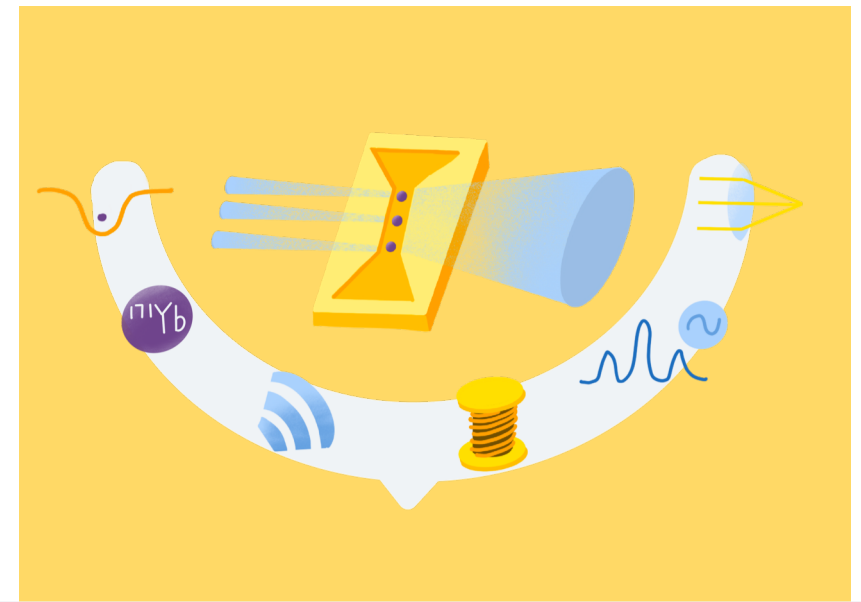


Systems level  
control

# Systems-level control



ARTIQ



ARTIQ Device Interface

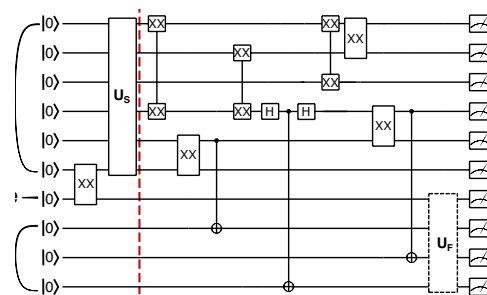
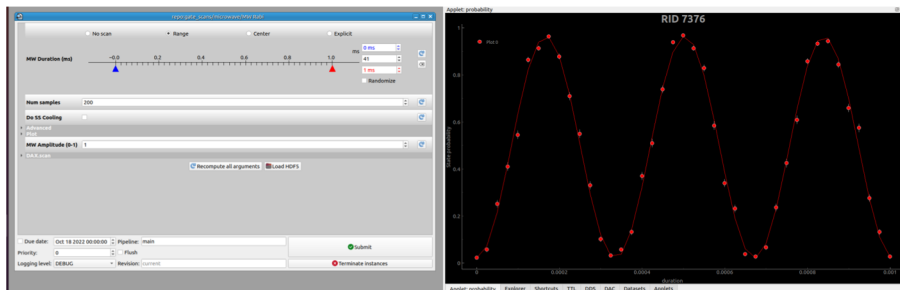
DAX System Registry

DAX Modules

DAX Services

Clients and Experiments

Gates and Circuits



# An MIPT in *Magic*

Niroula et al. arXiv: 2304.10481

# This work: Q-Lab at UMD

Duke  
UNIVERSITY



## Magic Team:

Pradeep Niroula (UMD)

Christopher David White (UMD)

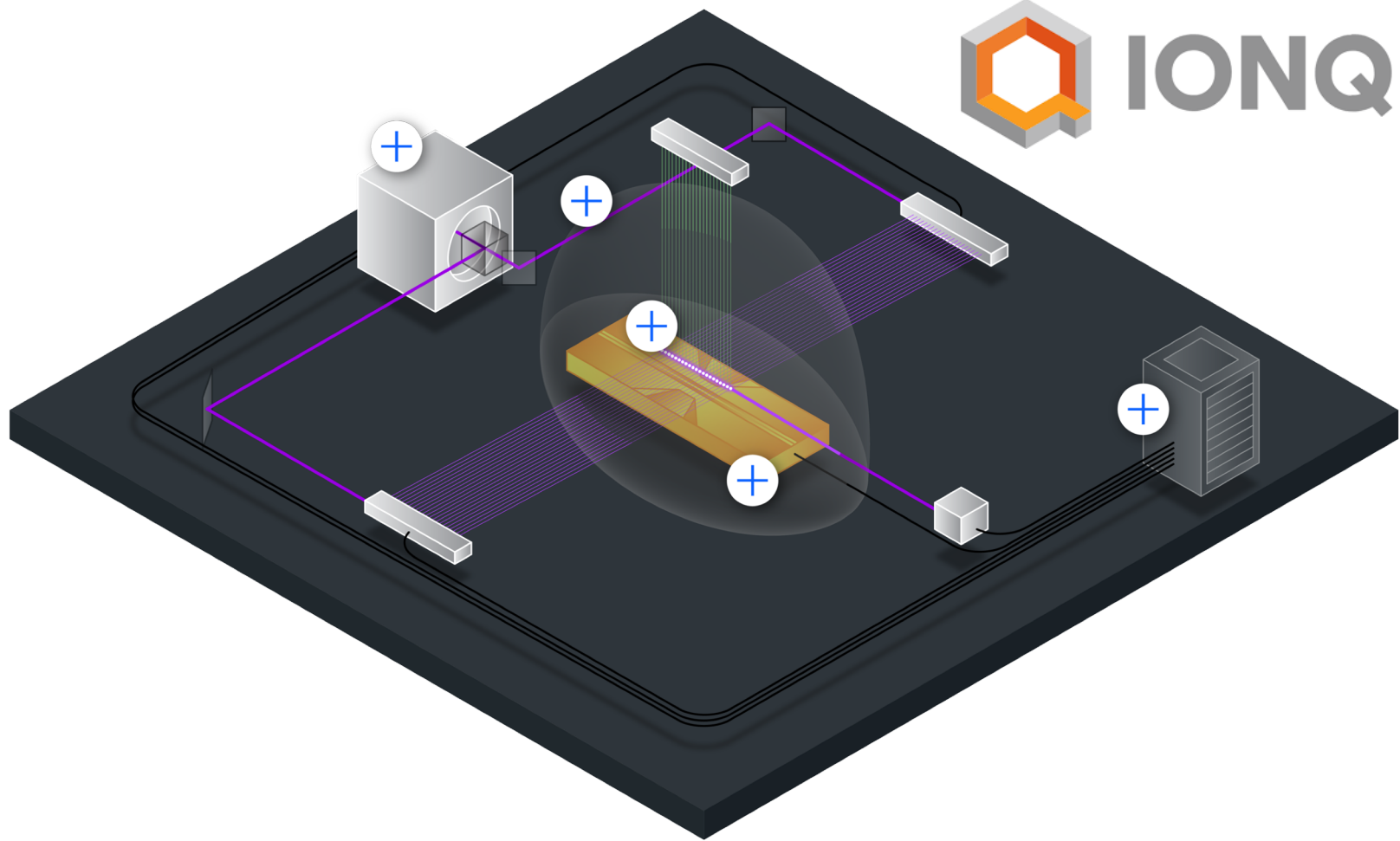
Qingfeng Wang (UMD)

Sonika Johri (IonQ)

Daiwei Zhu (IonQ)

Christopher Monroe (Duke/UMD/IonQ)

Michael Gullans (NIST/UMD)



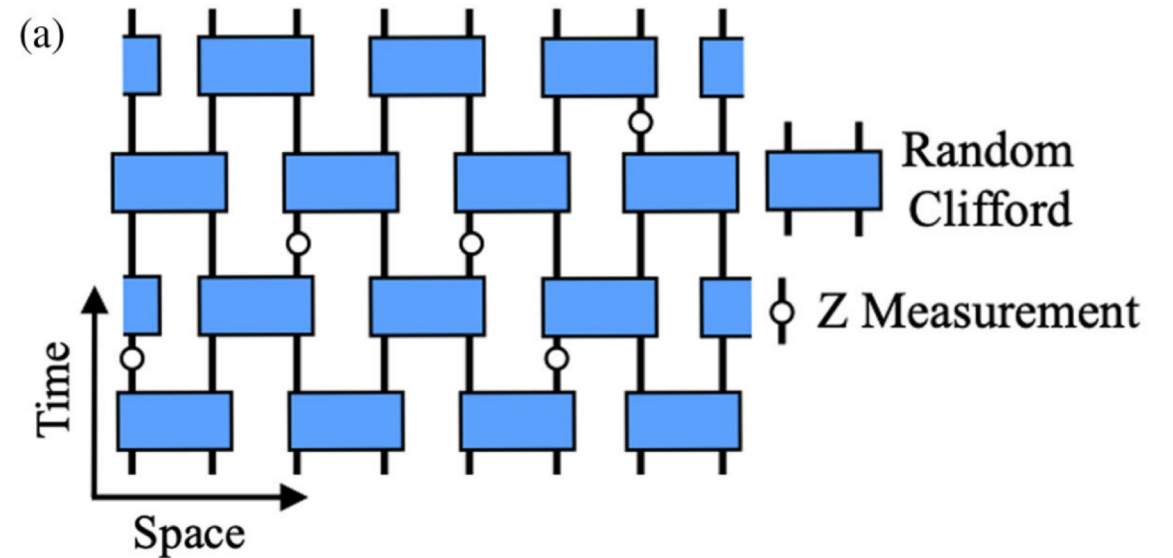
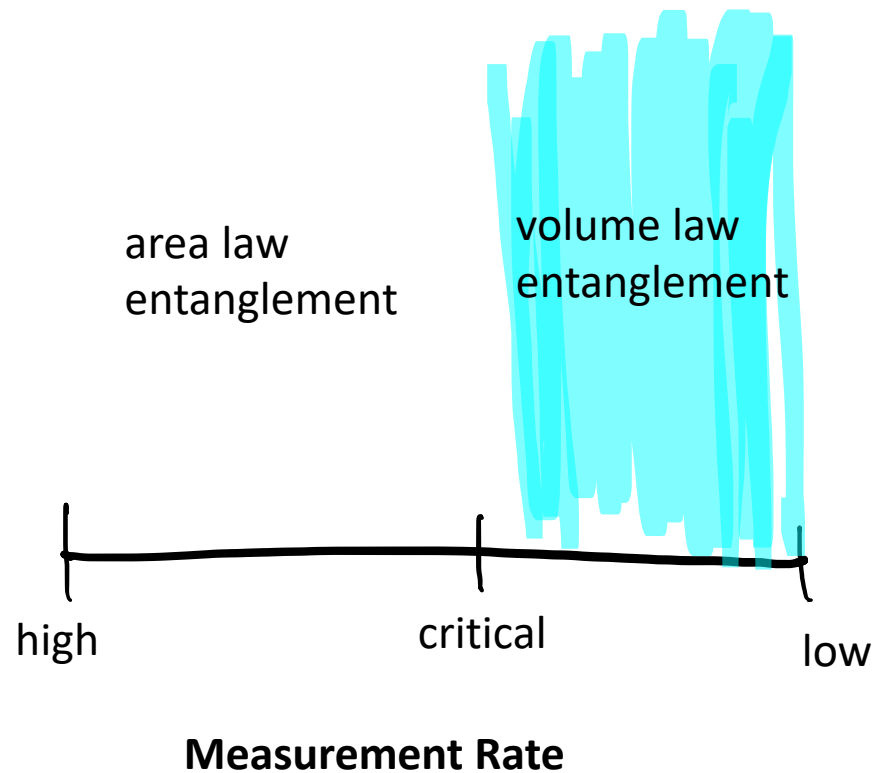
# The power of quantum computing?

- Superposition (coherence)
  - ~~Parallel computing!~~ → Measurement problem
- Entanglement
  - ~~GHZ states~~ → Easily simulated

**What is missing?**  
**Magic (nonstabilizerness)**

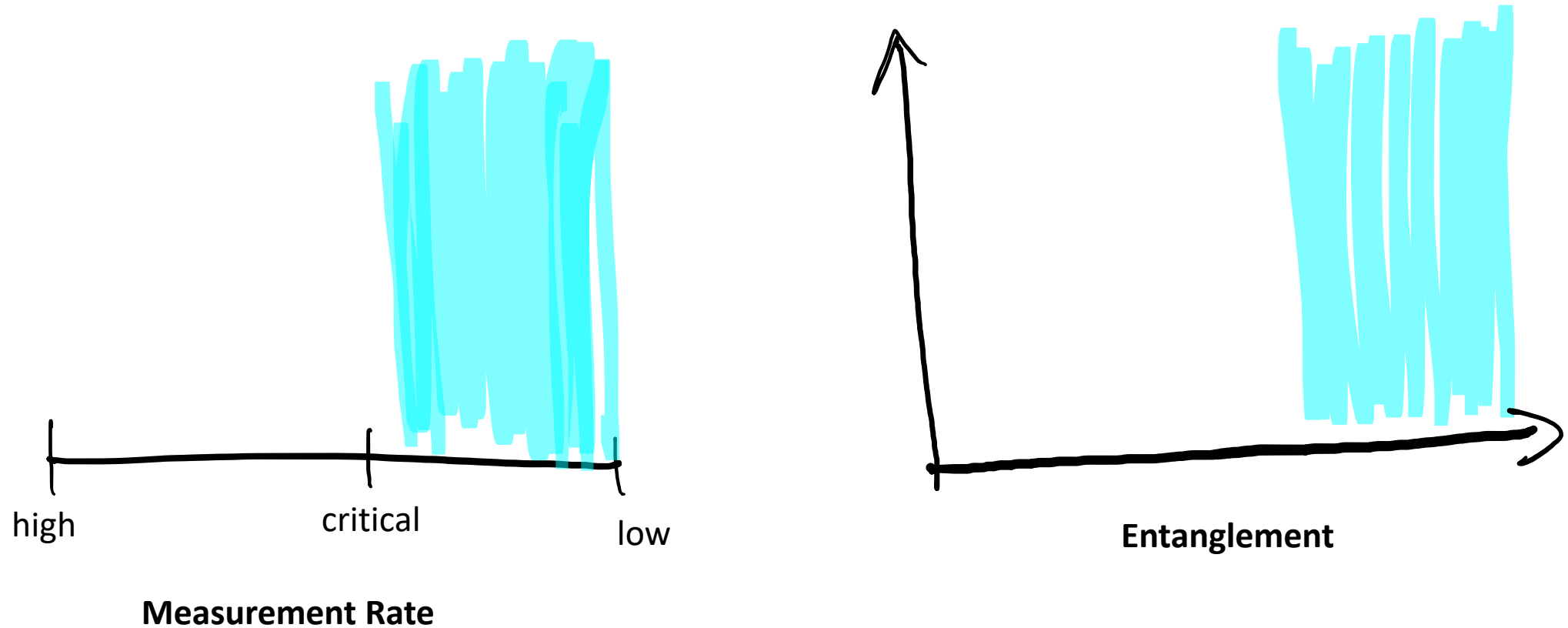
1. *Resource*: V. Veitch, S. A. H. Mousavian, D. Gottesman, J. Emerson, New Journal of Physics 16, 013009 (2014). ArXiv: 1307.7171.
2. *Complexity*: K. Bu, R. J. Garcia, A. Jaffe, D. E. Koh, L. Li, arXiv:2204.12051 [math-ph, physics:quant-ph] (2022).
3. *AdS-CFT*: C. D. White, C. Cao, B. Swingle, Physical Review B 103, 075145 (2021).
4. *Chaos*: L. Leone, S. F. Oliviero, Y. Zhou, A. Hamma, Quantum 5, 453 (2021).

# Measurement induced phase transition

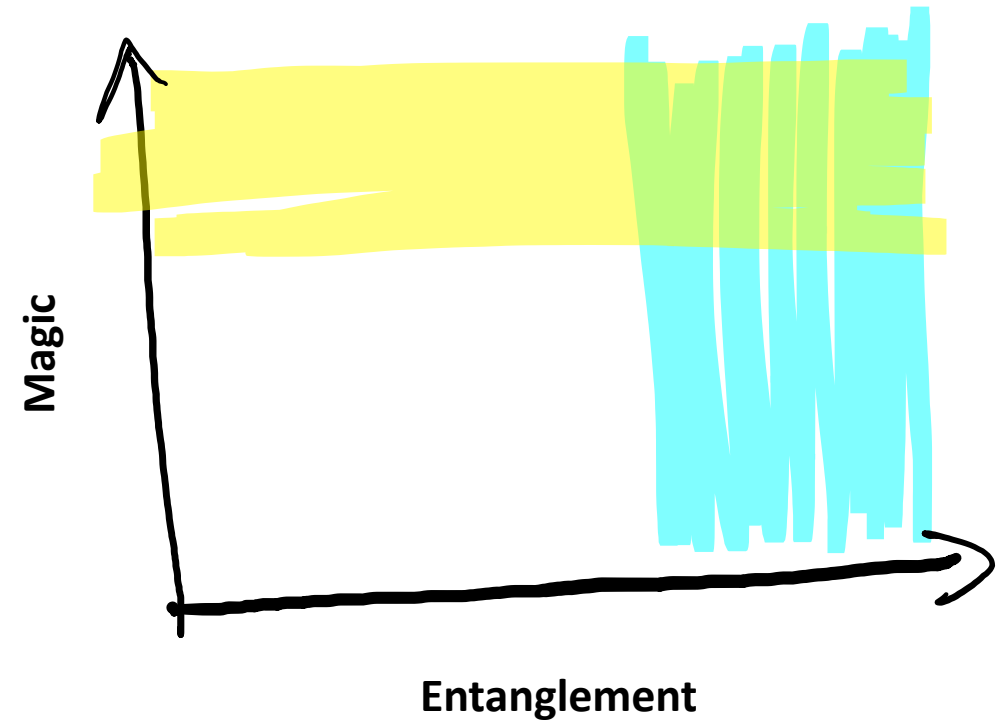
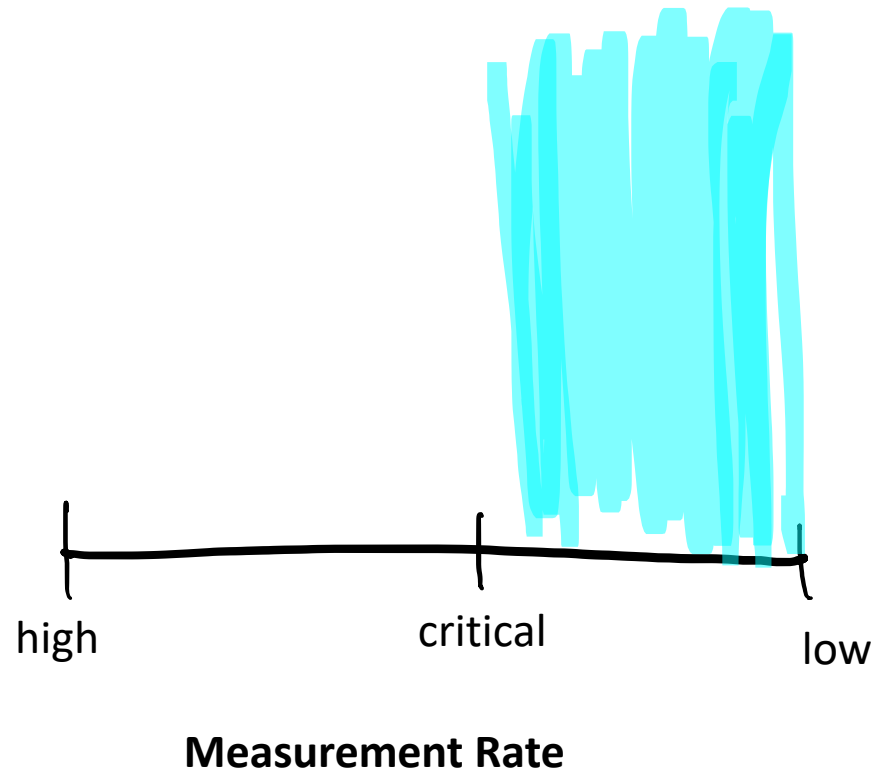




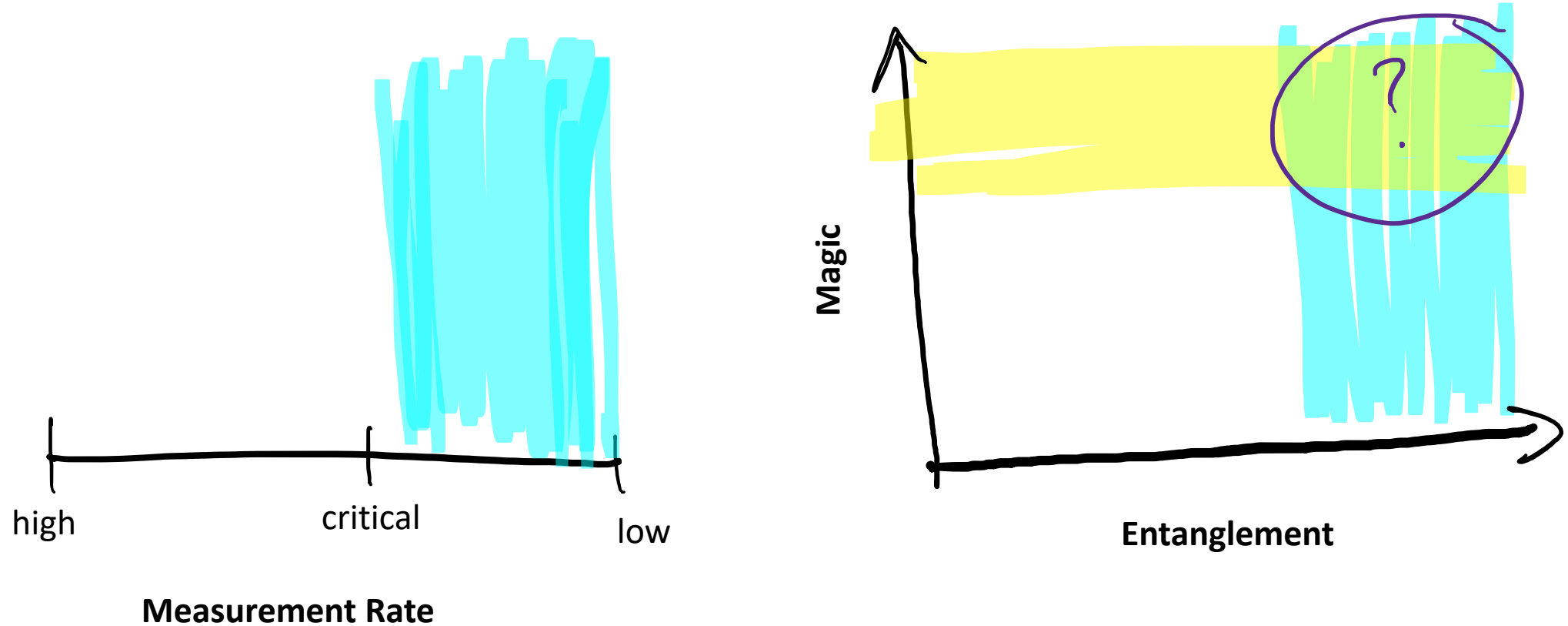
# Understanding quantum advantage



# Understanding quantum advantage


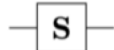
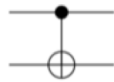


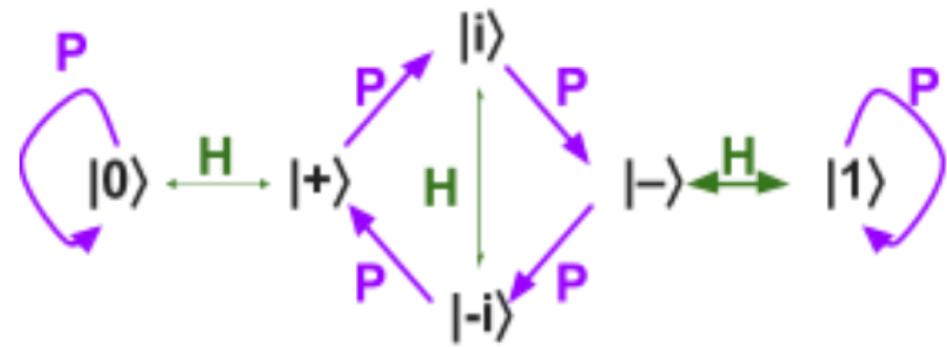
# Understanding quantum advantage



# Stabilizer states have no magic

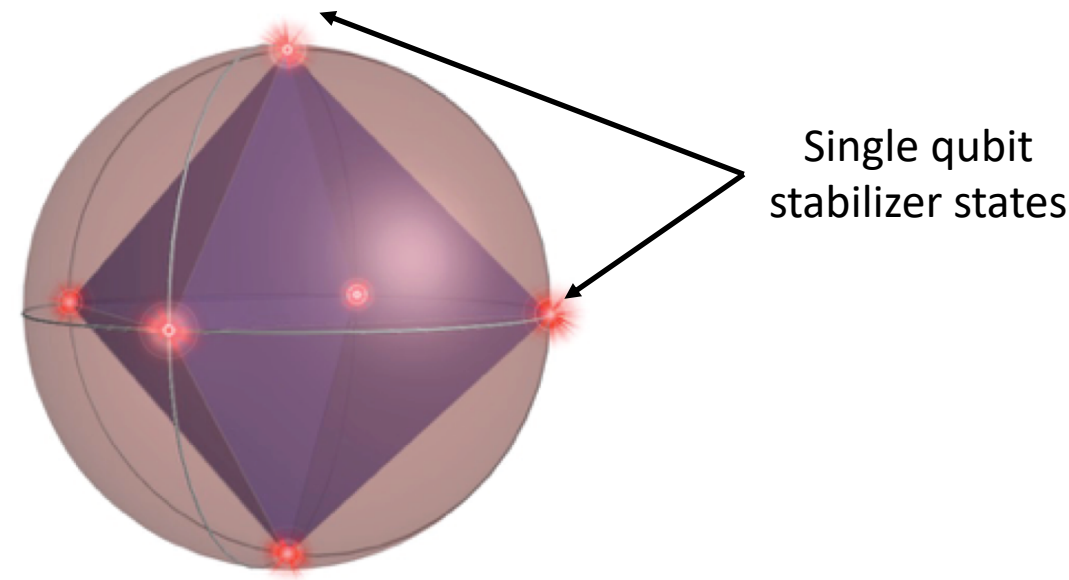
- Generated from a stabilizer circuit starting from 00000...
- Stabilizer circuits are made of stabilizer gates (Clifford)
- Cliffords: CNOT, H, P(S)

Hadamard (H)		$\frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$
Phase (S, P)		$\begin{bmatrix} 1 & 0 \\ 0 & i \end{bmatrix}$
Controlled Not (CNOT, CX)		$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}$



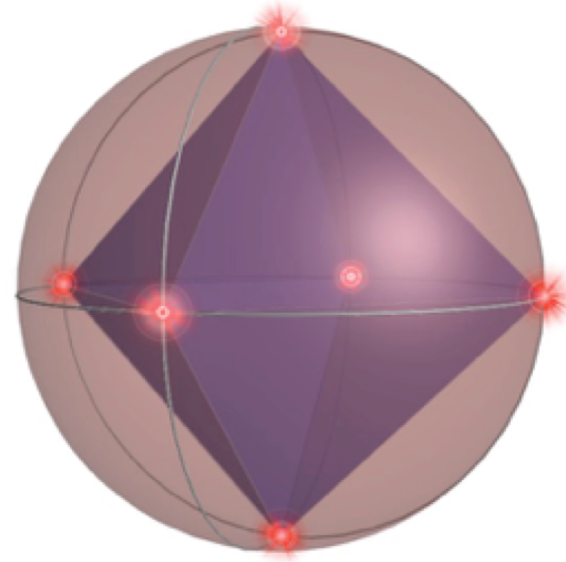
# Stabilizer states have no magic

- Generated from a stabilizer circuit starting from  $00000\dots$
- Stabilizer circuits are made of stabilizer gates (Clifford)
- Cliffords: CNOT, H, P(S)



# Stabilizer circuits

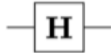
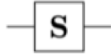
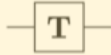
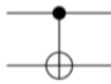
- Gottesman-Knill Theorem: stabilizer circuits are efficiently simulatable classically<sup>1,2</sup>
- Quantum advantage related to nonstabilizerness (magic)?



1. D. Gottesman, arXiv preprint quant-ph/9807006 (1998).
2. S. Aaronson, D. Gottesman, Physical Review A 70, 052328 (2004)

# From stabilizer to magical...

- Add T gate for magic
- Magic state distillation<sup>1-4</sup>
  - Required for stabilizer code FTQC
  - Resource intensive
- Magic can be used to measure noise<sup>5</sup>

Hadamard (H)		$\frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$
Phase (S, P)		$\begin{bmatrix} 1 & 0 \\ 0 & i \end{bmatrix}$
$\pi/8$ (T)		$\begin{bmatrix} 1 & 0 \\ 0 & e^{i\pi/4} \end{bmatrix}$
Controlled Not (CNOT, CX)		$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}$

1. S. Bravyi, A. Kitaev, Physical Review A 71, 022316 (2005). ArXiv: quant-ph/0403025.

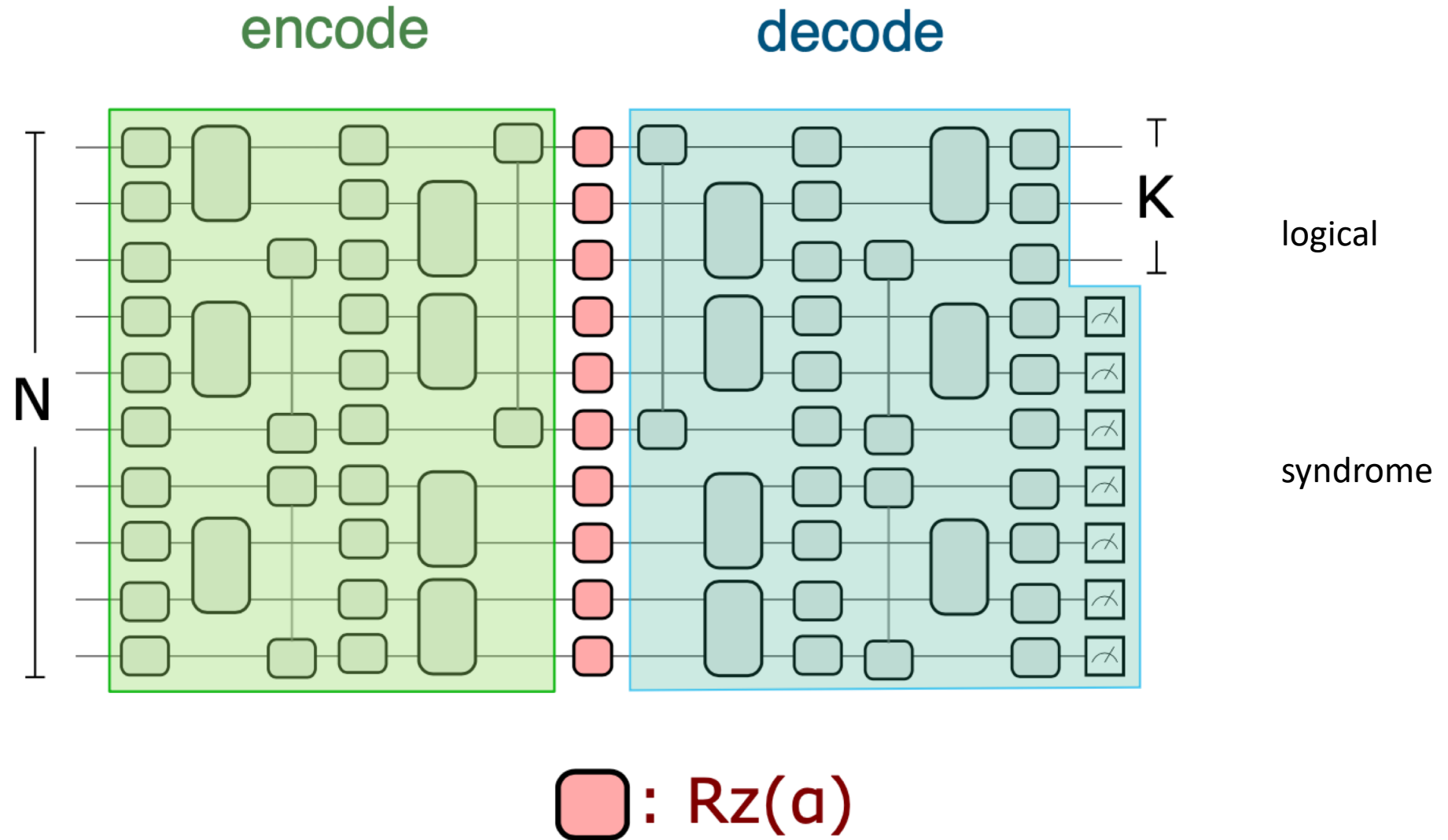
2. A. G. Fowler, M. Mariantoni, J. M. Martinis, A. N. Cleland, Physical Review A 86, 032324 (2012).

3. J. O’Gorman, E. T. Campbell, Physical Review A 95, 032338 (2017).

4. E. T. Campbell, B. M. Terhal, C. Vuillot, Nature 549, 172 (2017).

5. S.F.E. Oliviero, L. Leone, A. Hamma, S. Lloyd NPJ Quantum Information 8, 148 (2022).

# Random circuit model





# What makes a good measure of magic?

- Zero for a stabilizer state
- Non-increasing under stabilizer circuits (Clifford gates)
- Sub-additive for product states  $f(\sigma \otimes \rho) \leq f(\sigma) + f(\rho)$

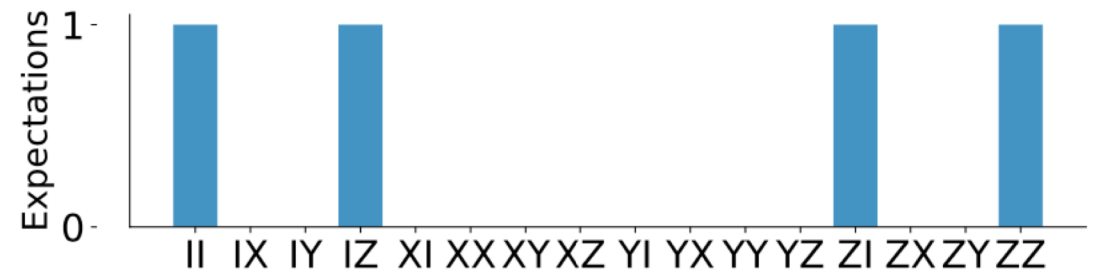
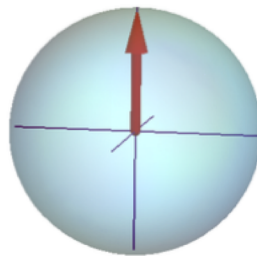
# Expansion into Pauli basis

$$\rho = |0\rangle\langle 0| = \mathbf{1} + \mathbf{Z}$$

$\rho$  is stabilized by  $\mathbf{1}$  and  $\mathbf{Z}$

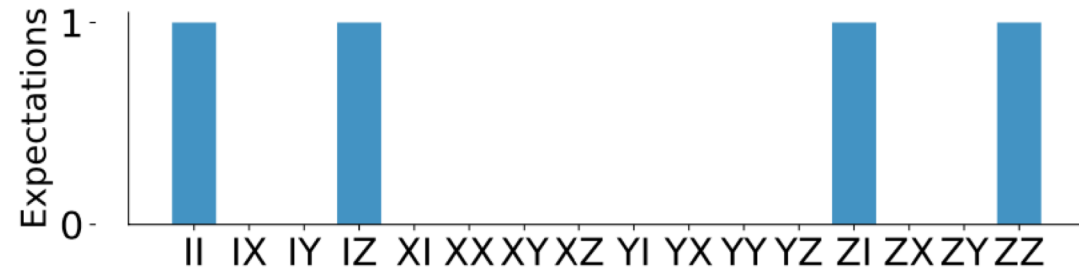
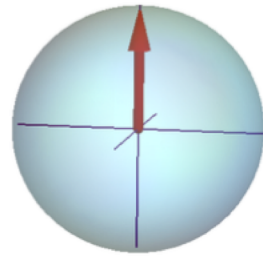
$$\rho = |00\rangle\langle 00|$$

is stabilized by  $\mathbf{II}, \mathbf{IZ}, \mathbf{ZI}, \mathbf{ZZ}$

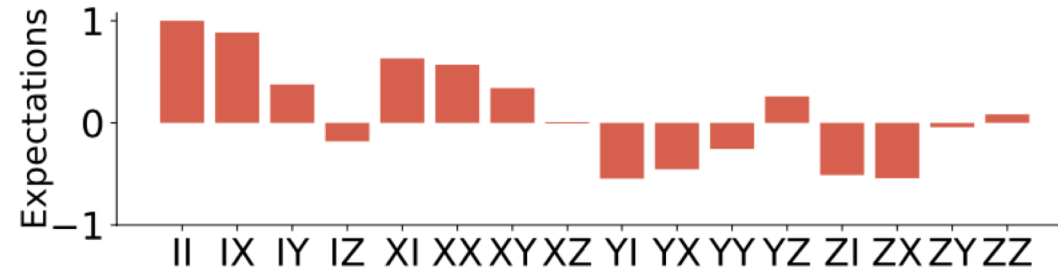
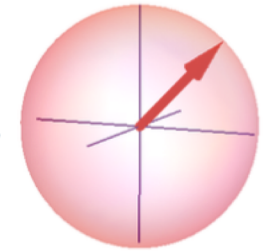


# Expansion into Pauli basis

**Stabilizer state**



**Haar random state**



# Second Stabilizer Renyi Entropy

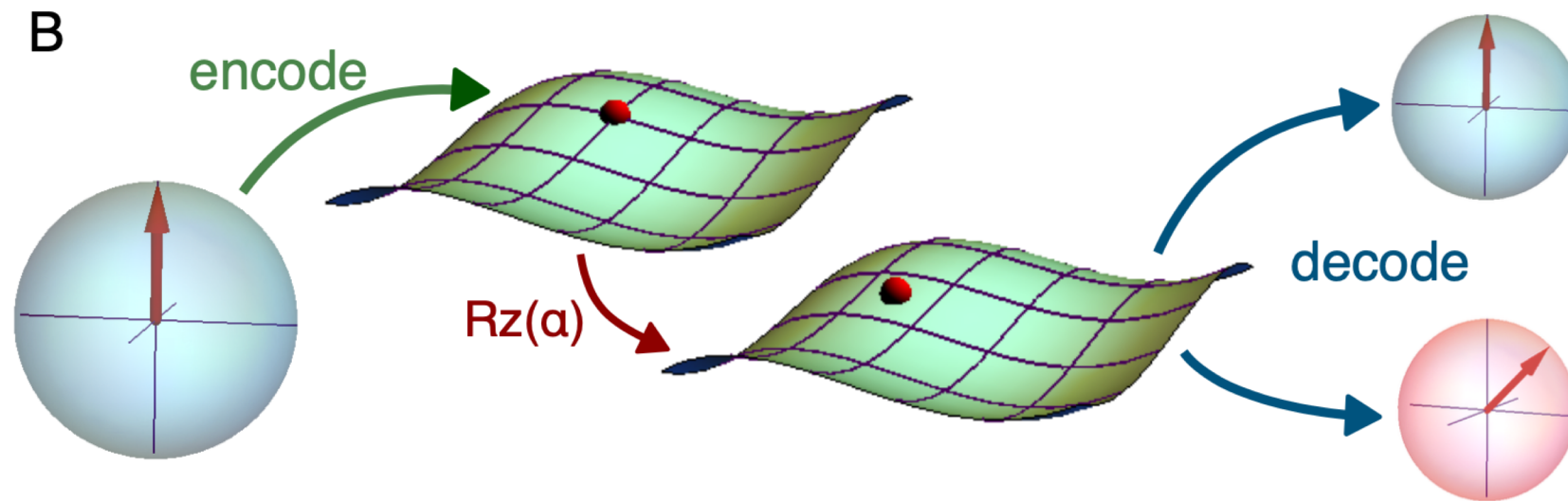
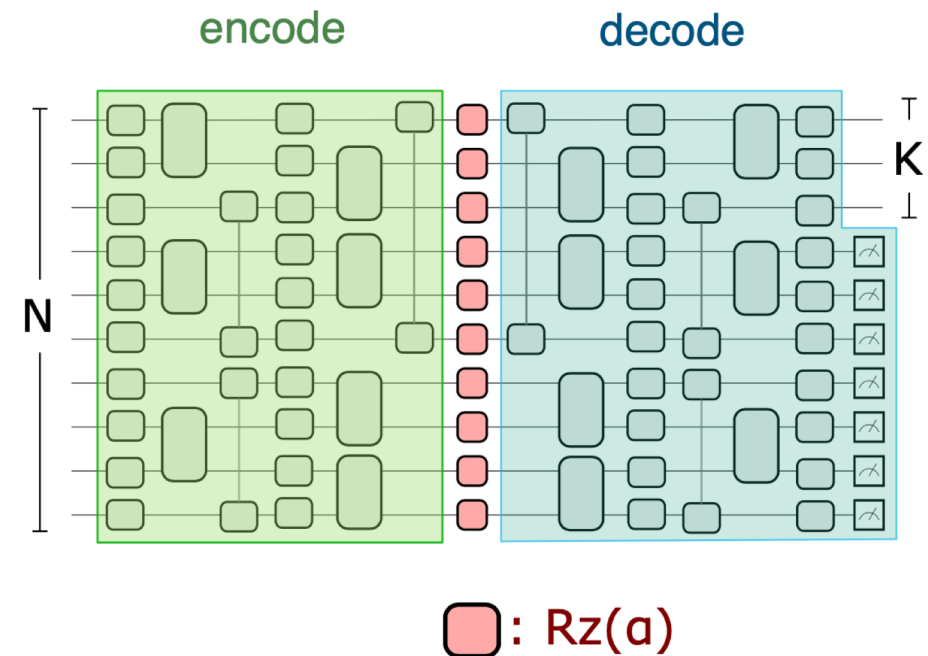
- Spread of  $\rho$  when expanded in basis of Pauli operators<sup>1</sup>

$$M_2(\rho) = -\log \frac{1}{2^N} \sum_{P \in \mathcal{P}} \text{Tr}(\rho P)^4$$

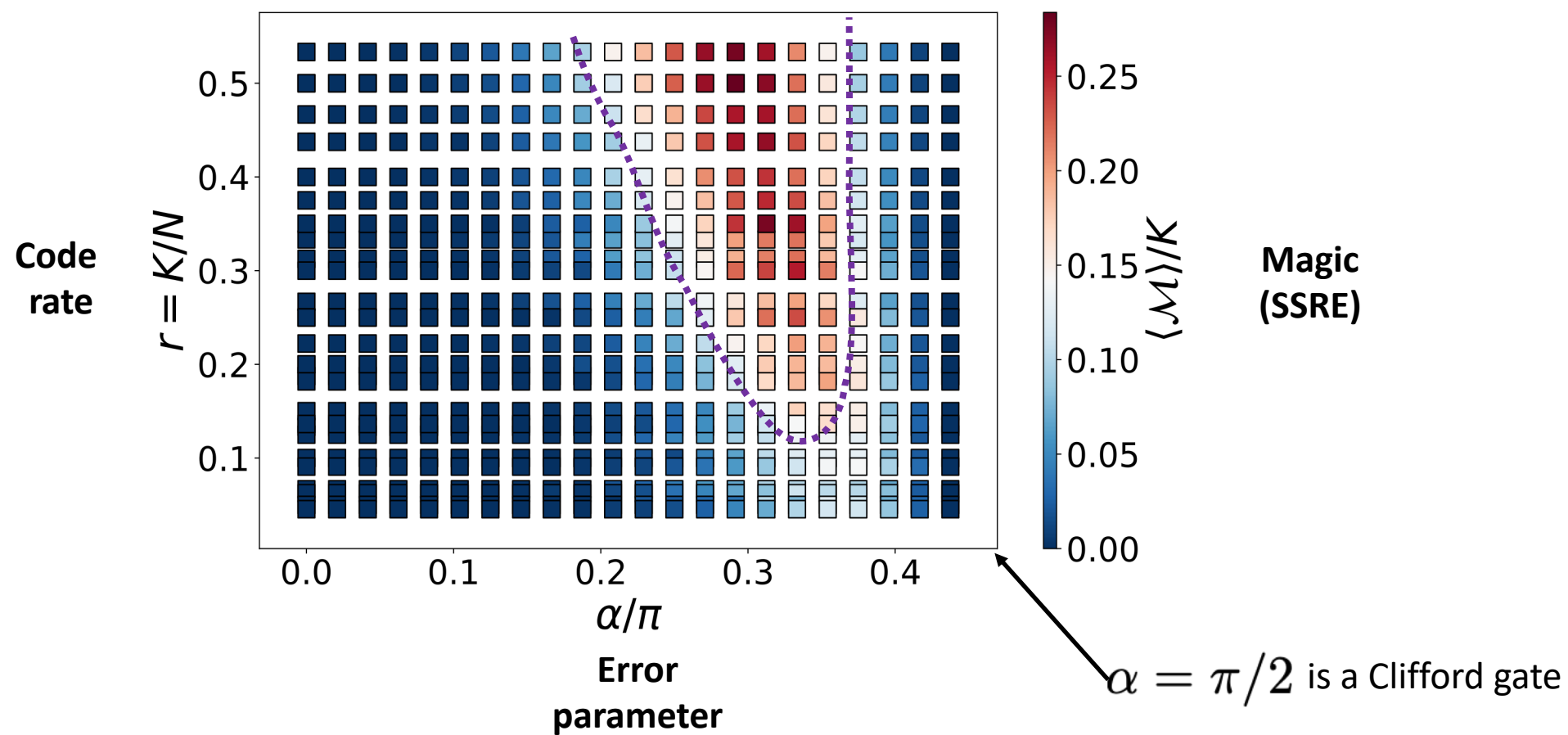
- Requires full (or partial<sup>2</sup>) knowledge of  $\rho$

1. L. Leone, S. FE Oliviero, and A. Hamma. *Physical Review Letters* 128.5 (2022): 050402.
2. S.F.E. Oliviero, L. Leone, A. Hamma, S. Lloyd *NPJ Quantum Information* 8, 148 (2022).

# Random circuit model

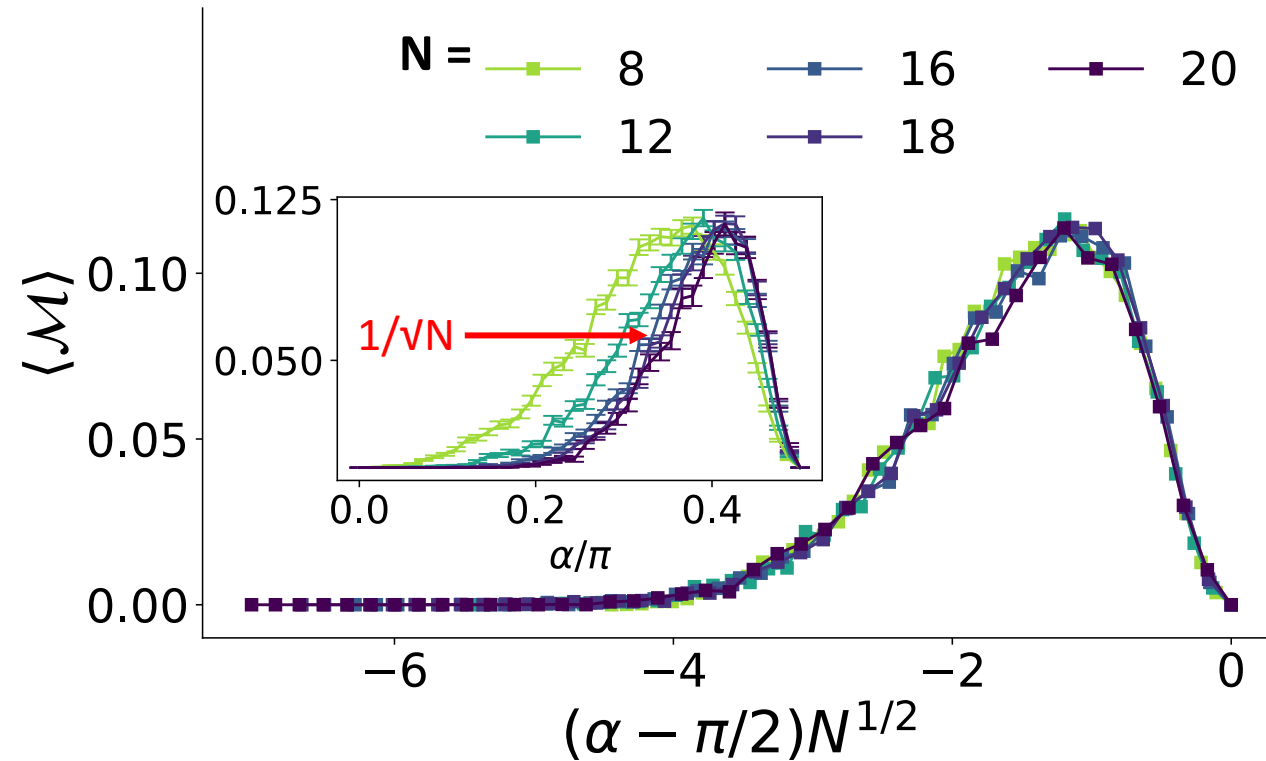


# Phase transition in magic



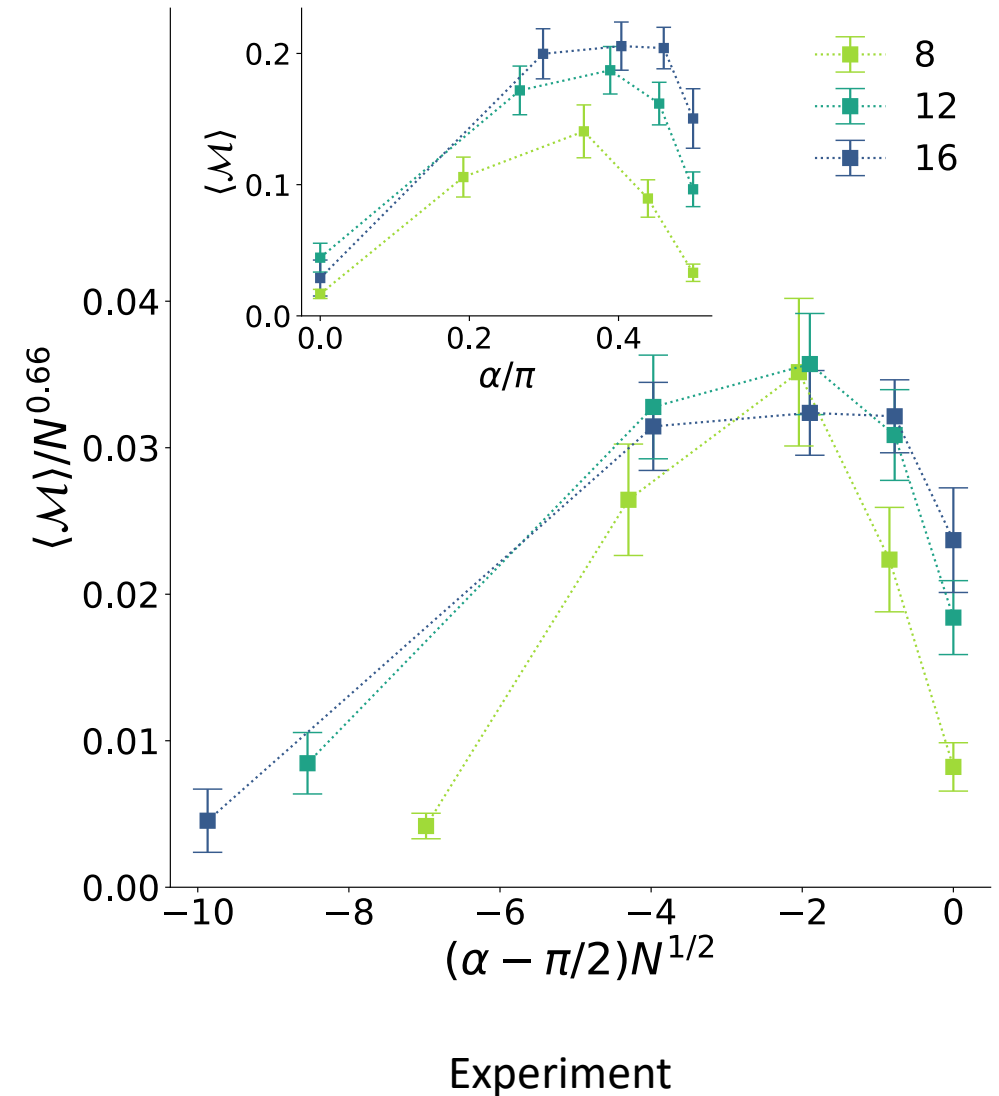
# Vanishing Rate Code

- Magic of the logical state when  $K=1$  (code rate  $r=1/N$ )



# Error mitigation strategies

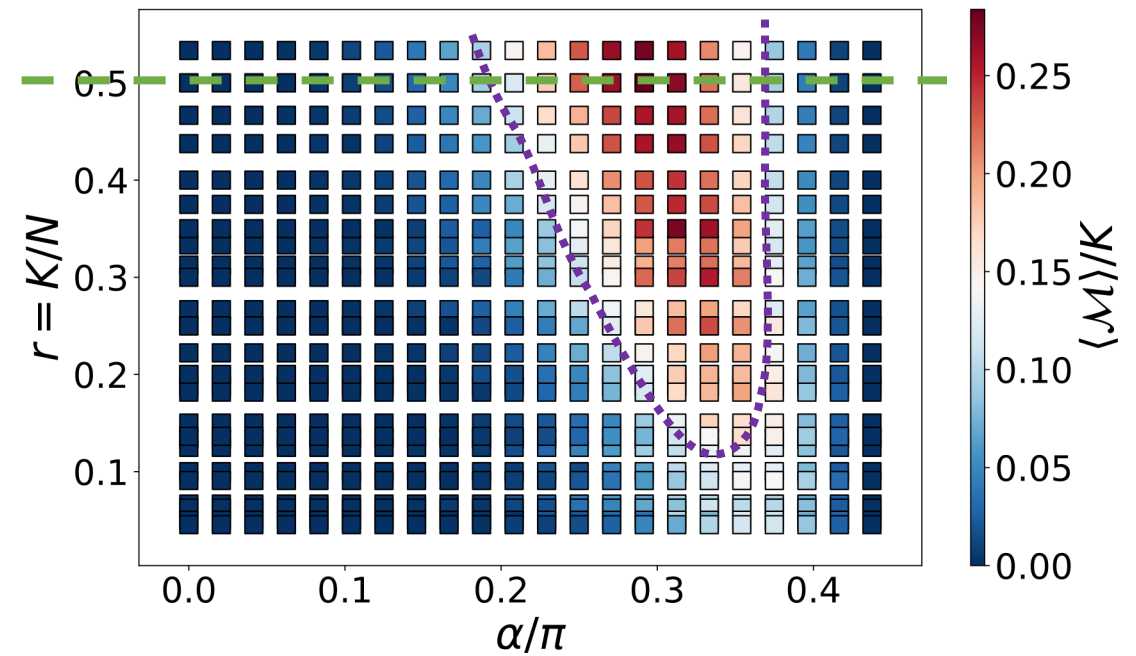
- Post-selection: Syndromes grouped into classes with equivalent logical qubit actions using classical simulations
- Decoherence: Project to nearest pure state in post processing





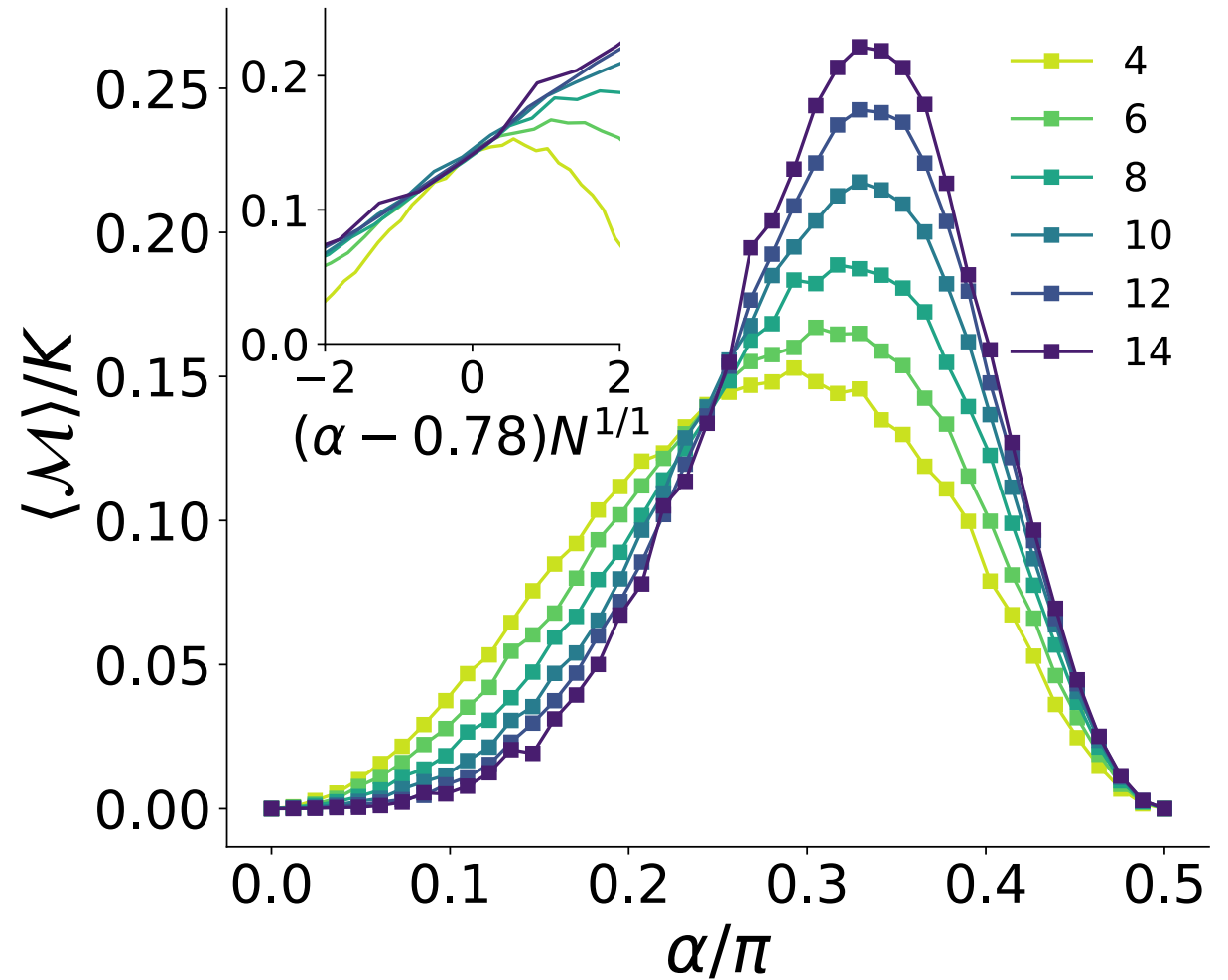
# Finite rate code

- $K = rN$  for fixed  $r$



# Finite rate code

- $K = rN$  for fixed  $r = \frac{1}{2}$
- SSRE takes full tomography



# Basis minimized measurement entropy

- The entropy of the Born probability distribution of measurement outcomes, minimized over the finite set of possible stabilizer measurement bases

Example:

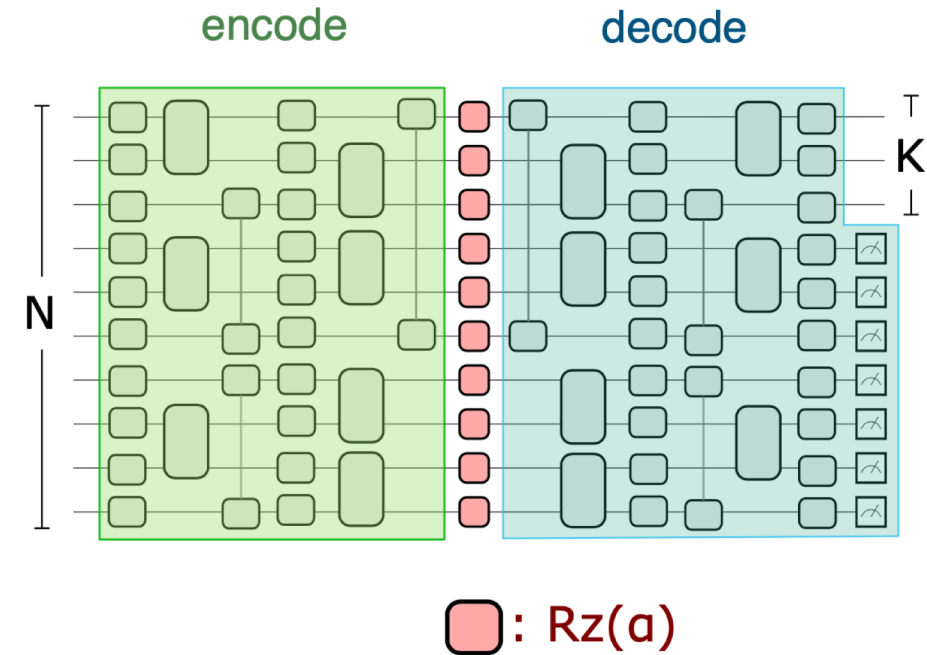
Measure  $|00\rangle$  in the x-basis, four equally probable measurement outcomes  $|\pm \pm\rangle$  with  $S=2$

Measure  $|00\rangle$  in the z-basis, only one outcome  $|00\rangle$  with  $S=0$

BMME = 0

# Experimental magic measure

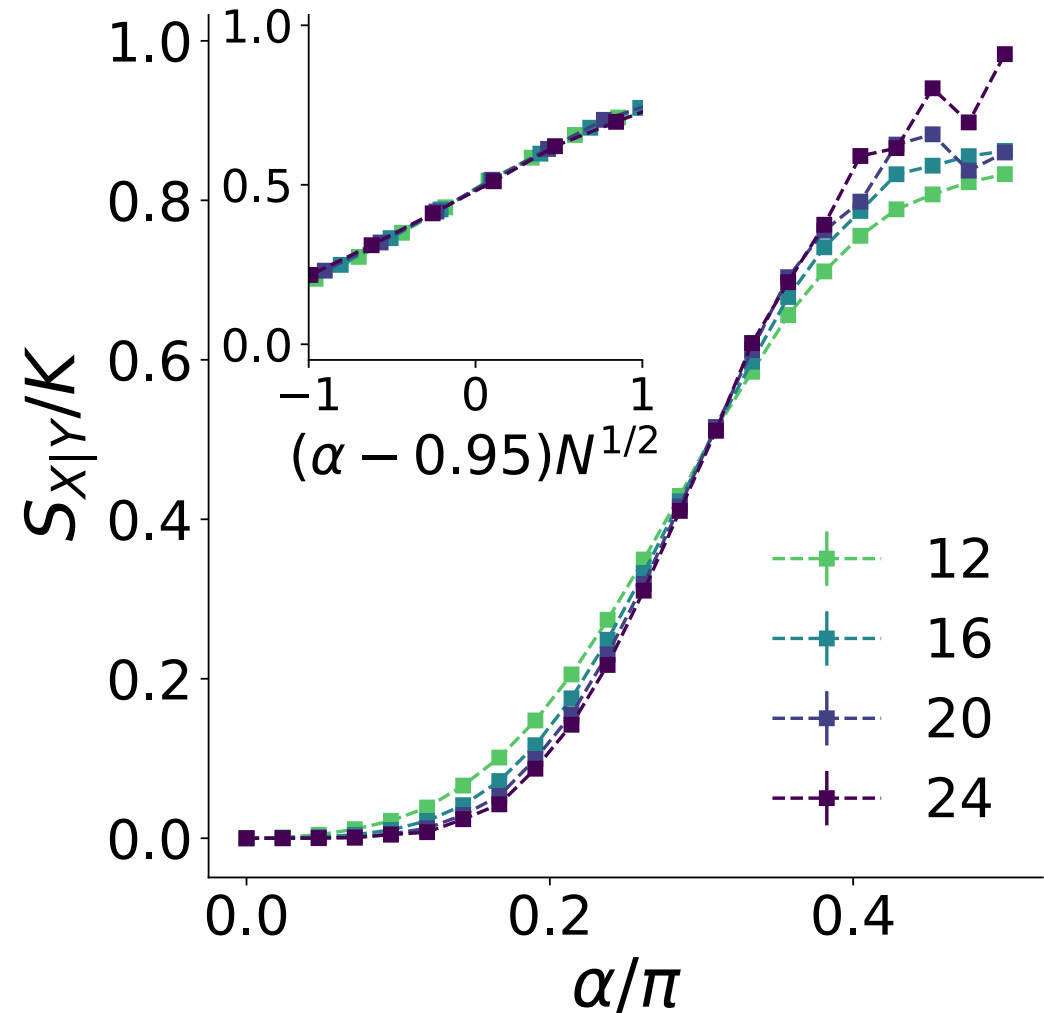
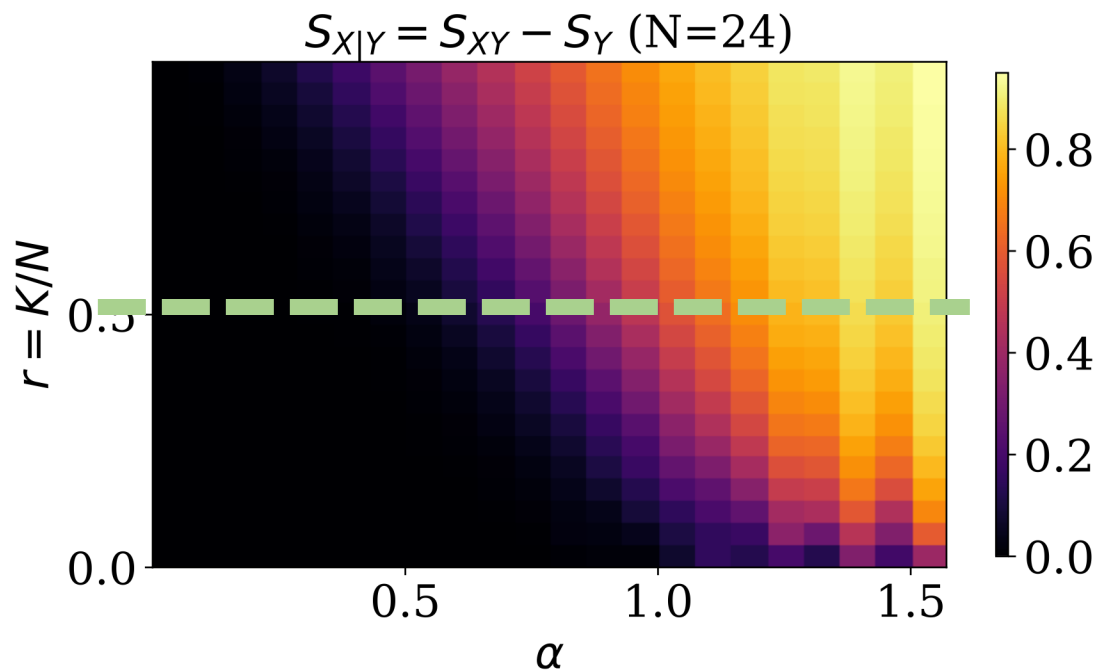
- Avoid full state tomography
- Conditional entropy :  $S_{X(B)|Y} = S_{X(B)Y} - S_Y$ 
  - Uncertainty about logical space, given syndrome.
- Basis minimized conditional entropy  $\min_B S_{X(B)|Y}$
- Error mitigation using classical simulation



$$S_X = - \sum_x p(x) \log \tilde{p}(x)$$

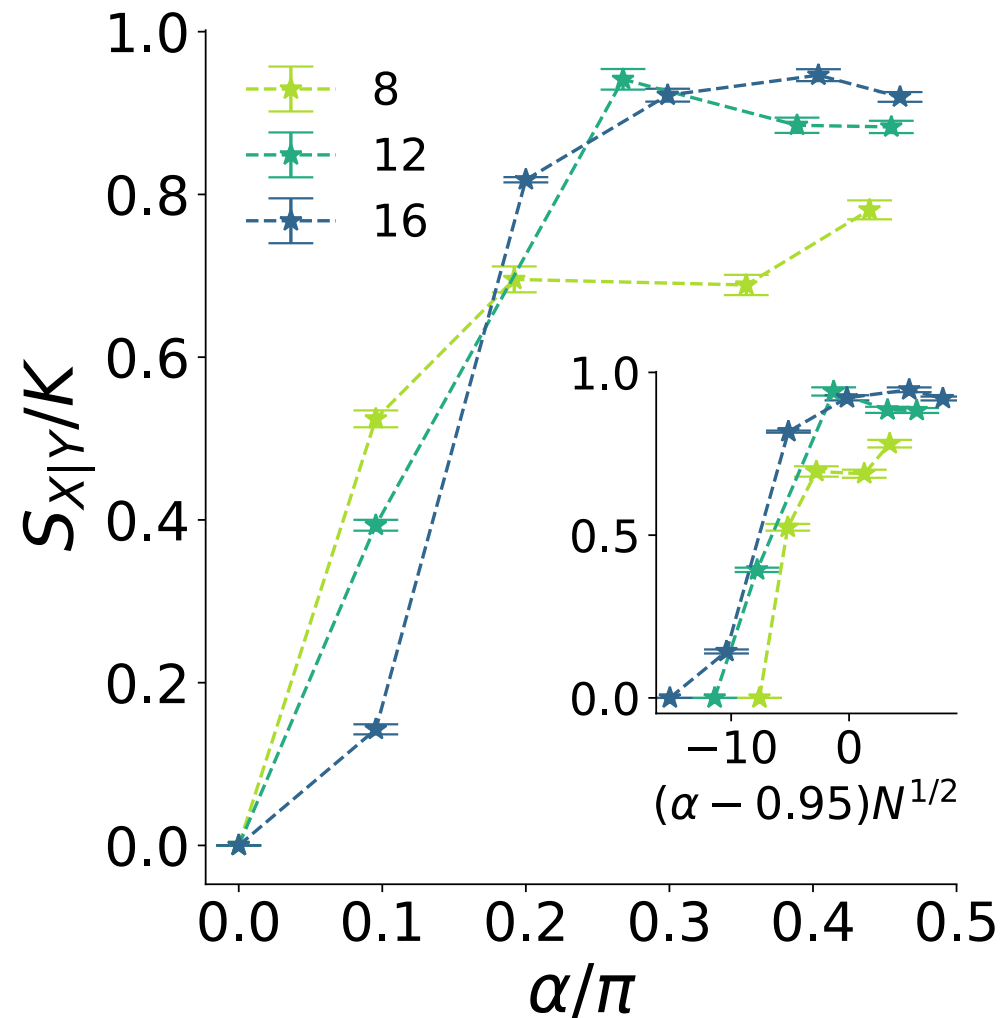
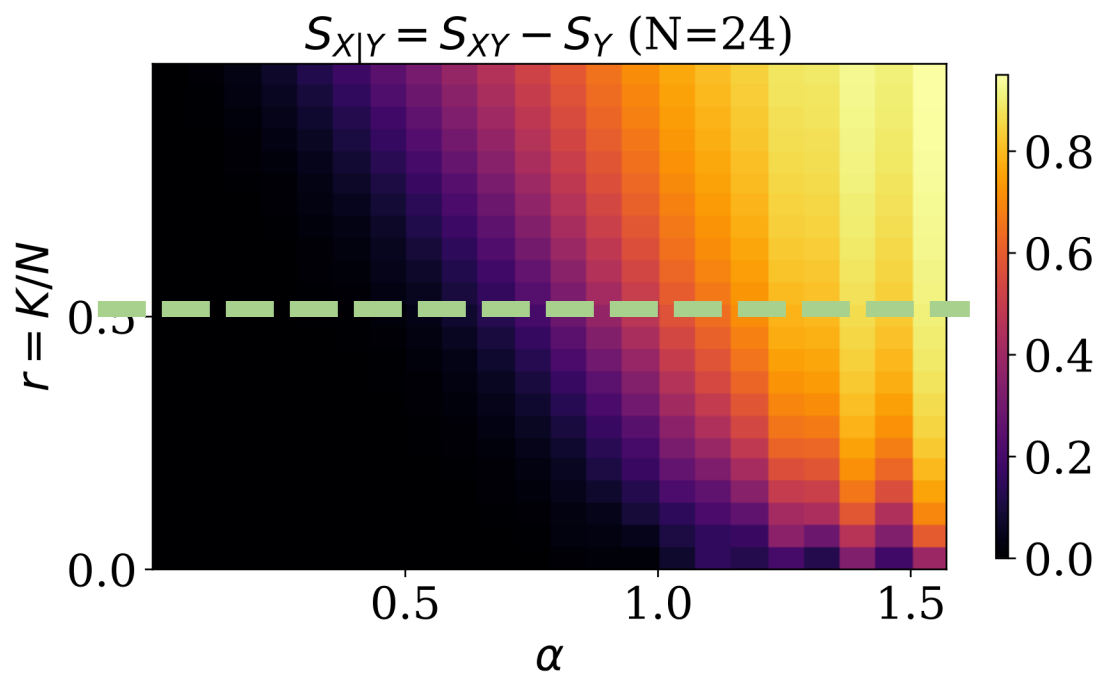
# Finite Rate Code: Conditional Entropy

- The conditional entropy is a good measure for the phase where magic is suppressed.

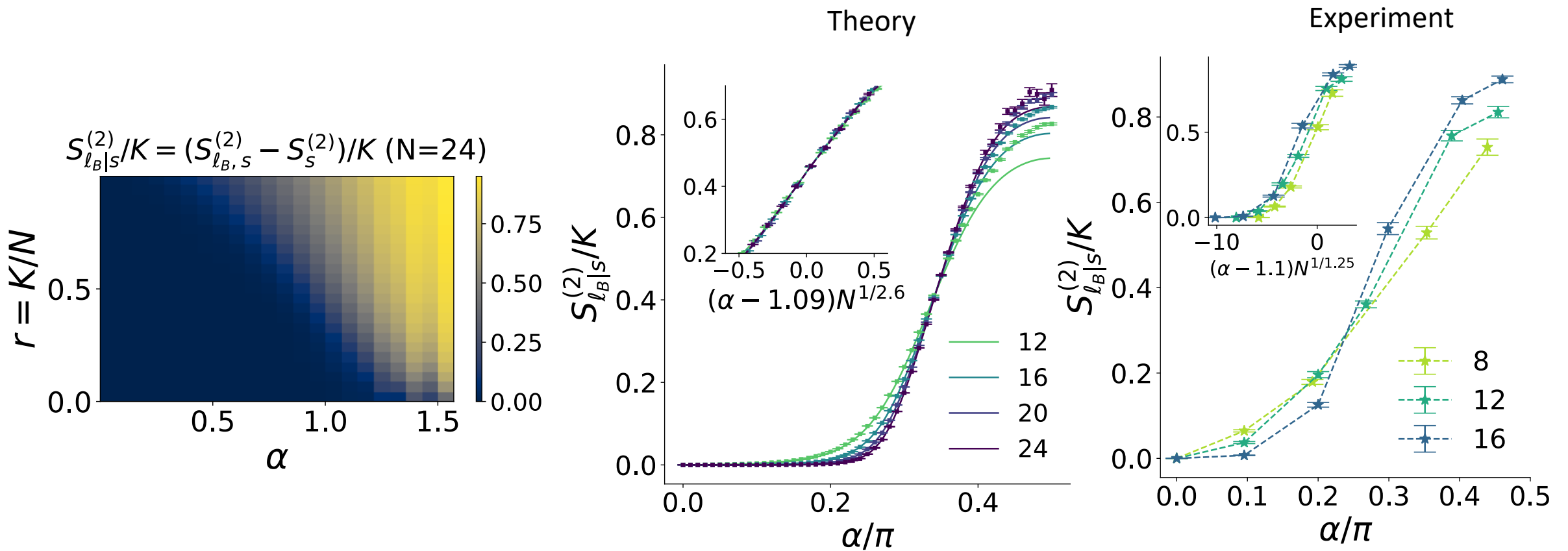


# Finite Rate Code: Conditional Entropy

- Can also observe this in experiment.

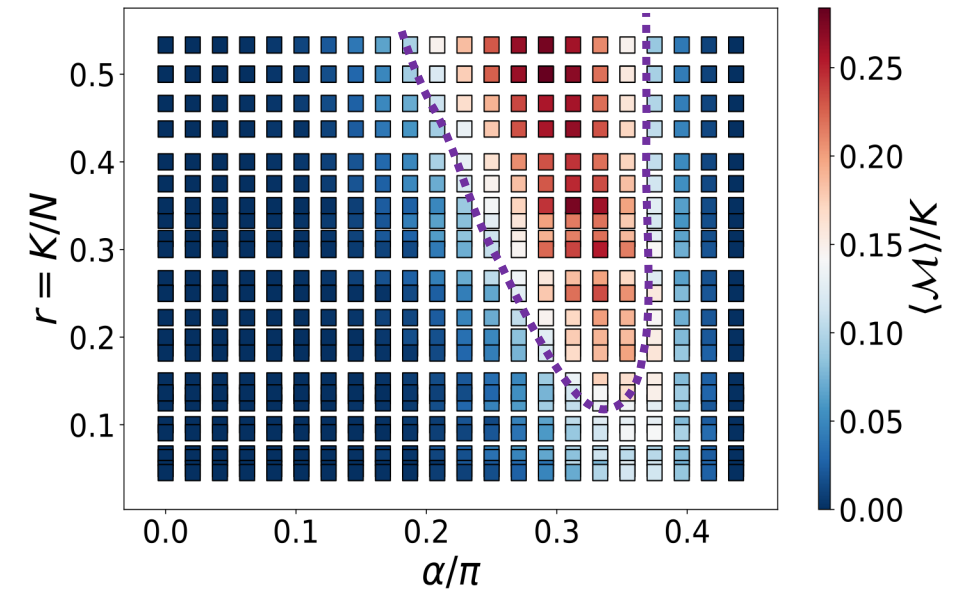


# Finite rate code: Renyi approximation of conditional entropy



# Outlook

- Efficient magic measures
- Expansion of MIPT beyond entanglement
  - Resource generation
  - Correlation generation
  - Resource destruction
- Magic state distillation from noise?





# Thank you!

## Magic Team:

Pradeep Niroula (UMD)

Christopher David White (UMD)

Qingfeng Wang (UMD)

Sonika Johri (IonQ)

Daiwei Zhu (IonQ)

Christopher Monroe (Duke/UMD/IonQ)

Michael Gullans (NIST/UMD)



Several quantum computers and simulators at Duke!

- 23-27 qubit Blue system
- 25 qubit Gold System
- upcoming Green system
- and more!

arXiv: 2304.10481



# Duke Quantum Center



Institute for  
**Robust Quantum  
Simulation**



I A R P A

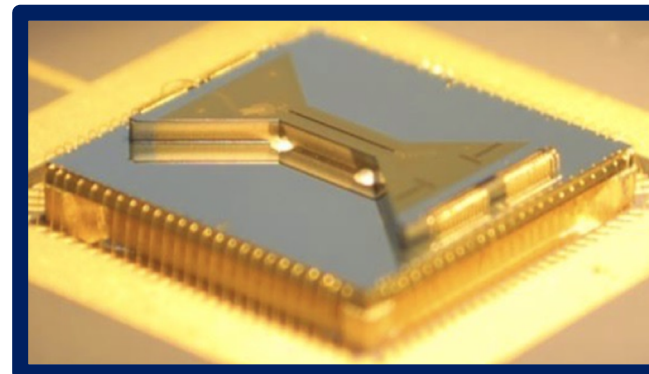
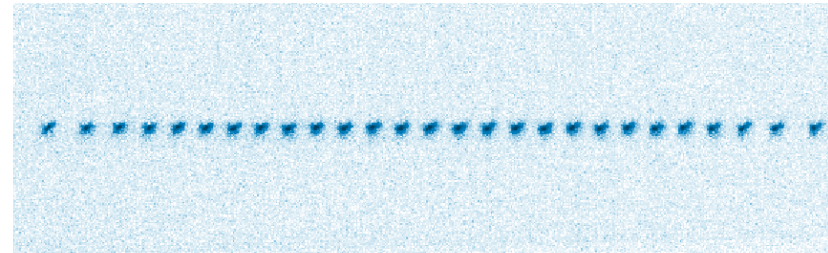


SOFTWARE-TAILORED ARCHITECTURES  
for QUANTUM CODESIGN



QUANTUM SYSTEMS ACCELERATOR

Catalyzing the Quantum Ecosystem



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