



Mechanics of tissue growth, homeostasis and repair

Part 1

Boulder Summer School 2024

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The Gang in London

Mao Lab past and present

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 Giulia Paci
 James van Hear
 Pablo Vicente Munuera
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 Veronika Lachina
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Collaborators

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 Shiladitya Banerjee (Cargenie Mellon)
 Buzz Baum (MRC LMB)
 Andela Saric (IST Vienna)
 Sophie Acton (LMCB, UCL)



“..the genetic instructions and building blocks used by all organisms are the same”

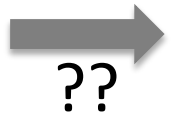


Kelvingrove Art Gallery,
Glasgow
Source: Yanlan's iPhone

“ It’s all in our genes ”

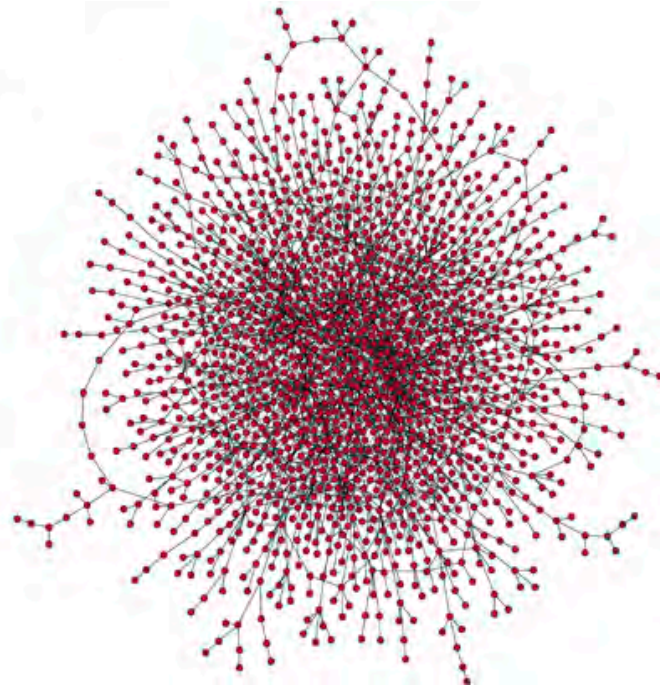


Genes



Shape

OMICs

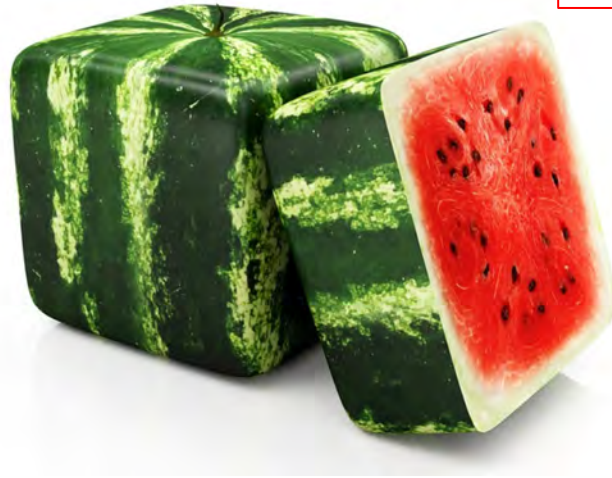


The importance of mechanical forces

Mechanics

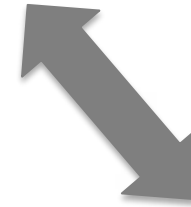
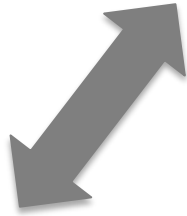
Cell Extrinsic Factors

- e.g. Basement membrane
- External forces



Genes

Shape



Role of mechanical forces

During development, homeostasis and repair, how do **forces and molecules** interact for tissues to:

Get into Shape

Stay in Shape

Get back into Shape

Structure of lectures

Day 1: Growth and morphogenesis

- i) some biomechanics background
- ii) case study on vertex modelling of tissue shape control

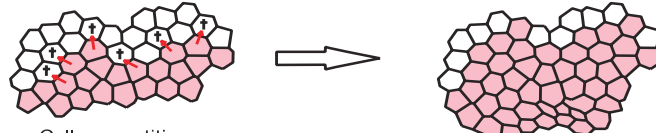
Day 2: Homeostasis and repair

- i) latest research – new tools and methods
- ii) case study on vertex modelling of tissue repair

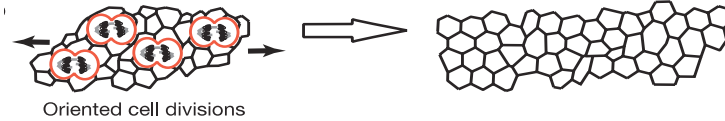
Exercise: modelling lymph node mechanics

Cellular mechanisms of tissue shape control

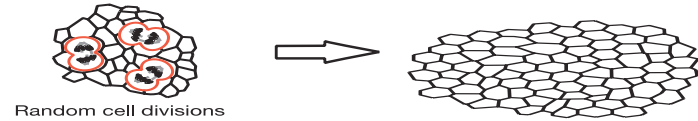
1. Growth rates



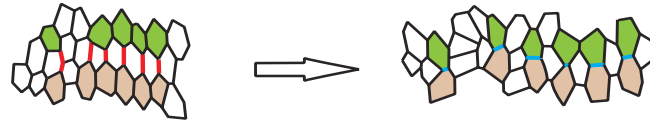
2. Division orientations



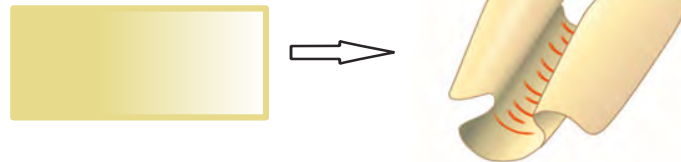
3. Cell shape changes



4. Planar cell rearrangements

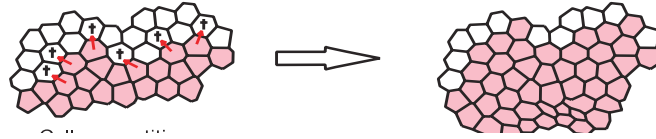


5. 3D tissue sculpting

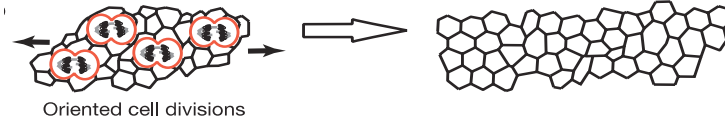


Mechanical control of cellular mechanisms

1. Growth rates

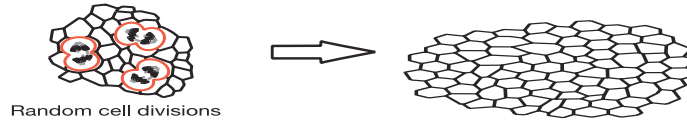


2. Division orientations



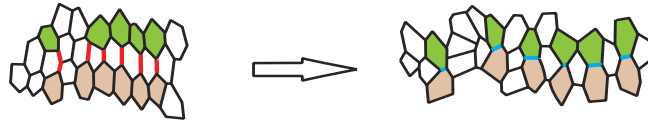
Oriented cell divisions

3. Cell shape changes

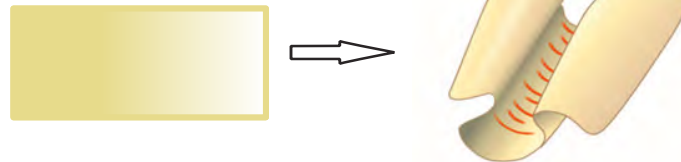


Random cell divisions

4. Planar cell rearrangements

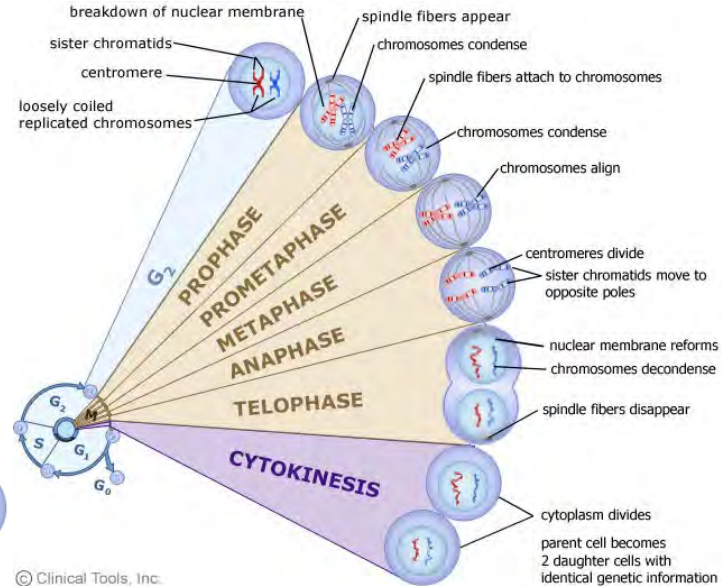
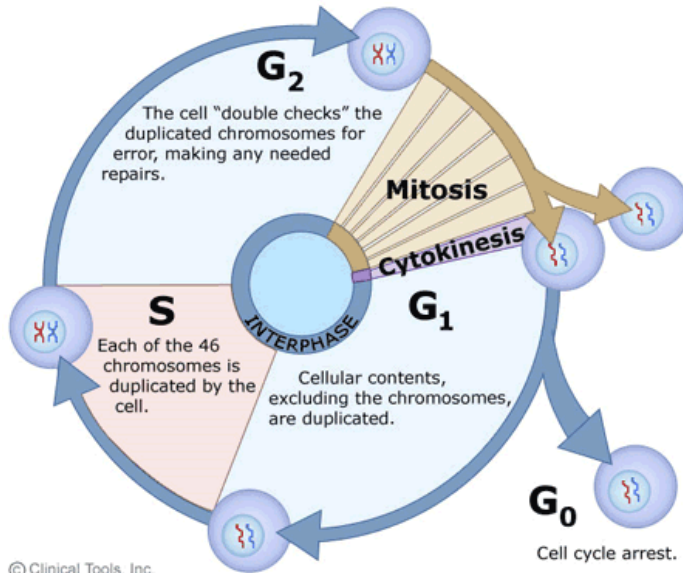


5. 3D tissue sculpting



1. Mechanical control of growth rates

Many growth factors and signalling pathways regulate the cell cycle



1. Mechanical control of growth rates

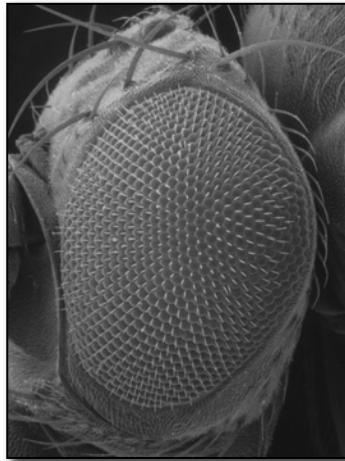
A. Some growth factors are also sensitive to mechanics, e.g. Yki/YAP/TAZ

The Hippo pathway limits cell number

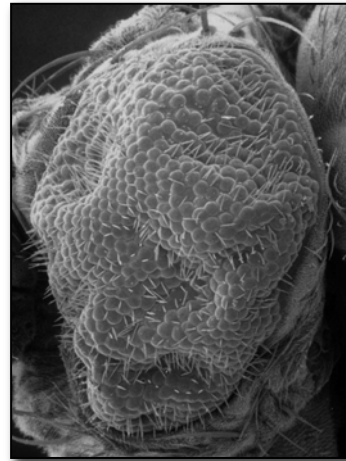
Pathway activity



Overexpression



Control

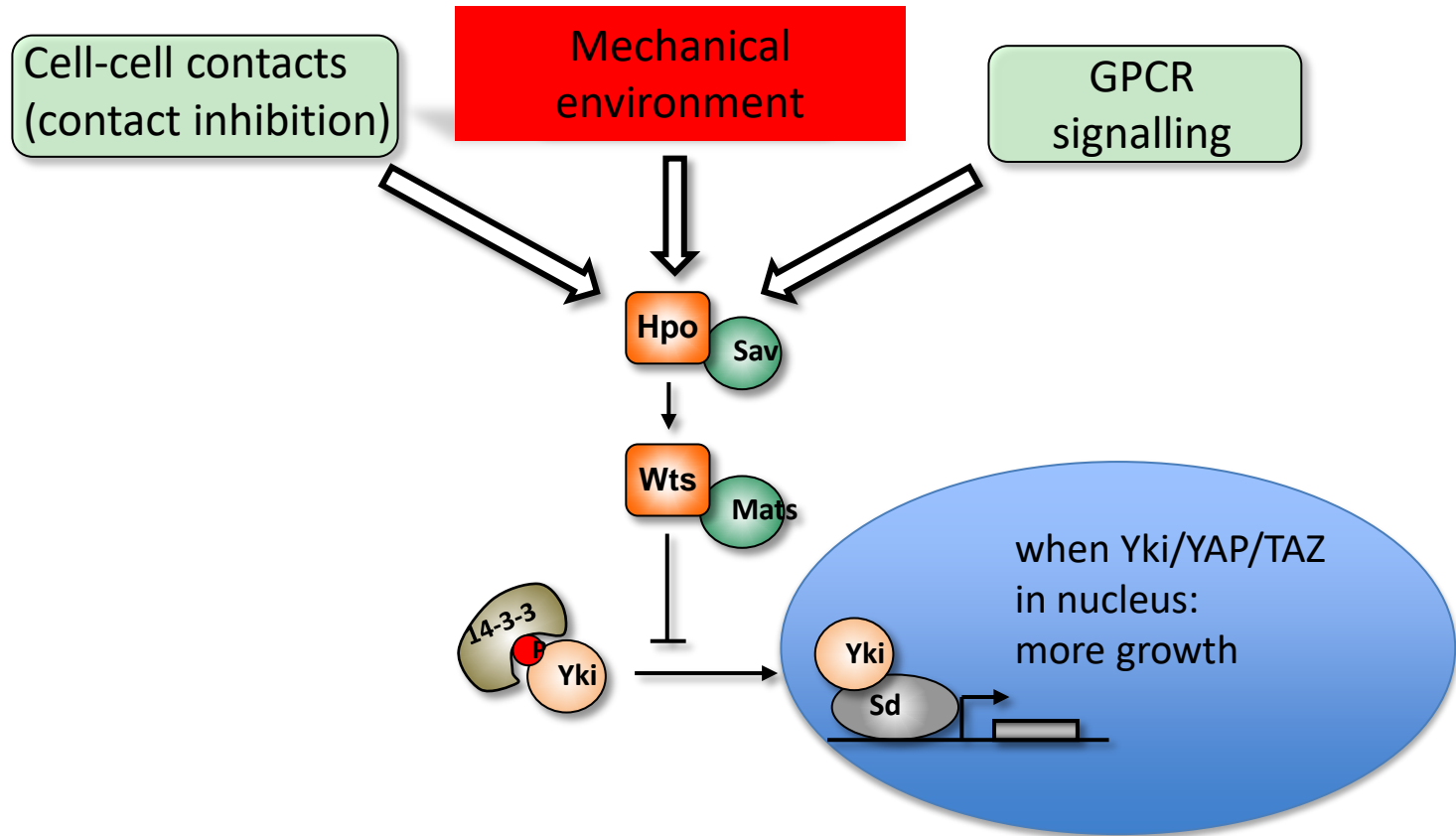


Mutant

Bryant, Xu, Hariharan, Pan, Halder, McNeill, Hafen, Harvey, Tapon, Jiang labs...

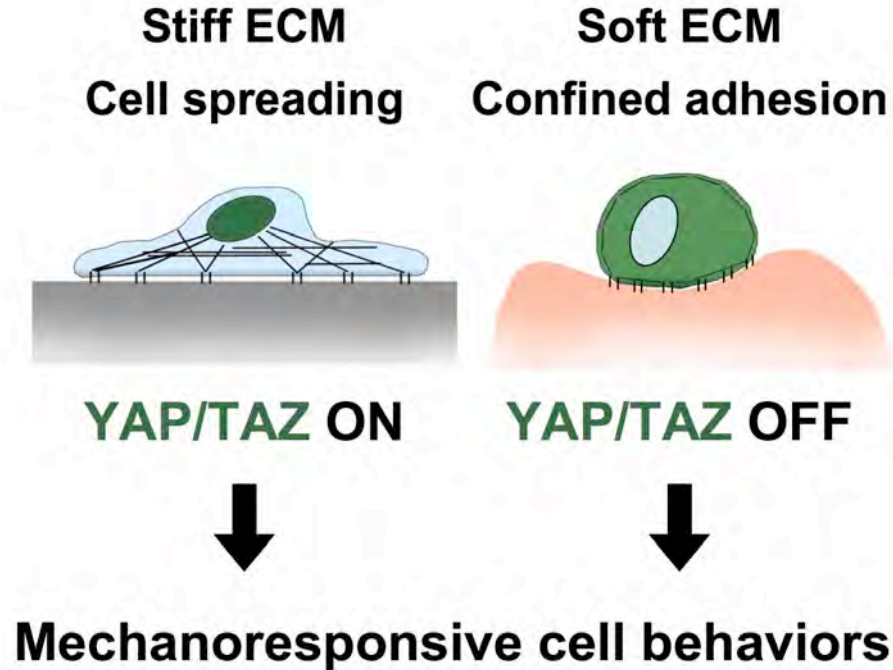
1. Mechanical control of growth rates

Hippo pathway upstream signals



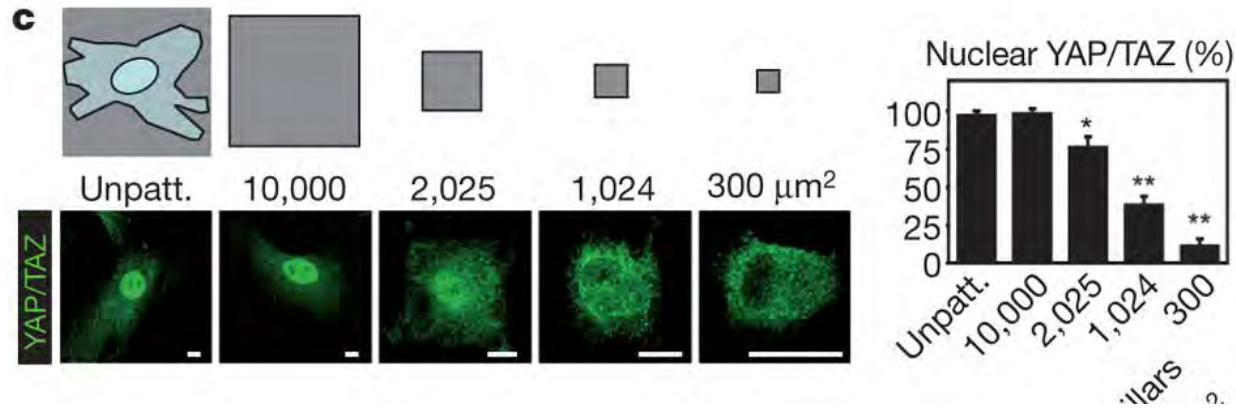
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A. Effect of mechanics on growth factors – transcriptional co-activators Yki/YAP/TAZ



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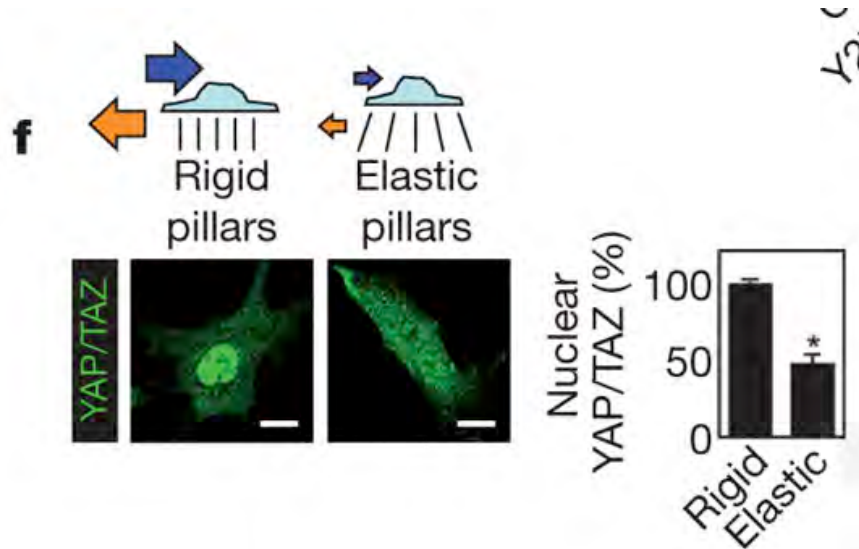
A. Effect of mechanics on growth factors – transcriptional co-activators Yki/YAP/TAZ .



Micropatterning to constrain shape

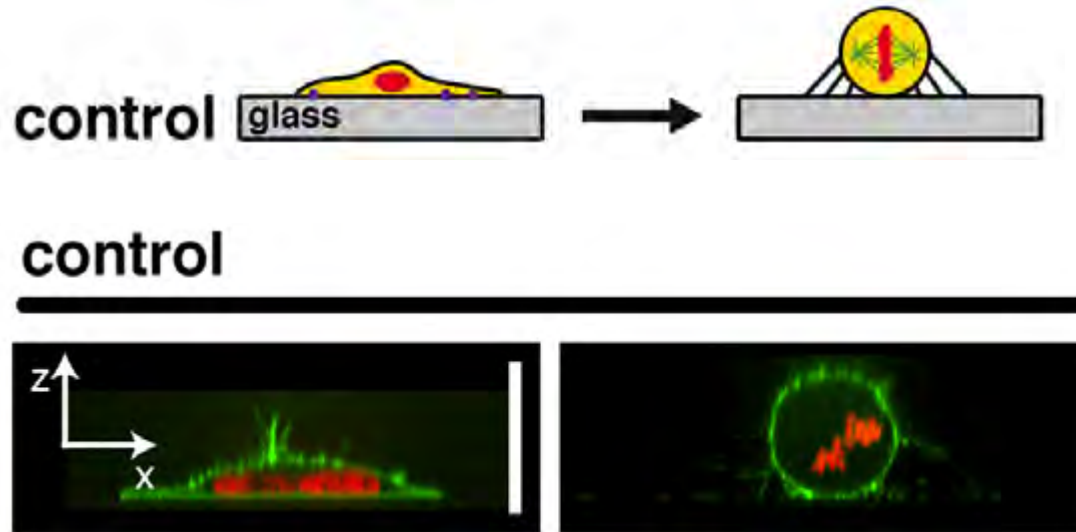
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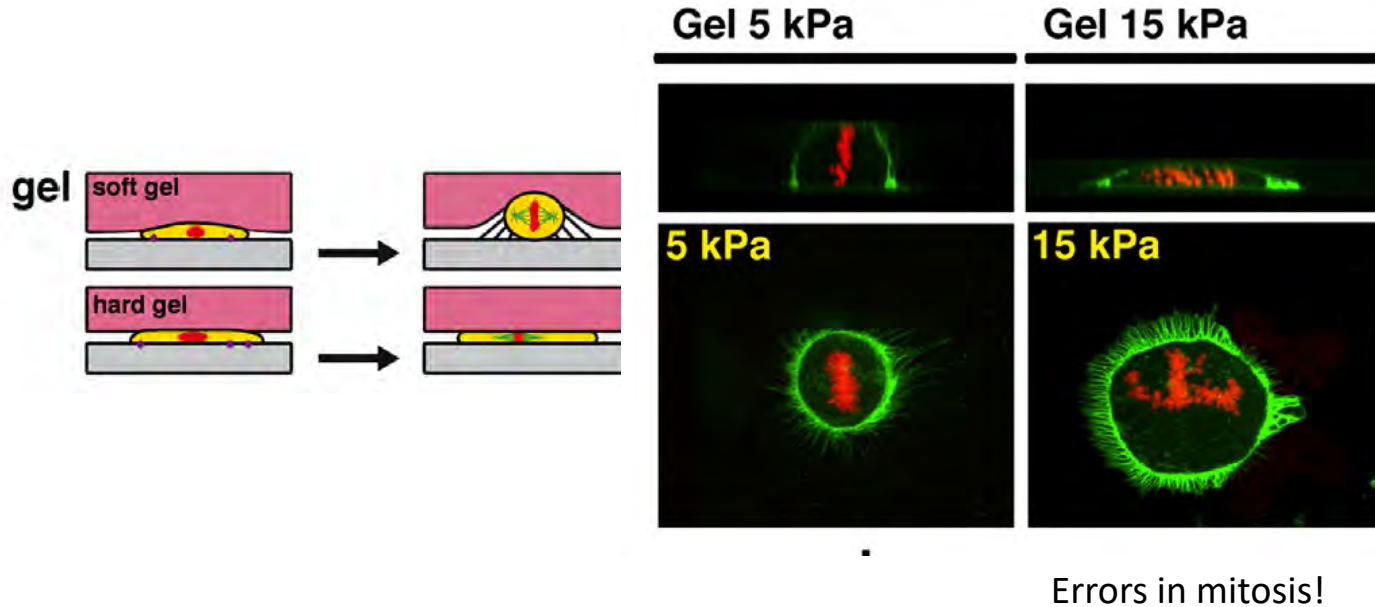
1. Mechanical control of growth rates

B. Effect of mechanics on mitosis



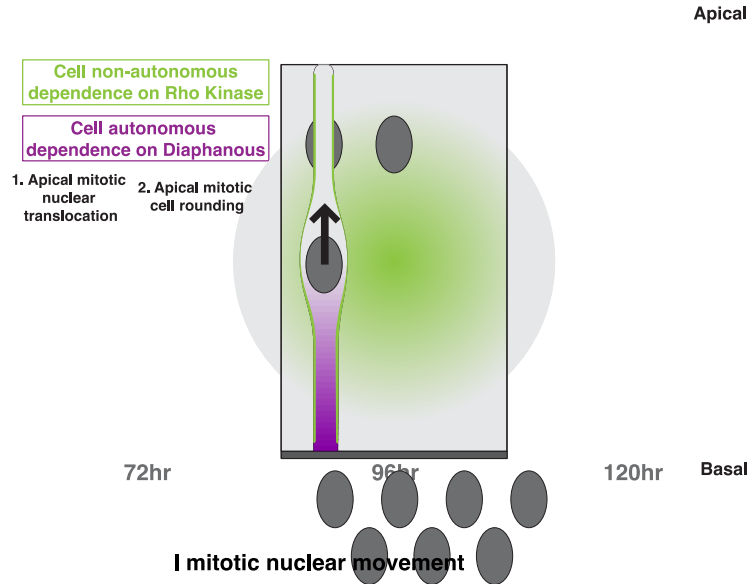
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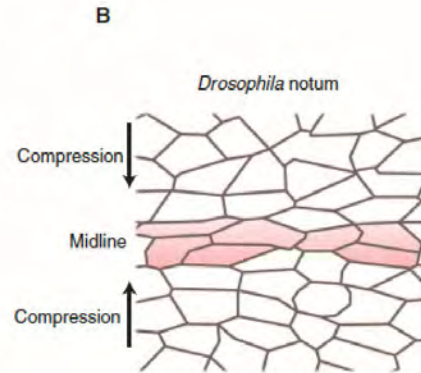
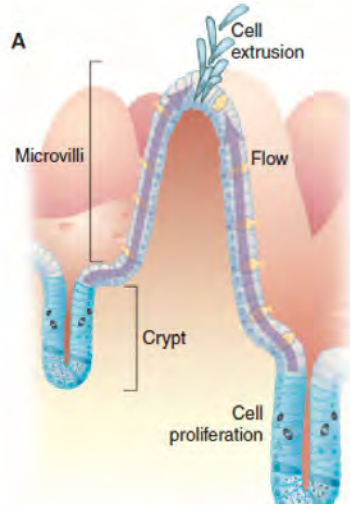
Tissue Mechanics Regulate Mitotic Nuclear Dynamics during Epithelial Development.
Kirkland et al., Current Biology 2020

1. Mechanical control of growth rates

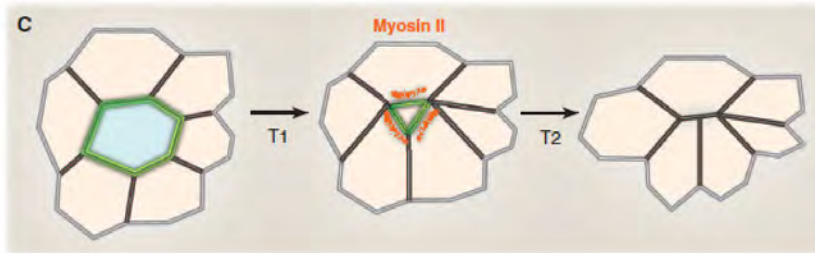
C. Effect of mechanics on **cell death** – non apoptotic extrusion

In the mammalian gut, cells divide in the crypt and move to the top of microvilli, where they die or extrude while alive.

Simons et al, Exp Cell Res 2011



In *Drosophila*, cell compression due to tissue growth changes cell shape (red) and causes live cell Extrusion. Marinari et al., Nature 2012

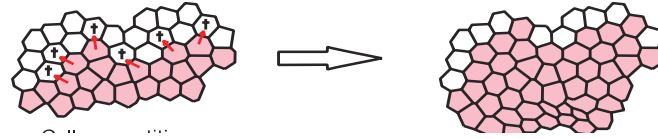


Extrusion occurs by cells destined to die signalling to surrounding epithelial cells to contract an actomyosin ring that squeezes the dying cell out.

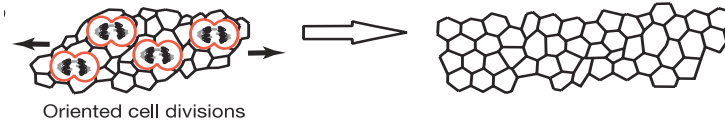
Eisenhoffer et al., Nature 2012

Mechanical control of cellular mechanisms

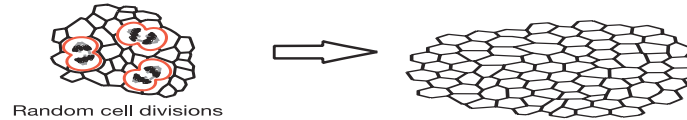
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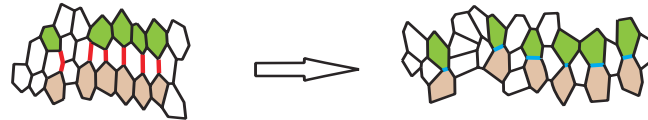
2. Division orientations



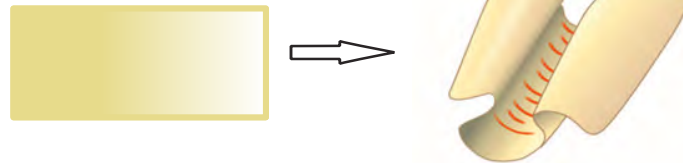
3. Cell shape changes



4. Planar cell rearrangements



5. 3D tissue sculpting



2. Mechanical control of division orientations

A. Cell shape and cell division orientation

1863: Hofmeister:

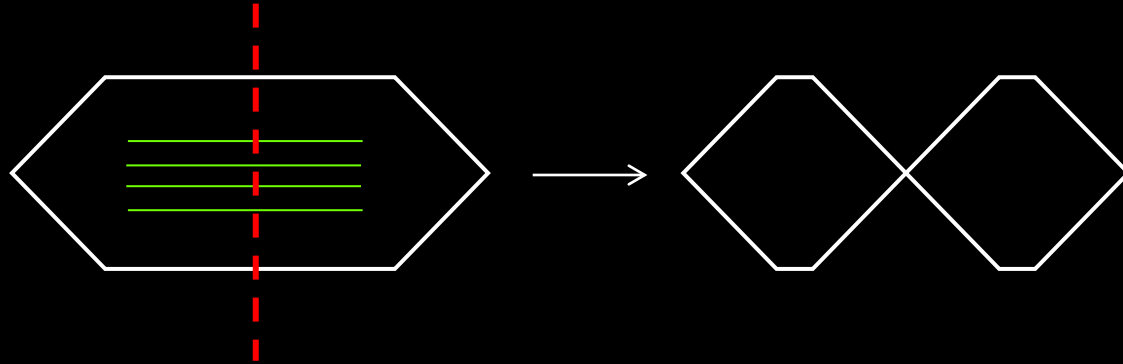
Cell geometry influences mitotic cleavage plans

1893: Hertwig's Rule:

Spindles align to longest axis of a cell

2. Mechanical control of division orientations

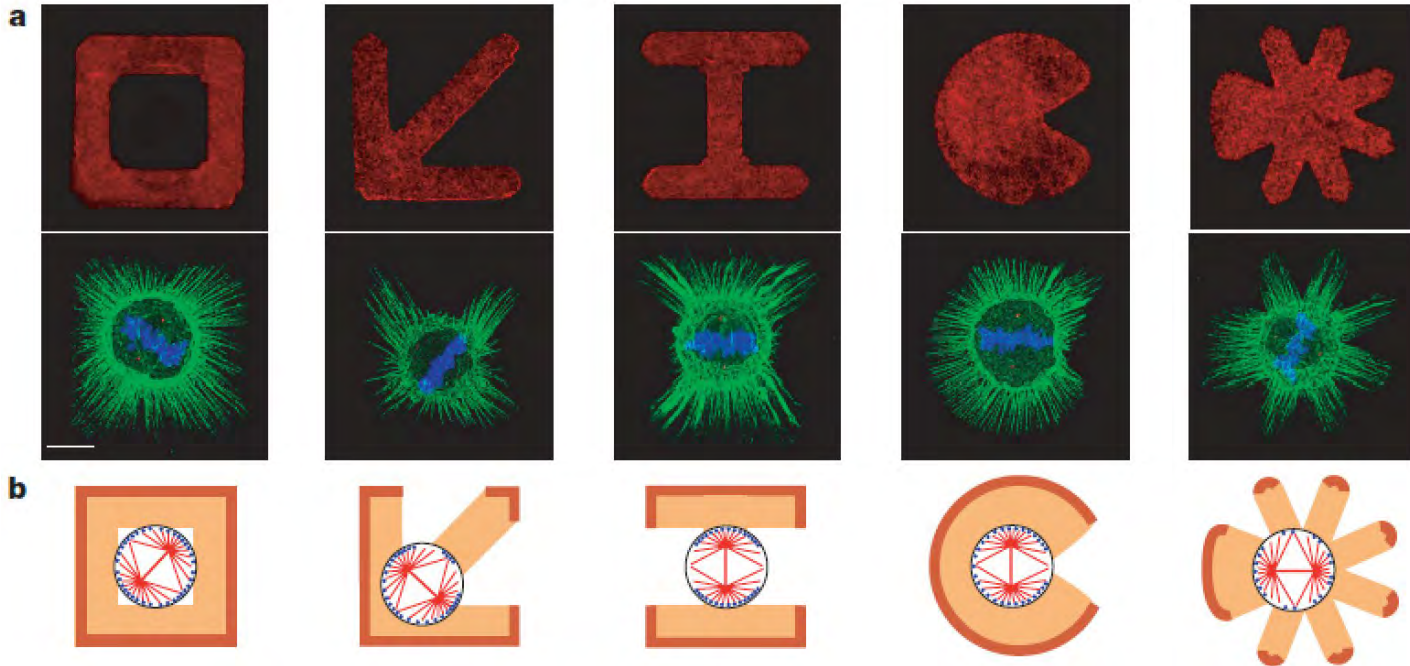
A. Cell shape and cell division orientation



Cell geometry dictates cell division orientation

2. Mechanical control of division orientations

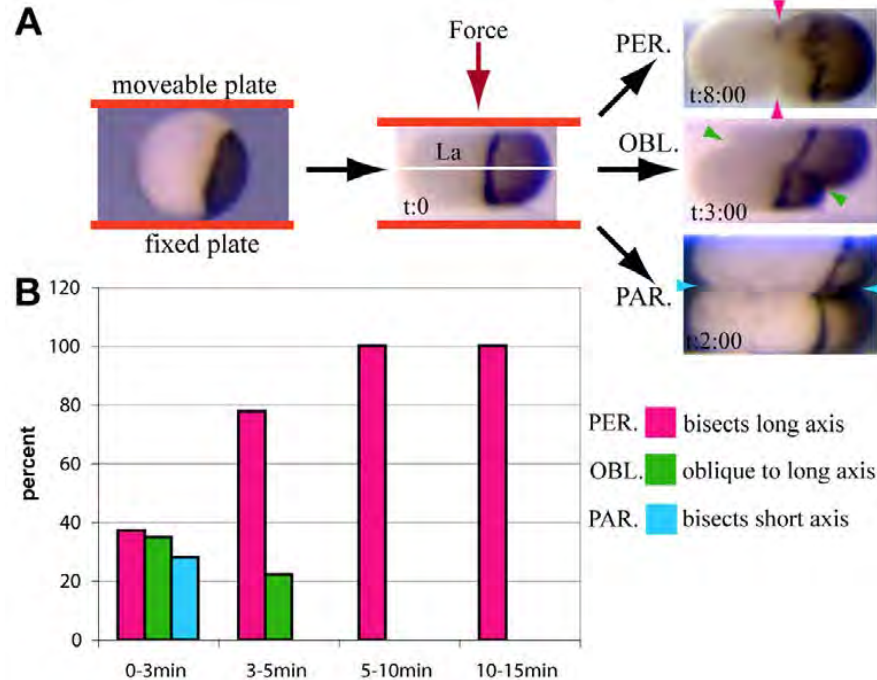
A. Cell shape and cell division orientation



Experimental and theoretical study of mitotic spindle orientation.
They et al., Nature 2007

2. Mechanical control of division orientations

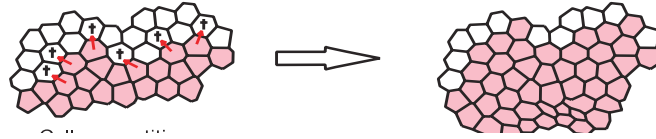
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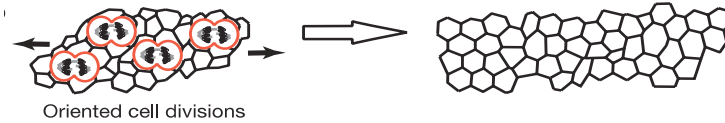
A default mechanism of spindle orientation based on cell shape is sufficient to generate cell fate diversity in polarised *Xenopus* blastomeres, Bernhard Strauss et al., Development 2006

Mechanical control of cellular mechanisms

1. Growth rates

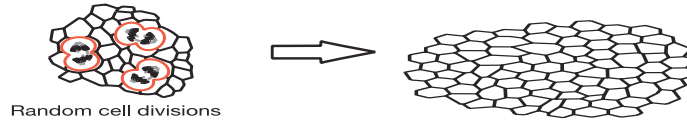


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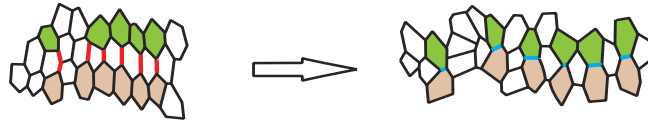
Oriented cell divisions

3. Cell shape changes

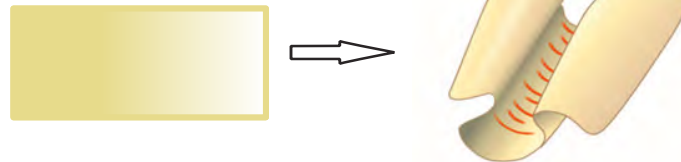


Random cell divisions

4. Planar cell rearrangements

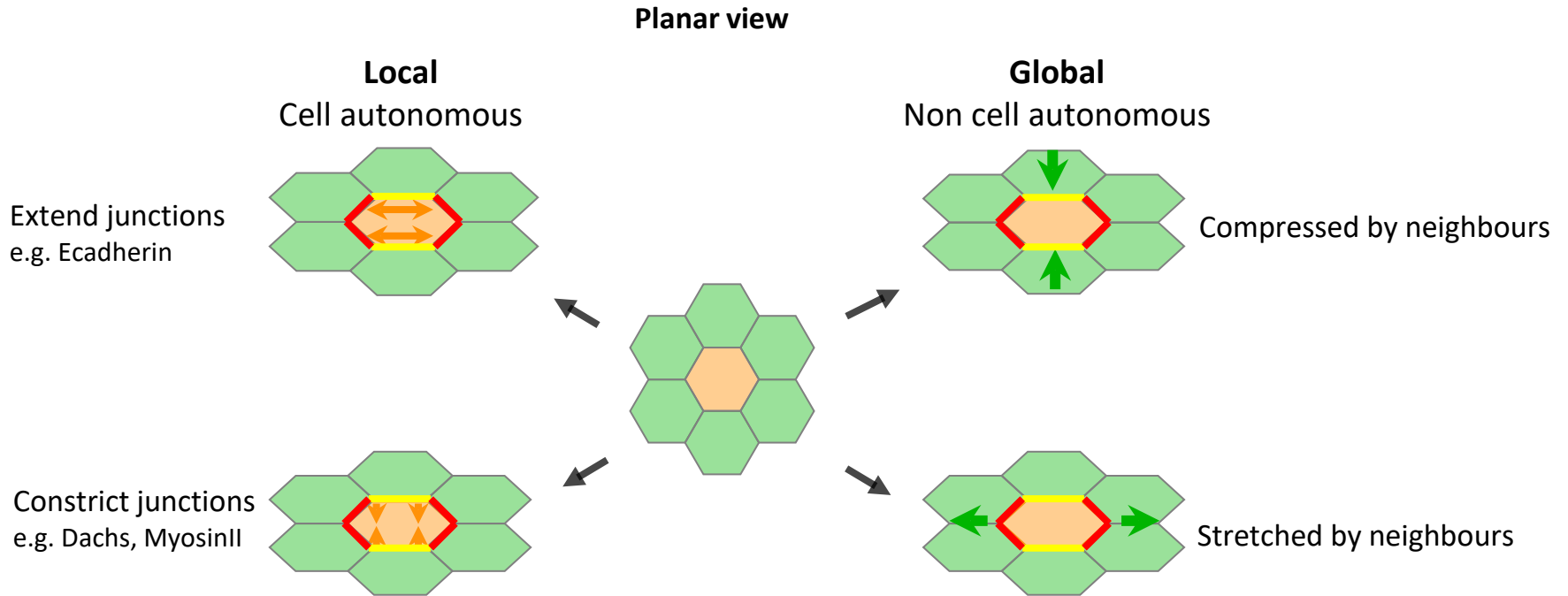


5. 3D tissue sculpting



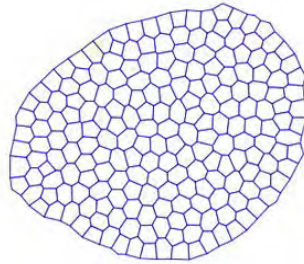
3. Mechanical control of cell shape

A. Different forces affect cell shape in a multicellular tissue



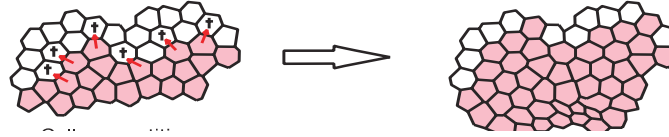
3. Mechanical control of cell shape

B. How forces are generated – differential tissue growth generates differential stress

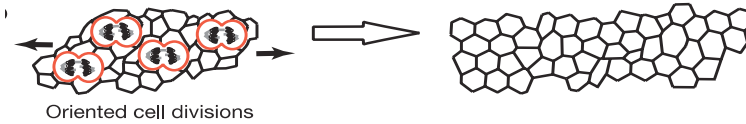


Mechanical control of cellular mechanisms

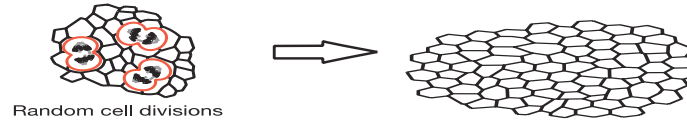
1. Growth rates



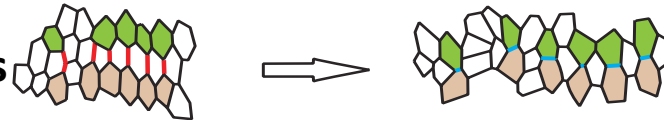
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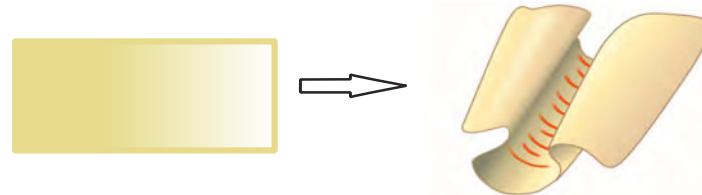
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4. Planar cell rearrangements

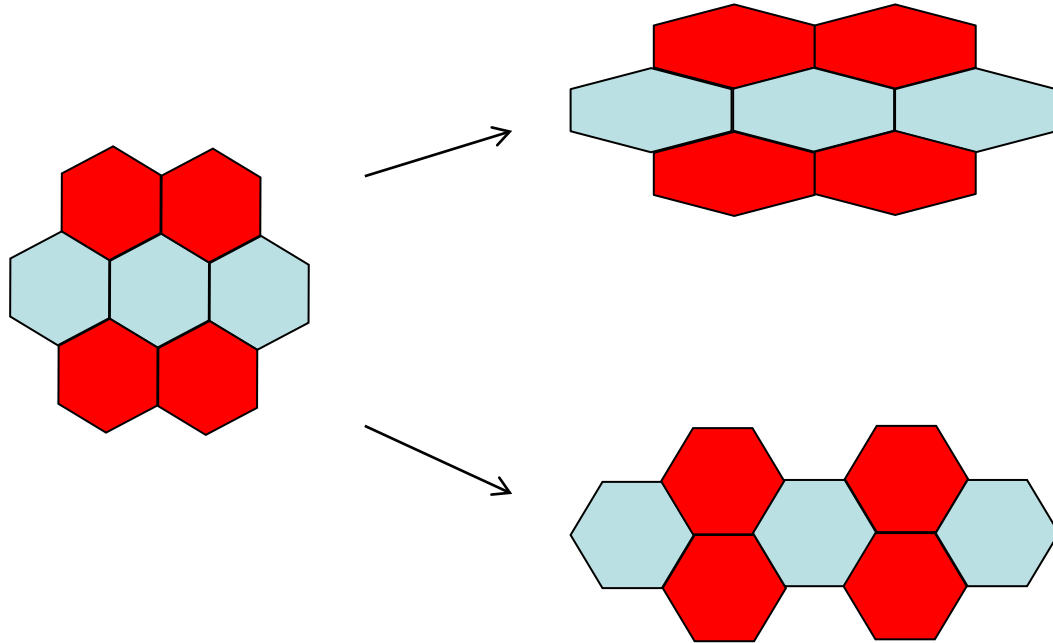


5. 3D tissue sculpting



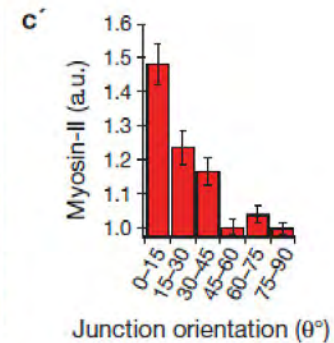
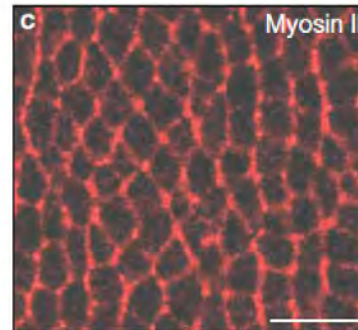
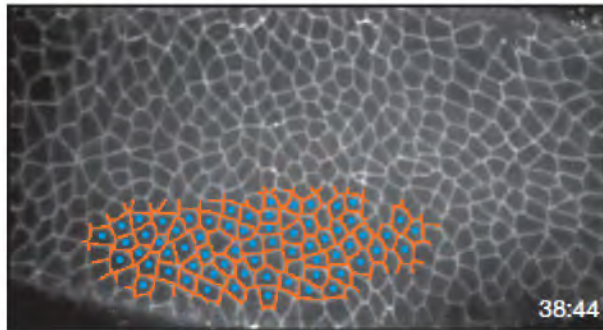
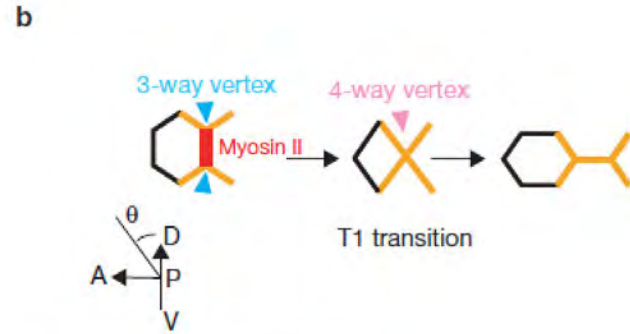
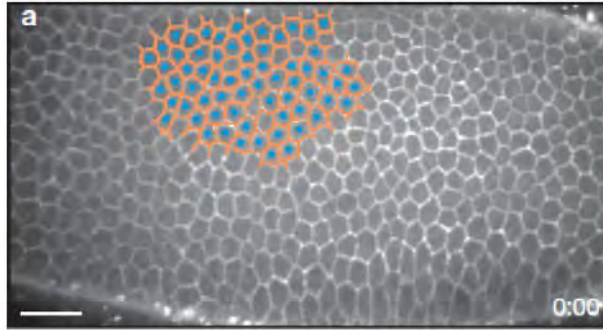
4. Mechanical control of cell rearrangements

A. Convergent / Extension - intercalation



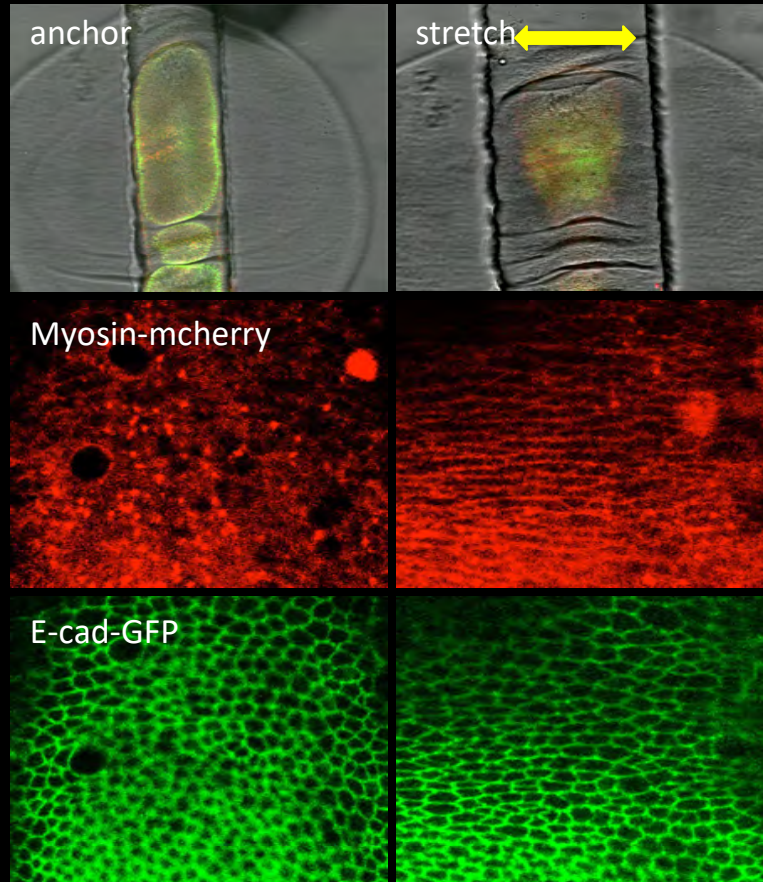
4. Mechanical control of cell rearrangements

A. Convergent / Extension – intercalation via Myosin II polarisation

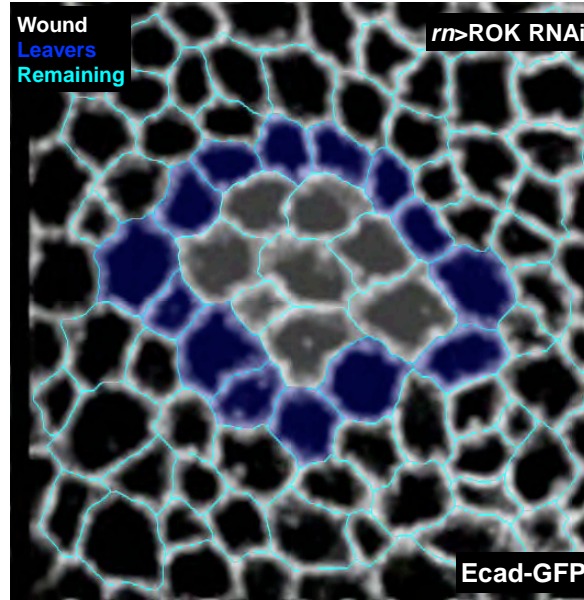


4. Mechanical control of cell rearrangements

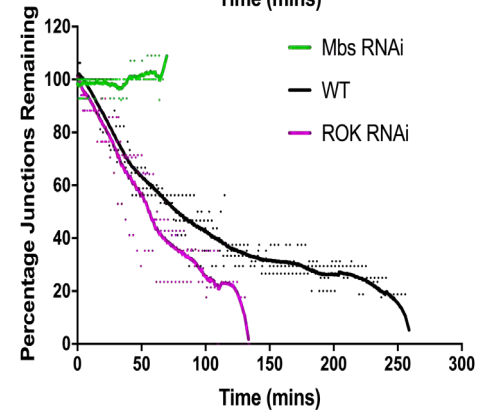
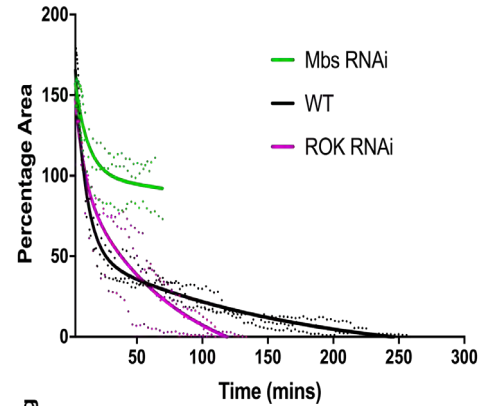
Myosin II polarisation is sensitive to mechanical forces



4. Mechanical control of cell rearrangements

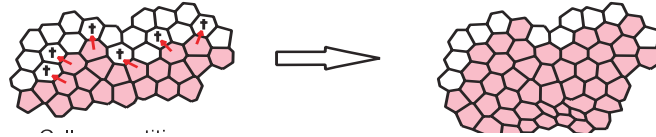


Cell intercalation drive more efficient wound closure

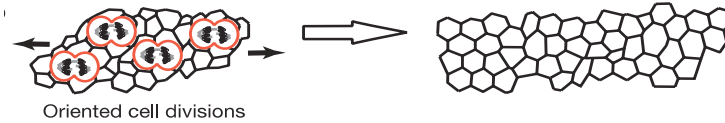


Mechanical control of cellular mechanisms

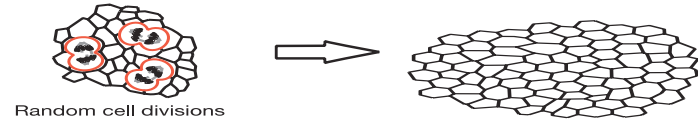
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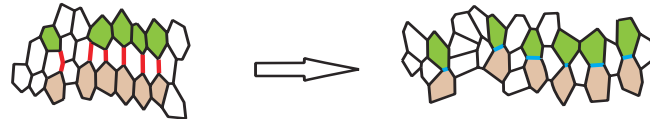
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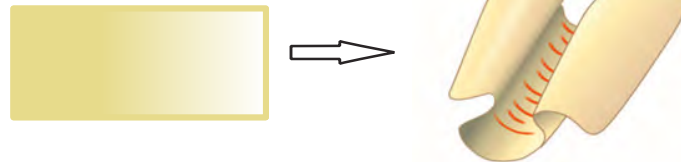
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4. Planar cell rearrangements

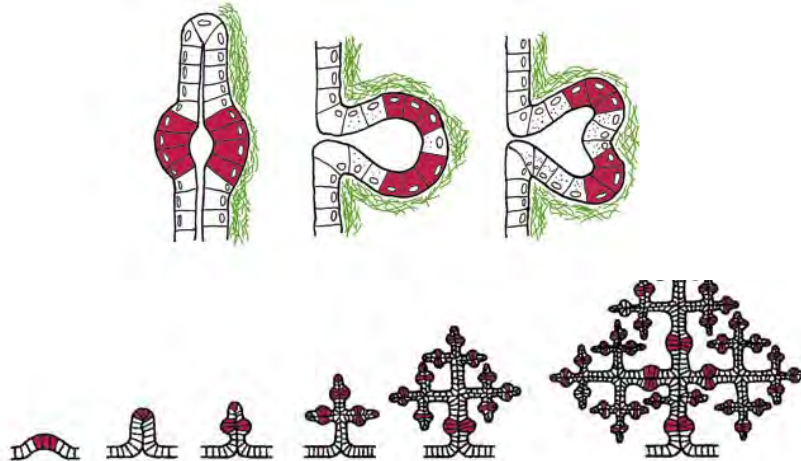


5. 3D tissue sculpting



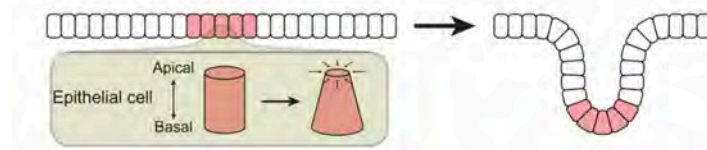
5. Mechanical 3D sculpting of tissues

Organogenesis

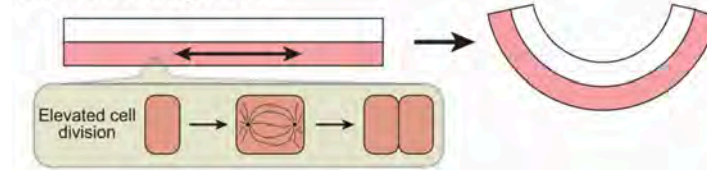


5. Mechanical 3D sculpting of tissues

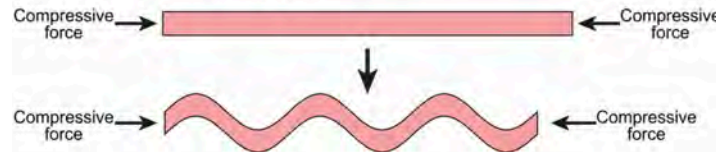
A Apical constriction , apoptotic forces, basal expansion, etc



B Differential growth



C Mechanical buckling



Works from labs of
Wieschaus,
Gartner,
Martin,
Leptin,
Suzanne,
Rauzi,
Dahmann,
Mahadevan, etc

Adapted from
Varner and Nelson 2014

5. Mechanical 3D sculpting of tissues

Differential planar growth rates induce precise patterns of folds



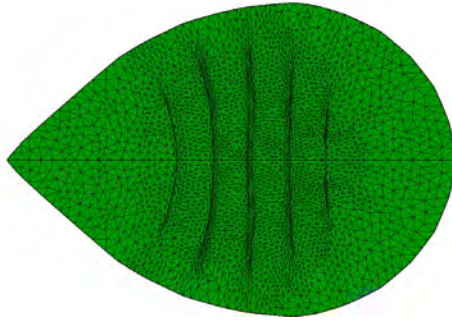
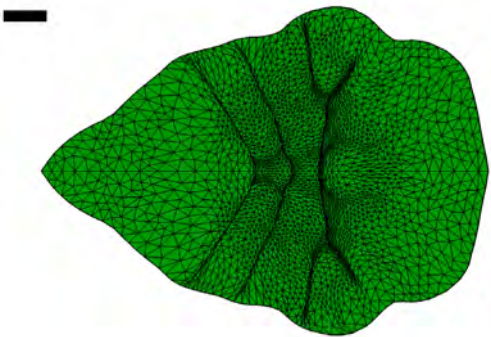
Finite Element Model of Tissue Folding



Differential planar growth rates induce patterns of folds

Experimental differential growth

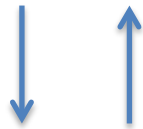
Uniform growth



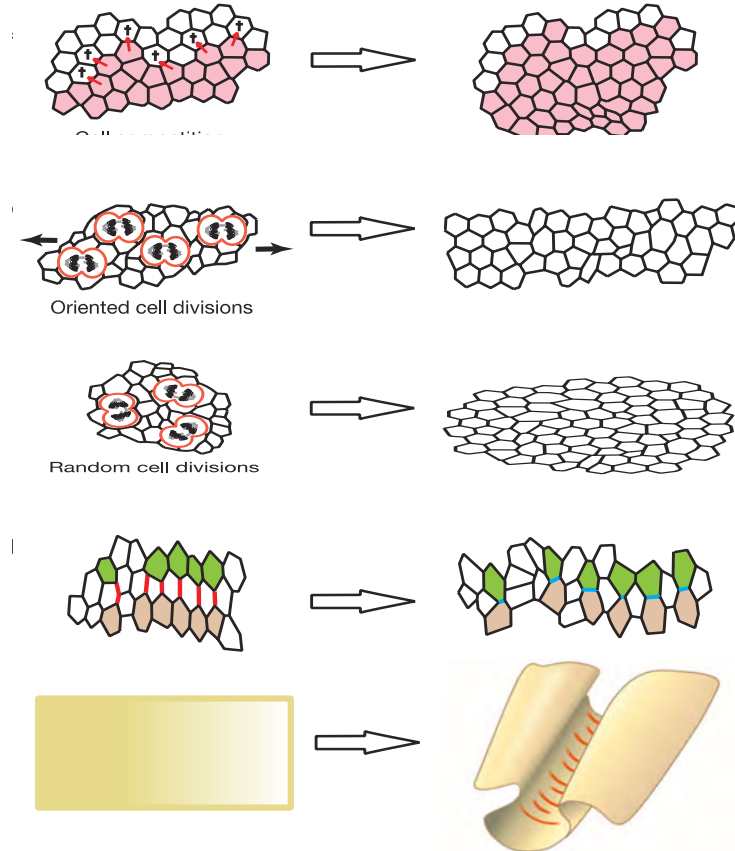
Cellular mechanisms of tissue morphogenesis

Interdependent
processes
through complex
feedback
mechanisms

Biochemical



Mechanical



Using mathematical models in biology



All models are wrong, but some are useful.

— *George E. P. Box* —

University College London

Using mathematical / physical models in biology - working with biologists

What is your question? - Biology is often too complicated! (or biologists like to make it so, too many genes, too many variables...

Using mathematical / physical models in biology - working with biologists

What is your question? - Biology is often too complicated! (or biologists like to make it so, too many genes, too many variables...

Can you simplify the question? – can you frame it more precisely?

Using mathematical / physical models in biology - working with biologists

What is your question? - Biology is often too complicated! (or biologists like to make it so, too many genes, too many variables...

Can you simplify the question? – can you frame it more precisely?

What is your hypothesis? – again, force them to be as precise as possible

Using mathematical / physical models in biology - working with biologists

What is your question? - Biology is often too complicated! (or biologists like to make it so, too many genes, too many variables...

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Using mathematical / physical models in biology - working with biologists

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Case study 1:

Control of orientation of cell divisions in *Drosophila*

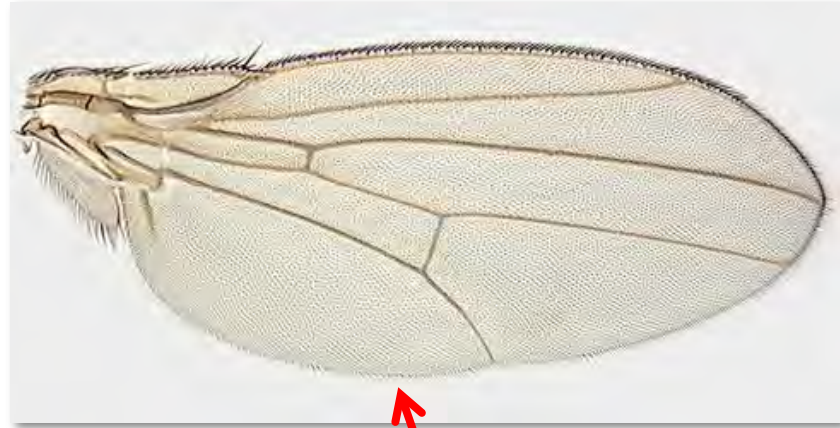
- Genetics
- Live imaging
- Computational 2D vertex model

Drosophila imaginal discs: the organ precursors

Wing imaginal disc



Adult wing

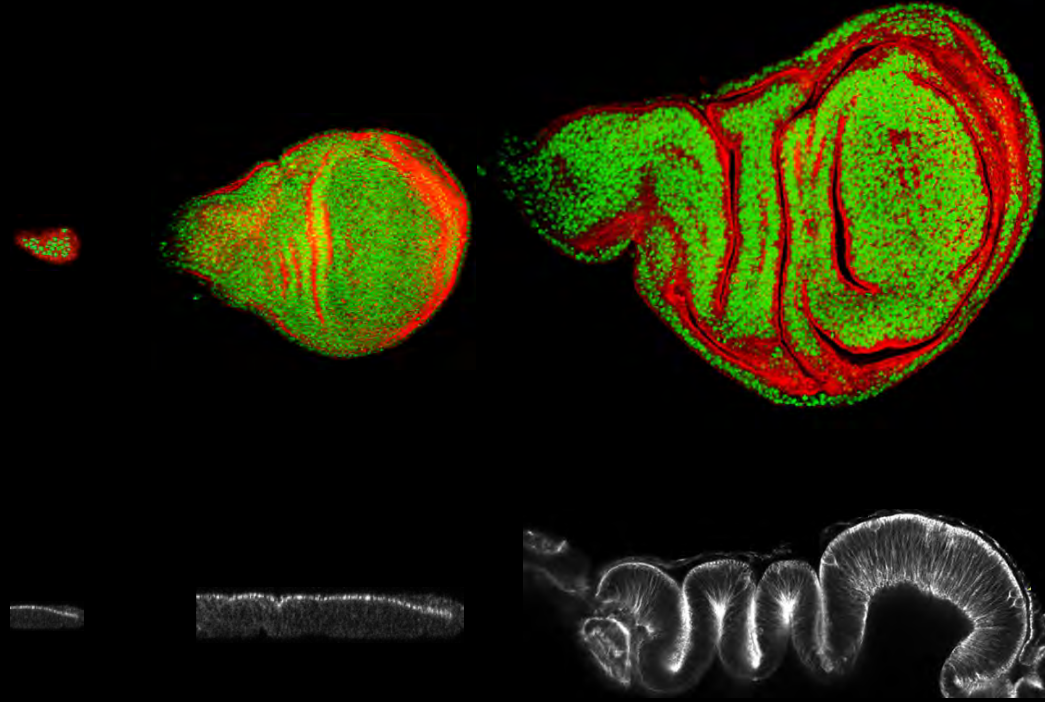


larva

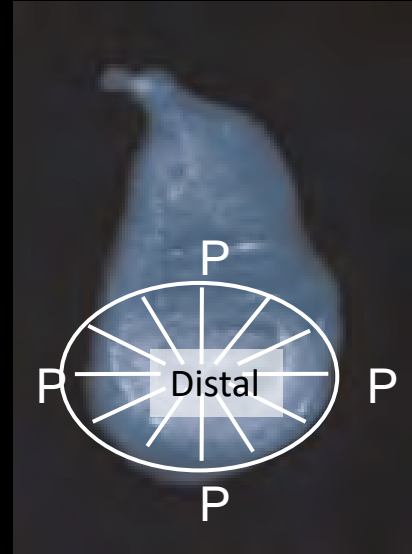
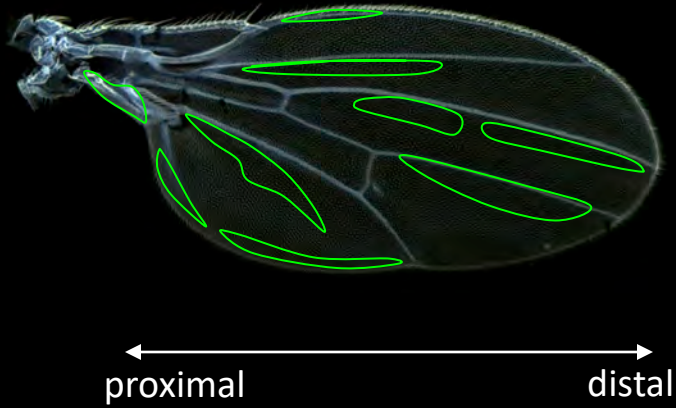


adult

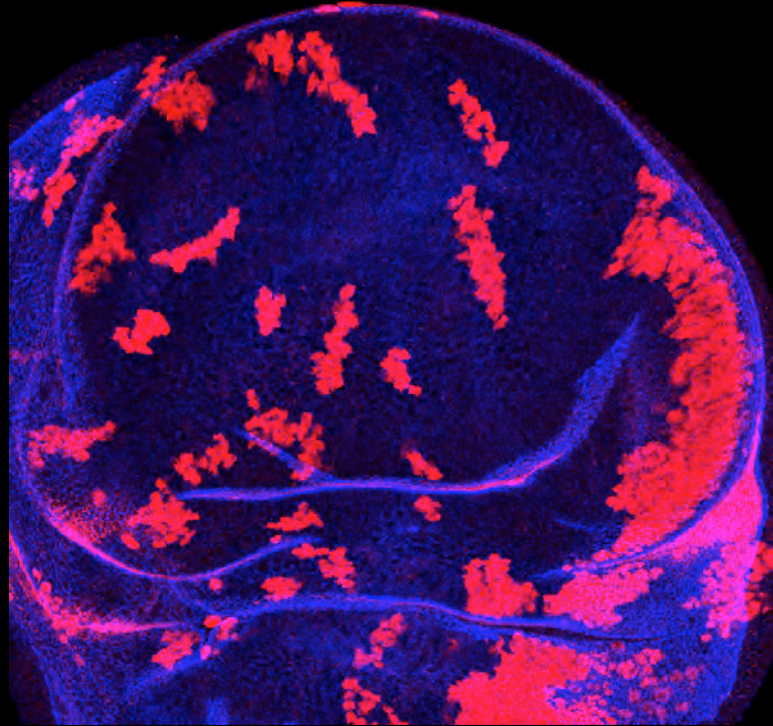
Drosophila imaginal discs: the organ precursors



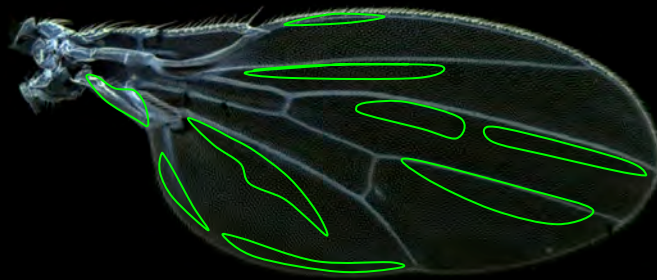
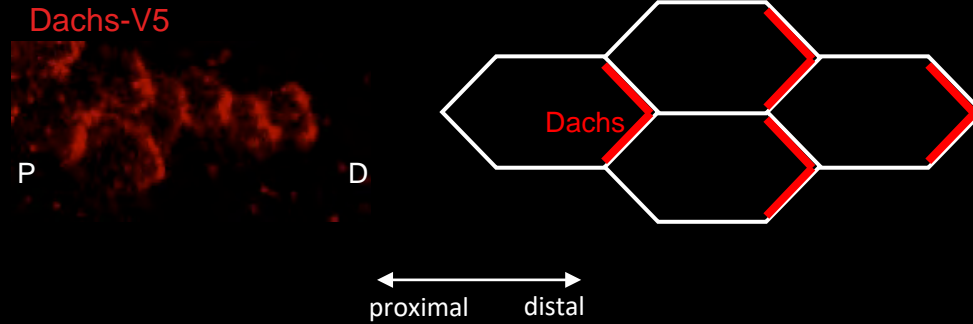
Drosophila wing growth in proximal - distal axis



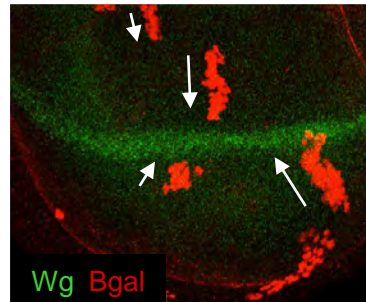
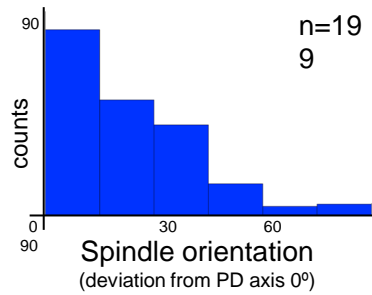
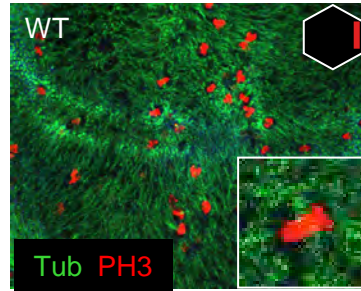
How are cell divisions oriented in the wing disc?



Planar polarisation of Dachs correlates with clone shape

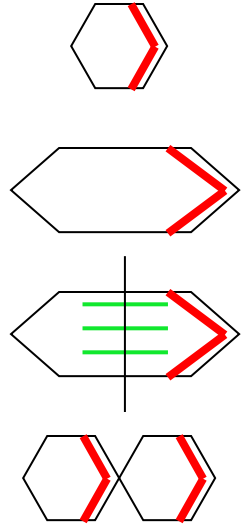


Polarisation of Dachs is required for spindle orientation and tissue growth



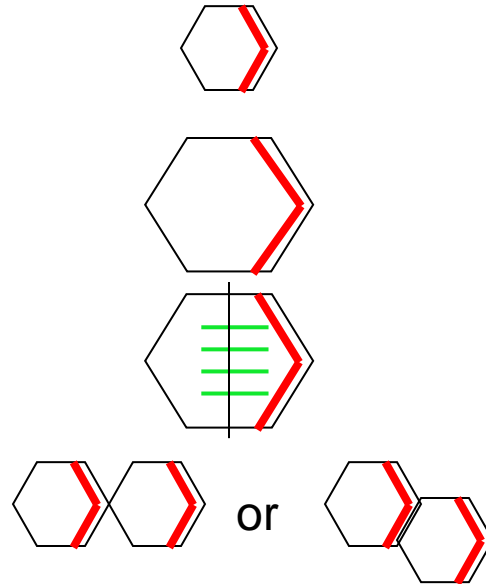
Models for how Dachs might orient cell division

Dachs (a myosin) affects cell shape, which orients spindle



???

Dachs orients spindle directly (somehow)



Using mathematical models in biology

What is your question?

Can you simplify the question?

What is your hypothesis?

Are there experiments / data to support hypothesis?

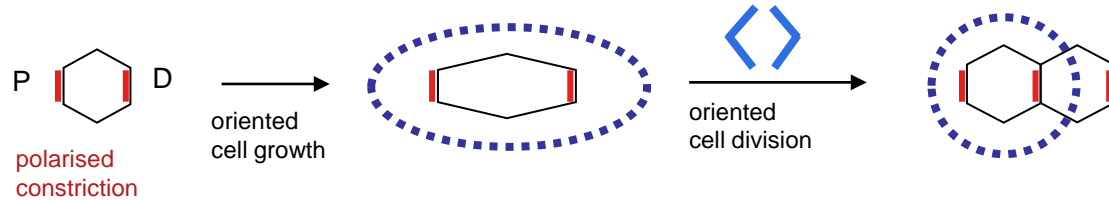
Can you create a simple mathematical model to test this hypothesis?

What experiments can you do to parameterise model and test model predictions?

Do cells show elongated growth and then divide in the same axis

and

Does this correlate with the P-D axis?

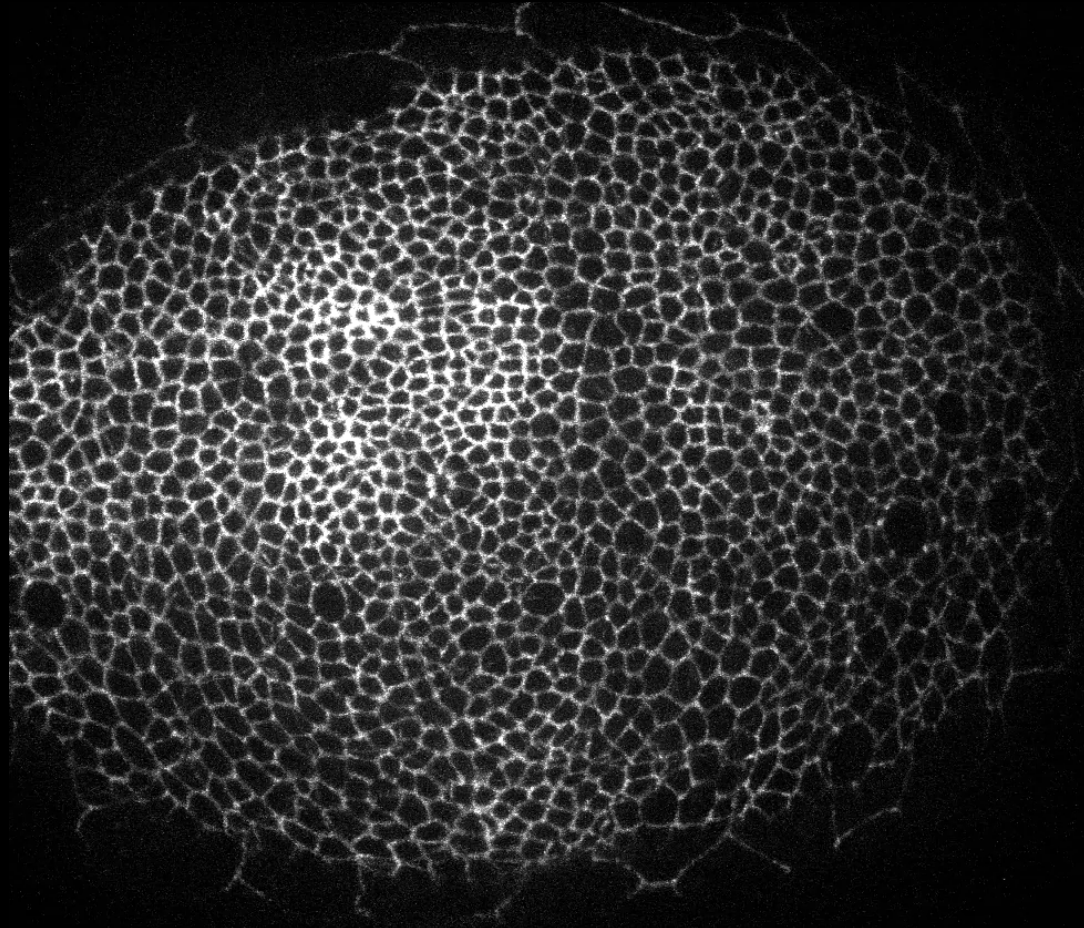


Proximal



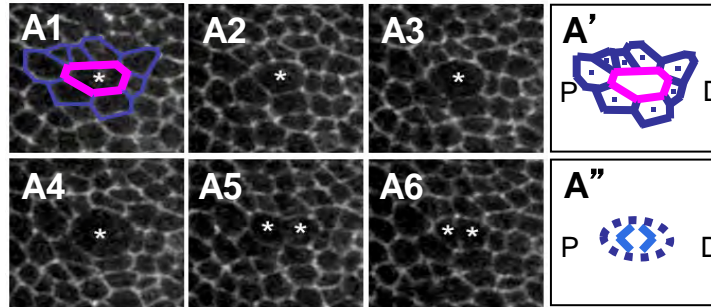
Distal ????

Examine apical cell shape and orientation of cell divisions live



ArmGFP

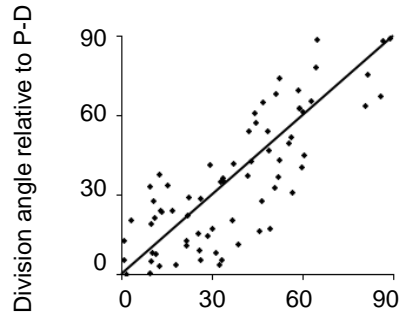
Cells do elongate, and divide perpendicular to long axis...



Dividing cell
elongation ratio

$$=1.45 \pm 0.31$$

n=97

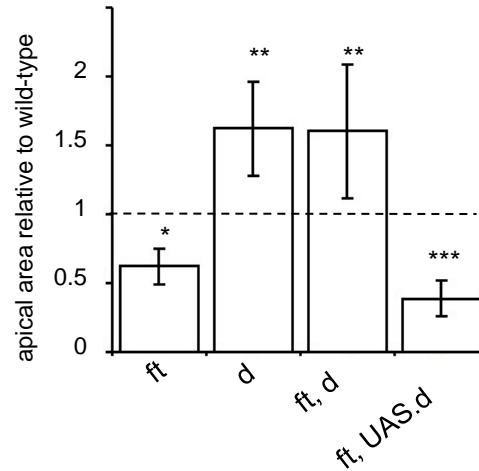
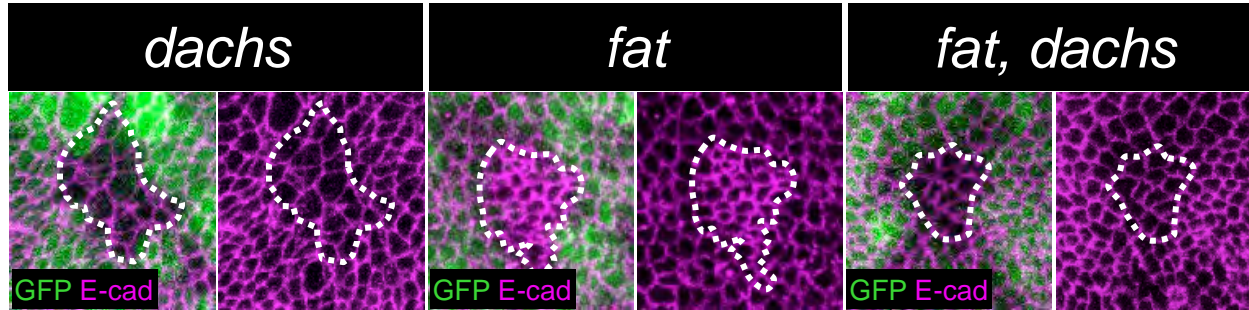


... even when it is not the P-D axis

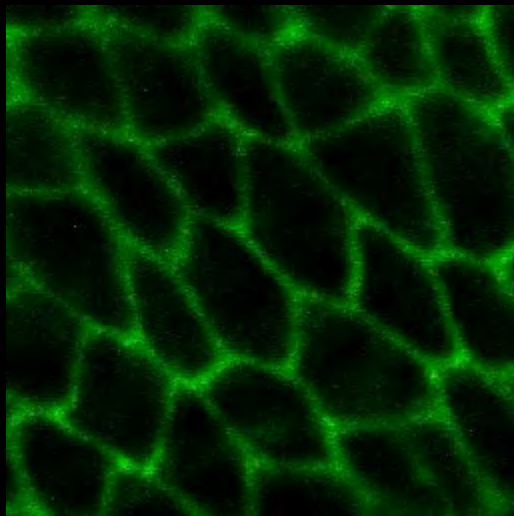
Dividing cell elongation angle relative to P-D

Geometry of apical cell-cell junctions
determine orientation of cell division

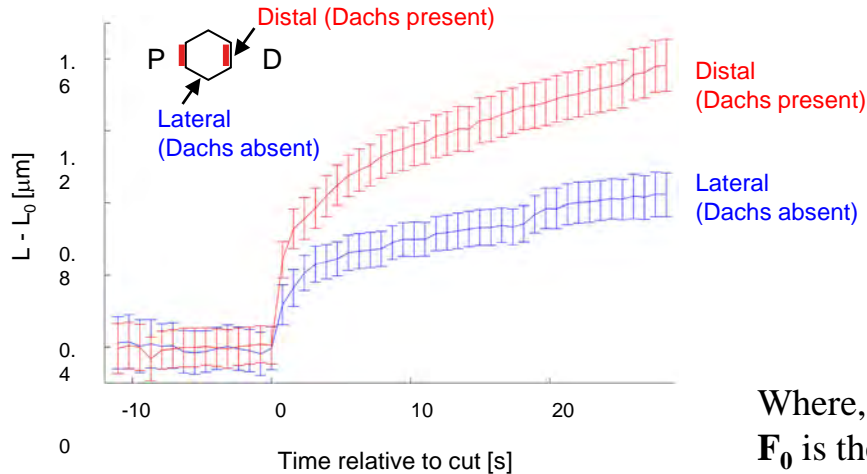
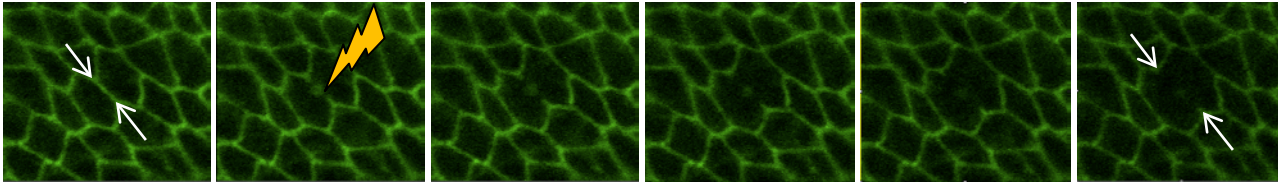
Dachs can control apical cell geometry



Measuring junctional tension with laser ablation



Increased tension correlates with Dachs localisation



Distal rate = $0.69 \mu\text{m/s}$, $n=55$ cuts
 Lateral rate = $0.34 \mu\text{m/s}$, $n=39$ cuts

Assume Kelvin-Voigt model:

$$\varepsilon(t) = L(t) - L(0) = \frac{F_0}{E} \left(1 - e^{-\left[\frac{E}{\mu}\right]*t}\right)$$

Where,

F_0 is the tensile force before laser ablation = initial recoil velocity $\times \mu$

E is the elasticity,

μ is the viscosity coefficient.

Using mathematical models in biology

What is your question?

Can you simplify the question?

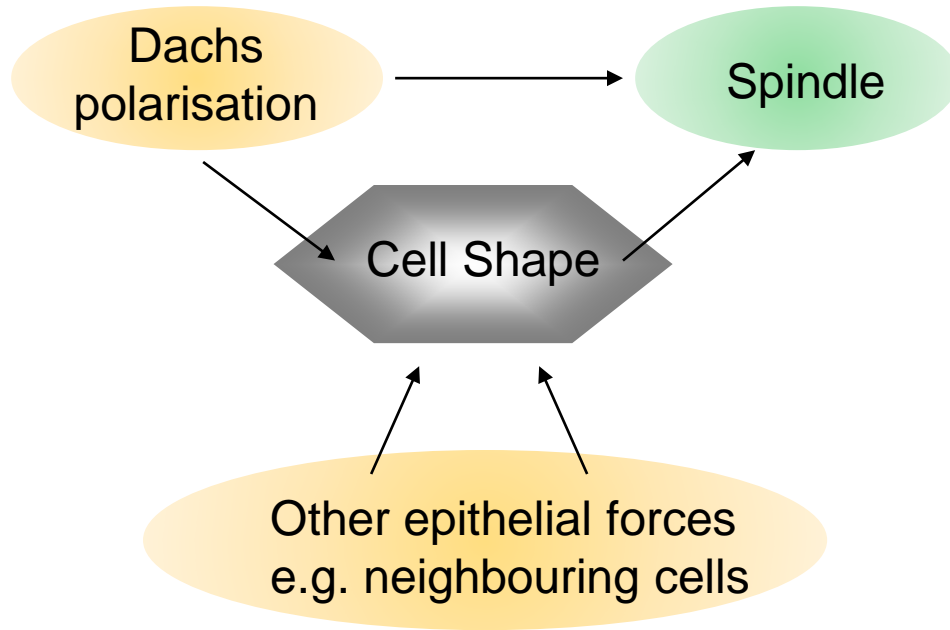
What is your hypothesis?

Are there experiments / data to support hypothesis?

Can you create a simple mathematical model to test this hypothesis?

What experiments can you do to parameterise model and test model predictions?

Supports Dachs influencing spindle orientation indirectly



How do forces contribute to epithelial packing??

Need a computational model of an epithelium

Using mathematical models in biology

What is your question?

Can you simplify the question?

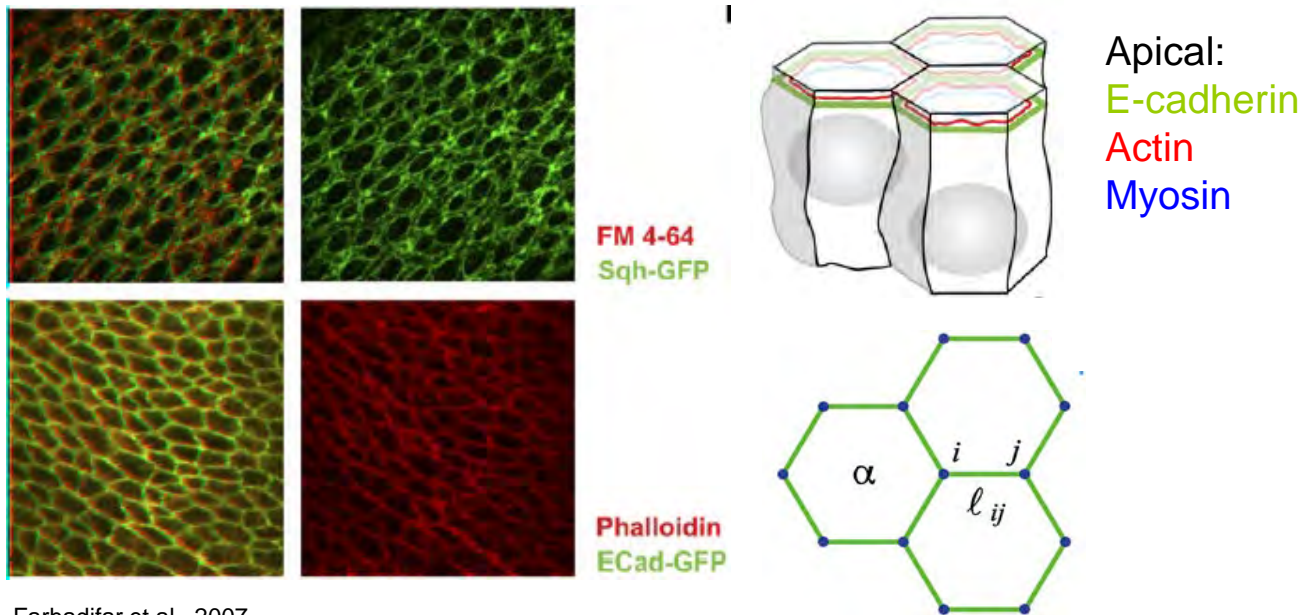
What is your hypothesis?

Are there experiments / data to support hypothesis?

Can you create a simple mathematical model to test this hypothesis?

What experiments can you do to parameterise model and test model predictions?

Where do the forces come from?



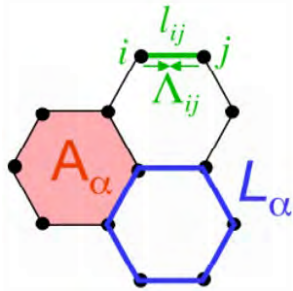
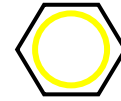
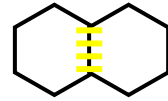
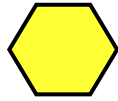
Farhadifar et al., 2007

Adhesive and contractile molecules change force balances within the epithelium

2D vertex model

Quantitative description of forces at apical vertices

Potential Energy of Whole system = \sum area elasticity + \sum junctional tension + \sum cortical contractility



$$E(R_i) = \sum_{\alpha} \frac{K_{\alpha}}{2} (A_{\alpha} - A_{\alpha}^{(0)})^2 + \sum_{\langle i,j \rangle} \Lambda_{ij} \ell_{ij} + \sum_{\alpha} \frac{\Gamma_{\alpha}}{2} L_{\alpha}^2$$

$$F_i = - \frac{\partial E}{\partial R_i}$$

$$\frac{\partial R_i}{\partial t} = \frac{F_i}{\zeta} + M$$

Area elasticity term

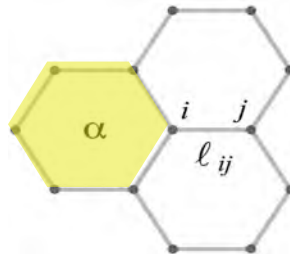
Pressure from volume and height of cell

$$E(R_i) = \sum_{\alpha} \frac{K_{\alpha}}{2} \left(A_{\alpha} - A_{\alpha}^{(0)} \right)^2 + \sum_{\langle i,j \rangle} \Delta_{ij} \ell_{ij} + \sum_{\alpha} \frac{\Gamma_{\alpha}}{2} L_{\alpha}^2$$

elastic coefficient

actual area

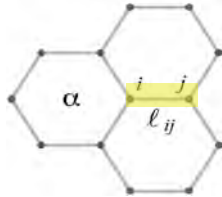
preferred area



Junctional line tension term

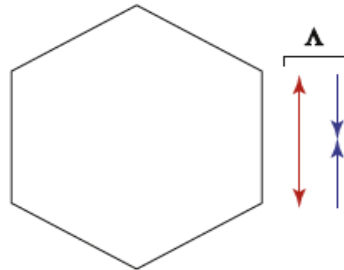
Force balance between adhesion molecules and contractile molecules

$$E(\mathbf{R}_i) = \sum_{\alpha} \frac{K_{\alpha}}{2} \left(A_{\alpha} - A_{\alpha}^{(0)} \right)^2 + \sum_{\langle i,j \rangle} \Delta_{ij} \ell_{ij} + \sum_{\alpha} \frac{\Gamma_{\alpha}}{2} L_{\alpha}^2$$



Line tension coefficient
 \propto **contractility** - **adhesion**

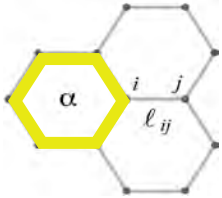
Length of junction



Perimeter contractility term

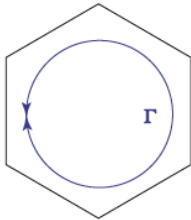
Contractile force of actin-myosin ring

$$E(\mathbf{R}_i) = \sum_{\alpha} \frac{K_{\alpha}}{2} \left(A_{\alpha} - A_{\alpha}^{(0)} \right)^2 + \sum_{\langle i, j \rangle} \Lambda_{ij} \ell_{ij} + \sum_{\alpha} \frac{\Gamma_{\alpha}}{2} L_{\alpha}^2$$



Perimeter contractility coefficient

Length of cell perimeter



To include Dachs: How would you do it?

To include Dachs: modify line tension term

$$E(R_i) = \frac{K}{2} \sum_{\alpha} (A_{\alpha} - A_{\alpha}^{(0)})^2 + \Lambda \sum_{\langle i,j \rangle} (1 + \varphi_{ij}^{Dachs}) l_{ij} + \frac{\Gamma}{2} \sum_{\alpha} L_{\alpha}^2$$

$$\varphi_{ij}^{Dachs} = |\sin(\text{edge angle} - \text{PD angle})| \varphi_{MAX}^{Dachs}$$

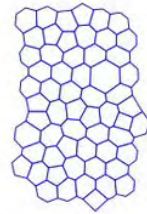
Dachs tension factor



Isometric tension & division in long axis



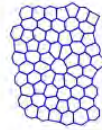
48 hrs simulated growth = ~ 45 min run time



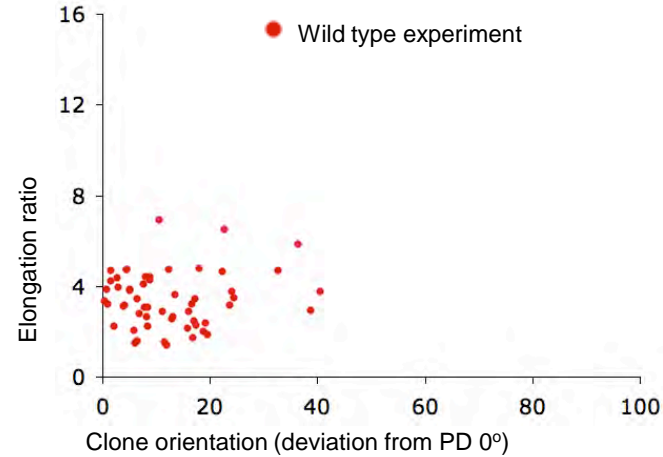
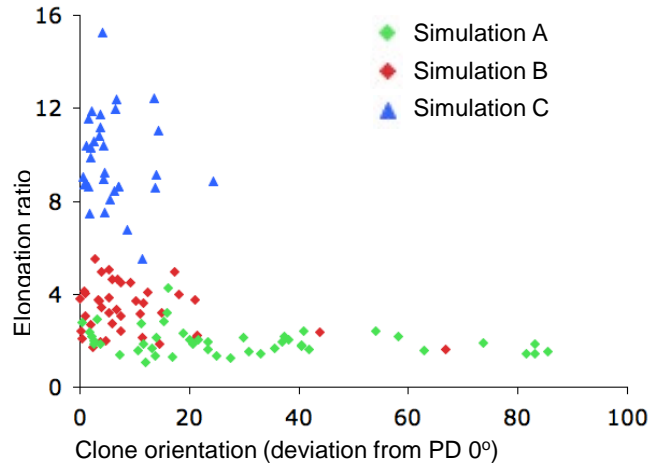
Polarized tension & division in long axis



Isometric tension & polarized cell division



Comparing simulations to *in vivo*



Maybe we parameterised (B) to get what we want? – partly true, we needed to parameterise Dachs-Max

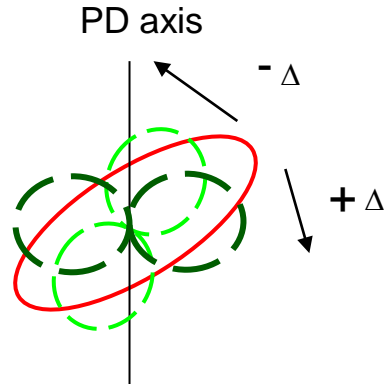
Cell shape vs spindle binding

Δ = angle between daughter cells and dividing cell

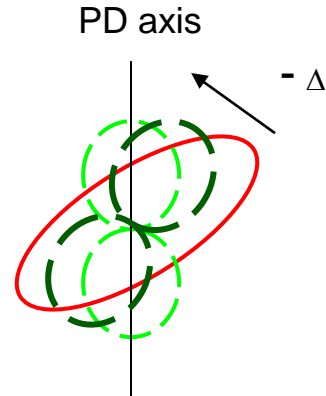
- Δ = towards P-D

+ Δ = away from P-D

cell shape

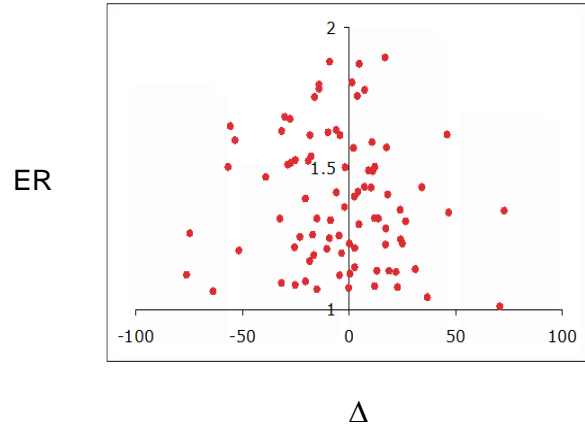


spindle

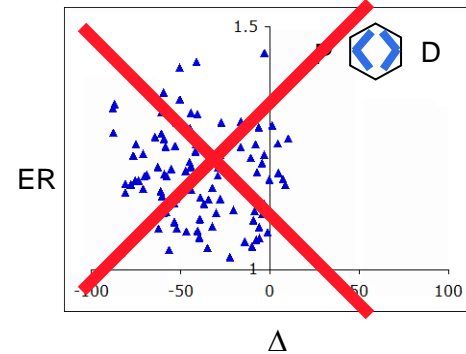
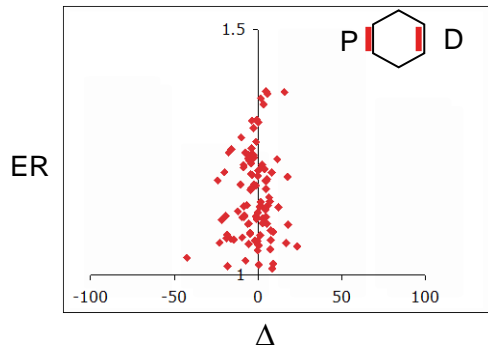


Δ Analysis

Experimentation



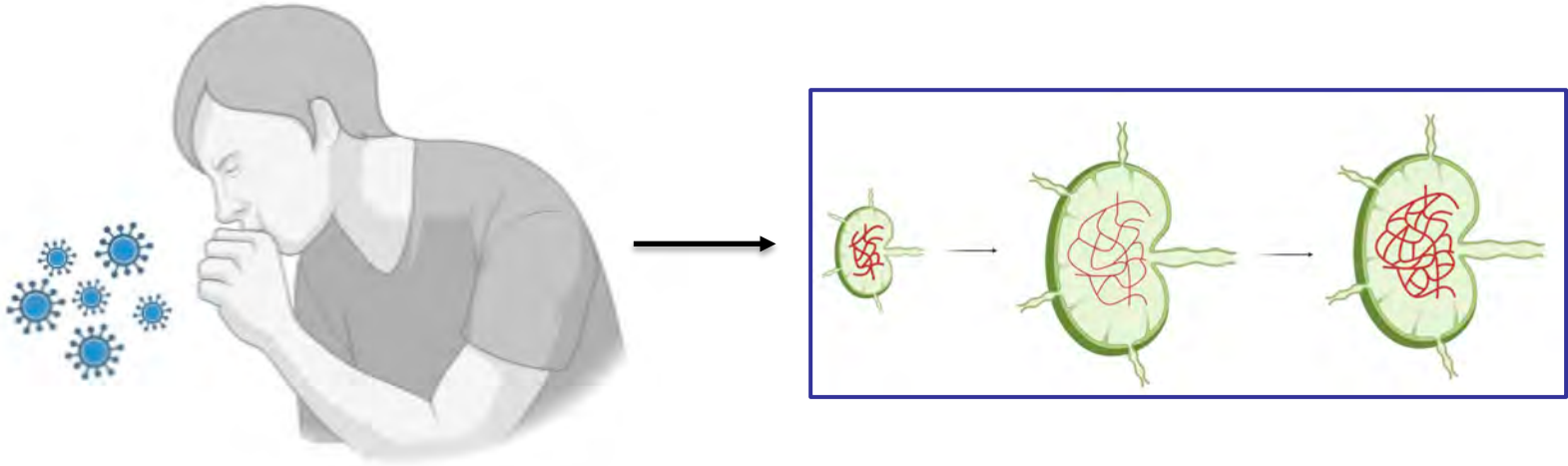
Simulations



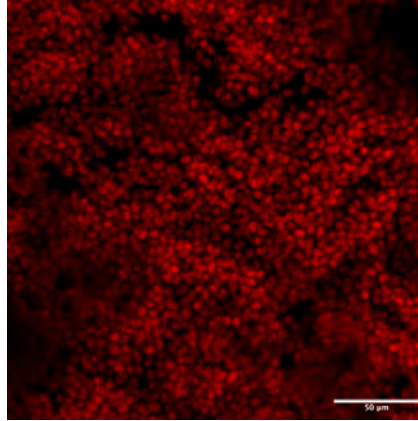
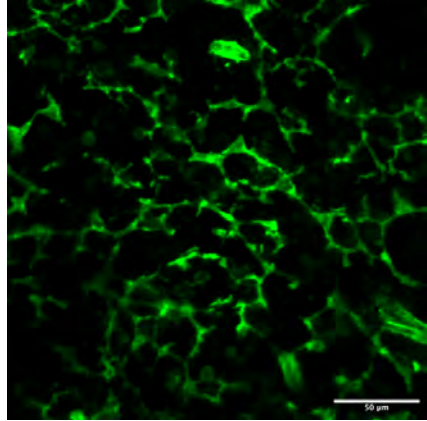
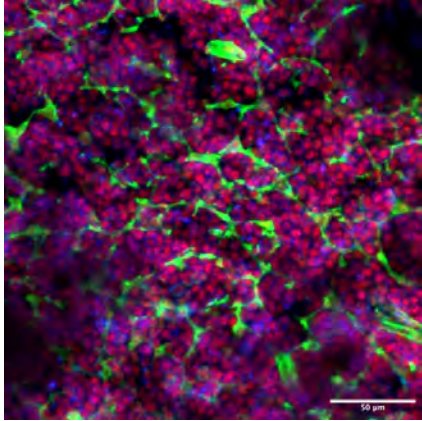
not via direct spindle binding

Exercise Questions

The Lymph Node: a dynamic homeostatic tissue

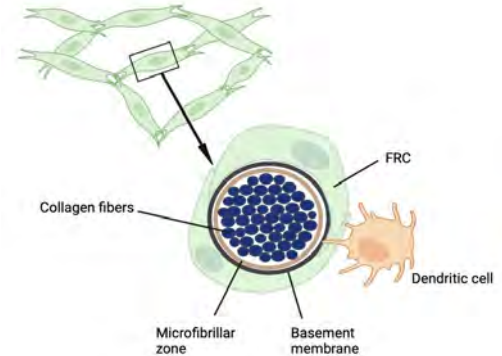
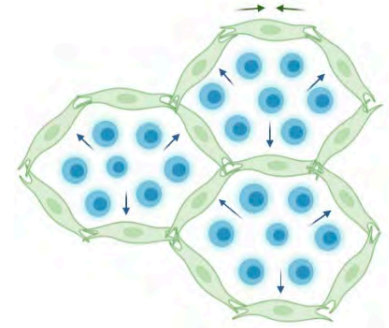


Geometry and topology of system:

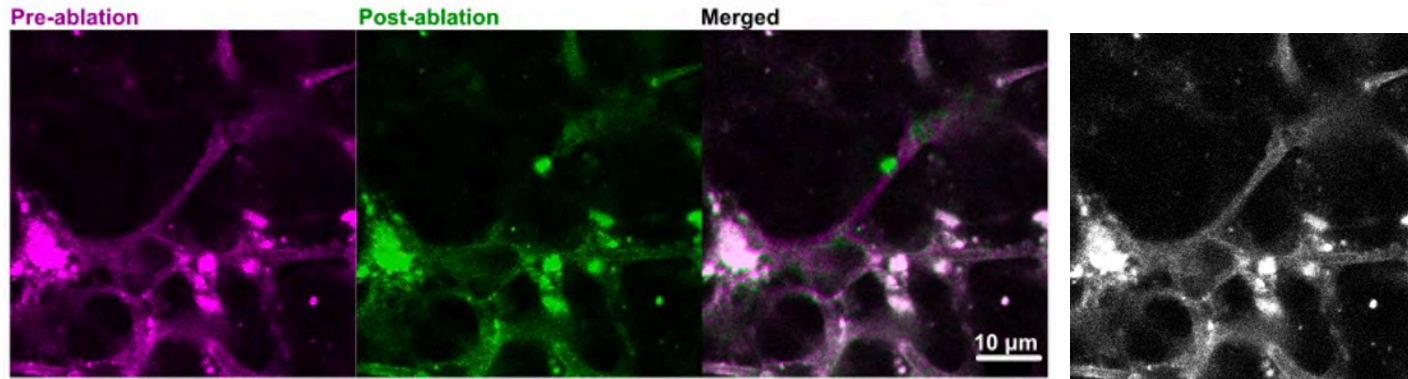


FRC Cells, T cells

FRC network cartoon

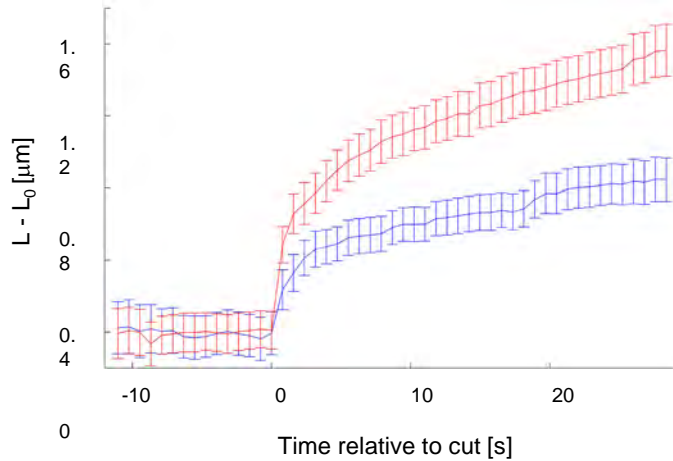
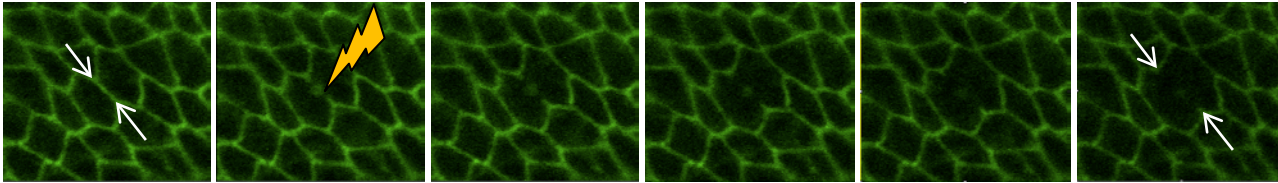


Mechanics of lymph node system:



Questions:

1. Analyze the laser ablation data provided to infer the mechanical properties of the lymph node FRC network, with and without ECM (after collagenase treatment). Infer: initial tensile force, elasticity, viscosity.
2. Laser ablation measures relative changes in tensile force, how would you measure absolute forces?
3. What does the ECM do to the mechanical properties of the FRC network?
4. How would you model the lymph node FRC network?



Assume Kelvin-Voigt model:

$$\varepsilon(t) = L(t) - L(0) = \frac{F_0}{E} \left(1 - e^{-\left[\frac{E}{\mu}\right]*t}\right)$$

Fit data to calculate:

F_0 : the tensile force before laser ablation

E : the elasticity,

μ : the viscosity coefficient.

Further reading:

Mao et al., EMBO J 2013.

Differential proliferation rates generate patterns of mechanical tension that orient tissue growth

Farhadifar et al., Current Biology 2007

Influence of cell mechanics... on epithelial packing

Tetley et al., Nature Physics, 2019.

Tissue fluidity promotes epithelial wound healing

Liang et al., Bio Protoc. 2017,

Measurement of Mechanical Tension at Cell-cell Junctions Using Two-photon Laser Ablation

Mao and Wickstrom, Nature Reviews MCB 2024,

Mechanical state transitions in the regulation of tissue form and function