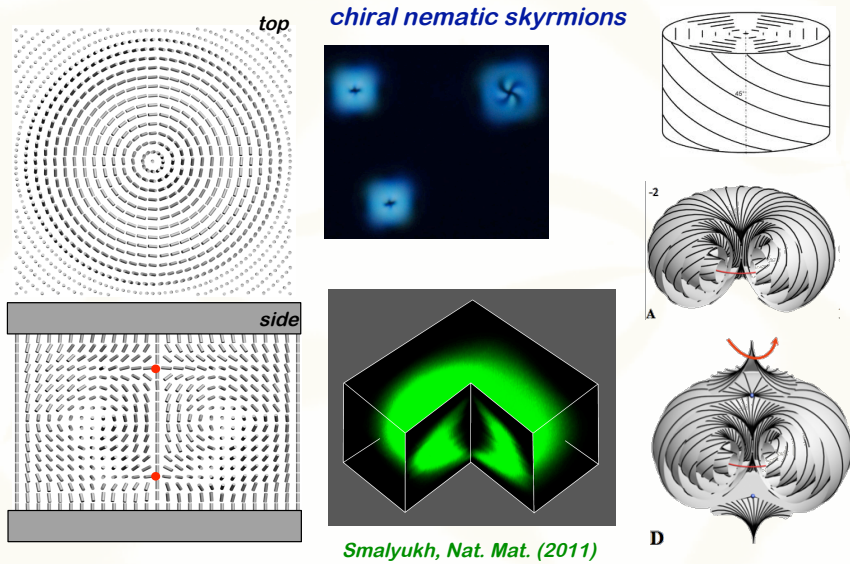
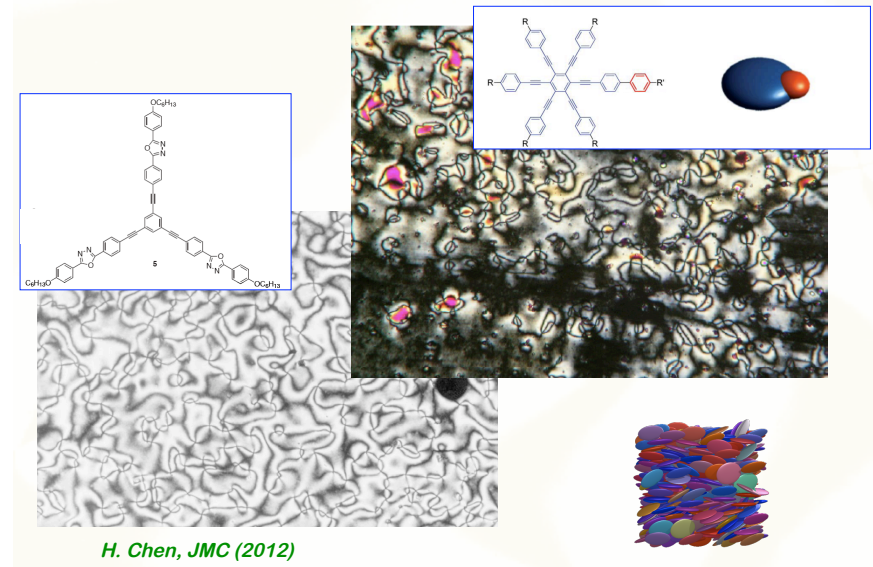


### 3D structures

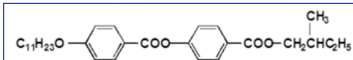


### discotic nematics

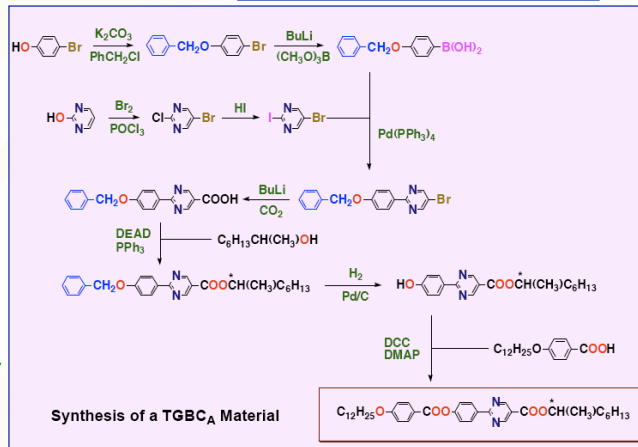
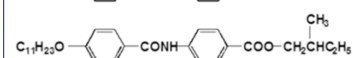


### molecules

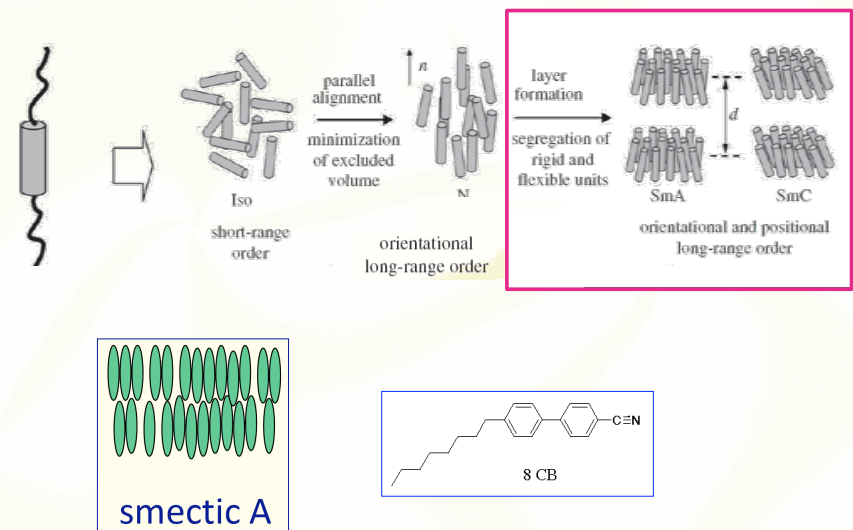
Iso - Smectics - Xtal



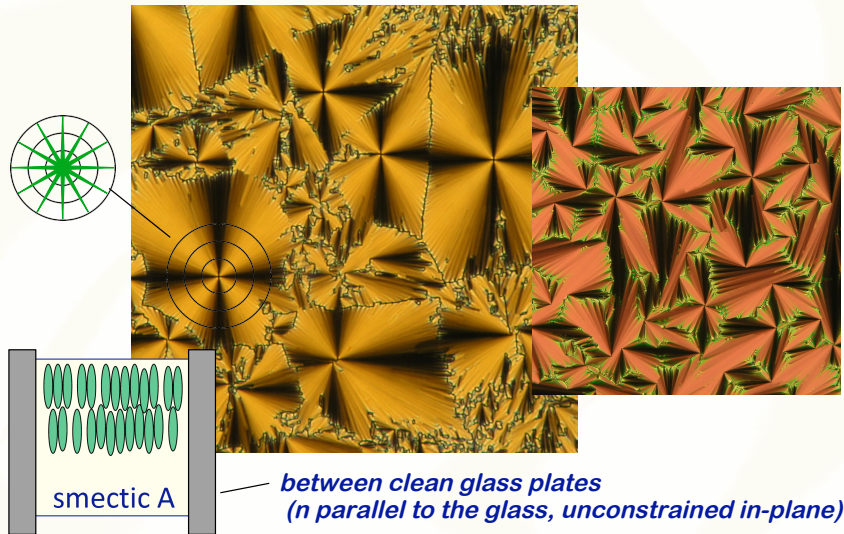
Iso - Xtal



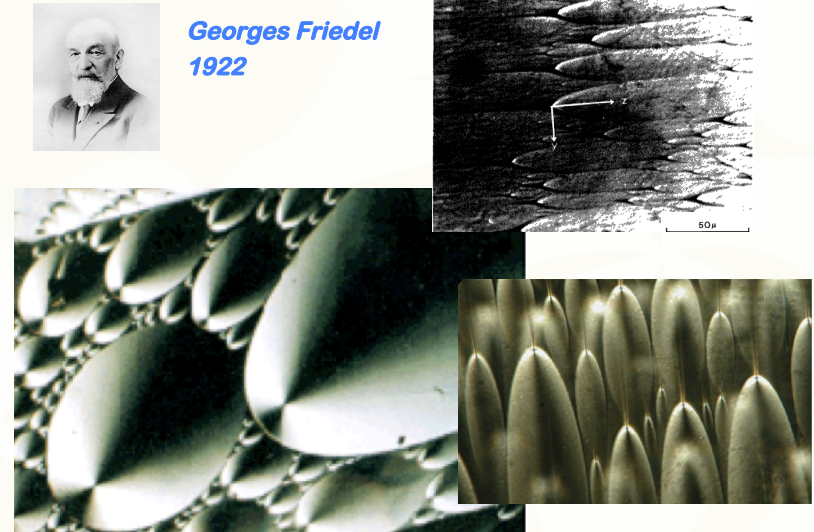
### pathways to LCs - fluid interfaces (positional ordering)



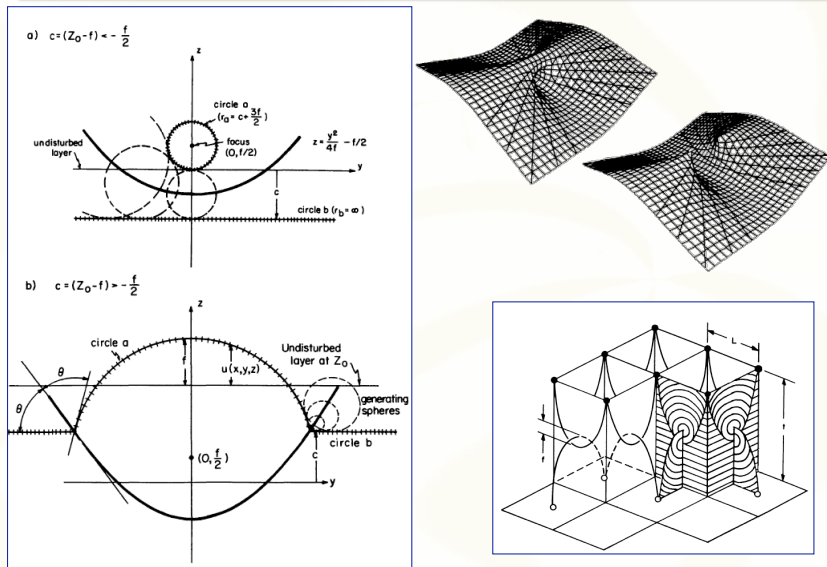
### smectic A textures



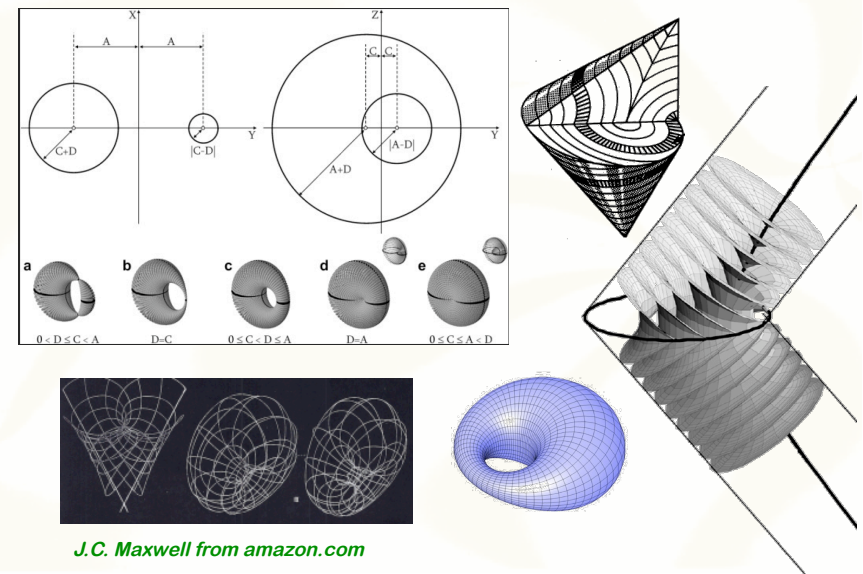
### smectic A focal conic domains



### cyclides of Dupain - parabolic



### cyclides of Dupain - ellipse / hyperbola

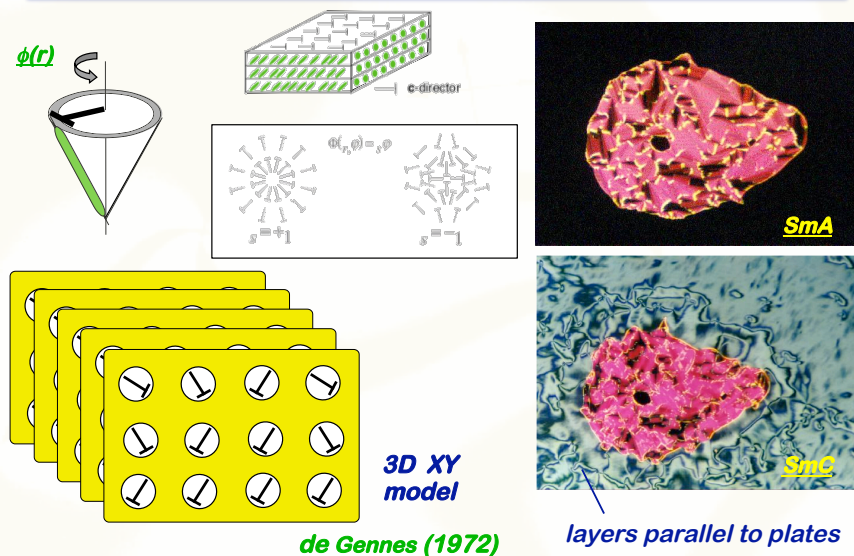




## textures - what do they depend on?

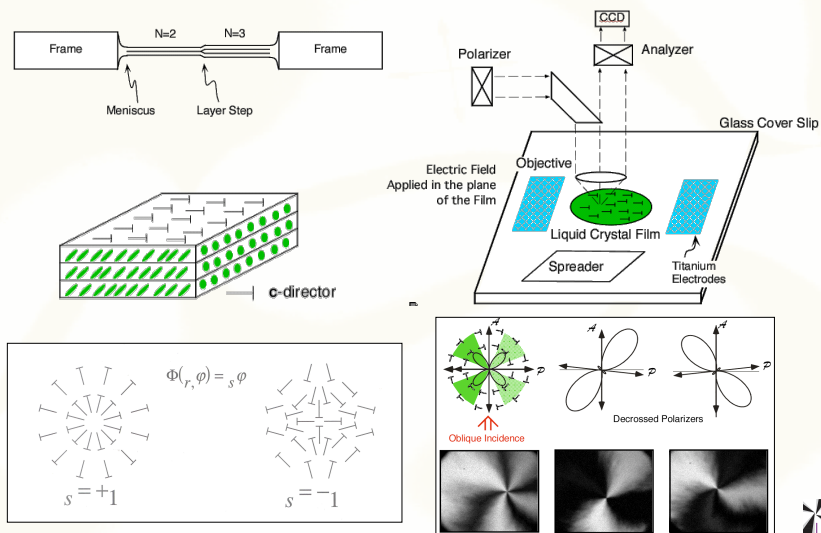
- ◆ **the phase**
- ◆ **cell thickness**
  - optics
  - structure
- ◆ **surface treatment**
- ◆ **thermal history**
  - cooling rate
  - increasing or decreasing  $T$
- ◆ **adjacent phases**
- ◆ **Impurities**
- ◆ **flow**
- ◆ **inhomogeneities**
  - quenched disorder
  - particles

## smectic C

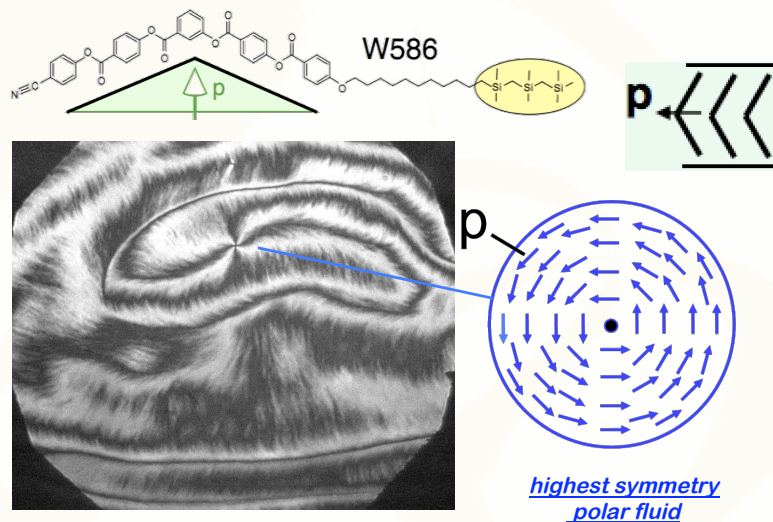


de Gennes (1972)

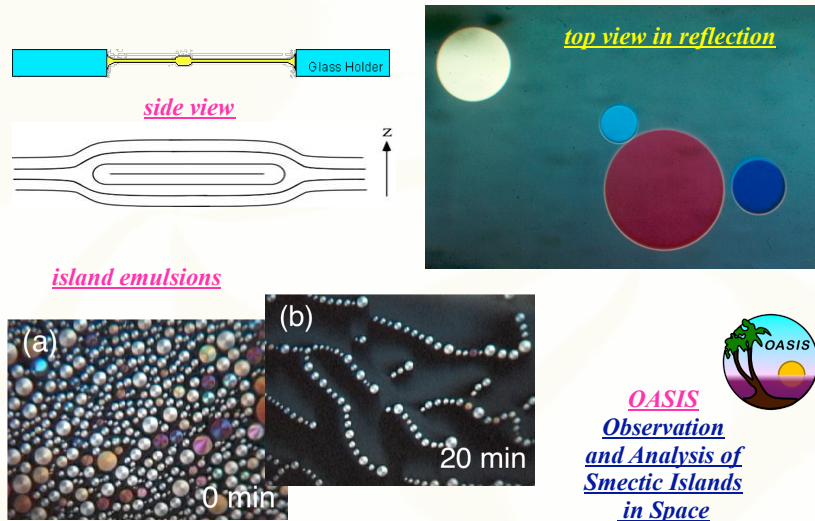
## freely suspended smectic films



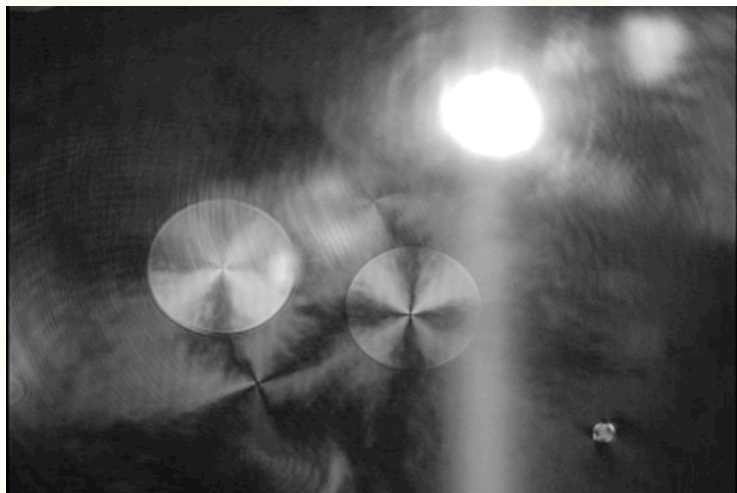
## single-layer films - polar smectic A ( $SmAP$ )



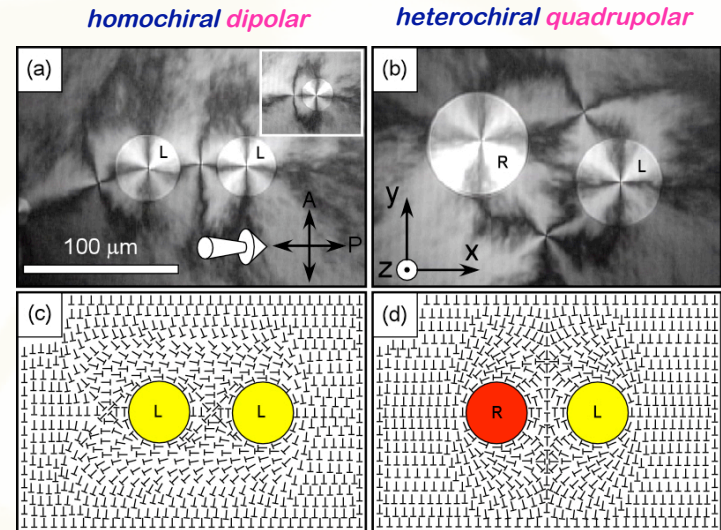
islands



real time



structure vs. handedness



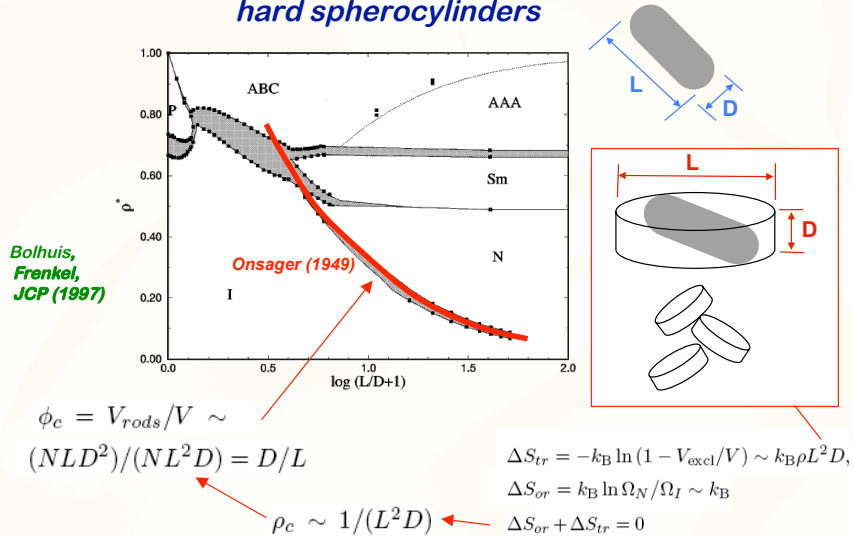
calamitic liquid crystal phases

| Nematic Phase     |  | Structures of Calamitic Nematic and Smectic Liquid Crystal Phases (Plan and Side Views) |  |  |                   |
|-------------------|--|---|--|--|-------------------|
| Orthogonal Phases |  | Tilted Phases   |  |  |                   |
|                   |  |   |  |  | Short Range Order |
|                   |  |   |  |  |                   |
|                   |  |   |  |  | Long Range Order  |

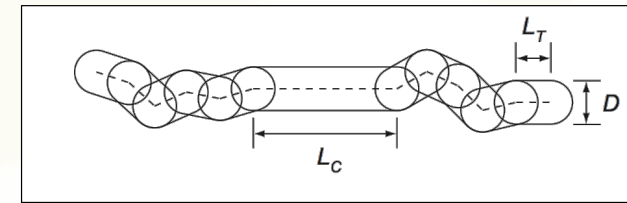


## molecular origins of nematics, smectics

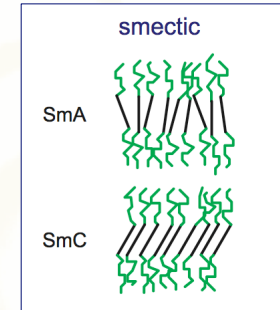
### hard spherocylinders



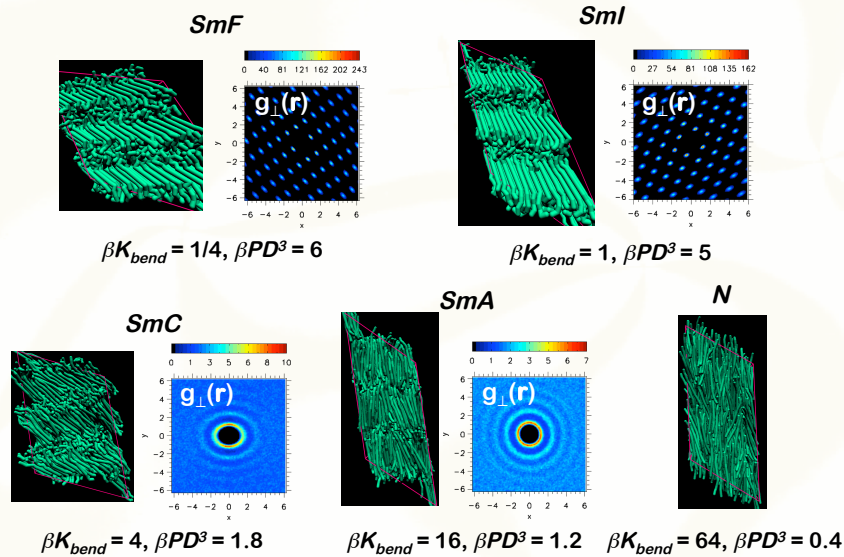
## adding flexible tails...



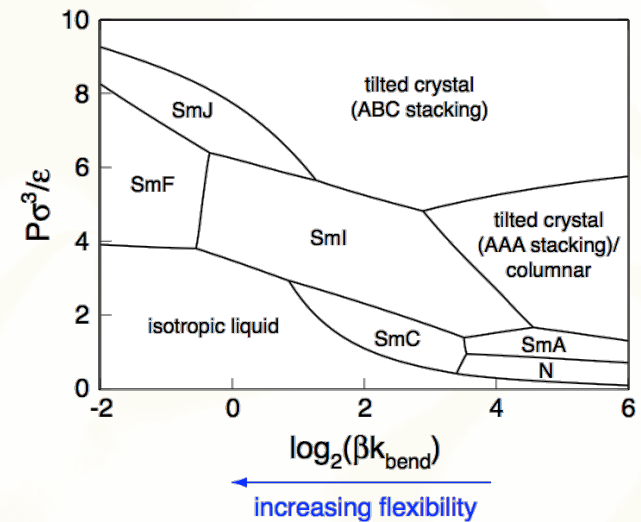
- ◆ soft spherocylinder polymer with rigid core and flexible chains
- ◆ molecular flexibility controlled by bond angle bending spring constant  $K_{bend}$
- ◆ studied using NPT MD simulation



## gives smectic phases



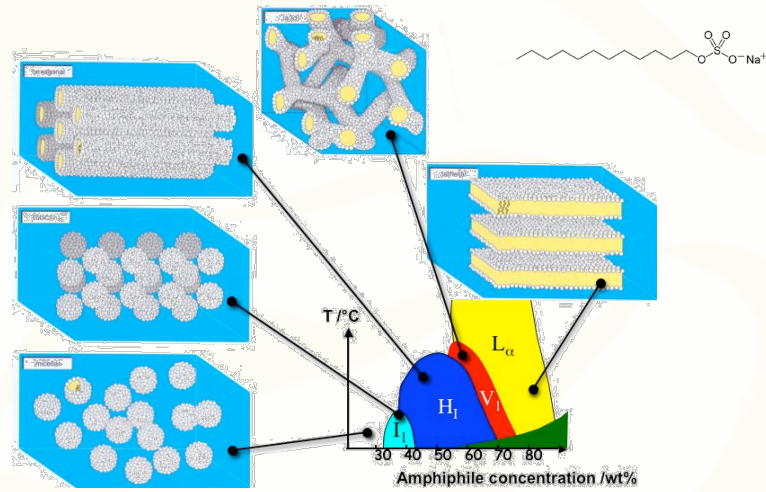
## phase diagram of flexible-tail spherocylinders







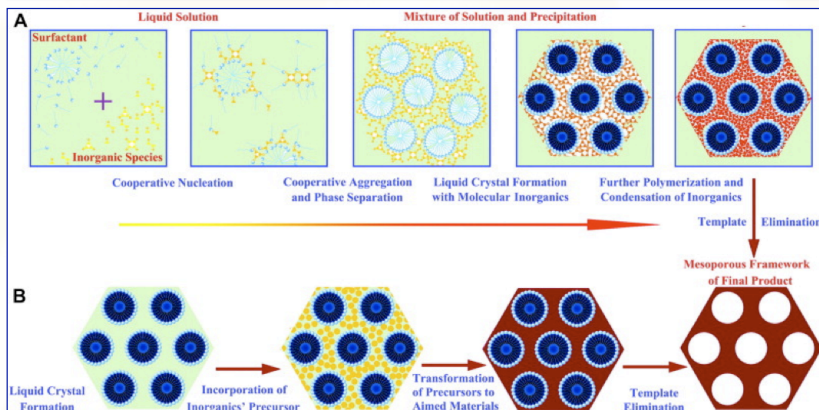
## lyotropics



## lyotropic variations

| Flat layers       | Undulated layers                          | Perforated layers                                  | Bicontinuous networks                   | Ribbon-phases                       | Columns          |                   |
|-------------------|---|--|---|-------------------------------------|------------------|-------------------|
| SmA<br>$L_\alpha$ | Egg-carton<br>Undulated<br>Superundulated | Random mesh<br>Square mesh<br>Tetragonal<br>$I4mm$ | Hexagonal mesh<br>Rhombohedral<br>$R3m$ | $Im3m$<br>$Ia3d$<br>$Pn3m$<br>$R3c$ | $c2mm$<br>$p2gg$ | $Col_h$<br>$p6mm$ |

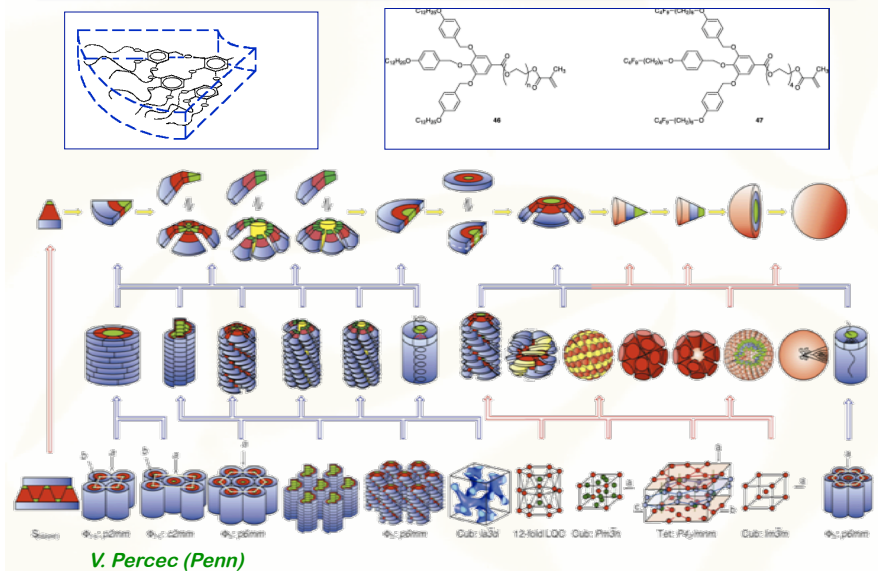
## nanoporous silica from lyotropic liquid crystals



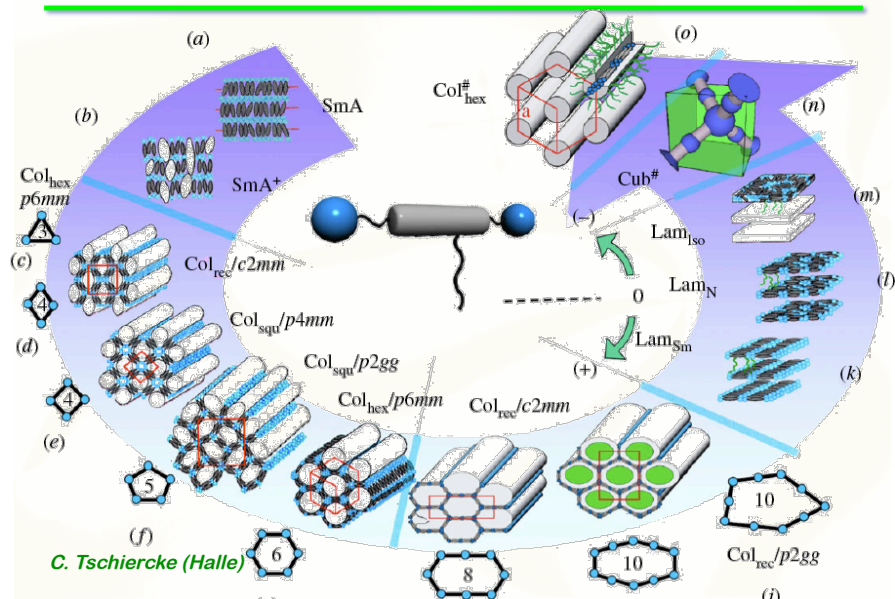
1. Title: ORDERED MESOPOROUS MOLECULAR-SIEVES SYNTHESIZED BY A LIQUID-CRYSTAL TEMPLATE MECHANISM  
 Author(s): KRESGE CT; LEONOWICZ ME; ROTH WJ; et al.  
 Source: NATURE Volume: 359 Issue: 6397 Pages: 710-712 DOI: 10.1038/359710a0 Published: OCT 22 1992  
 Times Cited: 9,613 (from Web of Science)

~ 10 of the 20 most cited liquid crystal papers

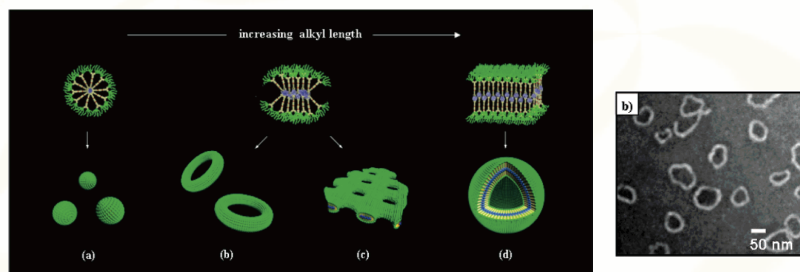
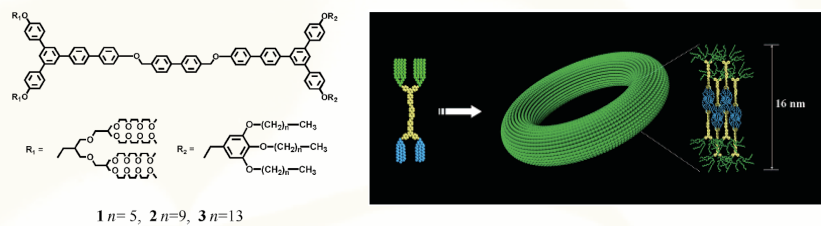
## hierarchical self assembly



## bola-amphiphiles

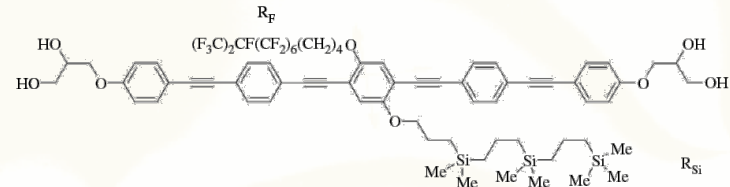


## agressive amphiphilics

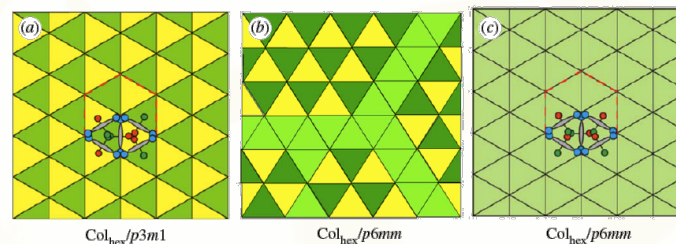


Myongsoo Lee (Seoul)

## bola-amphiphiles

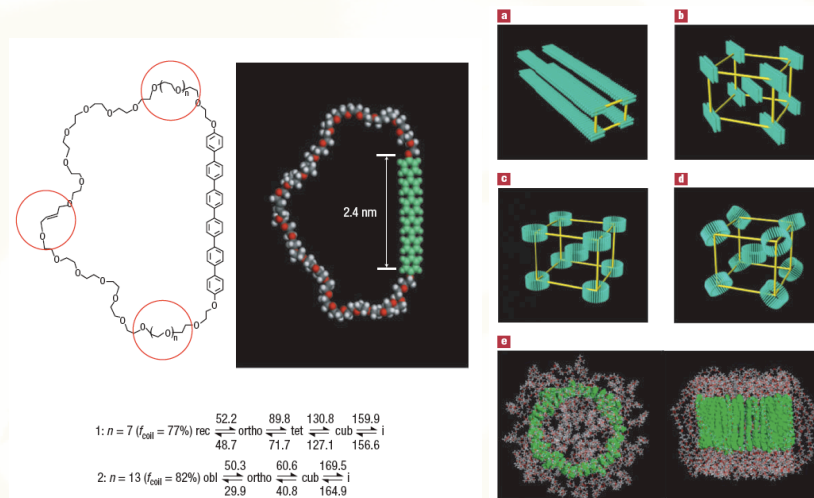


Cr 83 Col<sub>hex</sub>/p3m1 85 Col<sub>hex</sub>/p6mm 189 Iso (°C)



C. Tschiercke (Halle)

## amphiphilic rings

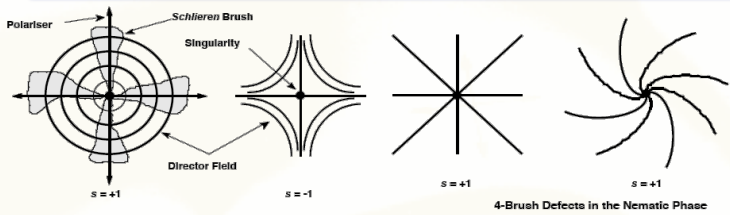


Myongsoo Lee (Seoul)

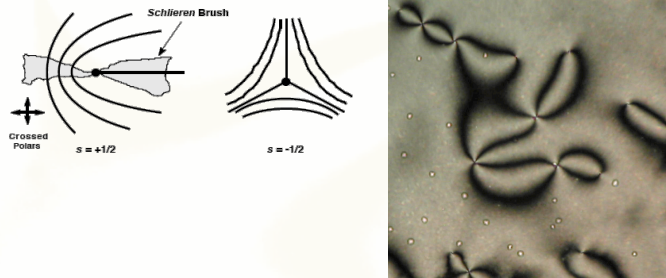




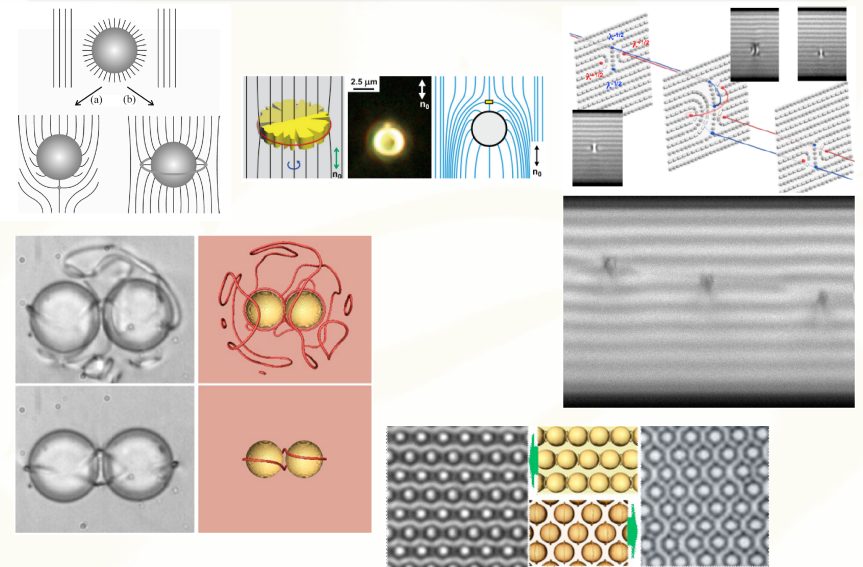
## defects- 2D



2-Brush Singularities in the Nematic Phase



## nematic defects – 3D



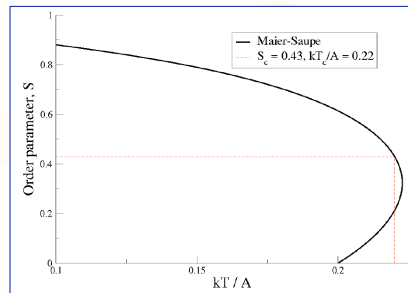
## Maier – Saue model of the isotropic / nematic transition

$$S = \langle \frac{1}{2} (3 \cos^2 \theta - 1) \rangle \quad S = \frac{2\pi}{Z} \int_0^\pi \left( \frac{3}{2} \cos^2 \theta - \frac{1}{2} \right) \exp \left[ -\frac{V(\theta, S)}{kT} \right] \sin \theta d\theta$$

$$V(\theta, S) = -AS \left( \frac{3}{2} \cos^2 \theta - \frac{1}{2} \right) \quad Z = 2\pi \int_0^\pi \exp \left[ -\frac{V(\theta, S)}{kT} \right] \sin \theta d\theta$$

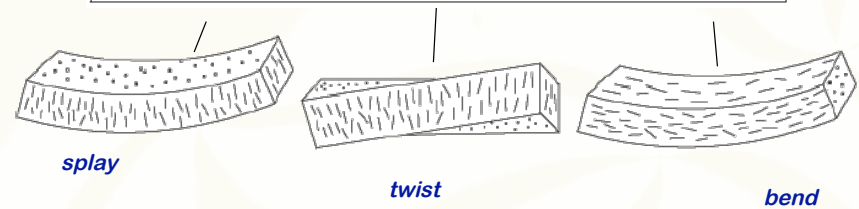
$$S = \frac{3}{4} \left[ \frac{\exp(x^2)}{xD(x)} - \frac{1}{x^2} \right] - \frac{1}{2}$$

$$\frac{kT}{A} = \frac{3S}{2x^2}$$



## nematic elasticity

$$g = \frac{1}{2} k_{11} (\nabla \cdot \mathbf{n})^2 + \frac{1}{2} k_{22} (\mathbf{n} \cdot \text{curl } \mathbf{n})^2 + \frac{1}{2} k_{33} (\mathbf{n} \times \text{curl } \mathbf{n})^2$$



$$g = \frac{1}{2} k_{22} \left( \frac{\partial \theta}{\partial z} \right)^2$$



$$\frac{\partial^2 \theta}{\partial z^2} = 0 \quad \theta = \alpha z$$



Oseen / Frank (1930s – 1950s)



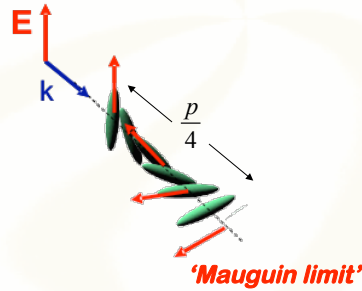
## optical properties: polarization rotation

1911



Charles Mauguin

- constructs nematic cells
- surface alignment by rubbing glass with paper
- observes that polarization follows optic axis if  $\lambda \ll p$



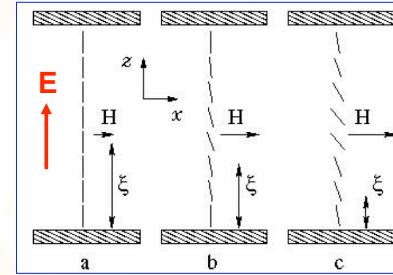
## coupling to applied fields

$$g_m = \frac{1}{2} \bar{H} \cdot \bar{\chi} \cdot \bar{H}$$

$$\chi_{ij} = \chi_{\perp} \delta_{ij} + \chi_a n_i n_j \quad \chi_a = \chi_{\parallel} - \chi_{\perp}$$

$$g_m = -\frac{1}{2} \chi_{\perp} H^2 - \frac{1}{2} \chi_a (\mathbf{n} \cdot \mathbf{H})^2$$

$$g_e = -\frac{1}{8\pi} \epsilon_{\perp} E^2 - \frac{1}{8\pi} \epsilon_a (\mathbf{n} \cdot \mathbf{E})^2$$



Fredericksz transition

$$n_x = \sin \theta(z), \quad n_y = 0, \quad n_z = \cos \theta(z)$$

$$\nabla \cdot \mathbf{n} = -\sin \theta \frac{\partial \theta}{\partial z}$$

$$\nabla \times \mathbf{n} = \mathbf{j} \cos \theta \frac{\partial \theta}{\partial z}$$

$$\mathbf{n} \cdot (\nabla \times \mathbf{n}) = 0$$

$$\mathbf{n} \times \text{curl } \mathbf{n} = (kn_x - in_z) \cos \theta \frac{\partial \theta}{\partial z}$$

## Fredericksz transition...

1931:



V.K. Fredericksz

$$g = \frac{1}{2} \int_{-d/2}^{d/2} dz \left[ (k_{11} \sin^2 \theta + k_{33} \cos^2 \theta) \left( \frac{\partial \theta}{\partial z} \right)^2 - \chi_a H^2 \sin^2 \theta \right]$$

$$g = \frac{1}{2} \frac{k}{\xi^2} \int_{-d/2}^{d/2} dz \left[ \xi^2 \left( \frac{\partial \theta}{\partial z} \right)^2 - \sin^2 \theta \right] \quad \xi = \sqrt{k/\chi_a H^2}$$

$$\xi^2 \frac{\partial^2 \theta}{\partial z^2} + \sin \theta \cos \theta = 0$$

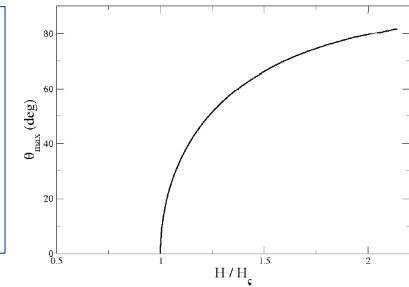
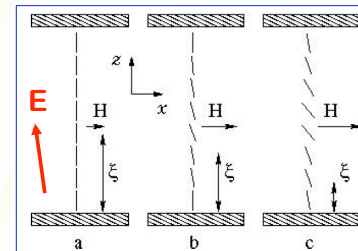
$$\xi^2 \left( \frac{\partial \theta}{\partial z} \right)^2 + \sin^2 \theta = \sin^2 \theta_m$$

$$\frac{1}{2} d - z = \xi \int_0^{\theta} \frac{d\theta'}{(\sin^2 \theta_m - \sin^2 \theta')^{1/2}} = \xi \csc \theta_m F(\csc \theta_m, \theta)$$

$$\frac{1}{2} d = \xi \csc \theta_m F(\csc \theta_m, \theta_m) = \xi K(\sin \theta_m)$$

## Fredericksz transition

$$H_c = \sqrt{\frac{k_{33}}{\chi_a} \frac{\pi}{d}} \quad \theta_m \sim 2 \left[ \frac{H}{H_c} - 1 \right]^{1/2}$$



## dynamics

static equilibrium: torque unbalance =  $\xi^2 \frac{\partial^2 \theta}{\partial z^2} + \sin \theta \cos \theta = 0$

dynamic torque unbalance =  $\gamma \frac{\partial \theta}{\partial t} = K \frac{\partial^2 \theta}{\partial z^2} + \epsilon_0 \Delta \epsilon E^2 \sin \theta \cos \theta$

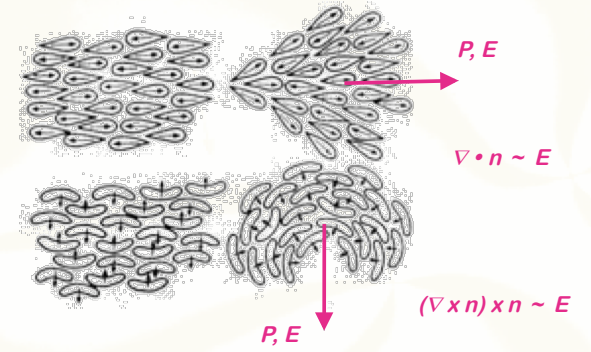
reorientation time

$$\tau = \frac{\gamma d^2}{\pi^2 K (1 - (E/E_c)^2)}$$

## flexoelectricity

$P = e_1 n (\nabla \cdot n)$   
splay

$P = e_3 (\nabla \times n) \times n$   
bend



for bend in an electric field:

$$g = K/2 [(\nabla \times n) \times n]^2 + E \cdot [(\nabla \times n) \times n]$$

$(\nabla \times n) \times n \sim E$

R.B. Meyer, PRL (1969)



## chirality - blue phases

