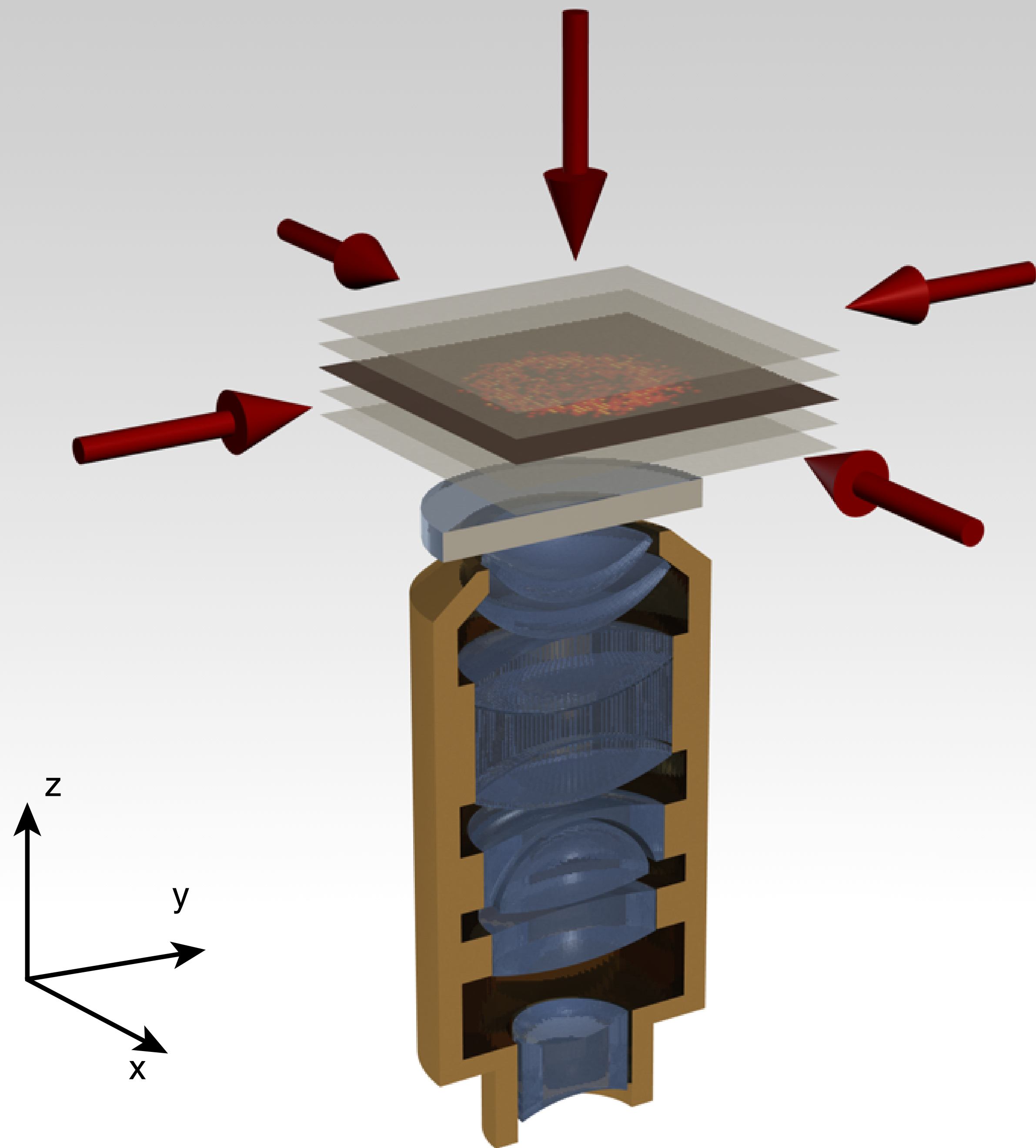


# Quantum Gas Microscopy

# Quantum Gas Microscopy





# Quantum Gas Microscopy

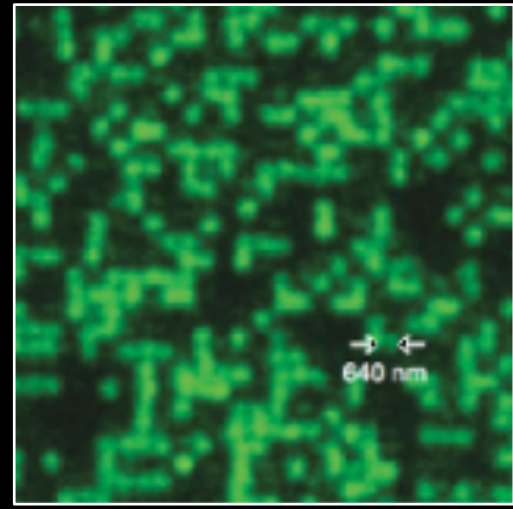
K. Kwon et al., Phys. Rev. A (2022)

W. Bakr et al., Science (2010)  
J. Sherson et al., Nature (2010)

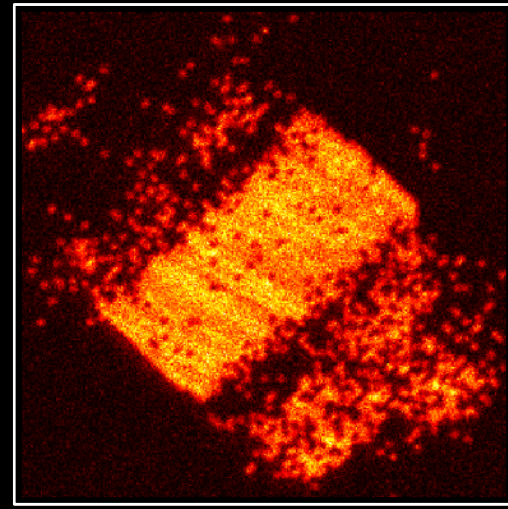


# Quantum gas microscopes

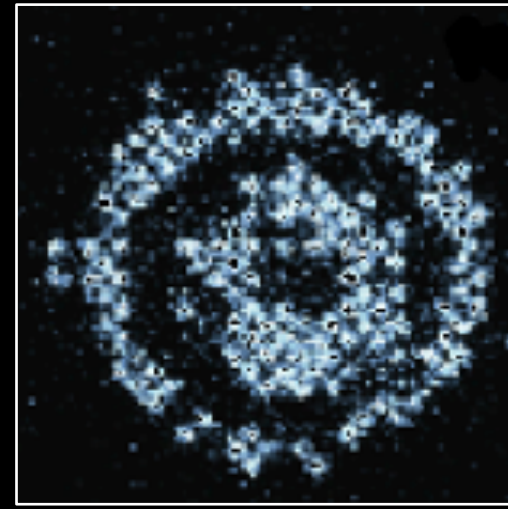
## BOSONS



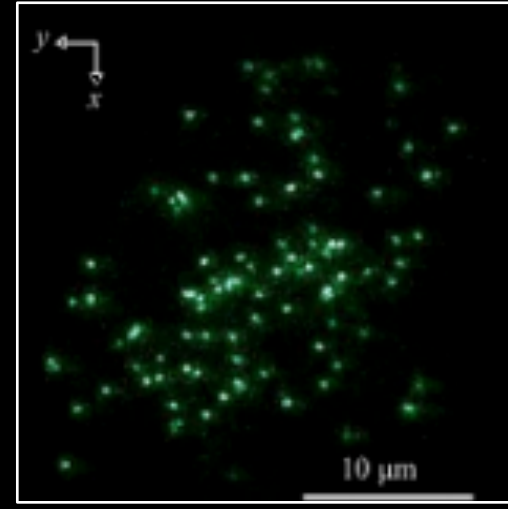
Harvard,  $^{87}\text{Rb}$



Munich,  $^{87}\text{Rb}$

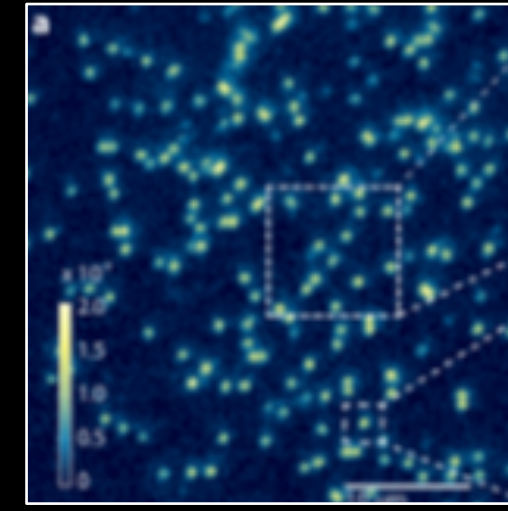


Tokyo,  $^{174}\text{Yb}$

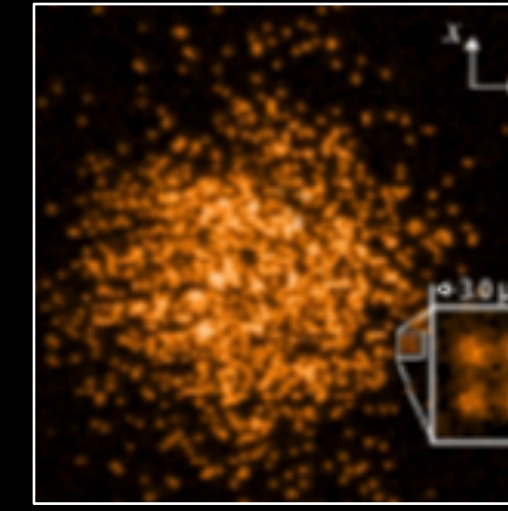


Kyoto,  $^{174}\text{Yb}$

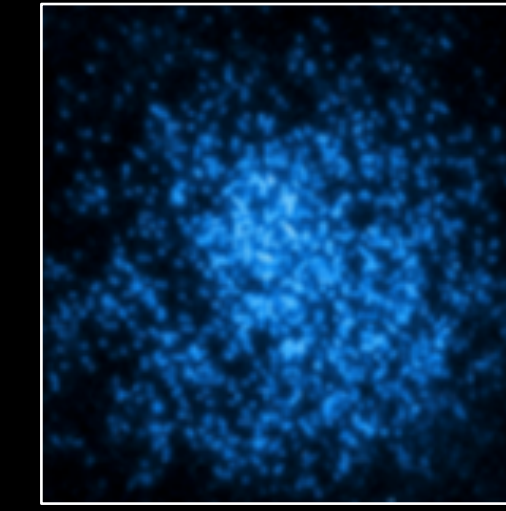
## FERMIONS



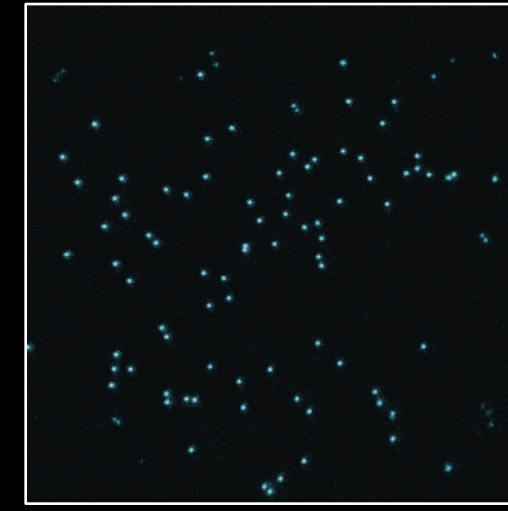
Glasgow,  $^{40}\text{K}$



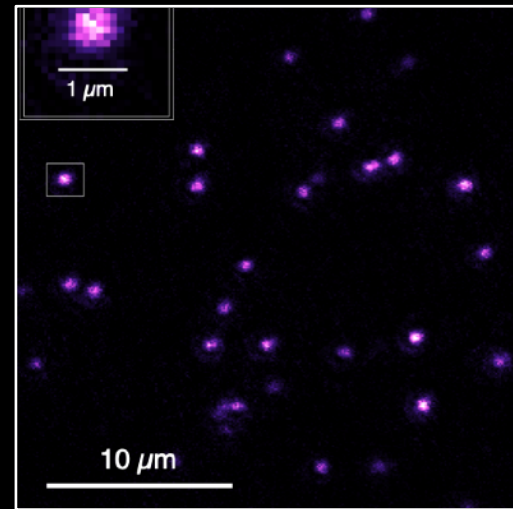
MIT,  $^{40}\text{K}$



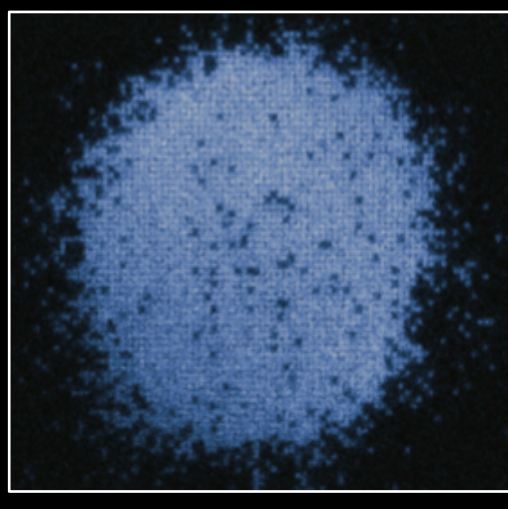
Harvard,  $^6\text{Li}$



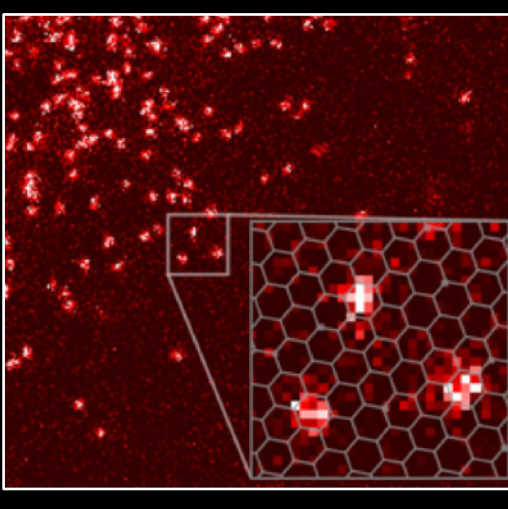
Princeton, NaRb



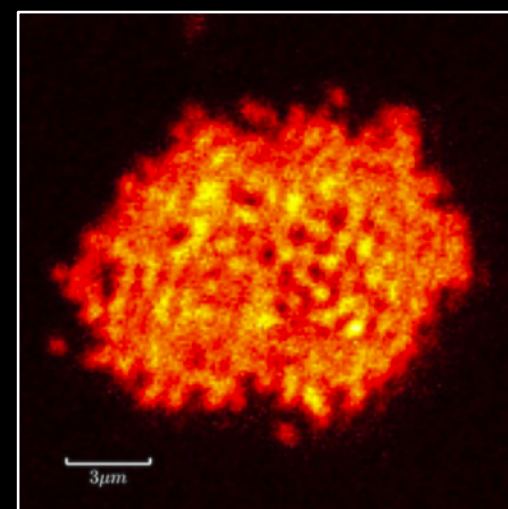
Aarhus,  $^{87}\text{Rb}$



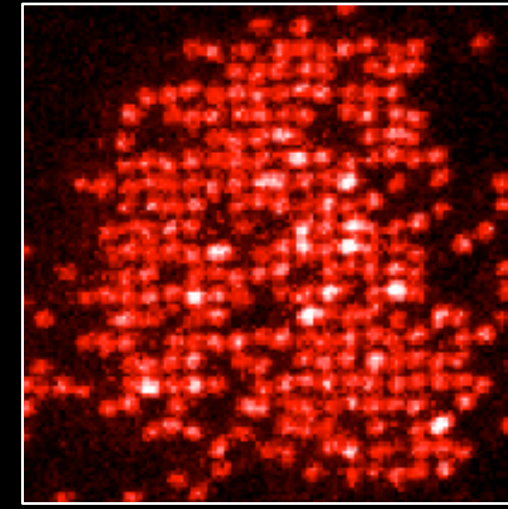
KAIST,  $^7\text{Li}$



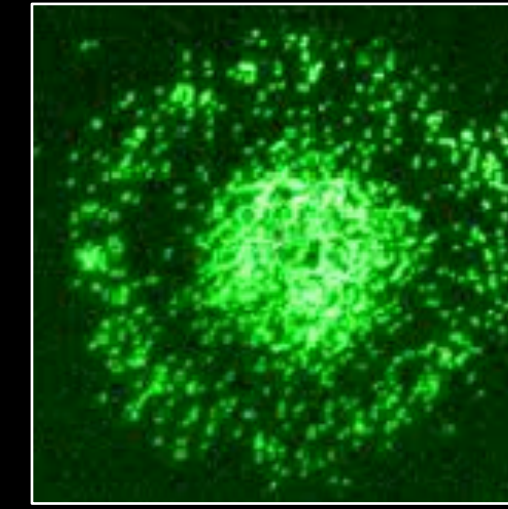
RIKEN,  $^{87}\text{Rb}$



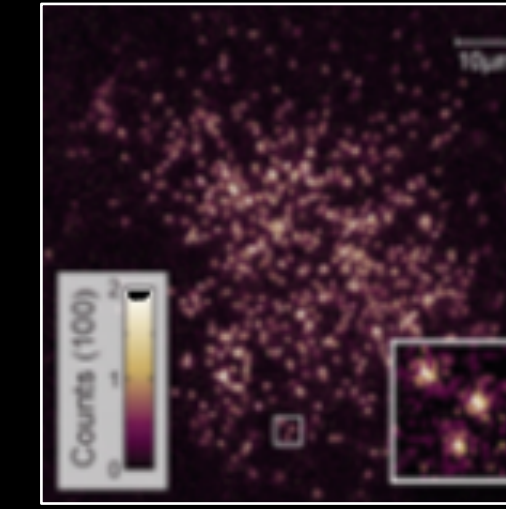
USTC,  $^{87}\text{Rb}$



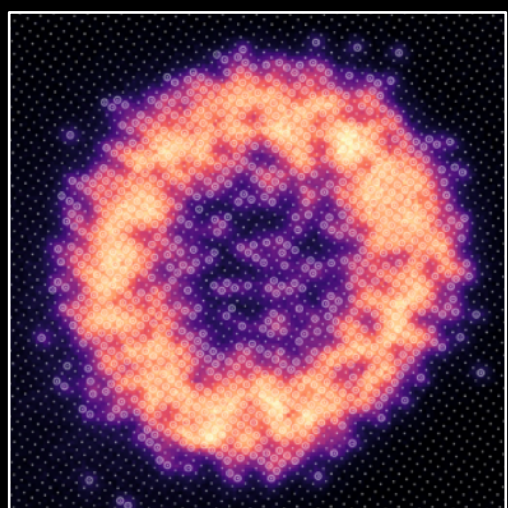
Munich,  $^6\text{Li}$



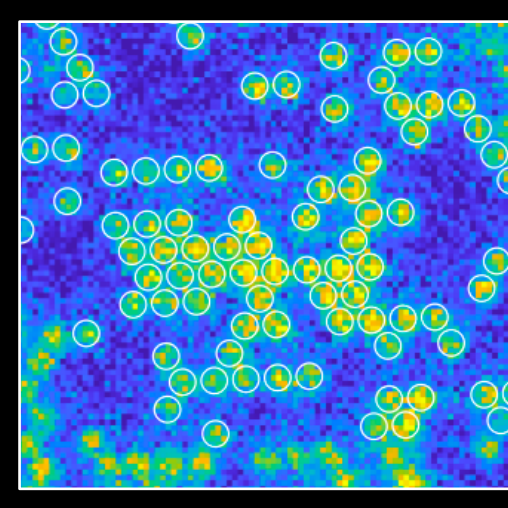
Princeton,  $^6\text{Li}$



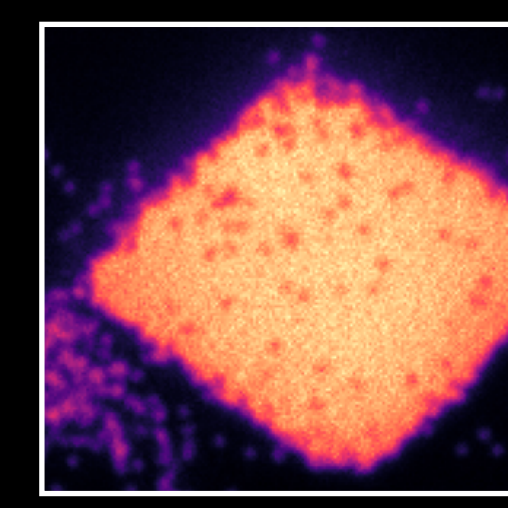
Toronto,  $^{40}\text{K}$



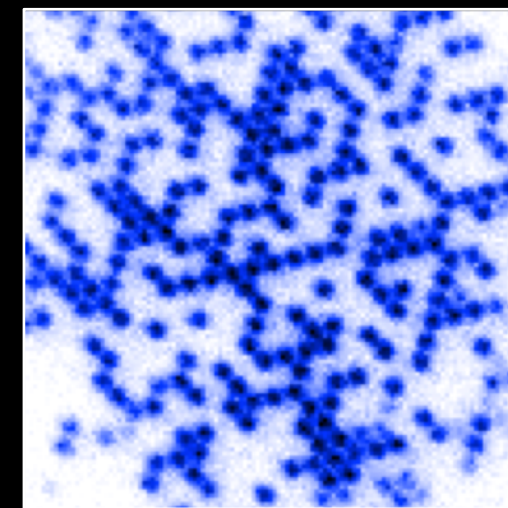
Munich,  $^{133}\text{Cs}$



Chicago,  $^{133}\text{Cs}$



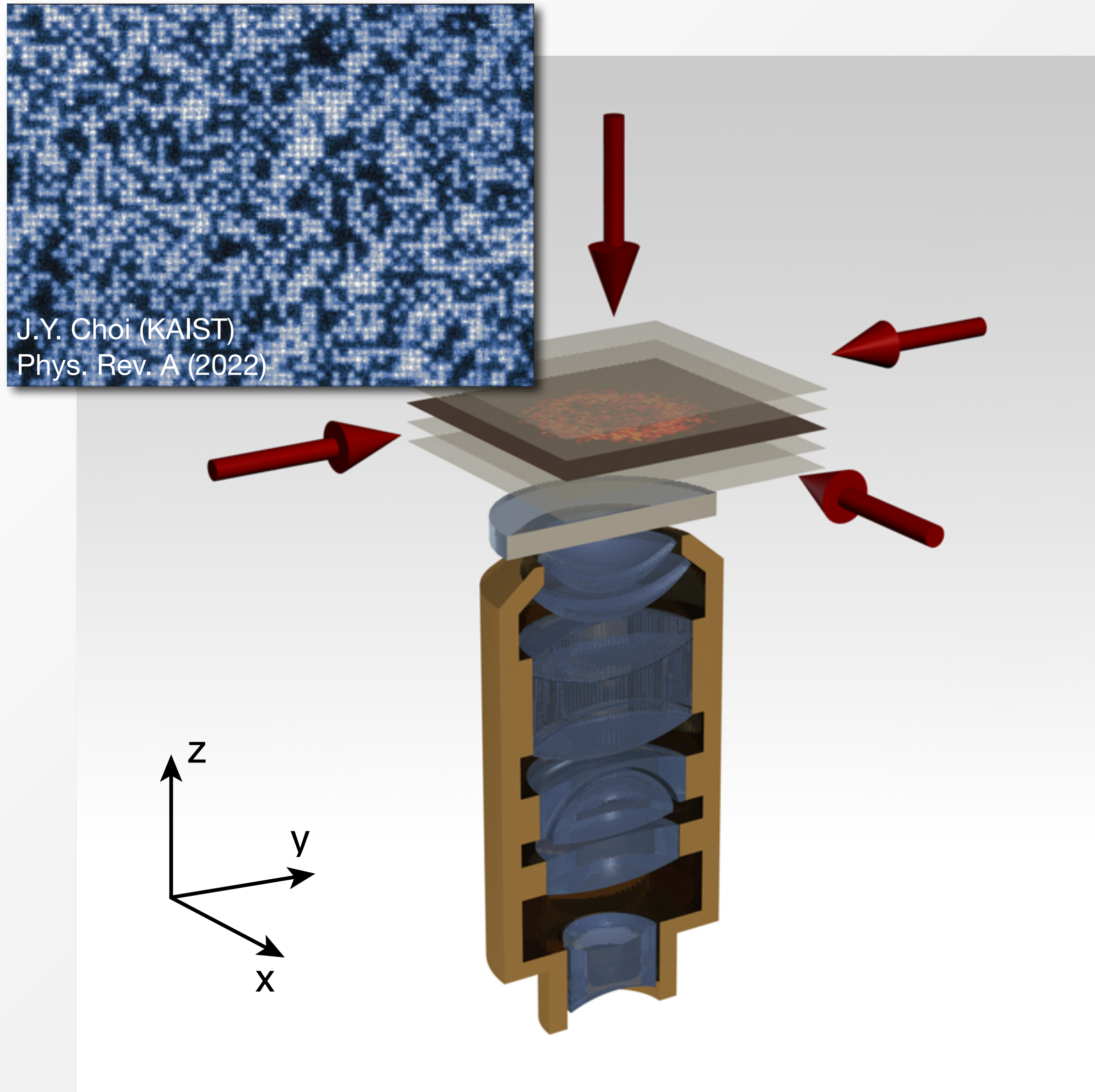
Munich,  $^{133}\text{Cs}$



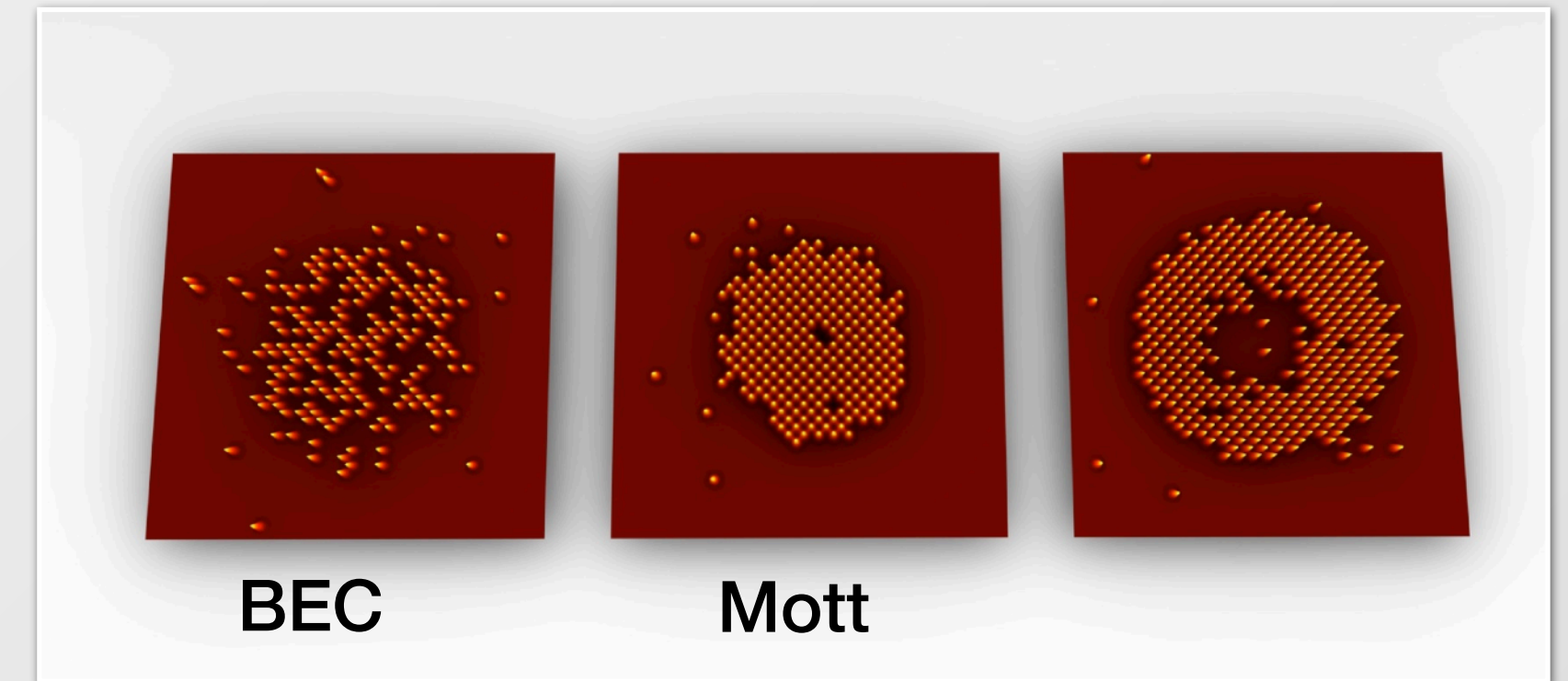
Virginia,  $^6\text{Li}$

Harvard,  $^{16}\text{xEr}$

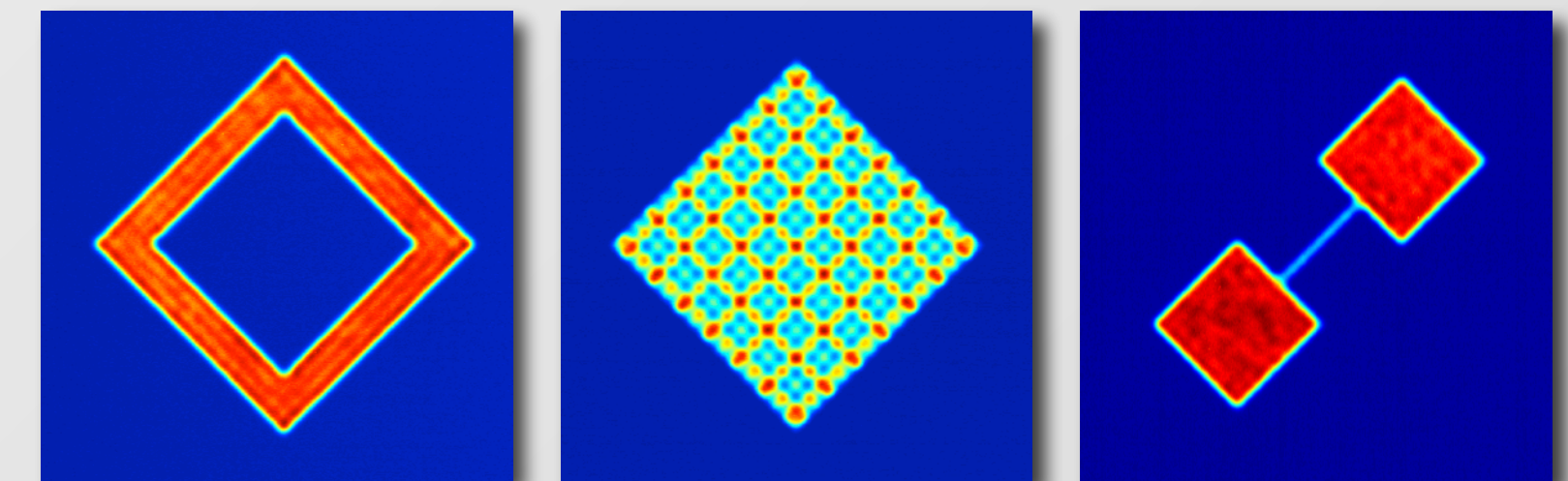




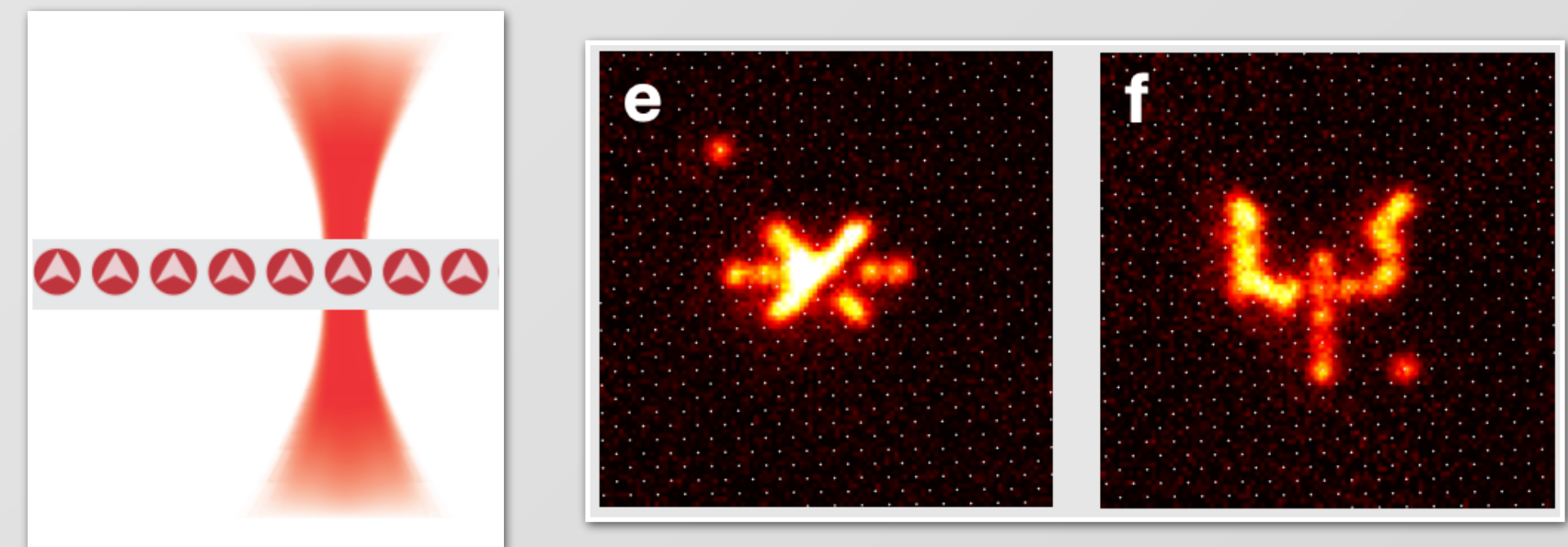
## Single atom detection



## Potential Engineering



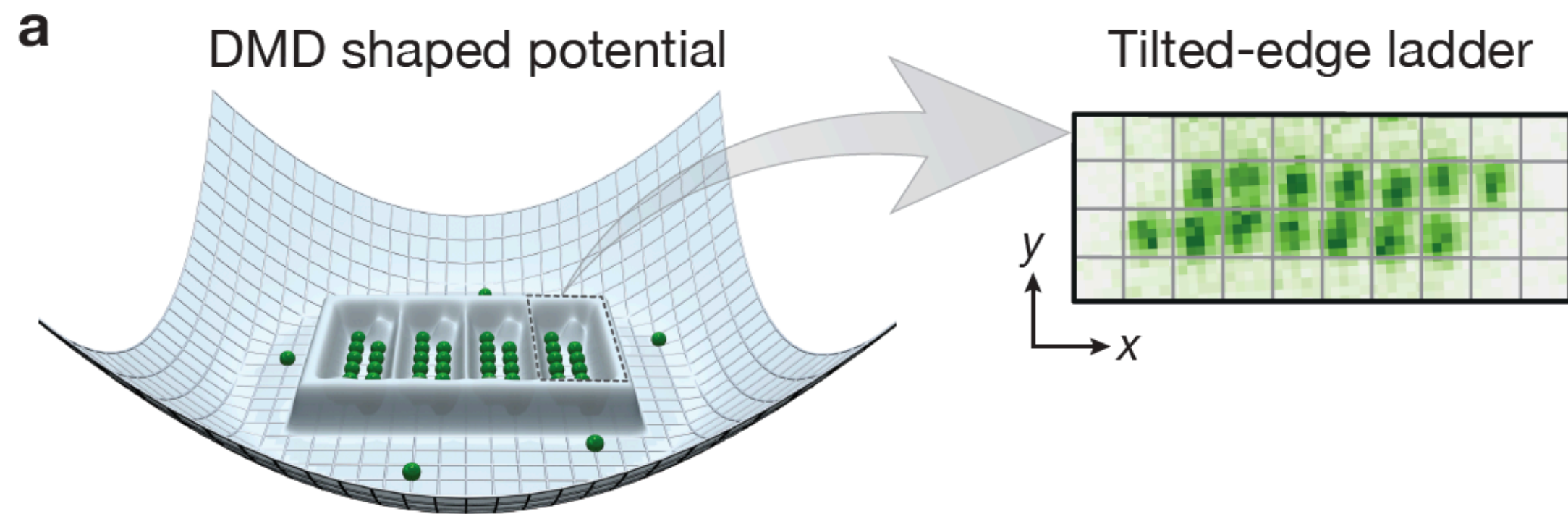
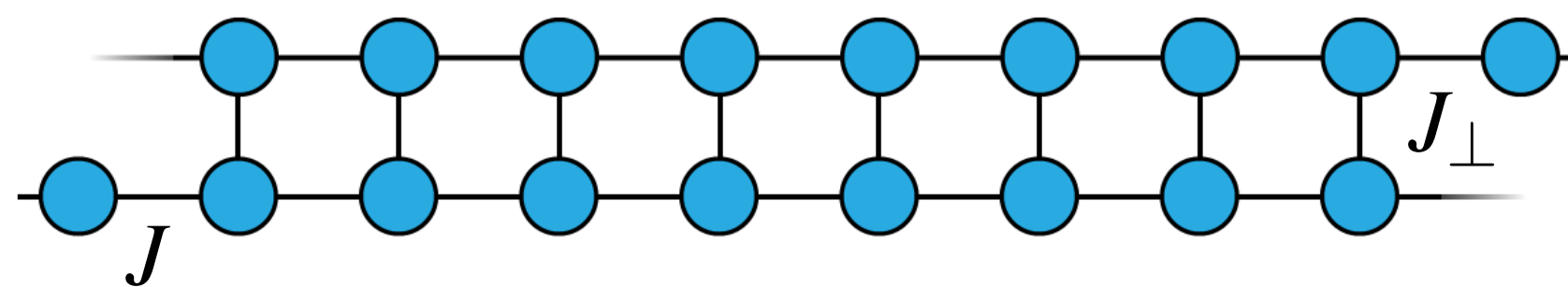
## Single Atom Addressing



W. Bakr et al., Science (2010) & J. Sherson et al., Nature (2010)  
**Addressing:** C. Weitenberg et al., Nature (2011)

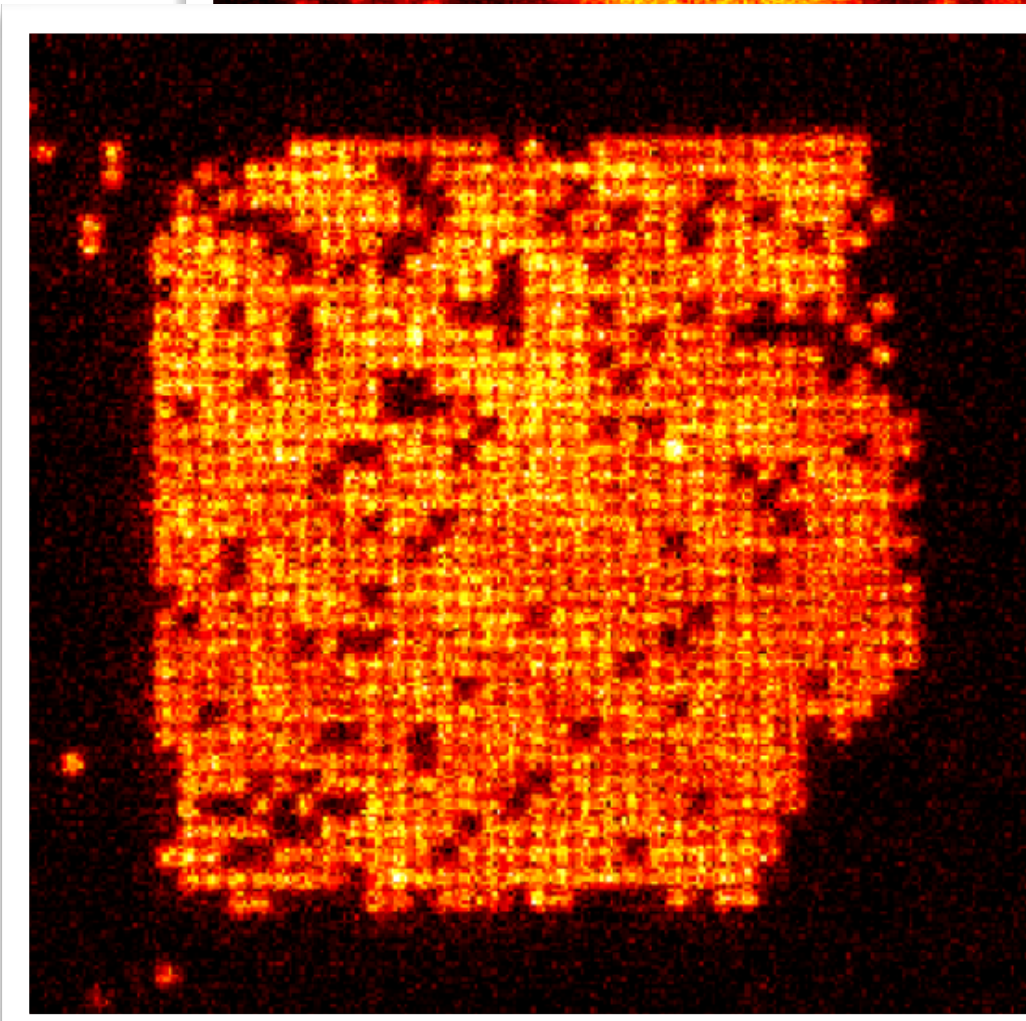
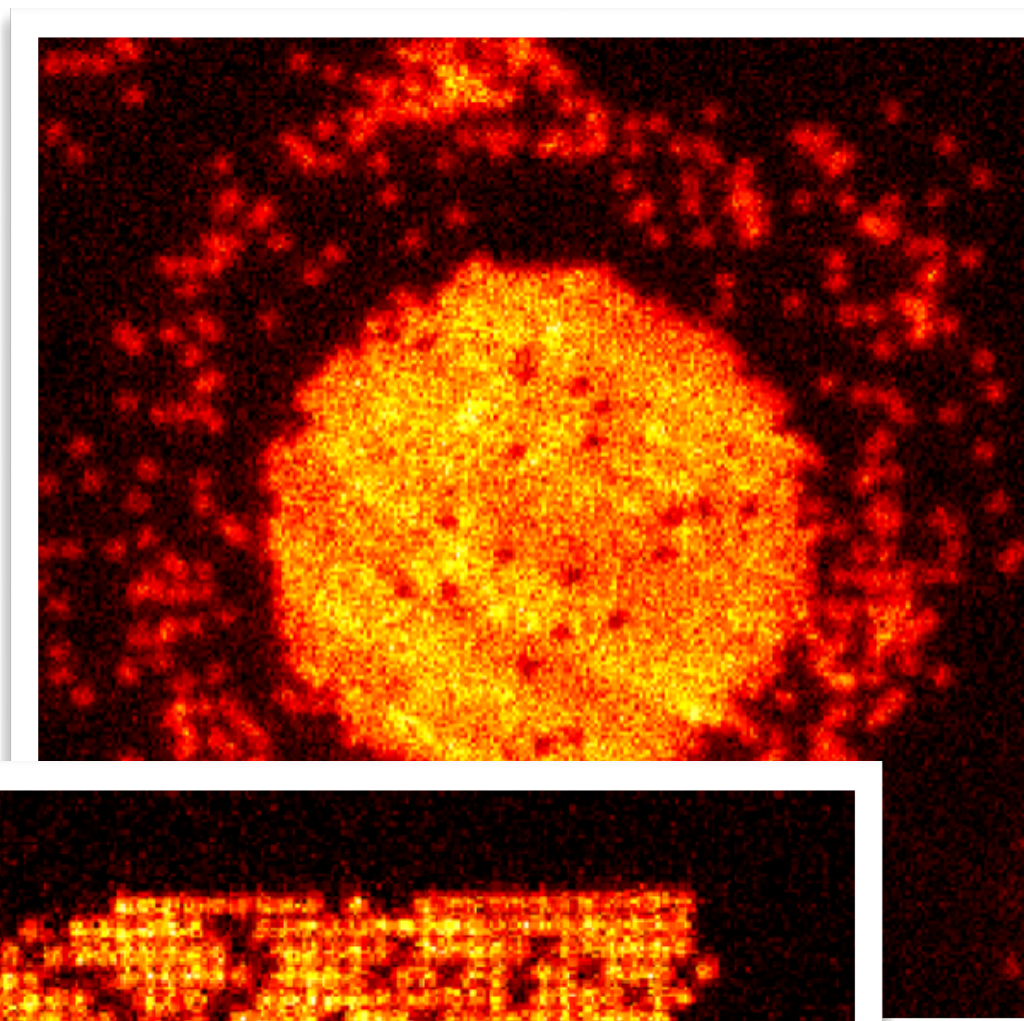


## Quantum Ladders with flexible edge geometries (SPT Spin-1 Haldane Phase)

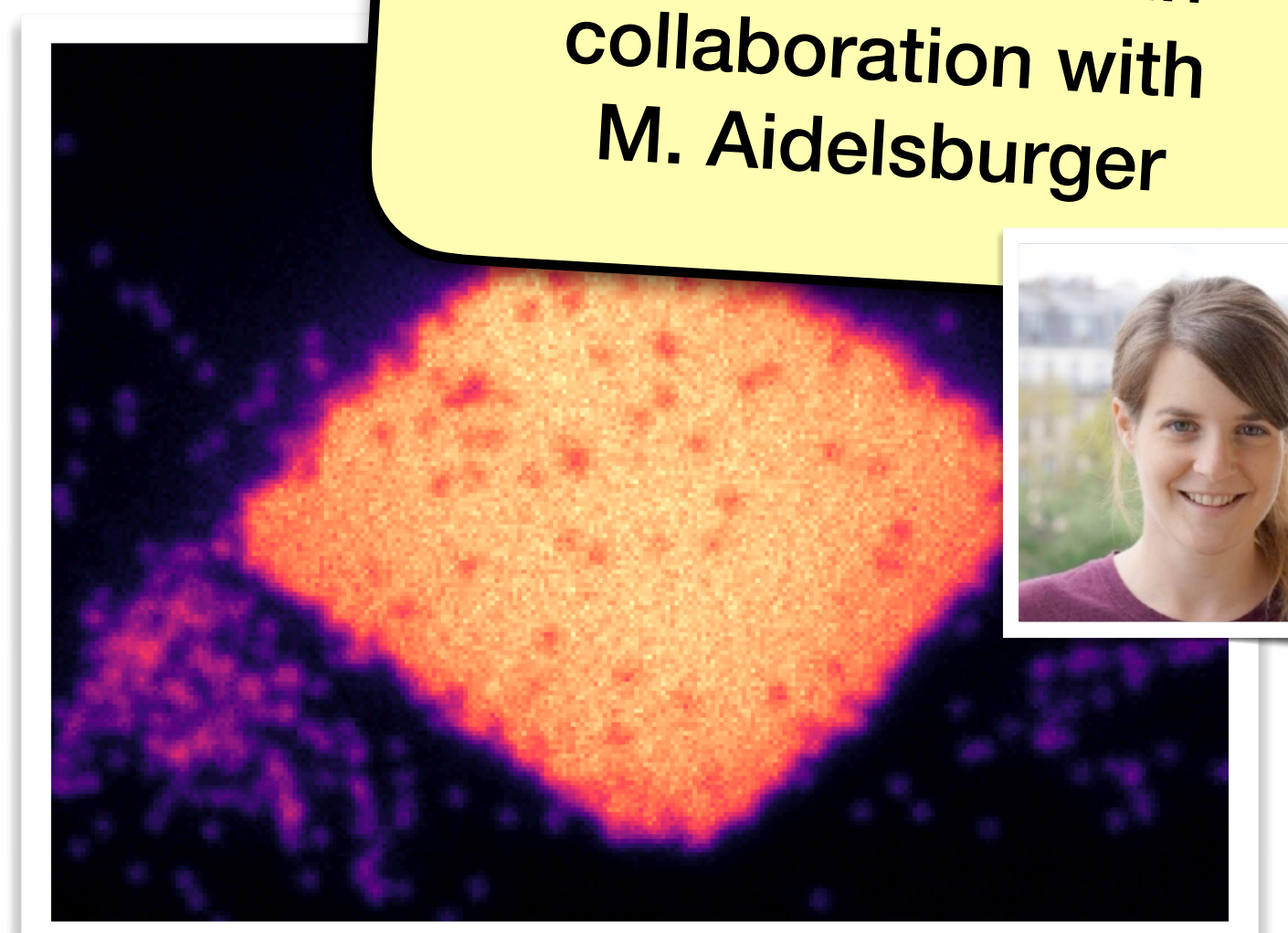


**Fully tuneable coupling strengths +dimensionality +flux +frustration**

## Large Homogeneous 2D Systems (2000-5000 atoms, filling 95-98%)



Rb Quantum Gas Microscope



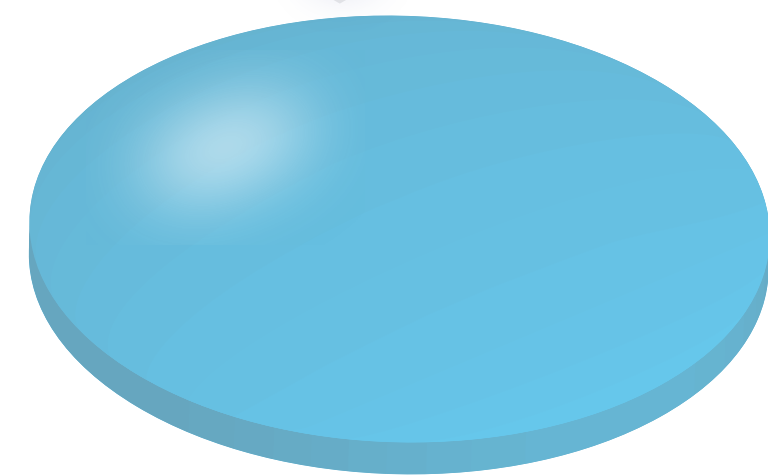
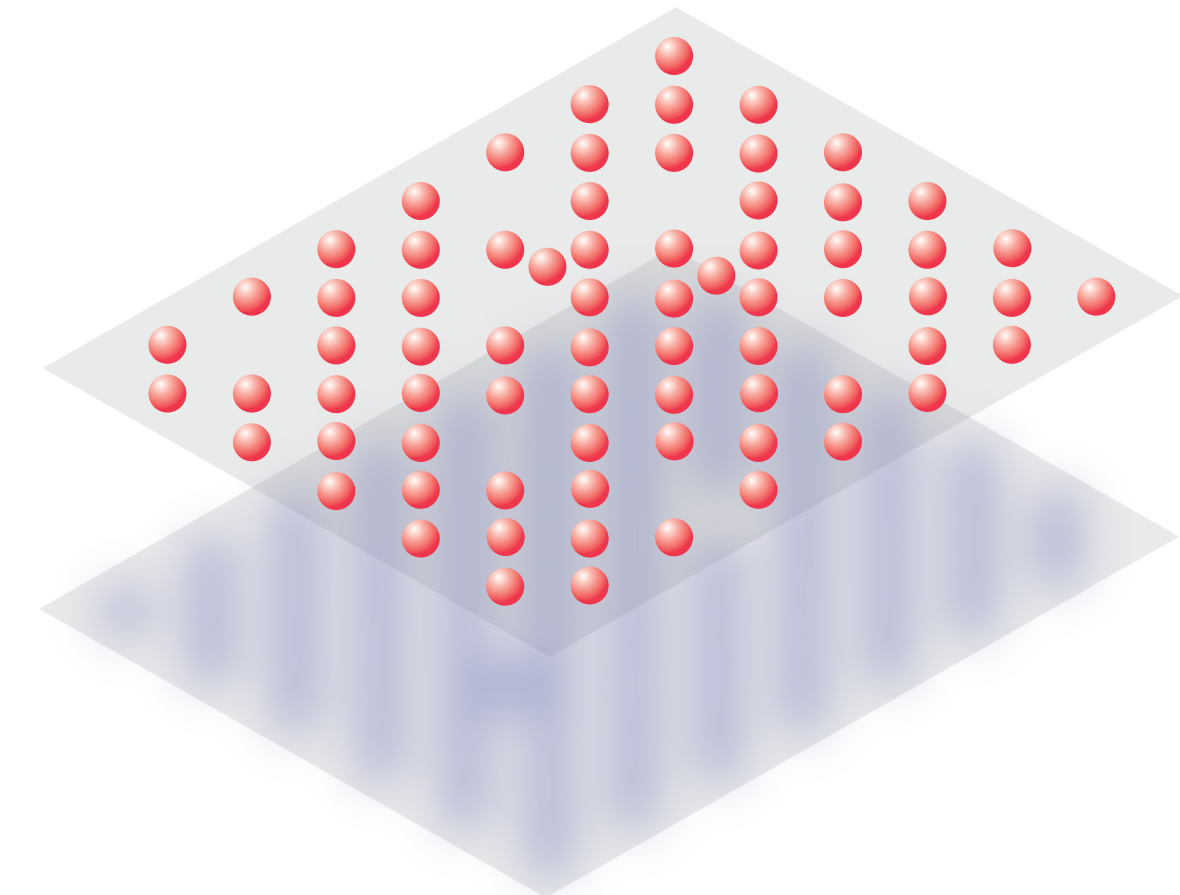
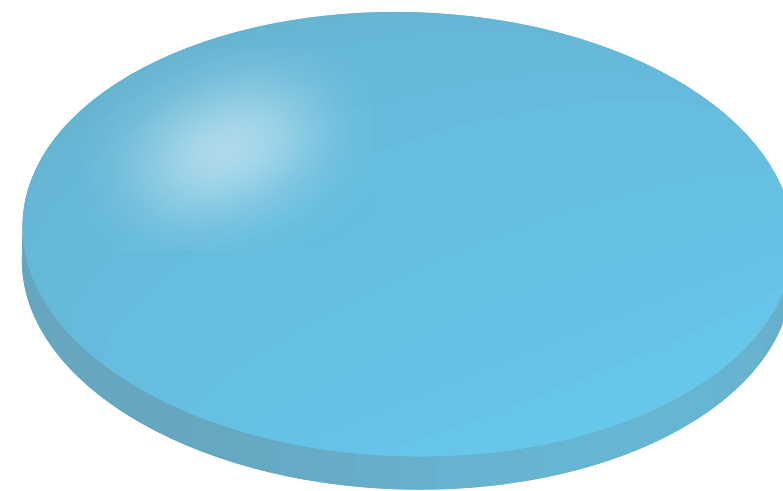
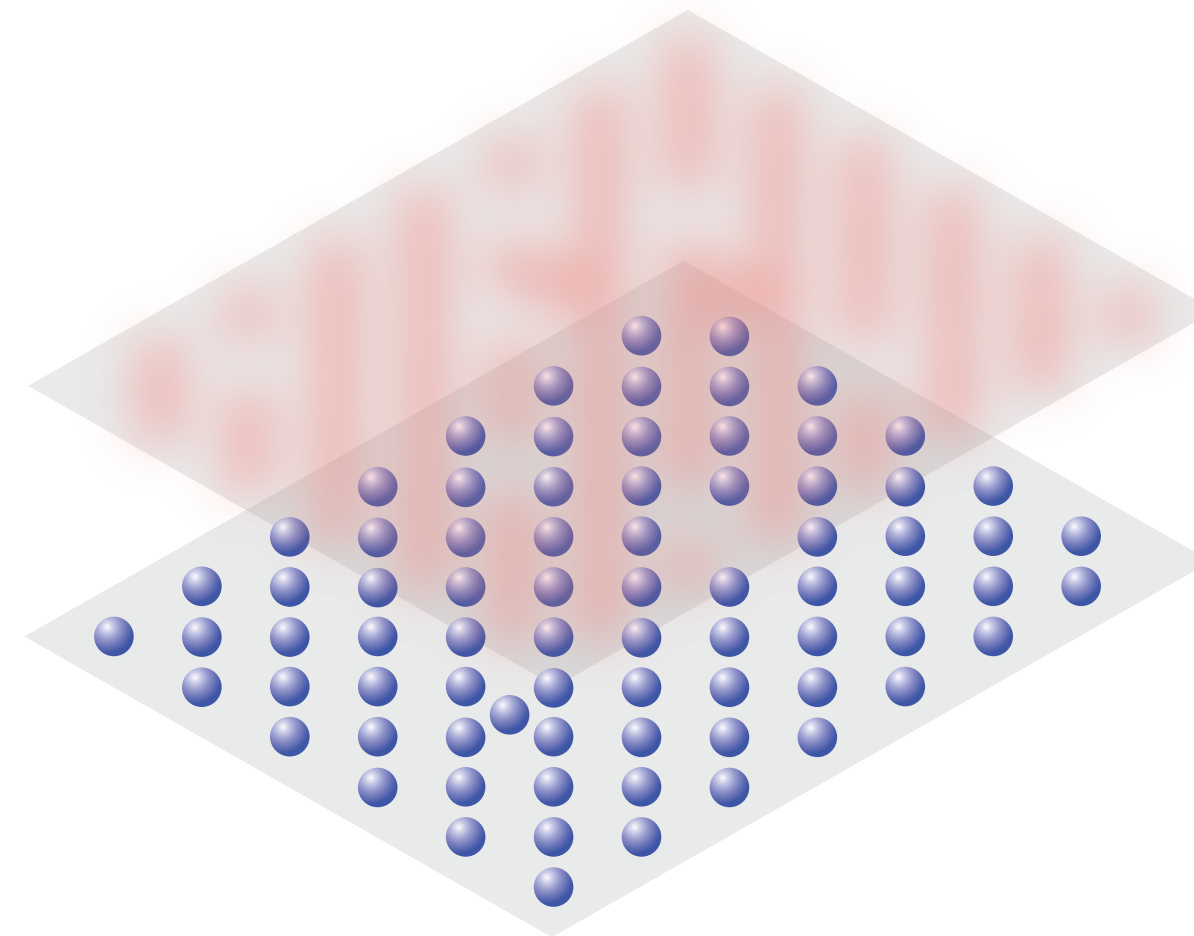
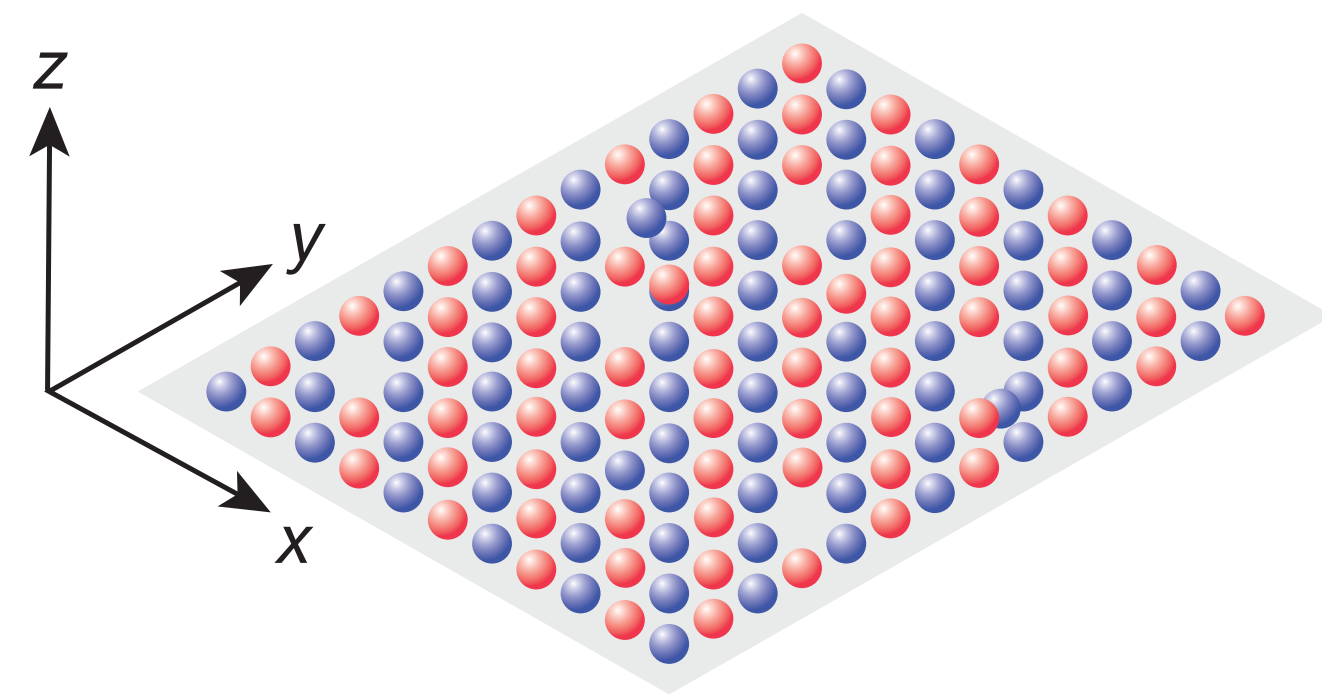
Cs Quantum Gas Microscope

Cs experiment in collaboration with M. Aidelsburger



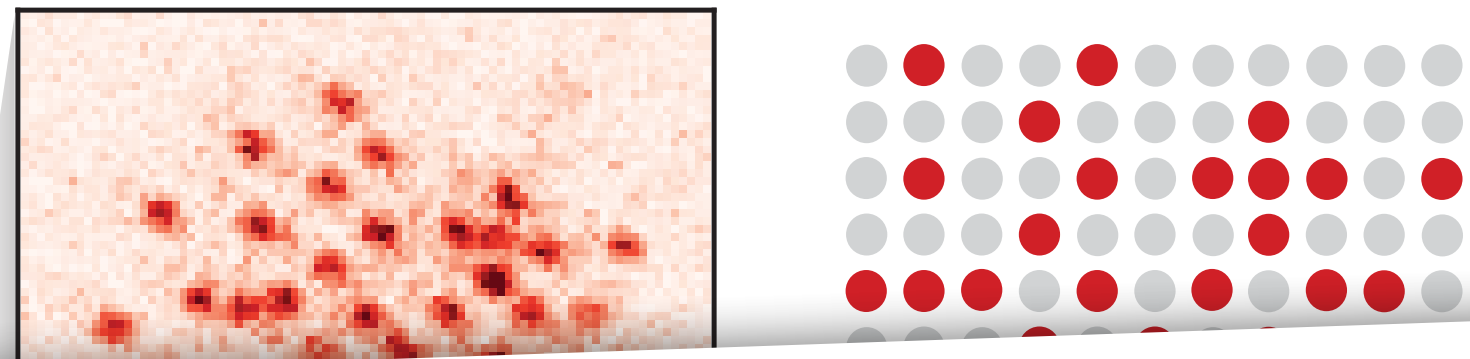
see also: C. Chiu *et al.* Phys. Rev. Lett. **120**, 243201 (2018)  
Idea: J.-S. Bernier *et al.* Phys. Rev. A **79**, 061601 (2009)  
T.-L. Ho & Q. Zhou arXiv:0911.5506











$$|\Psi\rangle = |\text{Snapshot 1}\rangle + |\text{Snapshot 2}\rangle + |\text{Snapshot 3}\rangle + \dots$$

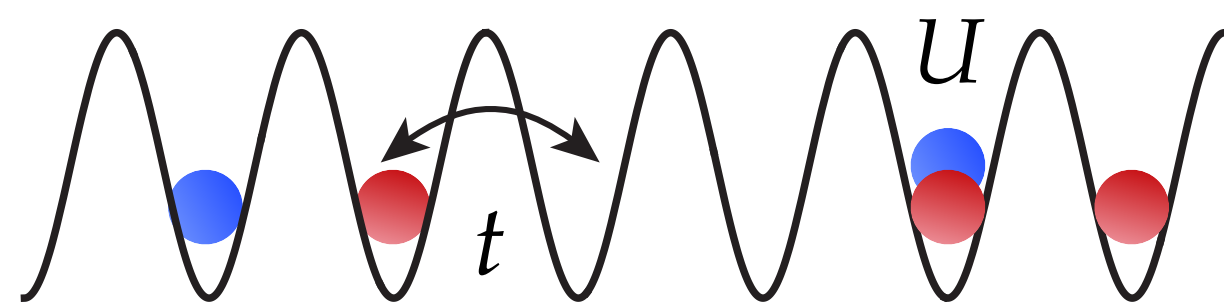
The equation shows a quantum state  $|\Psi\rangle$  as a superposition of several snapshots. Each snapshot is a 5x5 grid of particles. In the first snapshot, particles are colored red and green. In the second and third snapshots, some particles are missing, indicated by dashed circles. The sequence ends with three black dots, indicating further terms in the superposition.

**Snapshots where each "electron" is visible**



⊙ : doublon    ● : spin up

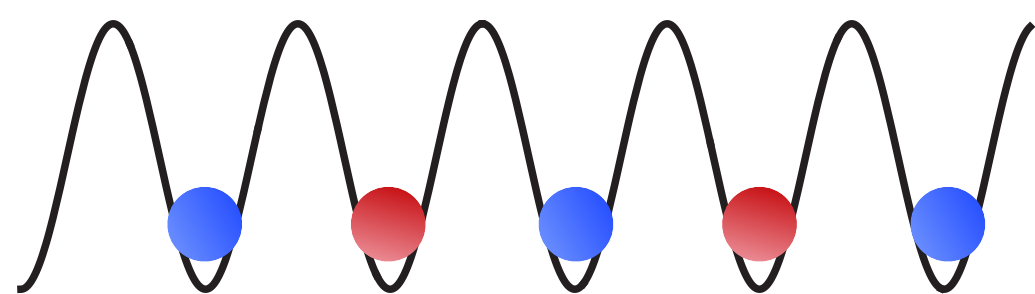
## Fermi-Hubbard Model



$$\hat{H} = -t \sum_{\langle i,j \rangle, \sigma} \hat{c}_{i,\sigma}^\dagger \hat{c}_{j,\sigma} + U \sum_i \hat{n}_{i,\uparrow} \hat{n}_{i,\downarrow}$$

## AFM Heisenberg Model

Half filling & strong interaction



$$H = J \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j \quad J = \frac{4t^2}{U}$$

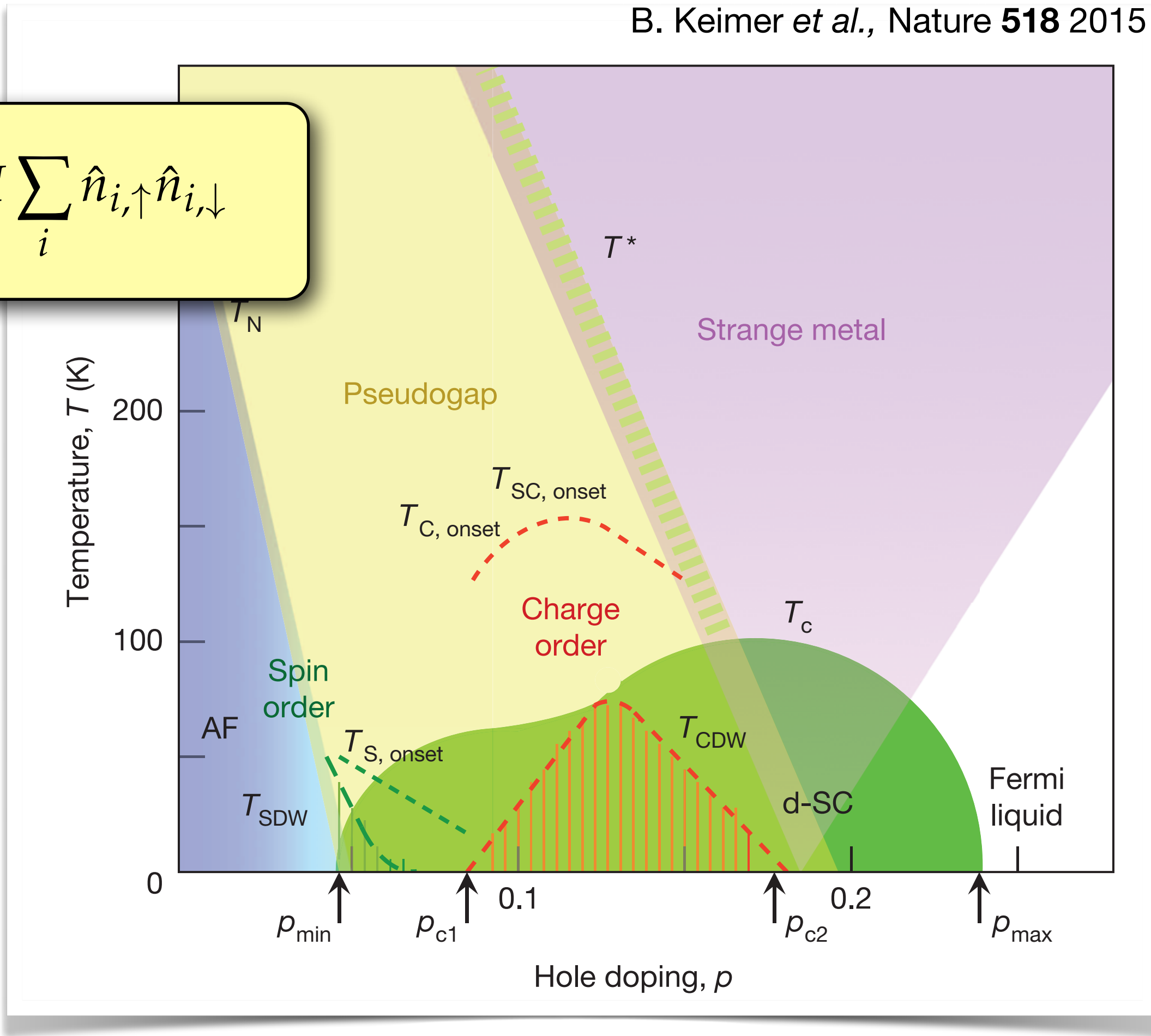
Away from half filling: ***t*-*J* model**  
competition between

**hole delocalization**



**magnetic order**

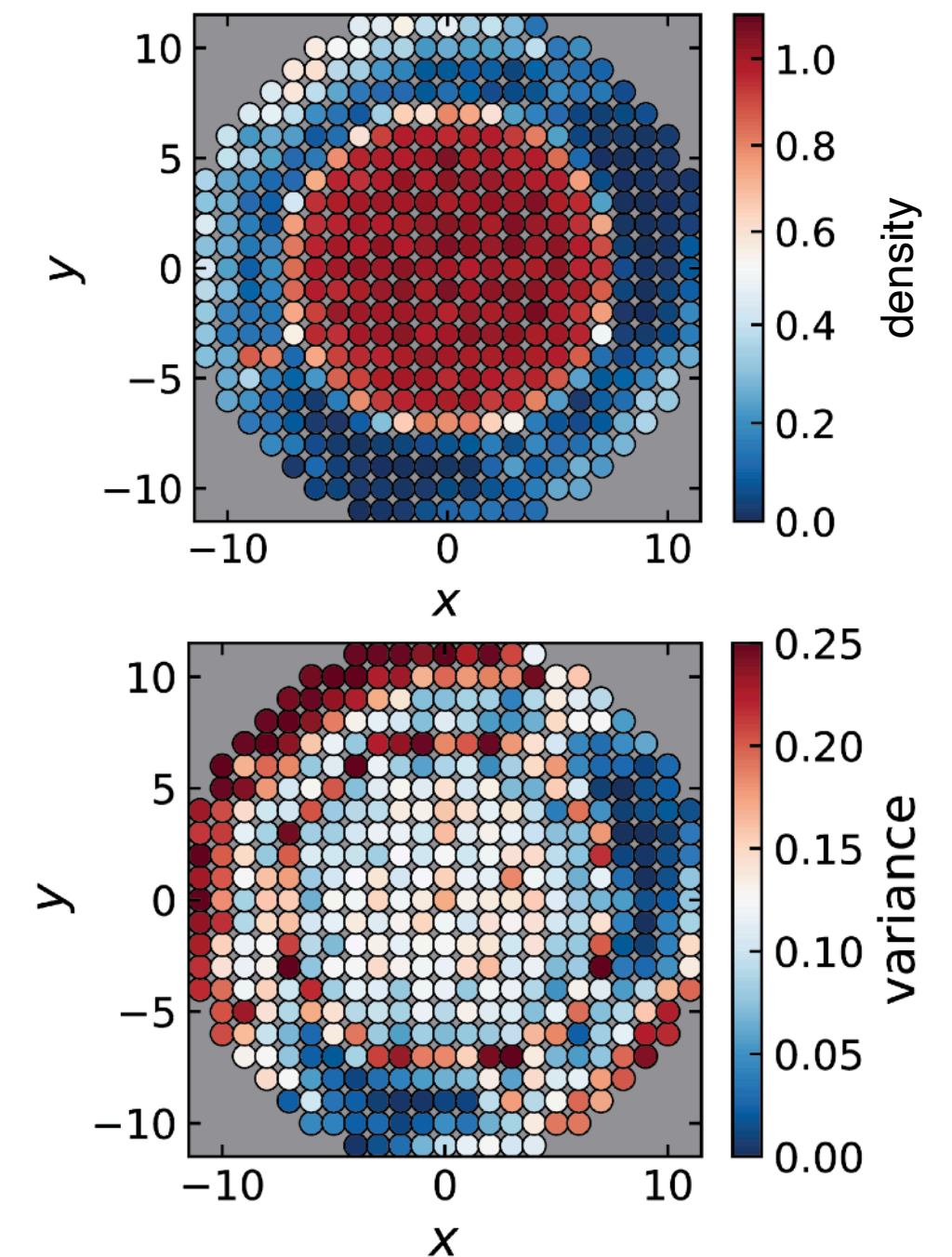
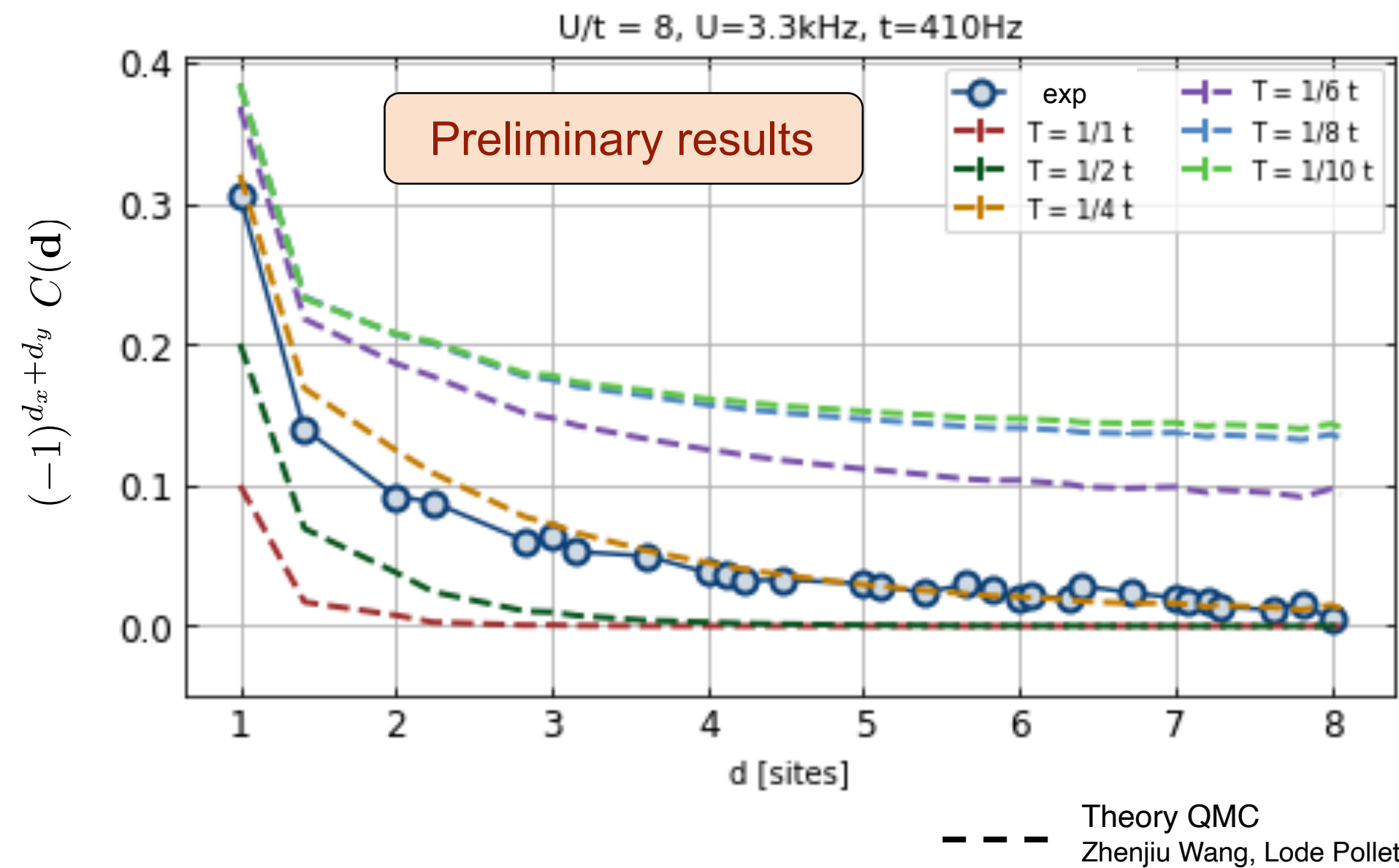
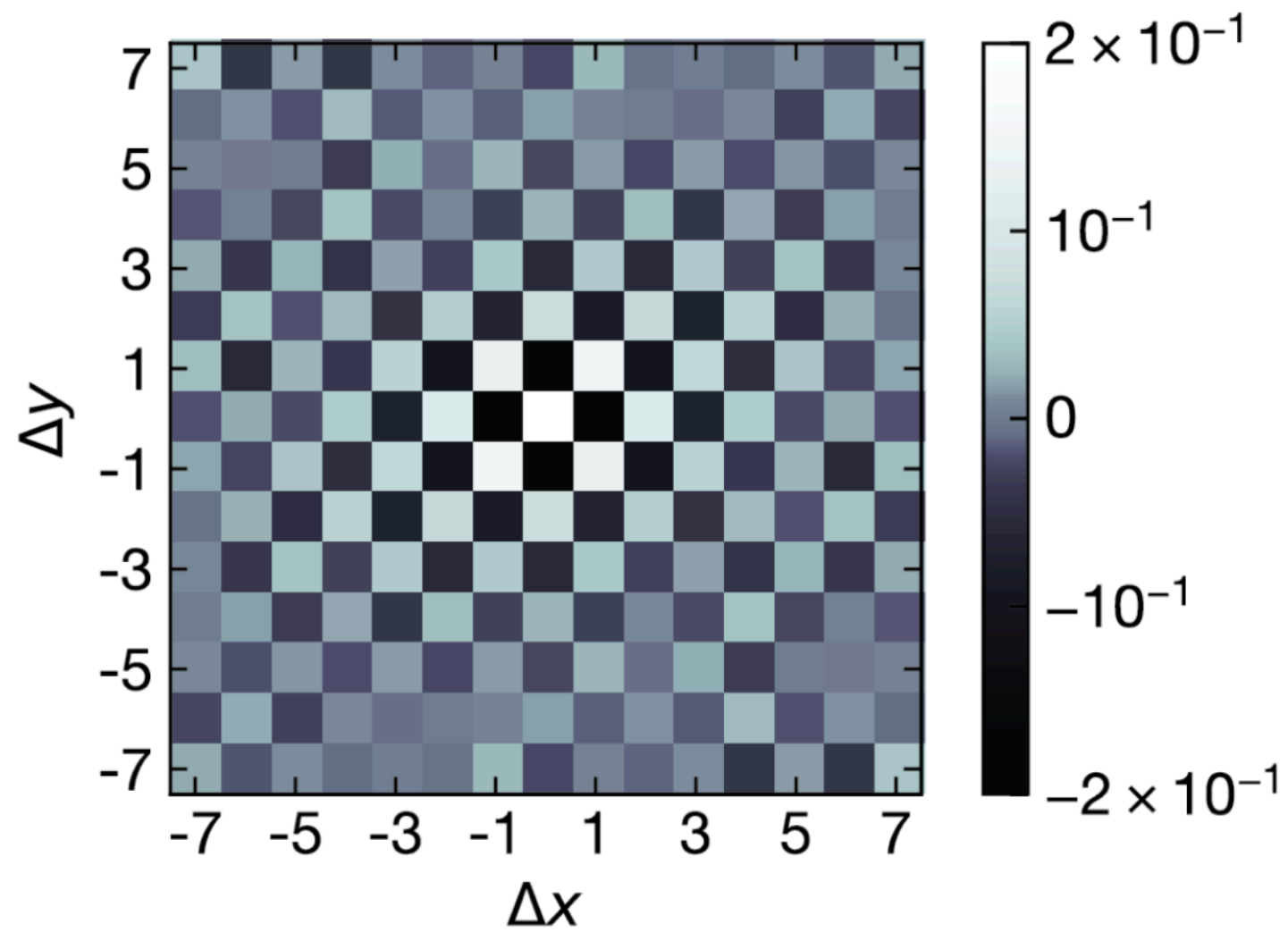
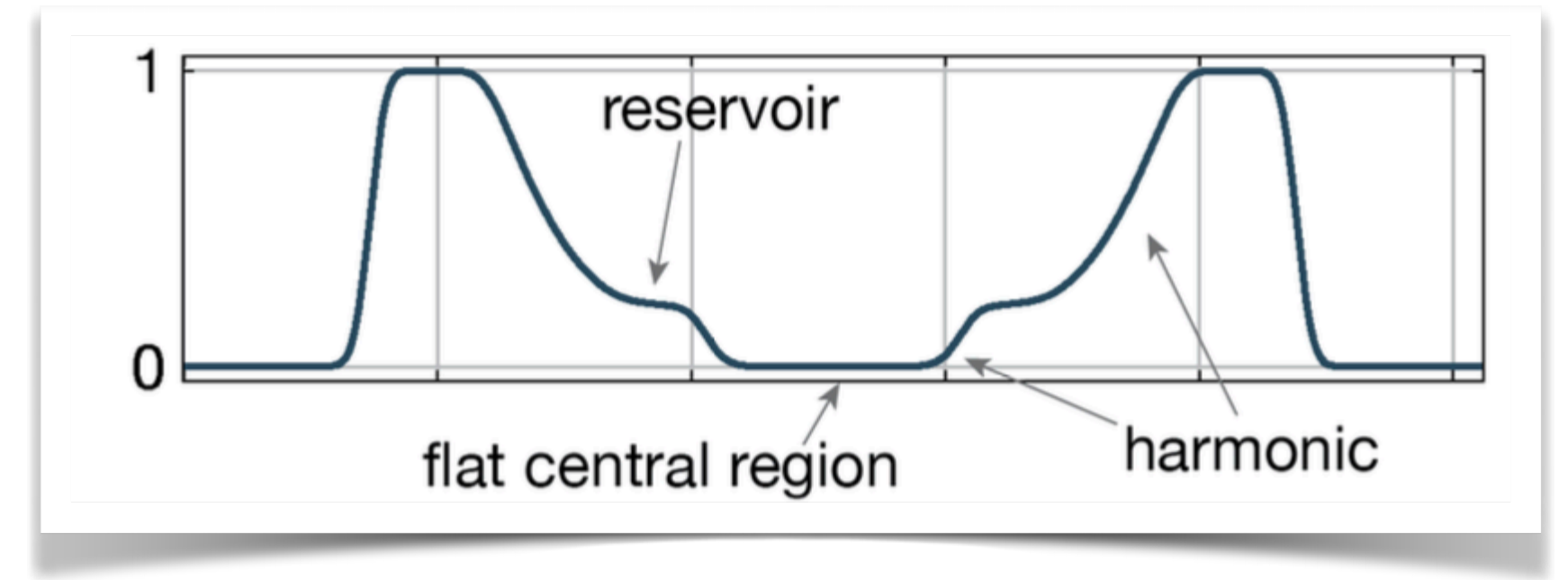
B. Keimer et al., Nature **518** 2015





# 2D Spin Correlations

$$\frac{\langle \hat{S}_i^z \hat{S}_j^z \rangle - \langle \hat{S}_i^z \rangle \langle \hat{S}_j^z \rangle}{\sigma(\hat{S}_j^z) \sigma(\hat{S}_i^z)}$$

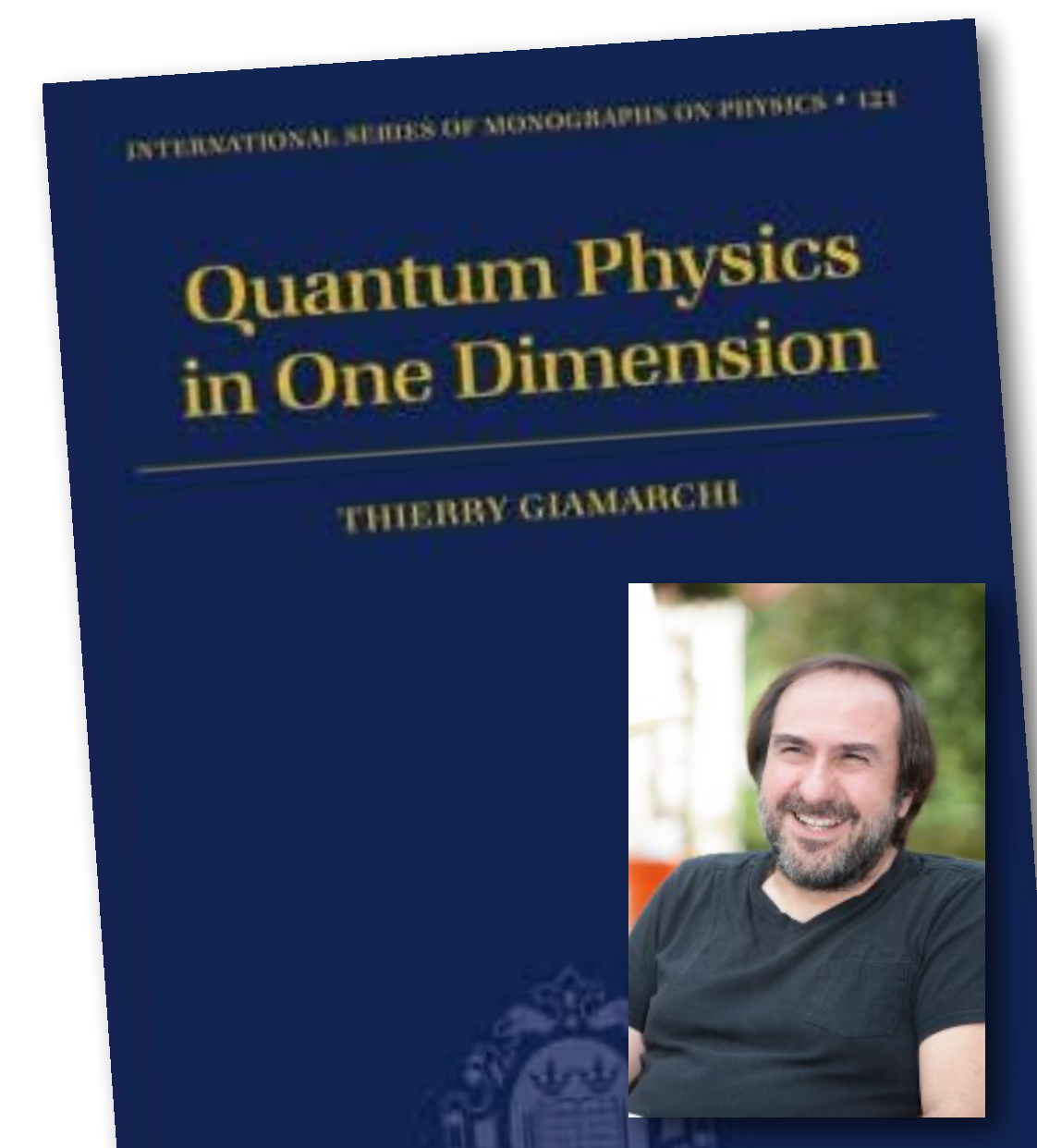
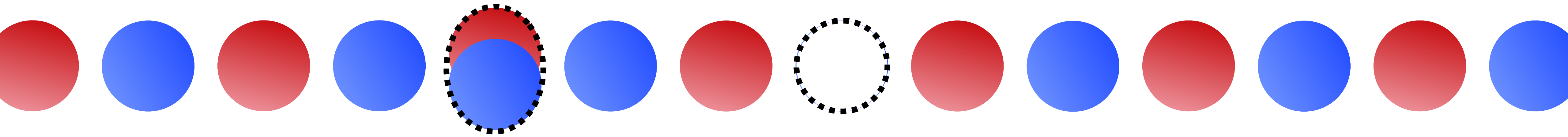


$$T/t \sim 0.2 - 0.25$$

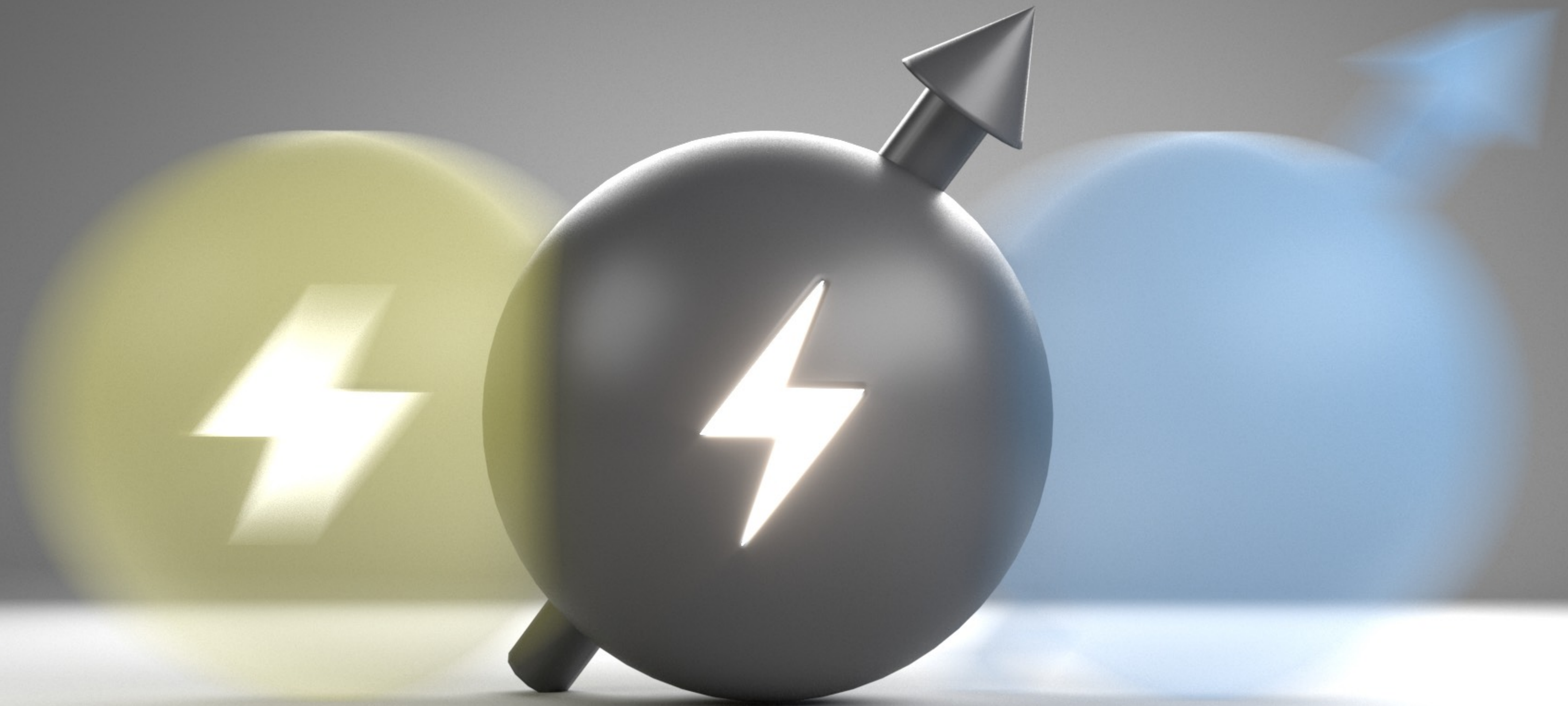
See also:

**Harvard:** Parsons et al., Science (2016), Mazurenko et al. Nature (2017),  
**MIT:** Cheuk et al., Science (2016), **Princeton:** Brown et al., Science (2017),  
**Bonn:** Drewes et al., PRL (2017)

# Doping in 1D Fermi Hubbard Model







J. Vijayan *et al.* Science **367**, 186 (2020)

# The Electron

Charge  $-e$

Spin  $1/2$

**Fractionalization**

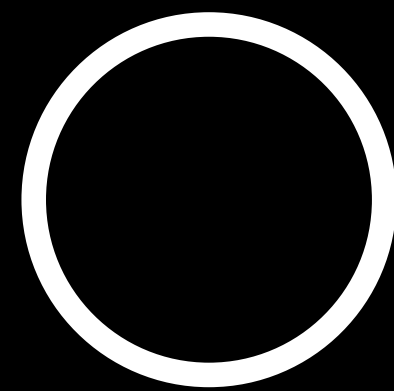
Deconfinement of Quasi-particles  
that make up the elementary particle

Charge  $-e$

Quasi-Particle

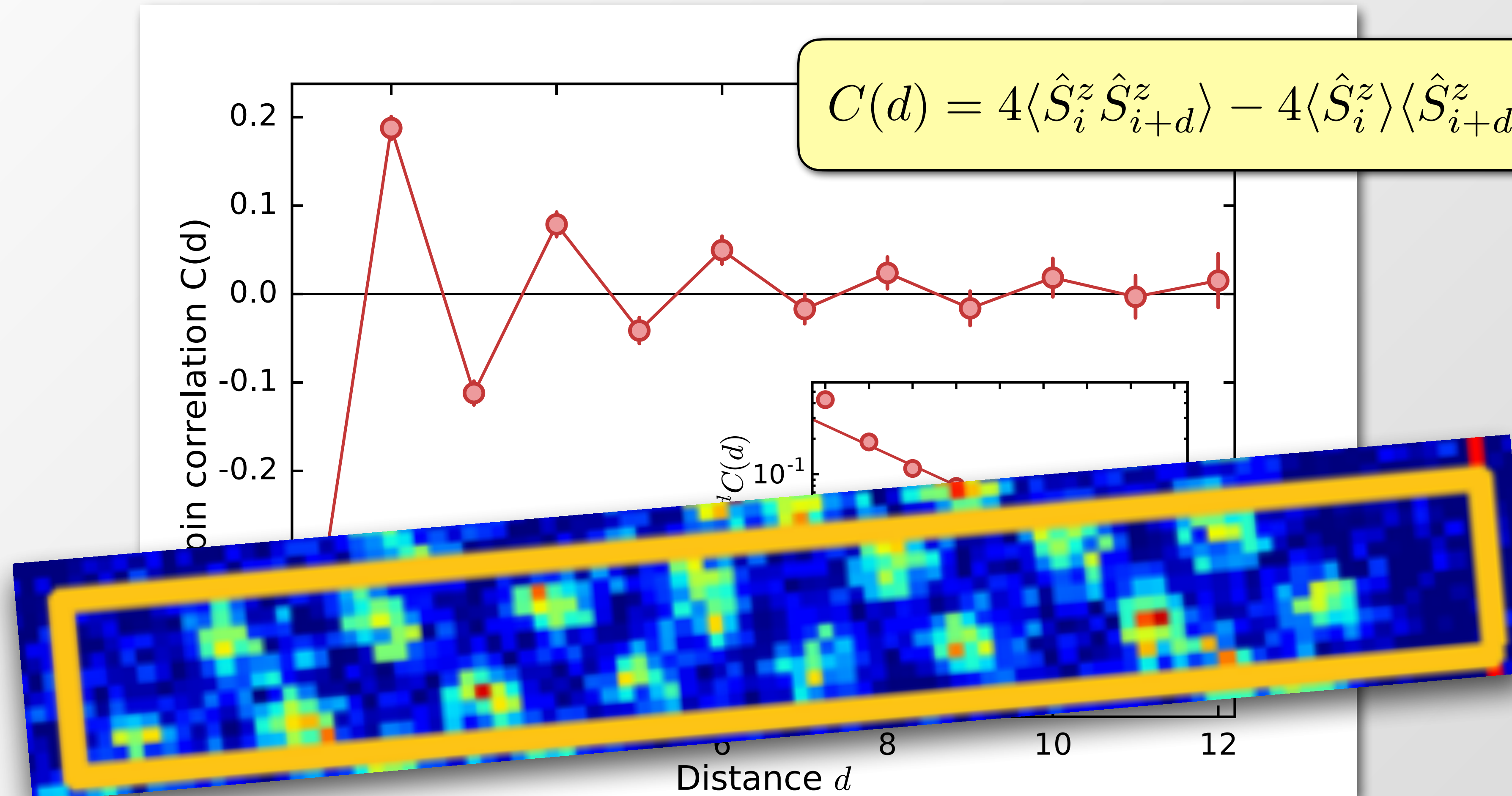
Spin  $1/2$

Quasi-Particle





Postselection to  $M_z = 0$  !



$\xi(0, T)$  Largest possible decays length !

# The Electron

Charge  $-e$

Spin  $1/2$

**Fractionalization**

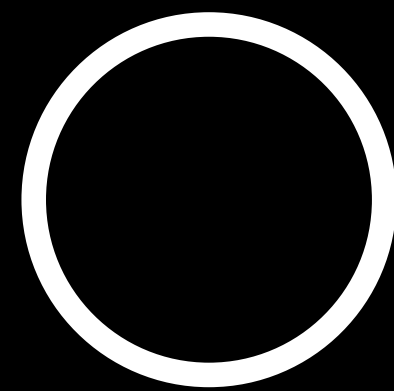
Deconfinement of Quasi-particles  
that make up the elementary particle

Charge  $-e$

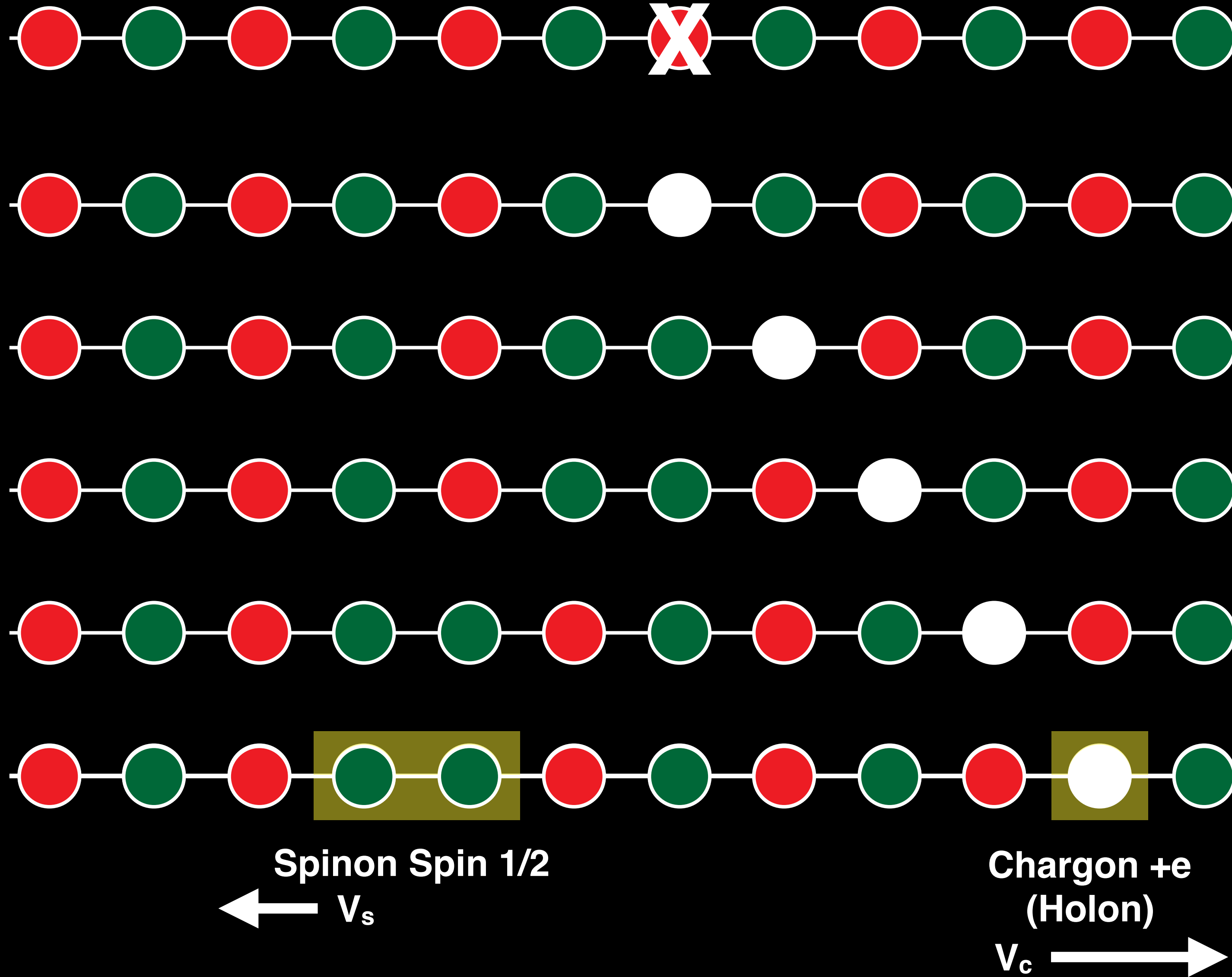
Quasi-Particle

Spin  $1/2$

Quasi-Particle

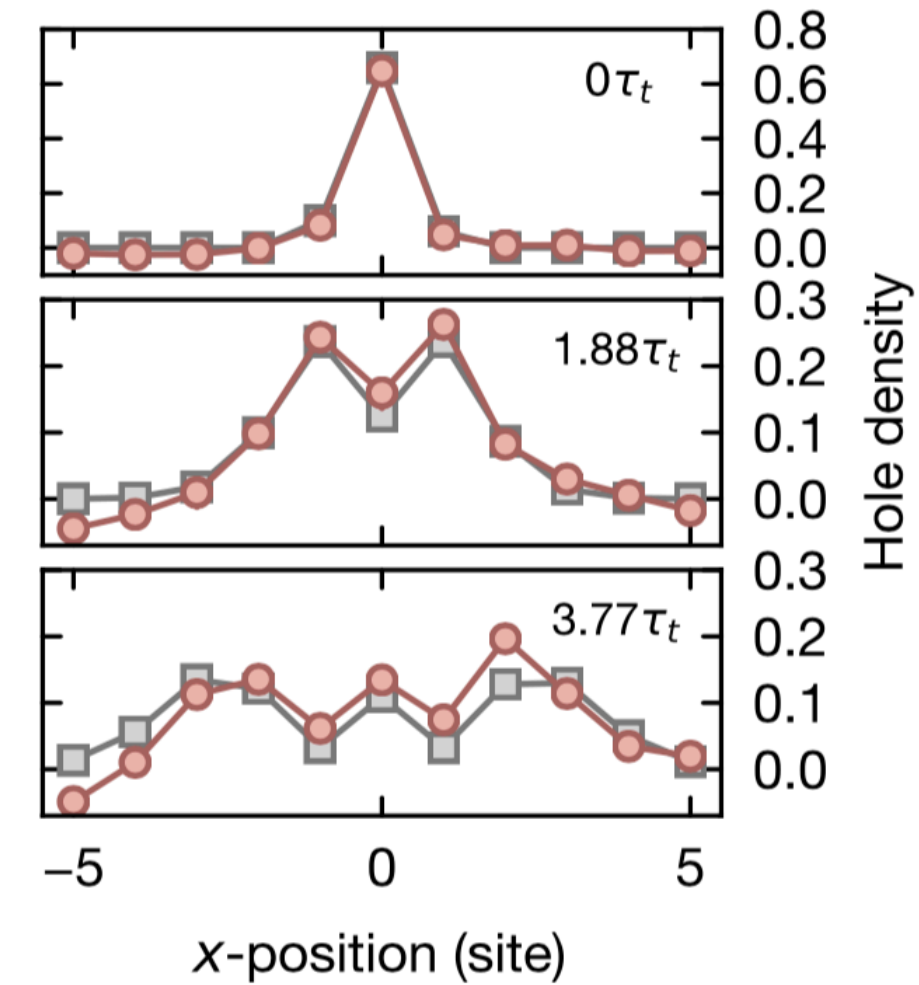
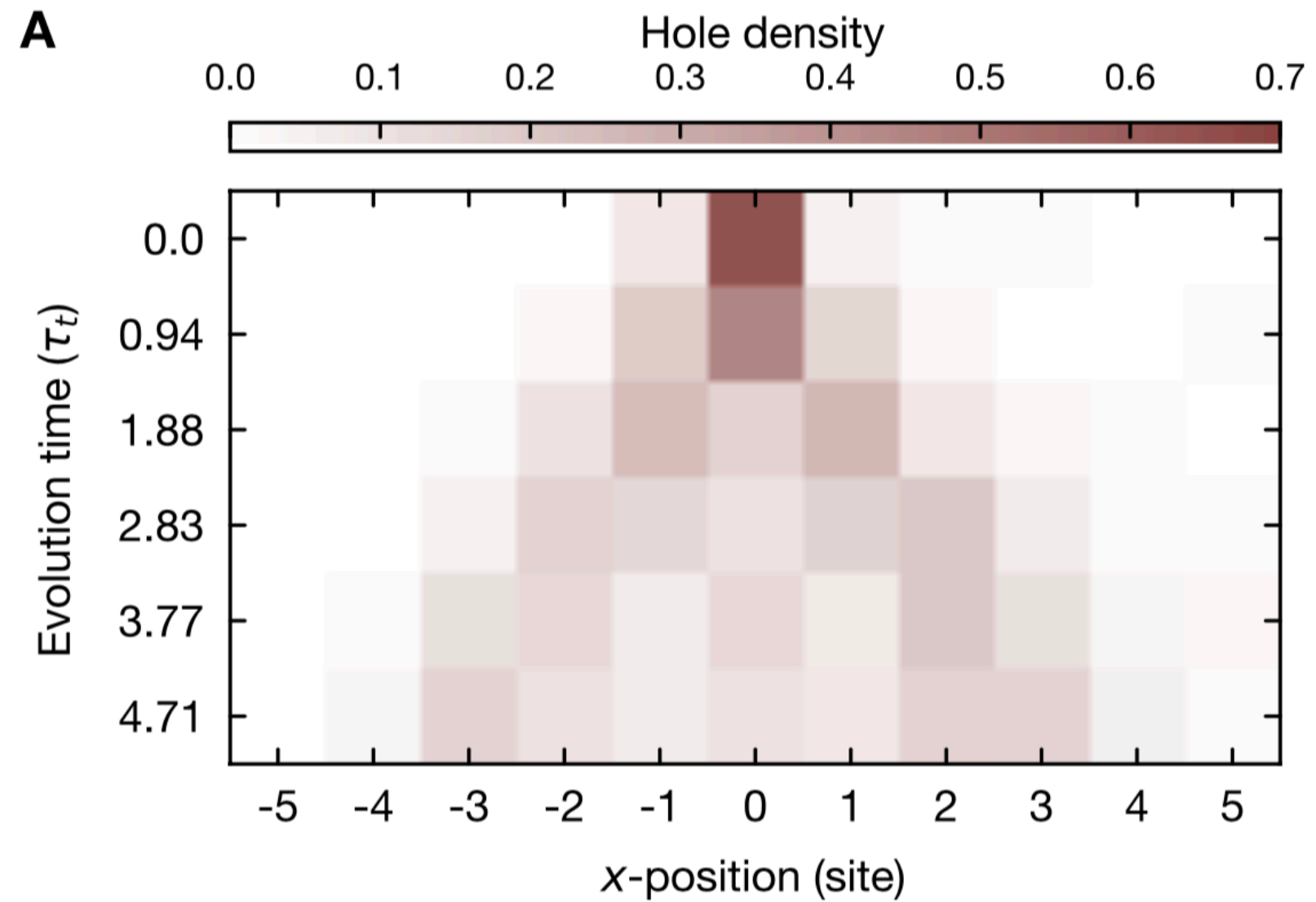


# Fractionalization



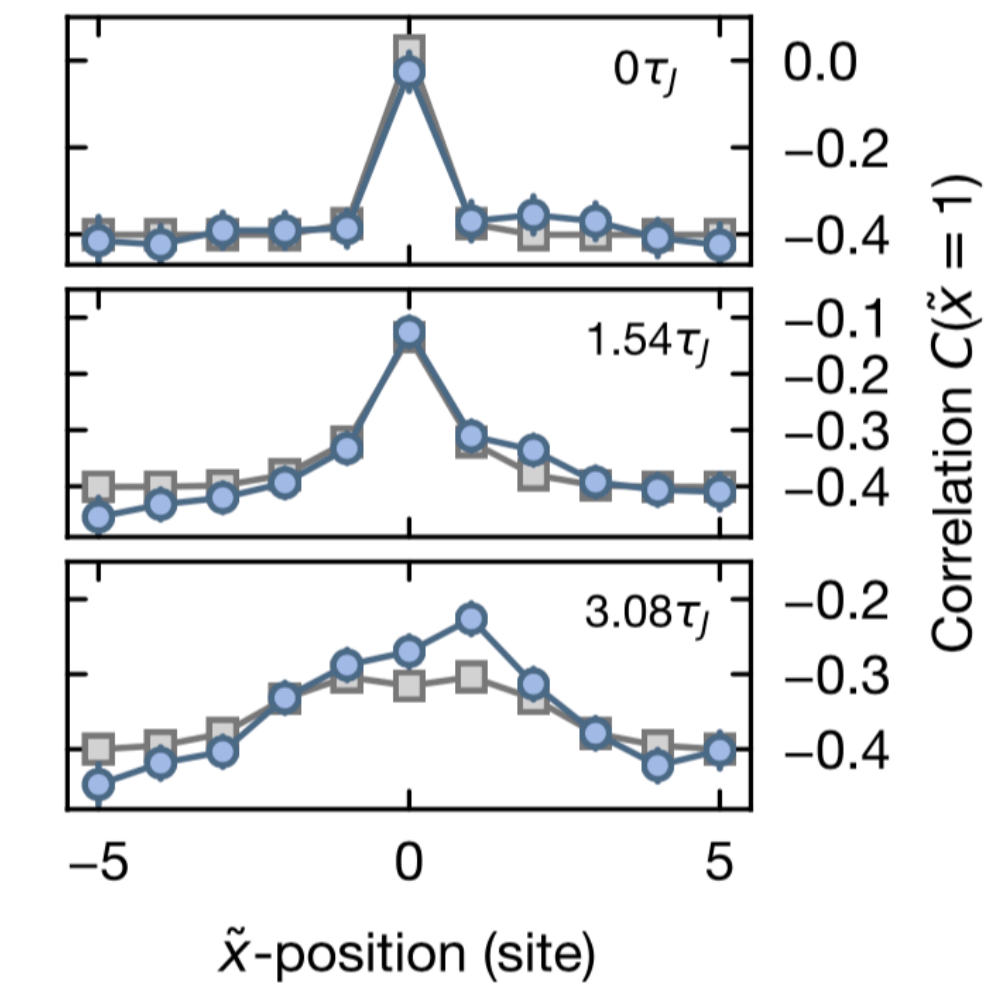
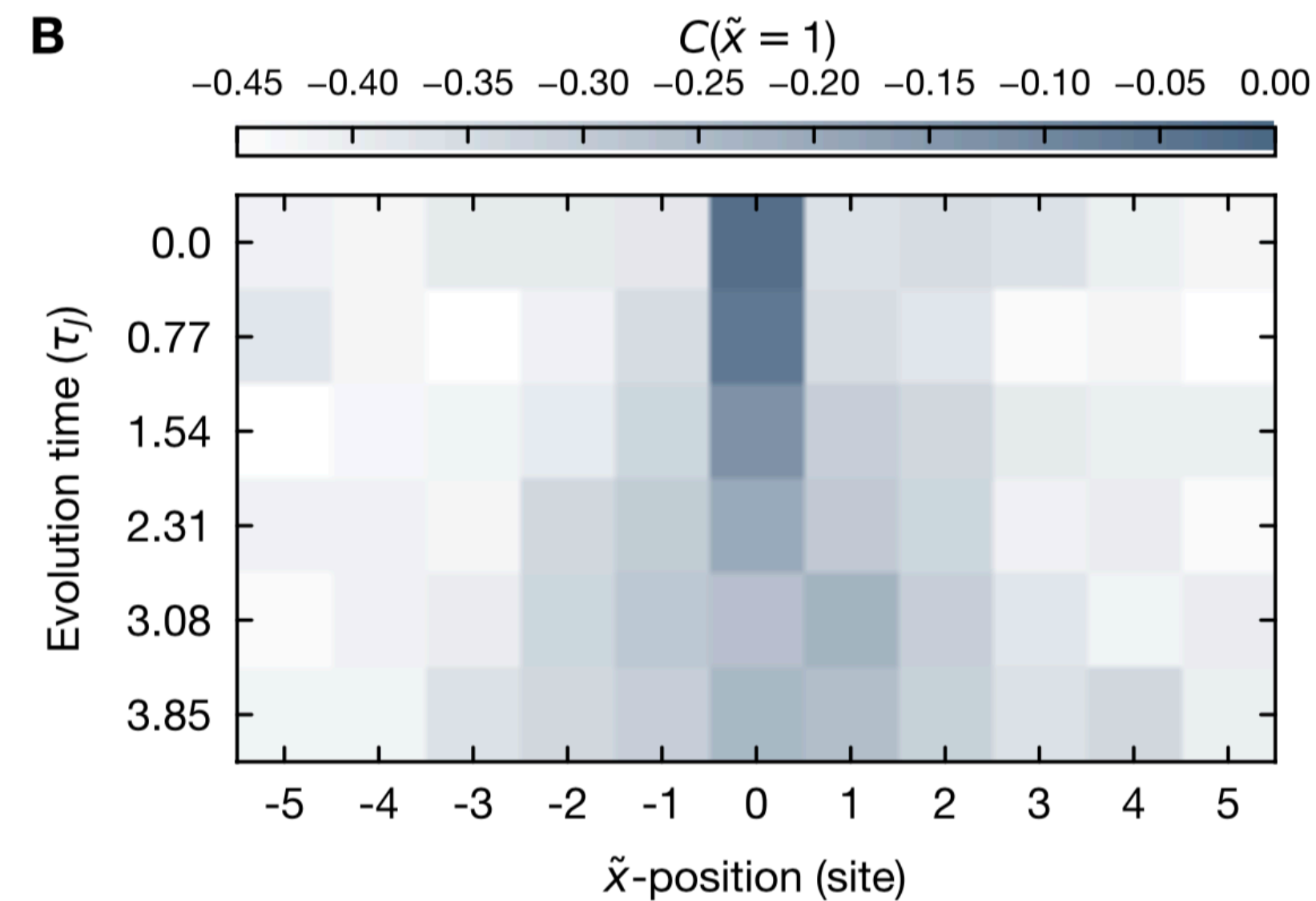
1.





## Hole Dynamics

$$\langle \hat{h}_i \rangle$$



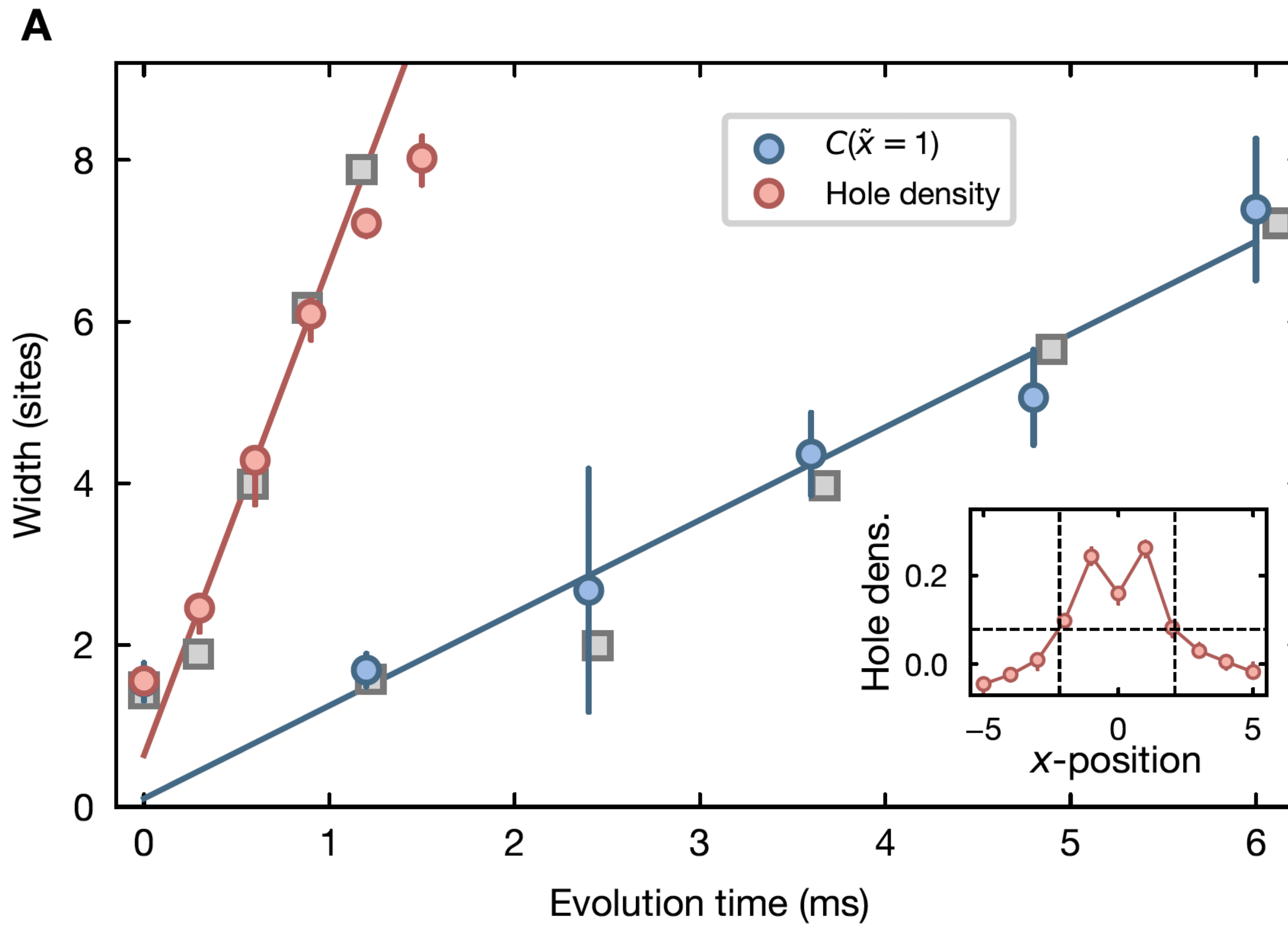
## Spin Dynamics

$$C(1) = \langle \hat{S}_i^z \hat{S}_{i+1}^z \rangle$$

(squeezed space)



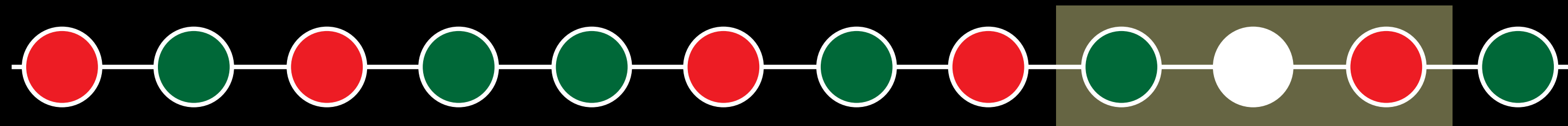
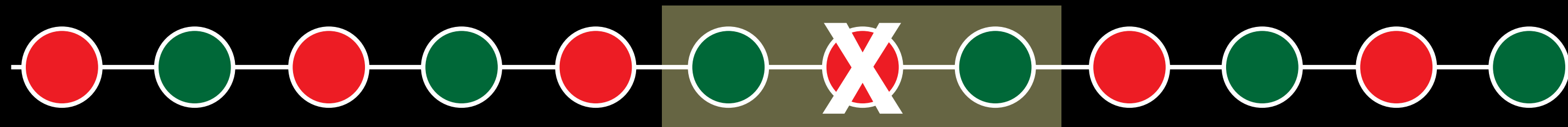




# Fractionalization - Hole Shedding Spinon

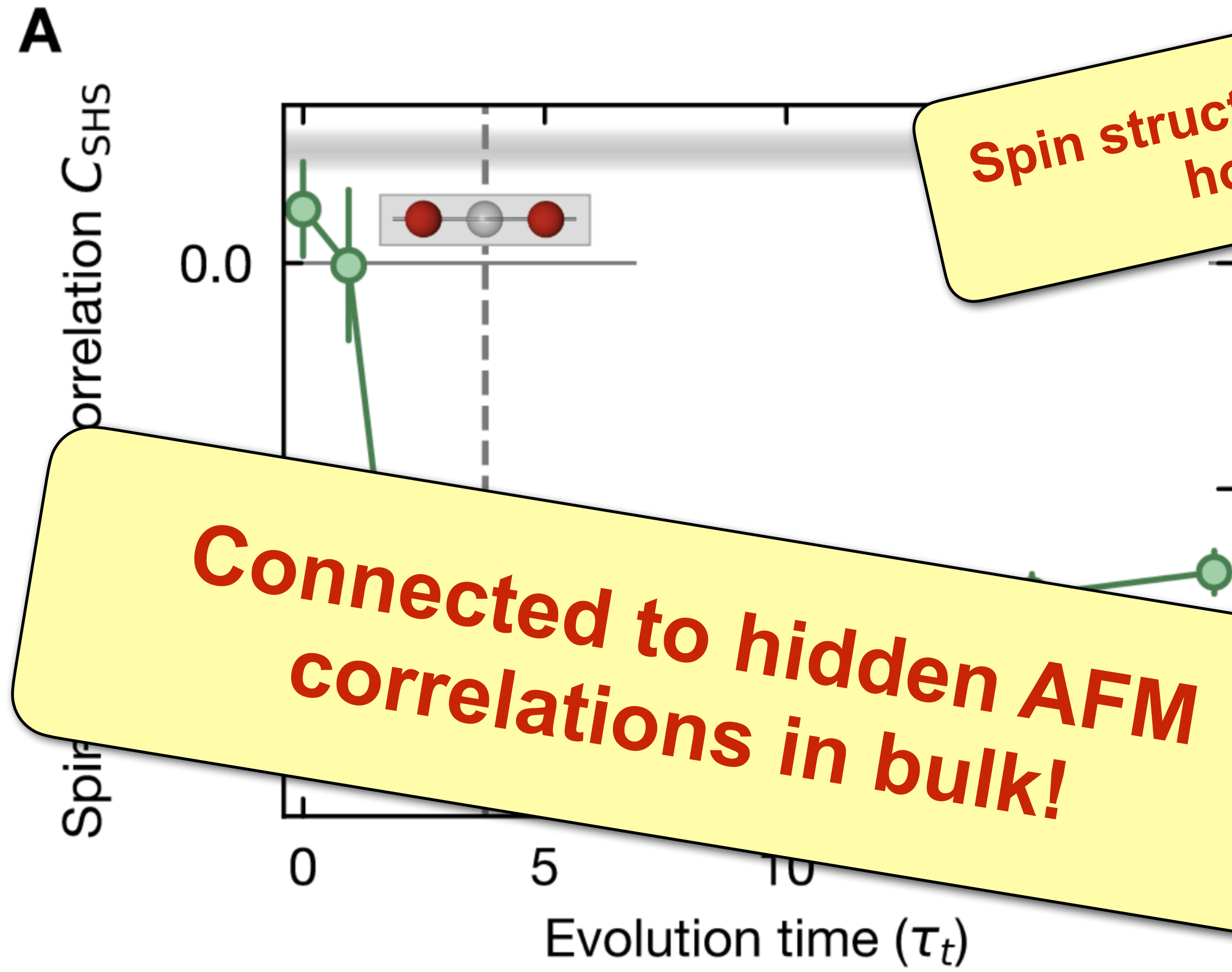
Spin attached to hole

$$\langle \hat{S}_{i-1}^z \hat{h}_i \hat{S}_{i+1}^z \rangle > 0$$



$$\langle \hat{S}_{i-1}^z \hat{h}_i \hat{S}_{i+1}^z \rangle < 0$$

Hole got rid of spin



**Spin structure independent of hole position!**

**Connected to hidden AFM correlations in bulk!**

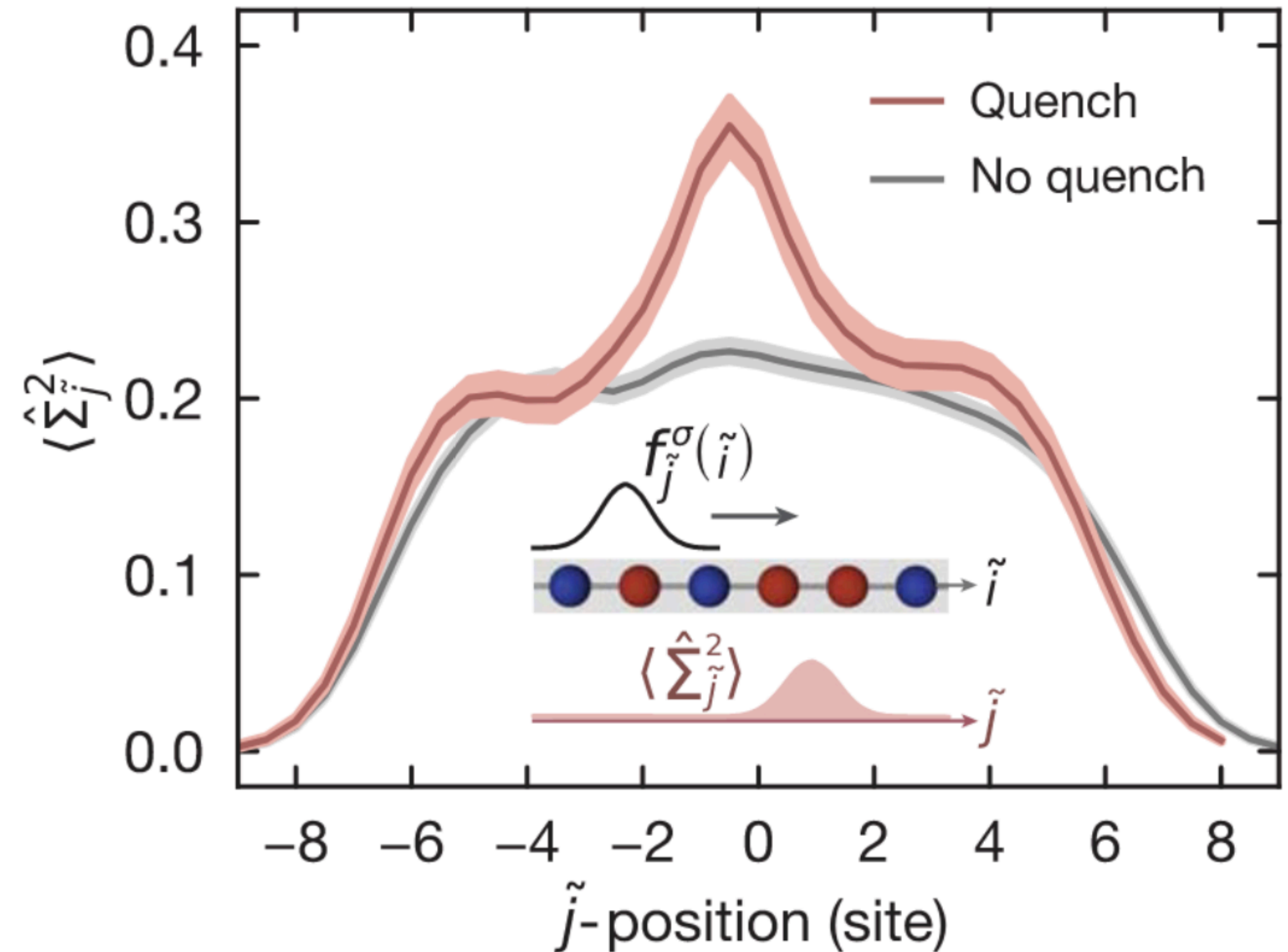
$$\langle \hat{S}_{i-1}^z \hat{h}_i \hat{S}_{i+1}^z \rangle$$

$$\hat{\Sigma}_j^2 = \left( \sum_i \hat{S}_i^z f_j^\sigma(i) \right)^2$$

$$\langle \hat{\Sigma}_j^2 \rangle - \langle \hat{\Sigma}_j^2 \rangle_{BG} = 1/4$$

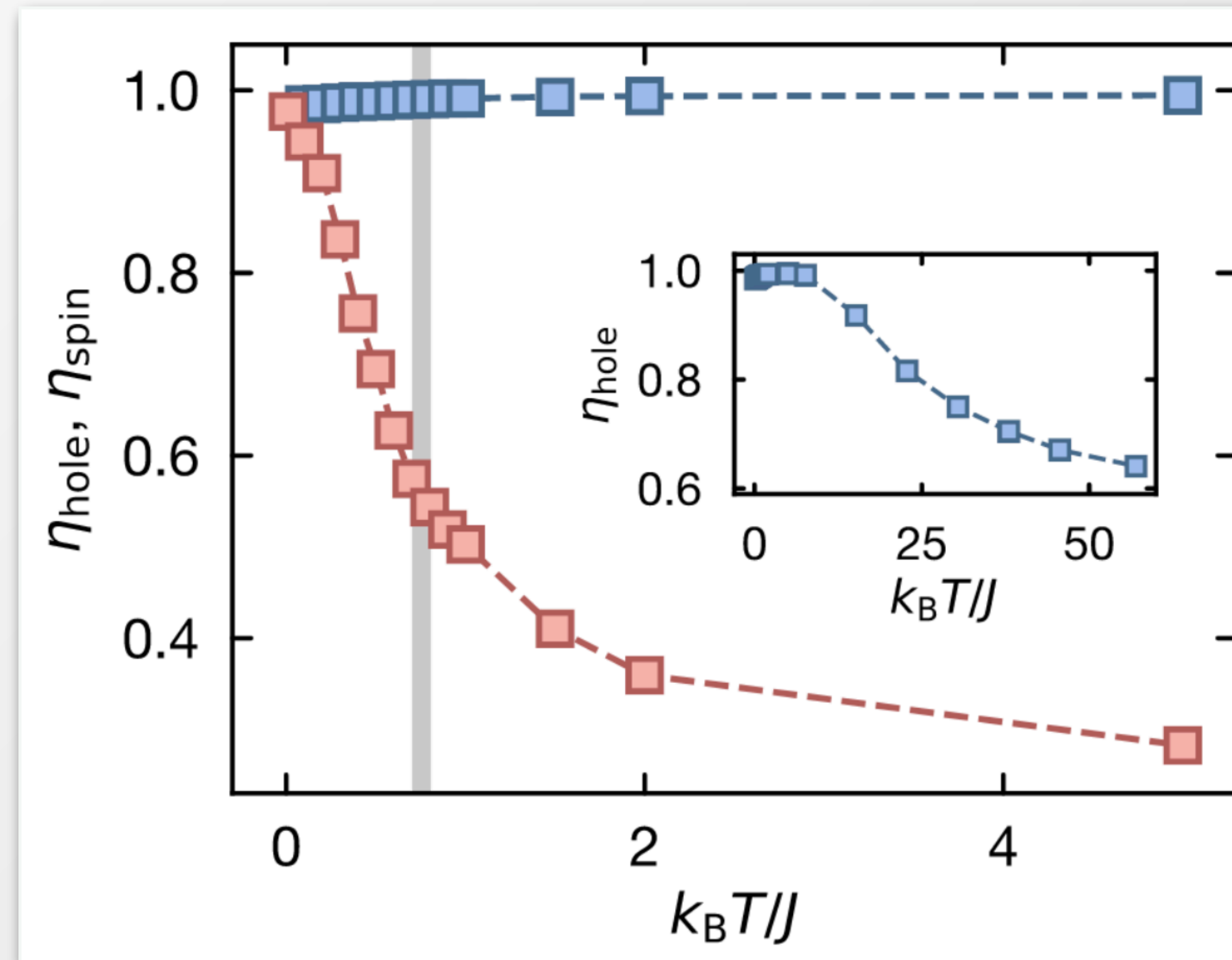
Probe Magnetization Fluctuations  
in Region  $\sigma$

J. Vijayan *et al.* *Science* **367**, 186 (2020)



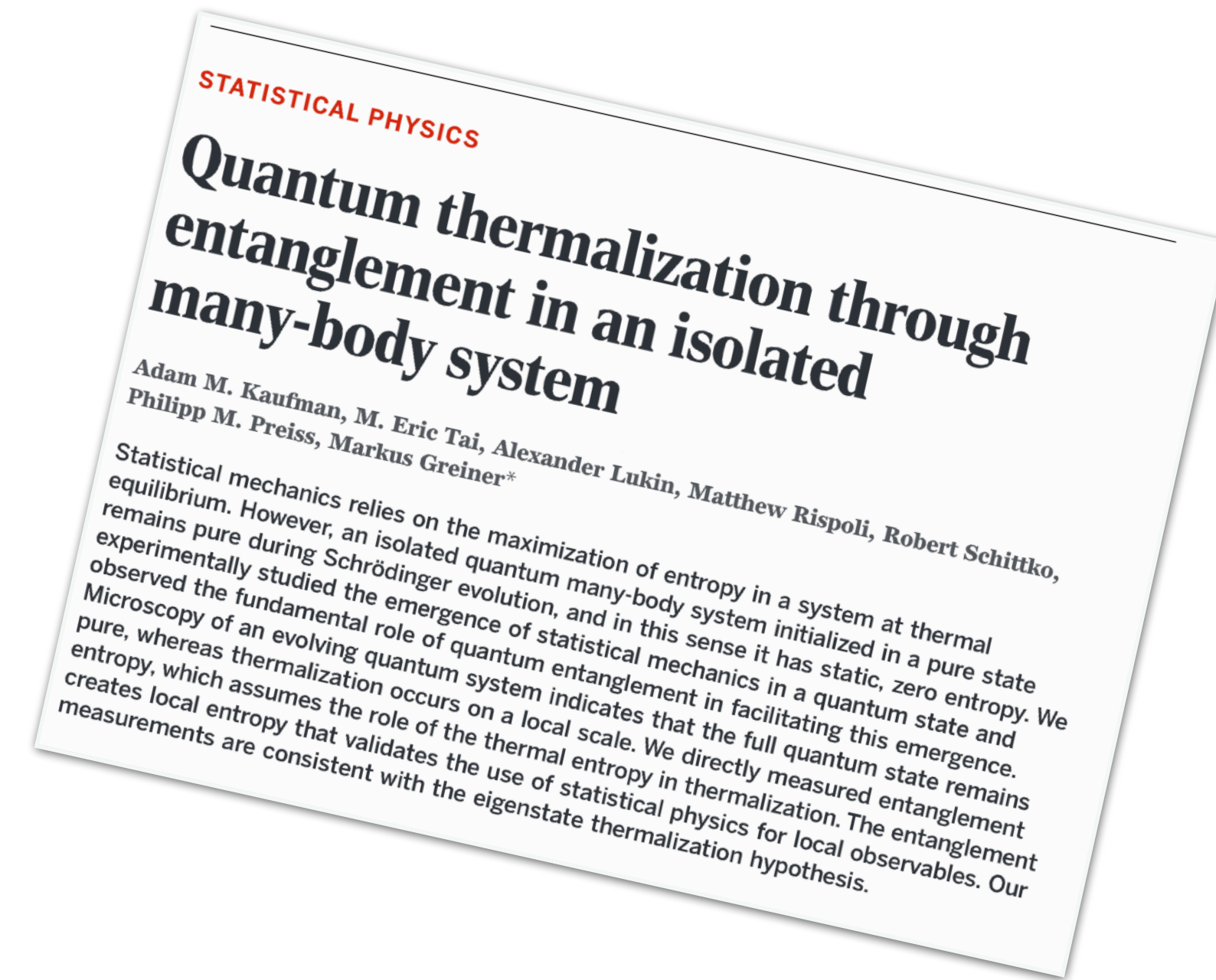
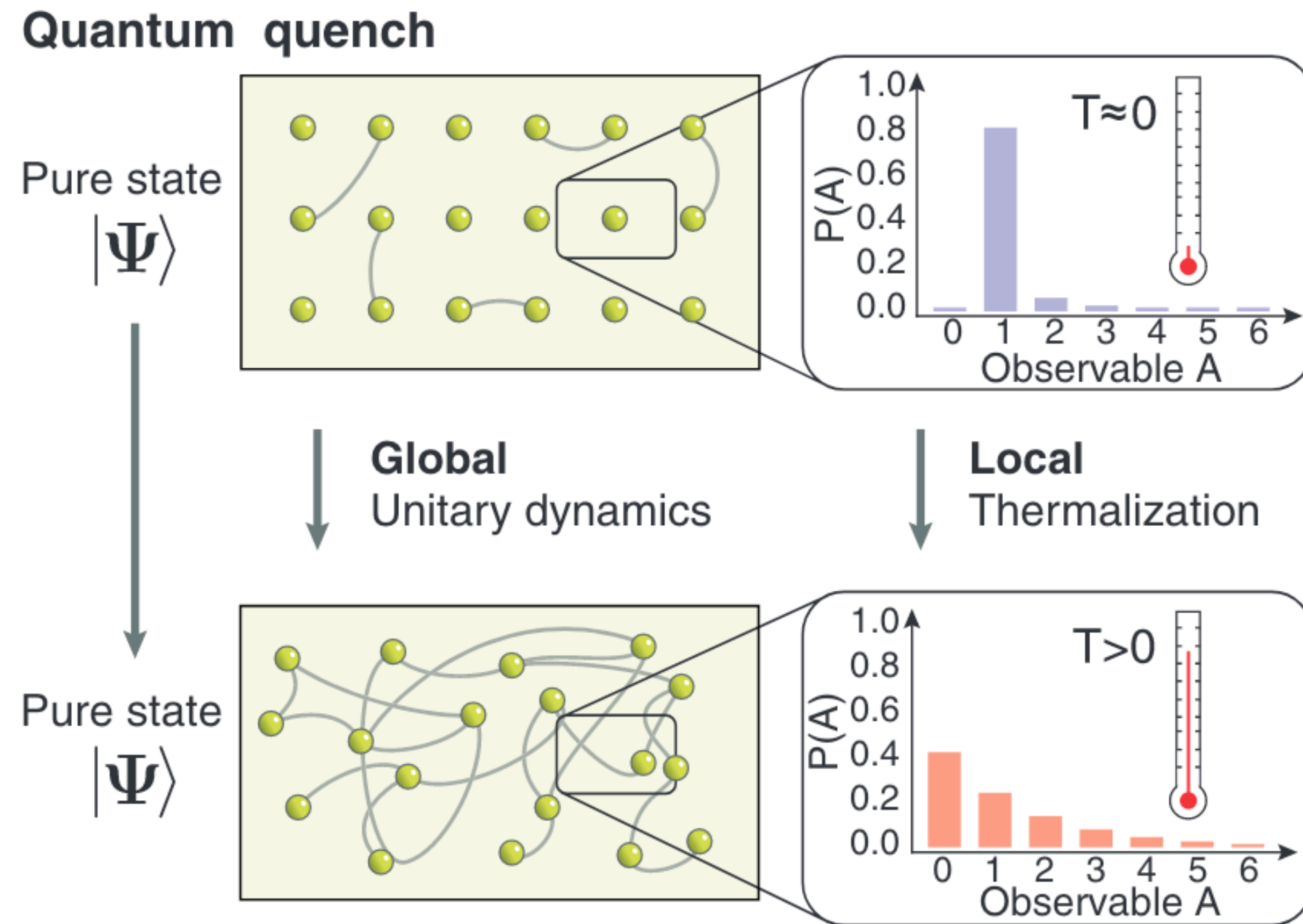
**See also:** Kivelson, S. & Schrieffer, J. R.  
Fractional charge, a sharp quantum observable.  
*Physical Review B* **25**, 6447–6451 (1982).





**Holon** created with **unit efficiency**  
**Spinon** created with **50-60% efficiency**

# Probing Thermalization in a QMB System



A. Kaufmann *et al.* Science 2016

ETH assumes that locally:  $\rho_A = \frac{1}{Z_A} e^{-\beta E_n}$

$$S_{VN} = -tr(\rho_A \log \rho_A) = S_{th}$$

Remaining System acts as “Thermal Reservoir” for smaller subsystem.

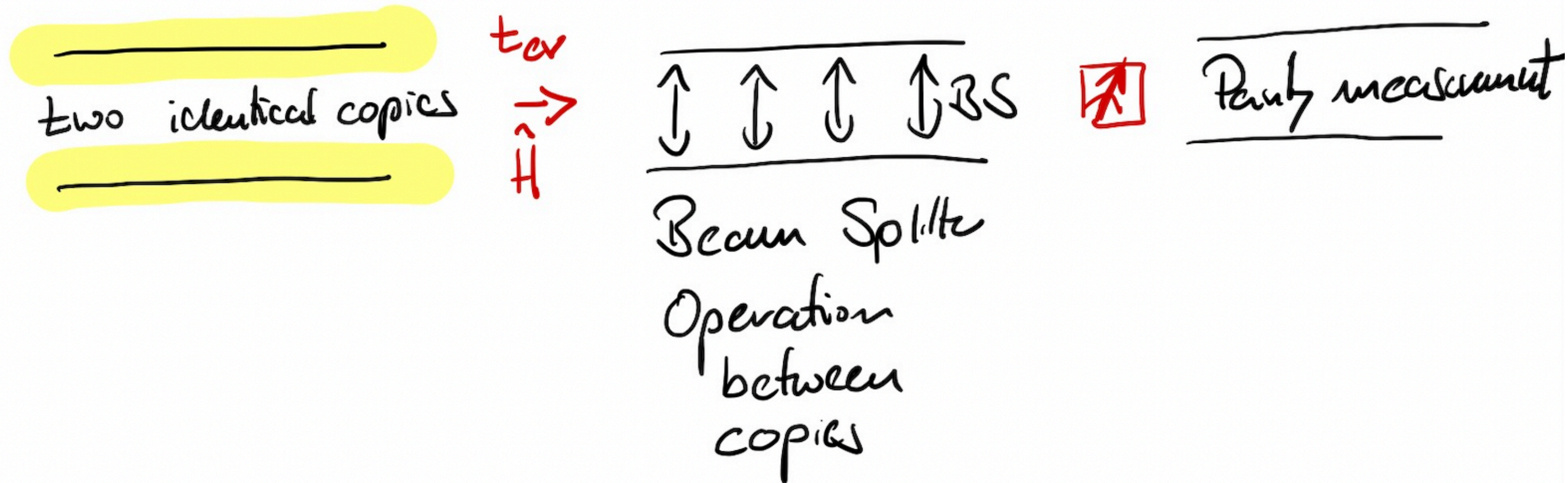
Entanglement Entropy **is** Thermal Entropy in a QMB System

## **To Show:**

- 1) Global State Remains Pure**
- 2) Locally, system looks thermal**
- 3) Probe local  $vN$  Entanglement Entropy**  
(or related quantity)



Probing State Purity via Many-Body Quantum Interference (here for bosons)



<b>Purity</b>	$tr(\rho^2)$
<b>Renyi-2 Entropy</b>	$S_2(\rho) = -\log(tr(\rho^2))$

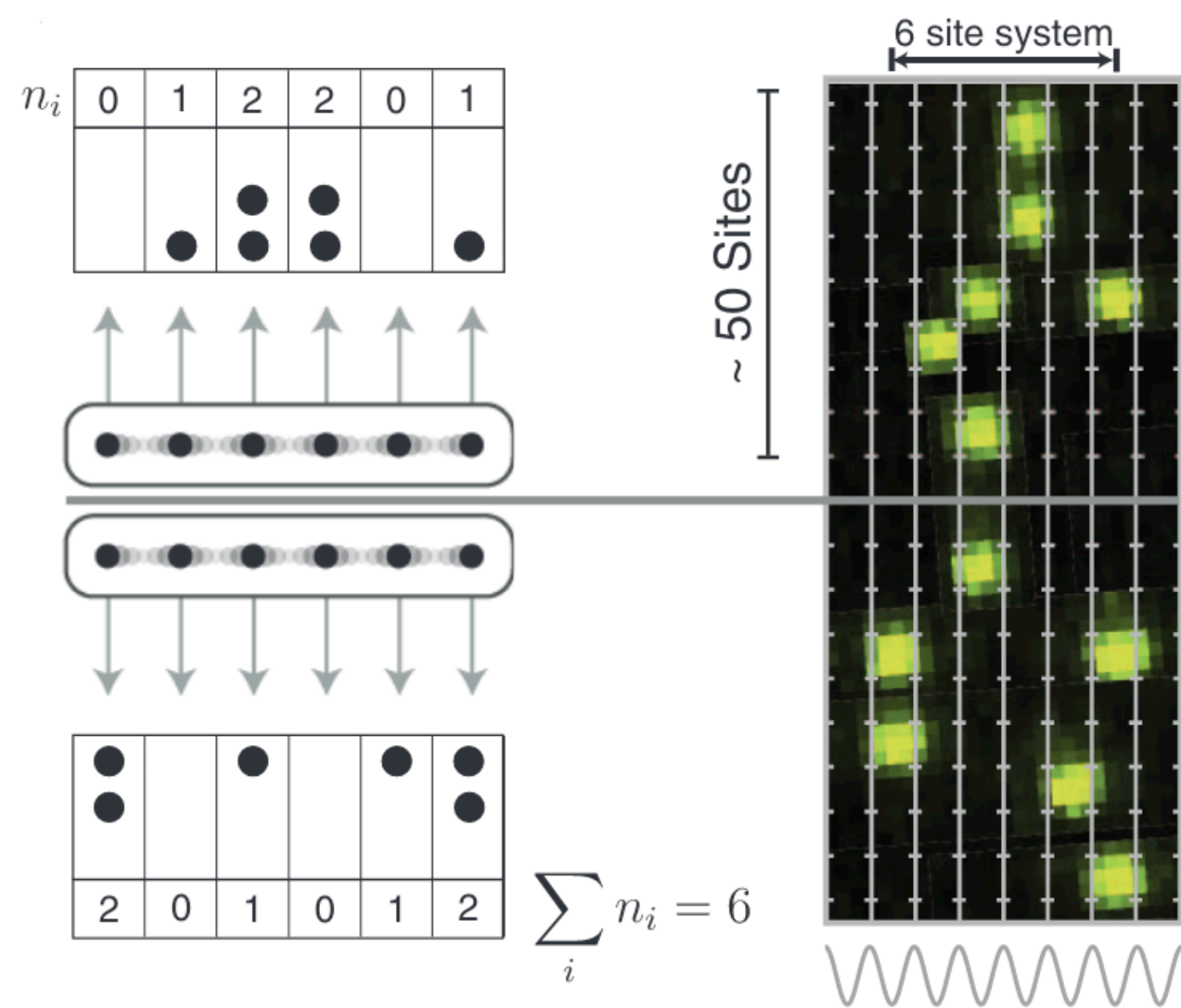
Bounds von Neumann Entropy

$$S_{vN} \geq S_2(\rho)$$

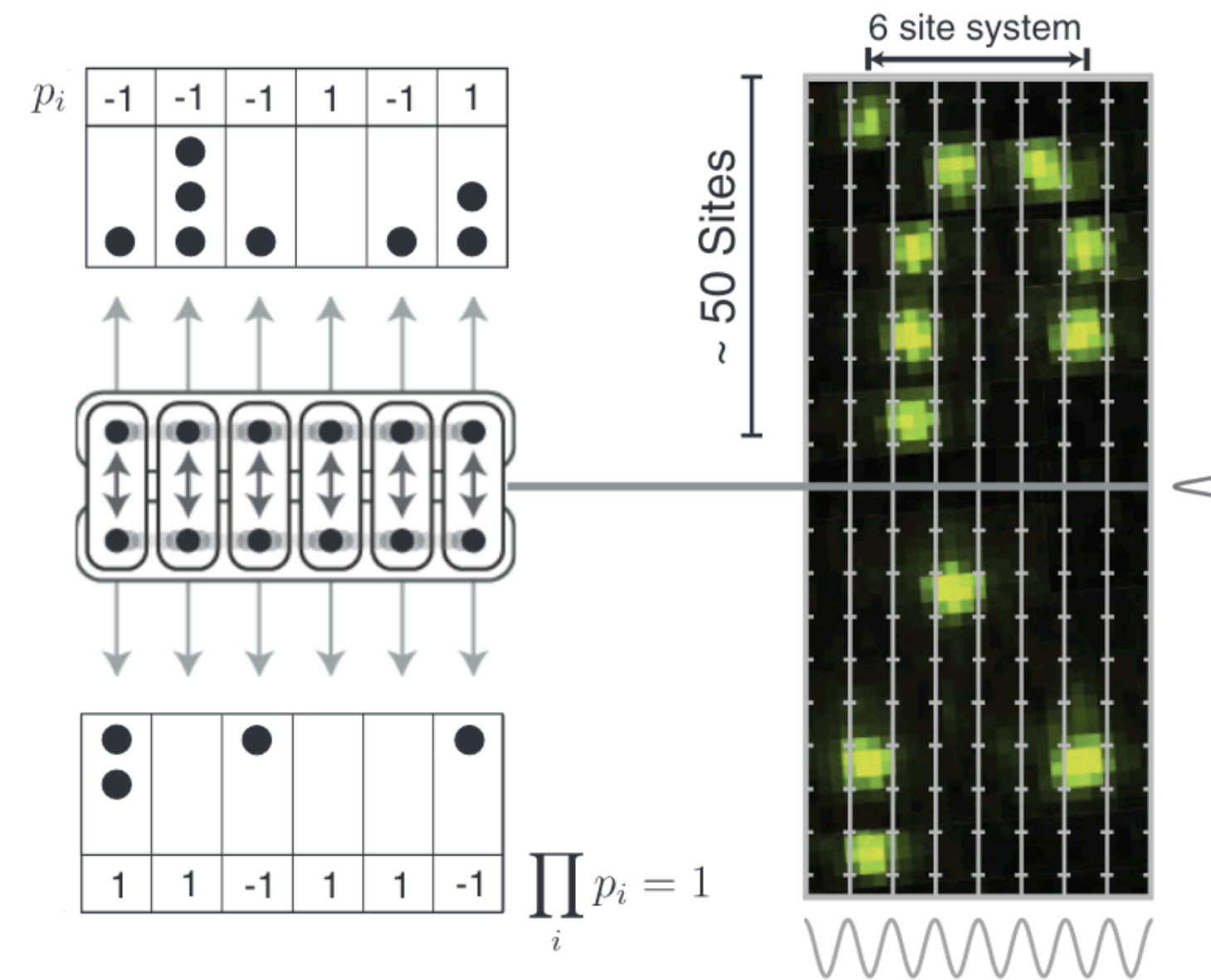


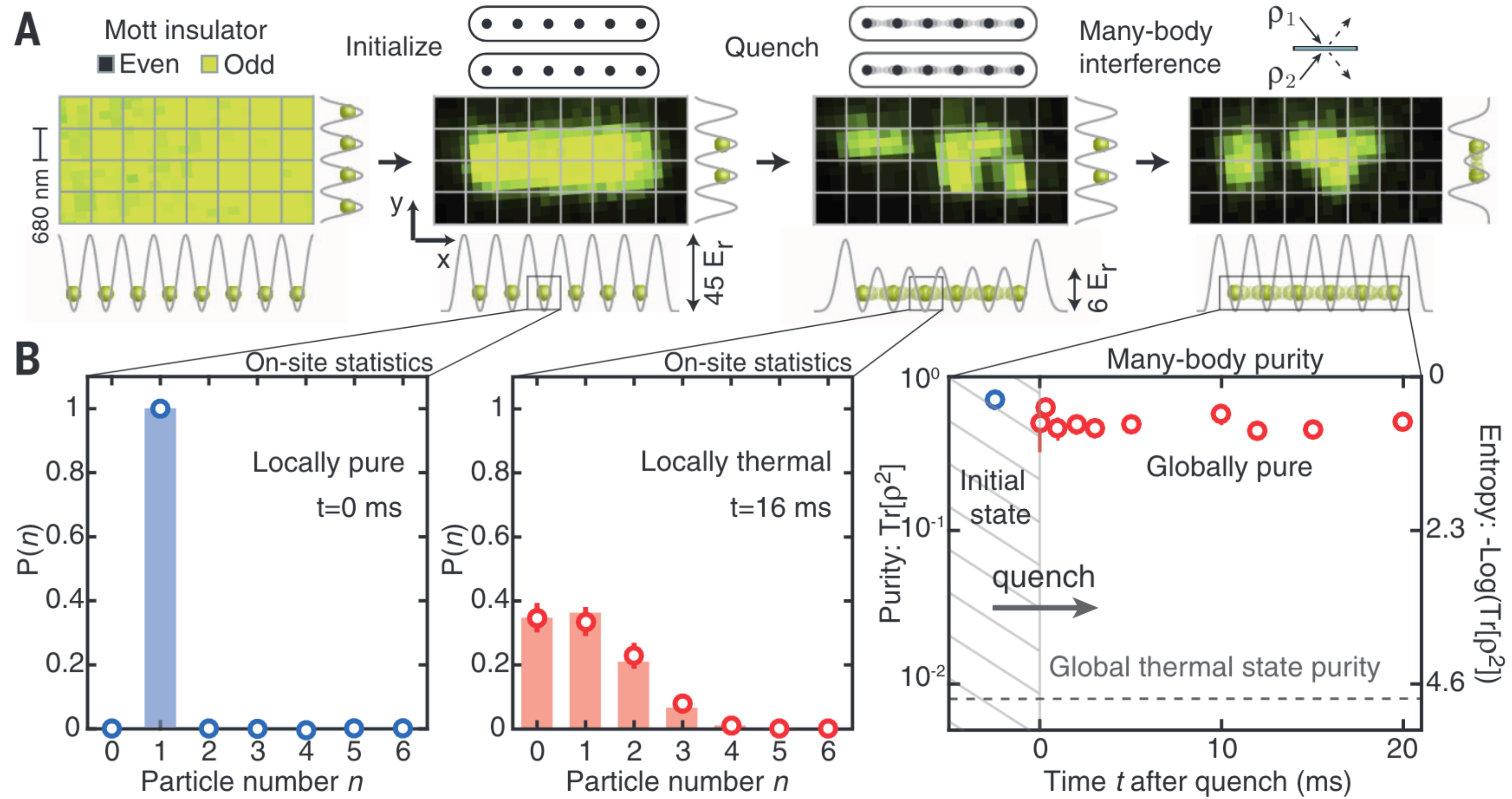
$$\text{tr}(\rho^2) = \langle \hat{P} \rangle = \langle \prod_i p_i^{(k)} \rangle$$

**C** Expansion to measure local occupation number

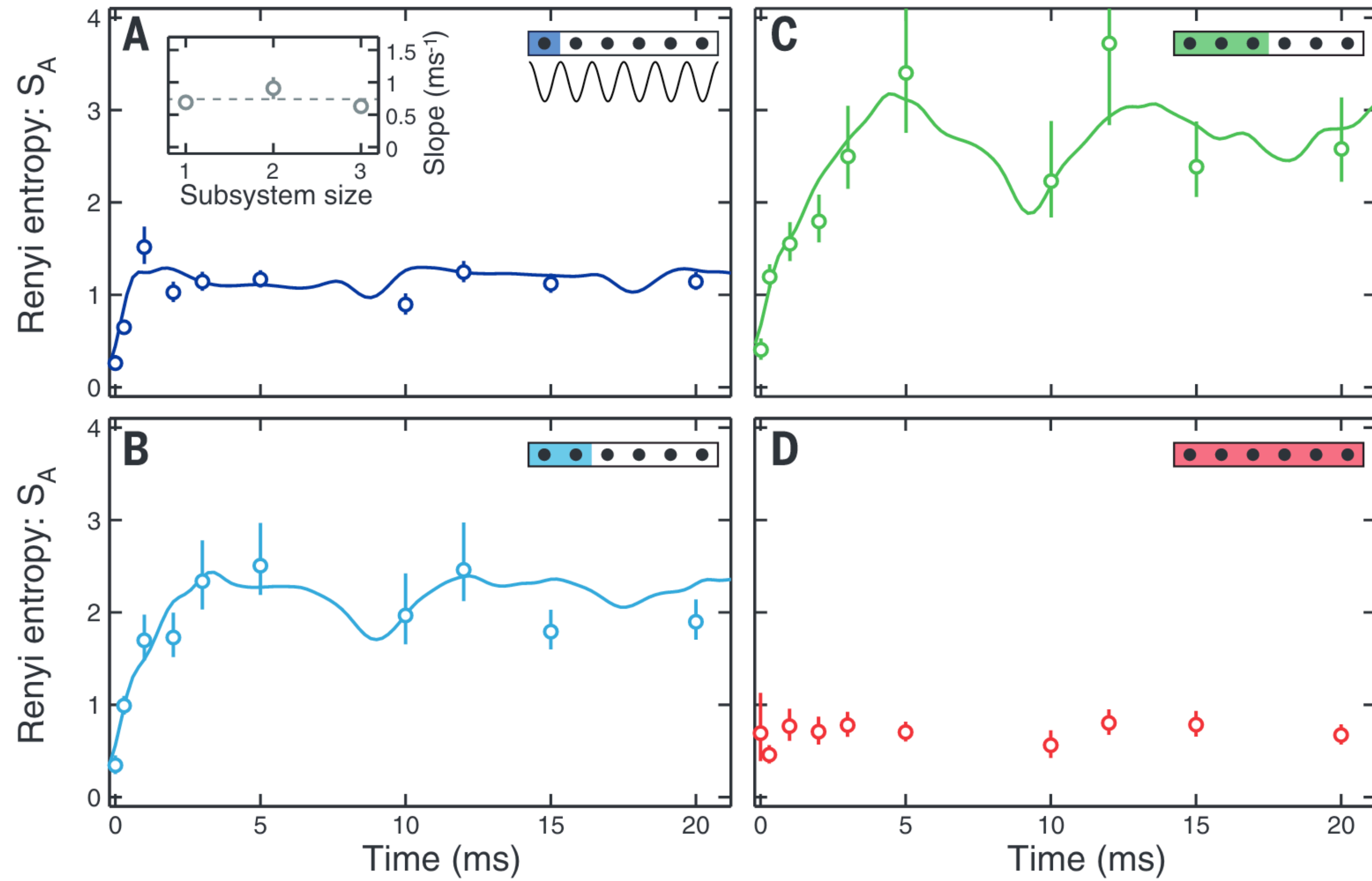


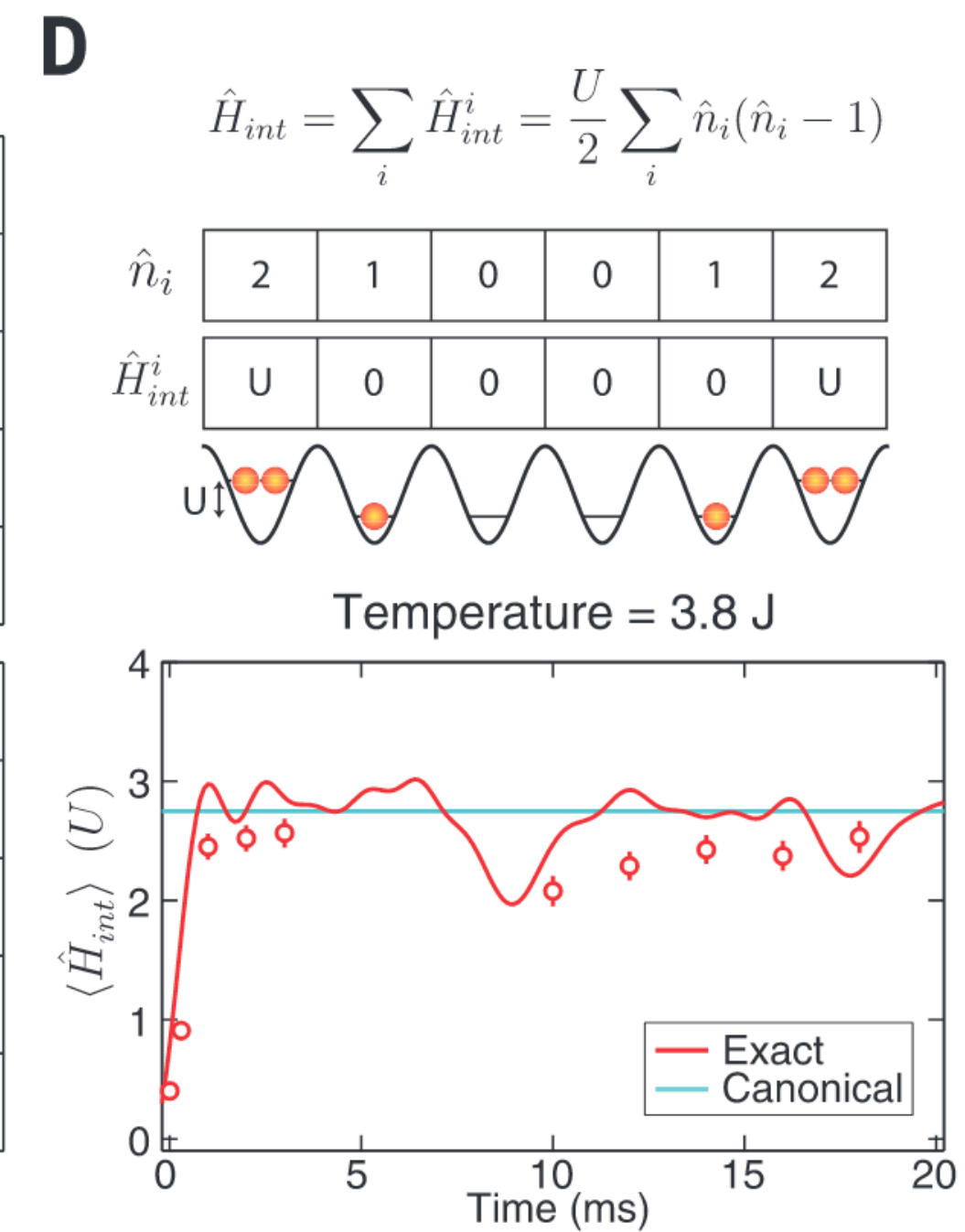
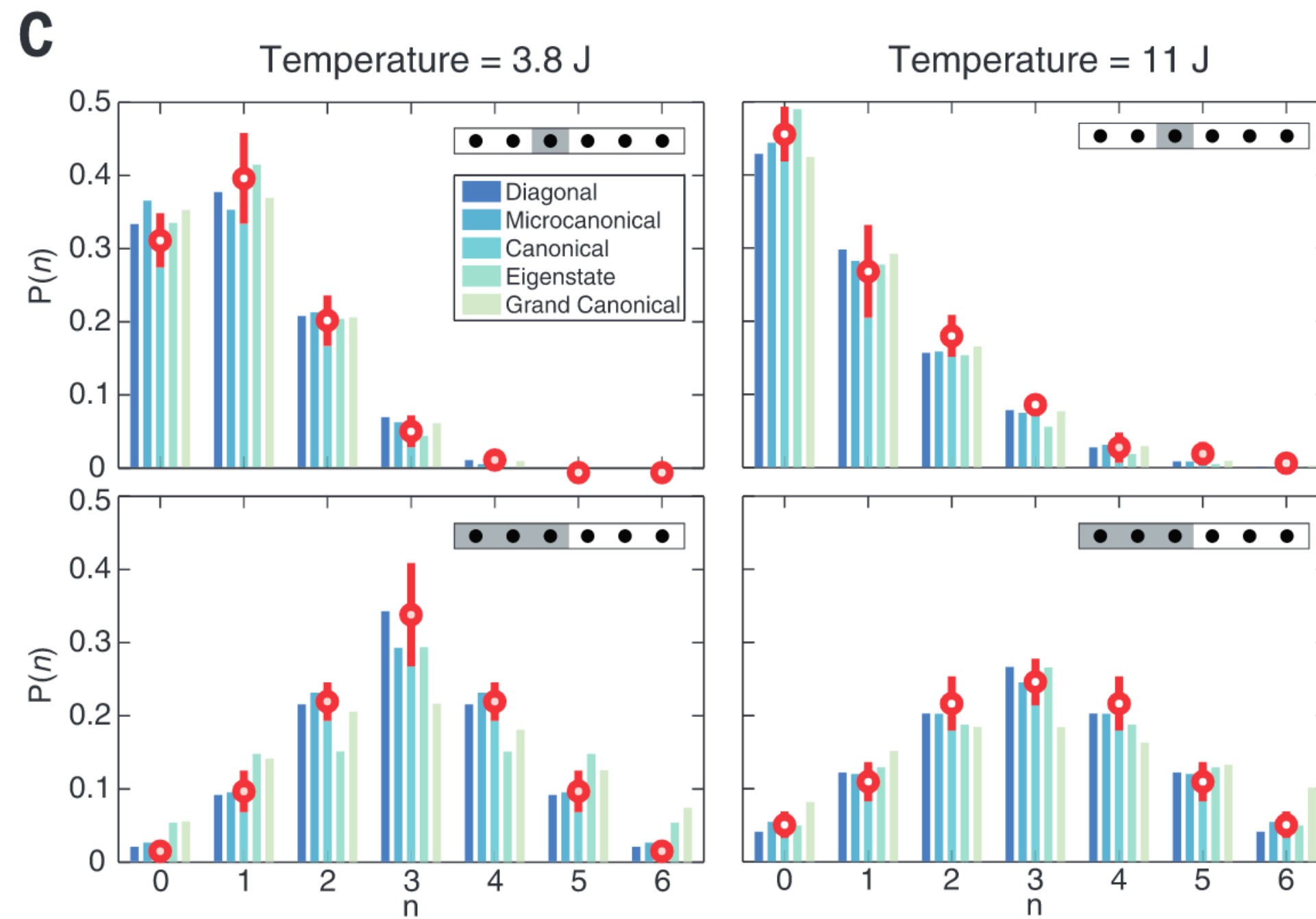
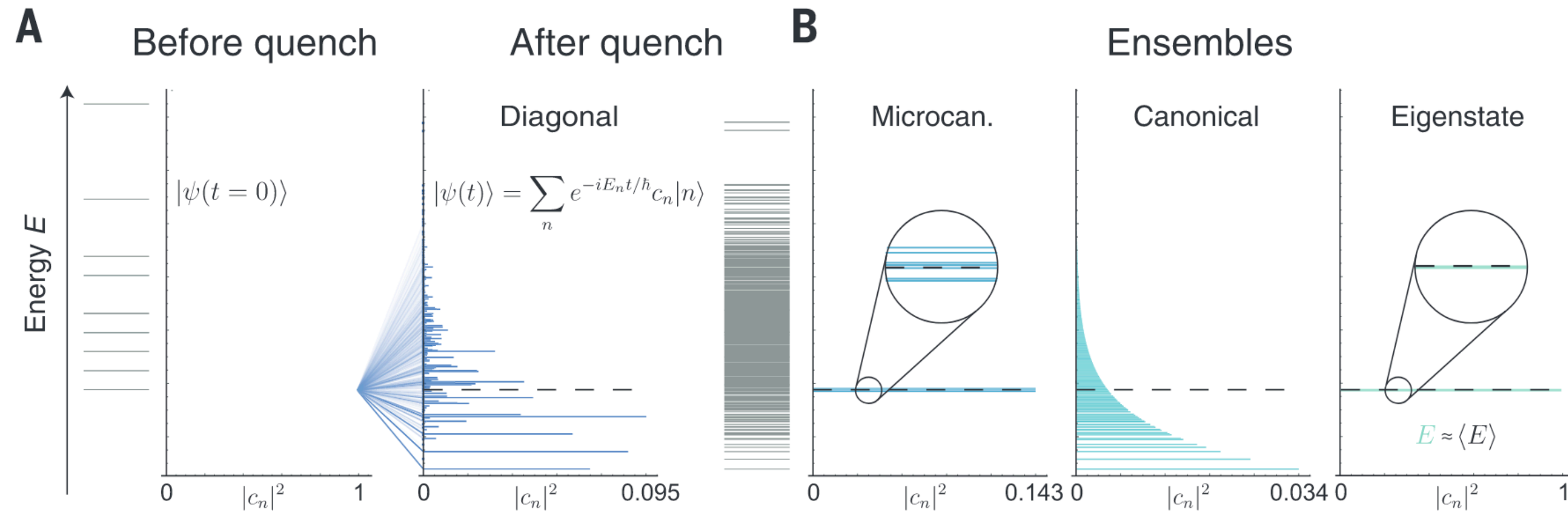
Expansion to measure local and global purity











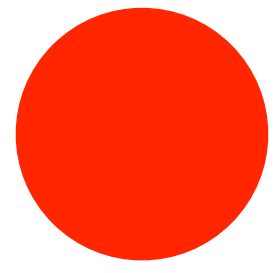
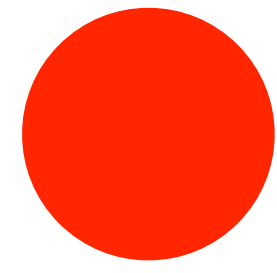
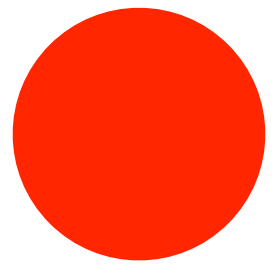
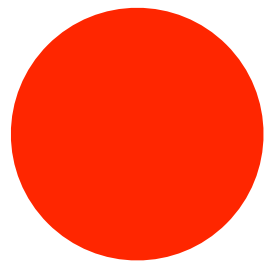
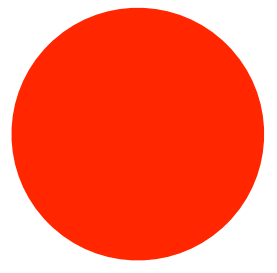
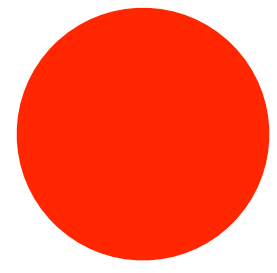
# Promising: Double Quantum Advantage (in Space & Time)

**But also challenging for experiments!**

- **Large System Sizes**
- **Homogeneous Systems**
- **Long Time Evolutions**

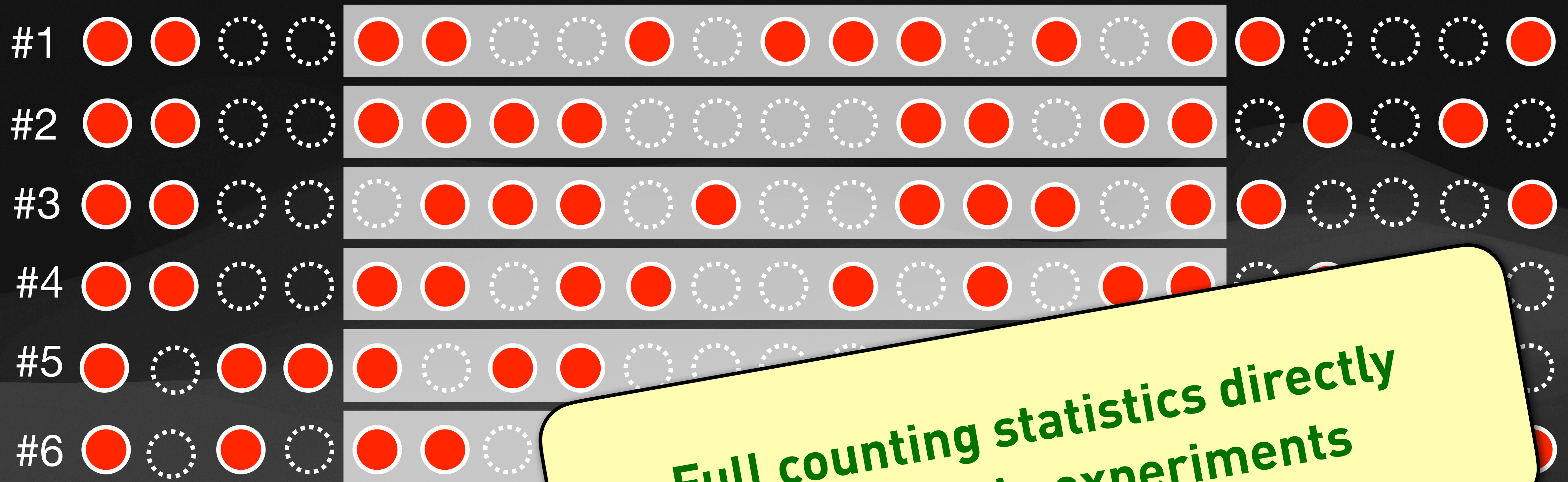
$$e^{-i\hat{H}t/\hbar}$$

**...Time evolution...**

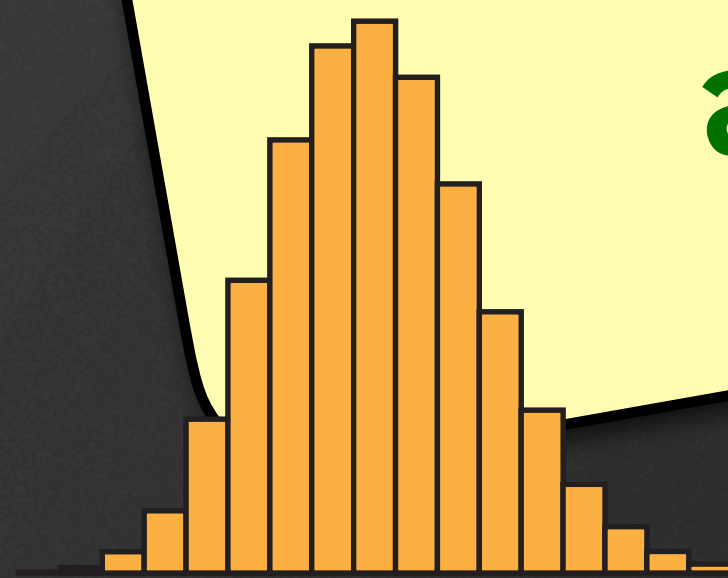
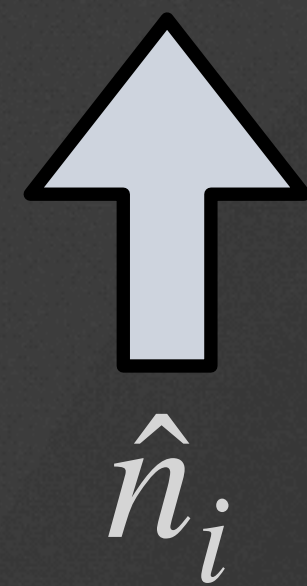




# Quantum Transport - Atom-by-Atom

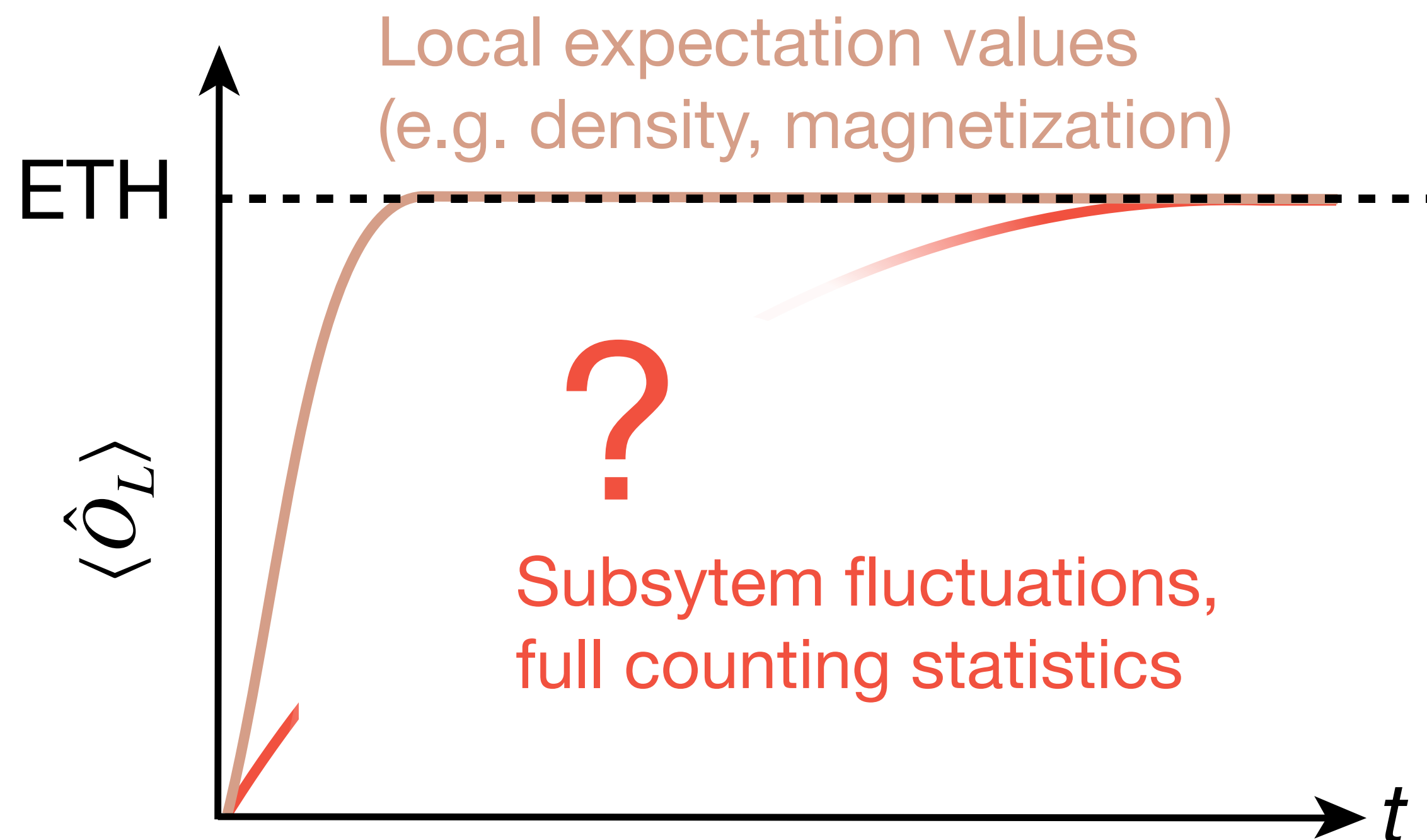
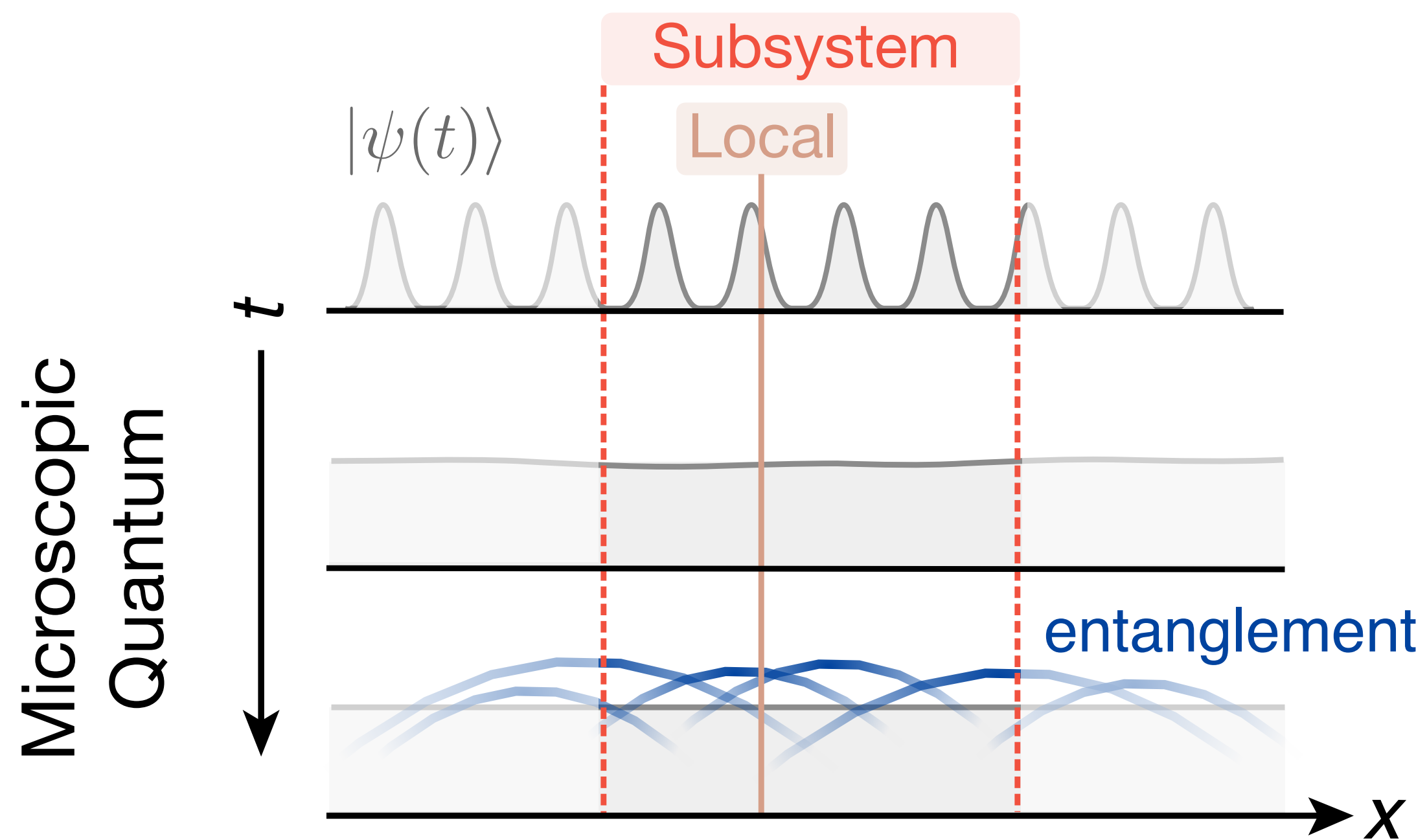


**Full counting statistics directly accessible in experiments**





## Stages of Dynamics



### Eigenstate Thermalisation Hypothesis

J. M. Deutsch, Phys. Rev. A **43**, 2046 (1991).

M. Srednicki, Phys. Rev. E **50**, 888 (1994).

M. Rigol, V. Dunjko, and M. Olshanii, Nature **452**, 854 (2008).

R. Nandkishore, Phys. Rev. B **92**, 245141 (2015).

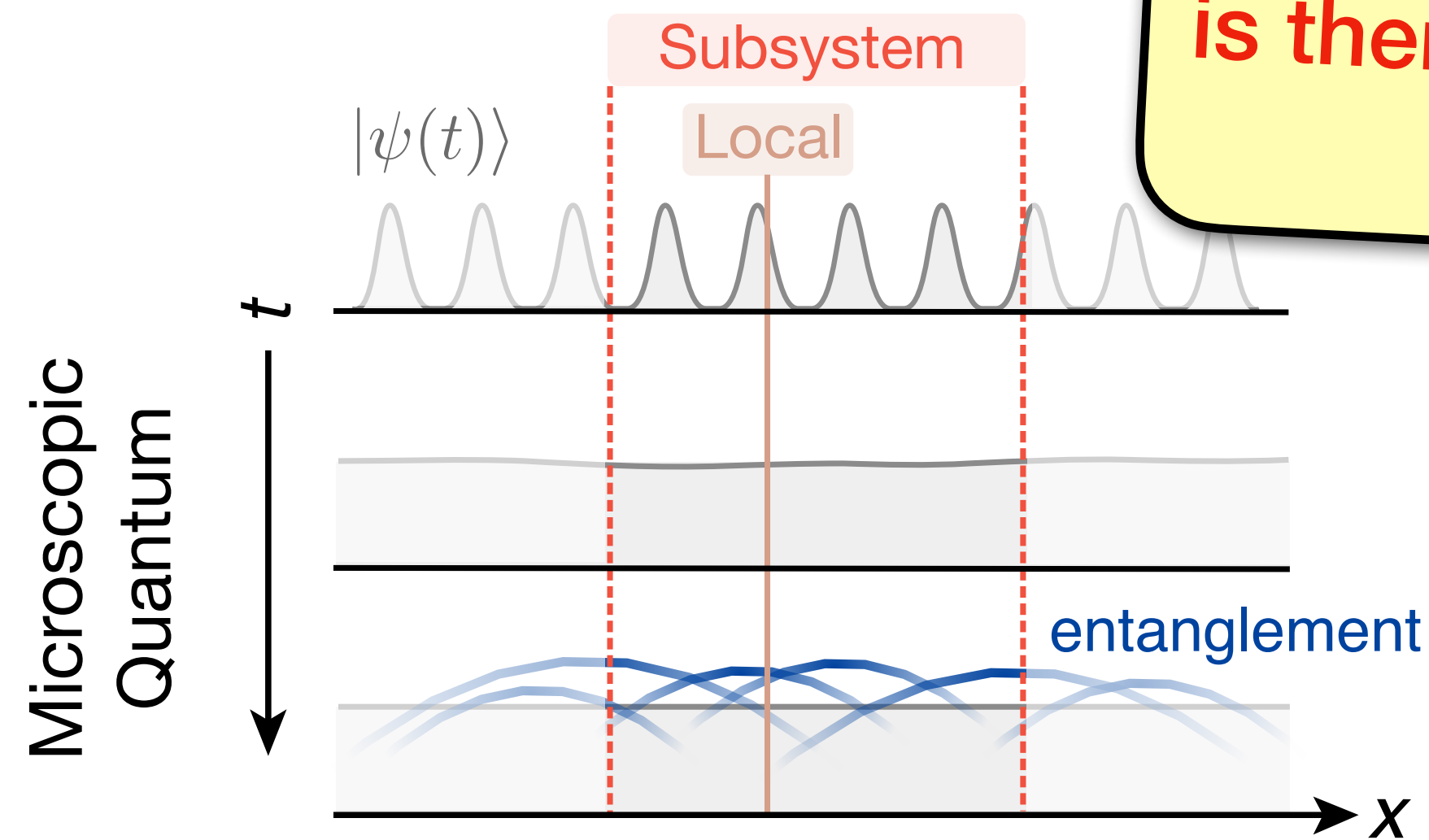
L. D'Alessio, Y. Kafri, A. Polkovnikov, and M. Rigol Adv. Phys. **65**, 239 (2016).

### Experiments Thermalisation

A. M. Kaufman et al., Science **353**,794 (2016).

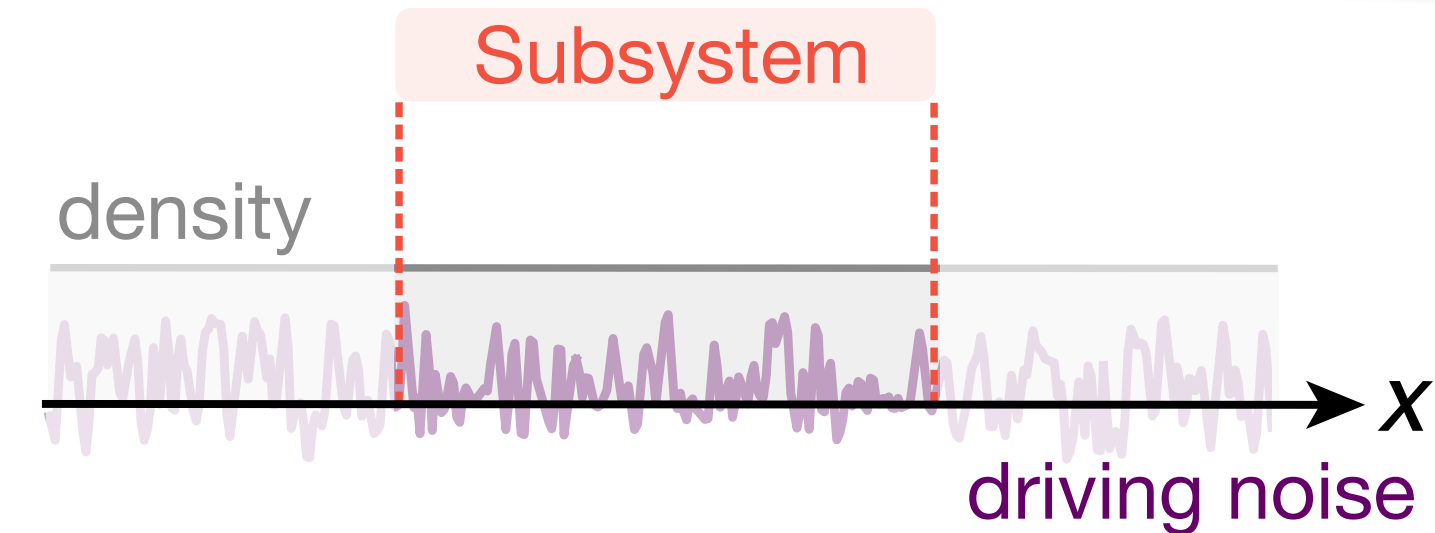


## Stages of Dynamics



Can this work for quantum systems as well ???  
is there an emergent hydrodynamics of fluctuations

Macroscopic  
Classical



## Classical Systems: Macroscopic Fluctuation Theory

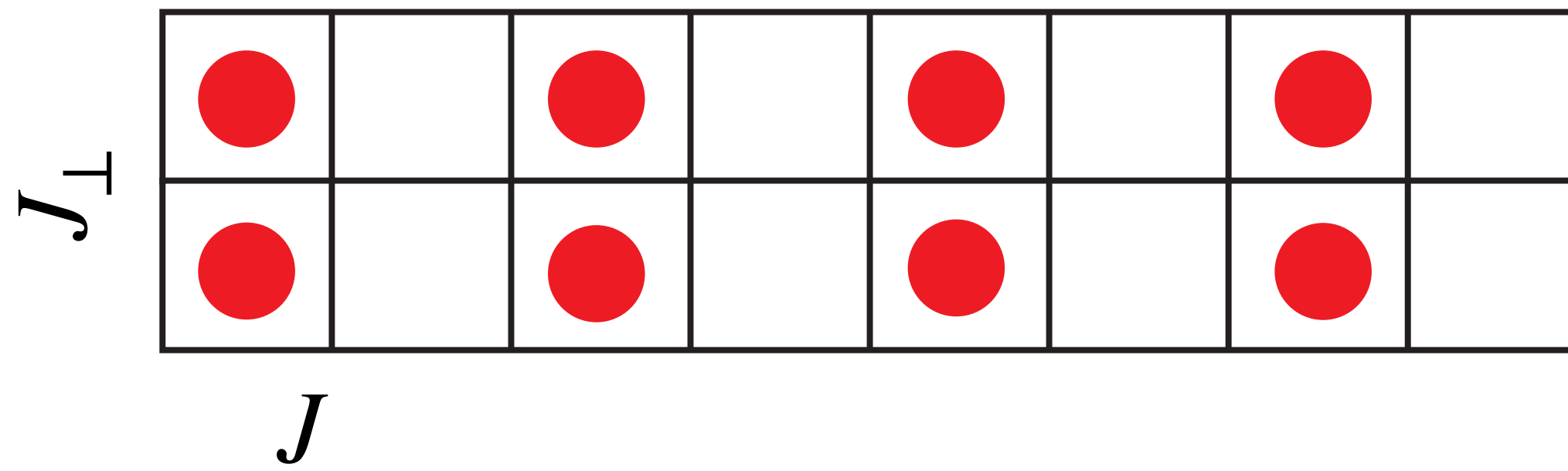
$$\partial_t n + \partial_x j = 0, \quad j = -D(n) \partial_x n + \sqrt{2D(n)} \chi(n) \xi$$

Nonlinear stochastic PDE

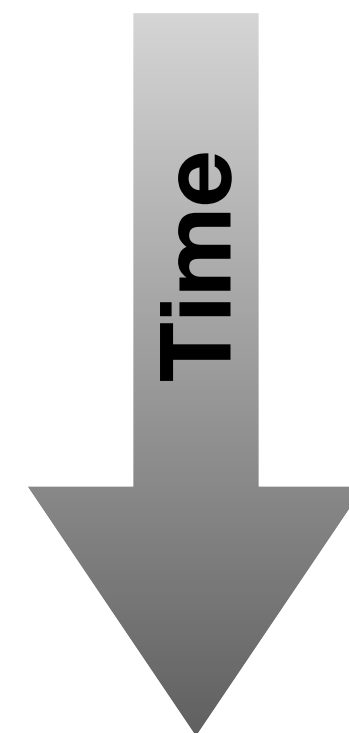
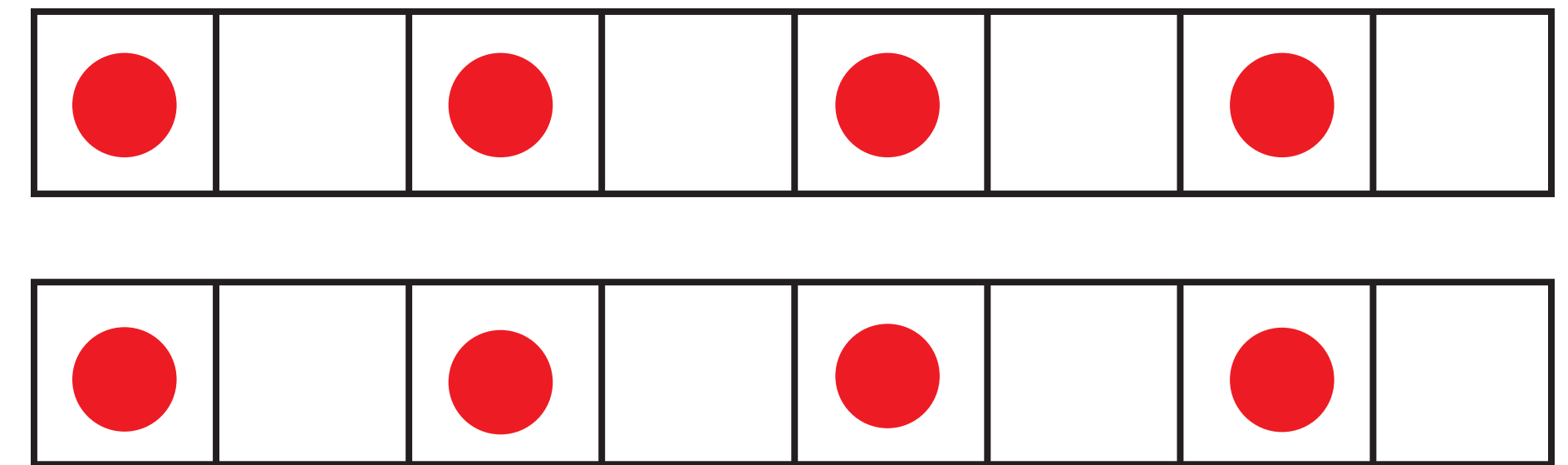
## Hardcore bosons

(on a ladder (2x50 sites) with tunable coupling)

Coupled ladders (interacting)

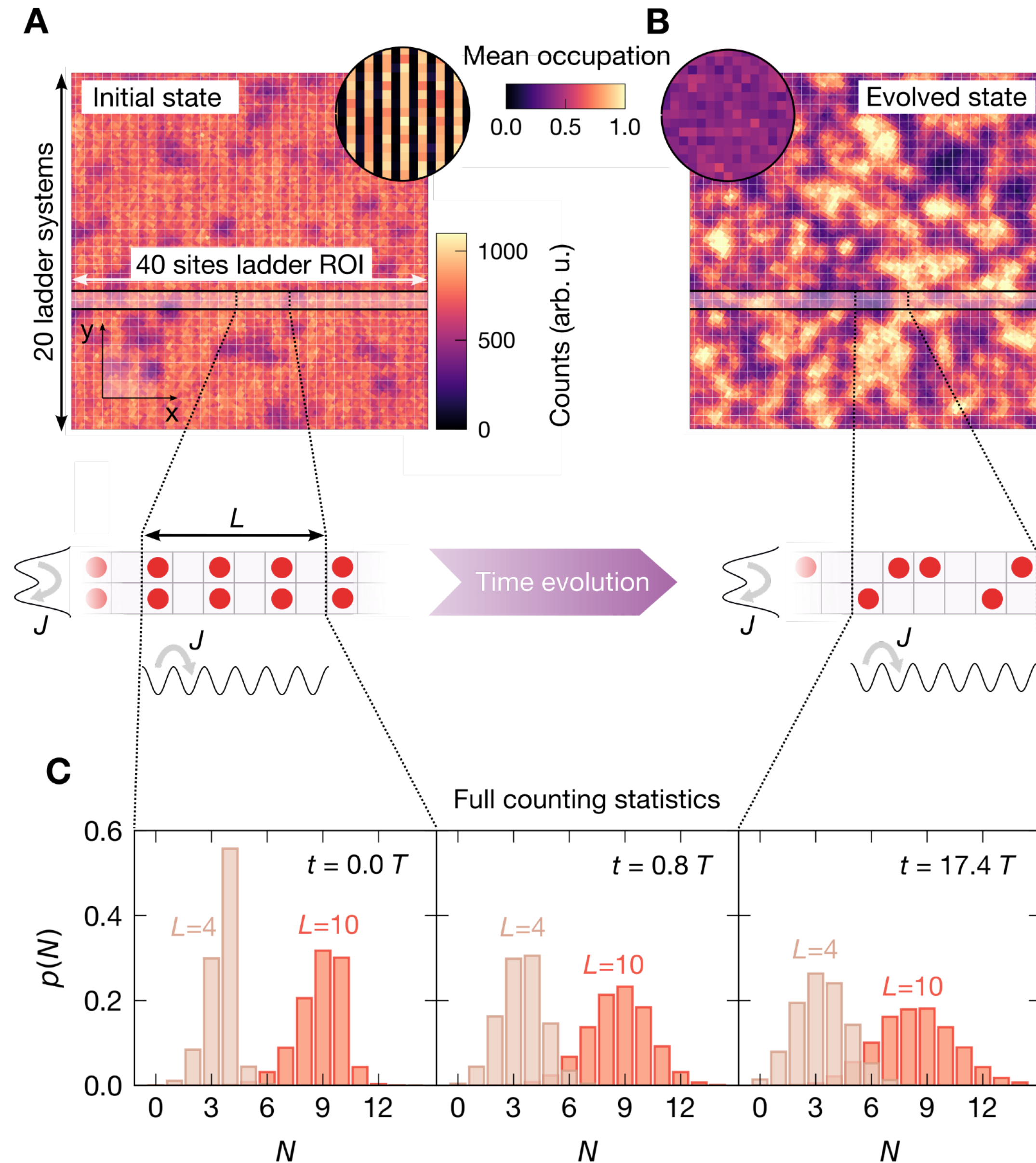


1d chains (free fermions)





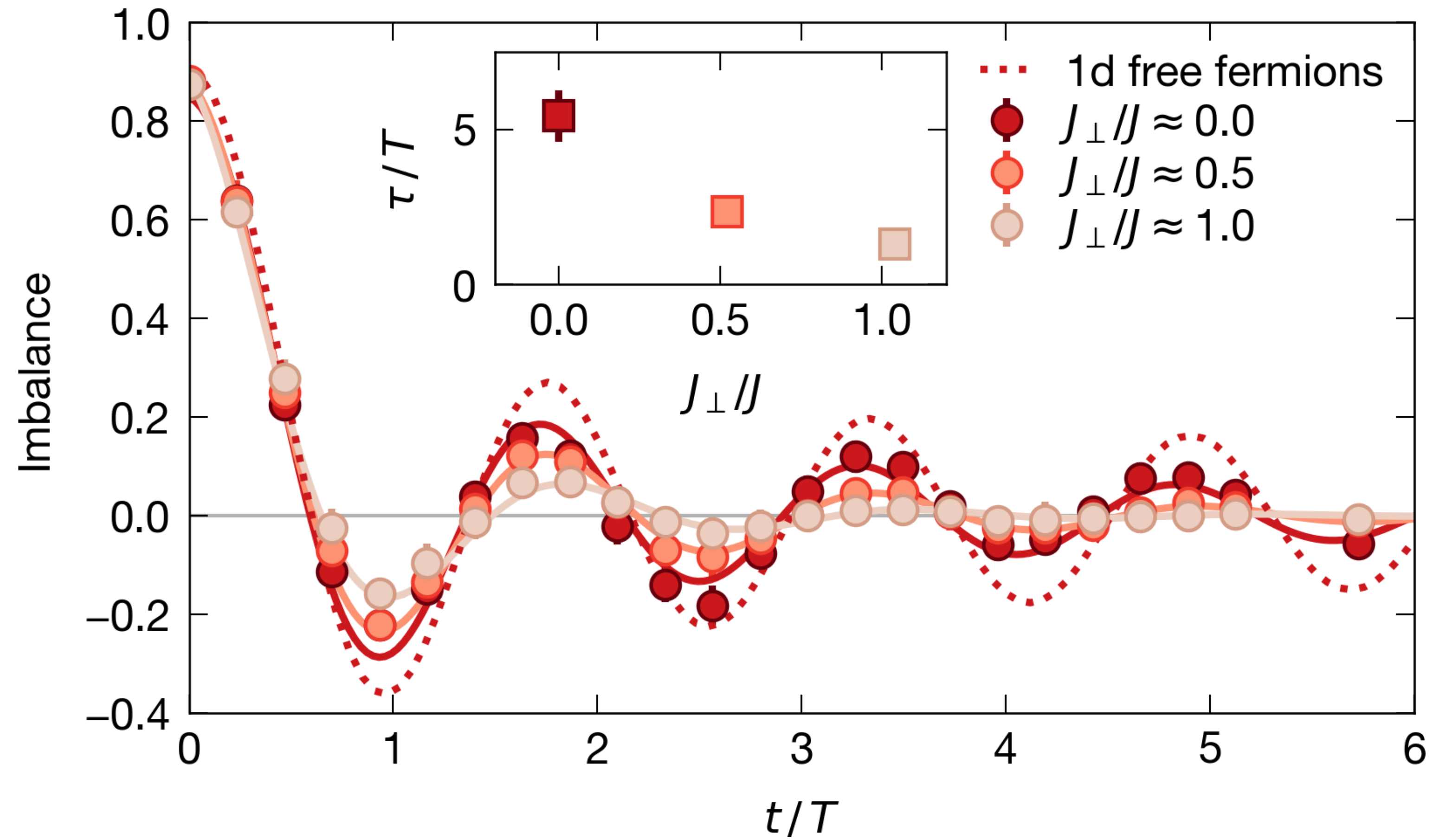
# Thermalisation: Integrable vs. Chaotic



**Hardcore bosons  
(tunable ladder coupling)**

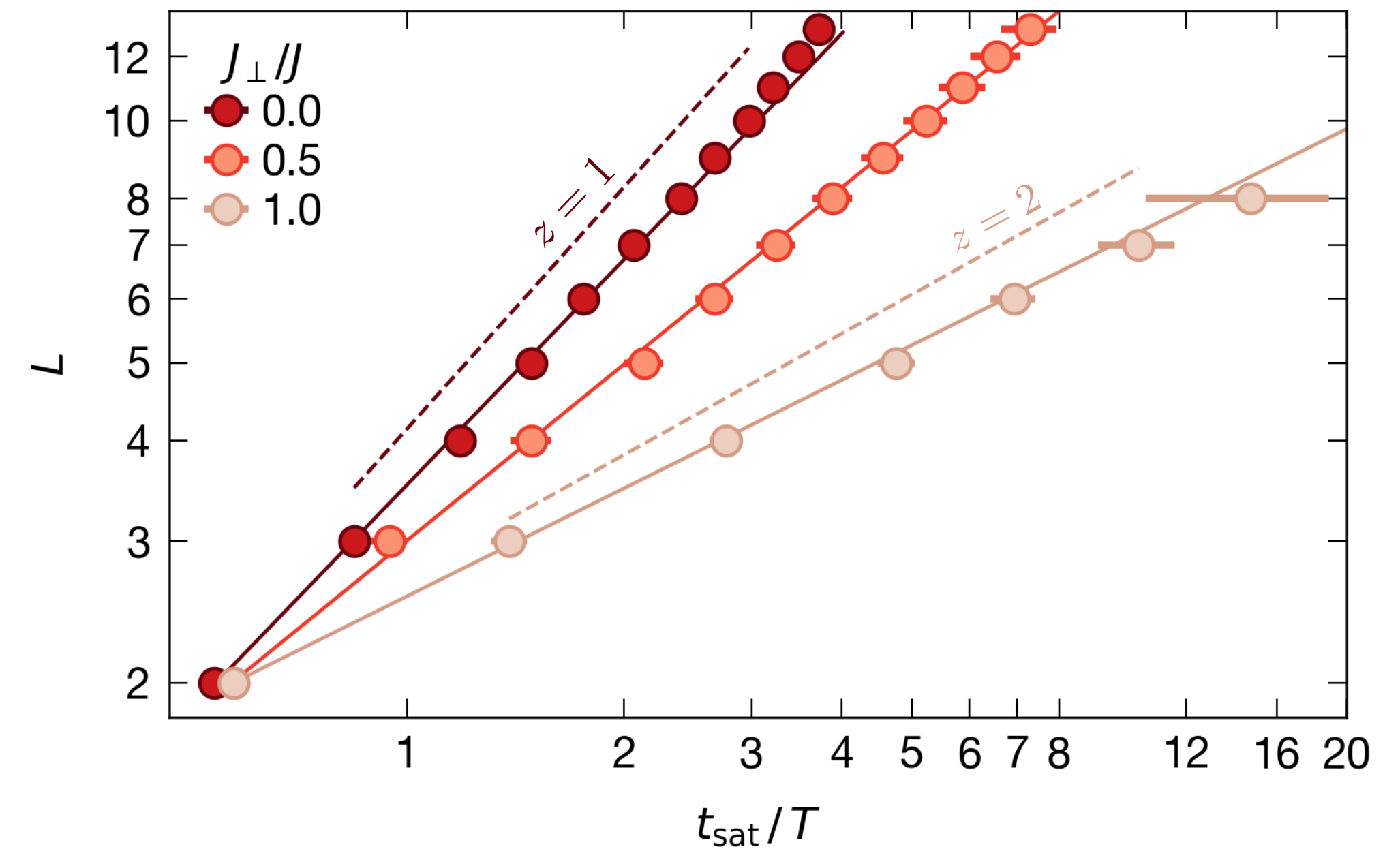
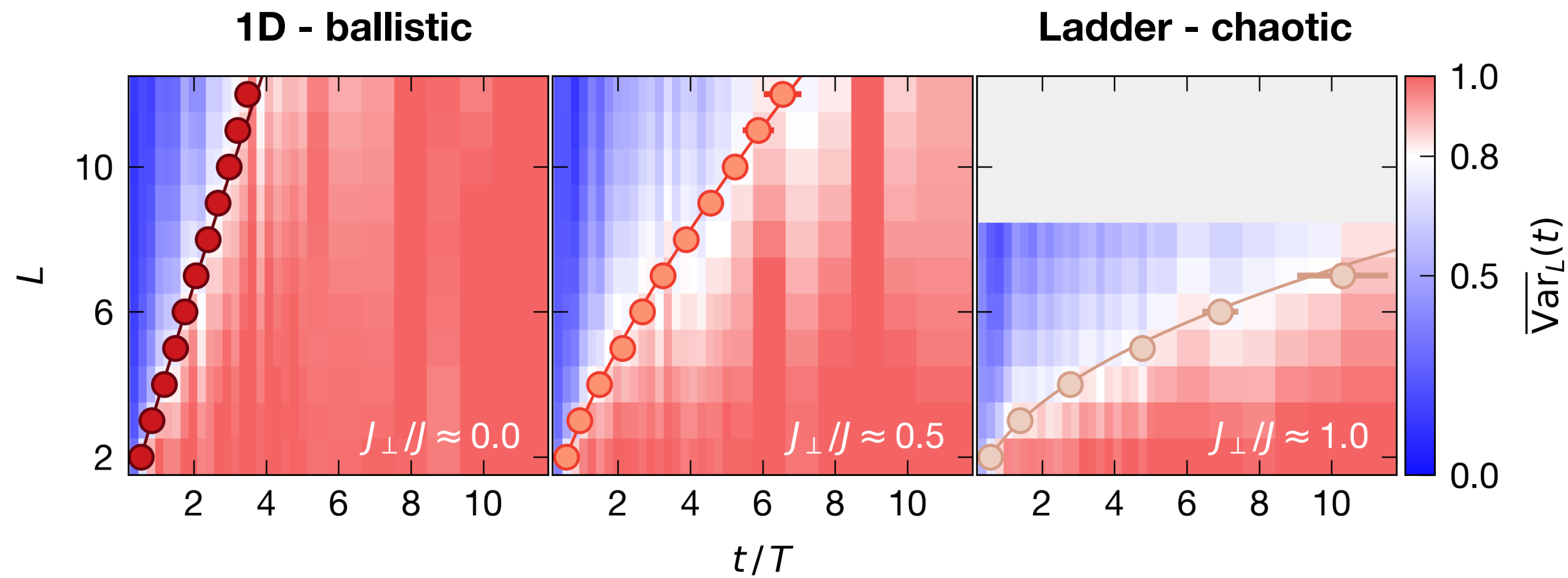
**Full counting statistics on  
different subsystem sizes**

**Related:**  
A.M. Kaufman *et al.*  
Science **353**, 794 (2016)  
and thermalisation  
experiments by D. Weiss (PennState)





## Subsystem fluctuations



$$\text{Var}_L(t) \approx \sqrt{\frac{2Dt}{\pi\alpha^2}}$$

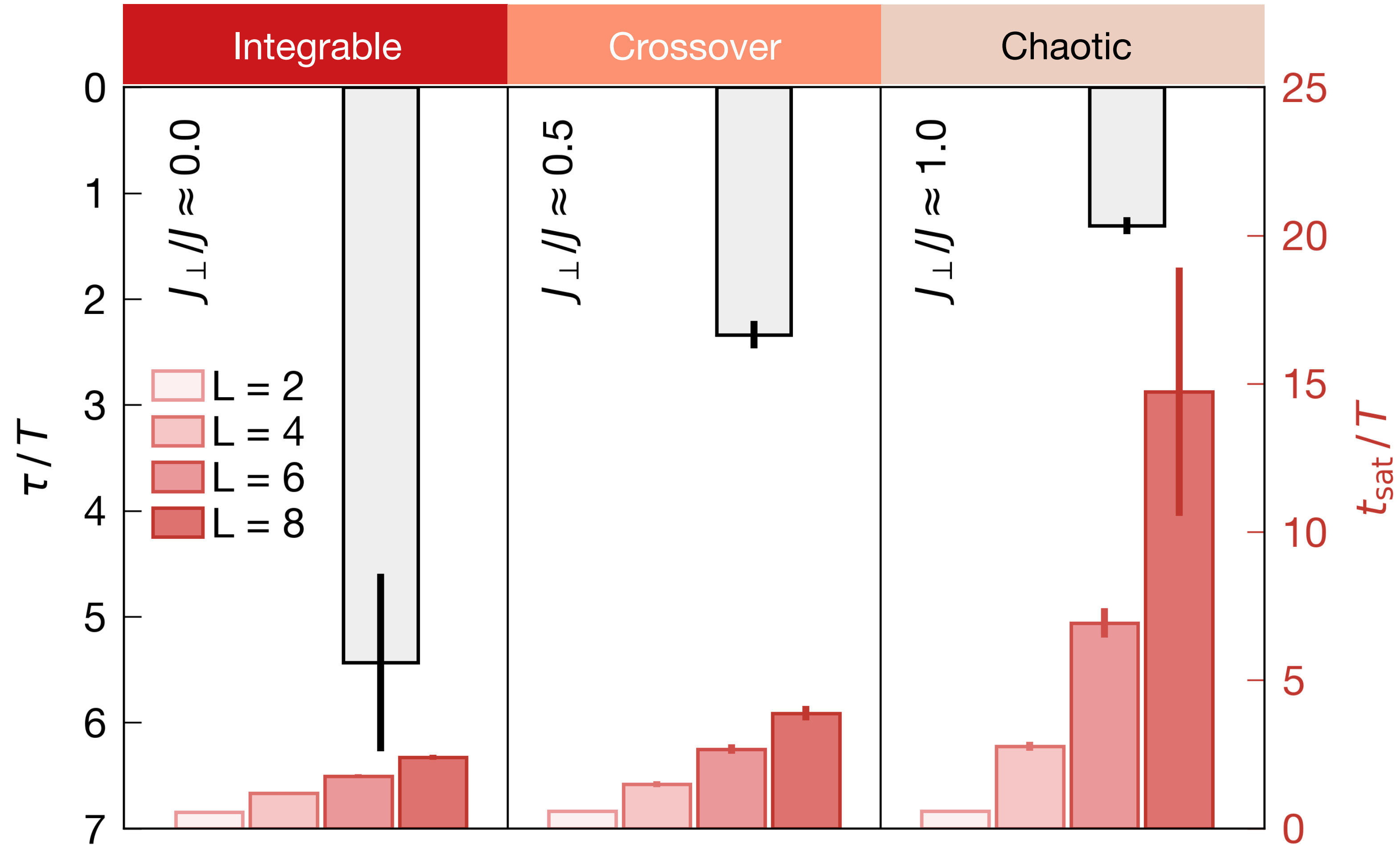
MFT prediction

► Enables quantitative determination of **dynamical exponent  $z$**  and **diffusion constant**

► **Global equilibrations** takes longer and longer for larger subsystem

$$L \propto t_{\text{sat}}^{1/z}$$

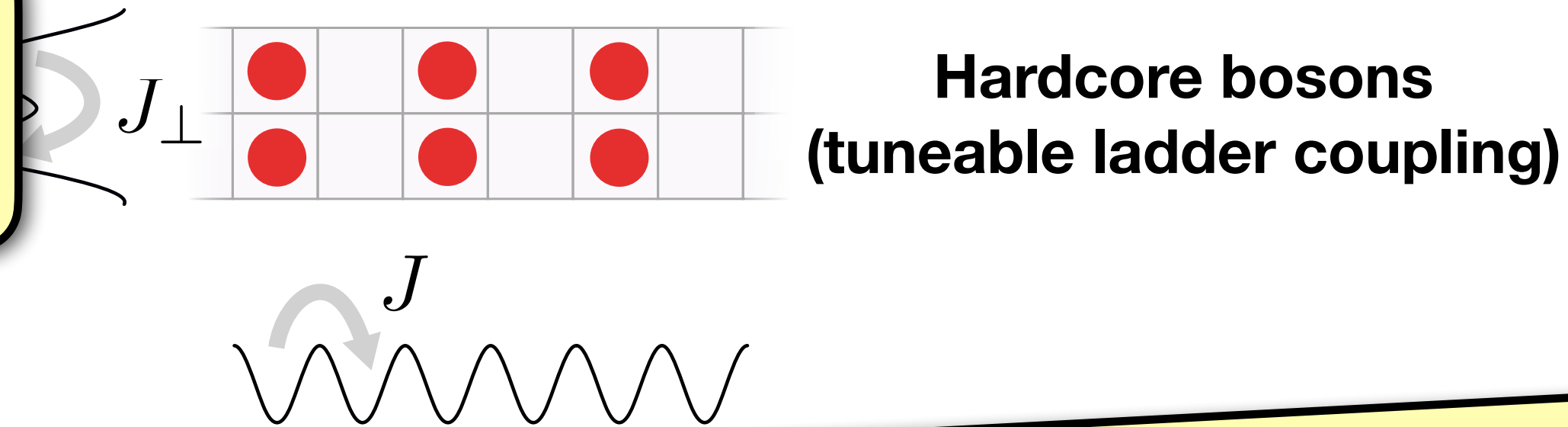
**Determination of dynamical exponent**



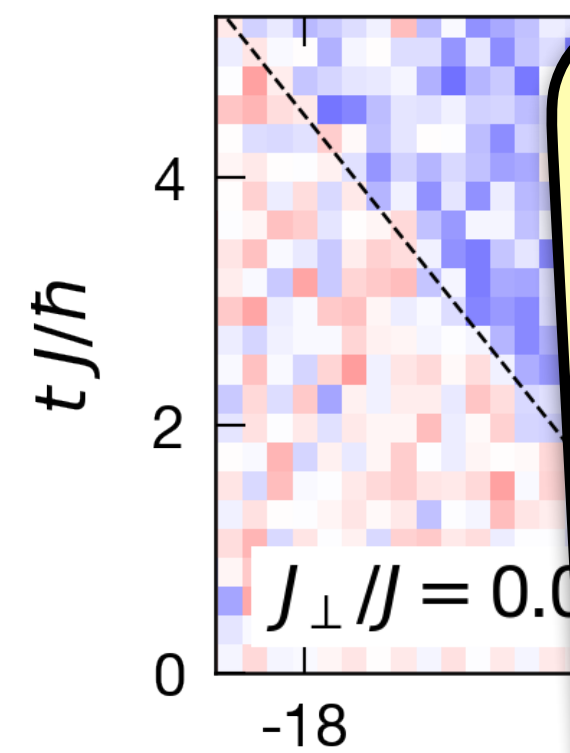


# Density-Density Correlations

$$C(i-j) = \langle \hat{N}_i \hat{N}_j \rangle - \langle \hat{N}_i \rangle \langle \hat{N}_j \rangle$$



Integrable (free fermions)



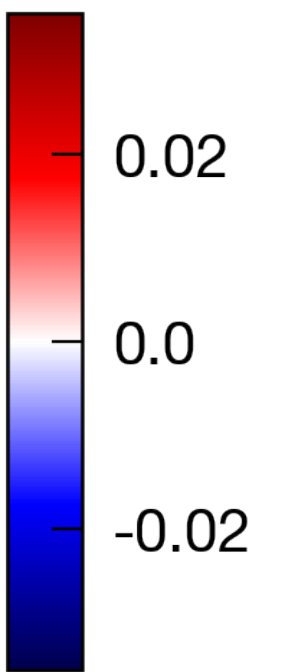
Experiment

$$D_{exp} = 0.88(5)$$

Equilibrium theory

$$D_{eq} = 0.95, 0.97$$

Test for **fluctuating hydrodynamics** in chaotic quantum systems



Distance  $i-j$

Distance  $i-j$

Distance  $i-j$

## See also:

M. Cheneau, ..., I. Bloch, S. Kuhr, Nature (2012)

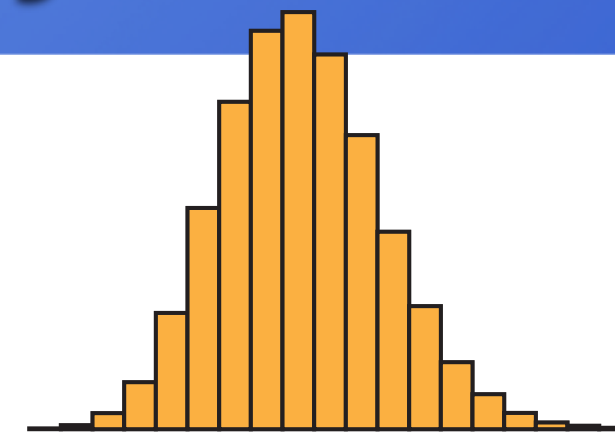
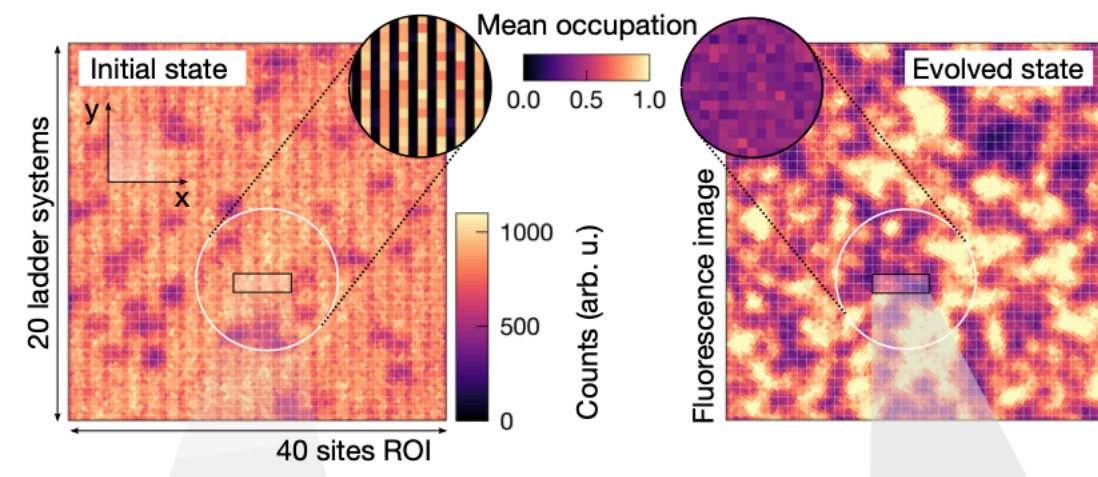
Y.-G. Zheng, ..., Z.-S. Yuan, J.-W. Pan, arXiv:2210.08556

## Equilibrium transport theory:

R. Steinigeweg et al., Phys. Rev. B (2014)

T. Rakovszky, C. W. von Keyserlingk & F. Pollmann Phys. Rev. B (2022)

## Rung Density-Density Correlations



- ▶ **Full counting statistic / fluctuations** powerful new observables for quantum transport
- ▶ **(Nonlinear) Noisy classical dynamics** can efficiently describe **charge fluctuation dynamics in chaotic quantum many-body systems** via MFT
- ▶ Test of **fluctuation-dissipation theorem**
- ▶ Determination of **equilibrium transport** through out-of-equilibrium dynamics
- ▶ **When does MFT fail? Higher order cumulants**

Can the Macroscopic Fluctuation Theory be Quantized ?

Denis BERNARD ♣<sup>1</sup>

♣<sup>1</sup> Laboratoire de Physique de l'Ecole Normale Supérieure, CNRS, ENS & Université PSL, Sorbonne Université, Université de Paris, 75005 Paris, France.

# KPZ Spin Transport in Heisenberg Quantum Magnets

## Numerical Evidence

M. Ljubotina et al., Nature Comm. (2017)

M. Ljubotina et al., Phys. Rev. Lett. (2019)

**Review:** see V. Bulchadini, S. Gopalakrishnan, E. Ilievski J. Stat. Mech. 084001 (2021)

## Experiment & Theory

**Experiment:** D. Wei, A. Rubio-Abadal, K. Srakaew, C. Gross, J. Zeiher, I.B.

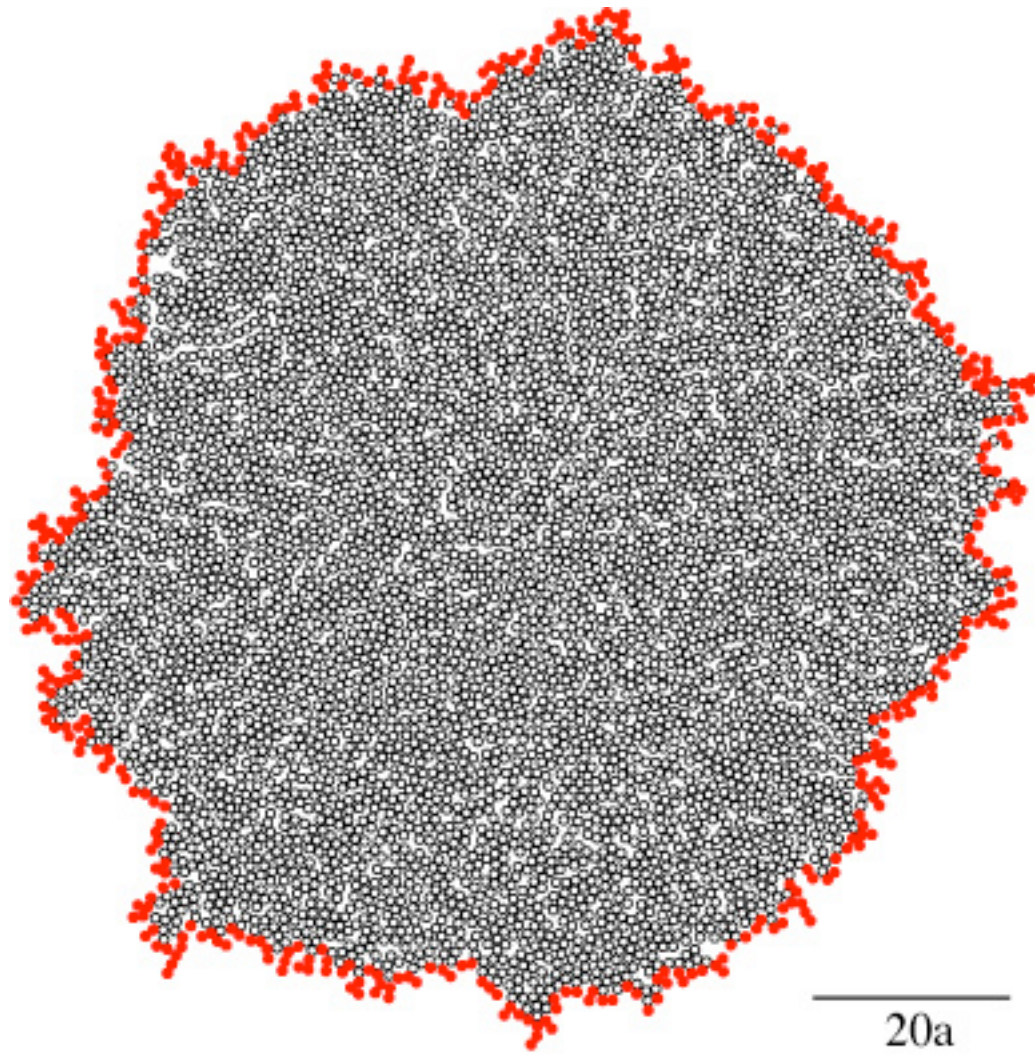
**Theory:** B. Ye , F. Machado, J. Kemp. N. Yao & S. Gopalakrishnan  
Science **376**, 716–720 (2022)

**See also:** E. Rosenberg et al arXiv:2306.11457 (Google)



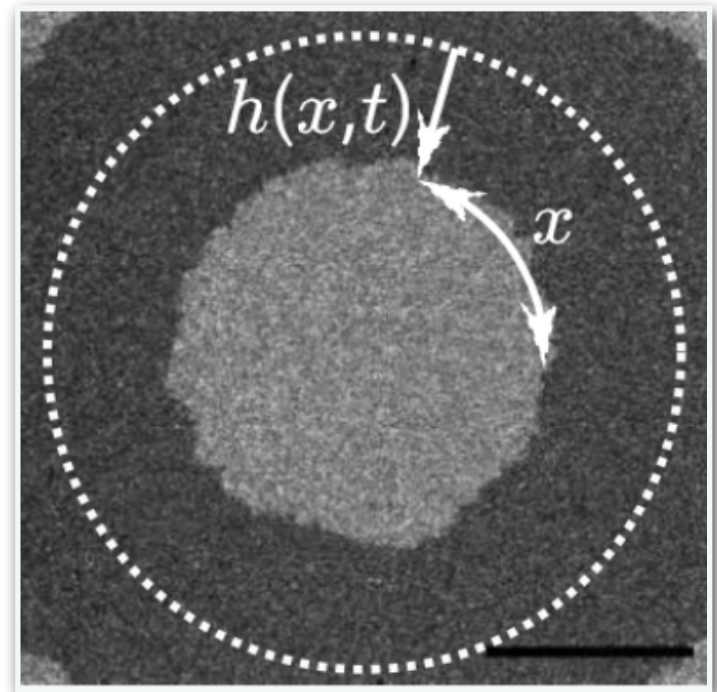


# Growth of Interfaces



Bacterial/Tumor Growth  
(Eden Growth Process)

Liquid Crystals  
Takeuchi PRL 2020

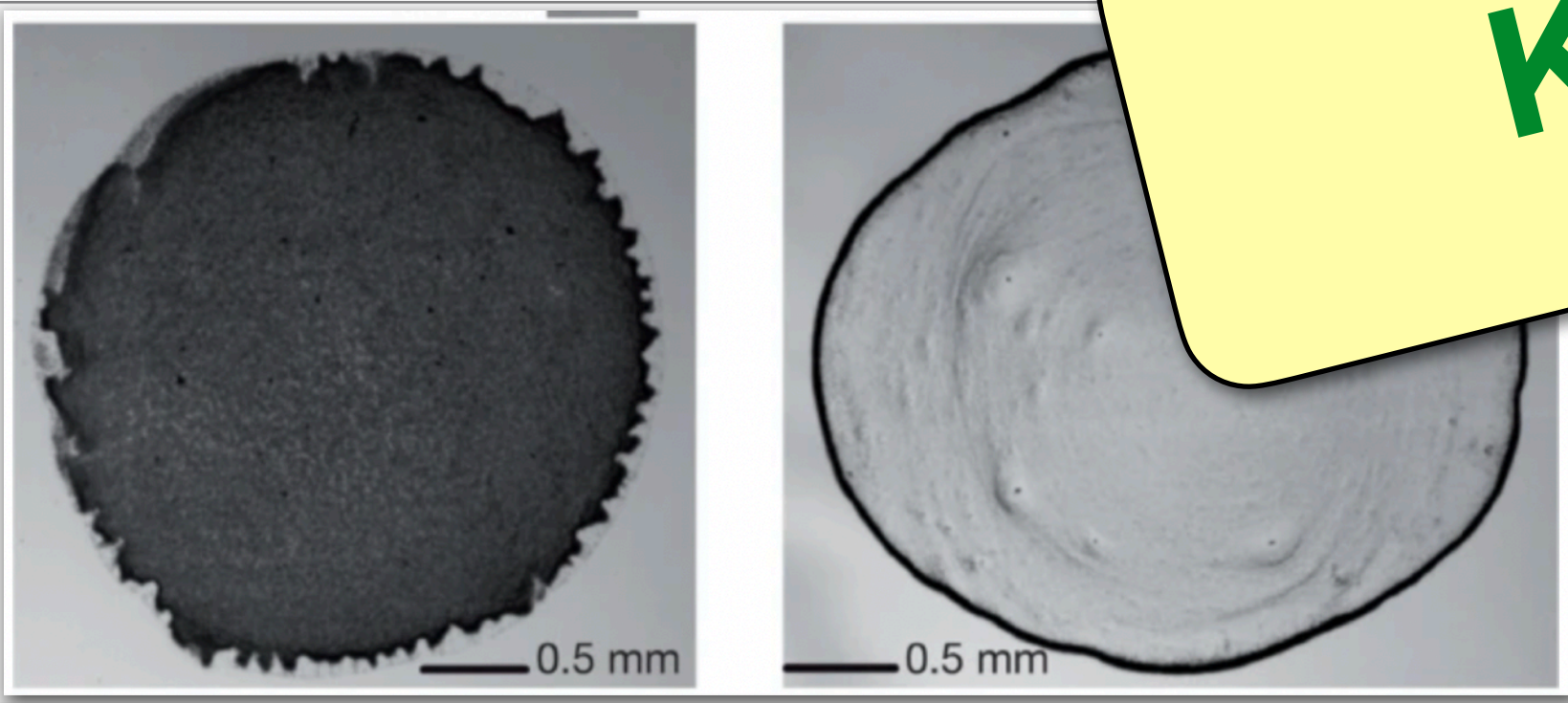


Traffic flow  
de Gier *et al.* PRE 2019

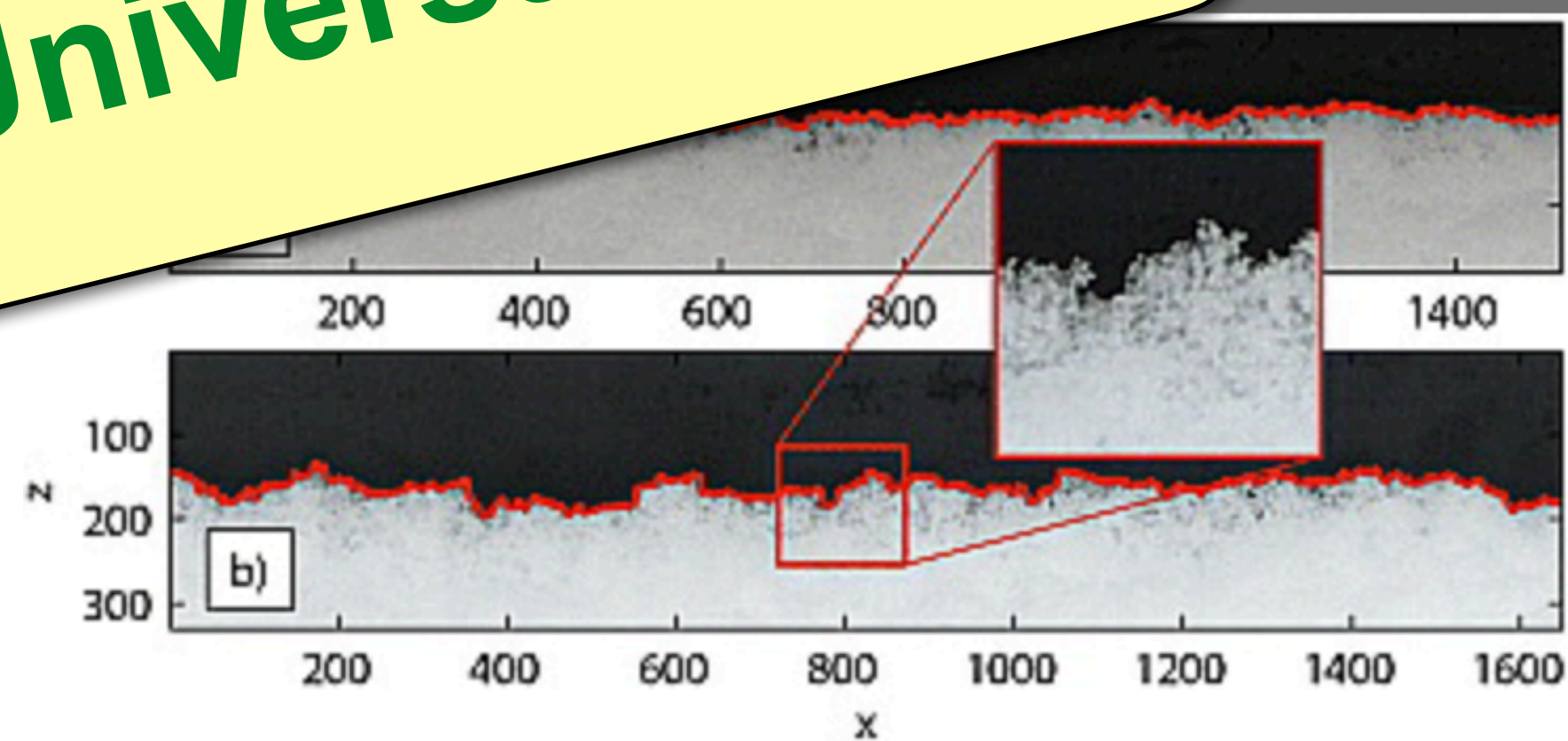


Fire, Forest Fires  
Burning Paper

**KPZ Universality!**



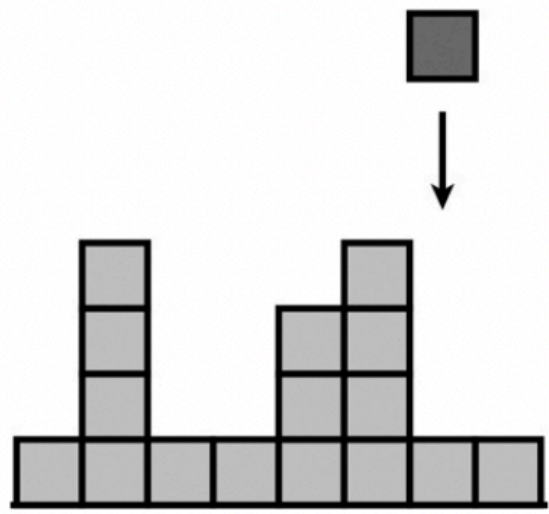
Coffee Stains Funker  
Yunker *et al.* Nature 2021



Snow Surfaces

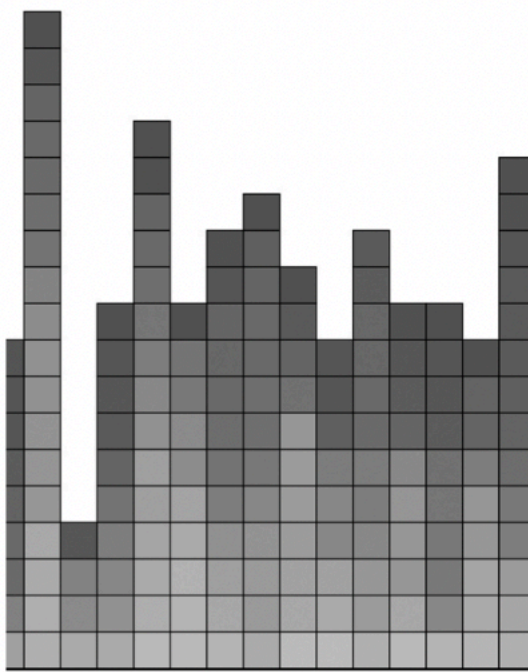


# Growth of Interfaces

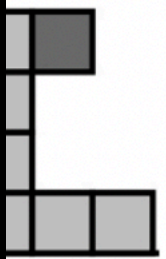


(A)

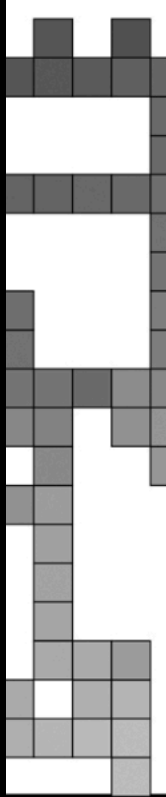
Random Deposition  
(non-sticky)



Random Deposition  
(non-sticky,  $\tau=1$ )



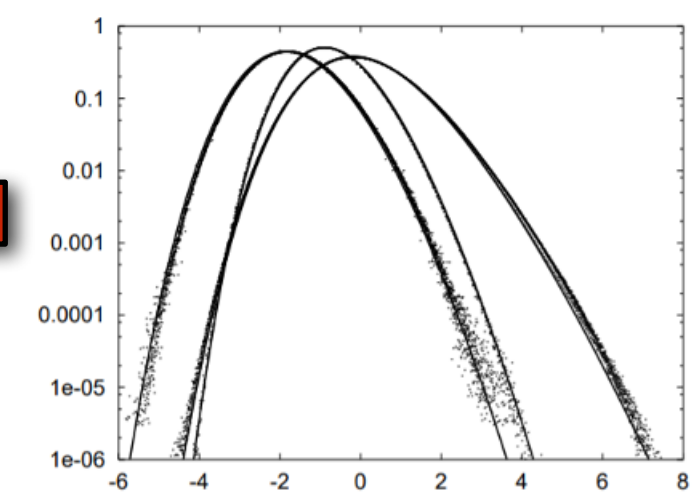
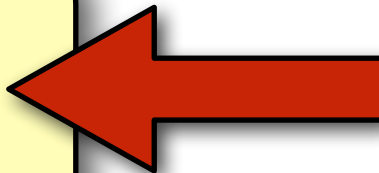
on



on

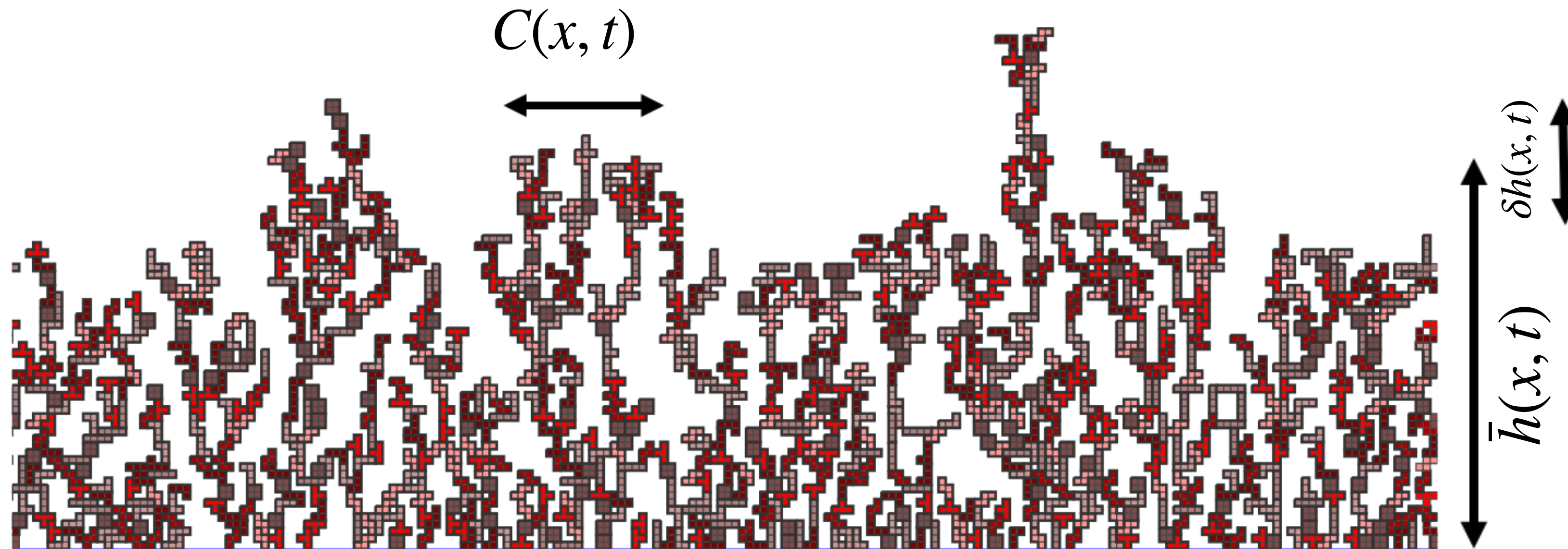
(Sticky Tetras)

$$h(x, t) \simeq v_\infty t + At^{1/3} \chi(X, t)$$



## KPZ Universality Class

- $t^{1/3}$  height fluctuation with **GOE/GUE Tracy-Widom Limit**
- $t^{2/3}$  transv. spatial correlations



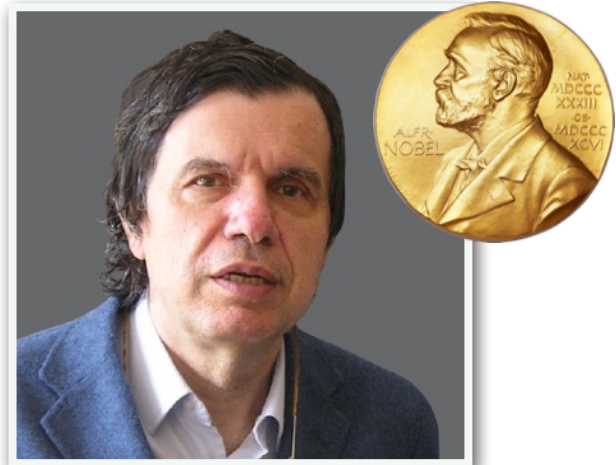
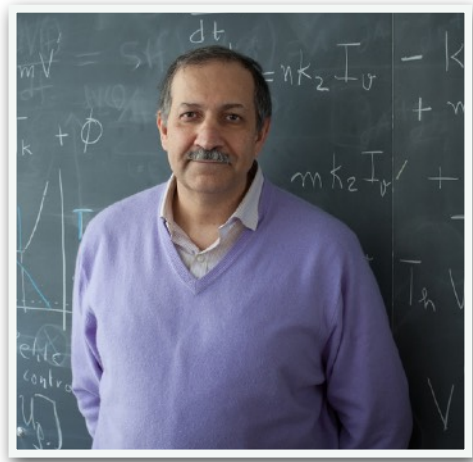
$$\begin{aligned} \delta h &\propto t^\beta & \beta &= 1/3 \\ \xi &\propto t^{1/z} & z &= 3/2 \end{aligned}$$

I. Corwin, Notices of the AMS **63**, 230 (2016)

K. Takeuchi Physica A **504**, 77 (2018)







Martin Hairer  
Fields Medal  
(2014)



# Kardar-Parisi-Zhang Equation

$$\frac{\partial h(\vec{x}, t)}{\partial t} = \nu \nabla^2 h + \frac{\lambda}{2} (\nabla h)^2 + \eta(\vec{x}, t)$$

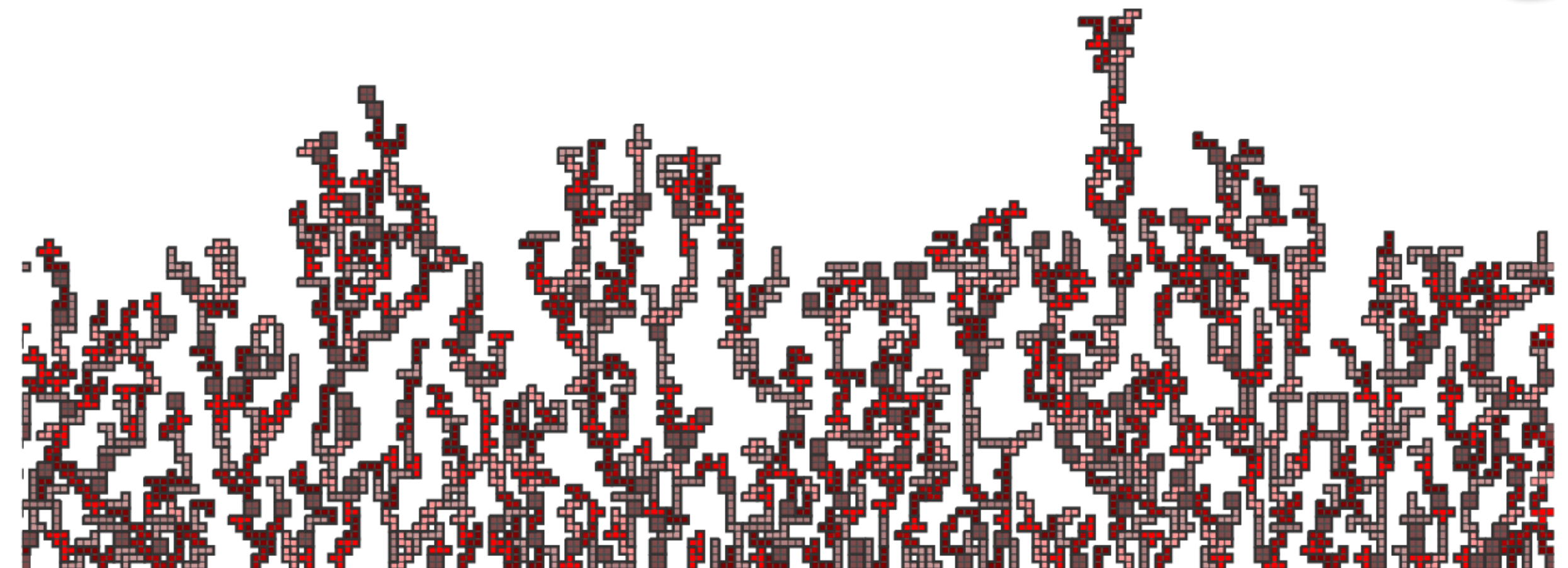
Non-linear stochastic differential equation describing **temporal change of height field**

M. Kardar, G. Parisi & Y.-C. Zhang PRL **56**, 889 (1986)

C.A. Tracy & H. Widom Comm. Math. Phys. **159**, 151 (1994)

C.A. Tracy & H. Widom Comm. Math. Phys. **177**, 727 (1994)

M. Prähofer & H. Spohn PRL **84**, 4882 (2000)



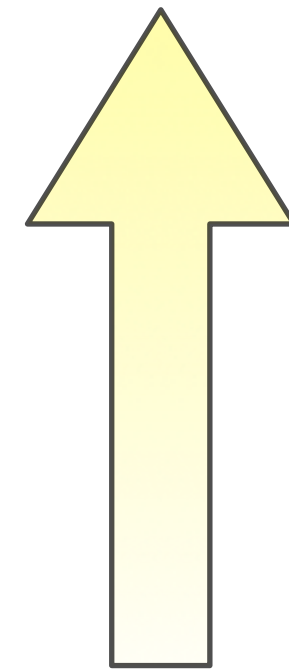
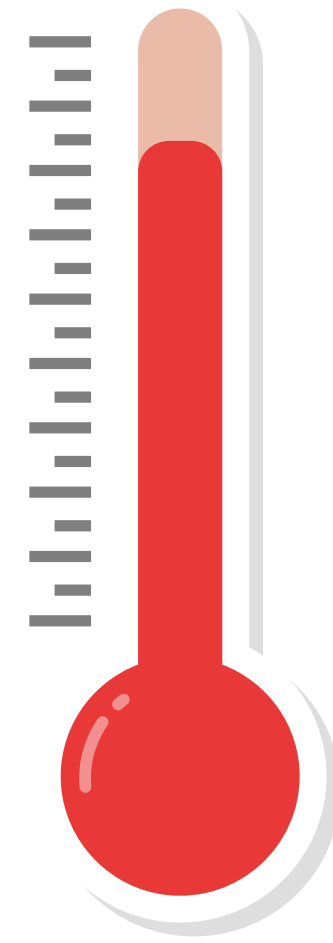
**Growth of interfaces/surface growth**

I. Corwin, Notices of the AMS **63**, 230 (2016)

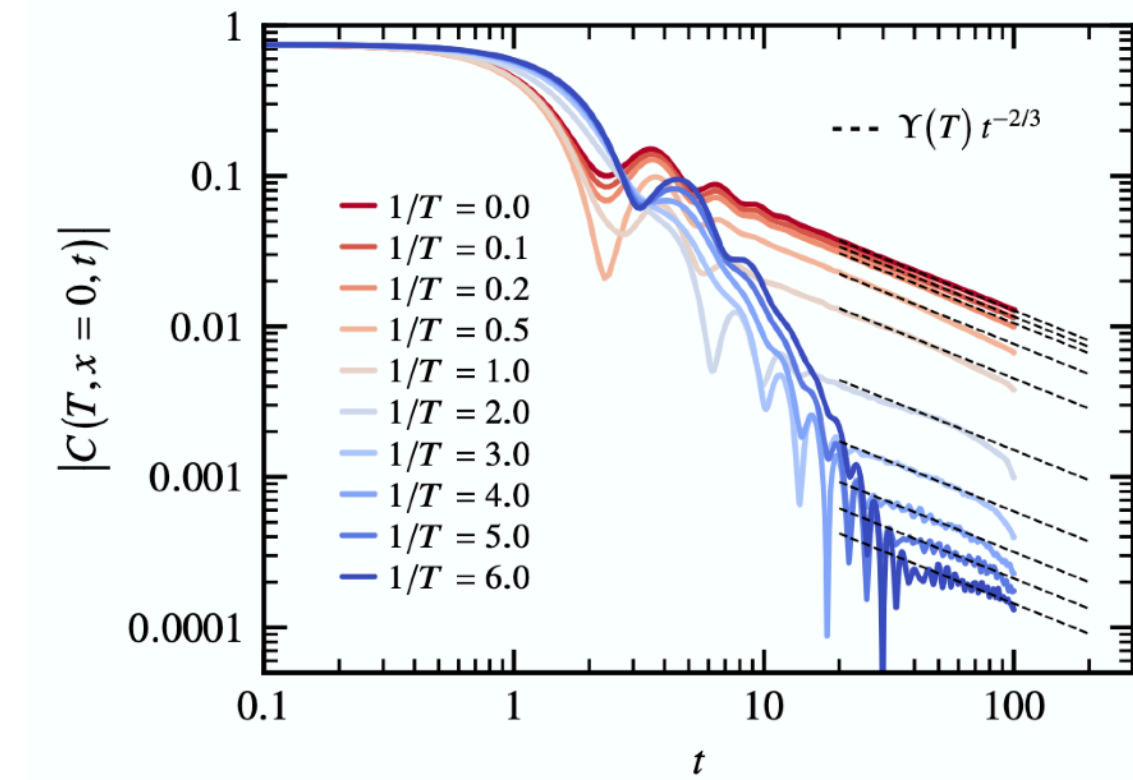
$$\hat{S}^z(x, t) \sim \partial_x h(x, t)$$

**KPZ Universality**

**High (Infinite) T  
Low-q, Long Times**

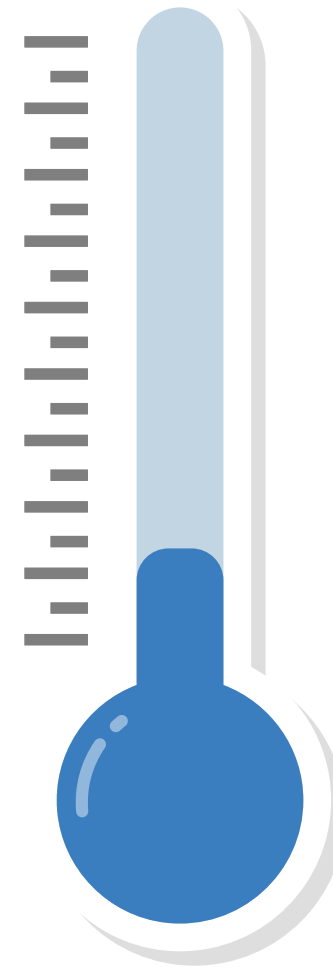


**Crossover**  
M. Dupont, N.E. Sherman &  
J.E. Moore PRL 2021



**Tomanaga-Luttinger  
Liquid**

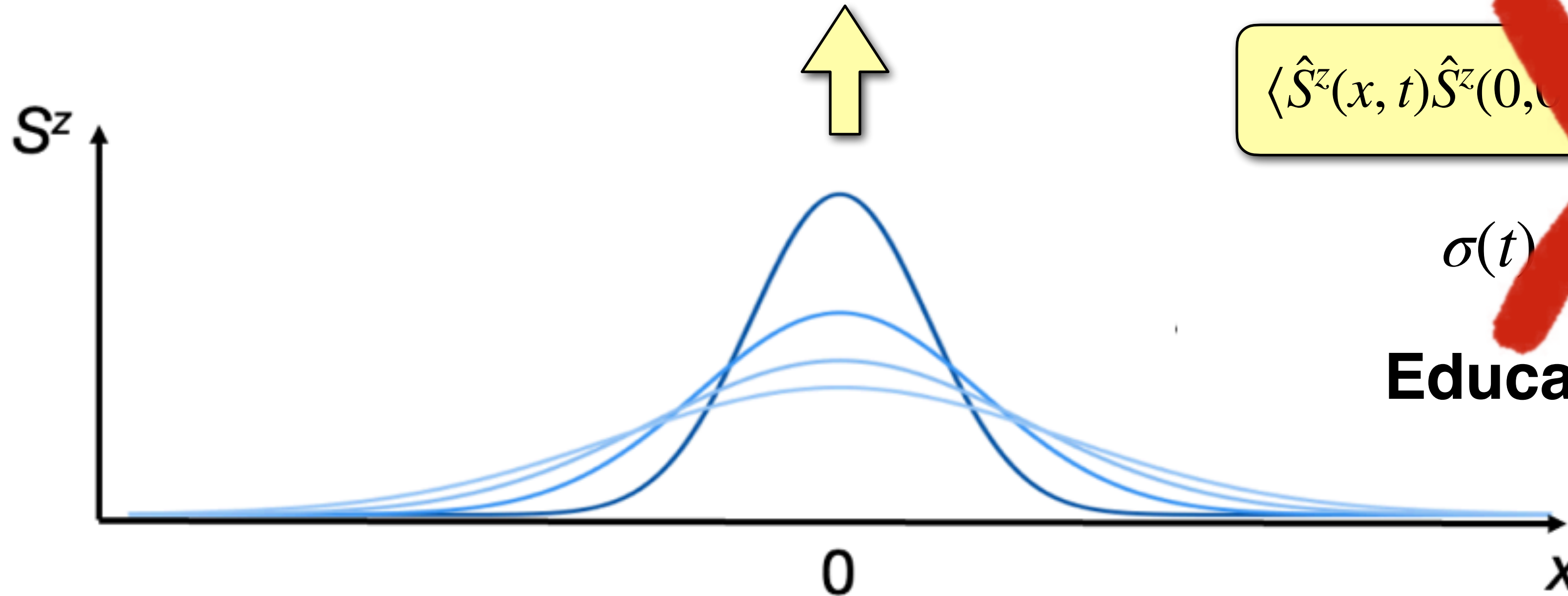
**Low T  
High-q (Spinons)**





# Infinite T Heisenberg Dynamics

How does a **single spin** spread in this environment?



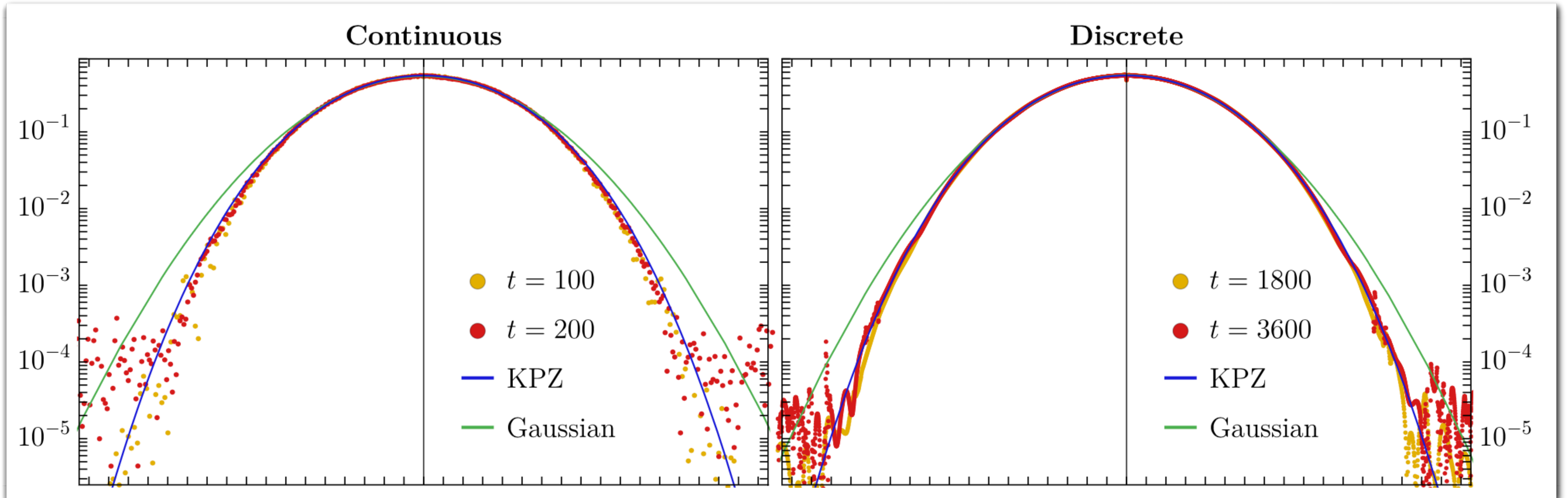
~~$\langle \hat{S}^z(x, t) \hat{S}^z(0, 0) \rangle \sim f_{Gauss}(x/t^{1/2})$~~

~~$\sigma(t) \sim t^{1/2}$~~

**Educated Guess !**



# Numerical Evidence - Infinite T Heisenberg Dynamics



M. Ljubotina *et al.*, Nature Comm. (2017)

M. Ljubotina *et al.*, Phys. Rev. Lett. (2019)

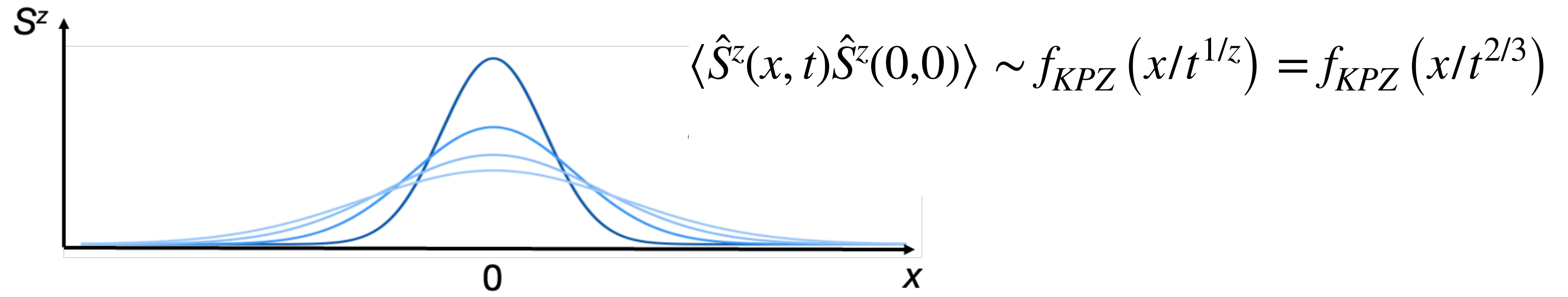
Review: see V. Bulchadini, S. Gopalakrishnan, E. Ilievski

J. Stat. Mech. 084001 (2021)

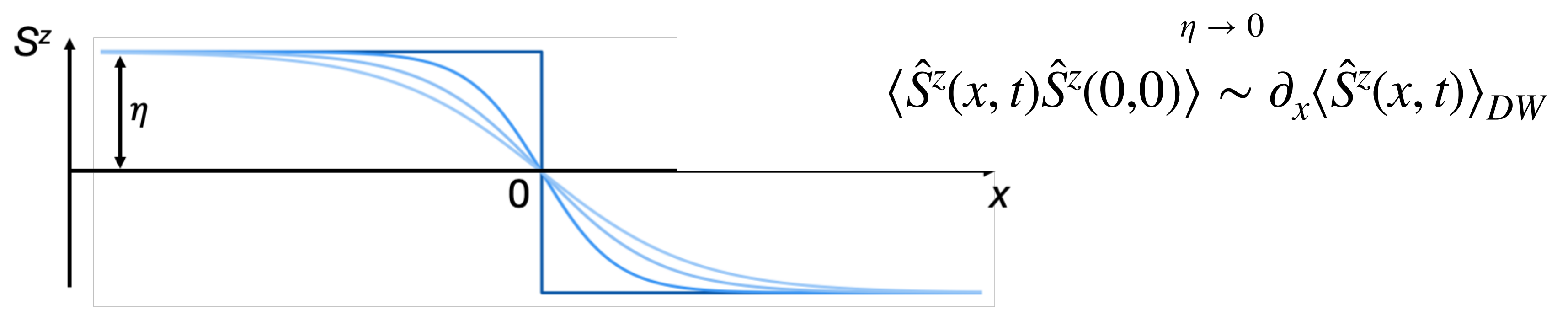


**Tomaž Prosen**  
Ljubljana

# Numerical Evidence - Infinite T Heisenberg Dynamics



Consider **spin domain wall** at  $T \rightarrow \infty$

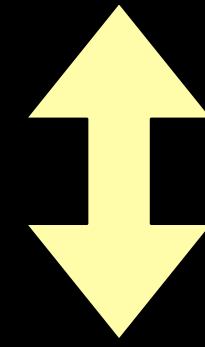


M. Ljubotina *et al.*, Nature Comm. (2017)  
 M. Ljubotina *et al.*, Phys. Rev. Lett. (2019)  
**Review:** see V. Bulchadini, S. Gopalakrishnan, E. Ilievski  
 J. Stat. Mech. 084001 (2021)

**Anomalous Transport!**

# Connecting Spin Transport Hydrodynamics to KPZ Equation

Quantum Numerics  $\langle \hat{S}^z(x, t) \hat{S}^z(0, 0) \rangle \sim f_{KPZ}(x/t^{1/z})$



## Solutions of KPZ Equation

Spatio-Temporal Correlations of Height Field

$$C(x, t) = \langle [h(x, t) - h(0, 0) - t \langle \partial_t h \rangle]^2 \rangle$$

Slope Correlations of Height Field

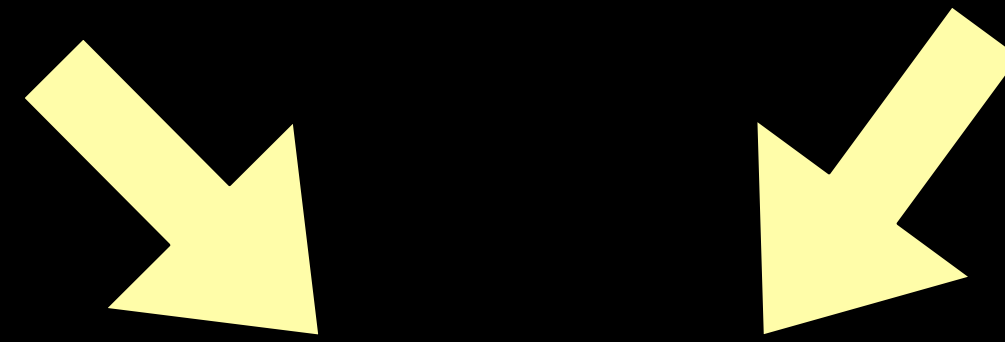
$$\langle \partial_x h(x, t) \partial_x h(0, 0) \rangle \sim \partial_x^2 C(x, t) \sim f_{KPZ}(x/t^{1/z})$$



# Conjecture

$$\langle \hat{S}^z(x, t) \hat{S}^z(0, 0) \rangle \sim f_{KPZ}(x/t^{1/z})$$

$$\langle \partial_x h(x, t) \partial_x h(0, 0) \rangle \sim f_{KPZ}(x/t^{1/z})$$



$$\hat{S}^z(x, t) \sim \partial_x h(x, t)$$

**Magnetization Profile**

$$\hat{P}(t) \sim h(0, t)$$

**Polarization Transfer**

# Consequences / Predictions

**Magnetisation Profile**

KPZ scaling function  $f_{KPZ}(x/t^{2/3})$

**Polarisation Transfer (Domain Wall)**

$$\langle \hat{P}(t) \rangle \propto t^{1/z} = t^{2/3}$$

$$z = 3/2$$

**Dynamical exponent**

**Fluctuations (Time)**

$$\delta P(t) = \delta h = At^{1/3} \chi(0,t) = A t^\beta \chi(0,t)$$

$$\beta = 1/3$$

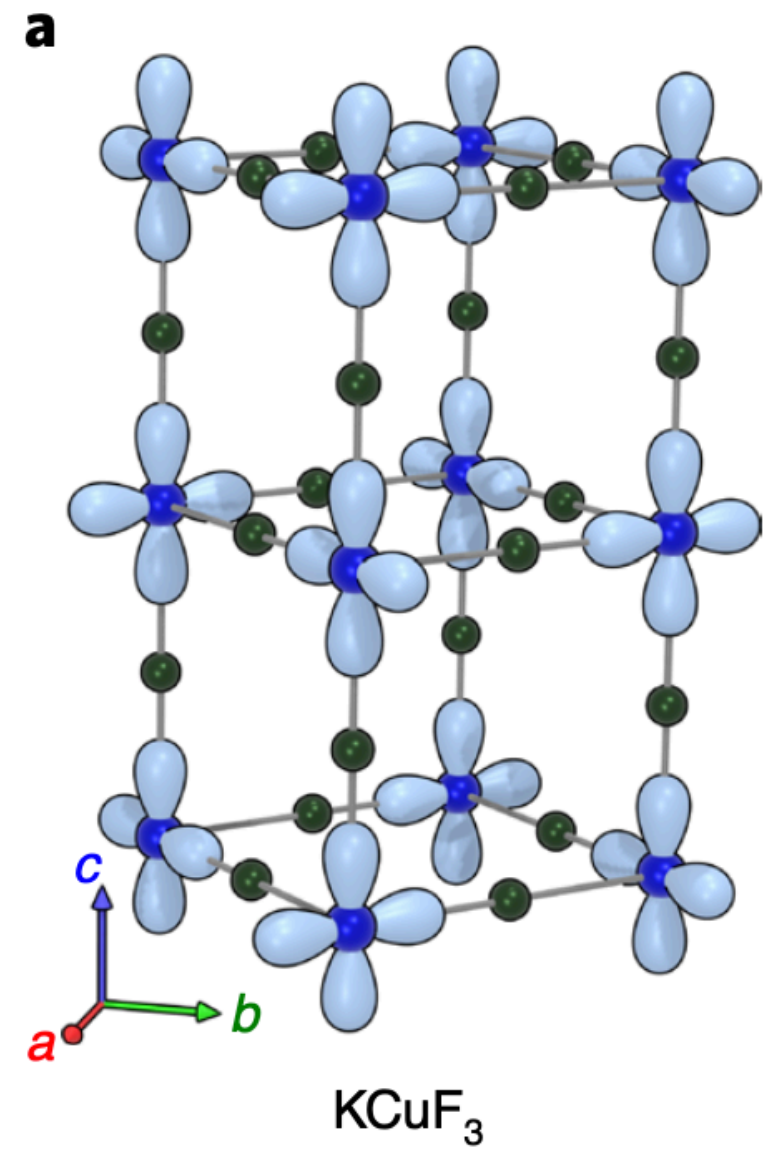
**Fluctuations**

**Tracy-Widom Distribution function**

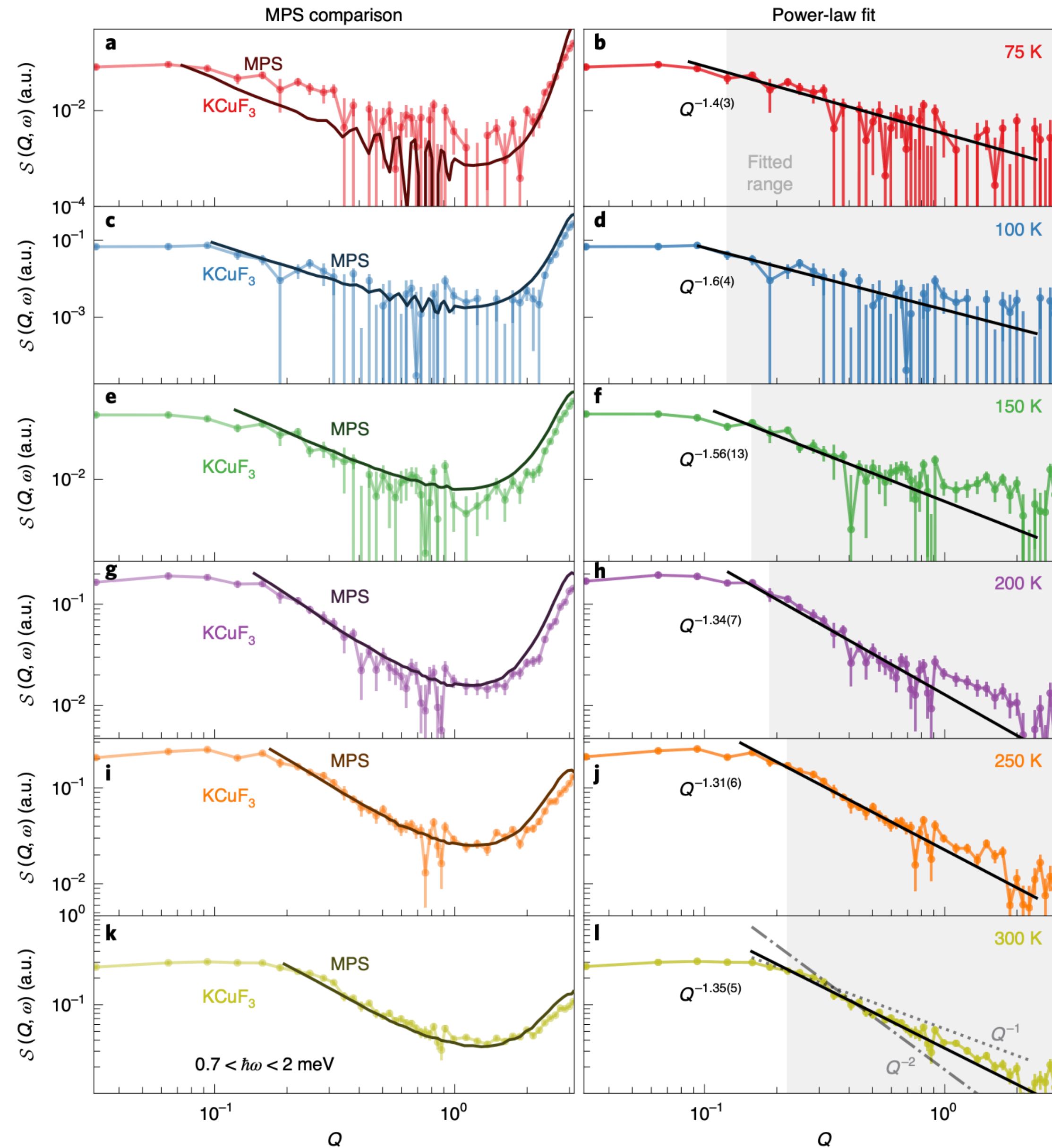




# Superdiffusive Transport in Spin Chains - Neutron Scattering



A. Scheie *et al.*  
 Nature Phys. **17**,  
 726–730 (2021)



Dynamical Structure Factor

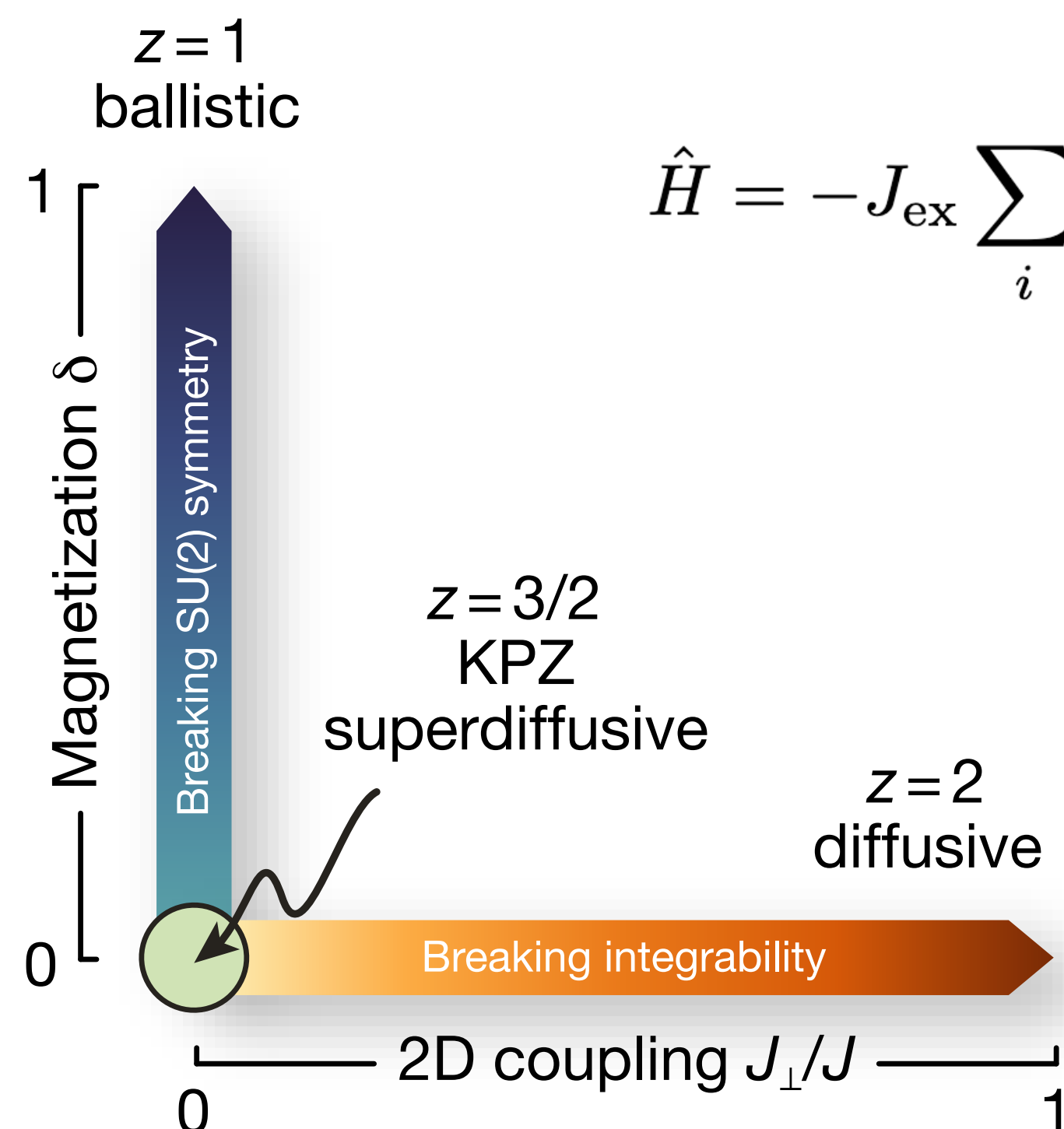
$$S(Q, \omega \rightarrow 0) \approx Q^{-z}$$

@ 300K

$$z = 1.35(5)$$



Alan Tennant,  
 Oak Ridge National Lab



$$\hat{H} = -J_{\text{ex}} \sum_i \left( \hat{S}_i^x \hat{S}_{i+1}^x + \hat{S}_i^y \hat{S}_{i+1}^y + \Delta \hat{S}_i^z \hat{S}_{i+1}^z \right)$$

Here:  $\Delta = 1$

## Space time scaling

$$x \sim t^{1/z}$$

- $z=1$  ballistic
- $1 < z < 2$  superdiffusive
- $z=2$  diffusive

## Numerical Evidence:

- M. Ljubotina *et al.*, Nature Comm. (2017)
- M. Ljubotina *et al.*, Phys. Rev. Lett. (2019)

## Understanding (generalised GHD, SU(2) & Integrability,...)

- S. Gopalakrishnan and R. Vasseur, Phys. Rev. Lett. (2019)
- J. De Nardis, Phys. Rev. Lett. (2019)
- S. Gopalakrishnan, R. Vasseur, and B. Ware, PNAS (2019)
- V. B. Bulchandani, Phys. Rev. B (2020)

## Reviews:

- B. Bertini *et al.* Rev. Mod. Phys. (2020)
- V. B. Bulchandani, S. Gopalakrishnan, and E. Ilievski, arXiv:2103.01976

Subtle interplay of **integrability** (stable quasiparticles) & **Non-abelian SU(2) symmetry** in Heisenberg model.

**Exp.:** A. Scheie *et al.* Nature Physics (2021)

**Related:** Transport via Spin-Spirals

S. Hild *et al.* Phys. Rev. Lett. (2014)

P.N. Jepsen *et al.* Nature (2020)



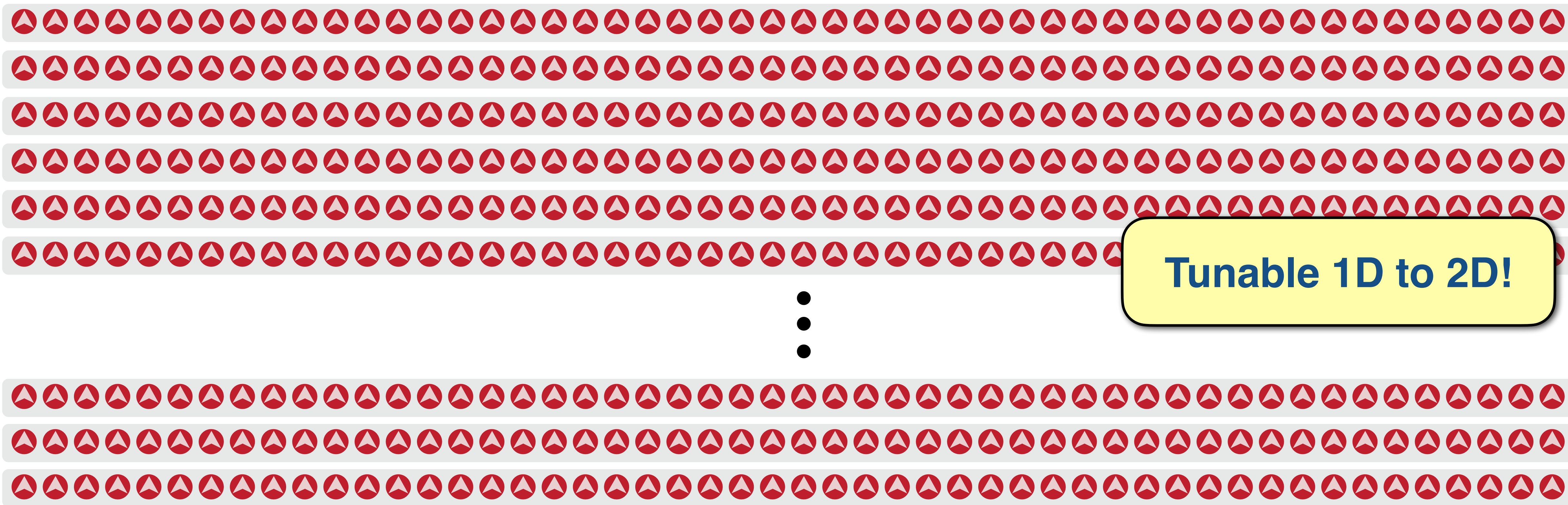


<sup>87</sup>Rb

$$\hat{H} = -J \sum \left( \hat{S}_i^x \hat{S}_{i+1}^x + \hat{S}_i^y \hat{S}_{i+1}^y + S_i^z \hat{S}_{i+1}^z \right)$$

50 spins

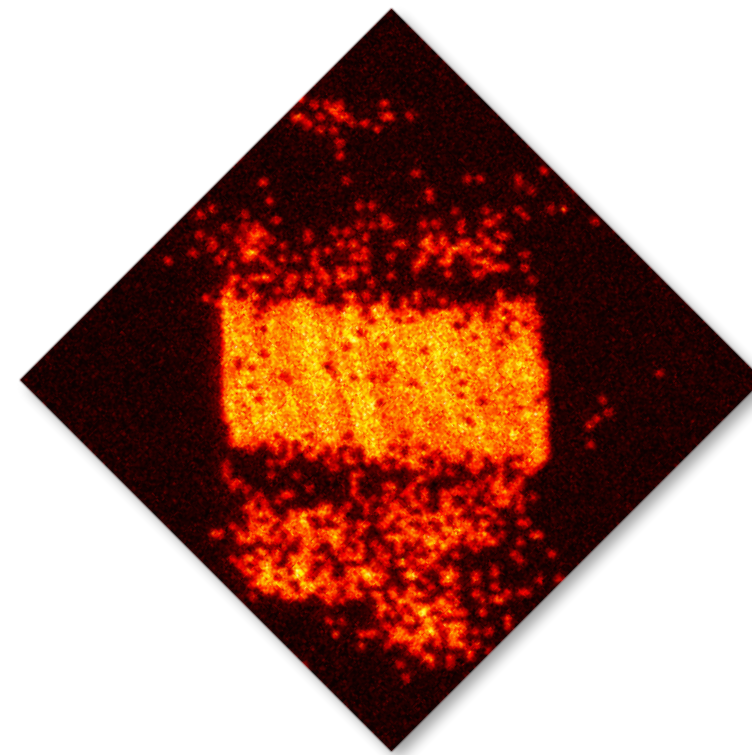
20 rows



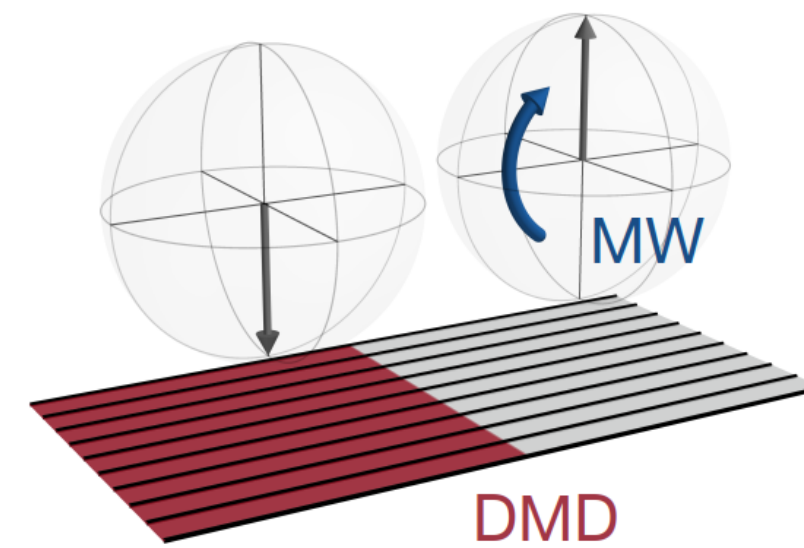
**Tunable 1D to 2D!**



① Mott insulator

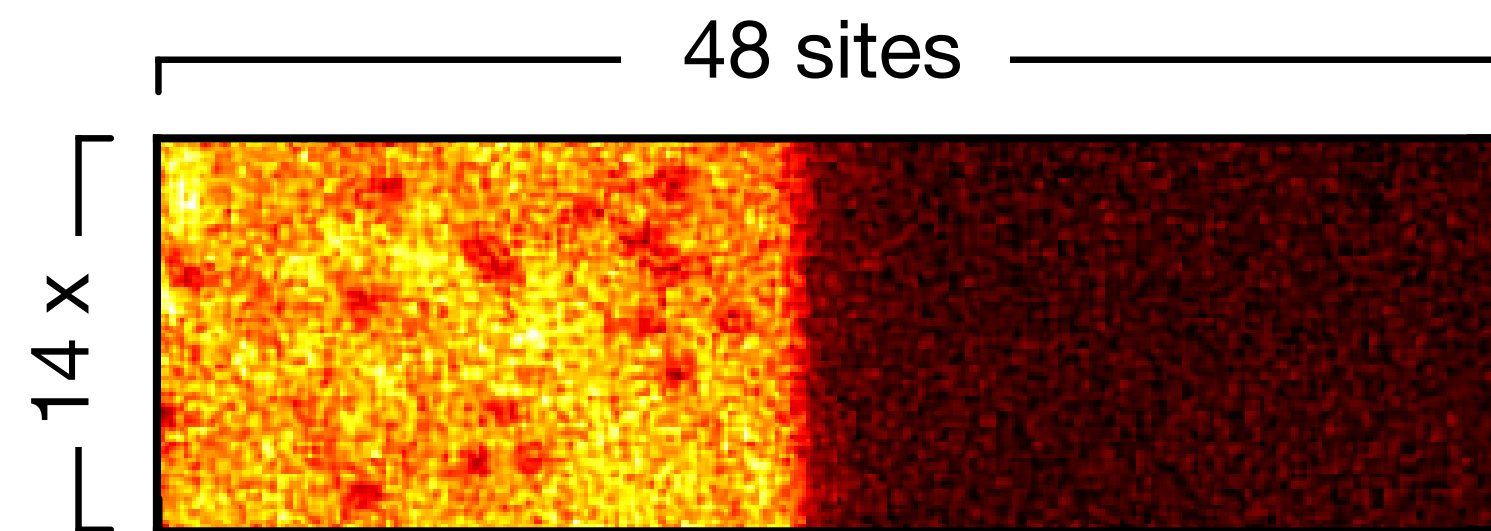


② Spin DW



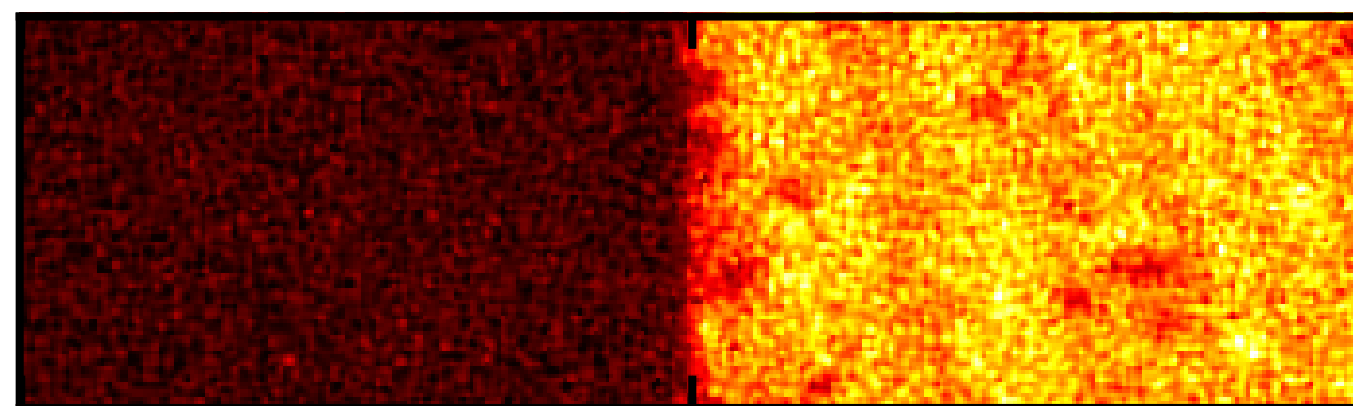


## Single shot images



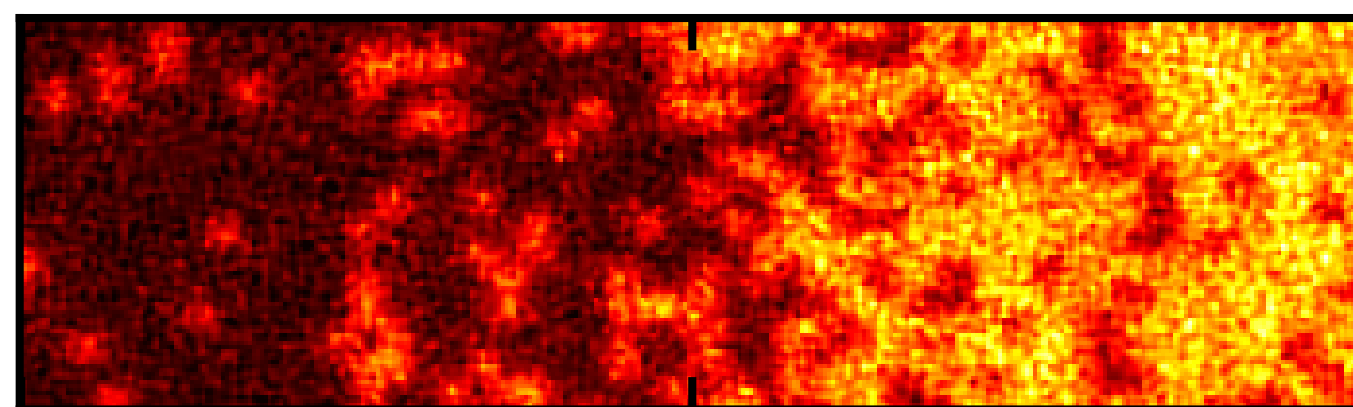
$|\uparrow\rangle$  atoms

$t = 0$



$|\downarrow\rangle$  atoms

$t = 0$



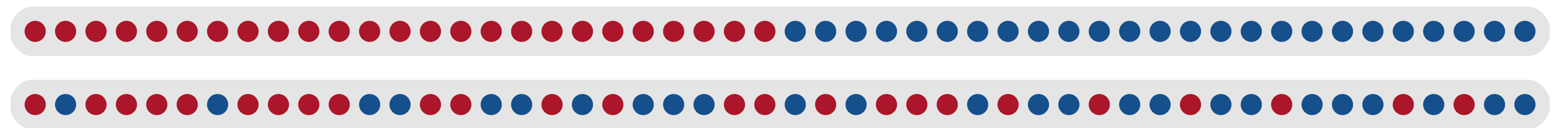
$|\downarrow\rangle$  atoms

$t/\tau = 36$

**Box potential!**  
**No harmonic confinement.**

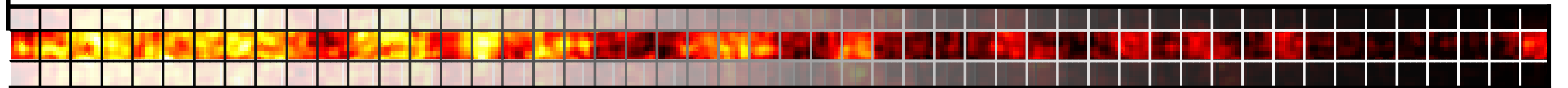
Spin domain wall

$t = 0$



$t/\tau = 36$

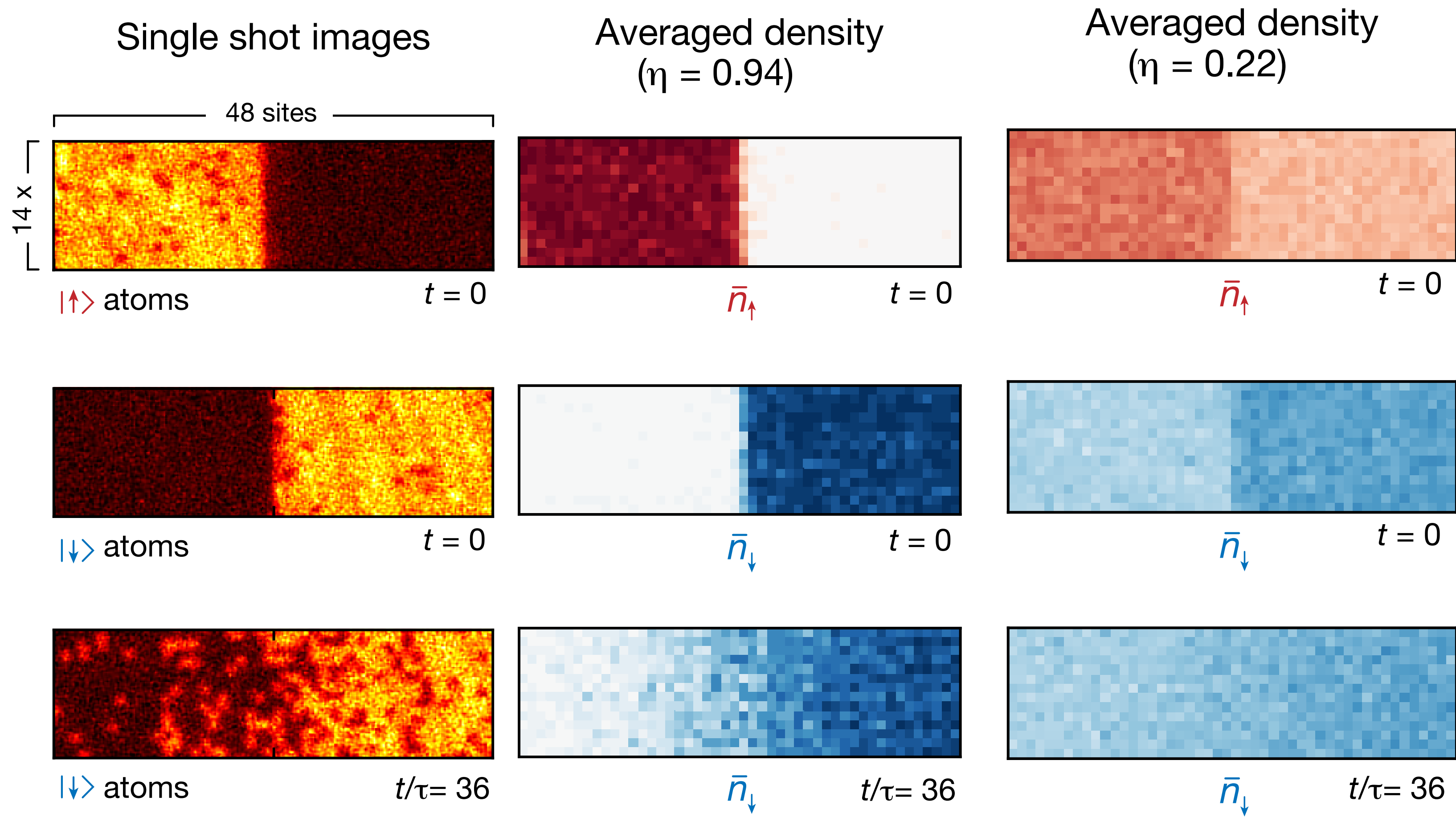
Single shot image of  $|\uparrow\rangle$  atoms



Reconstructed  $|\uparrow\rangle$  occupation

$t/\tau = 36$



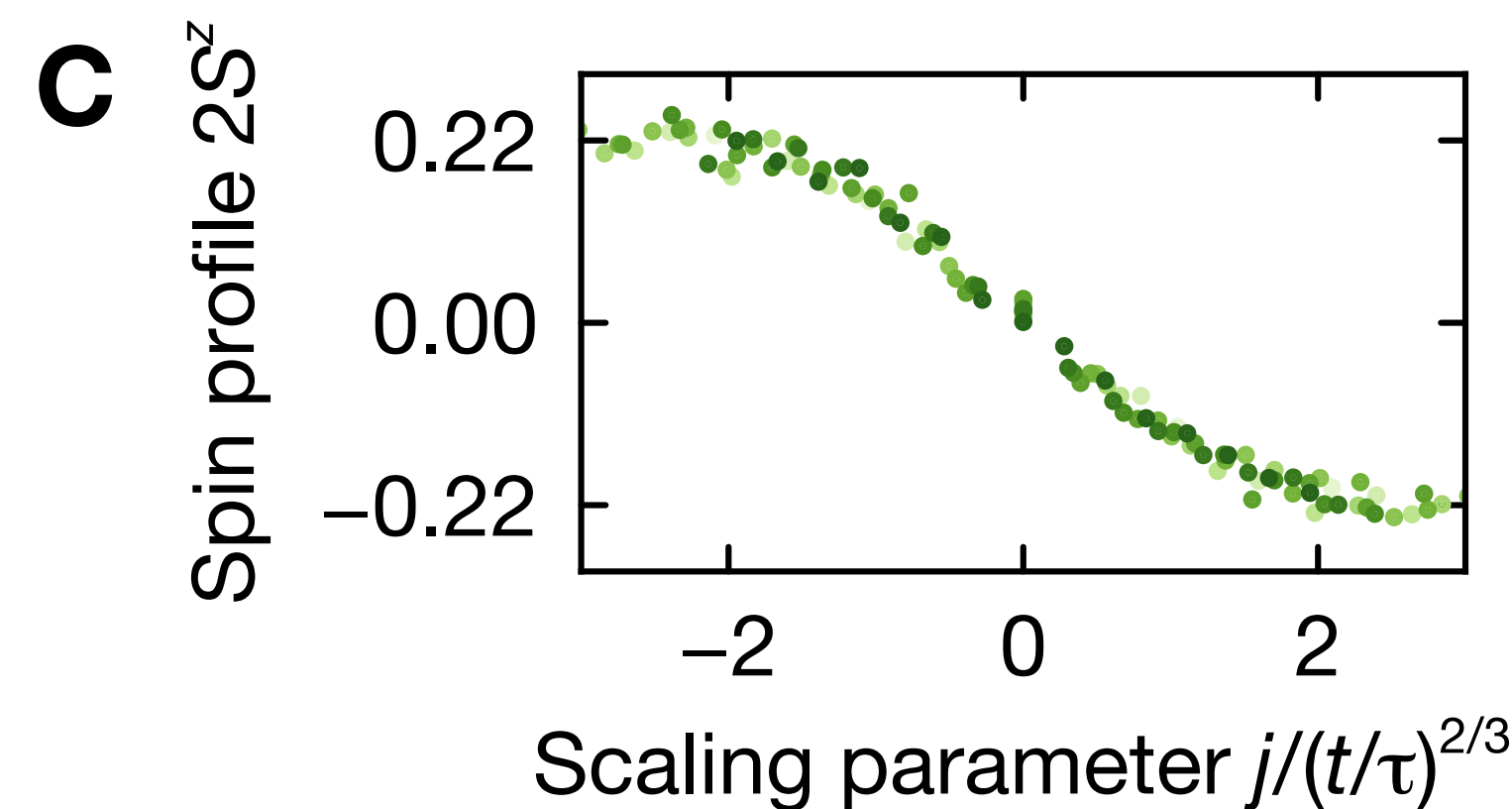
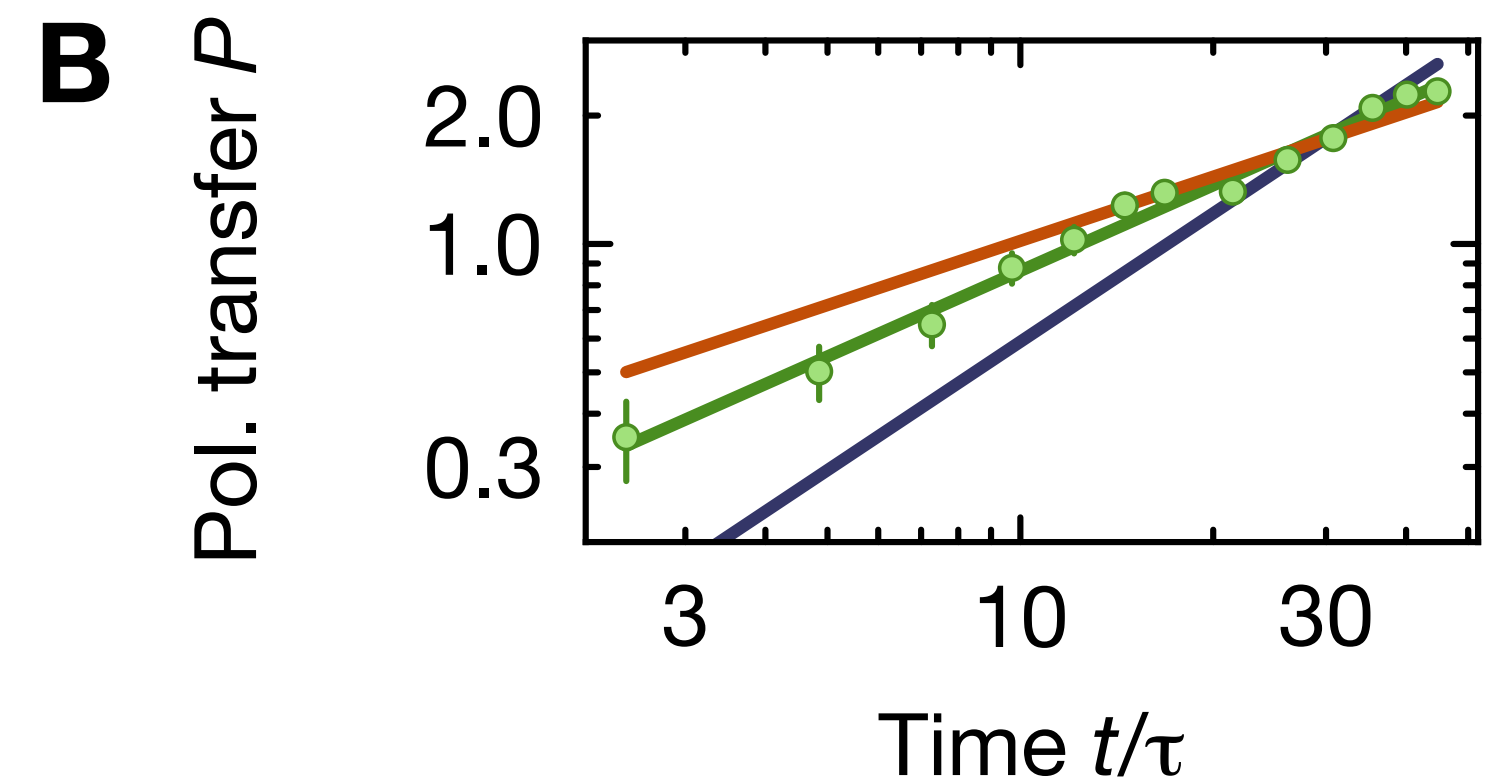
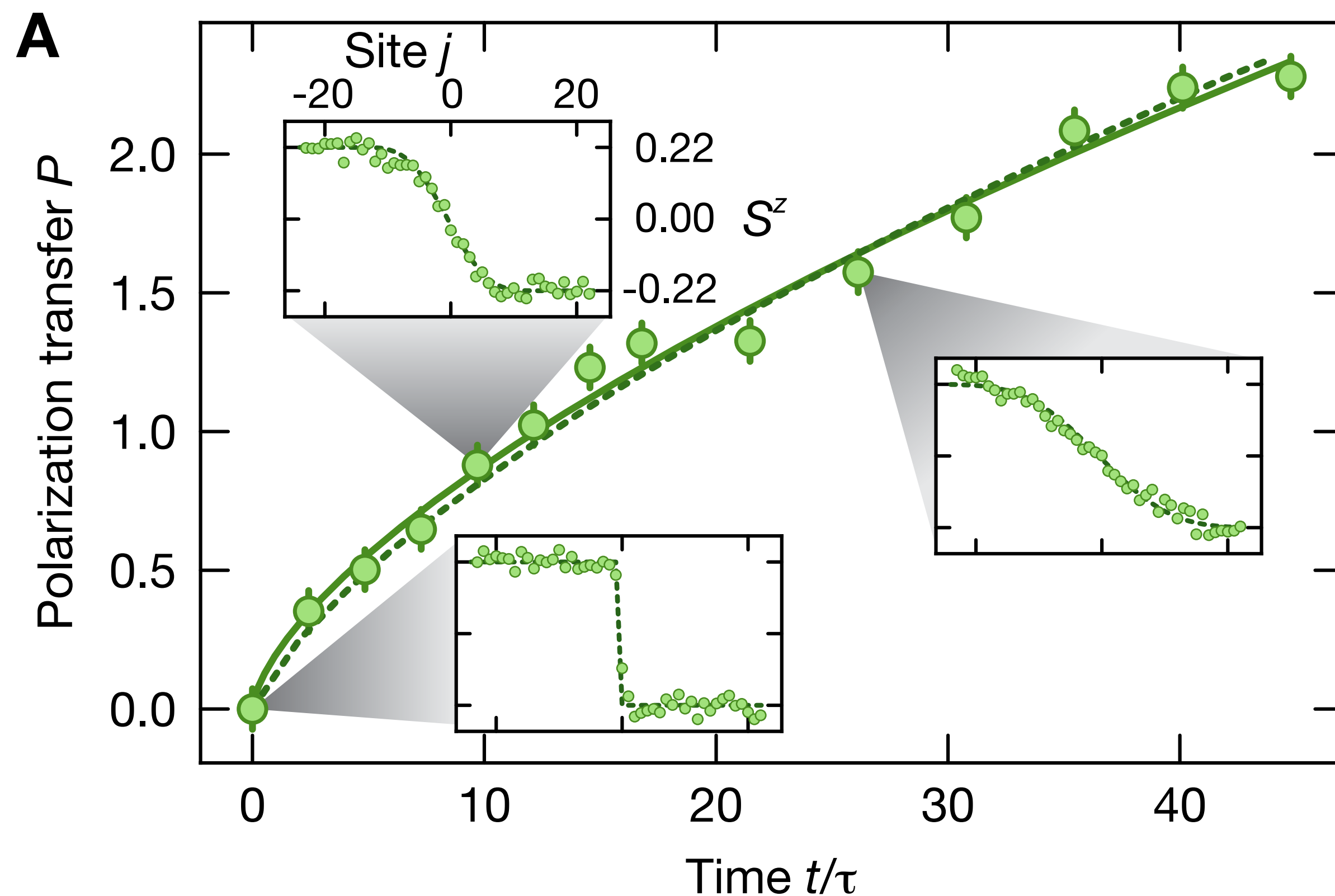


$$\rho \sim (1 + \eta\sigma_z)^{N/2} \otimes (1 - \eta\sigma_z)^{N/2}$$

**High Purity**

**Low Purity**

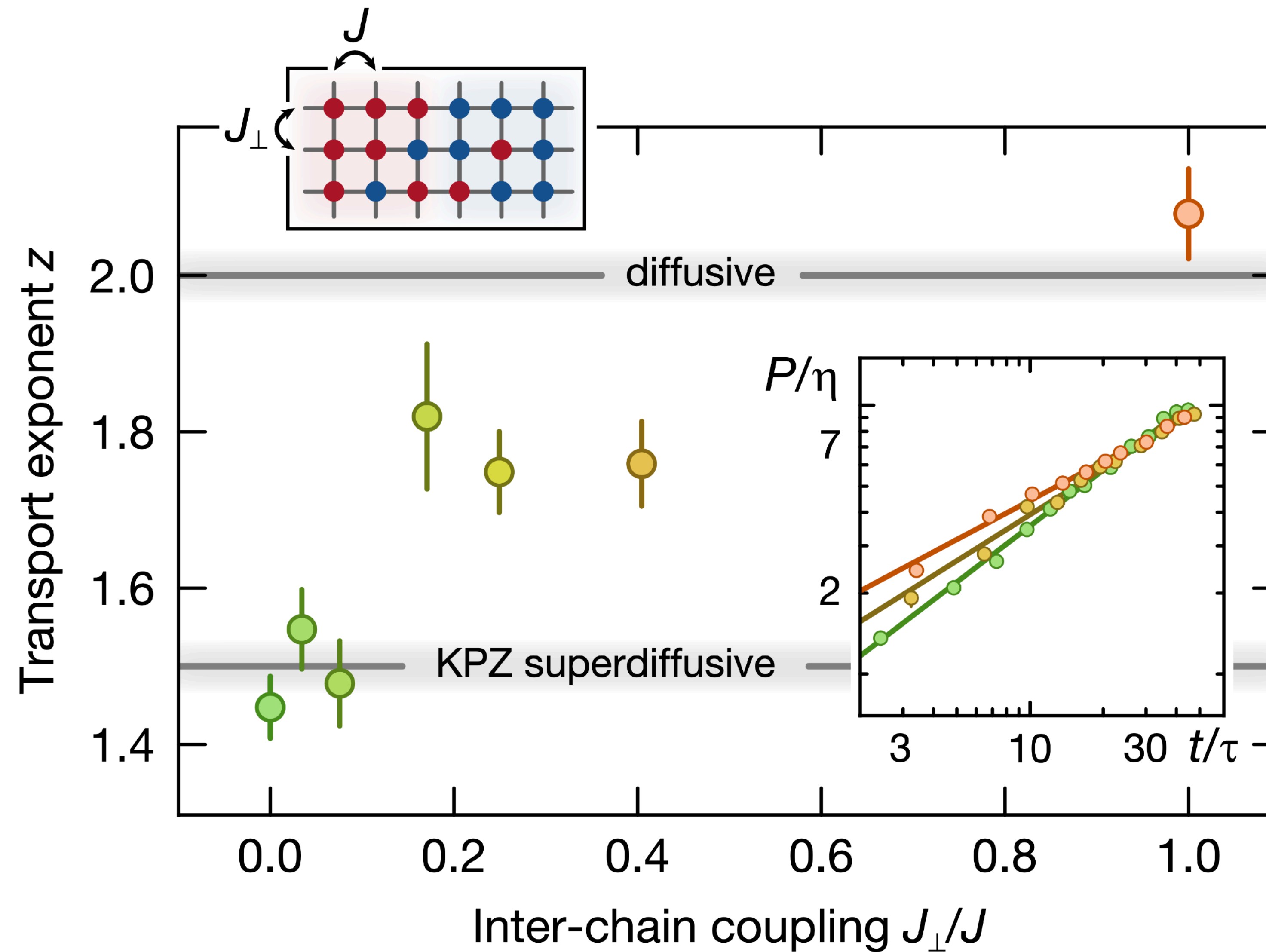




$$P(t) \sim t^{1/z} \quad z_{fit} = 1.54(7)$$

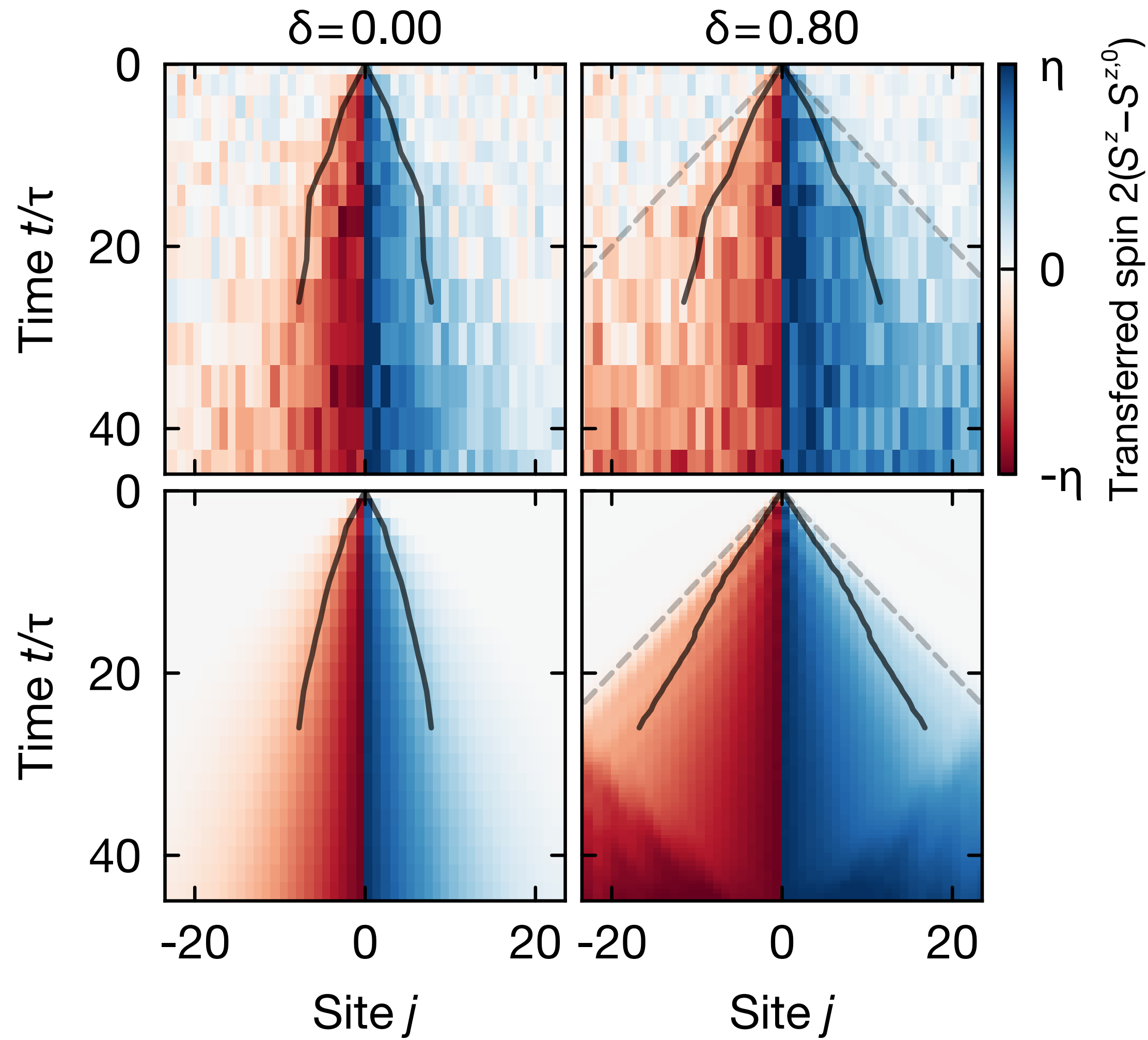
M. Ljubotina *et al.*, *Nature Comm.* (2017).  
 M. Ljubotina *et al.*, *Phys. Rev. Lett.* (2019)  
**Exp. Spin Chains:** A. Scheie *et al.*  
*Nat. Phys.* (2021)



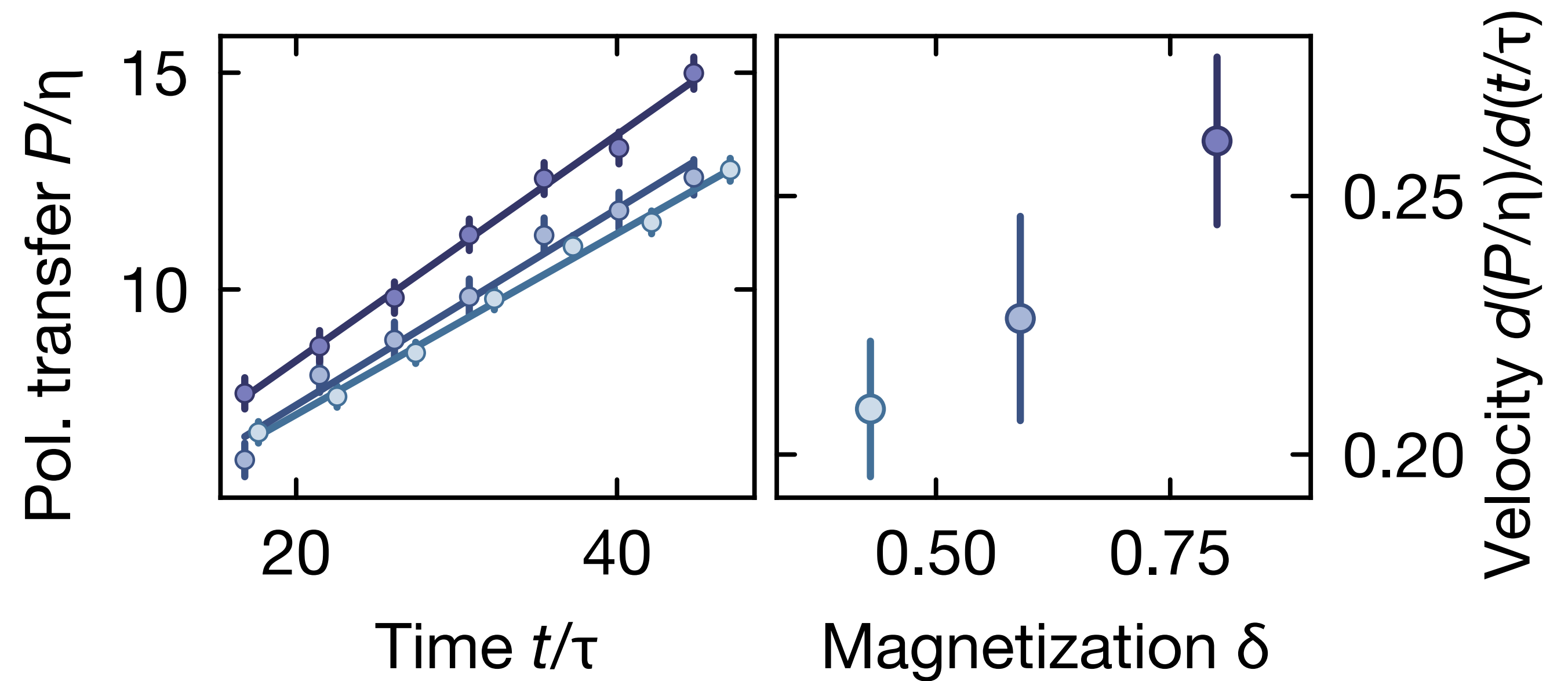


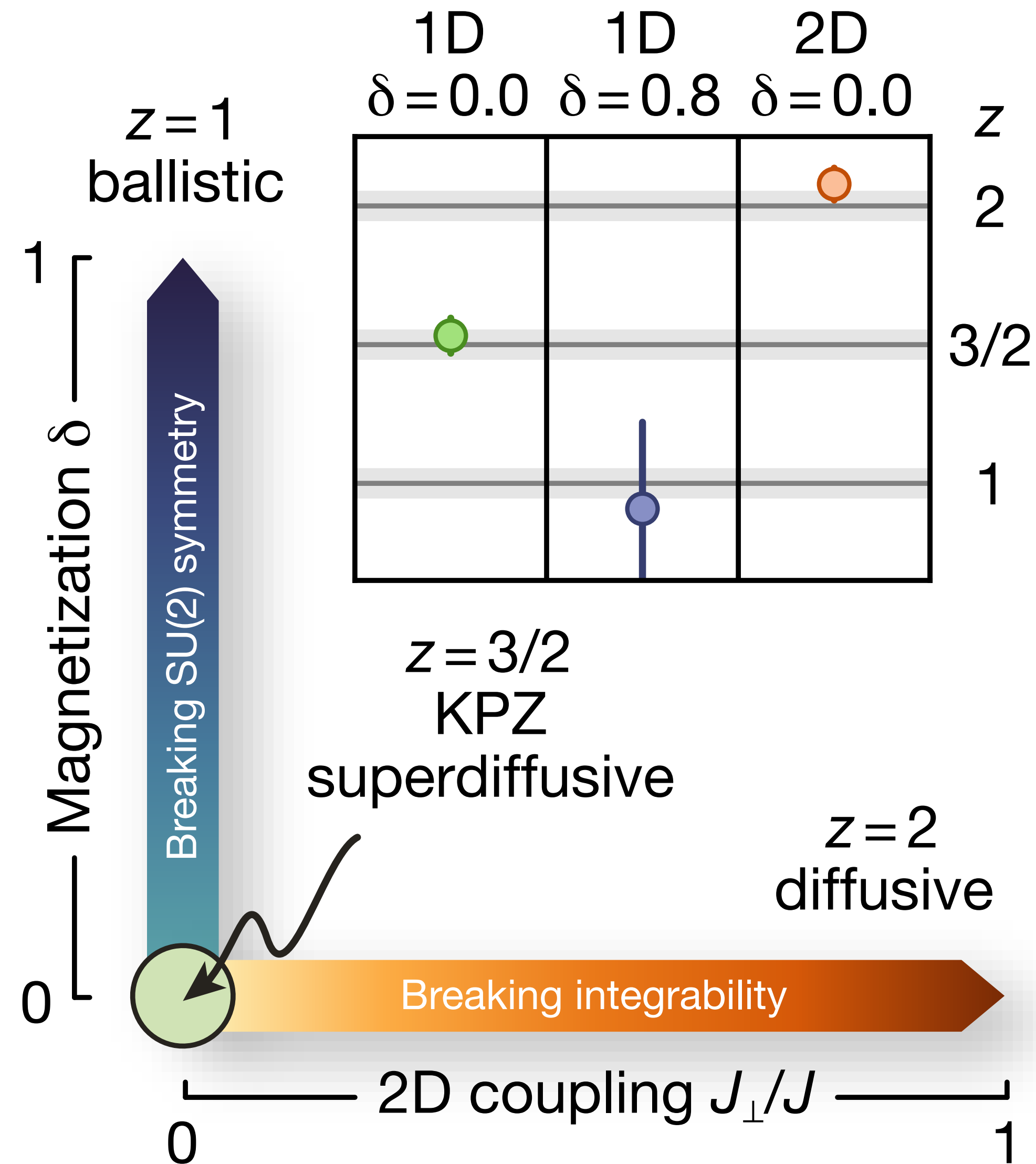


# Breaking Superdiffusion - Breaking Non-Abelian Symmetry



$\delta \neq 0$   
Magnetizing System





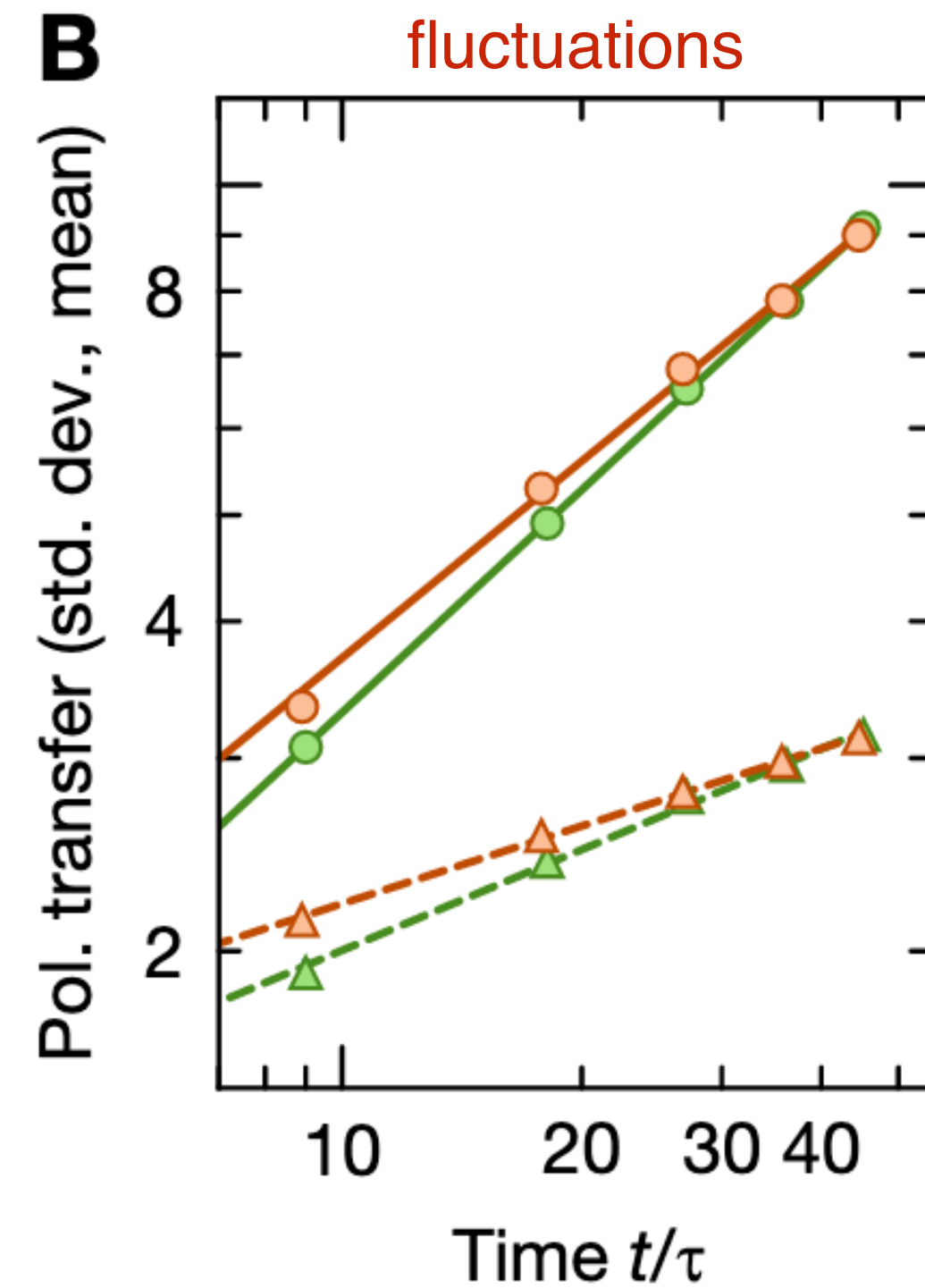
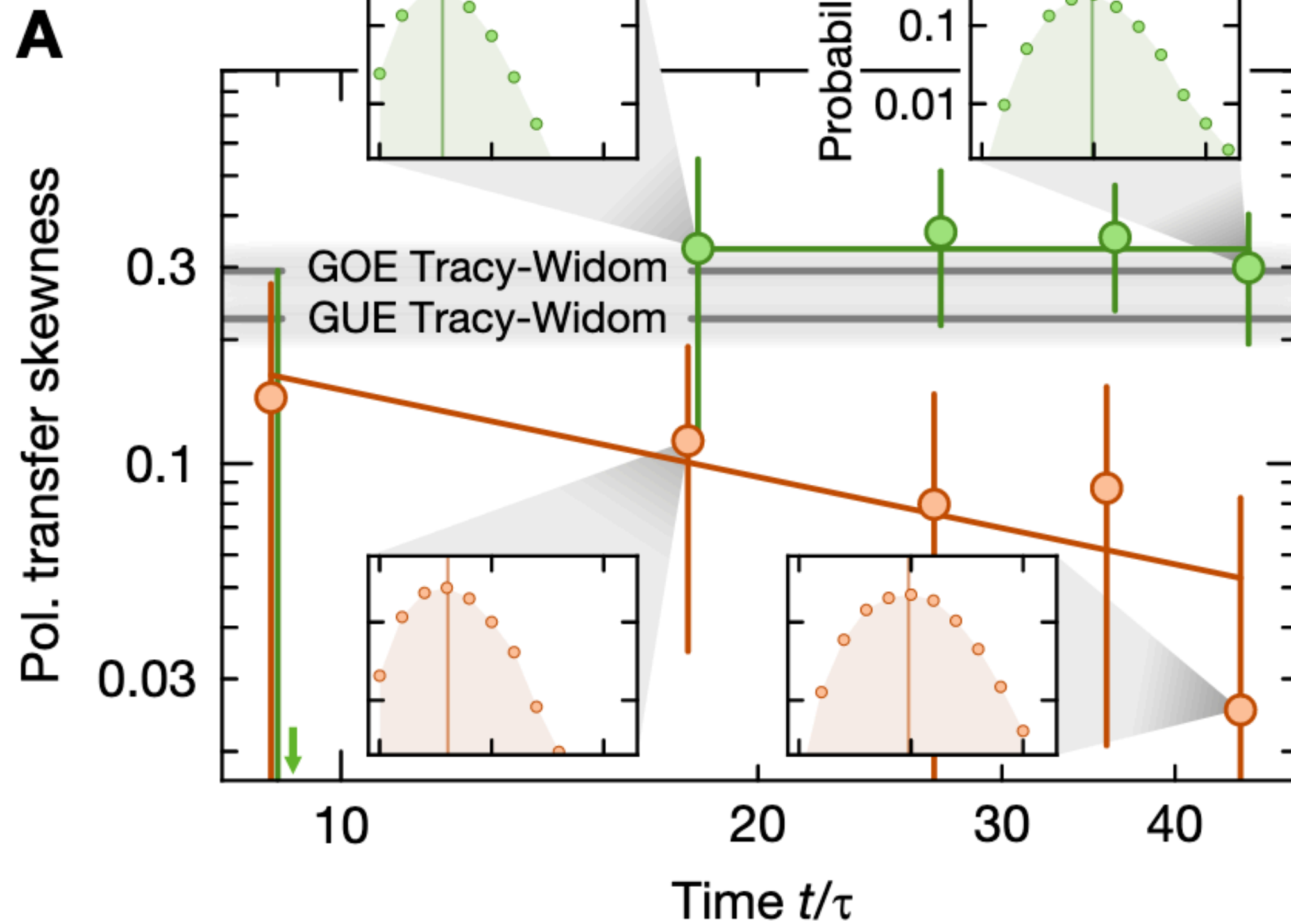


**Polarization transfer**  $\longleftrightarrow$  **height field (at origin) of KPZ equation**

$$\delta h = A t^{1/3} \chi(0,t) = A t^\beta \chi(0,t) \quad \text{Test!}$$

Scale of fluctuations

Tracy-Widom Distribution (non vanishing skewness)



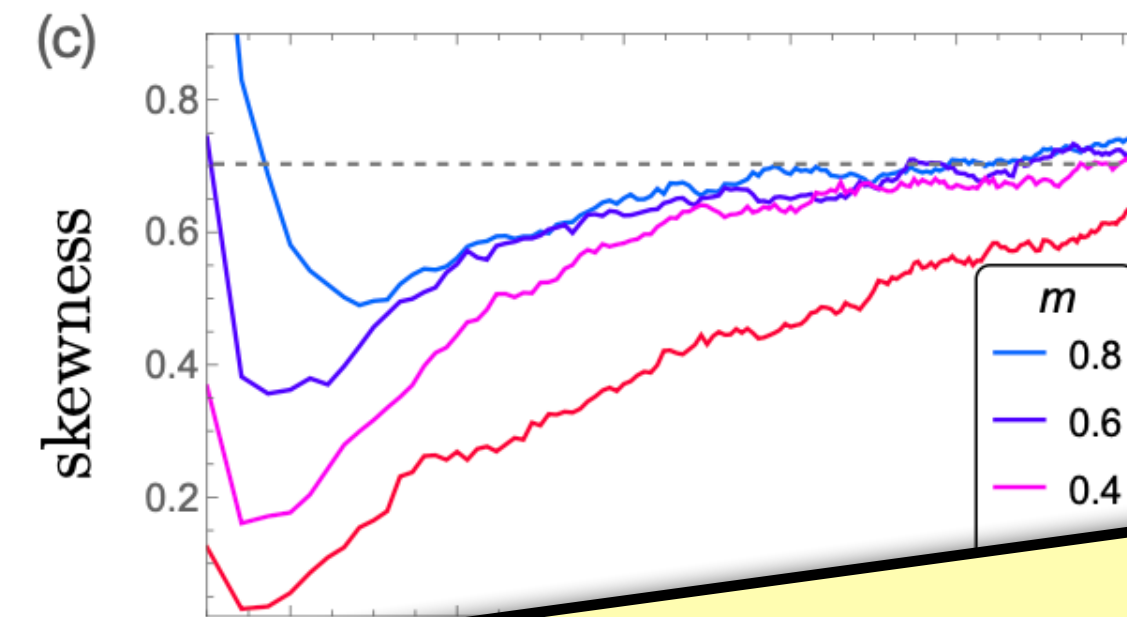
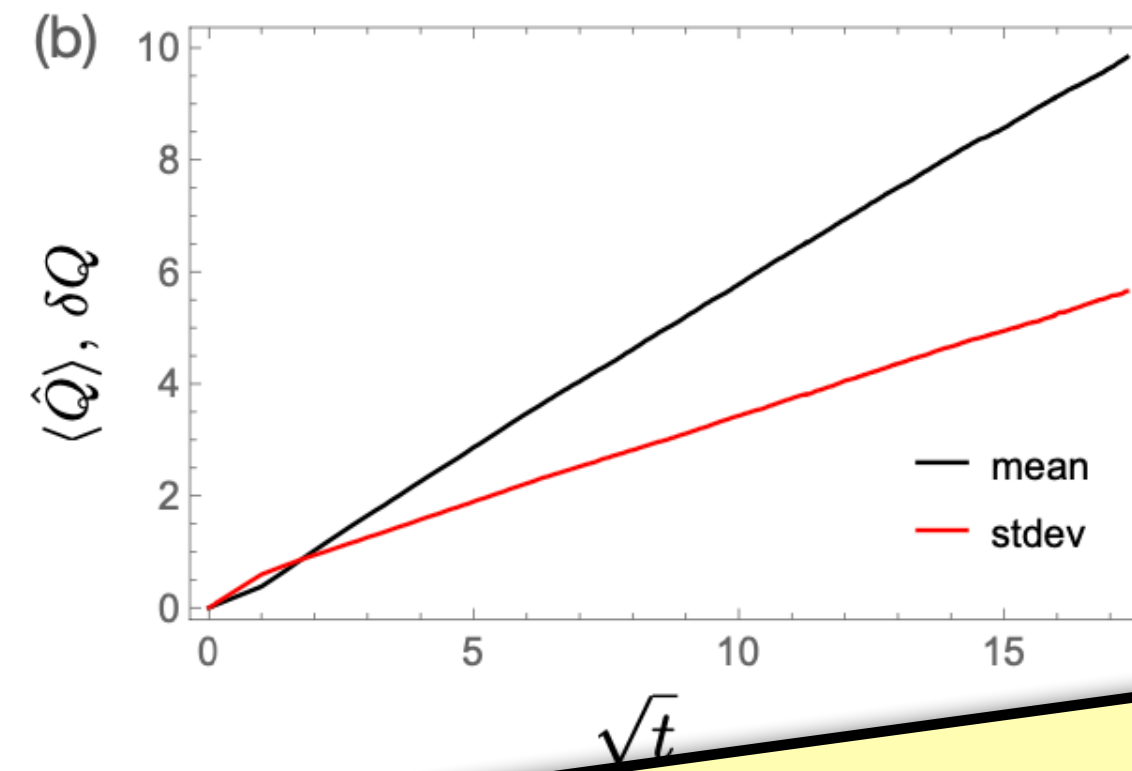
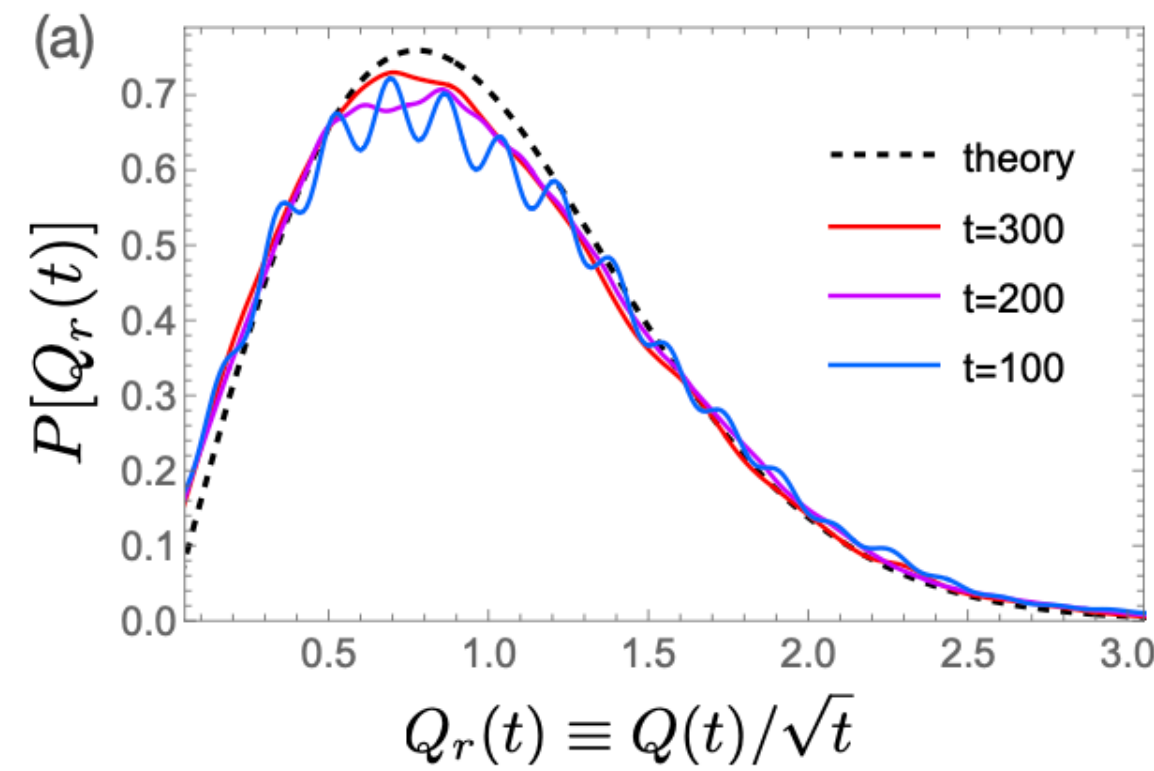
Mean  $z = 1.49(2)$

Standard Deviation  $\beta = 0.31(1)$

**KPZ  
Universality  
 $\beta = 1/3$**

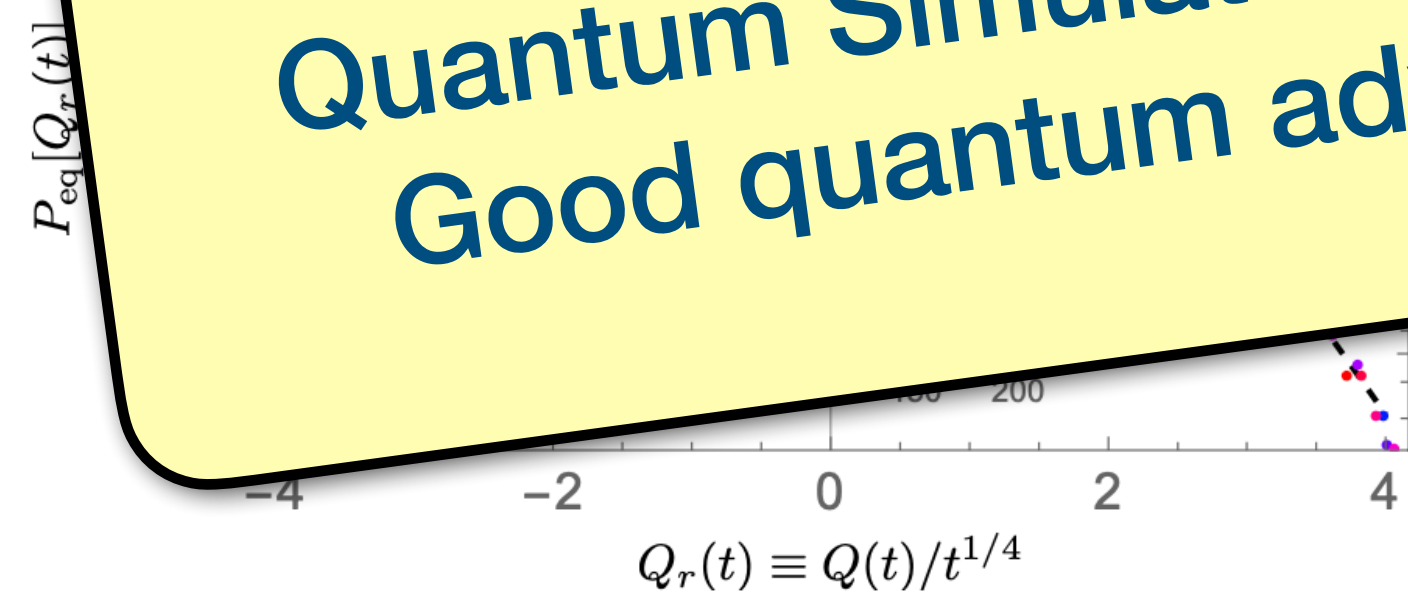
## Anomalous Transport in XXZ (easy axis)

$$\hat{H} = -J_{\text{ex}} \sum_i \left( \hat{S}_i^x \hat{S}_{i+1}^x + \hat{S}_i^y \hat{S}_{i+1}^y + \Delta \hat{S}_i^z \hat{S}_{i+1}^z \right) \quad \Delta > 1$$



**Full Counting Statistics**  
out-of-equilibrium ( $m > 0$ )

**Can we discover new transport regimes also in 2D?**  
**Quantum Simulators offer powerful new tools to probe this!**  
**Good quantum advantage (double exponential) regime!!**



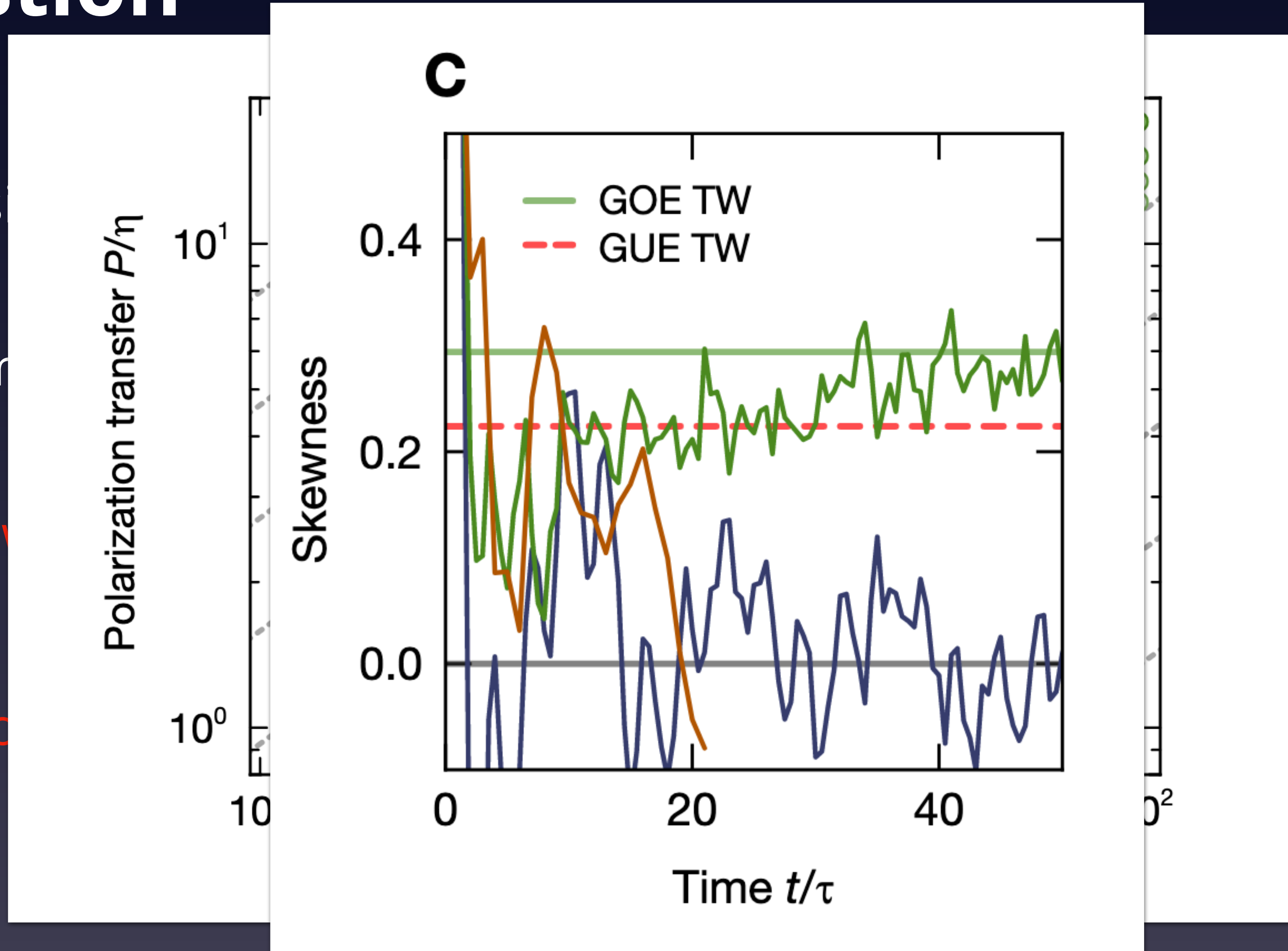


# Experimental Evidence for KPZ

- 1** Superdiffusive transport ( $z=3/2$ ) **can arise from linear model!**
- 2** Polarisation fluctuation scale ( $\beta = 1/3$ )
- 3** Skewness of Polarisation fluctuation distribution constant (and compatible with Tracy-Widom GOE/GUE)
- 4** Breaking SU(2) symmetry OR breaking integrability destroys KPZ behaviour

# Open Question

- 1 Superdiffus
- 2 Higher mom
- 3 Maybe a new
- 4 Derivation of



II visibility

model?

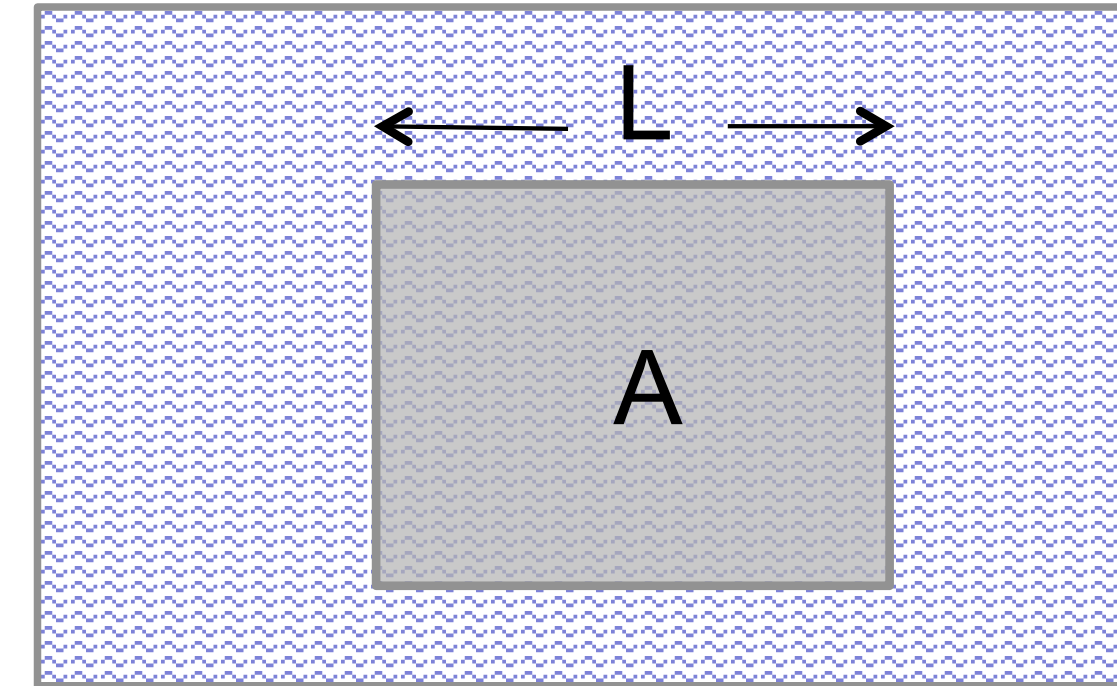


**Briefly: Probing MBL**

Deutsch (91), Srednicki (94,98), Rigol, Dunjko & Olshanii (2009),  
D'Alessio, Kafri, Polkovnikov, Rigol, Adv. Phys. **65**, 239 (2016)

$$\rho_A = \frac{1}{Z_A} e^{-\beta H_A}$$

$$S_A \equiv \text{tr} [\rho_A \ln \rho_A] \propto L^d$$



**Are there scenarios when this fails?**

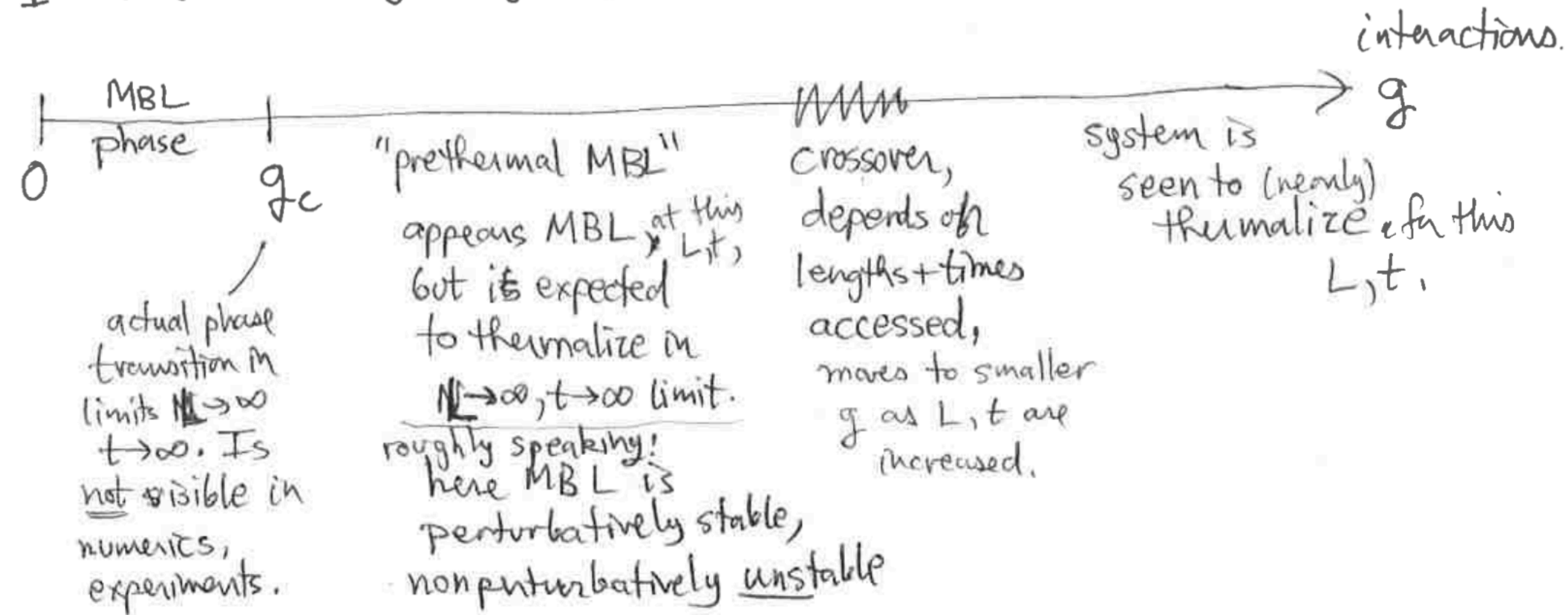
**System fails to act as its own heat bath!**

Nandkishore et al., Annu. Rev. Cond. Mat. 2015; Altman et al. Annu. Rev. Cond. Mat. 2015,

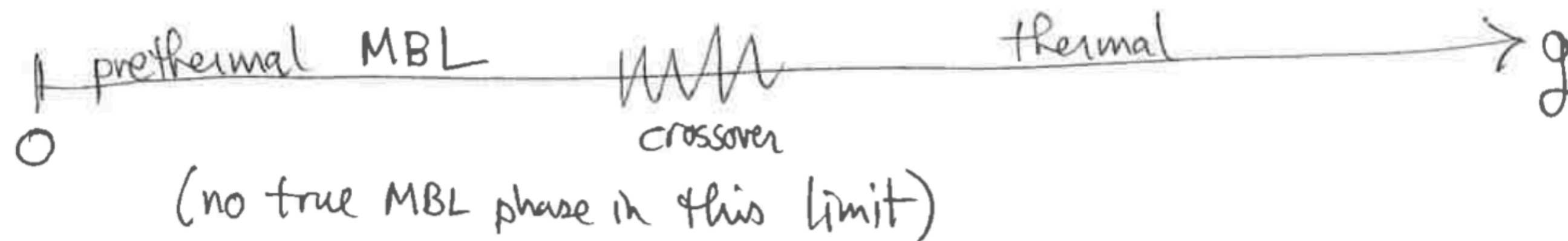


Dynamic phase diagram of MBL (nothing is there in the thermodynamics)

1D with short-enough range interactions:



Longer range interactions or  $d > 1$ , taking standard thermodynamic limit:  
 $g_c \rightarrow 0$



# Important Points

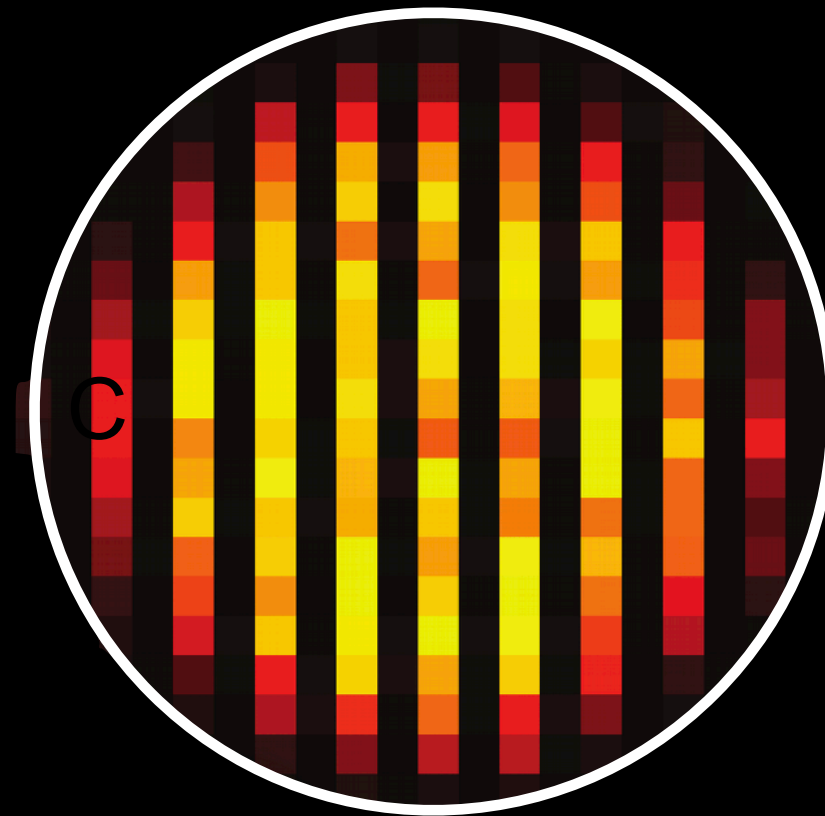
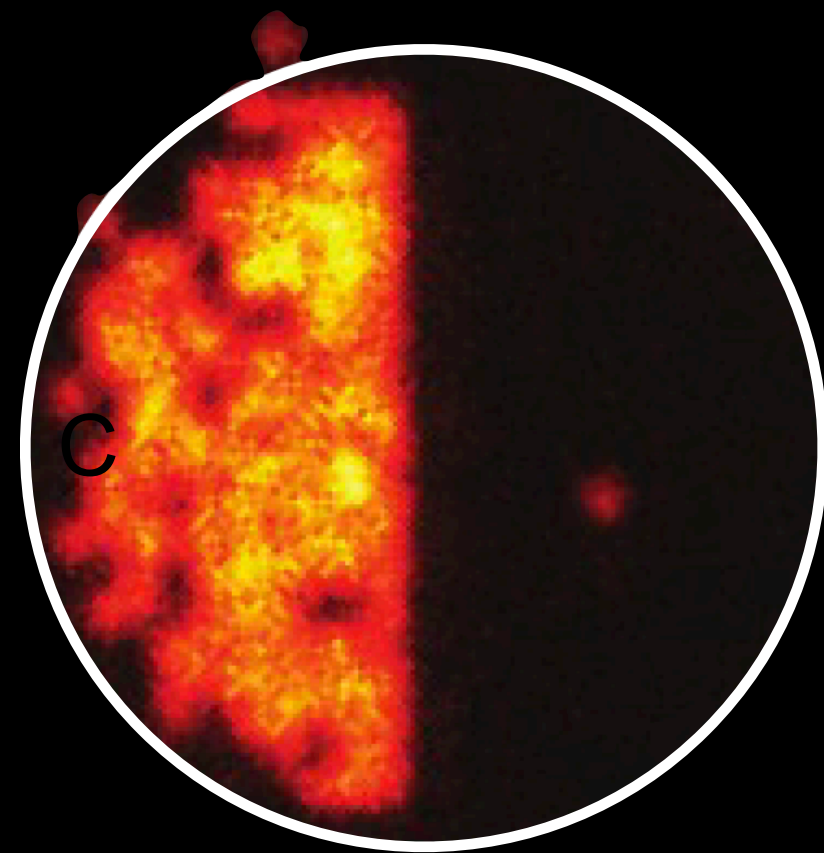
Very little theoretically known about MBL in  $d > 1$   
(**stability of MBL unclear**)

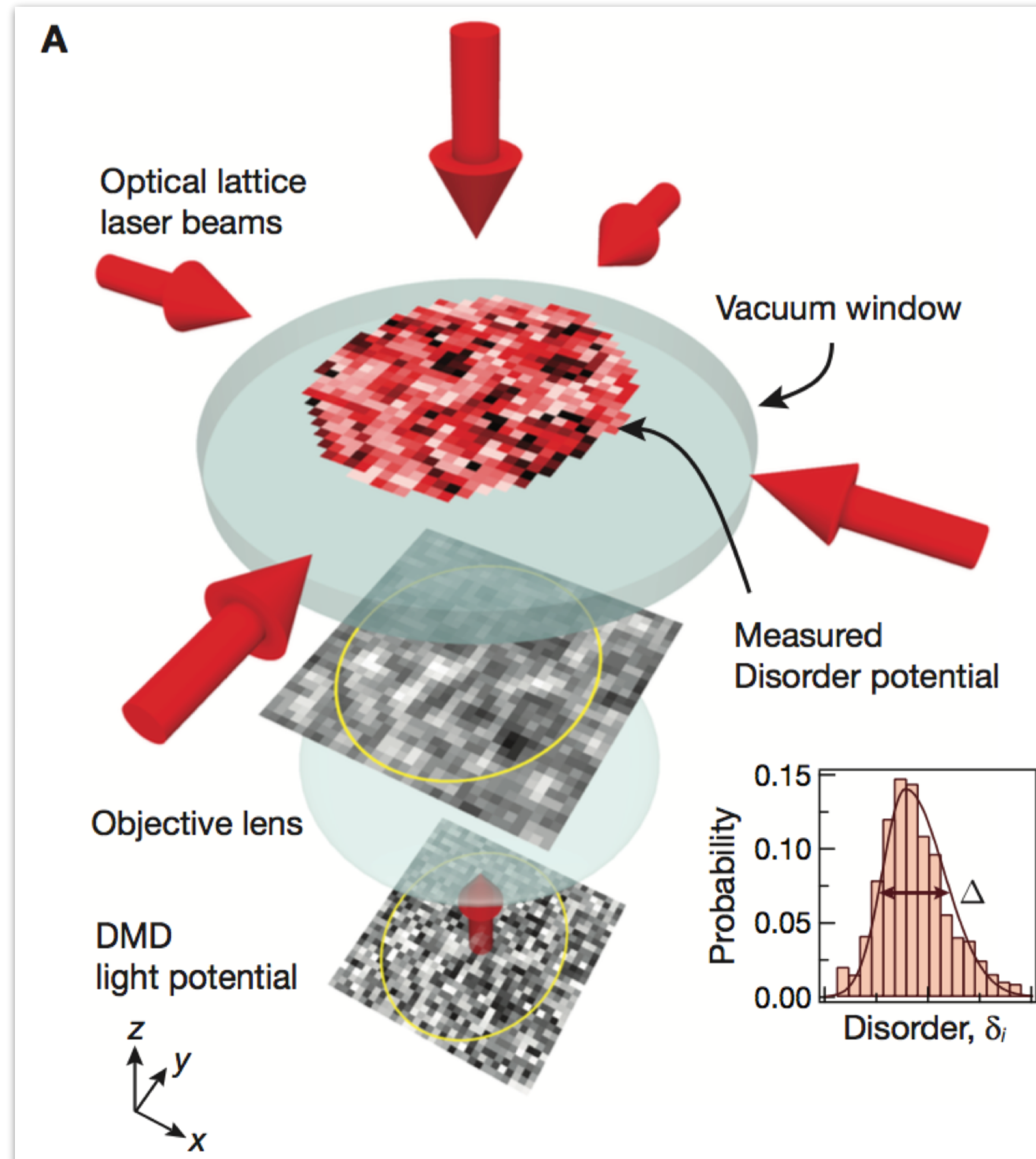
Calls for particularly precise characterization of the experiments  
(validation through a quantum simulator)

Experiments (almost) isolated from environment  
but **small residual coupling** limits observation time ( $> 1000 t$ )



# Probing MBL on Different Length and Timescales





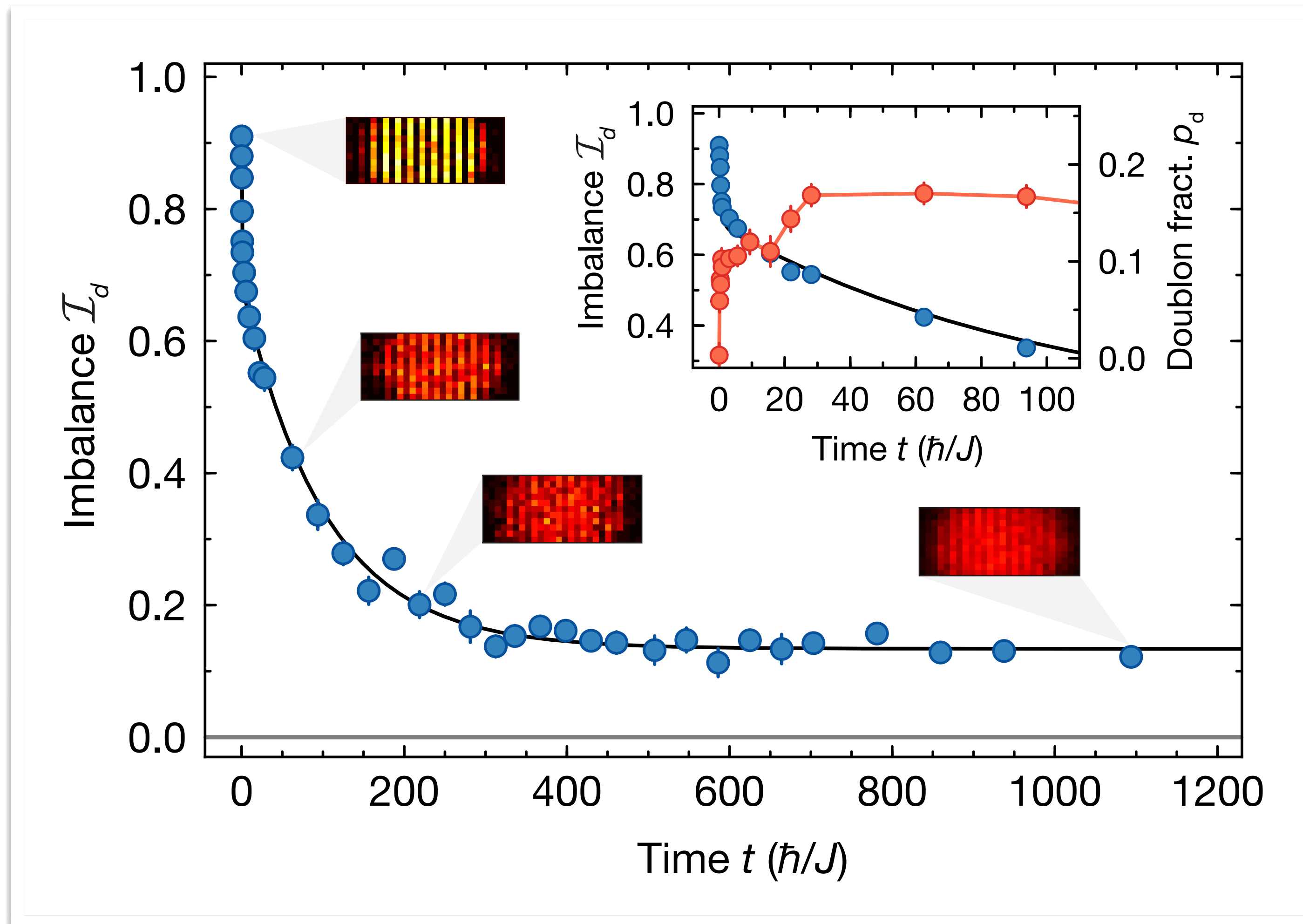
1. Prepare Domain Wall  
(no tunneling dynamics)
2. Turn on disorder potential
3. Lower the lattice depth  
(near critical point)
4. Measure atomic distribution

- \* Tunneling time is 6.4 ms.
- \* Disorder is changed for each image.
- \* Take 100 picture for averaging.

$$U = 24J$$

$$\Delta = 0 - 20J$$





$\tau_1 \sim 0.6 \hbar/J$

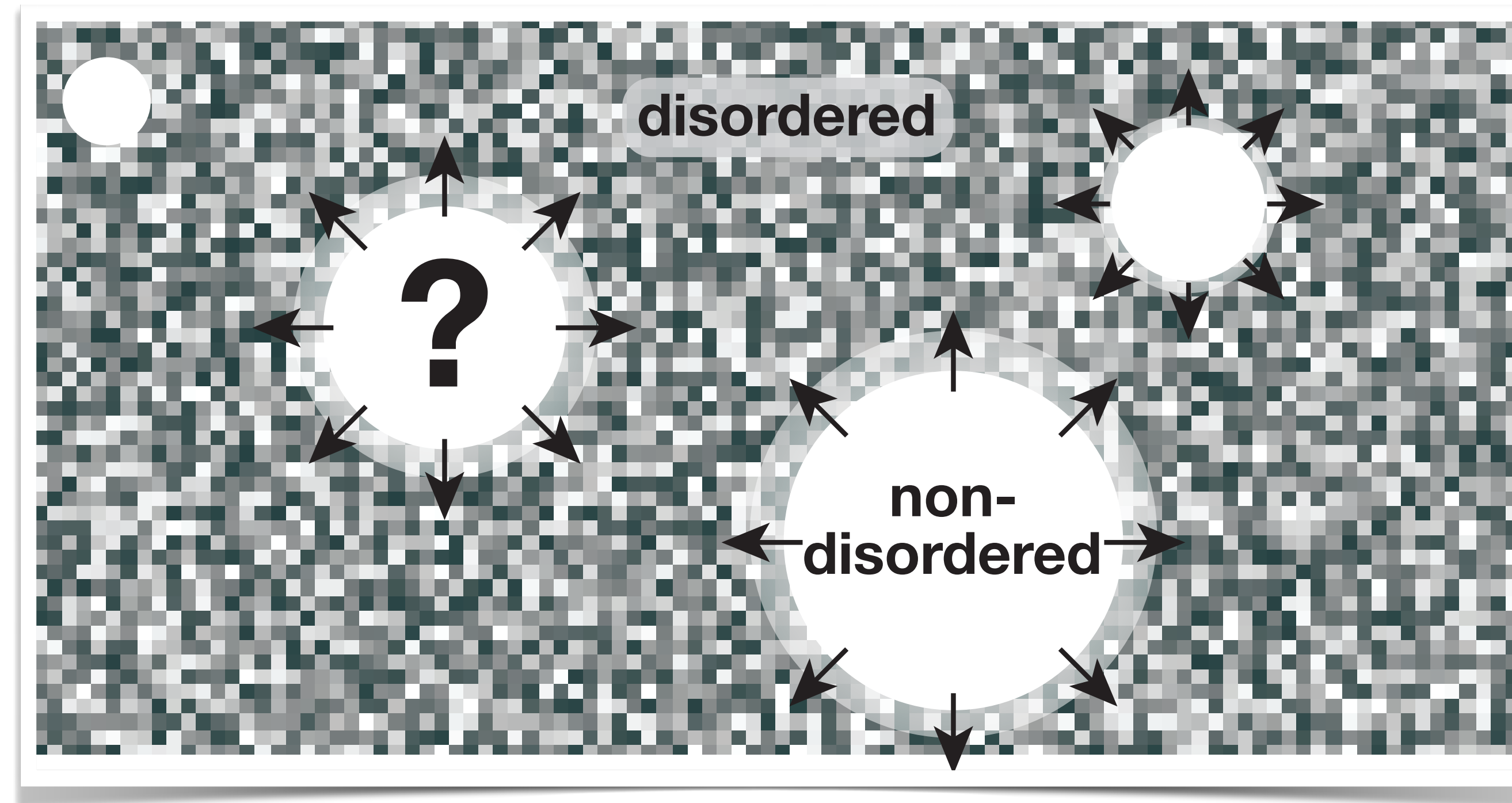
$\tau_2 \sim 105 \hbar/J$

$\tau_3 > 2500 \hbar/J$

Band width **8 J**

Interactions **U = 25 J**

Disorder **Δ = 28 J**



**Engineered disorder with controlled non-disordered (ergodic) grains!**

Avalanches?  
Stability?  
Range?  
Timescales of Instability?

⋮

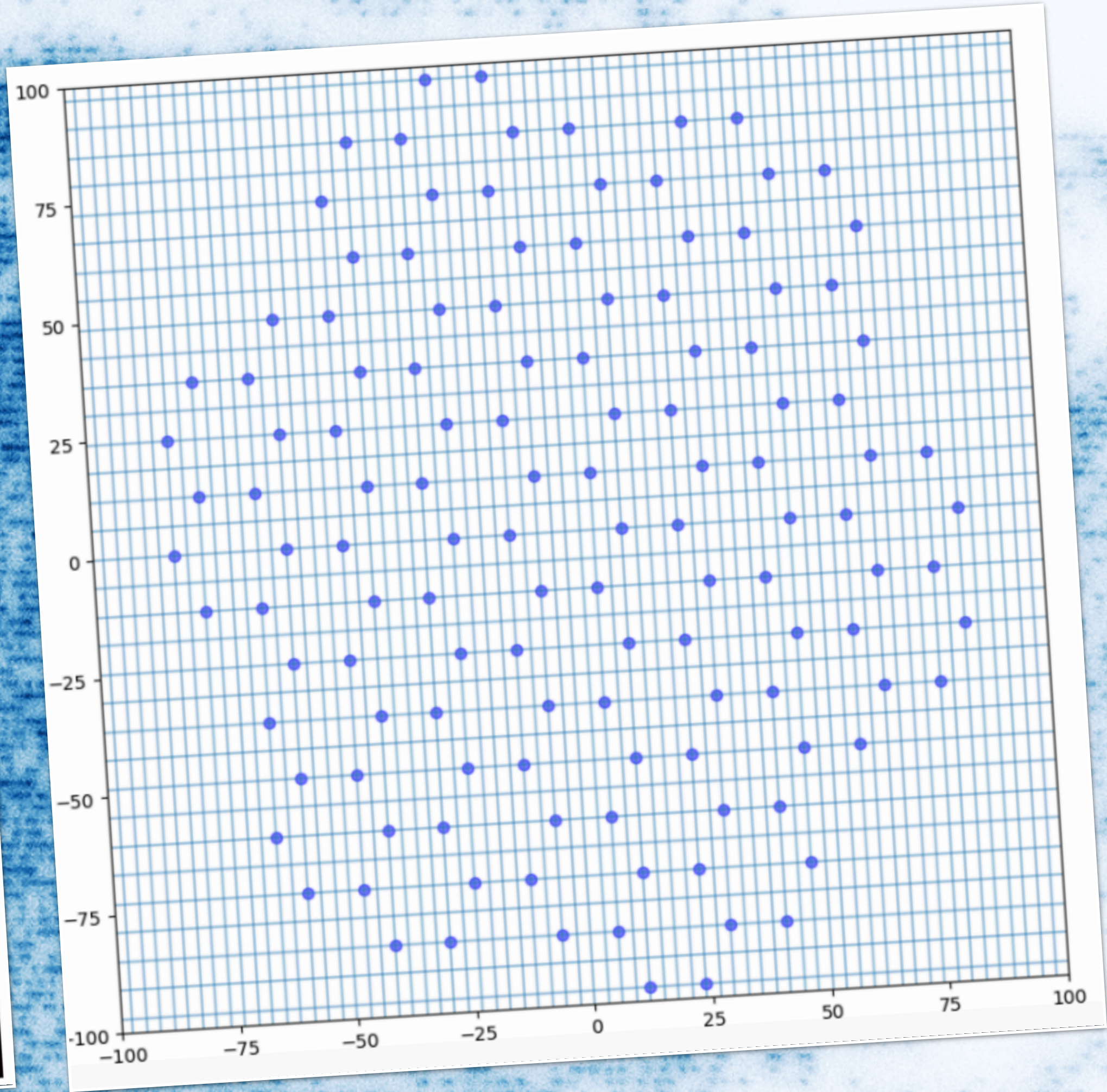
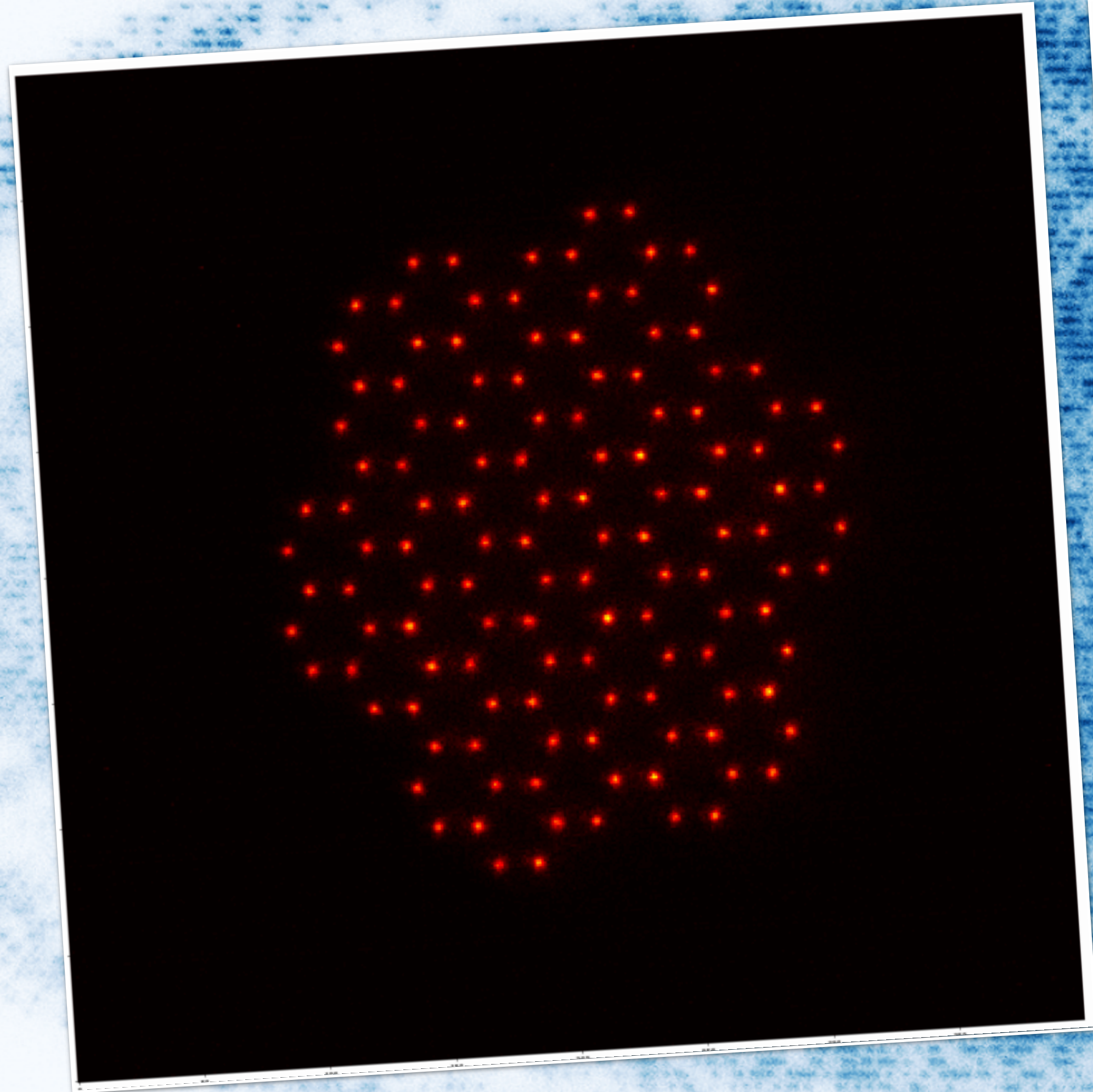
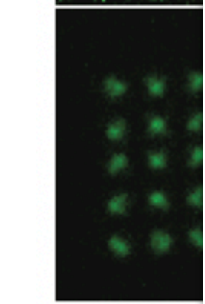
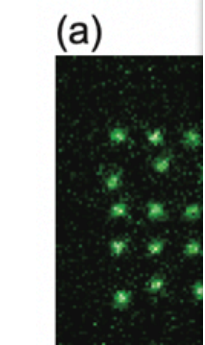
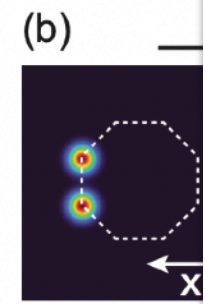
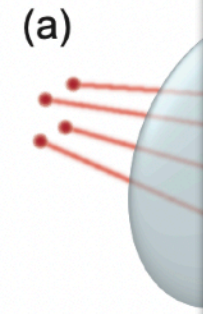




**Where Next?**



# Enhanced Programmability



Hubb  
(Princ

University,



## Opportunities

- ▶ (Precision) Many-body physics, New detection methods, Novel quantum phases, Non-equilibrium dynamics
- ▶ **Materials science, High-energy physics, Quantum chemistry, Coherent Quantum annealing, Optimization, Metrology ....**

## Challenges

- ▶ **Programmability, scalability, reducing calibration errors**
- ▶ **Certification and verification**; demonstration of *practical* quantum advantage.
- ▶ Developing **applications relevant to industry and other fields of science**, and connections to an end-user base (e.g. spin models / optimization)
- ▶ **Entropy management** (cooling)
- ▶ **Cycle times**

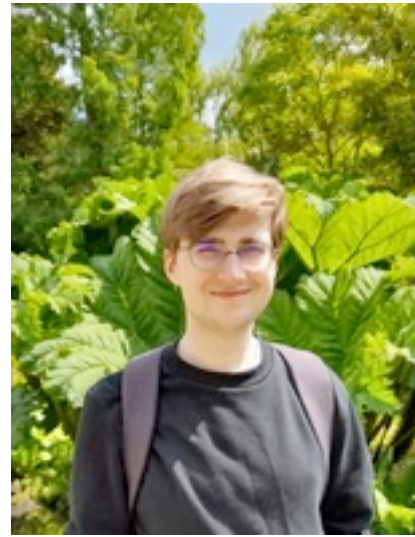




# Cs Quantum Gas Microscope Team



Ignacio  
Perez



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Karch



Christian  
Schweizer

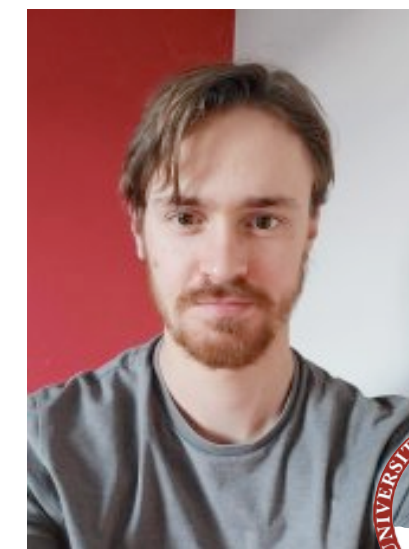


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Sophie Häfele

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Hendrik von Raven,  
**Julian Wienand**  
Till Klostermann,  
Monika Aidelsburger, IB

## Theory



Ewan  
McCulloch

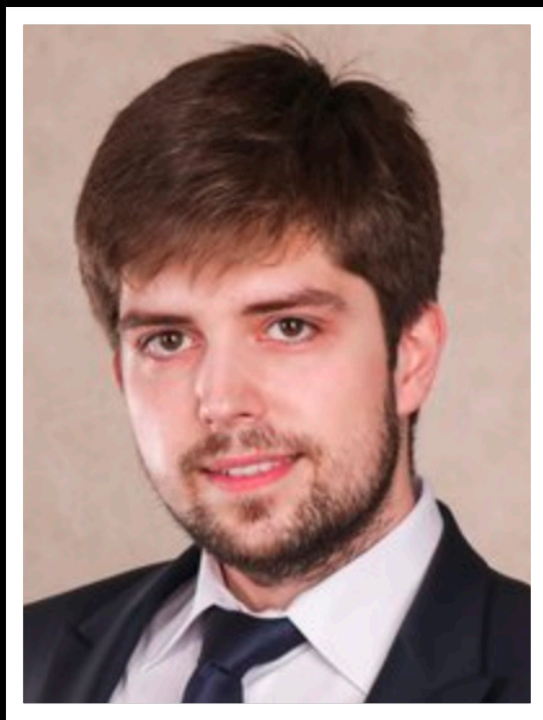


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Vasseur



Sarang  
Gopalakrishnan





**Petar Bojovic**



**Si Wang**



**Thomas Chalopin**



**Team leader: Timon Hilker**



**Joannis Koepsell**

**Jayadev Vijayan**

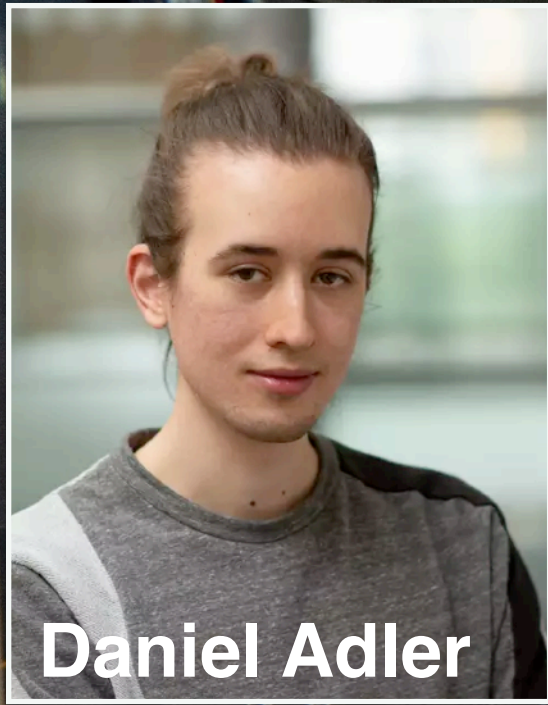
**Dominik Bourgound**

**Christian Gross**

**Sarah Hirthe**

**Pimponpan Sompert**





Daniel Adler



Suchita Agarwal



David Wei

Johannes Zeiher

Pascal Weckesser

Simon Hollerith

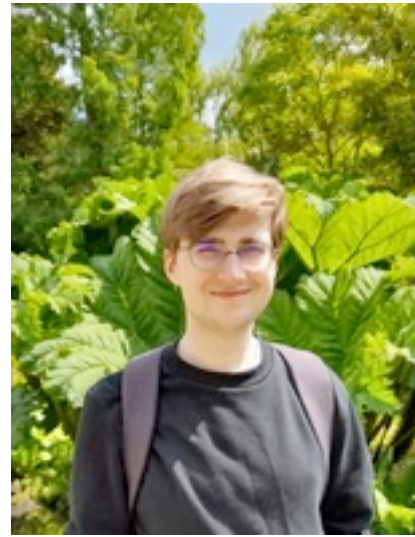
Kritsana Srakaew



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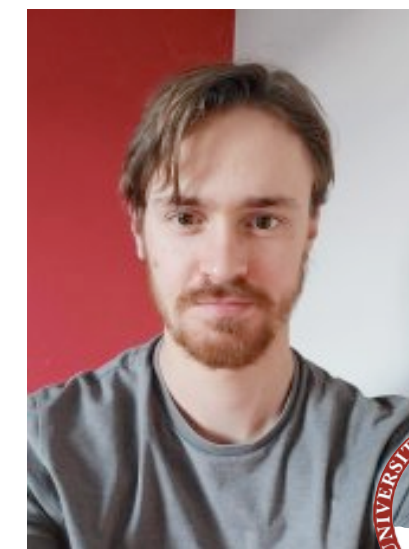


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